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**Games in the Eurasian gas supply network:  
Multinational bargaining, Strategic investment, and Hold-up**

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**Abstract**

The paper analyzes multilateral relations and distortions of investments in the Eurasian gas network, supplying gas from countries of the Former Soviet Union to Western Europe. We use a two stage model of endogenous coalition formation to study cooperation among gas producers and transmitters, some lacking the ability to make long-term commitments. In the first stage, the players cooperate to invest in pipelines and contract the sharing of rents. In the second stage, players form supply chains and bargain over supply profit sharing. Since competing supply chains can be formed, cooperation involves externalities. Our quantitative analysis predicts overinvestment as well as underinvestment in the network as an attempt to create countervailing power. Among other things we explain why Russia invests in the expensive pipeline through the Baltic sea and why Caspian gas producers are eager to build expensive bypasses around Russia.

Keywords: strategic investment, hold-up, coalitional bargaining, gas supply

JEL class.: L14, L91, L95, C71, C72, Q41

# 1 Introduction

Natural gas is the environment-friendly source of energy. Its share in the EU primary energy consumption is over 20% at present and it is likely to increase in the future. While the consumption of gas in Europe is growing, its domestic production is declining, so a substantial part of gas is to be imported. Over a quarter of the total consumption is satisfied with gas from the Former Soviet Union (FSU). Since alternative producers, like Algeria, Norway, and exporters of liquefied natural gas, are not able to increase their supplies considerably, the dependence of the EU on FSU gas will grow in the future. This fact raises concerns on reliability and security of supplies from FSU.

In the past, a network of pipelines was built to deliver gas from the Soviet Union, namely from Russia and Caspian Republics, including Turkmenistan, Kazakhstan, Azerbaijan, and Uzbekistan, to the European market. The pipelines of the Eurasian gas network pass across Russia, Ukraine, Belarus, and Eastern European countries connecting fields in permafrost regions of Siberia and the steppes of central Asia with the Western European transport system. After the collapse of the Soviet Union, most of the Republics became independent countries, each pursuing its own interests. Russia inherited the majority of gas fields and all export routes, including those linking Caspian producers with the European market. To insure its revenues, Russia blocked the access to its export pipeline system and squeezed out potential competitors, establishing itself as the only gas exporter in the region.

However, for the delivery of its gas to the markets in Western Europe, Russia itself depends on newly independent Ukraine and Belarus. For a decade, these two transiters have exploited their control over the essential transport capacities as a bargaining chip in negotiations with Russia. Production and transportation of natural gas are characterized by large upfront investment costs, most of which are sunk after capacities are installed. Building a pipeline requires international cooperation among the countries, on which territories the pipeline will pass. The parties of the supply chain have to form a stable coalition in order to coordinate investment and agree on long term rent sharing. Within the EU there acts an established legal system, built on a number of Treaties, to enforce property and contract rights. In particular, the EU members signed the Energy Charter Treaty - an international agreement, which regulates and adds credibility to energy trade, transit and investments within Europe. However, at present, there is no international court system established to enforce gas transit contracts within FSU and hence, there is a risk of ex post opportunism. Once investments are made, transit countries enjoy a much increased bargaining power. If they cannot credibly commit to stick to a long-term agreement on profit sharing, other countries will anticipate a strategic abuse and distort their investment.

Thus, to gain leverage over the transiters and strengthen its bargaining position, Russia decided to diversify its export routes and establish a new path to Europe. It would be enough to upgrade and renovate of the Ukrainian transport system and build another pipeline in Belarus to satisfy

the growing demand. Yet, in 2005 Russia initiated the construction of a large offshore pipeline - the North European Gas Pipeline, also known as Nord Stream. The pipeline will stretch through the Baltic sea and connect Russia directly to Europe, bypassing all the transit countries. The new project is by far the most expensive of all options. It is at least four times more expensive than the upgrade of the Ukrainian system and twice as expensive as the second pipeline through Belarus.

The observed investment pattern considerably deviates from the "non-strategic" investments, which would maximize the profit of the entire network and minimize transportation cost. In this paper we study how investments may alter the power structure in the Eurasian supply chain in order to provide a rationale for the observed developments in the network.

As the gas demand in Europe is growing, other FSU producers intend to enter the European market. The Caspian Republics can export as much gas as Russia does and do so at lower costs. Currently, the Caspian producers can reach the European market only via Russia. Unable to market their gas directly, the Caspian producers have been forced to sell their gas to Russia at low prices. However, with the support of the United States and the EU, these producers have developed plans to bypass Russia. The USA have offered its help to build a Trans-Caspian pipeline passing through Azerbaijan, Georgia, and Turkey. The EU has suggested an alternative route across Iran and Turkey - the Nabucco pipeline. Both projects are expensive, with transportation costs significantly exceeding the costs of transit through Russia. Progress has also been slow due to the the difficult political situation in the region. Nevertheless, the installation of pipelines have been started. A Georgian section of the pipeline, connecting Turkish border with Azerbaijan, is close to completion. Turkmenistan and Iran have a tentative agreement to raise financial capital to proceed with the Nabucco pipeline. The potential transitters for the Caspian gas can not afford a large scale investment as well as can not pay for the increase in bargaining power up front. However, after the pipelines are installed, the transitters will gain a strategic advantage and thus, the hold-up problem arises. In this work, we analyze how the ability to commit affects investment and try to answer the question whether the Caspian pipelines will finally be built.

The formation of a competing supply chain by the Caspian players will reduce Russian profits. Hence, the cooperation among players of the network involves a kind of externalities. Anticipating a potential loss, Russia has already made substantial concessions to the Caspian producers to prevent the construction of the alternative pipelines. It has contracted a large increase in gas imports and agreed to a much higher price for Turkmen gas. In this paper, we study the interrelated issues of bargaining in vertical supply chains with externalities and strategic investments to understand the change in relations between Russia and the Caspian Republics.

To analyze multinational relationship and distortion of investments in the Eurasian gas supply network we use a two stage model, with a setting similar to the one developed by Kreps and Scheinkman (1989) to represent the problem. At the first stage, players form coalitions and invest in transport capacities, contracting how the future investment profits are shared. At the second

stage, investment costs are sunk, players form supply chains and bargain on supply profits sharing. We assume that supply coalitions formed at the second stage compete in prices, given the capacities installed at the first period. Reliable players commit not to renegotiate the cooperation of the first stage. Since unreliable players may renegotiate at the second stage to get a higher payoff, they do not take part in cooperation of the first stage.

We derive the bargaining power and a coalition structure in the network endogenously. Therefore, on each stage we have to solve coalition formation and bargaining game. To do so, we describe the game in "partition function form" (PFF), introduced by Thrall and Lucas (1963).<sup>1</sup> The partition function allows to introduce interdependencies among players and captures the presence of externalities. It assigns to every possible coalition a value with respect to the entire coalition structure. A number of solution concepts have been proposed for games in partition function form (PFF). Some authors have developed extensive form approaches to a PFF game, e.g. Bloch (1996), Ray, Vohra (1999), and Gomes (2005). These models differ in protocols, which determine the order of players' moves and hence, how a game develops. To avoid protocol dependency of the outcome various axiomatic solutions have been proposed, e.g. Do, Norde (2002), Ju (2004), and Clippel, Serrano (2005). These models characterize a modification of the Shapley value and are based on the assumption that a grand coalition always forms. This assumption considerably limits the implications of these solutions. For our analysis, we choose another solution concept which has been proposed by Maskin (2003). The approach of Maskin (2003) is based on the "random order bargaining" concept, which essentially describes a game in extensive form. However, to specify the development of the game Maskin (2003) uses a set of axioms, which characterize the desirable properties of the solution. A major advantage of Maskin's (2003) solution is that it determines both the expected coalition structure and the expected payoffs of players endogenously.

In the quantitative part of the paper we numerically solve for equilibrium coalition structures, investments and expected payoffs of the players. The number of player in the network is small. Information on production, transport and investment costs for the existing and prospecting pipeline projects enable us to estimate the supply function. We derive the linear residual demand for the former Soviet Union region gas based on marginal costs of other European exporters. We assume that the bargaining among the network players is efficient and so is the use of the existing network, though investments in the capacities may be inefficient for strategic reasons. In the result, the European supply chain provides us with a rather unique opportunity to confront the theoretical solution of game theory with real world experience.

We consider three scenarios, which vary in the assumptions on the players' ability to commit. As a benchmark case we take the situation in which all the players can credibly commit. The

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<sup>1</sup>In the presence of externalities, we cannot describe the bargaining game in characteristic function form, since a value of a coalition depends on the allocation of the players outside. Therefore, we can not apply solution concepts, such as Shapley value (1953), Owen value (1977), core, and etc.

resulting first best investment plan would maximize the profit of the whole network. The second scenario describes the situation where only producers, Russia and Turkmenistan, can commit, while transitters are prone to recontract. In the third scenario none of the players can commit.

We find that the hold-up problem leads to overinvestment, as well as underinvestment, and "undercooperation". Underinvestment occurs when investment in a cost efficient pipeline weakens the bargaining position of a producer too much. Overinvestment occurs when investment in expensive pipelines, while reducing overall profits, yields a large enough gain in bargaining power. In other words, players increase capacities to strengthen their bargaining position vis-a-vis unreliable partners. By undercooperation we mean a more splintered coalition structure compared to the one which would prevail if all the players can commit.

It turns out that the ability to commit to long-term profit sharing is of an overriding importance and diminishes the role of investment cost. In the second scenario, when the transitters cannot commit, the producers cooperate at the investment stage and invest in expensive direct pipelines. The resulting overcapacity is justified by a bargaining advantage of the producers at the second stage. Yet if we assume that the producers were also not able to commit, competing supply coalitions form. The Caspian producers would build the pipelines bypassing Russia, in spite of the assumed unreliability of the Caspian transitters. Russia would still build the direct Baltic pipeline. The lack of commitment would substantially reduce the profit of the network.

This paper continues the analysis provided by Hubert, Ikonnikova (2004) and Ikonnikova (2006). Similar to Hubert, Ikonnikova (2004), we consider how the hold-up problem affects investments in the Eurasian network. In this paper, however, we add the Caspian Republics into consideration and enrich the model with externalities. We extend the framework of Ikonnikova (2006), who derives the strategic value of investment options in the Eurasian network in the presence of externalities, but assumes that all the players can commit. In our analysis we assume that some players lack the ability to make long-term commitments and opt to renegotiate their payoffs ex post to extract quasi-rents. By its application, the paper also relates to the literature on gas market: Grais, Zheng (1996), Stern (1999), Opitz, von Hirschhausen (2000) and von Hirschhausen, Meinhart, Pavel (2005). These works quantify the impact of cooperation on the supply network extension and consider the incentives to extend the pipelines along Ukraine and Belarus under different cooperation regimes. The Stackelberg leadership, Nash bargaining, Nash product concepts have been applied to predict investments and payoffs of the countries. However, all the previous works focus only on the relation of Russia and its transitters, so that the issue of externalities does not arise. We are not aware of any study tackling the coalition formation issue and hence, we pioneer in this respect.

From a standpoint of a general bargaining problem with externalities, our work relates to studies on other topics. In particular, Eyckmans, Tulkens (2001) explore the issue of Kyoto protocol, where players are countries and externalities are emissions affecting the environment of others. Jehiel,

Moldovanu (1996) study a patent acquisition problem, in which oligopoly firms collude to buy an innovation from a rival. Fridolfsson, Stennek (2002) analyze preemptive mergers, where firms merge with the hope of avoiding the negative externalities of being an "outsider" of the deal. Finally, Calvert, Dietz (1998) consider the formation of political parties. All these studies use the Nash equilibrium and Markov equilibrium solution concepts to find an outcome of a coalition formation game. To the best of our knowledge, our work is the first attempt to use the solution of Maskin (2003). Besides, we are aware of only two previous application of a partition function form game to analyze a real world problem. Eyckmans, Tulkens (2001) applied PFF game to study greenhouse gas emissions and Pintassilgo (2003) use PFF game to analyze the Northern Atlantic bluefin tuna fisheries. Both focus on a fair sharing rule for the distribution of the returns from cooperation, which will ensure stability of a coalition structure. Our approach is different since we derive the sharing of the profit endogenously.

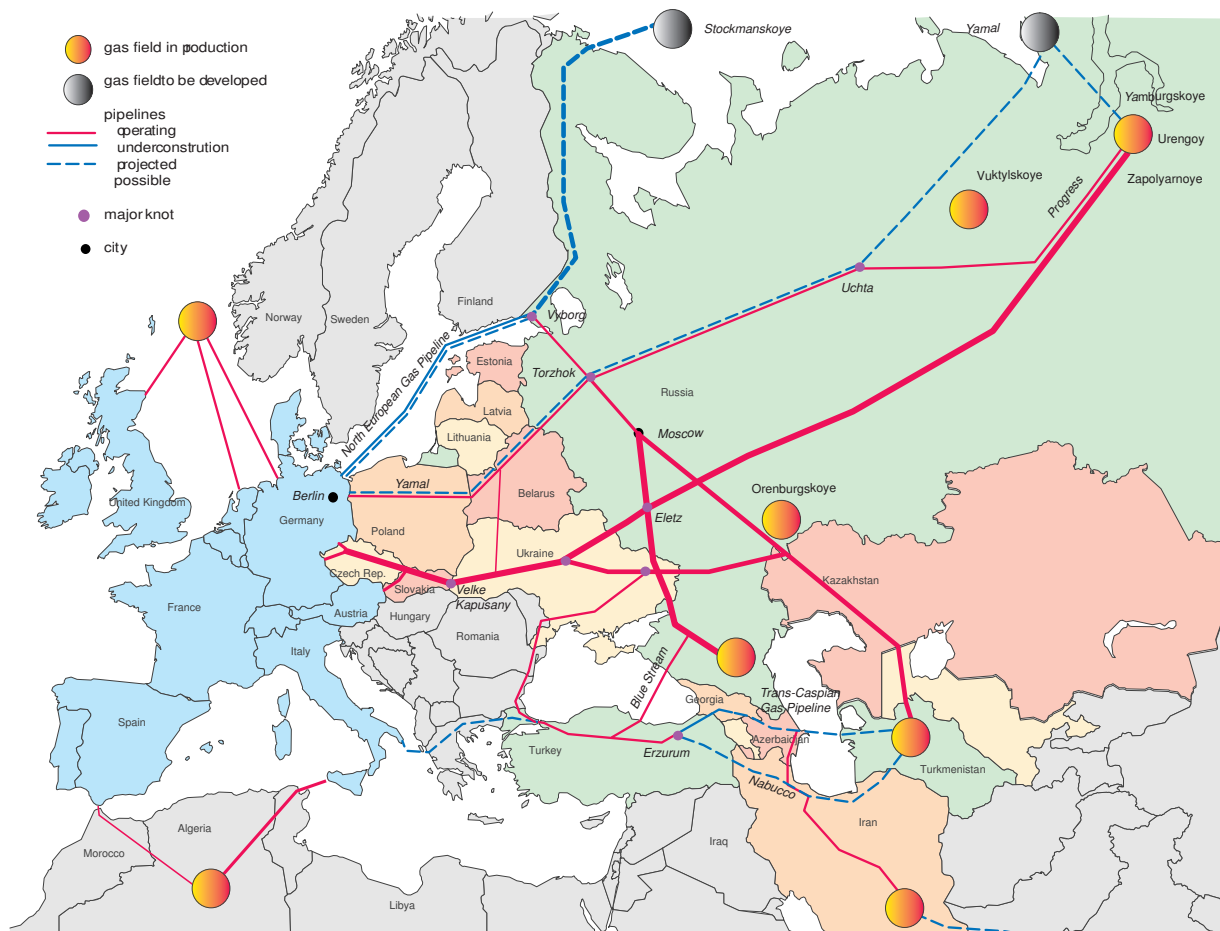
Although the results of our analysis fit the reality quite well, there are a number of limitations which lead to some discrepancy with the real world figures. Hence, several issues are left for further research. First, we do not explicitly model the interaction of the FSU gas producers with other exporters at the European market, such as Norway, Algeria, and African and Middle East supplies of liquified natural gas. Rather, we model the European market non-strategically and simply estimate a residual demand for gas from the Former Soviet Union. Second, in our study we focus on the relationship of producers and transitters only. However, in reality, major European importers, like French monopoly Gas du France, German giants E.ON and Wintershall, or Italian Eni, do take an active part in investments in pipelines. Hence, a natural extension of the models would be to include gas importers into the investment game. Third, our model is static by its nature. We assume that the players make investment decisions and negotiate cooperation once and for all. Hence, we do not account for the dynamics of repeated interaction. In the absence of an international enforcement system long-term cooperation can be sustained by mutual threat of retaliation in future periods. This type of dynamic cooperation, referred to as collusion, is explored in the literature on cartels and can be applied to the Eurasian gas network. Our fourth restriction concerns the players' ability to commit. In the course of our analysis we consider only extreme cases assuming that players either can commit or not. Alternatively, one could assume that players renegotiate with some probability.

The remainder of the paper is organized as follows. Section 2 introduces the players and explains their conflicts. Section 3 presents a formal modal. In Section 4 we give the assumptions of the quantitative analysis. In Section 5 we discuss the numerical results. Section 6 concludes.

## 2 Players and their Relations

In the following, we distinguish the two types of players in the Eurasian gas supply network: producers and transitters. The producers are Russia and Turkmenistan, the latter representing the Caspian gas producers.<sup>2</sup> Production fields are distant, to reach the European market the producers turn to transitters for transportation services. At present, Ukraine and Belarus transport Russian gas. Azerbaijan, Georgia and Iran are the prospective transitters for the Caspian gas.<sup>3</sup>

Figure 1: The Eurasian gas supply network



European countries buy gas by "take-or-pay" contracts, typically ranging from 15 to 25 years.<sup>4</sup>

<sup>2</sup>International gas affairs in the Former Soviet Republics are run by state monopolies, therefore, we will refer to respective countries instead of naming the companies, e.g. Russia instead of Gazprom.

<sup>3</sup>We do not consider other countries involved in gas transportation, e.g. Poland, Czech Republic, Turkey and etc. Assuming the open access and regulated tariffs there, we focus on interactions between the Former Soviet Republics only.

<sup>4</sup>So called 'take-or-pay' contracts regulate prices and quantities to ensure the efficient usage of the capacities and steady revenues. To account for changes in the economic environment gas prices used to be indexed to oil prices.



These long-term contracts are signed between a producer and a buyer: the former commits to steady deliveries of a certain quantity of gas, the latter is obliged to pay for that quantity whether it is taken or not. Historically, the point of delivery is considered to be the Western European border. Hence, producers have to also tackle the transportation issues, namely transit relations and coordination of investments in transport capacity.<sup>5</sup>

The Eurasian gas network was mainly shaped in the late 70s, when the Soviet Union started exporting gas to the European market. At that time a system of pipelines was built running through territories of Ukraine and Czechoslovakia and connecting to internal gas systems of Austria and Germany. When the Soviet Union collapsed, Russia found itself in the uncomfortable position with its only supply route to Western Europe passing through three newly independent states Ukraine, Slovakia and the Czech Republic. Looking westward towards integration with the EU, Slovakia and the Czech Republic privatize their transmission pipelines. The Slovakian section was acquired by the German Utility RWE, the Czech section by a consortium of Gazprom, Ruhrgas and Gaz du France. Since yielding control over pipelines to the importers, the countries never attempted to use their strategic location as a bargaining chip in negotiations with Russia.

In contrast, relations between Russia and Ukraine turned sour. In principle, Russia pays for transmission by supplying gas to Ukraine, approximately 26-30 bcm/a (plus an additional 6-7 bcm/a compressor gas). This payment in kind is sometimes translated into a 'transit fee' by assigning a price to the gas. Besides the quantities of gas delivered by Russia for transit, Ukraine needs additional 20 bcm/a. The conflict has essentially evolved over the compensation for this extra gas, which Ukraine could hardly pay for. While Russia claimed average European prices, Ukraine admitted only half of that. However, even this lower price has not fully been paid. As a result debts accumulated. In 2002, these amounted to \$ 1.4 bn, or \$ 3.5 bn, depending on which side one takes.

As the dispute about non-payments for gas deliveries and debts dragged on, Russia tried to reduce its supplies to Ukraine. In response the transiter syphoned off gas from Gazprom's storages on its territory and from European export pipelines. Russia has little choice but to supply whatever Ukraine takes or to default on its obligations to western importers. Although Ukraine's withdrawals interrupted gas supplies to Western Europe only occasionally for short periods, these episodes highlighted Russia's vulnerability and threatened to taint its reputation as a secure supplier.

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However, over a long period of time, the contracted quantities had to be paid for whether used or not, hence, the name 'take-or-pay' (Asche, Osmundsen, Tveteras (2000)). As the gas market developed, prices gained some independence from oil prices and the current drive for liberalization favors short-term contracts and third party access. In spite of these changes, it is still common that producers and importers form consortia to realize new projects under long-term agreements (Stern (2001)).

<sup>5</sup>Although gas buyers often contribute investment capital, they stay away from the supply and transit issues as such. See "Energy Information Administration" on <http://www.eia.doe.gov> for more information on international pipeline investment projects.

Meanwhile, in late 90s the capacity of the Ukrainian transmission network, which we will name *Ukold*, dropped to 70bcm/a due to aging compressors, lack of maintenance and underinvestment. The cheapest and fastest option to increase export capacities would be to upgrade the Ukrainian system. By replacing old compressors the transmission capacity could easily be increased by 15 bcm/a. Hereafter, we will refer to this possibility as *Upgrade*. In 2004 Gazprom and Ukrainian Naftogas reached a tentative agreement according to which Russia in co-operation with German Ruhrgas would attract \$ 2.5 bn to upgrade the system. Ukraine in its turn should have given the investors a control stake over the transit system. However, after Ukraine refused to sell the required package of shares, Russia declined to invest in Upgrade.

Instead, as a direct threat to Ukraine's strategic position, plans have been drawn up for a twin-pipeline going to Germany through Belarus and Poland. In 1994 Russia started the project often referred to as *Yamal*.<sup>6</sup> Initially Yamal included two pipelines with total capacity of 56bcm/a. Eventually, only the first export line, so called *Yamal 1* was installed. In the late nineties this pipeline with a potential capacity of 28 bcm/a had compressors to support only 18 bcm/a and reached its planned level only in 2006. Together with the first pipeline, at major river-crossings pipes for the second band, *Yamal 2*, have been laid.

To manage the transit through Yamal in Poland a joint stock company, EuroPolGaz, was established in which Polish PGNiG and Russian Gazprom hold equal shares. In 2004 Poland became an EU-member and since then its transit obligations can be enforced by the European legal system. Russia and Belarus agreed on a long-term solution for sales and transit relationships, including the transfer of the assets of Beltransgaz, Belarus' national gas company, to Gazprom under a 99-year lease. In exchange, Russia would have increased gas supplies to Belarus, which like Ukraine, buys Russian gas for its domestic needs at a special price. Yet, the Belorussian parliament did not ratify the agreement. Thus, Russia failed to gain control and to guarantee security of its export via Belarus. Instead, it again found itself in a weak bargaining position.

After the dissolution of the Union, Belarus' ties with Russia remained very close and its ability to act independently was fairly restricted due to its weak economy. The country had to rely on subsidies from Russia in the form of reduced prices on a bundle of goods, including gas. However, even in this situation Belarus accumulated significant debts. Shortly after the pipeline was installed, Belarus start exploiting its strategic position in financial disputes with Russia. Every attempt of Russia to raise the prices has resulted in renegotiations over the proportional increase in transit fees. When Russia cut off gas supply to Belarus in February 2006, the transiter took the required gas from export pipelines. To fulfil its export obligations Russia had to compromise and restored the

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<sup>6</sup>The name came from the idea to connect this pipeline to a large gas field in the Yamal peninsular. As demand was weak during the nineties the project was gradually scaled down. The development of the field was postponed. Only the section of the pipeline, from the Russian border to Europe, was to be built. See the extended description and the complete history of the project in Stern (2005).

delivery. A number of short-term agreements were produced to settle the feuds, but little progress was made to find a long-term solution. Only recently, on 31 December 2006, a new long-term contract was signed. It doubled the gas prices for Belarus from 47\$/tcm to 100\$/tcm, which is still only a half of the price Western Europe pays, and envisaged a stepwise adjustment to international prices by 2011. However, the increase in prices is partially compensated by a 70% increase of transit fees and by cash payments, that Gazprom is expected to make for the acquisition of Beltransgaz (see Yafimova and Stern (2007) for details). Given Gazprom's past failures in attempts to gain control over transit pipelines, it is very likely that Belarus may again fail to implement the last step and Gazprom's payments would mainly offset the price increase.

Increasing frustration with the demands of transit countries led Russia to look for a direct, although much more costly, offshore option. The project, known in 2000 under the name of North-Trans Gas and later called the North European Gas pipeline or Nord Stream, has been designed to carry Russian gas through the Baltic sea directly to the German border. The project, which we further denote as *NEGP*, was initially under the control of the German-Russian consortium of Gazprom, Wintershall, and E.ON-Ruhrgas. Investment costs of this offshore pipeline are at least twice as high as that of any onshore pipelines, and NEGP has long been regarded as unfeasible. Nevertheless, Russia started work on the offshore section of NEGP in 2005. Originally planned capacities were from 18 to 30 bcm/a, but the new scale of the project is 55bcm/a.

Several observations are particularly notable in this context. First, the transiters, Belarus and Ukraine, failed to establish long-term stable relations with Russia. They are involved in continuous bargaining over compensation for transit and for import of Russian gas. The renegotiations highlight the commitment problem. As a result, investments suffer from the hold-up problem. Second, despite the conflicts, interruptions to Russian supply have been very rare and short. As a rule, the players bargain and use their capacities efficiently. Third, we note that Russia's choice of investments reflects the desire to strengthen its position. However, while the capital costs of investment projects are known, the strategic gains can not be estimated directly.

### **Prospective players**

During the Soviet time, Russia and other Republics consumed a significant amount of gas from Caspian Republics, of whom the largest gas supplier was Turkmenistan. Turkmen gas, together with Russian gas, was also sent to the European market. After the collapse of the Soviet Union, the Caspian producer demanded "world prices" for their gas, but the FSU countries were not able to pay that price. Then, Turkmenistan stopped the delivery to its former customers hoping to receive profit from export to Europe. However, all the export routes from the Caspian fields to Europe run through the Russian territory. In the 90s gas demand in Europe shrank. To secure its own export revenues Russia denied potential rivals' access to its pipeline system. As a result, gas

production in Turkmenistan dropped from 84bcm/a in 1991 to 13bcm/a in 1998.<sup>7</sup>

With no other options to market its gas, Turkmenistan had to agree to supply Russia and neighboring countries for a price almost three times lower than that paid by Europe.<sup>8</sup> The largest consumer for Caspian gas was Ukraine. Turkmenistan had to meet Ukraine's demand not covered by gas import from Russia. However, when Ukraine was unable to pay for its import, Turkmenistan simply cut its deliveries. This move put Russia into troubles, as Ukraine threatened to take gas from the export pipelines. In 2004 Russia signed an agreement with Turkmenistan to buy its gas for Ukraine to relieve itself from the increased burden.

The terms of the cooperation between Russia and Turkmenistan, however, are highly dependent on the outside options of the Caspian producer. After 1997, the demand in Europe recovered and entered a phase of steady growth. Producers of the Caspian region again turned an eye on the European market. After keeping their fields idle for the last decade, they can easily raise the extraction since fields are developed and equipment is in place. The milder climate conditions of Caspian fields give them a cost advantage compared to most of the Russian fields, which are situated in the permafrost terrain. All this makes Turkmenistan, which can cover up to 80% of the Russian export, a potentially strong competitor in the European market. However, to reach the European market, the Caspian producers will have to bypass Russia.

At the beginning of the century, the USA and the EU proposed two projects with the intention to abate the dependency on the Russian gas supply and enhance the opportunity for the Caspian producers to access the European market. The USA offered its support to the Trans-Caspian Pipeline, to which we will refer as *TCP*. The project was first proposed in 1999 to supply 30bcm/a of Turkmen gas to Turkey across the Caspian sea and Azerbaijan. However, while Turkmenistan and Azerbaijan were arguing over a transit contract, Russian Gazprom accelerated its own negotiations with Turkey. As a result, Russia contracted to supply 16bcm/a of gas and started building the Blue Stream pipeline to supply Russian gas to Turkey through the bottom of the Black sea. A key partner in the construction of the pipeline was Italian gas monopoly Eni, whose intentions were to extend the pipeline further to deliver gas via Turkey to Italy. In 2003, when the United States suggested to build a pipeline bypassing Russia, the TCP project was revised and extended. The new plan was to export Turkmen gas via Azerbaijan and Georgia to Turkey and further to Italy and through Bulgaria to Austria.

In December 2006 Baku-Tbilisi-Ceyhan pipeline, the Georgian section of TCP connecting Turkish system with Azerbaijan, start delivering Azeri gas to Turkey. The growing US influence in the region made Georgia look like a reliable transiter. However, the project still faces a number of

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<sup>7</sup>See gas production statistic in Stern (2005).

<sup>8</sup>Until 2005, Turkmenistan obtained 44\$/tcm for its gas. As Ukraine agreed to pay more for Russian gas, the payment to the Caspian producer rose to 65\$/tcm. At present, the price agreed with Russia is 100\$/tcm, whereas Europe pays more than 200\$/tcm.

difficulties. The Nagorno-Karabakh conflict complicates installation of the pipeline and its security in Azerbaijan. The country has a tight budget and can hardly pay investment costs up front. The unstable position of the country complicates the attraction of the financial capital from outside. Besides, as before Azerbaijan and Turkmenistan stalled on a transit deal. Turkmenistan agrees to give up one third of supply profit on account of transit, yet Azerbaijan insists on at least a half. Taking into account the history of the dispute one can assume that it will take a long time to reach a compromise.

Sceptical on a result of these negotiations, the European Union favors an alternative pipeline running through Iran to Turkey and further to Europe. However, this pipeline, which we will refer to as *Nabucco*, also faces obstacles. Iran holds huge gas reserves and seems to be interested in the project for itself. Although it is ready to pay up front for its part of the pipeline and readily agrees on terms of a transit deal proposed by Turkmenistan, it seems very likely, that it would like to use the existing capacity for its own supply. A pipeline connecting the Nebit Dag, Korpedze and Okarem fields in Turkmenistan with the internal Iran grid at the Kord-Kul node was already launched in 1999. Currently it delivers less than 10bcm/a to Iran, but the plan for the additional 20bcm/a with a further connection to Turkey has already been outlined. However, it is unlikely that the project will be implemented without Turkmenistan, therefore Iran has to agree with a role of a transiter.

Some concerns regarding both Caspian pipelines have also been raised against Turkey. The country is located at the crossroad between Caspian and Middle East Countries. As the gas flow to Europe was growing, Turkey became ambitious to establish itself as an exporting country.<sup>9</sup> Hence there is a chance, that once the pipelines are completed, Turkey would recontract to change its role from a transiter to the role of an exporter. At the same time, however, it is looking forward towards its joining the EU. Hence, Europe has some leverage over Turkey, which might be pushed to sign the Energy Treaty, the agreement obliging its members to undertake a third party access to transit facilities. In this case, Turkey would not be permitted to compel a resale contract from Turkmenistan. In view of this argument, it seems more adequate to assume that Turkey will be held back, so that the Caspian producers can rely on the access to the transit capacities.

Despite all the problems, the Caspian pipelines present a viable threat for Russia. First, it may lose the inflow of low cost Caspian gas<sup>10</sup> and will have to develop new fields, significantly increasing the supply costs. Second, if Turkmenistan enters the market, Russia will meet a stronger competition and lose a part of its export profits. In view of the competition and its negative impact,

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<sup>9</sup>Turkey imports Russian gas through the Blue stream pipeline in the Black Sea. The amount of gas contracted leaves Turkey with 6-8 bcm/a of excess gas. Recently, Turkey won the right to sell excess gas to Europe. Together with 5bcm/a of Iranian gas and over 20bcm/a of Turkmen gas, Turkey may export up to 30bcm/a.

<sup>10</sup>At present, fields in Siberia are at peak production or in decline. To increase its export Russia has to develop new fields on the Yamal peninsular. This requires significant investments and will raise the supply cost of Russian gas.

Russia had to comply with demands of Turkmenistan in recent negotiations over the export price on Turkmen gas. In 2005 Turkmenistan enjoyed a 20% increase in prices from 44\$/tcm to 56\$/tcm and in 2006 the price jumped to 100\$/tcm. Russia also contracted a drastic increase of Turkmen export volumes from 30 bcm/a in 2006 to 80 bcm/a in 2025. These concessions dampened Turkmenistan's interest in the alternative routes. At present it looks as if the bypass projects have been postponed.

To conclude, it is worth mentioning a few issues related to the Caspian players. If Turkmenistan succeeds in forming a coalition with Iran and/or Azerbaijan, a competing supply chain will form. Competition will reduce profits of Russian gas supply and weaken the strategic position of Russia. We refer to this negative effect as "externality". Further, by analogy with the Russian supply chain, the lack of enforcement of transit contracts between Turkmenistan and its transiters, results in the hold-up problem. In the next section we develop a formal model of how network architecture and investments determine the cooperation and the sharing of profits in the network.

### 3 The model

#### 3.1 Basic notions

To analyze the investment problem we use a two stage model. We consider a set of players  $N = \{..., i, ...\}$  consisting of producers and transiters cooperating to sell gas. Gas is transported through pipelines. Before trade takes place the players set up capacities by investing in pipelines. Players may form coalitions to invest cooperatively. By the time of supply, investment costs are sunk and capacities generate quasi-rents. Before implementing the investments, members of coalitions sign long-term contracts specifying how expected rents are to be shared. We assume that some players may be not able to credibly commit to such contracts and may renegotiate payoffs ex post. Hence, the "hold-up" problem may arise. As a result, only credible players will cooperate to invest.

In detail the game unfolds as follows. At the first stage, marked with the superscript  $I$ , players form "investment coalitions"  $S^I$ . The set of coalitions  $P^I = \{..., S_k^I, ..\}$  is referred to as a *partition*, or a coalition structure. We assume that coalitions embedded in any partition are pairwise disjoint  $S_k \cap S_h = \emptyset$  for all  $k \neq h$  and  $\bigcup_{k=1}^{|P^I|} S_k = N$ , where  $|\cdot|$  denotes cardinality. In view of the hold-up problem we limit the set of possible coalition structures by allowing only the set of credible players  $N^c$  to form coalitions. The players, who cannot credibly commit  $N \setminus N^c$ , play as singletons. We denote the new set of partitions formed within this restriction as  $\Pi^I$ . Note that  $\Pi^I$  is a subset of the set  $\mathbf{P}^I$  of *all* possible coalition structures that can be formed by the players  $N$ . The two sets are equal if all the players can commit  $\Pi^I = \mathbf{P}^I \Leftrightarrow N = N^c$ , if none of the players can commit  $N^c = \emptyset$  the only possible partition is a set of singletons  $\Pi^I = \{N\}$ .

Each coalition  $S^I \in \Pi^I$  invests in network capacities  $k^*(S^I)$  to maximize its future rent. The rent depends on the total capacity of the network and hence, on the entire partition. Therefore,

we use a partition function for its representation. The partition function  $w : \Pi^I \rightarrow R^{|\Pi^I|}$  maps all possible terminal coalition structures into a vector of values for embedded coalitions  $w^I(S^I; \Pi^I)$ . The advantage of the PFF approach is that it captures the presence of externalities. Formally, we speak of externalities whenever

$$\exists S : w(S; P) \neq w(S; P'), \quad \text{for } P \setminus S_k \setminus S_j = P' \setminus \{S_k \cup S_j\} \quad (1)$$

there is at least one coalition, which value changes with a change in a partition. When the inequality sign in (1) becomes "greater than", the externalities are negative. In this case the union of the coalitions  $S_k$  and  $S_j$  impose a loss on  $S$ . If the inequality sign is "less than", the externalities are positive. This means that the merger of  $S_k$  and  $S_j$  brings  $S$  a gain.

Forming coalitions, the players simultaneously bargain over the rent sharing and fix the payoffs  $\psi^I = (\dots, \psi_i^I, \dots)$  with long-term contracts. To sum up, at the first stage, the coalition formation and bargaining game in a partition function form (PFF) is given by  $(N, N^c, w^I)$ . The solution of this game we search as a vector of expected payoffs  $E[\psi^I]$  and a probability distribution of equilibrium partitions  $p(\Pi^I)$ .

At the second or "supply" stage, investment costs are sunk, the network capacities  $k^* = \sum_{S^I \in \Pi^I} k^*(S^I)$  are fixed and players form coalitions  $S$  and supply gas to the market. We will use the superscript  $S$  to label the variables of the second stage.<sup>11</sup> At this stage, the set of players is represented by coalitions  $\Pi^I$  formed at the previous stage of our model. In other words, each coalition  $S^I$  acts as a single player. We denote the coalition structure at the second stage as  $P^S$ . Newly formed coalitions  $S$  compete on the market setting prices  $p_S$  and quantities  $q_S$ . The market equilibrium depends on the supply chains, or coalitions  $P^S$  formed. As a result, supply profits are again given by a partition function  $w^S(S; P^S)$ . As in the first stage, joining in coalitions players bargain over sharing of the supply profits. The outcome of the bargaining - vector of payoffs  $\psi^S = (\dots, \psi_{S^I}^S, \dots)$  - determines the rents of the first stage coalitions.

In short, the second stage is described by the game in partition function form  $(\Pi^I, w^S)$ . The outcome of the game is the pair  $(E[\psi^S], p(P^S))$  - the vector of expected payoffs and probability distribution of coalition structures.

By its structure, our two stage game is similar to a composite game developed by Owen (1977). Owen (1977) modelled a game, in which players form 'a priori' coalitions to gain an advantage in subsequent bargaining, where these coalitions act as units. He defined the expected payoff of a player as an outcome of the bargaining over sharing of the expected profit of an 'a priori' coalition, which the player joins. The approach of Owen (1977) is based on the Shapley value and hence, does not allow for externalities. We extend the framework of Owen (1977) to games with externalities by using the PFF game solution of Maskin (2003).

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<sup>11</sup>However, to avoid cumbersome notations we will denote coalitions formed at this stage as  $S$  instead  $S^S$ .

To solve the investment problem we need to find the outcome of the game  $(N, N^c, w^I)$ . To do so, we must calculate the values of the partition function. In what follows, we will first define how the values of the partition function are calculated. We work out the game backwards and hence, start with the bargaining at the second stage  $(\Pi^I, w^S)$  considering all possible equilibrium partitions of the first stage  $\Pi^I$ . Then, we proceed with the partition function  $w^I$ . We will describe the solution concept of the game in partition function form in section 3.4, until then we assume that we know how  $(E[\psi^I], p(\Pi^I))$  and  $(E[\psi^S], p(P^S))$  are determined based on the values of the partition functions.

### 3.2 The second stage

At the second stage the capacities of the network  $k^* = \{k_l^*\}_{l \in L}$  for  $L = \{NEGP, Ukold, Upgrade, Yamal1, Yamal2, TCP, Nabucco\}$  are fixed. By forming a coalition players combine their resources. We denote the capacities that a coalition has at its disposal by  $k^*(S)$ .<sup>12</sup> The available capacities constrain supply:  $q_S \leq k^*(S)$ . In order to be able to supply a coalition must include at least one producer. In our case, we have only two producers, so that at most two supply coalitions can form. We assume coalitions compete in prices and use the insight of Kreps, Scheinkman (1983) to analyze the price competition under capacity constraints. Each coalition sets a price and serves demand up to available capacities:

$$q_S = \begin{cases} \min[k^*(S), \max[0, D(p_S) - k^*(S')]], & p_S > p_{S'} \\ \min[k^*(S), D(p_S)], & p_S < p_{S'} \\ \min[k^*(S), \max[\frac{D(p_S)}{2}, D(p_S) - k^*(S')]], & p_S = p_{S'} \end{cases} \quad (2)$$

here  $D(p)$  is the demand function and  $S$  and  $S'$  are the competing coalitions. The coalition, which sets a lower price, supplies first, high price coalition faces residual demand. Following Kreps, Scheinkman (1983), we assume the efficient rationing of demand. If the prices are the same, competing coalitions share the demand equally. If both producers are in the same coalition, they form monopoly. As a result, coalitions obtain a net profit  $\pi(S; k^*(S), k^*(S'); p_S, p_{S'}) = p_S q_S - tc(q_S)$ , where  $tc(\cdot)$  is the total cost of supply.

According to Lemmas 2 to 6 in Kreps, Scheinkman (1983) there can be a pure strategy and a mixed strategy equilibrium. The former occurs when the total capacity is in the Cournot region, that is smaller than the optimal Cournot response:  $r(k^*(S')) = \arg \max_{k^*(S)} p(k^*(S) + k^*(S'))k^*(S) - tc(k^*(S)) \geq k^*(S)$ . In this case, coalitions earn Cournot profits. If  $k^*(S) > k^*(S')$  and  $k^*(S) \geq r(k^*(S'))$  there is a mixed strategy equilibrium, and the expected profit of a larger (in terms of capacity) coalition is equal to  $\pi^*(S; k^*) = p(r(k^*(S')) + k^*(S'))r(k^*(S')) - tc(r(k^*(S')))$ .

<sup>12</sup>Capacities available to a coalition are the pipelines running through the territories of the coalition members. For instance, Russia controls NEGP  $k^*({r}) = \{k_{NEGP}^*\}$ , Ukraine - Ukold and Upgrade  $k^*({u}) = \{k_{Ukold}^*, k_{Upgrade}^*\}$ .



The coalition with smaller capacities earns the expected profit of  $k(S')/k(S) \cdot \pi^*(S; k^*)$ .<sup>13</sup> The equilibrium profits determine the values of the partition function:

$$w^S(S^S; P^S) = \pi^*(S; k^*) \quad (3)$$

For coalitions consisting of transmitters only we have  $w^S(S^S; P^S) = 0$ .

Calculating the values of the partition function for all possible  $P^S$ , we obtain a full description of the game of the second stage, and can solve for the equilibrium  $(E[\psi^S], p(P^S))$ . Since the values of the partition function depend on capacities, the outcome of the game also depends on  $k^*$ . To make this relation explicit we further write  $E[\psi^S(k^*)]$  and  $p(P^S(k^*))$ . Now we proceed with the first stage at which the capacities are chosen.

### 3.3 The first stage

At this stage players form coalitions and agree on a long-term rent sharing. Recall that by assumption some players can not commit and will recontract. As a result, only credible players can cooperate in coalitions, whereas the others will act as singletons. Anticipating their future payoff  $E[\psi_{S^I}^S(k^*)]$  members of coalitions  $S^I$  invest as to maximize:

$$\pi^*(S^I; \Pi^I) = \max_{k(S^I)} E[\psi_{S^I}^S(k^o + k(S^I) + k(\Pi^I \setminus S^I))] - I(k(S^I)) \quad (4)$$

here  $k^o$  is the initial capacities of the network.<sup>14</sup> Coalitions choose investments  $k^*(S^I)$  taking into account the decisions of the outsiders  $k^*(\Pi^I \setminus S^I)$ . To find the Nash equilibrium  $S^I$  for a given partition  $\Pi^I$  we solve the optimization problem (4) simultaneously for all coalitions embedded in  $\Pi^I$ . Repeating the procedure for all feasible  $\Pi^I$  we define the partition function:

$$w^I(S^I; \Pi^I) = \pi^*(S^I; \Pi^I) \quad (5)$$

Finally, we proceed with the solution of the bargaining game and determine how the rents are shared, i.e. find  $(E[\psi^I], p(P^I))$ .<sup>15</sup>

### 3.4 The solution concept

As we have already mentioned in Introduction, for our analysis, we adopt the solution concept, which has been recently proposed by Maskin (2003). In this approach, the players negotiate sequentially and the game is described in an extensive form. To introduce the extensive form Maskin (2003) uses the random order bargaining procedure developed by Weber (1988). The procedure

<sup>13</sup>For more detail see Kreps, Scheinkman (1983).

<sup>14</sup>Since a coalition can invest in any pipeline in the network, in contrast to  $k^*(S)$ , the vector  $k^*(S^I)$  can include capacities which are not under the control of  $i \in S^I$  at the second stage.

<sup>15</sup>Note that for the players who can not commit  $E[\psi_i^I] = E[\psi_i^S(k^*)] - I(k(\{i\}))$ .

is commonly used in cooperative game theory to represent bargaining, in particular to depict the general solution concept - Shapley value (1952). Under random order bargaining, coalition formation is considered as a sequential process. The players enter the bargaining process one by one in some order  $\theta = \{\dots, \theta_i, \dots\}$ , where  $\theta_i$  gives the entry number position of a player  $i$ . When player  $i$  enters the game, he observes a partial partition  $P$  formed by his predecessors  $j : \theta_j < \theta_i$ . At each node of the game, represented by the pair  $(P, i)$ , the new coming player chooses to join one of the existing coalitions or to start a new one. We will use a subscript to point out, which coalition the player joins: if player  $i$  joins  $S \in P$  then  $P \rightarrow P_{S \cup i}$ . If the player sets a new coalition  $P \rightarrow P \cup \{i\}$  we write  $P_{\{i\}}$ . Decisions on allocation are irreversible so that coalitions may only increase but not break apart. Hereafter, we will distinguish terminal partitions, formed by all the players  $P^N : \bigcup_{k=1}^{|P^N|} S_k = N$ , where  $|\cdot|$  is a cardinality, and partial partitions  $P$  formed by  $K \subseteq N$ .<sup>16</sup>

Given the allocation, the player is assigned a payoff. The payoff depends on the partition function, the order, and the partial partition  $P$ , which has formed:  $\psi_i(w, \theta, P)$ . We will distinguish the equilibrium payoff vector  $\psi^*(w, \theta)$  under the terminal equilibrium coalition structure  $P^*(\theta)$  given the order  $\theta$  and a payoff vector  $\psi(w, \theta, P^N)$  corresponding to some terminal partition  $P^N$ . To simplify notation we will omit the argument  $w$  in the payoff function assuming that a partition function is given.

The overall solution is obtained as a randomization over all possible  $\theta$ . Following Maskin (2003), we assume the orders of players to be equally probable  $Pr(\theta) = 1/|N|!$  and calculate the expected payoff vector of the game as:

$$E[\psi_i^*] = \sum_{\theta \in \Theta} \frac{1}{|N|!} \cdot \psi_i^*(\theta) \quad (6)$$

The probability distribution for the equilibrium partition is obtained as the probability weighted collection of  $P^*(\theta)$ .

Maskin (2003) accepts the fundamental assumption that players cooperate within and play non-cooperatively across coalitions. This property is expressed in the first axiom:<sup>17</sup>

(i) the sharing of joint profits within each coalition should be Pareto optimal for any terminal partition

$$\sum_{i \in S} \psi_i(P^N) = w(S; P^N) \text{ for } \forall S, P^N \quad (7)$$

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<sup>16</sup>In this section we will consider the general solution concept without reference to a particular stage of the model. To simplify the notations, we will omit upper indexes.

<sup>17</sup>In the course of the paper we change the original sequence of the axioms by Maskin (2003). We start with the axioms describing the properties of the solution common to other PFF solutions, and then formulate the specific to Maskin (2003) ones.

where  $\psi(P^N)$  is the payoff vector given some partition of players  $P^N$ . The axiom requires that coalitions distribute their profits fully among their members. This condition is sometimes called "budget-balancing" and was justified by Aumann and Dreze (1974).

Maskin (2003) applies backward induction to solve the extensive form game. To that end, he formulates the second axiom, which states consistency, or sequential rationality, of the equilibrium outcome as follows:

- (ii) for any  $i$  and partial partition  $P$ , if  $i$  is assigned to  $S \in P$  and  $S \cup i \subseteq S^*$  where  $S^* \in P^*(\theta)$ , then the equilibrium partition  $P^*(\theta)$  resulting from  $P$  is the same as the one resulting from  $P_{S \cup i}$ , and so is the payoff vector  $\psi^*(P^*(\theta)) = \psi^*(P_{S \cup i}^*(\theta))$

There remain two questions to be answered: to which coalition is a player allocated and how are payoffs to players determined? The answers are specific to Maskin (2003) and are the essence of his solution. By his third axiom, Maskin (2003) demands efficiency of a players' allocation: a player joins the coalition such that his allocation has the greatest impact on the profit of this coalition. The impact of the player's allocation also reflects externalities. It is a relative measure and corresponds to a particular alternative. Namely, it is presented by the gross marginal contribution of a player to a coalition  $S$  given the alternative coalition  $S'$ , that is how much a profit of  $S$  changes if the player instead of joining this coalition will join  $S'$ :  $w(S \cup i; P_{S \cup i}^N) - w(S; P_{S' \cup i}^N)$ . A positive contribution creates incentives for coalitions to attract the player, since they will lose otherwise.

The partition function  $w$  gives the worth of coalitions under all possible terminal partitions  $P^N$ . Yet, to continue with axioms for allocation and assignment of payoffs we need to know the values of the coalitions embedded in partial partitions. We denote them  $\tilde{w}(S; P)$ . Since we solve the game backwards, we can determine the allocation and the payoff of the last player  $l : \theta_i < \theta_l$  for  $\forall i$  for all possible  $P^N$  knowing only  $w$ . Then, we can reduce a game to  $N \setminus l$ , and calculate the values of coalitions in partitions  $P^N \setminus l$ . For the coalitions not including  $l$  the value is  $\tilde{w}(S; P^N \setminus l) = w(S; P^N)$ , for the coalition  $S' \in P^N : l \in S'$  the  $w(S'; P^N \setminus l) = w(S'; P^N) - \psi_l(P^N)$ . Generalizing, for a partial partition  $P$  formed by  $j : \theta_j < \theta_i$  we obtain:

$$\tilde{w}(S; P) = w(S^N; P^N) - \sum_{i \in S^N \setminus S} \psi_i \quad (8)$$

where  $S^N \in P^N$  and  $S \subseteq S^N$

In words, the value  $\tilde{w}$  can be interpreted as an undistributed profit of a coalition  $S$ .

Now we proceed with the third axiom

- (iii) each player is allocated to the coalition  $S \in P$ , to which his gross marginal contribution is greatest

$$\tilde{w}(S \cup i; P_{S \cup i}) - \tilde{w}(S; P_{S' \cup i}) \geq \tilde{w}(S'' \cup i; P_{S'' \cup i}) - \tilde{w}(S''; P_{S \cup i}) \quad (9)$$

$$\forall S'' : S'' \neq S \quad S' = \arg \max_{S''} [\tilde{w}(S'' \cup i; P_{S'' \cup i}) - \tilde{w}(S''; P_{S \cup i})] \quad (10)$$

In words, of all possible alternatives  $S''$  one finds the one  $S'$ , compared to which the allocation of  $i$  to  $S$  has the largest impact (10). The coalition  $S$  attracts the player if the contribution of the player to  $S$  with respect to  $S'$  is greater than to  $S'$  with respect to  $S$ .

In a competition for a new player coalitions should be able to offer him at least as much as the others are ready to pay. In the result, payoffs of players are defined as follows:

(iv) every player earns his opportunity payoff, i.e. the second greatest gross marginal contribution

$$\psi_i(P, \theta) = \tilde{w}(S' \cup i; P_{S' \cup i}) - \tilde{w}(S'; P_{S \cup i}) \quad (11)$$

### 3.5 Equilibrium

According to Maskin (2003) for any superadditive game  $(N, w)$  the solution, satisfying axioms (i)-(iv) exists. This claim is proved as Theorem 1. The proof is done by construction and is based on the case of  $|N| = 3$ . Maskin (2003) asserts that for  $|N| > 3$  the result of the theorem holds as well. However, we have found that, in general, this is not true. We present our finding in the following proposition:

**Proposition 1** *For a game in partition function form  $(N, w)$  with  $|N| > 3$ , a solution pair  $(E[\psi^*], p(P^*))$  satisfying axioms (i)-(iv) may not exist*

We prove this proposition by an example, which is given in Appendix 9.

Furthermore, in Theorem 2, Maskin (2003) claims that if all externalities are non-positive the solution  $(E[\psi^*], p(P^*))$  fulfilling the axioms (i)-(iv) is unique. Once again the proof is done by construction for  $N = 3$ . In the course of our analysis we have revealed that this claim is not necessarily valid for  $|N| > 3$ . We state this result as

**Proposition 2** *For a game in a partition function form  $(N, w)$  with  $|N| > 3$  in which all externalities are nonpositive, that is for any  $S, S_k$ , and  $S_j$ :  $w(S; P) \neq w(S; P')$ , where  $P \setminus S_k \setminus S_j = P' \setminus \{S_k \cup S_j\}$ , the solution  $(E[\psi^*], p(P^*))$  may not be unique*

A proof by example is provided in Appendix 10.

In our study the number of players  $N = 6$  and, according to propositions (1) and (2) we may encounter the problems of non-existence and multiplicity. Non-existence of an equilibrium is a conceptual problem since in this case it is not clear what the outcome of the game is.<sup>18</sup> There is no

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<sup>18</sup>Note, however, that the solution of Maskin (2003) is not the only one susceptible to the non-existence problem. There are many others solutions, in particular, those based on a Nash equilibrium, in which an equilibrium may not exist.

reasonably simple way to show in which cases an equilibrium always exists in general.<sup>19</sup> Fortunately, in our calculations we have not encountered the problem of non-existence. This is largely due to a specific property of our game. We formulate this finding in

**Proposition 3** *For a game in a partition function form  $(N, w)$  with  $|N| > 3$  the solution  $(E[\psi^*], p(P^*))$  exists, if at any node  $(P, i)$  of the game there exist at most one coalition  $S \in P$  for which it matters to which of the alternative coalitions the new player is going to be allocated, so that*

$$\tilde{w}(S; P_{S' \cup i}) \neq \tilde{w}(S; P_{S'' \cup i})$$

and for all other  $\tilde{S} \neq S$  it holds true that

$$\tilde{w}(\tilde{S}; P_{S' \cup i}) = \tilde{w}(\tilde{S}; P_{S'' \cup i})$$

We prove proposition (3) and discuss in more detail the properties of our game in Appendix 11.

As multiple equilibria are concerned, they do occur in the course of our analysis. However, this does not present a severe problem since the choice of an equilibrium does not change the outcome of the game. In our analysis, multiplicity occurs only when the contribution of a player to all coalitions is zero. According to axiom (iii) the player can then be allocated to any coalition. As the number of such cases is small, we have been able to check that the allocations and the payoffs of the other players do not depend on the allocation of that player. To avoid additional complexity in computations we apply a simple tie-breaking rule: we assign such a player to the coalition formed by the first player.

## 4 Quantitative Assumptions

To calculate profits of gas supply and to solve the investment game numerically we have to make assumptions on demand and supply functions as well as on investment costs of the pipeline projects. In this section we introduce these assumptions in turn.

### 4.1 Demand

The market, we have in mind, is represented by the core members of the European Union – EU15, who's share in total European gas consumption is over 90%.<sup>20</sup> We refer to these countries as Western Europe. The import demand of Western Europe is covered by Algeria, Norway, LNG

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<sup>19</sup>See Ikonnikova and Willems (2007) for a further discussion on possible refinements to overcome the problem of non-existence and sufficient conditions for an equilibrium to exist.

<sup>20</sup>EU15 includes Austria, Denmark, Finland, France, Germany, Greece, Ireland, Italy, Luxembourg, Netherlands, Portugal, Spain, Sweden, Switzerland, and the UK. We look at the market formed by these countries as a whole, without specifying demand for each individual country.

suppliers, and the Former Soviet Union. The demand for FSU natural gas depends on preferences for natural gas, the prices of other exporters and substitutes such as oil and gas from competitors, preferences for diversifying energy supply, the cost of transporting gas within Western Europe etc. Unfortunately, data on gas prices and consumption in Western Europe are too poor to allow an econometric estimation of this function. The bulk of the deliveries is under a small number of long-term contracts, the details of which are not made public. Available data on gas prices largely reflect oil-price movements. They are of little relevance for the buyers tied up in these agreements. Moreover, many of the important structural determinants of demand for FSU gas, such as environmental concerns, preferences for diversity of supplies, turbine technology etc., are changing fast. For simplicity, we take a linear specification of the demand function and make ‘plausible assumptions’ for the parameters.<sup>21</sup> From figures on current and future marginal cost of non-Russian suppliers provided in Observatoire Mediterranéen de LEnergie (2002) we estimate a residual demand for the Former Soviet gas.

Based on data for the future consumption we calibrate the demand and supply functions as to fit the capacities and investment patterns observed. We adjusting ”the future demand” function to the planned development of the network, namely the building of NEGP. We obtain the demand with the intercept equal to 190 and the slope of 0.3. We present further details in Appendix 8.

## 4.2 Supply

Costs of supply consist of production and transportation costs. Production cost account for gas extraction and depend on terrain, climate conditions as well as infrastructure in place. The costs vary with fields and are specified for each producer individually. We assume a linear increasing function for the average production cost  $ac_i(q) = m + c \cdot q$ , we use the subscript to refer to the producer. Production costs tend to increase as production from old low cost fields declines and new, more expensive fields have to be developed. Hence, we again derive different functions depending on a time frame.

After 2000 the growth of domestic as well as of European gas demand led to increases in production. Old fields, like Medvezhye were in depletion and new gas fields have to be tapped. The costs of production from recently developed fields such as Zapolyaroye are estimated in the range of 20 to 30 \$/tcm ( World Bank (2005)). The cost of  $m_t = 20$  \$/tcm can also be taken as a ”sensible” figure for gas production in Turkmenistan. In ”The strategy for the Russian gas industry development” (2004) it is suggested that the costs of Russian gas may increase up to 40 \$/tcm, if fields like Stockman or Yamal have to be developed.

Further, according to scenarios of Russia energy sector development presented by World Bank (2003), we estimate the slope of the production cost function for Russia as  $c_r = 0.4$ . For Turk-

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<sup>21</sup>The detailed description of how we derive the demand for gas from FSU is given in the Appendix 8

menistan Mavrakis&Thomaidis&Ntroukas (2006) provide data which give the slope of production cost for Turkmenistan  $c_t=0.35$ .

Transportation costs account for operation costs and gas losses. These costs depend on the length of a pipeline and specific features of the track. The operation costs consist of expenses on management and maintenance of pipelines and compressor stations  $m$  and gas losses  $g$ , that is the per cent of gas utilized by compressors on pumping to keep the pressure in pipelines. Costs grow with the supply distance  $d$ . For the onshore pipeline the loss factor is  $g = 0.25\%$  of gas per  $100km$ , for the high pressure underwater pipelines the figure is doubled  $g = 0.5\%$ .<sup>22</sup> The maintenance costs also differ for onshore and offshore pipelines. Here we assume  $m = 0.1\$/tcm \cdot 100km$  and  $m = 0.2\$/tcm \cdot 100km$ , respectively.<sup>23</sup>

The total cost of gas supply includes both production and transportation costs. For our analysis we derive a simplified formula of the total cost of supply. We take that the costs should include all the expenses on the way, namely gas consumption by compressor stations and operation costs.<sup>24</sup> Then, we obtain:

$$tc(q) = ((\frac{m_l}{g_l} + ac_i(q))e^{g_l \cdot d_l} - \frac{m_l}{g_l})q_l, \quad i \in \{r, t\}. \quad (13)$$

Note, transport cost parameters are specified for each pipeline  $l$ .

As we express all figures on an annual basis, we also annualize investment cost, which are usually given in total. We use the following formula:  $I_i = \frac{r \cdot \bar{I}_i}{(1 - (1+r)^{-t})}$ , where  $\bar{I}_i$  is the total investment per capacity. We take the real interest rate for investment to be  $r = 0.15$ . The lifetime of pipelines is taken to be  $t = 25$  years.

We distinguish two types of investment projects: projects to increase capacity of an installed pipeline and projects to build a new pipeline. The first type of projects include installation of extra compressor stations and can be completed within months. As for a new pipeline, it might take two or three years, before the pipeline goes into operation and can deliver gas. To take this delay into account we inflate the investment cost of new pipelines by 15%.

Table 1 gives the aggregate figures for supply and investment costs for the investment options under the consideration. The figures for supply costs are calculated for the total supply of one thousand cubic meter of gas. In the table we mark with a star new pipelines, for which we inflate

<sup>22</sup>See Oil, gas and coal supply outlook (1995) for further explanations of the transportation technology.

<sup>23</sup>Maintenance costs are estimated based on operation costs details provided by Frank Tauchnitz (Wintershall).

<sup>24</sup>With every additional 100km the expenses increase due to gas consumption by compressor stations and maintenance costs that we express as follows:

$$\frac{tc(q, d + \Delta) - tc(q, d)}{\Delta} = m + g \cdot tc(q, d) \quad (12)$$

Taking the limit, we obtain a differential equation. We solve the equation given that supply costs at the source ( $d = 0$ ) are equal to the production cost. For further details see Hubert, Ikonnikova (2003).

Table 1: Description of the links

Link	max capacity $k_l$ [bcm/a]	invest. cost $I_l$ [\$/tcm]	distance d[100km]	supply cost tc(1tcm)[\$]	countries, forming a supply chain
Ukold	70	sunk	16	17.2	Russia, Ukraine
Yamal1	28	16.1/sunk	16	17.2	Russia, Belarus
Upgrade	15	7.7	16	17.2	Russia, Ukraine
Yamal2*	$\infty$	15.2	16	17.2	Russia, Belarus
NEGP*	$\infty$	24.9	16	17.2	Russia
TCP*	30	23.7	38	15.0	Turkmen., Azerb.
Nabucco*	30	23.7	38	15.0	Turkmen., Iran

the values. The first two rows of the table describe the existing pipelines in Ukraine and Belarus. Their capacities are fixed and investment costs are sunk. But if we look backwards to when the first Yamal pipeline was built we find that the investment cost of Yamal 1 was equal to 16.1\$/tcm. The next two links are the extension of the first two pipelines: Upgrade of Ukrainian pipeline system and the second Yamal pipeline. These two investment projects are the cheapest investment options, as one may see from the second column of figures.

The second column shows that we limit the capacities of investment projects TCP, Upgrade and Nabucco. To install capacity over the given limits, one would need to invest in the extension of the connected transmission network, i.e. the pipeline system in East Europe and Turkey. New players will be involved and supply costs of the unit of quantity delivered to the market will soar. In contrast, the Yamal 2 and NEGP directly join with the European gas network. Europe is assumed to adjust the internal grid to the import needs on its own, so no restrictions are put on the pipelines going directly to the EU border or owned by the EU companies. We assume the length of all the pipelines delivering Russian gas to be roughly the same. It is true for all the pipelines except for Ukrainian system, which is about 400km longer. Hubert & Ikonnikova (2003) have checked that this assumption does not lead to significant change in results, while allows us to avoid additional complexity in calculations.

## 5 Results

Based on the quantitative assumptions presented in the previous section, we evaluate the partition functions  $w^I, w^S$ . From these we calculate the equilibrium coalition structures and the expected payoffs at the first and second stages. Finally, we solve for the equilibrium investments and find



the resulting supply quantities.<sup>25</sup> We make these calculations for the three scenarios, varying the assumption on who can commit to a long-term profit sharing. The first scenario is a benchmark case, in which we assume that all players can commit. In this case, the hold-up problem does not arise and the first best strategy is chosen. We call this scenario accordingly - "first best". In the second scenario, titled " $\{r, t\}$ ", we assume that only Russia and Turkmenistan have the ability to make credible long-term commitments, while the transiters are prone to renegotiate their payoffs, after the new capacities are in place. Our third scenario, labelled " $\{\emptyset\}$ ", reflects the situation, in which none of the players can commit. Table 2 and Table 3 present the results.

Table 2: Equilibrium investments, quantities, profits

scenario	extra capacity <sup>a</sup> [bcm/a]					$\sum_S q_S \parallel \sum_l \bar{k}_l$	$\sum_l I_l$	net profit <sup>b</sup>
	NEGP	TCP	Nab	Uup	Yam	[bcm/a]	\$bn	\$bn
first best <sup>c</sup>	0	0	0	15	28	141    141	0.5	16.3
$\{r, t\}$	105	0	0	0	0	141    203	2.6	14.0
$\{\emptyset\}$	87	30	30	0	0	141    245	3.6	12.9

<sup>a</sup> Besides, there are two existing pipelines  $k_{Ukold}=70$ bcm/a and  $k_{Yamal}=28$ bcm/a

<sup>b</sup> for demand  $p(q)=250-0.4q$  and supply costs  $ac_r=40+0.4q$  and  $ac_t=30+0.35q$

<sup>c</sup> when the grand coalition forms

Table 3: Expected payoffs in \$mln

	first best <sup>c</sup>		$\{r, t\}$		$\{\emptyset\}$	
	$\psi^I$	$\widetilde{\psi^S}$	$\psi^I$	$\widetilde{\psi^S}$	$\psi^I$	$\psi^S$
Russia	10.2	8.6	10.0	12.7	8.6	10.8
Turkmenistan	3.5	1.0	3.4	1.4	2.1	3.5
Ukraine	0.8	4.0	0.3	0.9	0.2	0.2
Belarus	0.6	2.3	0.2	0.4	0.2	0.2
Azerbaijan	0.7	0	0	0	0.9	0.9
Iran	0.7	0	0	0	0.9	0.9

For the first scenario we obtain that in equilibrium the grand coalition will be formed with a probability of 0.91 at the investment stage  $P^I = \{N\}$ . With a probability of 0.09 two competing coalitions will form  $P^I = \{\{r, b, u\}, \{t, a, i\}\}$ .<sup>26</sup> The grand coalition will install additional capacities so as to maximize the network profit and invests in the pipelines with the lowest capacity costs. As it is shown in the first row of figures in Table 2, the players will invest in 15 bcm/a of Upgrade and

<sup>25</sup>Calculations are performed with Mathematica 5.1 program. Files with results are available upon request.

<sup>26</sup>With the probability less than 1% Azerbaijan and Iran will be left outside the coalition.

28 bcm/a of Yamal2. With 43 bcm/a of extra capacity, the total capacity of the network is 141 bcm/a, which is equal to the profit maximizing supply quantity. Deducting annual investment cost in the amount of \$0.5bn, the players obtain a net profit of \$16.3bn. This profit is shared among the players according to  $\psi^I$  as given in the second column of Table 3. If competing supply chains are formed, the coalition  $\{r, b, u\}$  will invest in Upgrade and add 10bcm/a. The Caspian players will build both TCP and Nabucco with the total capacity of 60bcm/a. However, at the second stage, the grand coalition forms and the players use the capacities installed at the first stage efficiently and supply 141bcm/a. In the next subsection we will look in more detail, why competing supply chains may form although players can commit.

Now to justify our next scenario, we consider a thought experiment on what would happen if the players renegotiate after the capacities are installed. The second column of table 9, entitled  $\widetilde{\psi}^S$ , presents the result of such an imaginary ex post bargaining. One can see, that Ukraine and Belarus would benefit a lot from recontracting, since the additional capacities strengthen their bargaining position and enable them to extract more rent. Hence, in the absence of international institutions, which would enforce investment contracts, renegotiations are to be expected. This leads us to the next scenario.

## 5.1 Hold-up and distortions

Assuming that the transitters can not commit we obtain that at the first stage the partition  $P^I = \{\{r, t\}, \{a\}, \{b\}, \{i\}, \{u\}\}$  will form with probability 1. As the second row of Table 2 shows, the producers will not implement Upgrade and Yamal 2, but will invest in the direct offshore pipeline. The North European Gas Pipeline will be built with a capacity of 105 bcm/a. At the supply stage the grand coalition will form, with the probability 0.99, and the optimal supply quantities will again be 141 bcm/a. As a result, 62bcm/a of new capacity will be left idle. With total investment cost of \$2.6bn, the net network profit will be \$14.0bn, that is much less than in the first best case.

Hence, we obtain that the hold-up problem leads not only to underinvestment as commonly predicted, but also to overinvestment and excess capacities. The producers underinvest in cheap options in Ukraine and Belarus, and overinvest in NEGP. These "strategic distortions" of investments reflect the efforts of the producers to strengthen their bargaining position and gain leverage vis-a-vis unreliable transitters. NEGP will allow the producers to bypass all the transitters and hence, will grant them a great strategic advantage in bargaining.

To motivate the third scenario, we look at what would happen if the producers fall apart and recontract ex post. The fourth column in Table 3 gives the expected payoffs of the players in this situation. Since  $\psi_r^I < \widetilde{\psi}_r^S$  we conclude, that now it is Russia who has incentives to renege on the agreement.

This leads us to the scenario " $\{\emptyset\}$ " in which no player can commit. As the last row in Table 2

shows, in equilibrium NEGP, TCP, and Nabucco will be built with the capacity of 87 bcm/a, 30 bcm/a, and 30 bcm/a, respectively. We find that the players will form the grand coalition at the supply stage, with a probability of about 0.85. With a probability 15% two competing coalitions  $\{r, b, u\}$  and  $\{t, a, i\}$  will form. Columns five and six report the expected payoffs of the players. We obtain that in equilibrium only Russia and Turkmenistan will invest. Therefore, the expected payoffs at the supply and investment stages are the same for the transitters, while the payoffs of Russia and Turkmenistan are reduced at the investment stage by investment costs.

In the third scenario we again observe strategic distortions of investments, including underinvestment, overinvestment, and excess capacity. If the grand coalition forms at the supply stage, more than a half of the new capacities will not be used. If the Caspian players form a separate coalition, capacities of TCP and Nabucco will be fully used to compete with Russian supply. Two thirds of the capacities along the Baltic sea will be left idle. Hence, the more players are not able to commit, the larger overinvestments are and the less likely the grand coalition be formed.

Considering the aggregate network profits given in the last column of Table 2, we evaluate the costs of the lack of commitment. The inability of transitters to commit to long-term rent sharing results in the loss of \$2.3bn, as the investment costs soar by almost three times, from \$0.5bn to \$2.6bn. Altogether, the lack of commitment, combined with the absence of any enforcement institution leads to the waste of over \$3.1bn annually.

## 5.2 Formation of competing coalitions

As we have mentioned above, under "all can commit" scenario, competing coalitions may form. Now we look at this phenomenon in more detail. First, note that the probability 0.09 means, that the partition  $P^* = \{\{t, a, i\}, \{r, b, u\}\}$  forms in 66 orders  $\theta$  out of  $|N|! = 6!$ . We find that a distinguishing feature of these orders is that Russia enters the game only after all the Caspian players and Ukraine or Belarus have already arrived. Here, for illustrative purpose we consider the order  $\theta : (t, a, b, i, u, r)$ . Although the game is in fact solved backwards, we will discuss the moves in the natural order.

Azerbaijan as a second players has to choose whether to join Turkmenistan or start a new coalition. As we have already discussed in this section, a transiter always joins his complement producer, hence  $\{t, a\}$  forms. The next step, allocation of Belarus, is a turning point of a game. If Belarus joins  $\{t, a\}$ , the grand coalition will form, if the transiter starts a new coalition, then competing coalitions form. Let's assume that Belarus enters coalition  $\{t, a\}$ . By the next step Iran will join Turkmenistan, without whom it can not use his resources. Then Ukraine enters the game. We find that Ukraine will not join  $\{t, a, b, i\}$ , because the worth of its resources is diminished by presence of other transitters. Instead Ukraine will organize a new coalition, which Russia joins on the next step. Russia will prefer to join Ukraine, because as in the case of Ukraine, the value of

its resources is smaller in the presence of Turkmenistan. Even without Russia, Turkmenistan can supply its gas via TCP and Nabucco, whereas the worth of a coalition of Ukraine without Russia is zero. Hence, we calculate that Russia's contribution to  $\{u\}$  is larger than to  $\{t, a, b, i\}$ . To sum up, the partition  $\{\{r, u\}, \{t, a, b, i\}\}$  would form, if Belarus enters the existing coalition.

Coming back to the question of the allocation of Belarus, we see that if it joins  $\{t, a\}$ , its resources will be idle without Russia. Therefore, Belarus may prefer to start a new coalition. In this case, the choice of Iran does not change and  $\{t, a, i\}$  forms. When Ukraine enters the game, it will join Belarus. In principle, it may start a new coalition  $\{u\}$  or join  $\{t, a, i\}$ . Russia will prefer to follow Ukraine both in  $\{\{t, a, i\}, \{u\}, \{b\}\}$  in  $\{\{t, a, i, u\}, \{b\}\}$ . However, neither of the two alternatives will give Ukraine a larger payoff, than in the  $\{b, u\}$  case. Finally, Russia enters the game and joins the coalition of complement transitters forming  $P^* = \{\{t, a, i\}, \{r, b, u\}\}$ .

Similar reasoning is applied to  $\emptyset$  scenario. Competing coalitions form in 108 orders at the supply stage. In these orders Russia, as in the example discussed above, arrives after the Caspian players. Thus, we revealed that the outcome of the game depends on the worth of resources of a player in the presence of other players.

### 5.3 Conclusions

In this paper we have developed a framework for the analysis of endogenous coalition formation and multilateral bargaining in an environment with externalities. We applied our study to analyze the Eurasian gas supply network. Since there are no international institutions which could enforce contracts between the countries involved in the network, we assumed that a commitment problem may arise. Our calculations demonstrate that the countries have incentives to hold-up in order to extract higher profits.

We looked at three different scenarios, varying the assumption on the players' ability to commit. Our results support the assumption that investments are mainly driven by strategic considerations and the desire to strengthen the bargaining position. We have shown that the "hold-up" problem may lead to underinvestments as well as overinvestments and excess capacities. The players underinvest in capacities of unreliable parties and overinvest in capacities which strengthen their bargaining position.

Applying the model to the Eurasian gas supply network we succeeded in providing a rationale for observed investment patterns. We find that the ability to commit prevails over investment costs. In our analysis we obtain that whenever there is a possibility that Ukraine and Belarus will recontract, the North European Gas Pipeline will be built. The disputes between Russia and Ukraine and Belarus questioned the credibility of these countries and led to strategic distortions in investments: underinvestments in the upgrade of the Ukrainian system and the Yamal 2 pipeline. Both projects have been abandoned in favor of the expensive Baltic pipeline. The fact that investment in NEGP

is under its way confirms our results. However, as to the amount for overinvestment our predictions appear to be too large. This result can be explained by the static nature of our model.<sup>27</sup> Recall that in our study we assume that the countries can invest, and hence, change their bargaining position, only once.

Furthermore, according to our results, the larger the number of players who can not commit, the larger is the overinvestment. If none of the players can commit, NEGP, TCP, and Nabucco will be built. This finding also corresponds with reality. When relations between Turkmenistan and Russia were bad, Turkmenistan worked out projects to bypass Russia. It signed a series of tentative agreements with the potential transiters, namely Turkey, Azerbaijan, and Iran, and even started to build sections of TCP in Georgia with massive support of the United States. However, after Russia has made price concessions and agreed to transit Turkmen gas, Turkmenistan slowed down the realization of its plans. Our calculations suggest that the only way to prevent TCP and Nabucco if Russia credibly commits to transit Turkmen gas. Otherwise, the Caspian producers will build the pipelines bypassing Russia, in spite of all the difficulties, if Russia does not prove its ability to commit.

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<sup>27</sup>See Hubert and Suleymanova (2006) for more details.

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## 8 Appendix

In this section we describe the procedure used to estimate the demand for FSU gas. As mentioned in section 4, we derive the residual demand function based on European gas consumption data and on information on supply quantities and costs of all European exporters. We take that consumption of gas  $Q$  is exogenously given and use the figures from BP Annual Energy Report (2005) and International Gas Union Report (2006). The information on capacities and marginal costs  $mc$  of all exporters are taken from Observatoire Mediteranen de L'Energie(2003).

We obtain the import demand for gas in Western Europe by deducting from the consumption of a corresponding year, quantities  $Q^{dom}$  covered by domestic production of the EU countries. The rest  $Q^{im} =$

$Q - Q^{dom}$  is imported from the Former Soviet Union (FSU) producers and "other" exporters. To derive the residual demand for FSU gas we assume that a reduction of supply from FSU would lead to an increase in supply from "other" sources  $q_{-FSU}$ , rather than a change in total demand. Hence, the associated changes in price are determined by the cost of the marginal supplier who replaces, or is driven out by, FSU gas. Figure 2 illustrates the approach to estimation of the demand function. Suppose Russia supplies  $q_{FSU}$  out of

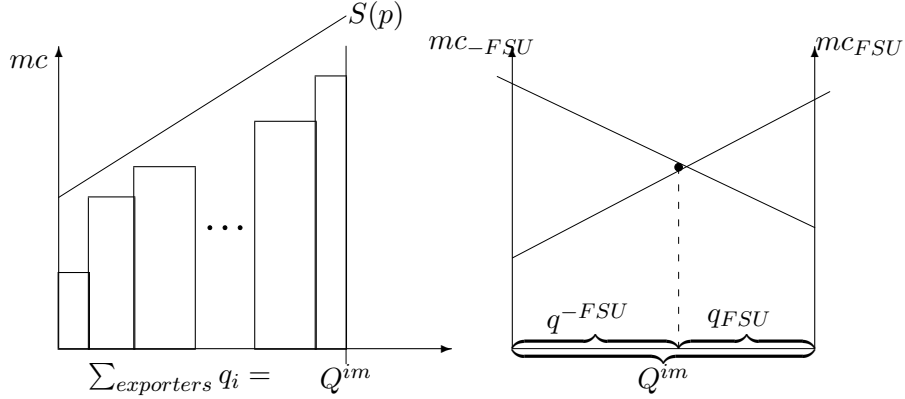


Figure 2: Estimating the demand for FSU gas

total  $Q^{im}$ . According to the data in Observatoire Mediteranen de L'Energie(2003), Nigeria LNG is the most expensive non-FSU gas producer. It supplies about 5 bcm/a. The second most expensive supplier is Oman with 1 bcm/a. Continuing down to the cheapest exporter, we end up with Algeria. If Russia increased its supply it would squeeze out the most expensive competitor first, the second most expensive exporter next and so on. Thus, we derive the demand for FSU gas as  $q_{FSU} = Q^{im} - q_{-FSU}(mc)$ .

The gas market is not perfectly competitive and the price for gas includes a substantial mark up on marginal cost. To obtain a realistic picture of the price for FSU gas we inflate the marginal cost by a mark-up of 20%. Finally, assuming a linear form of the inverse residual demand function, we estimate the parameters of the demand for FSU gas. For all three time perspectives we obtain price elasticities at equilibrium consumption around - 3.5. The high elasticity of demand reflects the flexibility of the European buyers in the choice of a producer. The obtained elasticity is close by its value to the estimates for the European market provided in Boots, Rijkers, and Hobbs (2004).

## 9 Appendix

In this section we prove proposition 1 providing an example of a superadditive game  $(N, w)$  in which the solution of Maskin (2003) does not result in any equilibrium. We consider a game of four players  $N = \{a, b, c, d\}$ . Let the players arrive to the game in the natural order  $\theta: (a, b, c, d)$  and when player  $d$  enters the game, he meets a coalition structure  $\{\{a\}, \{b\}, \{c\}\}$ . For simplicity we will omit additional brackets and write  $P = \{a, b, c\}$ . In principle, player  $d$  can be allocate to any of the three coalitions (players), or start a new coalition. To determine the equilibrium allocation we must apply axiom (iii) of Maskin (2003). According to this axiom, the player is allocated to the coalition to which his gross marginal contribution is

the largest. Let the values of the partition function be the following:

$$\begin{aligned}
w(a; \{a, b, c, d\}) &= 3 \\
w(b; \{a, b, c, d\}) &= 3 \\
w(c; \{a, b, c, d\}) &= 3 \\
w(d; \{a, b, c, d\}) &= 1 \\
w(ad; \{ad, b, c\}) &= 5 \\
w(bd; \{a, bd, c\}) &= 5 \\
w(cd; \{a, b, cd\}) &= 5 \\
w(b; \{ad, b, c\}) &= 1 \\
w(c; \{a, bd, c\}) &= 1 \\
w(a; \{a, b, cd\}) &= 1 \\
w(c; \{ad, b, c\}) &= 2 \\
w(a; \{a, bd, c\}) &= 2 \\
w(b; \{a, b, cd\}) &= 2
\end{aligned}$$

First, we notice that the game is superadditive that is for any  $S_i$  and  $S_j$  the following holds  $w(S_i; P) + w(S_j; P) \leq w(S_i \cup S_j; P_{S_i \cup S_j})$ :

$$\begin{aligned}
\forall S \neq d \text{ such that } S \in \{a, b, c, d\} : w(S; \{a, b, c, d\}) = 3 \quad w(d; \{a, b, c, d\}) = 1 \\
w(S \cup d; P_{S \cup d}) = 5 > 3 + 1
\end{aligned}$$

The superadditivity implies that player  $d$  will not start a new coalition, since his contribution to any coalition is greater than his stand alone value. Let's show that  $d$  also can not be allocated to  $a$ ,  $b$ , or  $c$ :

(i)  $d$  can not be allocated to  $a$ . We find that

$$w(bd; \{a, bd, c\}) - w(b; \{ad, b, c\}) > w(cd; \{a, b, cd\}) - w(c; \{ad, b, c\}) \quad 4 > 3$$

this means that coalition  $a$  will compete for player  $d$  with coalition  $b$ . We check that

$$w(ad; \{ad, b, c\}) - w(a; \{a, bd, c\}) < w(bd; \{a, bd, c\}) - w(b; \{ad, b, c\}) \quad 3 < 4$$

hence, player  $d$  can not be assigned to  $a$ .

(ii)  $d$  can not join  $b$ . The best alternative to  $b$  is  $c$ , because

$$w(ad; \{ad, b, c\}) - w(a; \{a, bd, c\}) < w(cd; \{a, b, cd\}) - w(c; \{a, bd, c\}) \quad 4 < 3$$

Moreover, the contribution of  $d$  to coalition  $c$  is greater than to  $b$

$$w(bd; \{a, bd, c\}) - w(b; \{a, b, cd\}) < w(cd; \{a, b, cd\}) - w(c; \{a, bd, c\}) \quad 3 < 4$$

therefore,  $d$  will not be allocated to  $b$

(iii)  $c$  can not hold  $d$ . Under the partition  $\{a, b, cd\}$  the relative contribution of  $d$  to  $a$  is larger than to  $b$

$$w(bd; \{a, bd, c\}) - w(b; \{a, b, cd\}) < w(ad; \{ad, b, c\}) - w(a; \{a, b, cd\}) \quad 4 < 3$$

this means that  $c$  has to compete with  $a$  to get  $d$ . In this case, however,

$$w(cd; \{a, b, cd\}) - w(c; \{ad, b, c\}) < w(ad; \{ad, b, c\}) - w(a; \{a, b, cd\}) \quad 3 < 4$$

so we infer that  $d$  will not join  $c$

Hence, we have shown that there is no equilibrium allocation for  $d$  and proposition 1 is proved.

## 10 Appendix

To prove proposition 2 we again take an example of four players  $N = \{a, b, c, d\}$ . We consider the game, which the players enter in natural order  $\theta: (a, b, c, d)$ . Let player  $d$  enter the game when the players are organized in partition  $P = \{a, b, c\}$ . Below we provide a partition function for which there exist more than one equilibrium allocation of  $d$ .

The values of the partition function be the following:

$$\begin{aligned}
 w(a; \{a, b, c, d\}) &= 4 \\
 w(b; \{a, b, c, d\}) &= 4 \\
 w(c; \{a, b, c, d\}) &= 4 \\
 w(d; \{a, b, c, d\}) &= 1 \\
 w(ad; \{ad, b, c\}) &= 5 \\
 w(bd; \{a, bd, c\}) &= 5 \\
 w(cd; \{a, b, cd\}) &= 5 \\
 w(b; \{ad, b, c\}) &= 3 \\
 w(c; \{ad, b, c\}) &= 2 \\
 w(c; \{a, bd, c\}) &= 2 \\
 w(a; \{a, bd, c\}) &= 3 \\
 w(a; \{a, b, cd\}) &= 1 \\
 w(b; \{a, b, cd\}) &= 1
 \end{aligned}$$

We check that the game is superadditive:

$$\begin{aligned}
 \forall S \neq d \text{ and } S \in \{a, b, c, d\}: \quad w(S; \{a, b, c, d\}) = 4 \quad w(d; \{a, b, c, d\}) = 1 \\
 w(S \cup d; P_{S \cup d}) = 5 \geq 4 + 1
 \end{aligned} \tag{14}$$

Notice that all externalities are nonpositive: for any  $i \neq j$ :  $w(i; \{a, b, c, d\}) \geq w(i; \{jd, \dots\})$ :

$$\begin{aligned}
 w(a; \{a, b, c, d\}) = 4 &\geq w(a; \{a, bd, c\}) = 3 \\
 w(a; \{a, b, c, d\}) = 4 &\geq w(a; \{a, b, cd\}) = 1 \\
 w(b; \{a, b, c, d\}) = 4 &\geq w(b; \{ad, b, c\}) = 3 \\
 w(b; \{a, b, c, d\}) = 4 &\geq w(b; \{a, b, cd\}) = 1 \\
 w(c; \{a, b, c, d\}) = 4 &\geq w(c; \{ad, b, c\}) = 2 \\
 w(c; \{a, b, c, d\}) = 4 &\geq w(c; \{a, bd, c\}) = 2
 \end{aligned}$$

Thus, the merger of  $d$  and any player imposes a loss on a third party.

Now we proceed with the allocation of player  $d$ . Applying axiom (iii) of Maskin (2003), we compare the contribution of  $d$  to different coalitions.

(i)  $d$  can be allocated to  $a$ . We find that

$$w(bd; \{a, bd, c\}) - w(b; \{ad, b, c\}) < w(cd; \{a, b, cd\}) - w(c; \{ad, b, c\}) \quad 2 < 3$$

that means that coalition  $a$  will compete for player  $d$  with coalition  $c$ . Since

$$w(ad; \{ad, b, c\}) - w(a; \{a, b, cd\}) > w(cd; \{a, b, cd\}) - w(c; \{ad, b, c\}) \quad 4 > 3$$

according to the solution of Maskin (2003) player  $d$  can be allocated to  $a$ .

(ii)  $d$  can be allocated to  $b$ . We find that the best alternative to  $b$  is  $c$ , since

$$w(ad; \{ad, b, c\}) - w(a; \{a, bd, c\}) < w(cd; \{a, b, cd\}) - w(c; \{a, bd, c\}) \quad 2 < 3$$

We observe that the contribution of  $d$  to  $b$  is larger than to  $c$

$$w(bd; \{a, bd, c\}) - w(b; \{a, b, cd\}) > w(cd; \{a, b, cd\}) - w(c; \{a, bd, c\}) \quad 4 > 3$$

therefore, we conclude  $d$  can join  $b$ .

(iii)  $c$  can not hold  $d$ . Under the partition  $\{a, b, cd\}$  the contributions of  $d$  to  $a$  and  $b$  are equal

$$w(bd; \{a, bd, c\}) - w(b; \{a, b, cd\}) = w(ad; \{ad, b, c\}) - w(a; \{a, b, cd\}) \quad 4 = 4$$

In this case we should check both coalitions, whether  $d$  can join them

$$w(cd; \{a, b, cd\}) - w(c; \{ad, b, c\}) < w(ad; \{ad, b, c\}) - w(a; \{a, b, cd\}) \quad 3 < 4$$

$$w(cd; \{a, b, cd\}) - w(c; \{a, bd, c\}) < w(bd; \{a, bd, c\}) - w(b; \{a, b, cd\}) \quad 3 < 4$$

thus,  $c$  fails to attract  $d$  from both  $a$  and  $b$ .

According to the results of (i) and (ii), we have obtained that  $d$  can be allocated to both  $a$  and  $b$ . Hence, we have multiple equilibria.

## 11 Appendix

In this section we prove that proposition 2 provides a sufficient condition for an equilibrium under the solution of Maskin (2003) to exist.

Consider an arbitrary game  $(N, w)$  and fix some order  $\theta$ . Let's take an arbitrary node  $(P, i)$ , in which player  $i$  enters the game and observe partition  $P$  with coalitional profits described by function  $\tilde{w}$ . Assume that there is the only coalition  $S$  such that its worth depends on the allocation of  $i$ :  $\tilde{w}(S; P_{S' \cup i}) \neq \tilde{w}(S; P_{S'' \cup i})$  for any  $S', S'' \neq S$ .

Since the contribution of  $i$  to coalitions in  $P \setminus S$  is always the same, we can arrange these coalitions according to the contribution of  $i$  in ascending order. Denote by  $S'$  the coalition with the greatest contribution  $\tilde{w}(S' \cup i; P_{S' \cup i}) - \tilde{w}(S'; \cdot) \geq \tilde{w}(S'' \cup i; P_{S'' \cup i}) - \tilde{w}(S''; \cdot)$  where  $S'' \in P \setminus S \setminus S'$ . To prove the proposition it is enough to consider whether the player can be allocated to  $S'$  or  $S$ , since by our assumption  $S'$  can overbid all other coalitions  $P \setminus S \setminus S'$ .

(i) if the contribution of  $i$  to  $S$  under  $P_{S' \cup i}$  is smaller than the contribution of  $i$  to  $S'$ , then player  $i$  is allocated to  $S'$  according to axiom (iii), since

$$\tilde{w}(S' \cup i) - \tilde{w}(S') \geq \tilde{w}(S \cup i; P_{S \cup i}) - \tilde{w}(S; P_{S' \cup i}) \quad \forall S \in P \setminus S' \quad (15)$$

(ii) if the contribution of  $i$  to  $S$  under  $P_{S' \cup i}$  is greater than the contribution of  $i$  to  $S'$ , then player  $i$  is allocated to  $S$ , because

$$\tilde{w}(S \cup i; P_{S \cup i}) - \tilde{w}(S; P_{S' \cup i}) \geq \tilde{w}(S' \cup i) - \tilde{w}(S') \quad \forall S' \in P \quad (16)$$

Thus, we have shown that the equilibrium allocation exists and hence, proposition (3) is proved.

Now we use proposition (3) to explain why we do not encounter the problem of non-existence. First, notice that if the node  $(P, i)$  is such that  $|P| \leq 2$  following Maskin (2003) we can prove that an equilibrium exists. For the other nodes we distinguish two cases: (I) when  $i$  is a producer and (II) when  $i$  is a transiter.

(I) Suppose a producer enters the game. Since in our analysis we have only two producers two situations are possible: (i) the other producer has already arrived and (ii) the other producer will enter the game later.

(i) the producer can face the following coalitions: a coalition including the rival producer and coalitions consisting of transiter only. The value of the coalition with the other producer may depend on which alternative the producer selects. All coalitions containing only transiter are not affected by the choice of the producer, their value will be zero if the producer does not join them. Thus, there is only one coalition such that  $\tilde{w}(S; P_{S' \cup i}) \neq \tilde{w}(S; P_{S'' \cup i})$  and we can apply proposition 6.

(ii) if the other producer comes later, the present coalitions include only transiter. The value of coalitions with the transiter, who are complementary to the producer, does depend on which alternative the producer chooses. But in principle, the allocation of the producer may affect the allocation of the other producer and hence, it might matter for the transiter who are complementary to the other producer. If these transiter form one coalition or there is only one such transiter, we can use proposition 6. Otherwise, there are two coalitions for which the allocation of the producer might be relevant. Fortunately, even in this case we can use proposition 6, because

(a) If Russia enters the game and Turkmenistan follows, then the coalitions at question are Azerbaijan and Iran. These players are symmetric and the allocation of Russia affects them in a similar way, therefore it is enough to consider only one of them. If there is only one coalition is such that  $\tilde{w}(S; P_{S' \cup i}) \neq \tilde{w}(S; P_{S'' \cup i})$ , we can use proposition 6.

(b) If Turkmenistan enters the game and Russia follows, then the coalitions at question are Ukraine and Belarus. We find that the allocation of Turkmenistan does not change the preference of Russia on which transiter to join. Thus, for all coalitions which  $\tilde{w}(S; P_{S' \cup i}) = \tilde{w}(S; P_{S'' \cup i})$  and by proposition 6 the equilibrium exists.

(II) Now we look at the situation when a transiter enters the game. Here, we will distinguish three cases:

(i) both producers are present, (ii) a complementary producer is absent, and (iii) both producers are absent.

(i) in the presence of both producers the allocation of the transiter is relevant for at most two coalitions, those including the producers, since his contribution to any other coalition is zero. The situation reduces to  $P \leq 2$  and the result of Maskin (2003) can be used.

(ii) in this case we should take into account that the allocation of the transiter may change the allocation of the complementary producer, who comes later. In this respect, the allocation of the transiter may affect the value of the coalition including the other producer. Besides, the allocation choice matters for the other complementary transiter, if he is present. The other coalitions are irrelevant, their value is zero and we can neglect them. Hence, we obtain that only two coalitions are relevant and we again use the proof of Maskin (2003).

(iii) when both producers are absent, the observed coalitions consist of transiter. We are interested only in the case when there are three coalitions. The allocation of the transiter might matter only for the transiter complementary to the other producer. Since the allocation of the transiter may change the preferences of his complementary producer that, in turn, by (ii) of (I) can lead to the change in

the allocation of the other producer. However, as we have discussed in (ii) of (I), in this case the equilibrium will exist.