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# Global Optimization by Differential Evolution and Particle Swarm Methods Evaluation on Some Benchmark Functions

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**I. A Brief History of Optimization Research:** The history of optimization of real-valued non-linear functions (including linear ones), unconstrained or constrained, goes back to Gottfried Leibniz, Isaac Newton, Leonhard Euler and Joseph Lagrange. However, those mathematicians often assumed differentiability of the optimand as well as constraint functions. Moreover, they often dealt with the equality constraints. Richard Valentine (1937) and William Karush (1939), however, were perhaps the first mathematicians to study optimization of nonlinear functions under inequality constraints. Leonid Kantorovich and George Dantzig are well known for developing and popularizing linear programming, which ushered a new era of ‘operations research’, a branch of mathematical science that specializes in optimization. The development of linear programming soon prompted the study of the optimization problem of nonlinear functions (often under linear or nonlinear constraints). The joint work of Harold Kuhn and Albert Tucker (1951) – that was backed up by the work of Karush – is a landmark in the history of optimization of nonlinear functions.

Initially, optimization of nonlinear functions was methodologically based on the Leibniz-Newton principles and therefore could not easily escape local optima. Hence, its development to deal with nonconvex (multimodal) functions stagnated until the mid 1950’s. Stanislaw Ulam, John von Neumann and Nicolas Metropolis had in the late 1940’s proposed the Monte Carlo method of simulation and it was gradually realized that the simulation approach could provide an alternative methodology to mathematical investigations in optimization. George Box (1957) was perhaps the first mathematician who exploited the idea and developed his evolutionary method of nonlinear optimization. Almost a decade later, MJ Box (1965) developed his complex method, which strews random numbers over the entire domain of the decision variables and therefore has a great potentiality to escape local optima and locate the global optimum of a nonlinear function. The simplex method of John Nelder and Roger Mead (1964) also incorporated the ability to learn from its earlier search experience and adapt itself to the topography of the surface of the optimand function.

**II. Global Optimization:** The 1970’s evidenced a great fillip in simulation-based optimization research due to the invention of the ‘genetic algorithm’ by John Holland (1975). A genetic algorithm is a class of population-based adaptive stochastic optimization procedures, characterizing the presence of randomness in the optimization process. The randomness may be present as either noise in measurements or Monte Carlo randomness in the search procedure, or both. The basic idea behind the genetic algorithm is to mimic a simple picture of the Darwinian natural selection in order to find a good algorithm and involves the operations such as ‘mutation’, ‘selection’ and ‘evaluation of

fitness' repeatedly. The genetic algorithms may claim to have ushered the new era of global optimization.

A little later, in 1978, Aimo Törn introduced his "Clustering Algorithm" of global optimization. The method improves upon the earlier local search algorithms that needed 'multiple start' from several points distributed over the whole optimization region. Multi-start is certainly one of the earliest global procedures used. It has even been used in local optimization for increasing the confidence in the obtained solution. However, one drawback of Multi-start is that when many starting points are used, the same minimum will eventually be determined several times. In order to improve the efficiency of Multi-start this should be avoided. The clustering method of Törn avoids this repeated determination of local minima. This is realized in three steps, which may be iteratively used. The three steps are: (i) sample points in the region of interest, (ii) transform the sample to obtain points grouped around the local minima, and (iii) use a clustering technique to recognize these groups (i.e. neighbourhoods of the local minima). If the procedure employing these steps is successful, then, starting a single local optimization from each cluster would determine the local minima and, thus, also the global minimum. The advantage in using this approach is that the work spared by computing each minimum just once can be spent on computations in (i) and (ii), which will increase the probability that the global minimum will be found.

While the clustering algorithm was optimizing on the multi-start requirements of local search algorithms and the genetic algorithm simulated the Darwinian struggle for the survival of the fittest, the simulated annealing method (Kirkpatrick et al., 1983; Cerny, 1985) proposed to mimic the annealing process in metallurgy. In an annealing process a metal in the molten state (at a very high temperature) is slowly cooled so that the system at any time is approximately in thermodynamic equilibrium. As cooling proceeds, the system becomes more ordered – the liquid freezes or the metal re-crystallizes – attaining the ground state at  $T=0$ . This process is simulated through the Monte Carlo experiment (Metropolis et al. 1953). If the initial temperature of the melt is too low or cooling is done unduly fast the metal may become 'quenched' due to being trapped in a local minimum energy state (meta-stable state) forming defects or freezing out. The simulated annealing method of optimization makes very few assumptions regarding the function to be optimized, and therefore, it is quite robust with respect to irregular surfaces. In this method, the mathematical system describing the problem mimics the thermodynamic system. The current solution to the problem mimics the current state of the thermodynamic system, the objective function mimics the energy equation for the thermodynamic system, and the global minimum mimics the ground state. However, nothing in the numerical optimization problem directly mimics the temperature,  $T$ , in the thermodynamic system underlying the metallurgical process of annealing. Therefore, a complex abstraction mimics it. An arbitrary choice of initial value of a variable called 'temperature', how many iterations are performed at each 'temperature', the step length at which the decision variables are adjusted, and the rate of fall of 'temperature' at each step as 'cooling' proceeds, together make an 'annealing schedule'. This schedule mimics the cooling process. At a high 'temperature' the step lengths at which the decision variables are adjusted are larger than those at a lower

‘temperature’. Whether the system is trapped into local minima (quenching takes place) or it attains the global minimum (faultless crystallization) is dependent on the said annealing schedule. A wrong choice of the initial ‘temperature’, or the rate of fall in the ‘temperature’ leads to quenching or entrapment of the solution in the local minima. The method does not provide any clear guideline as to the choice of the ‘annealing schedule’ and often requires judgment or trial and error. If the schedule is properly chosen, the process attains the global minimum. It is said that using this method is an art and requires a lot of experience and judgment.

A little later, Fred Glover (1986) introduced his ‘Tabu Search’ method. This method economizes on repeated visits to the already visited points and in some sense is close to the clustering algorithms. Glover attributes its origin to about 1977. The basic concept of Tabu Search as described by Glover is "a meta-heuristic superimposed on another heuristic. The overall approach is to avoid entrainment in cycles by forbidding or penalizing moves which take the solution, in the next iteration, to points in the solution space previously visited ( hence "tabu"). The Tabu method was partly motivated by the observation that human behavior appears to operate with a random element that leads to inconsistent behavior given similar circumstances. As Glover points out, the resulting tendency to deviate from a charted course, might be regretted as a source of error but can also prove to be source of gain. The Tabu method operates in this way with the exception that new courses are not chosen randomly. Instead the Tabu search proceeds according to the supposition that there is no point in accepting a new (poor) solution unless it is to avoid a path already investigated. This insures new regions of a problems solution space will be investigated in with the goal of avoiding local minima and ultimately finding the desired solution.

The pace of research in global optimization (GO) by stochastic process accelerated considerably in the 1990’s. Marco Dorigo in his Ph.D. thesis (1992) introduced his “Ant Colony” method of global optimization. It studies artificial systems that take inspiration from the behaviour of real ant colonies. Ants use pheromones that guide other fellow ants to identify the path that leads to a success. The chemical properties of pheromones and the ability of ants to gather information and use them are simulated in the Ant Colony method to reach at the global optimum. This method is well suited to combinatorial (discrete) optimization problems.

A couple of years later, James Kennedy and Russell Eberhart (1995) introduced their “Particle Swarm” method of global optimization. In the animal world we observe that a swarm of birds or insects or a school of fish searches for food, protection, etc. in a very typical manner. If one of the members of the swarm sees a desirable path to go, the rest of the swarm will follow quickly. The Particle Swarm method mimics this behaviour. Every individual of the swarm is considered as a particle in a multidimensional space that has a position and a velocity. These particles fly through hyperspace and remember the best position that they have seen. Members of a swarm communicate good positions to each other and adjust their own position and velocity based on these good positions. There are two main ways this communication is done: (i) “swarm best” that is known to all (ii) “local bests” are known in neighborhoods of particles. Updating of the position

and velocity are done at each iteration such that the solution often converges to the global optimum of the function. Interestingly, this method has a very sound and well-documented philosophical literature behind it (the British empiricist philosophy, the American pragmatism and others like those of Friedrich Hayek, Herbert Simon, etc.).

The method of Differential Evolution (DE) grew out of Kenneth Price's attempts to solve the Chebychev Polynomial fitting Problem that had been posed to him by Rainer Storn. A breakthrough happened (1996), when Price came up with the idea of using vector differences for perturbing the vector population. The crucial idea behind DE is a scheme for generating trial parameter vectors. Initially, a population of points ( $p$  in  $d$ -dimensional space) is generated and evaluated (i.e.  $f(p)$  is obtained) for their fitness. Then for each point ( $p_i$ ) three different points ( $p_a$ ,  $p_b$  and  $p_c$ ) are randomly chosen from the population. A new point ( $p_z$ ) is constructed from those three points by adding the weighted difference between two points ( $w(p_b-p_c)$ ) to the third point ( $p_a$ ). Then this new point ( $p_z$ ) is subjected to a crossover with the current point ( $p_i$ ) with a probability of crossover ( $c_r$ ), yielding a candidate point, say  $p_u$ . This point,  $p_u$ , is evaluated and if found better than  $p_i$  then it replaces  $p_i$  else  $p_i$  remains. Thus we obtain a new vector in which all points are either better than or as good as the current points. This new vector is used for the next iteration. This process makes the differential evaluation scheme completely self-organizing.

**III. The Characteristic Features of Population-Based GO Methods:** All population-based methods of global optimization partake of the probabilistic nature inherent to them. As a result, one cannot obtain certainty in their results, unless they are permitted to go in for indefinitely large search attempts. Larger is the number of attempts, greater is the probability that they would find out the global optimum, but even then it would not reach at the certainty. Secondly, all of them adapt themselves to the surface on which they find the global optimum. The scheme of adaptation is largely based on some guesswork since nobody knows as to the true nature of the problem (environment or surface) and the most suitable scheme of adaptation to fit the given environment. Surfaces may be varied and different for different functions. A particular type of surface may be suited to a particular method while a search in another type of surface may be a difficult proposition for it. Further, each of these methods operates with a number of parameters that may be changed at choice to make it more effective. This choice is often problem oriented and for obvious reasons. A particular choice may be extremely effective in a few cases, but it might be ineffective (or counterproductive) in certain other cases. Additionally, there is a relation of trade-off among those parameters. These features make all these methods a subject of trial and error exercises.

**IV. The Objectives:** Our objective in this paper is to compare the performance of the Differential Evolution (DE) and the Repulsive Particle Swarm (RPS) methods of global optimization. To this end, 70 test functions have been chosen (for their algebraic specifications, see Mishra, 2006-c, d and e). Among these test functions, some are new while others are well known in the literature; some are unimodal, the others multi-modal; some are small in dimension (no. of variables,  $x$  in  $f(x)$ ), while the others are large in

dimension; some are algebraic polynomial equations, while the other are transcendental, etc. In all, they together represent a wide variety of surfaces.

**V. Some Details of the Particle Swarm Methods Used Here:** In this exercise we have used (modified) Repulsive Particle Swarm method. The Repulsive Particle Swarm method of optimization is a variant of the classical Particle Swarm method (see Wikipedia, <http://en.wikipedia.org/wiki/RPSO>). It is particularly effective in finding out the global optimum in very complex search spaces (although it may be slower on certain types of optimization problems).

In the traditional RPS the future velocity,  $v_{i+1}$  of a particle at position with a recent velocity,  $v_i$ , and the position of the particle are calculated by:

$$v_{i+1} = \omega v_i + \alpha r_1 (\hat{x}_i - x_i) + \omega \beta r_2 (\hat{x}_{hi} - x_i) + \omega \gamma r_3 z$$

$$x_{i+1} = x_i + v_{i+1}$$

where,

- $x$  is the position and  $v$  is the velocity of the individual particle. The subscripts  $i$  and  $i+1$  stand for the recent and the next (future) iterations, respectively.
- $r_1, r_2, r_3$  are random numbers,  $\in [0,1]$
- $\omega$  is inertia weight,  $\in [0.01,0.7]$
- $\hat{x}$  is the best position of a particle
- $x_h$  is best position of a randomly chosen other particle from within the swarm
- $z$  is a random velocity vector
- $\alpha, \beta, \gamma$  are constants

Occasionally, when the process is caught in a local optimum, some *chaotic* perturbation in position as well as velocity of some particle(s) may be needed.

The traditional RPS gives little scope of local search to the particles. They are guided by their past experience and the communication received from the others in the swarm. We have modified the traditional RPS method by endowing stronger (wider) local search ability to each particle. Each particle flies in its local surrounding and searches for a better solution. The domain of its search is controlled by a new parameter (*nstep*). This local search has no preference to gradients in any direction and resembles closely to tunneling. This added exploration capability of the particles brings the RPS method closer to what we observe in real life. However, in some cases moderately wide search (*nstep=9*, say; see program) works better.

Each particle learns from its ‘chosen’ inmates in the swarm. At the one extreme is to learn from the best performer in the entire swarm. This is how the particles in the original PS method learn. However, such learning is not natural. How can we expect the individuals to know as to the best performer and interact with all others in the swarm? We believe in limited interaction and limited knowledge that any individual can possess and acquire. So, our particles do not know the ‘best’ in the swarm. Nevertheless, they interact with some chosen inmates that belong to the swarm. Now, the issue is: how does the particle choose its inmates? One of the possibilities is that it chooses the inmates

closer (at lesser distance) to it. But, since our particle explores the locality by itself, it is likely that it would not benefit much from the inmates closer to it. Other relevant topologies are : (the celebrated) *ring topology*, ring topology hybridized with random topology, star topology, von Neumann topology, etc.

Now, let us visualize the possibilities of choosing (a predetermined number of) inmates randomly from among the members of the swarm. This is much closer to reality in the human world. When we are exposed to the mass media, we experience this. Alternatively, we may visualize our particles visiting a public place (e.g. railway platform, church, etc) where it (he) meets people coming from different places. Here, geographical distance of an individual from the others is not important. Important is how the experiences of others are communicated to us. There are large many sources of such information, each one being selective in what it broadcasts and each of us selective in what we attend to and, therefore, receive. This selectiveness at both ends transcends the geographical boundaries and each one of us is practically exposed to randomized information. Of course, two individuals may have a few common sources of information. We have used these arguments in the scheme of dissemination of others' experiences to each individual particle. Presently, we have assumed that each particle chooses a pre-assigned number of inmates (randomly) from among the members of the swarm. However, this number may be randomized to lie between two pre-assigned limits.

**VI. Some Details of the Differential Evolution Methods Used Here:** The differential Evolution method consists of three basic steps: (i) generation of (large enough) population with  $N$  individuals [ $x = (x_1, x_2, \dots, x_m)$ ] in the  $m$ -dimensional space, randomly distributed over the entire domain of the function in question and evaluation of the individuals of the so generated by finding  $f(x)$ ; (ii) replacement of this current population by a better fit new population, and (iii) repetition of this replacement until satisfactory results are obtained or certain criteria of termination are met.

The crux of the problem lays in replacement of the current population by a new population that is better fit. Here the meaning of 'better' is in the Pareto improvement sense. A set  $S_a$  is better than another set  $S_b$  **iff** : (i) **no**  $x_i \in S_a$  is inferior to the corresponding member of  $x_i \in S_b$  ; **and** (ii) **at least one** member  $x_k \in S_a$  is better than the corresponding member  $x_k \in S_b$ . Thus, every new population is an improvement over the earlier one. To accomplish this, the DE method generates a candidate individual to replace each current individual in the population. The candidate individual is obtained by a crossover of the current individual and three other randomly selected individuals from the current population. The crossover itself is probabilistic in nature. Further, if the candidate individual is better fit than the current individual, it takes the place of the current individual, else the current individual stays and passes into the next iteration. The crossover scheme (called exponential crossover, as suggested by Kenneth Price in his personal letter to the author) is given below. This is coded for  $ncross \Rightarrow 1$  in the program.

The mutant vector is  $vi,g = xr1,g + F*(xr2,g - xr3,g)$  and the target vector is  $xi,g$  and the trial vector is  $ui,g$ . The indices  $r1, r2$  and  $r3$  are randomly but different from each other.  $Uj(0,1)$  is a uniformly distributed random number between 0 and 1 that is chosen anew for each parameter as needed.

Step 1: Randomly pick a parameter index  $j = \text{jrاند}$ .

Step 2: The trial vector inherits the  $j$ th parameter (initially =  $\text{jrاند}$ ) from the mutant vector, i.e.,  $u_{j,i,g} = v_{j,i,g}$ .

Step 3: Increment  $j$ ; if  $j = D$  then reset  $j = 0$ .

Step 4: If  $j = \text{jrاند}$  end crossover; else goto Step 5.

Step 5: If  $Cr \leq U_j(0,1)$ , then goto Step 2; else goto Step 6

Step 6: The trial vector inherits the  $j$ th parameter from the target vector, i.e.,  $u_{j,i,g} = x_{j,i,g}$ .

Step 7: Increment  $j$ ; if  $j = D$  then reset  $j = 0$ .

Step 8: If  $j = \text{jrاند}$  end crossover; else goto Step 6.

There could be other schemes (as many as 10 in number) of crossover, including no crossover (only probabilistic replacement,  $\text{NCROSS} \leq 0$  that works better in case of a few functions.

**VII. Specification of Adjustable Parameters:** As it has been mentioned before, these methods need certain parameters to be defined before they work. In case of the DE, we have fixed: max number of iterations allowed,  $\text{Iter} = 10000$ , population size,  $N = 10$  times of the dimension of the function or 100 whichever maximum; scheme of crossover,  $\text{ncross} = 1$  (defined in the program); crossover probability,  $\text{pcros} = 0.9$ ; scale factor,  $\text{fact} = 0.5$ , random number seed,  $\text{iu} = 1111$  and all random numbers are uniformly distributed between -1000 and 1000; accuracy needed,  $\text{eps} = 1.0\text{e-}08$ . If  $x$  in  $f(x)$  violates the boundary then it is forcibly brought within the specified limits through replacing it by a random number lying in the given limits of the function concerned. In case of the RPS: population size,  $N=100$ ; neighbour population,  $\text{NN}=50$ ; steps for local search,  $\text{NSTEP}=11$ ; Max no. of iterations permitted,  $\text{ITRN}=10000$ ; chaotic perturbation allowed,  $\text{NSIGMA}=1$ ; selection of neighbour : random,  $\text{ITOP}=3$ ;  $\text{A1}=\text{A2}=0.5$ ;  $\text{A3}=5.\text{e-}04$ ;  $\text{W}=.5$ ;  $\text{SIGMA}=1.\text{e-}03$ ;  $\text{EPSI}=1.\text{d-}04$ . Meanings of these parameters are explained in the programs (appended).

**VIII. Results and Discussion:** Among 70 functions, a few have been run for small as well as large dimensions. In total, 73 optimization exercises have been done. DE has succeeded in 65 cases while RPS has succeeded in 55 cases. In almost all cases, DE has converged faster and given much more accurate results. The convergence of RPS is much slower even for lesser stringency on accuracy. The summary of results is presented in table-1. Some test functions have been hard for both the methods. These are: Zero-Sum (30D), Perm#1, Perm#2, Power and Bukin-6 functions.

From what we see in table 1, one cannot yet reach at the definite conclusion that the DE performs better (or worse) than the RPS. None could assure a supremacy over the other. Each one faltered in some case; each one succeeded in some others. However, *DE is unquestionably faster, more accurate and more frequently successful than the RPS*. It may be argued, nevertheless, that alternative choice of adjustable parameters could have yielded better results in either method's case. The protagonists of either method could

suggest that. Our purpose is not to join with the one or the other. We simply want to highlight that in certain cases they both succeed, in certain other case they both fail and each one has some selective preference over some particular type of surfaces. What is needed is to identify such structures and surfaces that suit a particular method most.

It is needed that we find out some criteria to classify the problems that suit (or does not suit) a particular method. This classification will highlight the comparative advantages of using a particular method for dealing with a particular class of problems.

<b>Table 1: A Summary of Success or Failure of DE and RPS Methods in Optimization of Test Functions</b>									
SI No	Test Function	Dim (M)	Success		SI No	Test Function	Dim (M)	Success	
			DE	RPS				DE	RPS
1	New Fn #1	2	yes	yes	38	Linear Programming	3	yes	yes
2	New Fn #2	2	yes	yes	39	Hougen Fn	5	no	no
3	New Fn #3	2	yes	yes	40	Giunta Fn	2	yes	yes
4	New Fn #4	2	yes	yes	41	Egg-Holder Fn	2	yes	yes
5	New Fn #8	2	yes	yes	42	Trid Fn	30	yes	yes
6	Quintic Fn	4	yes	no	43	Greiwank Fn	30	yes	yes
7	Quintic Fn	30	yes	no	44	Weierstrass Fn	20	yes	no
8	Needle-eye Fn	10	yes	no	45	Levy#3 Fn	2	yes	yes
9	Needle-eye Fn	30	yes	no	46	Levy#5 Fn	2	yes	yes
10	Zero-sum Fn	10	yes	no	47	Levy#8 Fn	3	yes	yes
11	Zero-sum Fn	30	no	no	48	Rastrigin Fn	30	yes	no
12	Corana Fn	4	yes	yes	49	Ackley Fn	30	yes	yes
13	Mod RCos Fn	2	yes	yes	50	Michalewicz Fn	20	yes	no
14	Freud-Roth Fn	2	yes	yes	51	Schwefel Fn	30	yes	no
15	Anns XOR Fn	9	yes	no	52	Shubert Fn	2	yes	yes
16	Perm #1 Fn	4	no	no	53	Dixon-Price Fn	10	yes	no
17	Perm #2 Fn	5	no	no	54	Shekel Fn	4	yes	yes
18	Power-Sum Fn	4	no	no	55	Paviani Fn	10	yes	yes
19	Goldstein-Price Fn	2	yes	yes	56	Branin#1 Fn	2	yes	yes
20	Bukin-6 Fn	2	no	no	57	Branin#2 Fn	2	yes	yes
21	DCS Fn	4	yes	yes	58	Bohachevsky#1 Fn	2	yes	yes
22	New Factorial Fn	4	yes	yes	59	Bohachevsky#2 Fn	2	yes	yes
23	New Decanomial Fn	2	yes	yes	60	Bohachevsky#3 Fn	2	yes	yes
24	Judge Fn	2	yes	yes	61	Easom Fn	2	yes	yes
25	New Dodecal Fn	3	yes	yes	62	Rosenbrock Fn	10	yes	yes
26	New sum=prod Fn	2	yes	yes	63	Crosslegged Table Fn	2	yes	no
27	New AM=GM Fn	10	yes	yes	64	Cross Fn	2	yes	yes
28	Yao-Liu#2 Fn	30	yes	yes	65	Cross-in-Tray Fn	2	yes	yes
29	Yao-Liu#3 Fn	30	yes	yes	66	Crowned Cross Fn	2	yes	yes
30	Yao-Liu#4 Fn	30	yes	yes	67	TT-Holder Fn	2	yes	yes
31	Yao-Liu#6 Fn	30	yes	yes	68	Holder Table Fn	2	yes	yes
32	Yao-Liu#7 Fn	30	no	yes	69	Carrom Table Fn	2	yes	yes
33	Yao-Liu#12 Fn	30	yes	yes	70	Pen-Holder Fn	2	yes	yes
34	Yao-Liu#13 Fn	30	yes	yes	71	Bird Fn	2	yes	yes
35	Yao-Liu#14 Fn	2	yes	yes	72	Chichinadze Fn	2	yes	yes
36	Yao-Liu#15 Fn	4	no	yes	73	McCormick Fn	2	yes	yes
37	Linear Programming	2	yes	yes	<b>Failed in no. of cases (in 73 trials)</b>			<b>8</b>	<b>18</b>

Note: For differently set adjustable parameters, either method may perform better or worse than reported here.

## Bibliography

- Bauer, J.M.: "Harnessing the Swarm: Communication Policy in an Era of Ubiquitous Networks and Disruptive Technologies", *Communications and Strategies*, 45, 2002.
- Box, M.J.: "A new method of constrained optimization and a comparison with other methods". *Comp. J.* 8, pp. 42-52, 1965.
- Bukin, A. D.: *New Minimization Strategy For Non-Smooth Functions*, Budker Institute of Nuclear Physics preprint BUDKER-INP-1997-79, Novosibirsk 1997.
- Cerny, V.: "Thermodynamical Approach to the Traveling Salesman Problem: An Efficient Simulation Algorithm", *J. Opt. Theory Appl.*, 45, 1, 41-51, 1985.
- Eberhart R.C. and Kennedy J.: "A New Optimizer using Particle Swarm Theory", *Proceedings Sixth Symposium on Micro Machine and Human Science*, pp. 39-43. IEEE Service Center, Piscataway, NJ, 1995.
- Fleischer, M.: "Foundations of Swarm Intelligence: From Principles to Practice", Swarming Network Enabled C4ISR, arXiv:nlin.AO/0502003 v1 2 Feb 2005.
- G.E.P. Box, "Evolutionary operation: A method for increasing industrial productivity", *Applied Statistics*, 6, pp. 81-101, 1957.
- Glover F., "Future paths for Integer Programming and Links to Artificial Intelligence", *Computers and Operations Research*, 5:533-549, 1986.
- Hayek, F.A.: *The Road to Serfdom*, Univ. of Chicago Press, Chicago, 1944.
- Holland, J.: *Adaptation in Natural and Artificial Systems*, Univ. of Michigan Press, Ann Arbor, 1975.
- Karush, W. *Minima of Functions of Several Variables with Inequalities as Side Constraints*. M.Sc. Dissertation. Dept. of Mathematics, Univ. of Chicago, Chicago, Illinois, 1939.
- Kirkpatrick, S., Gelatt, C.D. Jr., and Vecchi, M.P.: "Optimization by Simulated Annealing", *Science*, 220, 4598, 671-680, 1983.
- Kuhn, H.W. and Tucker, A.W.: "Nonlinear Programming", in Neymann, J. (ed) *Proceedings of Second Berkeley Symposium on Mathematical Statistics and Probability*, Univ. of California Press, Berkeley, Calif. pp. 481-492, 1951.
- Metropolis, N. [The Beginning of the Monte Carlo Method](#). *Los Alamos Science*, No. 15, Special Issue, pp. 125-130, 1987.
- Metropolis, N., Rosenbluth, A., Rosenbluth, M., Teller, A., and Teller, E.: "Equation of State Calculations by Fast Computing Machines", *J. Chem. Phys.*, 21, 6, 1087-1092, 1953.
- Mishra, S.K.: "Some Experiments on Fitting of Gielis Curves by Simulated Annealing and Particle Swarm Methods of Global Optimization", *Social Science Research Network (SSRN)*: <http://ssrn.com/abstract=913667>, Working Papers Series, 2006 (a).
- Mishra, S.K.: "Least Squares Fitting of Chacón-Gielis Curves by the Particle Swarm Method of Optimization", *Social Science Research Network (SSRN)*, Working Papers Series, <http://ssrn.com/abstract=917762>, 2006 (b).
- Mishra, S.K.: "Performance of Repulsive Particle Swarm Method in Global Optimization of Some Important Test Functions: A Fortran Program", *Social Science Research Network (SSRN)*, Working Papers Series, <http://ssrn.com/abstract=924339>, 2006 (c).
- Mishra, S.K.: "Some New Test Functions for Global Optimization and Performance of Repulsive Particle Swarm Method", *Social Science Research Network (SSRN)* Working Papers Series, <http://ssrn.com/abstract=927134>, 2006 (d).
- Mishra, S.K.: "Repulsive Particle Swarm Method on Some Difficult Test Problems of Global Optimization", SSRN: <http://ssrn.com/abstract=928538>, 2006 (e).
- Nagendra, S.: *Catalogue of Test Problems for Optimization Algorithm Verification*, Technical Report 97-CRD-110, General Electric Company, 1997.
- Nelder, J.A. and Mead, R.: "A Simplex method for function minimization" *Computer Journal*, 7: pp. 308-313, 1964.
- Parsopoulos, K.E. and Vrahatis, M.N., "Recent Approaches to Global Optimization Problems Through Particle Swarm Optimization", *Natural Computing*, 1 (2-3), pp. 235- 306, 2002.

- Prigogine, I. and Stengers, I.: *Order Out of Chaos: Man's New Dialogue with Nature*, Bantam Books, Inc. NY, 1984.
- Silagadze, Z.K.: "Finding Two-Dimensional Peaks", Working Paper, Budkar Institute of Nuclear Physics, Novosibirsk, Russia, arXiv:physics/0402085 V3 11 Mar 2004.
- Simon, H.A.: *Models of Bounded Rationality*, Cambridge Univ. Press, Cambridge, MA, 1982.
- Smith, A.: *The Theory of the Moral Sentiments*, The Adam Smith Institute (2001 e-version), 1759.
- Sumper, D.J.T.: "The Principles of Collective Animal Behaviour", *Phil. Trans. R. Soc. B.* 361, pp. 5-22, 2006.
- Törn, A.A and Viitanen, S.: "Topographical Global Optimization using Presampled Points", *J. of Global Optimization*, 5, pp. 267-276, 1994.
- Törn, A.A.: "A search Clustering Approach to Global Optimization" , in Dixon, LCW and Szegö, G.P. (Eds) *Towards Global Optimization – 2*, North Holland, Amsterdam, 1978.
- Tsallis, C. and Stariolo, D.A.: "Generalized Simulated Annealing", *ArXiv condmat/9501047 v1* 12 Jan, 1995.
- Valentine, R.H.: *Travel Time Curves in Oblique Structures*, Ph.D. Dissertation, MIT, Mass, 1937.
- Veblen, T.B.: "Why is Economics Not an Evolutionary Science" *The Quarterly Journal of Economics*, 12, 1898.
- Veblen, T.B.: *The Theory of the Leisure Class*, The New American library, NY. (Reprint, 1953), 1899.
- Vesterstrøm, J. and Thomsen, R.: "A comparative Study of Differential Evolution, Particle Swarm Optimization, and Evolutionary Algorithms on Numerical Benchmark Problems", *Congress on Evolutionary Computation, 2004. CEC2004*, 2, pp. 1980-1987, 2004.
- Whitley, D., Mathias, K., Rana, S. and Dzubera, J.: "Evaluating Evolutionary Algorithms", *Artificial Intelligence*, 85, pp. 245-276, 1996.
- Yao, X. and Liu, Y.: "Fast Evolutionary Programming", in Fogel, LJ, Angeline, PJ and Bäck, T (eds) *Proc. 5<sup>th</sup> Annual Conf. on Evolutionary programming*, pp. 451-460, MIT Press, Mass, 1996.

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1: C      MAIN PROGRAM : PROVIDES TO USE REPULSIVE PARTICLE SWARM METHOD
2: C      (SUBROUTINE RPS) AND DIFFERENTIAL EVOLUTION METHOD (DE)
3: C      -----
4: C      Adjust the parameters suitably in subroutines DE and RPS
5: C      When the program asks for parameters, feed them suitably
6: C      -----
7:      PROGRAM DERPS
8:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
9:      COMMON /KFF/KF,NFCALL ! FUNCTION CODE AND NO. OF FUNCTION CALLS
10:     CHARACTER *30 METHOD(2)
11:     CHARACTER *1 PROCEED
12:     DIMENSION XX(2,50),KKF(2),MM(2),FMINN(2)
13:     DIMENSION X(50)! X IS THE DECISION VARIABLE X IN F(X) TO MINIMIZE
14: C     M IS THE DIMENSION OF THE PROBLEM, KF IS TEST FUNCTION CODE AND
15: C     FMIN IS THE MIN VALUE OF F(X) OBTAINED FROM DE OR RPS
16:     WRITE(*,*)'Adjust the parameters suitably in subroutines DE & RPS'
17:     WRITE(*,*)'===== WARNING ====='
18:     METHOD(1)=' : DIFFERENTIAL EVALUATION'
19:     METHOD(2)=' : REPULSIVE PARTICLE SWARM'
20:     DO I=1,2
21:
22:     IF(I.EQ.1) THEN
23:     WRITE(*,*)'===== DIFFERENTIAL EVOLUTION PROGRAM ====='
24:     WRITE(*,*)'TO PROCEED TYPE ANY CHARACTER AND STRIKE ENTER'
25:     READ(*,*) PROCEED
26:     CALL DE(M,X,FMINDE) ! CALLS DE AND RETURNS OPTIMAL X AND FMIN
27:     FMIN=FMINDE
28:     ELSE
29:     WRITE(*,*) ' '
30:     WRITE(*,*) ' '
31:     WRITE(*,*)'=====REPULSIVE PARTICLE SWARM PROGRAM ====='
32:     WRITE(*,*)'TO PROCEED TYPE ANY CHARACTER AND STRIKE ENTER'
33:     READ(*,*) PROCEED
34:     CALL RPS(M,X,FMINRPS) ! CALLS RPS AND RETURNS OPTIMAL X AND FMIN
35:     FMIN=FMINRPS
36:     ENDIF
37:     DO J=1,M
38:     XX(I,J)=X(J)
39:     ENDDO
40:     KKF(I)=KF
41:     MM(I)=M
42:     FMINN(I)=FMIN
43:     ENDDO
44:     WRITE(*,*) ' '
45:     WRITE(*,*) ' '
46:     WRITE(*,*)'----- FINAL RESULTS-----'
47:     DO I=1,2
48:     WRITE(*,*)'FUNCT CODE=',KKF(I),' FMIN=',FMINN(I),' : DIM=',MM(I)
49:     WRITE(*,*)'OPTIMAL DECISION VARIABLES : ',METHOD(I)
50:     WRITE(*,*)(XX(I,J),J=1,M)
51:     WRITE(*,*)'/////////////////////////////////////'
52:     ENDDO
53:     WRITE(*,*)'PROGRAM ENDED'
54:     END
55: C     -----
56:     SUBROUTINE DE(M,A,FBEST)
57: C     PROGRAM: "DIFFERENTIAL EVOLUTION ALGORITHM" OF GLOBAL OPTIMIZATION
58: C     THIS METHOD WAS PROPOSED BY R. STORN AND K. PRICE IN 1995. REF --
59: C     "DIFFERENTIAL EVOLUTION - A SIMPLE AND EFFICIENT ADAPTIVE SCHEME
60: C     FOR GLOBAL OPTIMIZATION OVER CONTINUOUS SPACES" : TECHNICAL REPORT
61: C     INTERNATIONAL COMPUTER SCIENCE INSTITUTE, BERKLEY, 1995.
62: C     PROGRAM BY SK MISHRA, DEPT. OF ECONOMICS, NEHU, SHILLONG (INDIA)
63: C     -----
64: C     PROGRAM EVOLDIF
65:     IMPLICIT DOUBLE PRECISION (A-H, O-Z) ! TYPE DECLARATION
66:     PARAMETER(NMAX=500,MMAX=50) ! MAXIMUM DIMENSION PARAMETERS
67:     PARAMETER(NCROSS=1) ! CROSS-OVER SCHEME (NCROSS <=0 OR >=1)

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68:      PARAMETER (IPRINT=500, EPS=1.d-08) !FOR WATCHING INTERMEDIATE RESULTS
69:      C      IT PRINTS THE INTERMEDIATE RESULTS AFTER EACH IPRINT ITERATION AND
70:      C      EPS DETERMINES ACCURACY FOR TERMINATION. IF EPS= 0, ALL ITERATIONS
71:      C      WOULD BE UNDERGONE EVEN IF NO IMPROVEMENT IN RESULTS IS THERE.
72:      C      ULTIMATELY "DID NOT CONVERGE" IS REOPORTED.
73:      COMMON /RNDM/IU,IV ! RANDOM NUMBER GENERATION (IU = 4-DIGIT SEED)
74:      INTEGER IU,IV ! FOR RANDOM NUMBER GENERATION
75:      COMMON /KFF/KF,NFCALL ! FUNCTION CODE AND NO. OF FUNCTION CALLS
76:      CHARACTER *70 FTIT ! TITLE OF THE FUNCTION
77:      C      -----
78:      C      THE PROGRAM REQUIRES INPUTS FROM THE USER ON THE FOLLOWING -----
79:      C      (1) FUNCTION CODE (KF), (2) NO. OF VARIABLES IN THE FUNCTION (M);
80:      C      (3) N=POPULATION SIZE (SUGGESTED 10 TIMES OF NO. OF VARIABLES, M,
81:      C      FOR SMALLER PROBLEMS N=100 WORKS VERY WELL);
82:      C      (4) PCROS = PROB. OF CROSS-OVER (SUGGESTED : ABOUT 0.85 TO .99);
83:      C      (5) FACT = SCALE (SUGGESTED 0.5 TO .95 OR SO);
84:      C      (6) ITER = MAXIMUM NUMBER OF ITERATIONS PERMITTED (5000 OR MORE)
85:      C      (7) RANDOM NUMBER SEED (4 DIGITS INTEGER)
86:      C      -----
87:      DIMENSION X (NMAX,MMAX) , Y (NMAX,MMAX) , A (MMAX) , FV (NMAX)
88:      DIMENSION IR(3)
89:      C      -----
90:      C      ----- SELECT THE FUNCTION TO MINIMIZE AND ITS DIMENSION -----
91:      CALL FSELECT(KF,M,FTIT)
92:      C      SPECIFY OTHER PARAMETERS -----
93:      WRITE (*,*) 'POPULATION SIZE [N] AND NO. OF ITERATIONS [ITER] ?'
94:      WRITE (*,*) 'SUGGESTED : N => 100 OR =>10.M; ITER 10000 OR SO'
95:      READ (*,*) N,ITER
96:      WRITE (*,*) 'CROSSOVER PROBABILITY [PCROS] AND SCALE [FACT] ?'
97:      WRITE (*,*) 'SUGGESTED : PCROS ABOUT 0.9; FACT=.5 OR LARGER BUT < 1'
98:      READ (*,*) PCROS,FACT
99:      WRITE (*,*) 'RANDOM NUMBER SEED ?'
100:     WRITE (*,*) 'A FOUR-DIGIT POSITIVE ODD INTEGER, SAY, 1171'
101:     READ (*,*) IU
102:
103:     NFCALL=0 ! INITIALIZE COUNTER FOR FUNCTION CALLS
104:     GBEST=1.D30 ! TO BE USED FOR TERMINATION CRITERION
105:     C      INITIALIZATION : GENERATE X(N,M) RANDOMLY
106:     DO I=1,N
107:     DO J=1,M
108:     CALL RANDOM(RAND)
109:     X(I,J)=(RAND-.5D00)*2000
110:     C      RANDOM NUMBERS BETWEEN -RRANGE AND +RRANGE (BOTH EXCLUSIVE)
111:     ENDDO
112:     ENDDO
113:     WRITE (*,*) 'COMPUTING --- PLEASE WAIT '
114:     IPCOUNT=0
115:     DO 100 ITR=1,ITER ! ITERATION BEGINS
116:
117:     C      EVALUATE ALL X FOR THE GIVEN FUNCTION
118:     DO I=1,N
119:     DO J=1,M
120:     A(J)=X(I,J)
121:     ENDDO
122:     CALL FUNC(A,M,F)
123:     C      STORE FUNCTION VALUES IN FV VECTOR
124:     FV(I)=F
125:     ENDDO
126:     C      -----
127:     C      FIND THE FITTEST (BEST) INDIVIDUAL AT THIS ITERATION
128:     FBEST=FV(1)
129:     KB=1
130:     DO IB=2,N
131:     IF (FV(IB) .LT. FBEST) THEN
132:     FBEST=FV(IB)
133:     KB=IB
134:     ENDIF

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135:          ENDDO
136: C      BEST FITNESS VALUE = FBEST : INDIVIDUAL X(KB)
137: C      -----
138: C      GENERATE OFFSPRINGS
139: DO I=1,N      ! I LOOP BEGINS
140: C      INITIALIZE CHILDREN IDENTICAL TO PARENTS; THEY WILL CHANGE LATER
141:         DO J=1,M
142:           Y(I,J)=X(I,J)
143:         ENDDO
144: C      SELECT RANDOMLY THREE OTHER INDIVIDUALS
145: 20      DO IRI=1,3      ! IRI LOOP BEGINS
146:         IR(IRI)=0
147:
148:         CALL RANDOM(RAND)
149:         IRJ=INT(RAND*N)+1
150: C      CHECK THAT THESE THREE INDIVIDUALS ARE DISTICT AND OTHER THAN I
151:         IF(IRI.EQ.1.AND.IRJ.NE.I) THEN
152:           IR(IRI)=IRJ
153:         ENDF
154:         IF(IRI.EQ.2.AND.IRJ.NE.I.AND.IRJ.NE.IR(1)) THEN
155:           IR(IRI)=IRJ
156:         ENDF
157:         IF(IRI.EQ.3.AND.IRJ.NE.I.AND.IRJ.NE.IR(1).AND.IRJ.NE.IR(2)) THEN
158:           IR(IRI)=IRJ
159:         ENDF
160:         ENDDO      ! IRI LOOP ENDS
161: C      CHECK IF ALL THE THREE IR ARE POSITIVE (INTEGERS)
162:         DO IX=1,3
163:           IF(IR(IX).LE.0) THEN
164:             GOTO 20      ! IF NOT THEN REGENERATE
165:           ENDF
166:         ENDDO
167: C      THREE RANDOMLY CHOSEN INDIVIDUALS DIFFERENT FROM I AND DIFFERENT
168: C      FROM EACH OTHER ARE IR(1),IR(2) AND IR(3)
169: C      -----
170: C      NO CROSS OVER, ONLY REPLACEMENT THAT IS PROBABILISTIC
171:         IF(NCROSS.LE.0) THEN
172:           DO J=1,M      ! J LOOP BEGINS
173:             CALL RANDOM(RAND)
174:             IF(RAND.LE.PCROS) THEN ! REPLACE IF RAND < PCROS
175:               A(J)=X(IR(1),J)+X(IR(2),J)-X(IR(3),J)*FACT ! CANDIDATE CHILD
176:             ENDF
177:           ENDDO      ! J LOOP ENDS
178:         ENDF
179:
180: C      -----
181: C      Crossover scheme (exponential) suggested by Kenneth Price in his
182: C      personal letter to the author (dated September 29, 2006)
183:         IF(NCROSS.GE.1) THEN
184:           CALL RANDOM(RAND)
185: 1      JR=INT(RAND*M)+1
186:           J=JR
187: 2      A(J)=X(IR(1),J)+FACT*(X(IR(2),J)-X(IR(3),J))
188: 3      J=J+1
189:           IF(J.GT.M) J=1
190: 4      IF(J.EQ.JR) GOTO 10
191: 5      CALL RANDOM(RAND)
192:           IF(PCROS.LE.RAND) GOTO 2
193: 6      A(J)=X(I,J)
194: 7      J=J+1
195:           IF(J.GT.M) J=1
196: 8      IF(J.EQ.JR) GOTO 10
197: 9      GOTO 6
198: 10     CONTINUE
199:         ENDF
200: C      -----
201:         CALL FUNC(A,M,F) ! EVALUATE THE OFFSPRING

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202:         IF (F.LT.FV(I)) THEN ! IF BETTER, REPLACE PARENTS BY THE CHILD
203:         FV(I)=F
204:         DO J=1,M
205:         Y(I,J)=A(J)
206:         ENDDO
207:         ENDIF
208:     ENDDO ! I LOOP ENDS
209:     DO I=1,N
210:     DO J=1,M
211:     X(I,J)=Y(I,J) ! NEW GENERATION IS A MIX OF BETTER PARENTS AND
212: C         BETTER CHILDREN
213:     ENDDO
214:     ENDDO
215:     IPCOUNT=IPCOUNT+1
216:     IF (IPCOUNT.EQ.IPRINT) THEN
217:     DO J=1,M
218:     A(J)=X(KB,J)
219:     ENDDO
220:     WRITE(*,*) (X(KB,J),J=1,M), ' FBEST UPTO NOW = ',FBEST
221:     WRITE(*,*) 'TOTAL NUMBER OF FUNCTION CALLS =',NFCALL
222:     IF (DABS (FBEST-GBEST) .LT.EPS) THEN
223:     WRITE(*,*) FTIT
224:     WRITE(*,*) 'COMPUTATION OVER'
225:     RETURN
226:     ELSE
227:     GBEST=FBEST
228:     ENDIF
229:     IPCOUNT=0
230:     ENDIF
231: C -----
232: 100 ENDDO ! ITERATION ENDS : GO FOR NEXT ITERATION, IF APPLICABLE
233: C -----
234: C WRITE(*,*) 'DID NOT CONVERGE. REDUCE EPS OR RAISE ITER OR DO BOTH'
235: C WRITE(*,*) 'INCREASE N, PCROS, OR SCALE FACTOR (FACT)'
236: C RETURN
237: C END
238: C -----
239: C RANDOM NUMBER GENERATOR (UNIFORM BETWEEN 0 AND 1 - BOTH EXCLUSIVE)
240: C SUBROUTINE RANDOM(RAND1)
241: C     DOUBLE PRECISION RAND1
242: C     COMMON /RNDM/IU,IV
243: C     INTEGER IU,IV
244: C     RAND=REAL(RAND1)
245: C     IV=IU*65539
246: C     IF (IV.LT.0) THEN
247: C     IV=IV+2147483647+1
248: C     ENDIF
249: C     RAND=IV
250: C     IU=IV
251: C     RAND=RAND*0.4656613E-09
252: C     RAND1= (RAND)
253: C     RETURN
254: C     END
255: C -----
256: C SUBROUTINE FSELECT(KF,M,FTIT)
257: C THE PROGRAM REQUIRES INPUTS FROM THE USER ON THE FOLLOWING -----
258: C (1) FUNCTION CODE (KF), (2) NO. OF VARIABLES IN THE FUNCTION (M);
259: C CHARACTER *70 TIT(100),FTIT
260: C WRITE(*,*) '-----'
261: C DATA TIT(1)/'KF=1 NEW FUNCTION(N#1) 2-VARIABLES M=2'/
262: C DATA TIT(2)/'KF=2 NEW FUNCTION(N#2) 2-VARIABLES M=2'/
263: C DATA TIT(3)/'KF=3 NEW FUNCTION(N#3) 2-VARIABLES M=2'/
264: C DATA TIT(4)/'KF=4 NEW FUNCTION(N#4) 2-VARIABLES M=2'/
265: C DATA TIT(5)/'KF=5 NEW QUINTIC FUNCTION M-VARIABLES M=?'/
266: C DATA TIT(6)/'KF=6 NEW NEEDLE-EYE FUNCTION (N#6) M-VARIABLES M=?'/
267: C DATA TIT(7)/'KF=7 NEW ZERO-SUM FUNCTION (N#7) M-VARIABLES M=?'/
268: C DATA TIT(8)/'KF=8 CORANA FUNCTION 4-VARIABLES M=4'/

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269: DATA TIT(9)/'KF=9 MODIFIED RCOS FUNCTION 2-VARIABLES M=2'/
270: DATA TIT(10)/'KF=10 FREUDENSTEIN ROTH FUNCTION 2-VARIABLES M=2'/
271: DATA TIT(11)/'KF=11 ANNS XOR FUNCTION 9-VARIABLES M=9'/
272: DATA TIT(12)/'KF=12 PERM FUNCTION #1 (SET BETA) 4-VARIABLES M=4'/
273: DATA TIT(13)/'KF=13 PERM FUNCTION #2 (SET BETA) M-VARIABLES M=?'/
274: DATA TIT(14)/'KF=14 POWER-SUM FUNCTION 4-VARIABLES M=4'/
275: DATA TIT(15)/'KF=15 GOLDSTEIN PRICE FUNCTION 2-VARIABLES M=2'/
276: DATA TIT(16)/'KF=16 BUKIN 6TH FUNCTION 2-VARIABLES M=2'/
277: DATA TIT(17)/'KF=17 NEW FUNCTION (N#8) 2-VARIABLES M=2'/
278: DATA TIT(18)/'KF=18 DEFL CORRUG SPRING FUNCTION M-VARIABLES M=?'/
279: DATA TIT(19)/'KF=19 NEW FACTORIAL FUNCTION M-VARIABLES M=?'/
280: DATA TIT(20)/'KF=20 NEW DECANOMIAL FUNCTION 2-VARIABLES M=2'/
281: DATA TIT(21)/'KF=21 JUDGE FUNCTION 2-VARIABLES M=2'/
282: DATA TIT(22)/'KF=22 NEW DODECAL FUNCTION 3-VARIABLES M=3'/
283: DATA TIT(23)/'KF=23 NEW SUM-EQ-PROD FUNCTION 2-VARIABLES M=2'/
284: DATA TIT(24)/'KF=24 NEW AM-EQ-GM FUNCTION M-VARIABLES M=?'/
285: DATA TIT(25)/'KF=25 YAO-LIU FUNCTION#2 M-VARIABLES M=?'/
286: DATA TIT(26)/'KF=26 YAO-LIU FUNCTION#3 M-VARIABLES M=?'/
287: DATA TIT(27)/'KF=27 YAO-LIU FUNCTION#4 M-VARIABLES M=?'/
288: DATA TIT(28)/'KF=28 YAO-LIU FUNCTION#6 M-VARIABLES M=?'/
289: DATA TIT(29)/'KF=29 YAO-LIU FUNCTION#7 M-VARIABLES M=?'/
290: DATA TIT(30)/'KF=30 YAO-LIU FUNCTION#12 M-VARIABLES M=?'/
291: DATA TIT(31)/'KF=31 YAO-LIU FUNCTION#13 M-VARIABLES M=?'/
292: DATA TIT(32)/'KF=32 YAO-LIU FUNCTION#14 2-VARIABLES M=2'/
293: DATA TIT(33)/'KF=33 YAO-LIU FUNCTION#15 4-VARIABLES M=4'/
294: DATA TIT(34)/'KF=34 LINEAR PROGRAMMING-I : 2-VARIABLES M=2'/
295: DATA TIT(35)/'KF=35 LINEAR PROGRAMMING-II : 3-VARIABLES M=3'/
296: DATA TIT(36)/'KF=36 HOUGEN FUNCTION : 5-VARIABLES M=5'/
297: DATA TIT(37)/'KF=37 GIUNTA FUNCTION : 2-VARIABLES M=2'/
298: DATA TIT(38)/'KF=38 EGGHOLDER FUNCTION : M-VARIABLES M=?'/
299: DATA TIT(39)/'KF=39 TRID FUNCTION : M-VARIABLES M=?'/
300: DATA TIT(40)/'KF=40 GRIEWANK FUNCTION : M-VARIABLES M=?'/
301: DATA TIT(41)/'KF=41 WEIERSTRASS FUNCTION : M-VARIABLES M=?'/
302: DATA TIT(42)/'KF=42 LEVY-3 FUNCTION : 2-VARIABLES M=2'/
303: DATA TIT(43)/'KF=43 LEVY-5 FUNCTION : 2-VARIABLES M=2'/
304: DATA TIT(44)/'KF=44 LEVY-8 FUNCTION : 3-VARIABLES M=3'/
305: DATA TIT(45)/'KF=45 RASTRIGIN FUNCTION : M-VARIABLES M=?'/
306: DATA TIT(46)/'KF=46 ACKLEY FUNCTION : M-VARIABLES M=?'/
307: DATA TIT(47)/'KF=47 MICHALEWICZ FUNCTION : M-VARIABLES M=?'/
308: DATA TIT(48)/'KF=48 SCHWEFEL FUNCTION : M-VARIABLES M=?'/
309: DATA TIT(49)/'KF=49 SHUBERT FUNCTION : 2-VARIABLES M=2'/
310: DATA TIT(50)/'KF=50 DIXON-PRICE FUNCTION : M-VARIABLES M=?'/
311: DATA TIT(51)/'KF=51 SHEKEL FUNCTION : 4-VARIABLES M=4'/
312: DATA TIT(52)/'KF=52 PAVIANI FUNCTION : 10-VARIABLES M=10'/
313: DATA TIT(53)/'KF=53 BRANIN FUNCTION#1 : 2-VARIABLES M=2'/
314: DATA TIT(54)/'KF=54 BRANIN FUNCTION#2 : 2-VARIABLES M=2'/
315: DATA TIT(55)/'KF=55 BOHACHEVSKY FUNCTION#1 : 2-VARIABLES M=2'/
316: DATA TIT(56)/'KF=56 BOHACHEVSKY FUNCTION#2 : 2-VARIABLES M=2'/
317: DATA TIT(57)/'KF=57 BOHACHEVSKY FUNCTION#3 : 2-VARIABLES M=2'/
318: DATA TIT(58)/'KF=58 EASOM FUNCTION : 2-VARIABLES M=2'/
319: DATA TIT(59)/'KF=59 ROSENBROCK FUNCTION : M-VARIABLES M=?'/
320: DATA TIT(60)/'KF=60 CROSS-LEGGED TABLE FUNCTION:2-VARIABLES M=2'/
321: DATA TIT(61)/'KF=61 CROSS FUNCTION : 2-VARIABLES M=2'/
322: DATA TIT(62)/'KF=62 CROSS-IN-TRAY FUNCTION : 2-VARIABLES M=2'/
323: DATA TIT(63)/'KF=63 CROWNED CROSS FUNCTION : 2-VARIABLES M=2'/
324: DATA TIT(64)/'KF=64 TT-HOLDER FUNCTION : 2-VARIABLES M=2'/
325: DATA TIT(65)/'KF=65 HOLDER-TABLE FUNCTION : 2-VARIABLES M=2'/
326: DATA TIT(66)/'KF=66 CARRON-TABLE FUNCTION : 2-VARIABLES M=2'/
327: DATA TIT(67)/'KF=67 PENHOLDER FUNCTION : 2-VARIABLES M=2'/
328: DATA TIT(68)/'KF=68 BIRD FUNCTION : 2-VARIABLES M=2'/
329: DATA TIT(69)/'KF=69 CHICHINADZE FUNCTION : 2-VARIABLES M=2'/
330: DATA TIT(70)/'KF=70 MCCORMICK FUNCTION : 2-VARIABLES M=2'/
331: -----
332: DO I=1,70
333: WRITE(*,*)TIT(I)
334: ENDDO
335: WRITE(*,*)'-----'

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336:      WRITE(*,*) 'FUNCTION CODE [KF] AND NO. OF VARIABLES [M] ?'
337:      READ(*,*) KF,M
338:      FTIT=TIT(KF) ! STORE THE NAME OF THE CHOSEN FUNCTION IN FTIT
339:      RETURN
340:      END
341: C -----
342:      SUBROUTINE FUNC(X,M,F)
343: C TEST FUNCTIONS FOR GLOBAL OPTIMIZATION PROGRAM
344:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
345:      COMMON /RNDM/IU,IV
346:      COMMON /KFF/KF,NFCALL
347:      INTEGER IU,IV
348:      DIMENSION X(*)
349:
350:      PI=4.D+00*DATAN(1.D+00)! DEFINING THE VALUE OF PI
351:      NFCALL=NFCALL+1 ! INCREMENT TO NUMBER OF FUNCTION CALLS
352: C KF IS THE CODE OF THE TEST FUNCTION
353: C -----
354:      IF (KF.EQ.1) THEN
355: C FUNCTION #1 MIN AT -0.18467 APPROX AT (-8.4666, -10) APPROX
356:      F=0.D00
357:      DO I=1,M
358:      IF (DABS(X(I)).GT.10.D00) THEN
359:      CALL RANDOM(RAND)
360:      X(I)=(RAND-0.5D00)*20
361:      ENDIF
362:      ENDDO
363:      F=DABS(DCOS(DSQRT(DABS(X(1)**2+X(2)))))**0.5 +0.01*X(1)+.01*X(2)
364:      RETURN
365:      ENDIF
366: C -----
367:      IF (KF.EQ.2) THEN
368: C FUNCTION #2 MIN = -0.199409 APPROX AT (-9.94112, -10) APPROX
369:      F=0.D00
370:      DO I=1,M
371:      IF (DABS(X(I)).GT.10.D00) THEN
372:      CALL RANDOM(RAND)
373:      X(I)=(RAND-0.5D00)*20
374:      ENDIF
375:      ENDDO
376:      F=DABS(DSIN(DSQRT(DABS(X(1)**2+X(2)))))**0.5 +0.01*X(1)+.01*X(2)
377:      RETURN
378:      ENDIF
379: C -----
380:      IF (KF.EQ.3) THEN
381: C FUNCTION #3 MIN = -1.01983 APPROX AT (-1.98682, -10.00000) APPROX
382:      F=0.D00
383:      DO I=1,M
384:      IF (DABS(X(I)).GT.10.D00) THEN
385:      CALL RANDOM(RAND)
386:      X(I)=(RAND-0.5D00)*20
387:      ENDIF
388:      ENDDO
389:      F1=DSIN(( DCOS(X(1))+DCOS(X(2)) )**2)**2
390:      F2=DCOS(( DSIN(X(1))+DSIN(X(2)) )**2)**2
391:      F=(F1+F2+X(1))**2 ! IS MULTIMODAL
392:      F=F+ 0.01*X(1)+0.1*X(2) ! MAKES UNIMODAL
393:      RETURN
394:      ENDIF
395: C -----
396:      IF (KF.EQ.4) THEN
397: C FUNCTION #4 MIN = -2.28395 APPROX AT (2.88631, 1.82326) APPROX
398:      F=0.D00
399:      DO I=1,M
400:      IF (DABS(X(I)).GT.10.D00) THEN
401:      CALL RANDOM(RAND)
402:      X(I)=(RAND-0.5D00)*20

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403:      ENDIF
404:      ENDDO
405:      F1=DSIN((DCOS(X(1))+DCOS(X(2)))**2)**2
406:      F2=DCOS((DSIN(X(1))+DSIN(X(2)))**2)**2
407:      F3=-DLOG((F1-F2+X(1))**2)
408:      F=F3+0.1D00*(X(1)-1.D00)**2+0.1D00*(X(2)-1.D00)**2
409:      RETURN
410:      ENDIF
411: C -----
412:      IF(KF.EQ.5) THEN
413: C      QUINTIC FUNCTION:GLOBAL MINIMA,EXTREMELY DIFFICULT TO OPTIMIZE
414: C      MIN VALUE = 0 AT PERMUTATION OF (2, 2,..., 2, -1, -1, ..., -1,
415: C      -0.402627941) GIVES MIN F = 0.
416:      F=0.D00
417:      DO I=1,M
418:      IF(DABS(X(I)).GT.10.D00) THEN
419:      CALL RANDOM(RAND)
420:      X(I)=(RAND-0.5D00)*20
421:      ENDIF
422:      ENDDO
423:      CALL QUINTIC(M,F,X)
424:      RETURN
425:      ENDIF
426: C -----
427:      IF(KF.EQ.6) THEN
428: C      NEEDLE-EYE FUNCTION M=>1;
429: C      MIN = 1 IF ALL ABS(X) ARE SMALLER THAN THE EYE
430: C      SMALLER THE VALUE OF ZZ, MORE DIFFICULT TO ENTER THE EYE
431: C      LARGER THE VALUE OF M, MORE DIFFICULT TO FIND THE OPTIMUM
432:      F=0.D00
433:      EYE=0.000001D00
434:      FP=0.D00
435:      DO I=1,M
436:      IF(DABS(X(I)).GT.EYE) THEN
437:      FP=1.D00
438:      F=F+100.D00+DABS(X(I))
439:      ELSE
440:      F=F+1.D00
441:      ENDIF
442:      ENDDO
443:      IF(FP.EQ.0.D00) F=F/M
444:      RETURN
445:      ENDIF
446: C -----
447:      IF(KF.EQ.7) THEN
448: C      ZERO SUM FUNCTION : MIN = 0 AT SUM(X(I))=0
449:      F=0.D00
450:      DO I=1,M
451:      IF(DABS(X(I)).GT.10.D00) THEN
452:      CALL RANDOM(RAND)
453:      X(I)=(RAND-0.5D00)*20
454:      ENDIF
455:      ENDDO
456:      SUM=0.D00
457:      DO I=1,M
458:      SUM=SUM+X(I)
459:      ENDDO
460:      IF(SUM.NE.0.D00) F=1.D00+(10000*DABS(SUM))**0.5
461:      RETURN
462:      ENDIF
463: C -----
464:      IF(KF.EQ.8) THEN
465: C      CORANA FUNCTION : MIN = 0 AT (0, 0, 0, 0) APPROX
466:      F=0.D00
467:      DO I=1,M
468:      IF(DABS(X(I)).GT.1000.D00) THEN
469:      CALL RANDOM(RAND)

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470:      X(I)=(RAND-0.5D00)*2000
471:      ENDDIF
472:      ENDDO
473:      DO J=1,M
474:          IF(J.EQ.1) DJ=1.D00
475:          IF(J.EQ.2) DJ=1000.D00
476:          IF(J.EQ.3) DJ=10.D00
477:          IF(J.EQ.4) DJ=100.D00
478:          ISGNXJ=1
479:          IF(X(J).LT.0.D00) ISGNXJ=-1
480:          ZJ=(DABS(X(J)/0.2D00)+0.49999)*ISGNXJ*0.2D00
481:          ISGNZJ=1
482:          IF(ZJ.LT.0.D00) ISGNZJ=-1
483:          IF(DABS(X(J)-ZJ).LT.0.05D00) THEN
484:              F=F+0.15D00*(ZJ-0.05D00*ISGNZJ)**2 * DJ
485:          ELSE
486:              F=F+DJ*X(J)**2
487:          ENDDIF
488:      ENDDO
489:      RETURN
490:      ENDDIF
491:  C -----
492:      IF(KF.EQ.9) THEN
493:  C  MODIFIED RCOS FUNCTION MIN=-0.179891 AT (-3.196989, 12.52626)APPRX
494:      F=0.D00
495:      IF(X(1).LT.-5.D00 .OR. X(1).GT.10.D00) THEN
496:          CALL RANDOM(RAND)
497:          X(1)=RAND*15.D00 -5.D00
498:      ENDDIF
499:      IF(X(2).LT.0.D00 .OR. X(2).GT.15.D00) THEN
500:          CALL RANDOM(RAND)
501:          X(2)=RAND*15.D00
502:      ENDDIF
503:      CA=1.D00
504:      CB=5.1/(4*PI**2)
505:      CC=5.D00/PI
506:      CD=6.D00
507:      CE=10.D00
508:      CF=1.0/(8*PI)
509:      F1=CA*(X(2)-CB*X(1)**2+CC*X(1)-CD)**2
510:      F2=CE*(1.D00-CF)*DCOS(X(1))*DCOS(X(2))
511:      F3=DLOG(X(1)**2+X(2)**2+1.D00)
512:      F=-1.0/(F1+F2+F3+CE)
513:      RETURN
514:      ENDDIF
515:  C -----
516:      IF(KF.EQ.10) THEN
517:  C  FREUDENSTEIN ROTH FUNCTION : MIN = 0 AT (5, 4)
518:      F=0.D00
519:      DO I=1,M
520:          IF(DABS(X(I)).GT.10.D00) THEN
521:              CALL RANDOM(RAND)
522:              X(I)=(RAND-0.5D00)*20
523:          ENDDIF
524:      ENDDO
525:      F1=(-13.D00+X(1)+((5.D00-X(2))*X(2)-2)*X(2))**2
526:      F2=(-29.D00+X(1)+((X(2)+1.D00)*X(2)-14.D00)*X(2))**2
527:      F=F1+F2
528:      RETURN
529:      ENDDIF
530:  C -----
531:      IF(KF.EQ.11) THEN
532:  C  ANNS XOR FUNCTION (PARSOPOULOS, KE, PLAGIANAKOS, VP, MAGOULAS, GD
533:  C  AND VRAHATIS, MN "STRETCHING TECHNIQUE FOR OBTAINING GLOBAL
534:  C  MINIMIZERS THROUGH PARTICLE SWARM OPTIMIZATION")
535:  C  MIN=0.9597588 FOR X=(1, -1, 1, -1, -1, 1, 1, -1, 0.421134) APPROX
536:  C  OBTAINED BY DIFFERENTIAL EVOLUTION PROGRAM

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537:      F=0.D00
538:      DO I=1,M
539:      IF (DABS(X(I)).GT.1.D00) THEN
540:      CALL RANDOM(RAND)
541:      X(I)=(RAND-0.5D00)*2
542:      ENDDO
543:      ENDDO
544:      F11=X(7)/(1.D00+DEXP(-X(1)-X(2)-X(5)))
545:      F12=X(8)/(1.D00+DEXP(-X(3)-X(4)-X(6)))
546:      F1=(1.D00+DEXP(-F11-F12-X(9)))**(-2)
547:      F21=X(7)/(1.D00+DEXP(-X(5)))
548:      F22=X(8)/(1.D00+DEXP(-X(6)))
549:      F2=(1.D00+DEXP(-F21-F22-X(9)))**(-2)
550:      F31=X(7)/(1.D00+DEXP(-X(1)-X(5)))
551:      F32=X(8)/(1.D00+DEXP(-X(3)-X(6)))
552:      F3=(1.D00-(1.D00+DEXP(-F31-F32-X(9)))**(-1))**2
553:      F41=X(7)/(1.D00+DEXP(-X(2)-X(5)))
554:      F42=X(8)/(1.D00+DEXP(-X(4)-X(6)))
555:      F4=(1.D00-(1.D00+DEXP(-F41-F42-X(9)))**(-1))**2
556:      F=F1+F2+F3+F4
557:      RETURN
558:      ENDDO
559: C -----
560:      IF (KF.EQ.12) THEN
561: C      PERM FUNCTION #1 MIN = 0 AT (1, 2, 3, 4)
562: C      BETA => 0. CHANGE IF NEEDED. SMALLER BETA RAISES DIFFICULTY
563: C      FOR BETA=0, EVERY PERMUTED SOLUTION IS A GLOBAL MINIMUM
564:      BETA=50.D00
565:      F=0.D00
566:      DO I=1,M
567:      IF (DABS(X(I)).GT.M) THEN
568:      CALL RANDOM(RAND)
569:      X(I)=(RAND-0.5D00)*2*M
570:      ENDDO
571:      ENDDO
572:      DO K=1,M
573:      SUM=0.D00
574:      DO I=1,M
575:      SUM=SUM+(I**K+BETA)*((X(I)/I)**K-1.D00)
576:      ENDDO
577:      F=F+SUM**2
578:      ENDDO
579:      RETURN
580:      ENDDO
581: C -----
582:      IF (KF.EQ.13) THEN
583: C      PERM FUNCTION #2 MIN = 0 AT (1/1, 1/2, 1/3, 1/4,..., 1/M)
584: C      BETA => 0. CHANGE IF NEEDED. SMALLER BETA RAISES DIFFICULTY
585: C      FOR BETA=0, EVERY PERMUTED SOLUTION IS A GLOBAL MINIMUM
586:      BETA=10.D00
587:      DO I=1,M
588:      IF (DABS(X(I)).GT.1.D00) THEN
589:      CALL RANDOM(RAND)
590:      X(I)=(RAND-.5D00)*2
591:      ENDDO
592:      SGN=X(I)/DABS(X(I))
593:      ENDDO
594:      F=0.D00
595:      DO K=1,M
596:      SUM=0.D00
597:      DO I=1,M
598:      SUM=SUM+(I+BETA)*(X(I)**K-(1.D00/I)**K)
599:      ENDDO
600:      F=F+SUM**2
601:      ENDDO
602:      RETURN
603:      ENDDO

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604: C -----
605: IF (KF.EQ.14) THEN
606: C POWER SUM FUNCTION; MIN = 0 AT PERM(1,2,2,3) FOR B=(8,18,44,114)
607: C 0 =< X <=4
608: F=0.D00
609: DO I=1,M
610: C ANY PERMUTATION OF (1,2,2,3) WILL GIVE MIN = ZERO
611: IF (X(I).LT.0.D00 .OR. X(I).GT.4.D00) THEN
612: CALL RANDOM(RAND)
613: X(I)=RAND*4
614: ENDIF
615: ENDDO
616: DO K=1,M
617: SUM=0.D00
618: DO I=1,M
619: SUM=SUM+X(I)**K
620: ENDDO
621: IF (K.EQ.1) B=8.D00
622: IF (K.EQ.2) B=18.D00
623: IF (K.EQ.3) B=44.D00
624: IF (K.EQ.4) B=114.D00
625: F=F+(SUM-B)**2
626: ENDDO
627: RETURN
628: ENDIF
629: C -----
630: IF (KF.EQ.15) THEN
631: C GOLDSTEIN PRICE FUNCTION : MIN VALUE = 3 AT (0, -1)
632: F=0.D00
633: DO I=1,M
634: IF (DABS(X(I)).GT.10.D00) THEN
635: CALL RANDOM(RAND)
636: X(I)=(RAND-.5D00)*20
637: ENDIF
638: ENDDO
639: F11=(X(1)+X(2)+1.D00)**2
640: F12=(19.D00-14*X(1)+ 3*X(1)**2-14*X(2)+ 6*X(1)*X(2)+ 3*X(2)**2)
641: F1=1.00+F11*F12
642: F21=(2*X(1)-3*X(2))**2
643: F22=(18.D00-32*X(1)+12*X(1)**2+48*X(2)-36*X(1)*X(2)+27*X(2)**2)
644: F2=30.D00+F21*F22
645: F=(F1*F2)
646: RETURN
647: ENDIF
648: C -----
649: IF (KF.EQ.16) THEN
650: C BUKIN'S 6TH FUNCTION MIN = 0 FOR (-10, 1)
651: C -15.LE. X(1).LE. -5 AND -3.LE. X(2).LE. 3
652: IF (X(1).LT. -15.D00 .OR. X(1).GT. -5.D00) THEN
653: CALL RANDOM(RAND)
654: X(1)=- (RAND*10+5.D00)
655: ENDIF
656: IF (DABS(X(2)).GT.3.D00) THEN
657: CALL RANDOM(RAND)
658: X(2)=(RAND-.5D00)*6
659: ENDIF
660: F=100.D0*DSQRT(DABS(X(2)-0.01D0*X(1)**2))+ 0.01D0*DABS(X(1)+10.D0)
661: RETURN
662: ENDIF
663: C -----
664: IF (KF.EQ.17) THEN
665: C NEW N#8 FUNCTION (MULTIPLE GLOBAL MINIMA)
666: C MIN VALUE = -1 AT (AROUND .7 AROUND, 0.785 APPROX)
667: F=0.D00
668: DO I=1,M
669: IF (X(I).LT.0.5D00 .OR. X(I).GT.1.D00) THEN
670: CALL RANDOM(RAND)

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671:      X(I)=RAND/2.D00
672:      ENDF
673:      ENDDO
674:      F=-DEXP(-DABS(DLOG(.001D00+DABS((DSIN(X(1)+X(2))+DSIN(X(1)-X(2))+
675:      & (DCOS(X(1)+X(2))*DCOS(X(1)-X(2))+.001)**2)+
676:      & .01D00*(X(2)-X(1)**2)))
677:      RETURN
678:      ENDF
679: C -----
680:      IF(KF.EQ.18) THEN
681: C      DEFLECTED CORRUGATED SPRING FUNCTION
682: C      MIN VALUE = -1 AT (5, 5, ..., 5) FOR ANY K AND ALPHA=5; M VARIABLE
683:      CALL DCS(M,F,X)
684:      RETURN
685:      ENDF
686: C -----
687:      IF(KF.EQ.19) THEN
688: C      FACTORIAL FUNCTION, MIN =0 AT X=(1,2,3,...,M)
689:      CALL FACTOR1(M,F,X)
690:      RETURN
691:      ENDF
692: C -----
693:      IF(KF.EQ.20) THEN
694: C      DECANOMIAL FUNCTION, MIN =0 AT X=(2, -3)
695:      DO I=1,M
696:      IF(DABS(X(I)).GT.4.D00) THEN
697:      CALL RANDOM(RAND)
698:      X(I)=(RAND-0.5D00)*8
699:      ENDF
700:      ENDDO
701:      CALL DECANOM(M,F,X)
702:      RETURN
703:      ENDF
704: C -----
705:      IF(KF.EQ.21) THEN
706: C      JUDGE'S FUNCTION F(0.864, 1.23) = 16.0817; M=2
707:      CALL JUDGE(M,X,F)
708:      RETURN
709:      ENDF
710: C -----
711:      IF(KF.EQ.22) THEN
712: C      DODECAL FUNCTION
713:      CALL DODECAL(M,F,X)
714:      RETURN
715:      ENDF
716: C -----
717:      IF(KF.EQ.23) THEN
718: C      WHEN X(1)*X(2)=X(1)*X(2) ? M=2
719:      CALL SEQP(M,F,X)
720:      RETURN
721:      ENDF
722: C -----
723:      IF(KF.EQ.24) THEN
724: C      WHEN ARITHMETIC MEAN = GEOMETRIC MEAN ? : M =>1
725:      CALL AMGM(M,F,X)
726:      RETURN
727:      ENDF
728: C -----
729:      IF(KF.EQ.25) THEN
730: C      M =>2
731:      CALL FUNCT2(M,F,X)
732:      RETURN
733:      ENDF
734: C -----
735:      IF(KF.EQ.26) THEN
736: C      M =>2
737:      CALL FUNCT3(M,F,X)

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738:      RETURN
739:      ENDIF
740: C -----
741:      IF (KF.EQ.27) THEN
742: C      M =>2
743:      CALL FUNCT4 (M, F, X)
744:      RETURN
745:      ENDIF
746: C -----
747:      IF (KF.EQ.28) THEN
748: C      M =>2
749:      CALL FUNCT6 (M, F, X)
750:      RETURN
751:      ENDIF
752: C -----
753:      IF (KF.EQ.29) THEN
754: C      M =>2
755:      CALL FUNCT7 (M, F, X)
756:      RETURN
757:      ENDIF
758: C -----
759:      IF (KF.EQ.30) THEN
760: C      M =>2
761:      CALL FUNCT12 (M, F, X)
762:      RETURN
763:      ENDIF
764: C -----
765:      IF (KF.EQ.31) THEN
766: C      M =>2
767:      CALL FUNCT13 (M, F, X)
768:      RETURN
769:      ENDIF
770: C -----
771:      IF (KF.EQ.32) THEN
772: C      M =2
773:      CALL FUNCT14 (M, F, X)
774:      RETURN
775:      ENDIF
776: C -----
777:      IF (KF.EQ.33) THEN
778: C      M =4
779:      CALL FUNCT15 (M, F, X)
780:      RETURN
781:      ENDIF
782: C -----
783:      IF (KF.EQ.34) THEN
784: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM : M =2
785:      CALL LINPROG1 (M, F, X)
786:      RETURN
787:      ENDIF
788: C -----
789:      IF (KF.EQ.35) THEN
790: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM : M =3
791:      CALL LINPROG2 (M, F, X)
792:      RETURN
793:      ENDIF
794: C -----
795:      IF (KF.EQ.36) THEN
796: C      HOUGEN FUNCTION 5 VARIABLES : M =3
797:      CALL HOUGEN (X, M, F)
798:      RETURN
799:      ENDIF
800: C -----
801:      IF (KF.EQ.37) THEN
802: C      GIUNTA FUNCTION 2 VARIABLES :M =2
803:      CALL GIUNTA (M, X, F)
804:      RETURN
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805:      ENDIF
806:  C -----
807:      IF (KF.EQ.38) THEN
808:  C      EGGHOLDER FUNCTION M VARIABLES
809:      CALL EGGHOLD (M, X, F)
810:      RETURN
811:      ENDIF
812:  C -----
813:      IF (KF.EQ.39) THEN
814:  C      TRID FUNCTION M VARIABLES
815:      CALL TRID (M, X, F)
816:      RETURN
817:      ENDIF
818:  C -----
819:      IF (KF.EQ.40) THEN
820:  C      GRIEWANK FUNCTION M VARIABLES
821:      CALL GRIEWANK (M, X, F)
822:      RETURN
823:      ENDIF
824:  C -----
825:      IF (KF.EQ.41) THEN
826:  C      WEIERSTRASS FUNCTION M VARIABLES
827:      CALL WEIERSTRASS (M, X, F)
828:      RETURN
829:      ENDIF
830:  C -----
831:      IF (KF.EQ.42) THEN
832:  C      LEVY-3 FUNCTION 2 VARIABLES
833:      CALL LEVY3 (M, X, F)
834:      RETURN
835:      ENDIF
836:  C -----
837:      IF (KF.EQ.43) THEN
838:  C      LEVY-5 FUNCTION 2 VARIABLES
839:      CALL LEVY5 (M, X, F)
840:      RETURN
841:      ENDIF
842:  C -----
843:      IF (KF.EQ.44) THEN
844:  C      LEVY-8 FUNCTION 3 VARIABLES
845:      CALL LEVY8 (M, X, F)
846:      RETURN
847:      ENDIF
848:  C -----
849:      IF (KF.EQ.45) THEN
850:  C      RASTRIGIN FUNCTION M VARIABLES
851:      CALL RASTRIGIN (M, X, F)
852:      RETURN
853:      ENDIF
854:  C -----
855:      IF (KF.EQ.46) THEN
856:  C      ACKLEY FUNCTION M VARIABLES
857:      CALL ACKLEY (M, X, F)
858:      RETURN
859:      ENDIF
860:  C -----
861:      IF (KF.EQ.47) THEN
862:  C      MICHALEWICZ FUNCTION M VARIABLES
863:      CALL MICHALEWICZ (M, X, F)
864:      RETURN
865:      ENDIF
866:  C -----
867:      IF (KF.EQ.48) THEN
868:  C      SCHWEFEL FUNCTION M VARIABLES
869:      CALL SCHWEFEL (M, X, F)
870:      RETURN
871:      ENDIF
```

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872: C -----
873: IF (KF.EQ.49) THEN
874: C SHUBERT FUNCTION 2 VARIABLES
875: CALL SHUBERT (M, X, F)
876: RETURN
877: ENDIF
878: C -----
879: IF (KF.EQ.50) THEN
880: C DIXON AND PRICE FUNCTION M VARIABLES
881: CALL DIXPRICE (M, X, F)
882: RETURN
883: ENDIF
884: C -----
885: IF (KF.EQ.51) THEN
886: C SHEKEL FUNCTION 4 VARIABLES
887: CALL SHEKEL (M, X, F)
888: RETURN
889: ENDIF
890: C -----
891: IF (KF.EQ.52) THEN
892: C PAVIANI FUNCTION 10 VARIABLES
893: CALL PAVIANI (M, X, F)
894: RETURN
895: ENDIF
896: C -----
897: IF (KF.EQ.53) THEN
898: C BRANIN FUNCTION#1 2 VARIABLES
899: CALL BRANIN1 (M, X, F)
900: RETURN
901: ENDIF
902: C -----
903: IF (KF.EQ.54) THEN
904: C BRANIN FUNCTION#2 2 VARIABLES
905: CALL BRANIN2 (M, X, F)
906: RETURN
907: ENDIF
908: C -----
909: IF (KF.EQ.55) THEN
910: C BOHACHEVSKY FUNCTION#1 2 VARIABLES
911: CALL BOHACHEVSKY1 (M, X, F)
912: RETURN
913: ENDIF
914: C -----
915: IF (KF.EQ.56) THEN
916: C BOHACHEVSKY FUNCTION#2 2 VARIABLES
917: CALL BOHACHEVSKY2 (M, X, F)
918: RETURN
919: ENDIF
920: C -----
921: IF (KF.EQ.57) THEN
922: C BOHACHEVSKY FUNCTION#3 2 VARIABLES
923: CALL BOHACHEVSKY3 (M, X, F)
924: RETURN
925: ENDIF
926: C -----
927: IF (KF.EQ.58) THEN
928: C EASOM FUNCTION#3 2 VARIABLES
929: CALL EASOM (M, X, F)
930: RETURN
931: ENDIF
932: C -----
933: IF (KF.EQ.59) THEN
934: C ROSENBROCK FUNCTION M VARIABLES
935: CALL ROSENBROCK (M, X, F)
936: RETURN
937: ENDIF
938: C -----
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939:      IF (KF.EQ.60) THEN
940: C     CROSS-LEGGED TABLE FUNCTION : 2 VARIABLES
941:      CALL CROSSLEG (M, X, F)
942:      RETURN
943:      ENDIF
944: C     -----
945:      IF (KF.EQ.61) THEN
946: C     CROSS FUNCTION : 2 VARIABLES
947:      CALL CROSS (M, X, F)
948:      RETURN
949:      ENDIF
950: C     -----
951:      IF (KF.EQ.62) THEN
952: C     CROSS-IN-TRAY FUNCTION : 2 VARIABLES
953:      CALL CROSSINTRAY (M, X, F)
954:      RETURN
955:      ENDIF
956: C     -----
957:      IF (KF.EQ.63) THEN
958: C     CROWNED-CROSS FUNCTION : 2 VARIABLES
959:      CALL CROWNEDCROSS (M, X, F)
960:      RETURN
961:      ENDIF
962: C     -----
963:      IF (KF.EQ.64) THEN
964: C     TT-HOLDER FUNCTION : 2 VARIABLES, MIN F ([+/-]1.5706, 0) = -10.8723
965:      CALL TTHOLDER (M, X, F)
966:      RETURN
967:      ENDIF
968: C     -----
969:      IF (KF.EQ.65) THEN
970: C     HOLDER-TABLE FUNCTION : 2 VARIABLES
971: C     MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -26.92034 APPROX
972:      CALL HOLDERTABLE (M, X, F)
973:      RETURN
974:      ENDIF
975: C     -----
976:      IF (KF.EQ.66) THEN
977: C     CARROM-TABLE FUNCTION : 2 VARIABLES
978: C     MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -24.15682 APPROX
979:      CALL CARROMTABLE (M, X, F)
980:      RETURN
981:      ENDIF
982: C     -----
983:      IF (KF.EQ.67) THEN
984: C     PEN-HOLDER FUNCTION : 2 VARIABLES
985: C     MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -0.963535 APPROX
986:      CALL PENHOLDER (M, X, F)
987:      RETURN
988:      ENDIF
989: C     -----
990:      IF (KF.EQ.68) THEN
991: C     BIRD FUNCTION : 2 VARIABLES
992: C     MIN F (4.70104, 3.15294) APPROX = -106.764537 APPROX OR
993: C     MIN F (-1.58214, -3.13024) APPROX = -106.764537 APPROX
994:      CALL BIRD (M, X, F)
995:      RETURN
996:      ENDIF
997: C     -----
998:      IF (KF.EQ.69) THEN
999: C     CHICHINADZE FUNCTION : -30 <=X(I)<= 30; M=2
1000: C     MIN F (5.901329, 0.5) = -43.3158621
1001:      CALL CHICHINADZE (M, X, F)
1002:      RETURN
1003:      ENDIF
1004: C     -----
1005:      IF (KF.EQ.70) THEN

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1073:      RETURN
1074:      END
1075: C -----
1076:      SUBROUTINE JUDGE(M,X,F)
1077:      PARAMETER (N=20)
1078: C      THIS SUBROUTINE IS FROM THE EXAMPLE IN JUDGE ET AL., THE THEORY
1079: C      AND PRACTICE OF ECONOMETRICS, 2ND ED., PP. 956-7. THERE ARE TWO
1080: C      OPTIMA: F(0.86479,1.2357)=16.0817307 (WHICH IS THE GLOBAL MINIMUM)
1081: C      AND F(2.35,-0.319)=20.9805 (WHICH IS LOCAL). ADAPTED FROM BILL
1082: C      GOFFE'S SIMMAN (SIMULATED ANNEALING) PROGRAM
1083:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1084:      DIMENSION Y(N), X2(N), X3(N), X(*)
1085:      DATA (Y(I),I=1,N)/4.284,4.149,3.877,0.533,2.211,2.389,2.145,
1086: & 3.231,1.998,1.379,2.106,1.428,1.011,2.179,2.858,1.388,1.651,
1087: & 1.593,1.046,2.152/
1088:      DATA (X2(I),I=1,N)/.286,.973,.384,.276,.973,.543,.957,.948,.543,
1089: & .797,.936,.889,.006,.828,.399,.617,.939,.784,.072,.889/
1090:      DATA (X3(I),I=1,N)/.645,.585,.310,.058,.455,.779,.259,.202,.028,
1091: & .099,.142,.296,.175,.180,.842,.039,.103,.620,.158,.704/
1092:
1093:      F=0.D00
1094:      DO I=1,N
1095:      F=F+(X(1) + X(2)*X2(I) + (X(2)**2)*X3(I) - Y(I))**2
1096:      ENDDO
1097:      RETURN
1098:      END
1099: C -----
1100:      SUBROUTINE DODECAL(M,F,X)
1101:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1102:      DIMENSION X(*)
1103: C      DODECAL POLYNOMIAL MIN F(1,2,3)=0
1104:      F=0.D00
1105:      F1=2*X(1)**3+5*X(1)*X(2)+4*X(3)-2*X(1)**2*X(3)-18.D00
1106:      F2=X(1)+X(2)**3+X(1)*X(2)**2+X(1)*X(3)**2-22.D00
1107:      F3=8*X(1)**2+2*X(2)*X(3)+2*X(2)**2+3*X(2)**3-52.D00
1108:      F=(F1*F3*F2**2+F1*F2*F3**2+F2**2+(X(1)+X(2)-X(3))**2)**2
1109:      RETURN
1110:      END
1111: C -----
1112:      SUBROUTINE SEQP(M,F,X)
1113:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1114:      DIMENSION X(*)
1115: C      FOR WHAT VALUES X(1)+X(2)=X(1)*X(2) ? ANSWER: FOR (0,0) AND (2,2)
1116: C      WHILE X(1), X(2) ARE INTEGERS.
1117:      X(1)=INT(X(1)) ! X(1) CONVERTED TO INTEGER
1118:      X(2)=INT(X(2)) ! X(2) CONVERTED TO INTEGER
1119:
1120:      F1=X(1)+X(2)
1121:      F2=X(1)*X(2)
1122:      F=(F1-F2)**2 ! TURN ALIVE THIS XOR
1123: C      F=DABS(F1-F2) ! TURN ALIVE THIS - BUT NOT BOTH -----
1124:      RETURN
1125:      END
1126: C -----
1127:      SUBROUTINE AMGM(M,F,X)
1128:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1129:      DIMENSION X(*)
1130: C      FOR WHAT VALUES ARITHMETIC MEAN = GEOMETRIC MEAN ? THE ANSWER IS:
1131: C      IF X(1)=X(2)=...=X(M) AND ALL X ARE NON-NEGATIVE
1132: C      TAKE ONLY THE ABSOLUTE VALUES OF X
1133:      SUM=0.D00
1134:      DO I=1,M
1135:      X(I)=DABS(X(I))
1136:      ENDDO
1137: C      SET SUM = SOME POSITIVE NUMBER. THIS MAKES THE FUNCTION UNIMODAL
1138:      SUM= 100.D00 ! TURNED ALIVE FOR UNIQUE MINIMUM AND SET SUM TO
1139: C      SOME POSITIVE NUMBER. HERE IT IS 100; IT COULD BE ANYTHING ELSE.

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1140:      F1=0.D00
1141:      F2=1.D00
1142:      DO I=1,M
1143:      F1=F1+X(I)
1144:      F2=F2*X(I)
1145:      ENDDO
1146:      XSUM=F1
1147:      F1=F1/M ! SUM DIVIDED BY M = ARITHMETIC MEAN
1148:      F2=F2**(1.D00/M) ! MTH ROOT OF THE PRODUCT = GEOMETRIC MEAN
1149:      F=(F1-F2)**2
1150:      IF (SUM.GT.0.D00) F=F+(SUM-XSUM)**2
1151:      RETURN
1152:      END
1153: C -----
1154:      SUBROUTINE FUNCT2 (M,F,X)
1155: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1156: C      IN FOGEL, L.J., ANGELIN, P.J. AND BACK, T. (ED) PROCEEDINGS OF THE
1157: C      FIFTH ANNUAL CONFERENCE ON EVOLUTIONARY PROGRAMMING, PP. 451-460,
1158: C      MIT PRESS, CAMBRIDGE, MASS.
1159: C      MIN F (0, 0, ..., 0) = 0
1160:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1161:      DIMENSION X(*)
1162:      F=0.D00
1163:      F1=1.D00
1164:      DO I=1,M
1165:      IF (DABS (X(I)) .GT.10.D00) THEN
1166:      CALL RANDOM (RAND)
1167:      X(I)=(RAND-.5D00)*20
1168:      ENDIF
1169:      ENDDO
1170:      DO I=1,M
1171:      F=F+DABS (X(I))
1172:      F1=F1*DABS (X(I))
1173:      ENDDO
1174:      F=F+F1
1175:      RETURN
1176:      END
1177: C -----
1178:      SUBROUTINE FUNCT3 (M,F,X)
1179: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1180: C      MIN F (0, 0, ..., 0) = 0
1181:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1182:      DIMENSION X(*)
1183:      F=0.D00
1184:      F1=0.D00
1185:      DO I=1,M
1186:      IF (DABS (X(I)) .GT.100.D00) THEN
1187:      CALL RANDOM (RAND)
1188:      X(I)=(RAND-.5D00)*200
1189:      ENDIF
1190:      ENDDO
1191:      DO I=1,M
1192:      F1=0.D00
1193:      DO J=1,I
1194:      F1=F1+X(J)**2
1195:      ENDDO
1196:      F=F+F1
1197:      ENDDO
1198:      RETURN
1199:      END
1200: C -----
1201:      SUBROUTINE FUNCT4 (M,F,X)
1202: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1203: C      MIN F (0, 0, ..., 0) = 0
1204:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1205:      DIMENSION X(*)
1206:      F=0.D00

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1207:      DO I=1,M
1208:      IF (X(I) .LT. 0.D00 .OR. X(I) .GE. M) THEN
1209:      CALL RANDOM(RAND)
1210:      X(I)=RAND*2*M
1211:      ENDF
1212:      ENDDO
1213: C      FIND MAX(X(I))=MAX(ABS(X(I))) NOTE: HERE X(I) CAN BE ONLY POSITIVE
1214:      XMAX=X(1)
1215:      DO I=1,M
1216:      IF (XMAX .LT. X(I)) XMAX=X(I)
1217:      ENDDO
1218:      F=XMAX
1219:      RETURN
1220:      END
1221: C      -----
1222:      SUBROUTINE FUNCT6 (M,F,X)
1223: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1224: C      MIN F (-.5, -.5, ..., -.5) = 0
1225:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1226:      DIMENSION X(*)
1227:      F=0.D00
1228:      DO I=1,M
1229:      IF (DABS(X(I)) .GT. 100.D00) THEN
1230:      CALL RANDOM(RAND)
1231:      X(I)=(RAND-.5D00)*200
1232:      ENDF
1233:      ENDDO
1234:      DO I=1,M
1235:      F=F+(X(I)+0.5D00)**2
1236:      ENDDO
1237:      RETURN
1238:      END
1239: C      -----
1240:      SUBROUTINE FUNCT7 (M,F,X)
1241: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1242: C      MIN F (0, 0, ..., 0) = 0
1243:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1244:      COMMON /RNDM/IU,IV
1245:      INTEGER IU,IV
1246:      DIMENSION X(*)
1247:      F=0.D00
1248:      DO I=1,M
1249:      IF (DABS(X(I)) .GT. 1.28D00) THEN
1250:      CALL RANDOM(RAND)
1251:      X(I)=(RAND-0.5D00)*2.56D00
1252:      ENDF
1253:      ENDDO
1254:      DO I=1,M
1255:      CALL RANDOM(RAND)
1256:      F=F+(I*X(I))**4
1257:      ENDDO
1258:      CALL RANDOM(RAND)
1259:      F=F+RAND
1260:      RETURN
1261:      END
1262: C      -----
1263:      SUBROUTINE FUNCT12 (M,F,X)
1264: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1265:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1266:      DIMENSION X(100),Y(100)
1267:      DATA A,B,C /10.D00,100.D00,4.D00/
1268:      PI=4.D00*DATAN(1.D00)
1269:      F=0.D00
1270: C      MIN F (-1, -1, -1, ..., -1) = 0
1271: C      X(I)=-1.D00 ! TO CHECK, TURN IT ALIVE
1272:      DO I=1,M
1273:      IF (DABS(X(I)) .GT. 50.D00) THEN

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1274:      CALL RANDOM(RAND)
1275:      X(I)=(RAND-0.5D00)*100.D00
1276:      ENDIF
1277:      ENDDO
1278:      F1=0.D00
1279:      DO I=1,M
1280:      XX=DABS(X(I))
1281:      U=0.D00
1282:      IF (XX.GT.A) U=B*(XX-A)**C
1283:      F1=F1+U
1284:      ENDDO
1285:      F2=0.D00
1286:      DO I=1,M-1
1287:      Y(I)=1.D00+.25D00*(X(I)+1.D00)
1288:      F2=F2+(Y(I)-1.D00)**2*(1.D00+10.D00*(DSIN(PI*X(I+1)))**2)
1289:      ENDDO
1290:      Y(M)=1.D00+.25D00*(X(M)+1.D00)
1291:      F3=(Y(M)-1.D00)**2
1292:      Y(1)=1.D00+.25D00*(X(1)+1.D00)
1293:      F4=10.D00*(DSIN(PI*Y(1)))**2
1294:      F=(PI/M)*(F4+F2+F3)+F1
1295:      RETURN
1296:      END
1297: C -----
1298:      SUBROUTINE FUNCT13(M,F,X)
1299: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1300:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1301:      DIMENSION X(100)
1302:      DATA A,B,C /5.D00,100.D00,4.D00/
1303:      PI=4*DATAN(1.D00)
1304:      F=0.D00
1305: C      MIN F (1, 1, 1, ..., 4.7544 APPROX) = -1.15044 APPROX
1306: C      X(I)=1.D00 ! TO CHECK, TURN IT ALIVE
1307: C      X(M)=-4.7544 ! TO CHECK, TURN IT ALIVE
1308:      DO I=1,M
1309:      IF (DABS(X(I)).GT.50.D00) THEN
1310:      CALL RANDOM(RAND)
1311:      X(I)=(RAND-.5D00)*100.D00
1312:      ENDIF
1313:      ENDDO
1314:      F1=0.D00
1315:      DO I=1,M
1316:      XX=DABS(X(I))
1317:      U=0.D00
1318:      IF (XX.GT.A) U=B*(XX-A)**C
1319:      F1=F1+U
1320:      ENDDO
1321:      F2=0.D00
1322:      DO I=1,M-1
1323:      F2=F2+(X(I)-1.D00)**2*(1.D00+(DSIN(3*PI*X(I+1)))**2)
1324:      ENDDO
1325:      F3=(X(M)-1.D00)*(1.D00+(DSIN(2*PI*X(M)))**2)
1326:      F4=(DSIN(3*PI*X(1)))**2
1327:      F=0.1*(F4+F2+F3)+F1
1328:      RETURN
1329:      END
1330: C -----
1331:      SUBROUTINE FUNCT14(M,F,X)
1332: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1333: C      MIN F (-31.98, 31.98) = 0.998
1334:      PARAMETER (N=25,NN=2)
1335:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1336:      DIMENSION X(2), A(NN,N)
1337:      DATA (A(1,J),J=1,N) /-32.D00,-16.D00,0.D00,16.D00,32.D00,-32.D00,
1338:      & -16.D00,0.D00,16.D00,32.D00,-32.D00,-16.D00,0.D00,16.D00,32.D00,
1339:      & -32.D0,-16.D0,0.D0,16.D0,32.D0,-32.D0,-16.D0,0.D0,16.D0,32.D0/
1340:      DATA (A(2,J),J=1,N) /-32.D00,-32.D00,-32.D00,-32.D00,-32.D00,

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1341:      & -16.D00,-16.D00,-16.D00,-16.D00,-16.D00,0.D00,0.D00,0.D00,0.D00,
1342:      & 0.D00,16.D00,16.D00,16.D00,16.D00,16.D00,32.D00,32.D00,
1343:      & 32.D00,32.D00,32.D00/
1344:
1345:      F=0.D00
1346:      DO I=1,M
1347:      IF (DABS (X(I)) .GT.100.D00) THEN
1348:      CALL RANDOM(RAND)
1349:      X(I)=(RAND-.5D00)*200.D00
1350:      ENDIF
1351:      ENDDO
1352:      F1=0.D00
1353:      DO J=1,N
1354:      F2=0.D00
1355:      DO I=1,2
1356:      F2=F2+(X(I)-A(I,J))**6
1357:      ENDDO
1358:      F2=1.D00/(J+F2)
1359:      F1=F1+F2
1360:      ENDDO
1361:      F=1.D00/(0.002D00+F1)
1362:      RETURN
1363:      END
1364: C -----
1365:      SUBROUTINE FUNCT15(M,F,X)
1366: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1367: C      MIN F(.19, .19, .12, .14) = 0.3075
1368:      PARAMETER (N=11)
1369:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1370:      DIMENSION X(*), A(N),B(N)
1371:      DATA (A(I),I=1,N) /.1957D00,.1947D00,.1735D00,.16D00,.0844D00,
1372:      & .0627D00,.0456D00,.0342D00,.0323D00,.0235D00,.0246D00/
1373:      DATA (B(I),I=1,N) /0.25D00,0.5D00,1.D00,2.D00,4.D00,6.D00,8.D00,
1374:      & 10.D00,12.D00,14.D00,16.D00/
1375:      DO I=1,N
1376:      B(I)=1.D00/B(I)
1377:      ENDDO
1378:      F=0.D00
1379:      DO I=1,M
1380:      IF (DABS (X(I)) .GT.5.D00) THEN
1381:      CALL RANDOM(RAND)
1382:      X(I)=(RAND-.5D00)*10.D00
1383:      ENDIF
1384:      ENDDO
1385:      DO I=1,N
1386:      F1=X(1)*(B(I)**2+B(I)*X(2))
1387:      F2=B(I)**2+B(I)*X(3)+X(4)
1388:      F=F+(A(I)-F1/F2)**2
1389:      ENDDO
1390:      F=F*1000
1391:      RETURN
1392:      END
1393: C -----
1394:      SUBROUTINE LINPROG1(M,F,X)
1395: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM
1396: C      IN THIS PROBLEM : M = NO. OF DECISION VARIABLES = 2
1397: C      MIN F (2.390, 2.033) = -19.7253 APPROX
1398: C      MIN F = OVER J=1, M : DO SUM(A(1,J)*X(J)) SUBJECT TO CONSTRAINTS
1399: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=2
1400: C      . . . . .
1401: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=N
1402: C      ALL X(I) => 0
1403:      PARAMETER (N=3) ! N IS THE NO. OF CONSTRAINTS + 1
1404:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1405:      DIMENSION X(*),A(20,10),C(20),FF(20)
1406:      DATA (A(1,J),J=1,2),C(1)/4.D0,5.D0,0.0D0!/COEFF OF OBJ FUNCTION
1407:      DATA (A(2,J),J=1,2),C(2)/10.D0,3.D0,30D0!/COEFF OF 1ST CONSTRAINT

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1408:      DATA (A(3,J),J=1,2),C(3)/6.D0,20.D0,55.D0/!COEFF OF 2ND CONSTRAINT
1409: C
1410: C      USING ONLY NON-NEGATIVE VALUES OF X(I)
1411:      DO I=1,M
1412:      X(I)=DABS(X(I))
1413:      ENDDO
1414: C      EVALUATION OF OBJ FUNCTION AND CONSTRAINTS
1415:      DO I=1,N
1416:      FF(I)=0.D00
1417:      DO J=1,M
1418:      FF(I)=FF(I)+A(I,J)*X(J)
1419:      ENDDO
1420:      ENDDO
1421:      F=-FF(1) ! CHANGE OF SIGN FOR MINIMIZATION
1422: C      CHECK FOR SATISFYING OR VIOLATING THE CONSTRAINTS
1423:      DO I=2,N
1424:      FF(I)=FF(I)-C(I) ! SLACK
1425: C      PENALTY FOR CROSSING LIMITS
1426:      IF(FF(I).GT.0) F=F+(10+FF(I))**2
1427:      ENDDO
1428:      RETURN
1429:      END
1430: C
1431:      SUBROUTINE LINPROG2(M,F,X)
1432: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM
1433: C      IN THIS PROBLEM : M = NO. OF DECISION VARIABLES = 3
1434: C      MIN F (250, 625, 0) = -3250
1435: C      MIN F = OVER J=1, M : DO SUM(A(I,J)*X(J)) SUBJECT TO CONSTRAINTS
1436: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=2
1437: C      . . . . .
1438: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=N
1439: C      ALL X(I) => 0
1440:      PARAMETER (N=4) ! N IS THE NO. OF CONSTRAINTS + 1
1441:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1442:      DIMENSION X(*),A(20,10),C(20),FF(20)
1443:      DATA (A(1,J),J=1,3),C(1)/30.D0,40.D0,20.D0,0.0D0/! COEFF OF OBJ FUNCTION
1444:      DATA (A(2,J),J=1,3),C(2)/10.D0,12.D0,7.D0,10000.0D0/!COEFF OF 1ST CONSTRAINT
1445:      DATA (A(3,J),J=1,3),C(3)/7.D0,10.D0,8.D0,8000.0D0/! COEFF OF 2ND CONSTRAINT
1446:      DATA (A(4,J),J=1,3),C(4)/1.D0,1.D0,1.D0,1000.0D0/! COEFF OF 3RD CONSTRAINT
1447: C
1448: C      USING ONLY NON-NEGATIVE VALUES OF X(I)
1449:      DO I=1,M
1450:      X(I)=DABS(X(I))
1451:      ENDDO
1452: C      EVALUATION OF OBJ FUNCTION AND CONSTRAINTS
1453:      DO I=1,N
1454:      FF(I)=0.D00
1455:      DO J=1,M
1456:      FF(I)=FF(I)+A(I,J)*X(J)
1457:      ENDDO
1458:      ENDDO
1459:      F=-FF(1) ! CHANGE OF SIGN FOR MINIMIZATION
1460: C      CHECK FOR SATISFYING OR VIOLATING THE CONSTRAINTS
1461:      DO I=2,N
1462:      FF(I)=FF(I)-C(I) ! SLACK
1463: C      PENALTY FOR CROSSING LIMITS
1464:      IF(FF(I).GT.0.D00) F=F+(100.D00+FF(I))**2
1465:      ENDDO
1466:      RETURN
1467:      END
1468: C
1469:      SUBROUTINE HOUGEN(A,M,F)
1470:      PARAMETER (N=13,K=3)
1471:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1472:      DIMENSION X(N,K),RATE(N),A(*)
1473: C
1474: C      HOUGEN FUNCTION (HOUGEN-WATSON MODEL FOR REACTION KINATICS)

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1475: C      NO. OF PARAMETERS (A) TO ESTIMATE = 5 = M
1476: C      ----- BEST RESULTS -----
1477: C      FMIN =0.298900994 FOR A(1)=1.253031; A(2)=1.190943; A(3)=0.062798;
1478: C      A(4)=0.040063; A(5)=0.112453 BY ROSENBROCK & QUASI-NEWTON METHOD
1479: C      R=0.99945 = CORRELATION COEFF BETWEEN OBSERVED & EXPECTED RATE.
1480: C      next:fmin =0.298901 for x(1.25258611, 0.0627758222, 0.0400477567,
1481: C      0.112414812, 1.19137715) by de with ncross=0, pcross=0.9, fact=0.5
1482: C      THE NEXT BEST RESULTS GIVEN BY HOOKE-JEEVES & QUASI-NEWTON
1483: C      A(1)=2.475221;A(2)=0.599177; A(3)=0.124172; A(4)=0.083517
1484: C      A(5)=0.217886; SUM OF SQUARES OF DEVIATION = 0.318593458 = FMIN
1485: C      R=0.99941. MOST OF THE OTHER METHODS DO NOT PERFORM WELL.
1486: C      -----
1487: C      DATA X(1,1),X(1,2),X(1,3),RATE(1) /470,300,10,8.55/
1488: C      DATA X(2,1),X(2,2),X(2,3),RATE(2) /285,80,10,3.79/
1489: C      DATA X(3,1),X(3,2),X(3,3),RATE(3) /470,300,120,4.82/
1490: C      DATA X(4,1),X(4,2),X(4,3),RATE(4) /470,80,120,0.02/
1491: C      DATA X(5,1),X(5,2),X(5,3),RATE(5) /470,80,10,2.75/
1492: C      DATA X(6,1),X(6,2),X(6,3),RATE(6) /100,190,10,14.39/
1493: C      DATA X(7,1),X(7,2),X(7,3),RATE(7) /100,80,65,2.54/
1494: C      DATA X(8,1),X(8,2),X(8,3),RATE(8) /470,190,65,4.35/
1495: C      DATA X(9,1),X(9,2),X(9,3),RATE(9) /100,300,54,13/
1496: C      DATA X(10,1),X(10,2),X(10,3),RATE(10) /100,300,120,8.5/
1497: C      DATA X(11,1),X(11,2),X(11,3),RATE(11) /100,80,120,0.05/
1498: C      DATA X(12,1),X(12,2),X(12,3),RATE(12) /285,300,10,11.32/
1499: C      DATA X(13,1),X(13,2),X(13,3),RATE(13) /285,190,120,3.13/
1500: C      WRITE(*,1) ((X(I,J),J=1,K),RATE(I),I=1,N)
1501: C      1 FORMAT(4F8.2)
1502: C      DO J=1,M
1503: C      IF (DABS(A(J)).GT.5.D00) THEN
1504: C      CALL RANDOM(RAND)
1505: C      A(J)=(RAND-0.5D00)*10.D00
1506: C      ENDDIF
1507: C      ENDDO
1508: C      F=0.D00
1509: C      DO I=1,N
1510: C      D=1.D00
1511: C      DO J=1,K
1512: C      D=D+A(J+1)*X(I,J)
1513: C      ENDDO
1514: C      FX=(A(1)*X(I,2)-X(I,3)/A(M))/D
1515: C      FX=(A(1)*X(I,2)-X(I,3)/A(5))/(1.D00+A(2)*X(I,1)+A(3)*X(I,2)+
1516: C      A(4)*X(I,3))
1517: C      F=F+(RATE(I)-FX)**2
1518: C      ENDDO
1519: C      RETURN
1520: C      END
1521: C      -----
1522: C      SUBROUTINE GIUNTA(M,X,F)
1523: C      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1524: C      DIMENSION X(*)
1525: C      GIUNTA FUNCTION
1526: C      X(I) = -1 TO 1; M=2
1527: C      DO I=1,M
1528: C      IF (DABS(X(I)).GT.1.D00) THEN
1529: C      CALL RANDOM(RAND)
1530: C      X(I)=(RAND-0.5D00)*2.D00
1531: C      ENDDIF
1532: C      ENDDO
1533: C      C=16.D00/15.D00
1534: C      F=DSIN(C*X(1)-1.D0)+DSIN(C*X(1)-1.D0)**2+DSIN(4*(C*X(1)-1.D0))/50+
1535: C      &DSIN(C*X(2)-1.D0)+DSIN(C*X(2)-1.D0)**2+DSIN(4*(C*X(2)-1.D0))/50+.6
1536: C      RETURN
1537: C      END
1538: C      -----
1539: C      SUBROUTINE EGGHOLD(M,X,F)
1540: C      EGG HOLDER FUNCTION
1541: C      IMPLICIT DOUBLE PRECISION (A-H, O-Z)

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1542:     DIMENSION X(*)
1543:     DO I=1,M
1544:       IF (DABS(X(I)) .GT. 512.D00) THEN
1545:         CALL RANDOM(RAND)
1546:         X(I)=(RAND-0.5D00)*1024.D00
1547:       ENDIF
1548:     ENDDO
1549:     F=0.D00
1550:     DO I=1,M-1
1551:       F1=-(X(I+1)+47.D00)
1552:       F2=DSIN( DSQRT( DABS( X(I+1)+X(I)/2+47.D00 ) ) )
1553:       F3=DSIN( DSQRT( DABS( X(I)-(X(I+1)+47.D00) ) ) )
1554:       F4=-X(I)
1555:       F=F+ F1*F2+F3*F4
1556:     ENDDO
1557:     RETURN
1558:   END
1559: C -----
1560:   SUBROUTINE TRID(M,X,F)
1561: C   TRID FUNCTION
1562:   IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1563:   DIMENSION X(*)
1564:   F1=0.D00
1565:   F2=0.D00
1566:   DO I=1, M
1567:     F1=F1+(X(I)-1.D00)**2
1568:   ENDDO
1569:   DO I=2, M
1570:     F2=F2+X(I)*X(I-1)
1571:   ENDDO
1572:   F=F1-F2
1573:   RETURN
1574:   END
1575: C -----
1576:   SUBROUTINE GRIEWANK(M,X,F)
1577:   IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1578:   DIMENSION X(*)
1579: C   GRIEWANK FUNCTION
1580:   F1=0.D00
1581:   F2=1.0D00
1582:   DO I=1,M
1583:     F1=F1+X(I)**2
1584:     FI=DFLOAT(I)
1585:     F2=F2*DCOS(X(I)/DSQRT(FI))
1586:   ENDDO
1587:   F=F1/4000.D00-F2+1.0D00
1588:   RETURN
1589:   END
1590: C -----
1591:   SUBROUTINE WEIERSTRASS(M,X,F)
1592:   IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1593:   DIMENSION X(*)
1594:   PI=4*DATAN(1.D00)
1595: C   WEIERSTRASS FUNCTION m variable fmin (0, 0, ..., 0)= 0
1596:   DATA AX,BX,KMAX/0.5D00,3.D00,20/
1597:   DO I=1,M
1598:     IF (DABS(X(I)) .GT. 0.5D00) THEN
1599:       CALL RANDOM(RAND)
1600:       X(I)=RAND-0.5D00
1601:     ENDIF
1602:   ENDDO
1603:   f1=0.D00
1604:   f2=0.D00
1605:   DO I=1,M
1606:     S=0.D00
1607:     DO KK=1,KMAX+1
1608:       K=KK-1

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1609:         S=S+(AX**K*DCOS(2*PI*BX**K*(X(I)+0.5D00)))
1610:         ENDDO
1611:         F1=F1+S
1612:         ENDDO
1613:         DO KK=1, KMAX+1
1614:         K=KK-1
1615:         F2=F2+(AX**K*DCOS(2*PI*BX**K*0.5D00))
1616:         ENDDO
1617:         F=F1-M*F2
1618:         RETURN
1619:         END
-----
1620: C
1621: SUBROUTINE LEVY3(M, X, F)
1622: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1623: DIMENSION X(*)
1624: C LEVY # 3 (LEVY ET AL. 1981) -----
1625:         DO I=1, M
1626:         IF (DABS(X(I)) .GT. 10.D00) THEN
1627:         CALL RANDOM(RAND)
1628:         X(I)=(RAND-0.5D00)*20
1629:         ENDIF
1630:         ENDDO
1631:         F1=0.0D+00
1632:         F2=0.0D+00
1633:         DO I=1, 5
1634:         F1=F1+(I*DCOS((I-1)*X(1)+I))
1635:         F2=F2+(I*DCOS((I+1)*X(2)+I))
1636:         ENDDO
1637:         F=F1*F2
1638:         RETURN
1639:         END
-----
1640: C
1641: SUBROUTINE LEVY5(M, X, F)
1642: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1643: DIMENSION X(*)
1644:         F1=0.0D+00
1645:         F2=0.0D+00
1646:         DO I=1, 5
1647:         F1=F1+(I*DCOS((I-1)*X(1)+I))
1648:         F2=F2+(I*DCOS((I+1)*X(2)+I))
1649:         ENDDO
1650:         F3=(X(1)+1.42513D+00)**2
1651:         F4=(X(2)+0.80032D+00)**2
1652:         F=(F1*F2) + (F3+F4)
1653:         RETURN
1654:         END
-----
1655: C
1656: SUBROUTINE LEVY8(M, X, F)
1657: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1658: DIMENSION X(*), Y(3)
1659: PI=4*DATAN(1.D00)
1660: C LEVY # 8 FUNCTION -----
1661:         DO I=1, 3
1662:         Y(I)=1.D+00+(X(I)-1.D+00)/4.D+00
1663:         ENDDO
1664:         F1=DSIN(PI*Y(1))**2
1665:         F3=(Y(3)-1.D+00)**2
1666:         F2=0.D+00
1667:         DO I=1, 2
1668:         F2=F2+((Y(I)-1.D+00)**2)*(1.D+00+10.D+00*(DSIN(PI*Y(I+1))))**2)
1669:         ENDDO
1670:         F=F1+F2+F3
1671:         RETURN
1672:         END
-----
1673: C
1674: SUBROUTINE RASTRIGIN(M, X, F)
1675: IMPLICIT DOUBLE PRECISION (A-H, O-Z)

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1676:     DIMENSION X(*)
1677:     PI=4*DATAN(1.D00)
1678: C     RASTRIGIN'S FUNCTION
1679:     F=0.D00
1680:     DO I=1,M
1681:     F=F+ X(I)**2 -10*DCOS(2*PI*X(I)) + 10.D00
1682:     ENDDO
1683:     RETURN
1684:     END
1685: C     -----
1686:     SUBROUTINE ACKLEY(M,X,F)
1687: C     ACKLEY FUNCTION
1688:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1689:     DIMENSION X(*)
1690:     PI=4*DATAN(1.D00)
1691:     F=20.D00+DEXP(1.D00)
1692:     DO I=1,M
1693:     IF(X(I).LT.-15.D00 .OR. X(I).GT.30.D00) THEN
1694:     CALL RANDOM(RAND)
1695:     X(I)=(RAND-0.5D00)*90 -15.D00
1696:     ENDIF
1697:     ENDDO
1698:     F1=0.D00
1699:     F2=0.D00
1700:     DO I=1,M
1701:     F1=F1+X(I)**2
1702:     F2=F2+DCOS(2*PI*X(I))
1703:     ENDDO
1704:     F1=-20*DEXP(-0.2D00*DSQRT(F1/M))
1705:     F2=-DEXP(F2/M)
1706:     F=F+F1+F2
1707:     RETURN
1708:     END
1709: C     -----
1710:     SUBROUTINE MICHALEWICZ(M,X,F)
1711:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1712:     DIMENSION X(*)
1713: C     MICHALEWICZ FUNCTION [ 0 <= X(I) <= PI ] MP IS A PARAMETER
1714: C     min f= -1.8013 (M=2); -4.6877 (M=5); -6.6809 (M=7); -9.6602 (M=10)
1715: C     -19.6370 (M=20); -29.6309 (M=30); -49.6248 (M=50), ETC
1716:     MP=10 ! SET IT TO THE DESIRED VALUE
1717:     PI=4*DATAN(1.D00)
1718:     DO I=1,M
1719:     IF(X(I).LT.0.D00 .OR. X(I).GT.PI) THEN
1720:     CALL RANDOM(RAND)
1721:     X(I)=RAND*PI
1722:     ENDIF
1723:     ENDDO
1724:     F=0.D00
1725:     DO I=1,M
1726:     F=F-DSIN(X(I))*(DSIN(I*X(I)**2/PI))**(2*MP)
1727:     ENDDO
1728:     RETURN
1729:     END
1730: C     -----
1731:     SUBROUTINE SCHWEFEL(M,X,F)
1732: C     SCHWEFEL FUNCTION
1733:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1734:     DIMENSION X(*)
1735:     DO I=1,M
1736:     IF(DABS(X(I)).GT.500) THEN
1737:     CALL RANDOM(RAND)
1738:     X(I)=(RAND-0.5D00)*1000
1739:     ENDIF
1740:     ENDDO
1741:     F=0.D00
1742:     DO I=1,M

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1743:      F=F+ X(I)*DSIN(DSQRT(DABS(X(I))))
1744:      ENDDO
1745:      F=418.9829D00*M - F
1746:      RETURN
1747:      END
1748: C -----
1749:      SUBROUTINE SHUBERT(M,X,F)
1750: C      SHUBERT FUNCTION
1751:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1752:      DIMENSION X(*)
1753:      DO I=1,M
1754:      IF(DABS(X(I)).GT.10.D00) THEN
1755:      CALL RANDOM(RAND)
1756:      X(I)=(RAND-0.5D00)*20
1757:      ENDIF
1758:      ENDDO
1759:      F1=0.D00
1760:      F2=0.D00
1761:      DO I=1,5
1762:      F1=F1+I*DCOS((I+1.D00)*X(1)+I)
1763:      F2=F2+I*DCOS((I+1.D00)*X(2)+I)
1764:      ENDDO
1765:      F=F1*F2
1766:      RETURN
1767:      END
1768: C -----
1769:      SUBROUTINE DIXPRICE(M,X,F)
1770: C      DIXON & PRICE FUNCTION
1771:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1772:      DIMENSION X(*)
1773:      DO I=1,M
1774:      IF(DABS(X(I)).GT.10.D00) THEN
1775:      CALL RANDOM(RAND)
1776:      X(I)=(RAND-0.5D00)*20
1777:      ENDIF
1778:      ENDDO
1779:      F=0.D00
1780:      DO I=2, M
1781:      F=F + I*(2*X(I)**2-X(I-1))**2
1782:      ENDDO
1783:      F=F+(X(1)-1.D00)**2
1784:      RETURN
1785:      END
1786: C -----
1787:      SUBROUTINE SHEKEL(M,X,F)
1788: C      SHEKEL FUNCTION FOR TEST OF GLOBAL OPTIMIZATION METHODS
1789:      PARAMETER(NROW=10,NCOL=4, NR=9)! NR MAY BE 2 TO 10
1790:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1791:      DIMENSION A(NROW,NCOL),C(NROW),X(*)
1792:      DATA ((A(I,J),J=1,NCOL),I=1,NROW)/4.,4.,4.,4.,1.,1.,1.,1.,8.,8.,
1793: & 8.,8.,6.,6.,6.,6.,3.,7.,3.,7.,2.,9.,2.,9.,5.,5.,3.,3.,8.,1.,8.,
1794: & 1.,6.,2.,6.,2.,7.,3.6D00,7.,3.6D00/
1795:      DATA (C(I),I=1,NROW)/0.1D00,0.2D00,0.2D00,0.4D00,0.4D00,0.6D00,
1796: & 0.3D00,0.7D00,0.5D00,0.5D00/
1797:      F=0.D00
1798:      DO I=1,NR
1799:      S=0.D00
1800:      DO J=1,M
1801:      S=S+(X(J)-A(I,J))**2
1802:      ENDDO
1803:      F=F-1.D00/(S+C(I))
1804:      ENDDO
1805:      RETURN
1806:      END
1807: C -----
1808:      SUBROUTINE PAVIANI(M,X,F)
1809: C      PAVIANI FUNCTION : MIN F(9.3502,...,9.3502)=45.77847 APPROX

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1810: C      IN THE DOMAIN  $2 \leq X(I) \leq 10$  FOR  $I=1,2,\dots,10$ .
1811:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1812:      DIMENSION X(*)
1813:      DO I=1,M
1814:      IF (X(I) .LE. 2.D00 .OR. X(I) .GE. 10.D00) THEN
1815:      CALL RANDOM(RAND)
1816:      X(I)=RAND*8+2.D00
1817:      ENDIF
1818:      ENDDO
1819:      F1=0.D00
1820:      F2=1.D00
1821:      DO I=1,M
1822:      F1=F1+ DLOG(X(I)-2.D00)**2+DLOG(10.D00-X(I))**2
1823:      F2=F2*X(I)
1824:      ENDDO
1825:      F=F1-F2**0.2
1826:      RETURN
1827:      END
1828: C      -----
1829:      SUBROUTINE BRANIN1(M,X,F)
1830: C      BRANIN FUNCTION #1 MIN F (1, 0) = 0
1831:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1832:      DIMENSION X(*)
1833:      PI=4*DATAN(1.D00)
1834:      DO I=1,M
1835:      IF (DABS(X(I)) .GT. 10.D00) THEN
1836:      CALL RANDOM(RAND)
1837:      X(I)=(RAND-0.5D00)*20
1838:      ENDIF
1839:      ENDDO
1840:      F=(1.D00-2*X(2)+DSIN(4*PI*X(2))/2.D00-X(1))**2+(X(2)-
1841: & DSIN(2*PI*X(1))/2.D00)**2
1842:      RETURN
1843:      END
1844: C      -----
1845:      SUBROUTINE BRANIN2(M,X,F)
1846: C      BRANIN FUNCTION #2 MIN F (3.1416, 2.25)= 0.397887 APPROX
1847:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1848:      DIMENSION X(*)
1849:      PI=4*DATAN(1.D00)
1850:      IF (X(1) .LT. -5.D00 .OR. X(1) .GT. 10.D00) THEN
1851:      CALL RANDOM(RAND)
1852:      X(1)=RAND*15-5.D00
1853:      ENDIF
1854:      IF (X(2) .LT. 0.D00 .OR. X(2) .GT. 15.D00) THEN
1855:      CALL RANDOM(RAND)
1856:      X(2)=RAND*15
1857:      ENDIF
1858:      F=(X(2)-5.D00*X(1))**2/(4*PI**2)+5*X(1)/PI-6.D00)**2 +
1859: & 10*(1.D00-1.D00/(8*PI))*DCOS(X(1))+10.D00
1860:      RETURN
1861:      END
1862: C      -----
1863:      SUBROUTINE BOHACHEVSKY1(M,X,F)
1864: C      BOHACHEVSKY FUNCTION #1 : MIN F (0, 0) = 0
1865:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1866:      DIMENSION X(*)
1867:      PI=4*DATAN(1.D00)
1868:      DO I=1,M
1869:      IF (DABS(X(I)) .GT. 100.D00) THEN
1870:      CALL RANDOM(RAND)
1871:      X(I)=(RAND-0.5D00)*200
1872:      ENDIF
1873:      ENDDO
1874:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1))-0.4D00*DCOS(4*PI*X(2))
1875: & +0.7D00
1876:      RETURN

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1877:      END
1878: C -----
1879:      SUBROUTINE BOHACHEVSKY2(M,X,F)
1880: C BOHACHEVSKY FUNCTION #2 : MIN F (0, 0) = 0
1881:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1882:      DIMENSION X(*)
1883:      PI=4*DATAN(1.D00)
1884:      DO I=1,M
1885:      IF (DABS(X(I)).GT.100.D00) THEN
1886:      CALL RANDOM(RAND)
1887:      X(I)=(RAND-0.5D00)*200
1888:      ENDIF
1889:      ENDDO
1890:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1))*DCOS(4*PI*X(2))+0.3D00
1891:      RETURN
1892:      END
1893: C -----
1894:      SUBROUTINE BOHACHEVSKY3(M,X,F)
1895: C BOHACHEVSKY FUNCTION #3 : MIN F (0, 0) = 0
1896:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1897:      DIMENSION X(*)
1898:      PI=4*DATAN(1.D00)
1899:      DO I=1,M
1900:      IF (DABS(X(I)).GT.100.D00) THEN
1901:      CALL RANDOM(RAND)
1902:      X(I)=(RAND-0.5D00)*200
1903:      ENDIF
1904:      ENDDO
1905:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1)+4*PI*X(2))+0.3D00
1906:      RETURN
1907:      END
1908: C -----
1909:      SUBROUTINE EASOM(M,X,F)
1910: C EASOM FUNCTION : 2-VARIABLES, MIN F (PI, PI) = -1.
1911:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1912:      DIMENSION X(*)
1913:      PI=4*DATAN(1.D00)
1914:      DO I=1,M
1915:      IF (DABS(X(I)).GT.100.D00) THEN
1916:      CALL RANDOM(RAND)
1917:      X(I)=(RAND-0.5D00)*200
1918:      ENDIF
1919:      ENDDO
1920:      F=-DCOS(X(1))*DCOS(X(2))*DEXP(-(X(1)-PI)**2 -(X(2)-PI)**2)
1921:      RETURN
1922:      END
1923: C -----
1924:      SUBROUTINE ROSENBROCK(M,X,F)
1925: C ROSENBROCK FUNCTION : M VARIABLE; MIN F (1, 1, ..., 1)=0
1926:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1927:      DIMENSION X(*)
1928:      DO I=1,M
1929:      IF (X(I).LT.-5.D00 .OR. X(I).GT.10.D00) THEN
1930:      CALL RANDOM(RAND)
1931:      X(I)=RAND*15-5.D00
1932:      ENDIF
1933:      ENDDO
1934:      F=0.D00
1935:      DO I=1,M-1
1936:      F=F+ (100.D00*(X(I+1)-X(I)**2)**2 + (X(I)-1.D00)**2)
1937:      ENDDO
1938:      RETURN
1939:      END
1940: C -----
1941:      SUBROUTINE CROSSLEG(M,X,F)
1942:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1943:      DIMENSION X(*)

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1944: C      CROSS-LEGGED TABLE FUNCTION ; -10<= X(I) <=10; M=2
1945: C      MIN F(0 , X ) OR F(X, 0) = -1.
1946:      PI=4*DATAN(1.D00)
1947:      DO I=1,M
1948:          IF( DABS(X(I)) .GT.10.D00) THEN
1949:              CALL RANDOM(RAND)
1950:              X(I)=(RAND-0.5D00)*20
1951:          ENDIF
1952:      ENDDO
1953:      F=- (DABS(DSIN(X(1)) *DSIN(X(2)) *DEXP(DABS(100.D00-(DSQRT
1954: & (X(1)**2+X(2)**2)/PI))))+1.D00)**(-.1)
1955:      RETURN
1956:      END
1957: C      -----
1958:      SUBROUTINE CROSS(M,X,F)
1959:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1960:      DIMENSION X(*)
1961: C      CROSS FUNCTION ; -10<= X(I) <=10; M=2;
1962: C      MIN F(A, B)=0 APPROX; A, B=1.3494 APPROX OF EITHER SIGN (+ OR -)
1963:      PI=4*DATAN(1.D00)
1964:      DO I=1,M
1965:          IF( DABS(X(I)) .GT.10.D00) THEN
1966:              CALL RANDOM(RAND)
1967:              X(I)=(RAND-0.5D00)*20
1968:          ENDIF
1969:      ENDDO
1970:      F=(DABS(DSIN(X(1)) *DSIN(X(2)) *DEXP(DABS(100.D00-(DSQRT
1971: & (X(1)**2+X(2)**2)/PI))))+1.D00)**(-.1)
1972:      RETURN
1973:      END
1974: C      -----
1975:      SUBROUTINE CROSSINTRAY(M,X,F)
1976:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1977:      DIMENSION X(*)
1978: C      CROSS IN TRAY FUNCTION ; -10<= X(I) <=10; M=2;
1979: C      MIN F(A, B)=-20626.1218 APPROX; A, B=1.3494 APPROX OF EITHER SIGN
1980:      PI=4*DATAN(1.D00)
1981:      DO I=1,M
1982:          IF( DABS(X(I)) .GT.10.D00) THEN
1983:              CALL RANDOM(RAND)
1984:              X(I)=(RAND-0.5D00)*20
1985:          ENDIF
1986:      ENDDO
1987:      F=- (DABS(DSIN(X(1)) *DSIN(X(2)) *DEXP(DABS(100.D00-(DSQRT
1988: & (X(1)**2+X(2)**2)/PI))))+1.D00)**(.1)
1989:      RETURN
1990:      END
1991: C      -----
1992:      SUBROUTINE CROWNEDCROSS(M,X,F)
1993:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1994:      DIMENSION X(*)
1995: C      CROWNED CROSS FUNCTION ; -10<= X(I) <=10; M=2; MIN F = 1
1996:      PI=4*DATAN(1.D00)
1997:      DO I=1,M
1998:          IF( DABS(X(I)) .GT.10.D00) THEN
1999:              CALL RANDOM(RAND)
2000:              X(I)=(RAND-0.5D00)*20
2001:          ENDIF
2002:      ENDDO
2003:      F=(DABS(DSIN(X(1)) *DSIN(X(2)) *DEXP(DABS(100.D00-
2004: & (DSQRT(X(1)**2+X(2)**2)/PI))))+1.D00)**(.1)
2005:      RETURN
2006:      END
2007: C      -----
2008:      SUBROUTINE TTHOLDER(M,X,F)
2009:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2010:      DIMENSION X(*)

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2011: C      TEST-TUBE HOLDER FUNCTION ; -10<= X(I) <=10; M=2;
2012: C      MIN F ([+/-]1.5706, 0) = -10.8723
2013:      PI=4*DATAN(1.D00)
2014:      DO I=1,M
2015:          IF ( DABS (X(I)) .GT. 10.D00) THEN
2016:              CALL RANDOM(RAND)
2017:              X(I)=(RAND-0.5D00)*20
2018:          ENDIF
2019:      ENDDO
2020:      F=-4*DABS (DSIN (X(1)) *DCOS (X(2)) *DEXP (DABS (DCOS ((X(1)**2+X(2)**2)/
2021: & 200))))
2022:      RETURN
2023:      END
2024: C      -----
2025:      SUBROUTINE HOLDERTABLE(M,X,F)
2026:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2027:      DIMENSION X(*)
2028: C      HOLDER-TABLE FUNCTION ; -10<= X(I) <=10; M=2;
2029: C      MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -26.92034 APPROX
2030:      PI=4*DATAN(1.D00)
2031:      DO I=1,M
2032:          IF ( DABS (X(I)) .GT. 10.D00) THEN
2033:              CALL RANDOM(RAND)
2034:              X(I)=(RAND-0.5D00)*20
2035:          ENDIF
2036:      ENDDO
2037:      F=-DABS (DCOS (X(1)) *DCOS (X(2)) *DEXP (DABS (1.D00- (DSQRT (X(1)**2+
2038: & X(2)**2)/PI))))
2039:      RETURN
2040:      END
2041: C      -----
2042:      SUBROUTINE CARROMTABLE(M,X,F)
2043:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2044:      DIMENSION X(*)
2045: C      CARROM-TABLE FUNCTION ; -10<= X(I) <=10; M=2;
2046: C      MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -24.15682 APPROX
2047:      PI=4*DATAN(1.D00)
2048:      DO I=1,M
2049:          IF ( DABS (X(I)) .GT. 10.D00) THEN
2050:              CALL RANDOM(RAND)
2051:              X(I)=(RAND-0.5D00)*20
2052:          ENDIF
2053:      ENDDO
2054:      F=-1.D00/30*(DCOS (X(1)) *DCOS (X(2)) *DEXP (DABS (1.D00-
2055: & (DSQRT (X(1)**2 + X(2)**2)/PI))))**2
2056:      RETURN
2057:      END
2058: C      -----
2059:      SUBROUTINE PENHOLDER(M,X,F)
2060:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2061:      DIMENSION X(*)
2062: C      PENHOLDER FUNCTION ; -11<= X(I) <=11; M=2;
2063: C      MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -0.963535 APPROX
2064:      PI=4*DATAN(1.D00)
2065:      DO I=1,M
2066:          IF ( DABS (X(I)) .GT. 11.D00) THEN
2067:              CALL RANDOM(RAND)
2068:              X(I)=(RAND-0.5D00)*22
2069:          ENDIF
2070:      ENDDO
2071:      F=-DEXP (- (DABS (DCOS (X(1)) *DCOS (X(2)) *DEXP (DABS (1.D0- (DSQRT
2072: & (X(1)**2+X(2)**2)/PI)))) ** (-1)))
2073:      RETURN
2074:      END
2075: C      -----
2076:      SUBROUTINE BIRD(M,X,F)
2077:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)

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2078:      DIMENSION X(*)
2079: C      BIRD FUNCTION ; -2PI<= X(I) <=2PI; M=2;
2080: C      MIN F (4.70104, 3.15294) APPROX = -106.764537 APPROX OR
2081: C      MIN F (-1.58214, -3.13024) APPROX = -106.764537 APPROX
2082:      PI=4*DATAN(1.D00)
2083:      DO I=1,M
2084:      IF( DABS(X(I)) .GT. 2*PI) THEN
2085:      CALL RANDOM(RAND)
2086:      X(I)=(RAND-0.5D00)*4*PI
2087:      ENDIF
2088:      ENDDO
2089:      F=(DSIN(X(1))*DEXP((1.D00-DCOS(X(2)))**2) +
2090: & DCOS(X(2))*DEXP((1.D00-DSIN(X(1)))**2)+(X(1)-X(2))**2
2091:      RETURN
2092:      END
2093: C      -----
2094:      SUBROUTINE CHICHINADZE(M,X,F)
2095:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2096:      DIMENSION X(*)
2097: C      CHICHINADZE FUNCTION : -30 <=X(I)<= 30; M=2
2098: C      MIN F (5.901329, 0.5) = -43.3158621
2099:      PI=4*DATAN(1.D00)
2100:      DO I=1,M
2101:      IF( DABS(X(I)) .GT. 30) THEN
2102:      CALL RANDOM(RAND)
2103:      X(I)=(RAND-0.5D00)*60
2104:      ENDIF
2105:      ENDDO
2106:      F=X(1)**2-12*X(1)+11.D00+10*DCOS(PI*X(1)/2)+8*DSIN(5*PI*X(1))-
2107: & (1.D00/DSQRT(5.D00))*DEXP(-(X(2)-0.5D00)**2/2)
2108:      RETURN
2109:      END
2110: C      -----
2111:      SUBROUTINE MCCORMICK(M,X,F)
2112:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2113:      DIMENSION X(*)
2114: C      MCCORMICK FUNCTION : -1.5<= X(1)<=4; -3<=X(2)<=4 ; M=2
2115: C      MIN F (-0.54719755, -1.54719755) = -1.913223 APPROX
2116:      IF(X(1) .LT. -1.5D00 .OR. X(1) .GT. 4.D00) THEN
2117:      CALL RANDOM(RAND)
2118:      X(1)=RAND*5.5D00-1.5D00
2119:      ENDIF
2120:      IF(X(2) .LT. -3.D00 .OR. X(2) .GT. 4.D00) THEN
2121:      CALL RANDOM(RAND)
2122:      X(2)=RAND*7.D00-3.D00
2123:      ENDIF
2124:      F=DSIN(X(1)+X(2))+(X(1)-X(2))**2-1.5*X(1)+2.5*X(2)+1.D00
2125:      RETURN
2126:      END
2127: C      =====
2128: C      ===== REPULSIVE PARTICLE SWARM METHOD =====
2129:      SUBROUTINE RPS(M,BST,FMINIM)
2130: C      PROGRAM TO FIND GLOBAL MINIMUM BY REPULSIVE PARTICLE SWARM METHOD
2131: C      WRITTEN BY SK MISHRA, DEPT. OF ECONOMICS, NEHU, SHILLONG (INDIA)
2132: C      -----
2133:      PARAMETER (N=100,NN=50,MX=50,NSTEP=11,ITRN=10000,NSIGMA=1,ITOP=3)
2134:      PARAMETER (NPRN=500) ! ECHOS RESULTS AT EVERY 500 TH ITERATION
2135: C      PARAMETER (N=50,NN=25,MX=100,NSTEP=9,ITRN=10000,NSIGMA=1,ITOP=3)
2136: C      PARAMETER (N=100,NN=15,MX=100,NSTEP=9,ITRN=10000,NSIGMA=1,ITOP=3)
2137: C      IN CERTAIN CASES THE ONE OR THE OTHER SPECIFICATION WORKS BETTER
2138: C      DIFFERENT SPECIFICATIONS OF PARAMETERS MAY SUIT DIFFERENT TYPES
2139: C      OF FUNCTIONS OR DIMENSIONS - ONE HAS TO DO SOME TRIAL AND ERROR
2140: C      -----
2141: C      N = POPULATION SIZE. IN MOST OF THE CASES N=30 IS OK. ITS VALUE
2142: C      MAY BE INCREASED TO 50 OR 100 TOO. THE PARAMETER NN IS THE SIZE OF
2143: C      RANDOMLY CHOSEN NEIGHBOURS. 15 TO 25 (BUT SUFFICIENTLY LESS THAN
2144: C      N) IS A GOOD CHOICE. MX IS THE MAXIMAL SIZE OF DECISION VARIABLES.

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2145: C      IN F(X1, X2, ..., XM) M SHOULD BE LESS THAN OR EQUAL TO MX. ITRN IS
2146: C      THE NO. OF ITERATIONS. IT MAY DEPEND ON THE PROBLEM. 200 (AT LEAST)
2147: C      TO 500 ITERATIONS MAY BE GOOD ENOUGH. BUT FOR FUNCTIONS LIKE
2148: C      ROSENBROCKOR GRIEWANK OF LARGE SIZE (SAY M=30) IT IS NEEDED THAT
2149: C      ITRN IS LARGE, SAY 5000 OR EVEN 10000.
2150: C      SIGMA INTRODUCES PERTURBATION & HELPS THE SEARCH JUMP OUT OF LOCAL
2151: C      OPTIMA. FOR EXAMPLE : RASTRIGIN FUNCTION OF DMENSION 30 OR LARGER
2152: C      NSTEP DOES LOCAL SEARCH BY TUNNELLING AND WORKS WELL BETWEEN 5 AND
2153: C      15, WHICH IS MUCH ON THE HIGHER SIDE.
2154: C      ITOP <=1 (RING); ITOP=2 (RING AND RANDOM); ITOP=>3 (RANDOM)
2155: C      NSIGMA=0 (NO CHAOTIC PERTURBATION); NSIGMA=1 (CHAOTIC PERTURBATION)
2156: C      NOTE THAT NSIGMA=1 NEED NOT ALWAYS WORK BETTER (OR WORSE)
2157: C      SUBROUTINE FUNC( ) DEFINES OR CALLS THE FUNCTION TO BE OPTIMIZED.
2158: C      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
2159: C      COMMON /RNDM/IU, IV
2160: C      COMMON /KFF/KF, NFCALL
2161: C      INTEGER IU, IV
2162: C      CHARACTER *70 FTIT
2163: C      DIMENSION X(N, MX), V(N, MX), A(MX), VI(MX)
2164: C      DIMENSION XX(N, MX), F(N), V1(MX), V2(MX), V3(MX), V4(MX), BST(MX)
2165: C      A1 A2 AND A3 ARE CONSTANTS AND W IS THE INERTIA WEIGHT.
2166: C      OCCASIONALLY, TINKERING WITH THESE VALUES, ESPECIALLY A3, MAY BE
2167: C      NEEDED.
2168: C      DATA A1, A2, A3, W, SIGMA, EPSI /.5D0, .5D0, 5.D-04, .5D00, 1.D-03, 1.D-08/
2169: C      -----
2170: C      CALL SUBROUTINE FOR CHOOSING FUNCTION (KF) AND ITS DIMENSION (M)
2171: C      CALL FSELECT(KF, M, FTIT)
2172: C      -----
2173: C      GGBEST=1.D30 ! TO BE USED FOR TERMINATION CRITERION
2174: C      LCOUNT=0
2175: C      NFCALL=0
2176: C      WRITE(*, *) '4-DIGITS SEED FOR RANDOM NUMBER GENERATION'
2177: C      WRITE(*, *) 'A FOUR-DIGIT POSITIVE ODD INTEGER, SAY, 1171'
2178: C      READ(*, *) IU
2179: C      DATA FMIN /1.0E30/
2180: C      GENERATE N-SIZE POPULATION OF M-TUPLE PARAMETERS X(I, J) RANDOMLY
2181: C      DO I=1, N
2182: C          DO J=1, M
2183: C              CALL RANDOM(RAND)
2184: C              X(I, J) = (RAND-0.5D00) * 2000
2185: C      WE GENERATE RANDOM(-5, 5). HERE MULTIPLIER IS 10. TINKERING IN SOME
2186: C      CASES MAY BE NEEDED
2187: C          ENDDO
2188: C          F(I) = 1.0D30
2189: C      ENDDO
2190: C      INITIALISE VELOCITIES V(I) FOR EACH INDIVIDUAL IN THE POPULATION
2191: C      DO I=1, N
2192: C          DO J=1, M
2193: C              CALL RANDOM(RAND)
2194: C              V(I, J) = (RAND-0.5D+00)
2195: C          V(I, J) = RAND
2196: C      ENDDO
2197: C      ENDDO
2198: C      DO 100 ITER=1, ITRN
2199: C      LET EACH INDIVIDUAL SEARCH FOR THE BEST IN ITS NEIGHBOURHOOD
2200: C          DO I=1, N
2201: C              DO J=1, M
2202: C                  A(J) = X(I, J)
2203: C                  VI(J) = V(I, J)
2204: C              ENDDO
2205: C              CALL LSRCH(A, M, VI, NSTEP, FI)
2206: C              IF(FI, LT, F(I)) THEN
2207: C                  F(I) = FI
2208: C                  DO IN=1, M
2209: C                      BST(IN) = A(IN)
2210: C                  ENDDO
2211: C      F(I) CONTAINS THE LOCAL BEST VALUE OF FUNCTION FOR ITH INDIVIDUAL

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2212: C      XX(I,J) IS THE M-TUPLE VALUE OF X ASSOCIATED WITH LOCAL BEST F(I)
2213:         DO J=1,M
2214:         XX(I,J)=A(J)
2215:         ENDDO
2216:         ENDDIF
2217:     ENDDO
2218: C      NOW LET EVERY INDIVIDUAL RANDOMLY CONSULT NN(<<N) COLLEAGUES AND
2219: C      FIND THE BEST AMONG THEM
2220: DO I=1,N
2221: C -----
2222: IF (ITOP.GE.3) THEN
2223: C      RANDOM TOPOLOGY *****
2224: C      CHOOSE NN COLLEAGUES RANDOMLY AND FIND THE BEST AMONG THEM
2225:     BEST=1.0D30
2226:     DO II=1,NN
2227:         CALL RANDOM(RAND)
2228:         NF=INT(RAND*N)+1
2229:         IF (BEST.GT.F(NF)) THEN
2230:             BEST=F(NF)
2231:             NFBEST=NF
2232:         ENDDIF
2233:     ENDDO
2234: ENDDIF
2235: C -----
2236: IF (ITOP.EQ.2) THEN
2237: C      RING + RANDOM TOPOLOGY *****
2238: C      REQUIRES THAT THE SUBROUTINE NEIGHBOR IS TURNED ALIVE
2239:     BEST=1.0D30
2240:     CALL NEIGHBOR(I,N,I1,I3)
2241:     DO II=1,NN
2242:         IF (II.EQ.1) NF=I1
2243:         IF (II.EQ.2) NF=I
2244:         IF (II.EQ.3) NF=I3
2245:         IF (II.GT.3) THEN
2246:             CALL RANDOM(RAND)
2247:             NF=INT(RAND*N)+1
2248:         ENDDIF
2249:         IF (BEST.GT.F(NF)) THEN
2250:             BEST=F(NF)
2251:             NFBEST=NF
2252:         ENDDIF
2253:     ENDDO
2254: ENDDIF
2255: C -----
2256: IF (ITOP.LE.1) THEN
2257: C      RING TOPOLOGY *****
2258: C      REQUIRES THAT THE SUBROUTINE NEIGHBOR IS TURNED ALIVE
2259:     BEST=1.0D30
2260:     CALL NEIGHBOR(I,N,I1,I3)
2261:     DO II=1,3
2262:         IF (II.NE.I) THEN
2263:             IF (II.EQ.1) NF=I1
2264:             IF (II.EQ.3) NF=I3
2265:             IF (BEST.GT.F(NF)) THEN
2266:                 BEST=F(NF)
2267:                 NFBEST=NF
2268:             ENDDIF
2269:         ENDDIF
2270:     ENDDO
2271: ENDDIF
2272: C -----
2273: C      IN THE LIGHT OF HIS OWN AND HIS BEST COLLEAGUES EXPERIENCE, THE
2274: C      INDIVIDUAL I WILL MODIFY HIS MOVE AS PER THE FOLLOWING CRITERION
2275: C      FIRST, ADJUSTMENT BASED ON ONES OWN EXPERIENCE
2276: C      AND OWN BEST EXPERIENCE IN THE PAST (XX(I))
2277:     DO J=1,M
2278:     CALL RANDOM(RAND)

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2279:      V1(J)=A1*RAND*(XX(I,J)-X(I,J))
2280: C      THEN BASED ON THE OTHER COLLEAGUES BEST EXPERIENCE WITH WEIGHT W
2281: C      HERE W IS CALLED AN INERTIA WEIGHT 0.01< W < 0.7
2282: C      A2 IS THE CONSTANT NEAR BUT LESS THAN UNITY
2283:      CALL RANDOM(RAND)
2284:      V2(J)=V(I,J)
2285:      IF(F(NFBEST) .LT. F(I)) THEN
2286:      V2(J)=A2*W*RAND*(XX(NFBEST,J)-X(I,J))
2287:      ENDIF
2288: C      THEN SOME RANDOMNESS AND A CONSTANT A3 CLOSE TO BUT LESS THAN UNITY
2289:      CALL RANDOM(RAND)
2290:      RND1=RAND
2291:      CALL RANDOM(RAND)
2292:      V3(J)=A3*RAND*W*RND1
2293: C      V3(J)=A3*RAND*W
2294: C      THEN ON PAST VELOCITY WITH INERTIA WEIGHT W
2295:      V4(J)=W*V(I,J)
2296: C      FINALLY A SUM OF THEM
2297:      V(I,J)= V1(J)+V2(J)+V3(J)+V4(J)
2298:      ENDDO
2299: ENDDO
2300: C      CHANGE X
2301: DO I=1,N
2302: DO J=1,M
2303: RANDB=0.D00
2304: C      -----
2305: IF(NSIGMA.EQ.1) THEN
2306: CALL RANDOM(RAND) ! FOR CHAOTIC PERTURBATION
2307: IF(DABS(RAND-.5D00) .LT. SIGMA) RANDB=RAND-0.5D00
2308: C      SIGMA CONDITIONED RANDB INTRODUCES CHAOTIC ELEMENT IN TO LOCATION
2309: C      IN SOME CASES THIS PERTURBATION HAS WORKED VERY EFFECTIVELY WITH
2310: C      PARAMETER (N=100,NN=15,MX=100,NSTEP=9,ITRN=100000,NSIGMA=1,ITOP=2)
2311: ENDF
2312: C      -----
2313: X(I,J)=X(I,J)+V(I,J)*(1.D00+RANDB)
2314: ENDDO
2315: ENDDO
2316: DO I=1,N
2317: IF(F(I) .LT. FMIN) THEN
2318: FMIN=F(I)
2319: II=I
2320: DO J=1,M
2321: BST(J)=XX(II,J)
2322: ENDDO
2323: ENDF
2324: ENDDO
2325: IF(LCOUNT.EQ.NPRN) THEN
2326: LCOUNT=0
2327: WRITE(*,*) 'OPTIMAL SOLUTION UPTO THIS (FUNCTION CALLS=',NFCALL,')'
2328: WRITE(*,*) 'X = ',(BST(J),J=1,M), ' MIN F = ',FMIN
2329: C      WRITE(*,*) 'NO. OF FUNCTION CALLS = ',NFCALL
2330: IF(DABS(FMIN-GGBEST) .LT. EPSI) THEN
2331: WRITE(*,*) 'COMPUTATION OVER'
2332: FMINIM=FMIN
2333: RETURN
2334: ELSE
2335: GGBEST=FMIN
2336: ENDF
2337: ENDF
2338: LCOUNT=LCOUNT+1
2339: 100 CONTINUE
2340: WRITE(*,*) 'COMPUTATION OVER:',FTIT
2341: FMINIM=FMIN
2342: RETURN
2343: END
2344: C      -----
2345: SUBROUTINE LSRCH(A,M,VI,NSTEP,FI)

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2346:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
2347:      COMMON /KFF/KF,NFCALL
2348:      COMMON /RNDM/IU,IV
2349:      INTEGER IU,IV
2350:      DIMENSION A(*),B(100),VI(*)
2351:      AMN=1.0D30
2352:      DO J=1,NSTEP
2353:         DO JJ=1,M
2354:            B(JJ)=A(JJ)+(J-(NSTEP/2)-1)*VI(JJ)
2355:         ENDDO
2356:      CALL FUNC(B,M,FI)
2357:      IF (FI.LT.AMN) THEN
2358:         AMN=FI
2359:         DO JJ=1,M
2360:            A(JJ)=B(JJ)
2361:         ENDDO
2362:      ENDIF
2363:      ENDDO
2364:      FI=AMN
2365:      RETURN
2366:      END
2367: C -----
2368: C THIS SUBROUTINE IS NEEDED IF THE NEIGHBOURHOOD HAS RING TOPOLOGY
2369: C EITHER PURE OR HYBRIDIZED
2370:      SUBROUTINE NEIGHBOR(I,N,J,K)
2371:         IF (I-1.GE.1 .AND. I.LT.N) THEN
2372:            J=I-1
2373:            K=I+1
2374:         ELSE
2375:            IF (I-1.LT.1) THEN
2376:               J=N-I+1
2377:               K=I+1
2378:            ENDIF
2379:            IF (I.EQ.N) THEN
2380:               J=I-1
2381:               K=1
2382:            ENDIF
2383:            ENDIF
2384:            RETURN
2385:            END
```