



Munich Personal RePEc Archive

Utilizing System Dynamics Models in Analyzing Macroeconomic Variables of Yemen

Mohamed, Issam A.W.

Al Neelain University, Khartoum, Sudan

2011

Online at <https://mpra.ub.uni-muenchen.de/31692/>
MPRA Paper No. 31692, posted 21 Jun 2011 13:36 UTC

Utilizing System Dynamics Models in Analyzing Macroeconomic Variables of Yemen

Professor Dr. Issam A.W. Mohamed¹

1. Abstract

The purpose of the System Dynamics method is to study the relationship between structure and behavior in non-linear, dynamic systems. In such systems, the significance of various structural components to the behavior pattern exhibited, changes as the behavior unfolds. Changes in structural significance modify that behavior pattern which, in turn, feeds back to change the relative significance of structural components. We develop a macroeconomic model through which we can study the characteristics of the feedback between structure and behavior. This model is based on multiplier-accelerator model, and inventory – adjustment model. This work is an extension of the work by Nathan Forrester on the use of basic macroeconomic theory to stabilize policy analysis. The design of a System Dynamics model begins with a problem and a time frame that contribute to the problem. They are listed and their structural relationships sketched the factors with particular attention to characterizing them as levels (or stocks) and rates (or flows) that feed or drain them. Levels and rates must alternate in the model; no level can control another without an intervening rate or any rate influence another without an intervening level.

2. Dynamic Hypotheses

The main assumption in the model is that exponential growth of oil production, GDP and other variables in the real life cannot continue forever. Exponential growth implies a constant doubling time. In all real systems, there will be limits, and when a system state approaches its limit, stress takes place in the system.

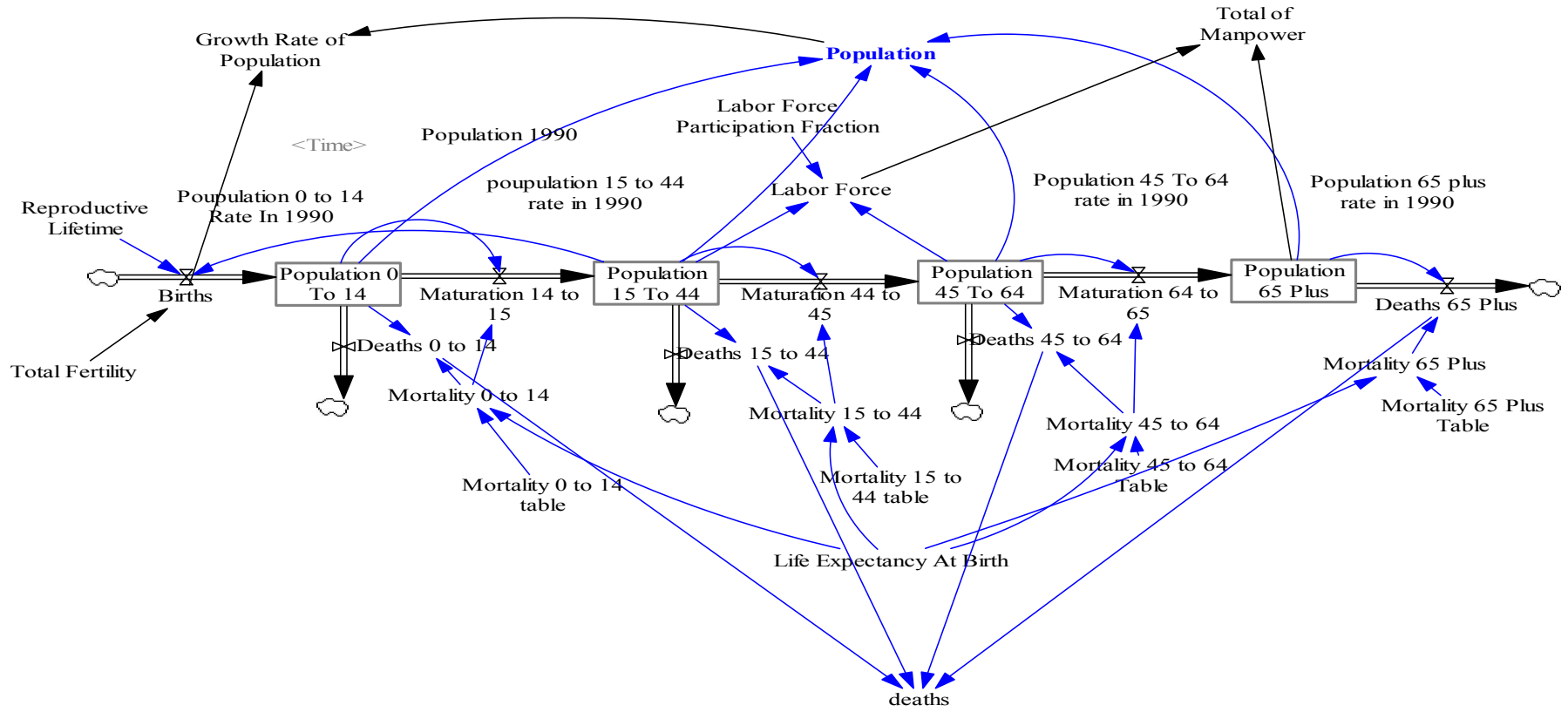
3. The Model

INITIAL TIME = 1990

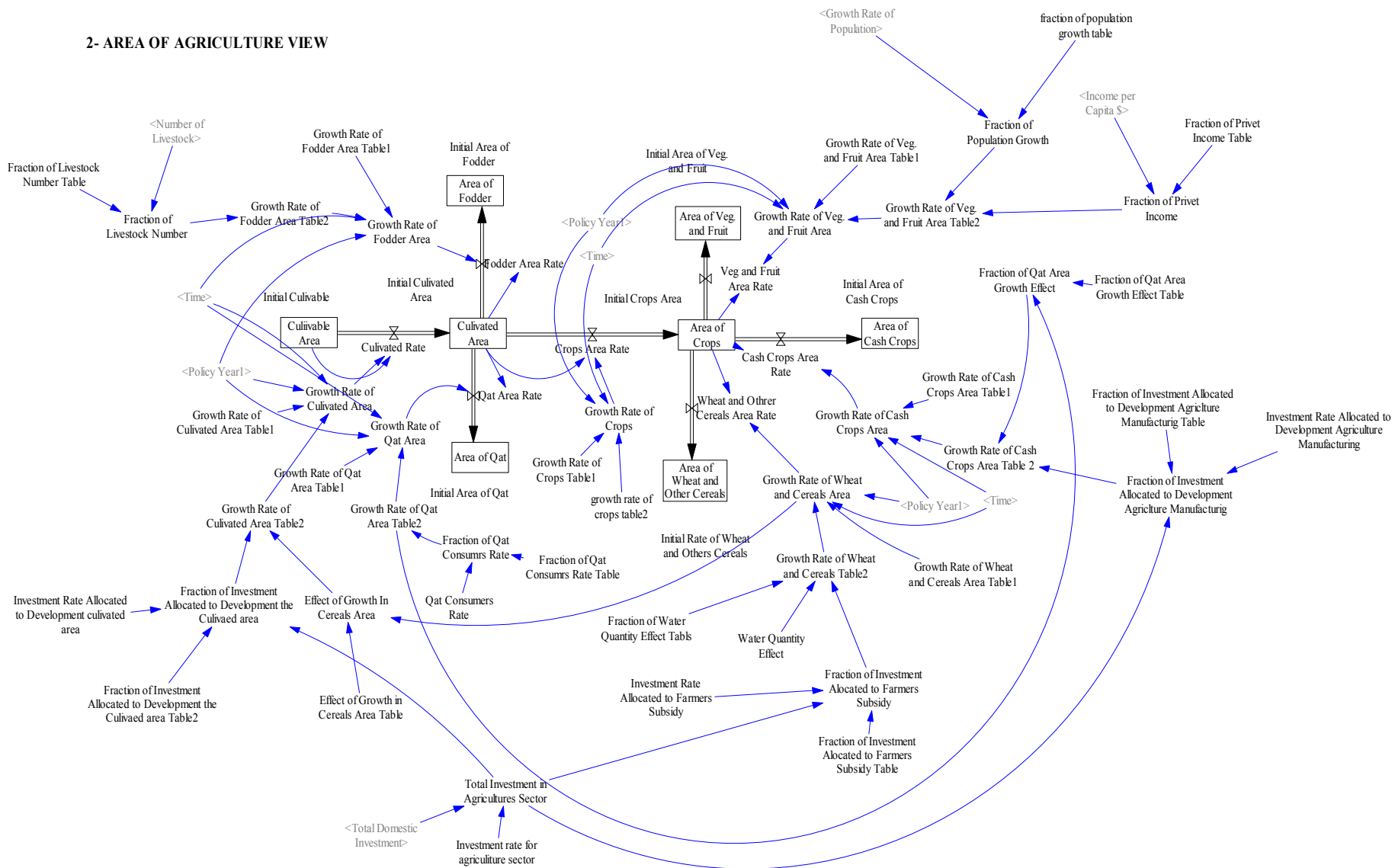
FINAL TIME = 2020 , TIME STEP = 1 YEAR

¹ Professor of Economics, Alneelain University, Khartoum-Sudan. P.O. Box 12910-11111.
issamawmohamed@hotmail.com

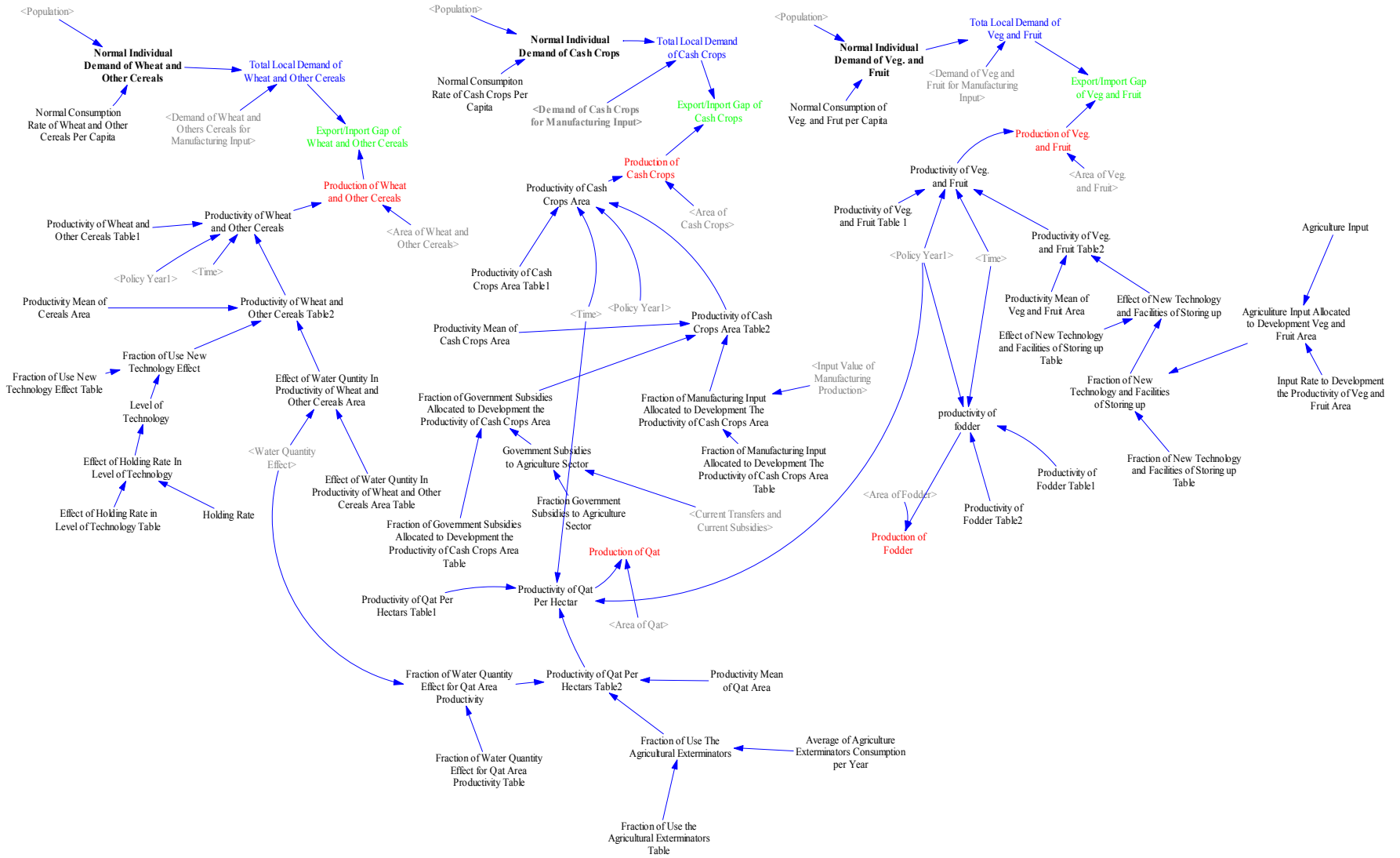
1- POPULATION VIEW



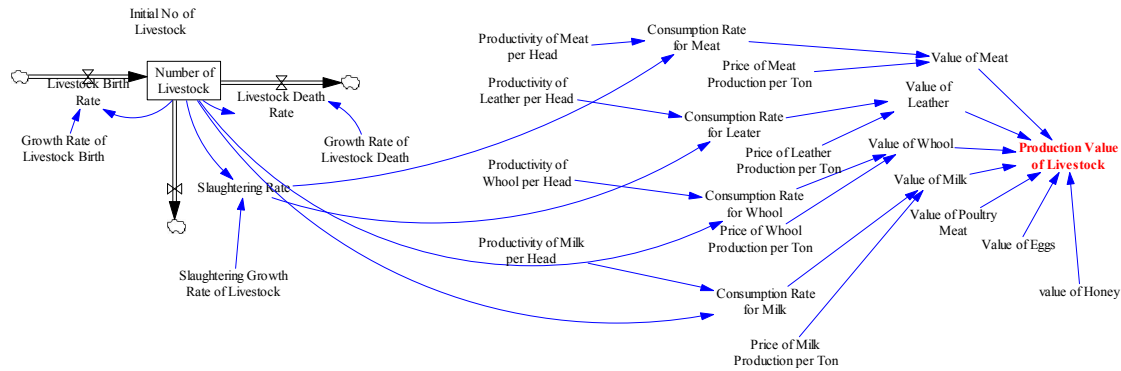
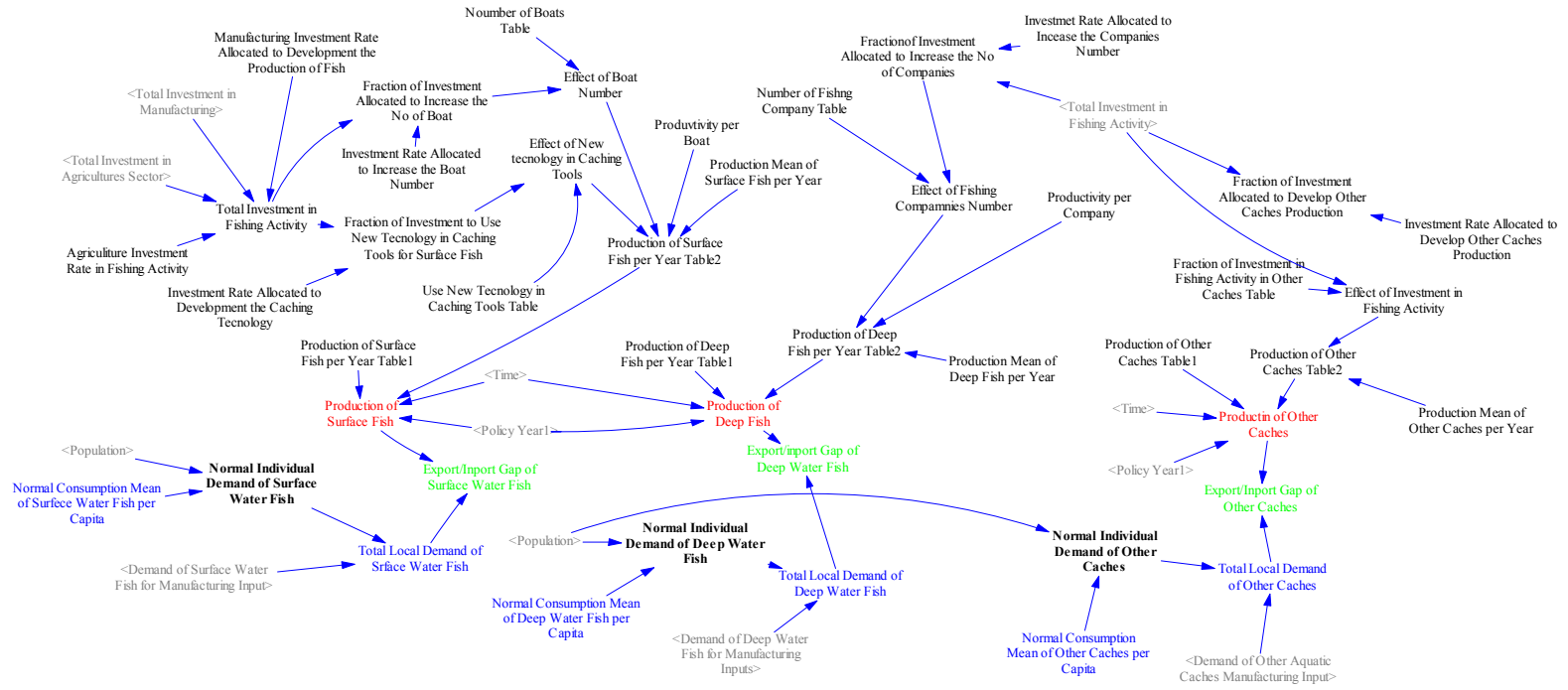
2- AREA OF AGRICULTURE VIEW



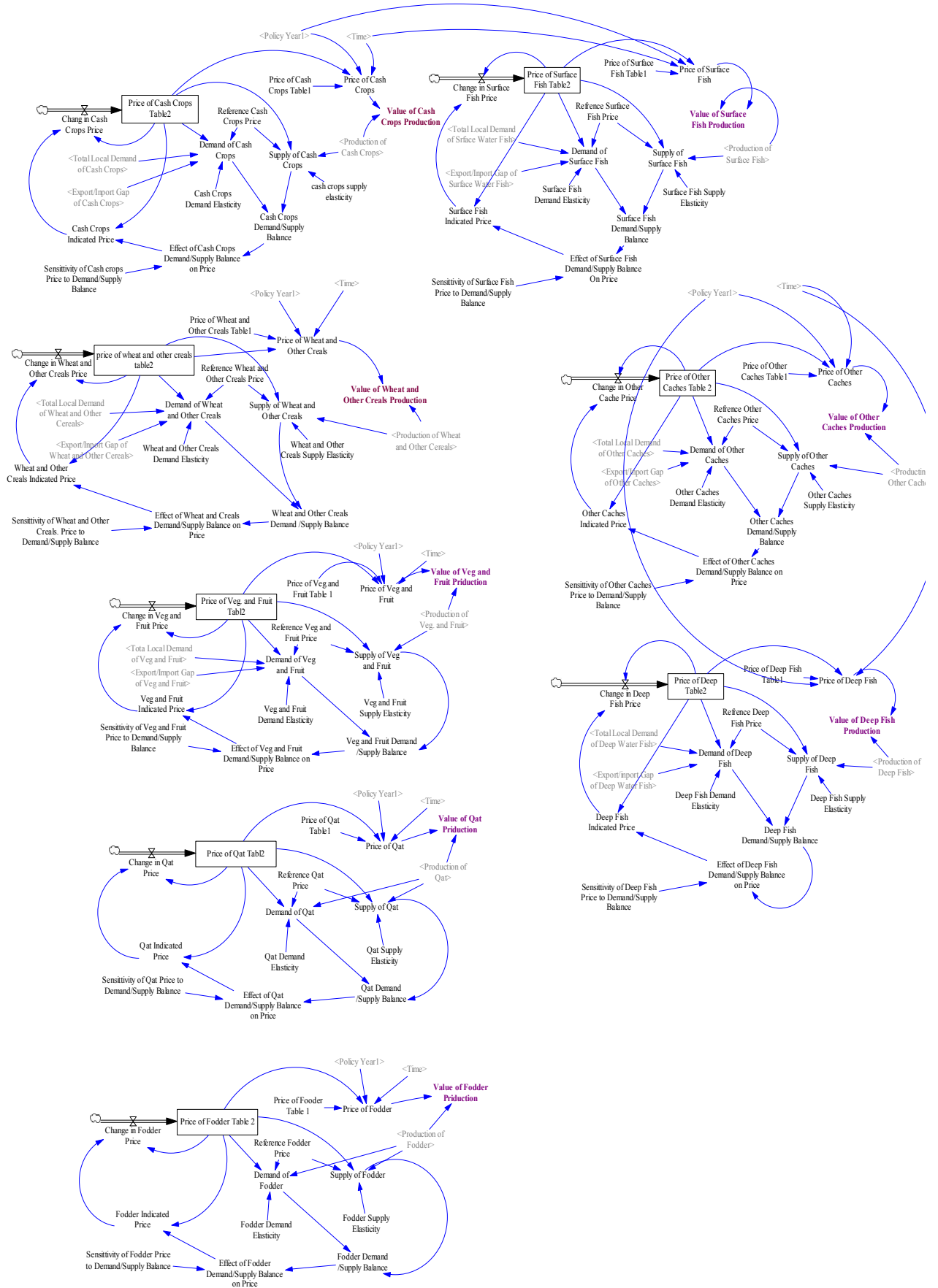
3- CROPS PRODUCTION VIEW



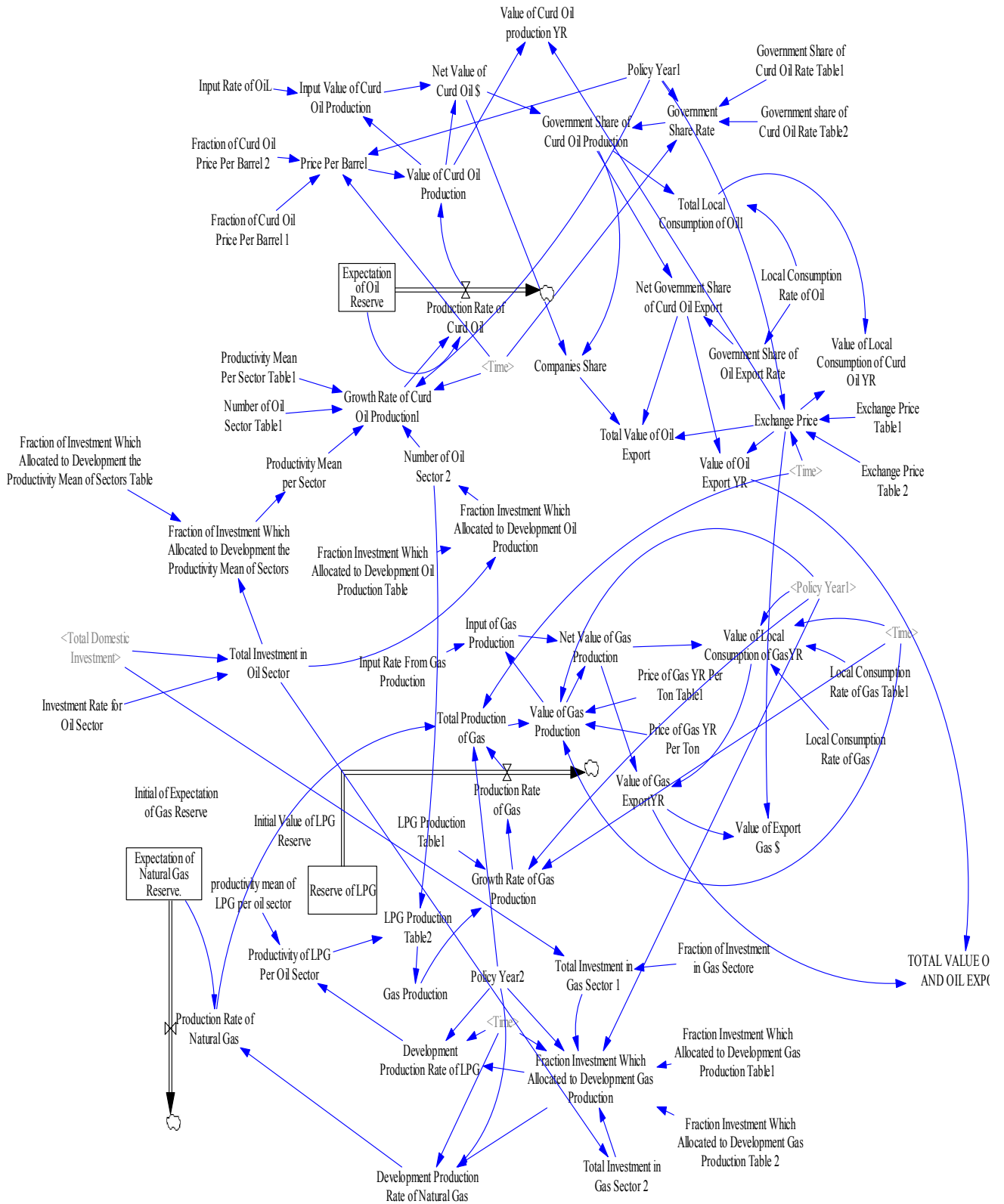
4- FISHING PRODUCTION VIEW



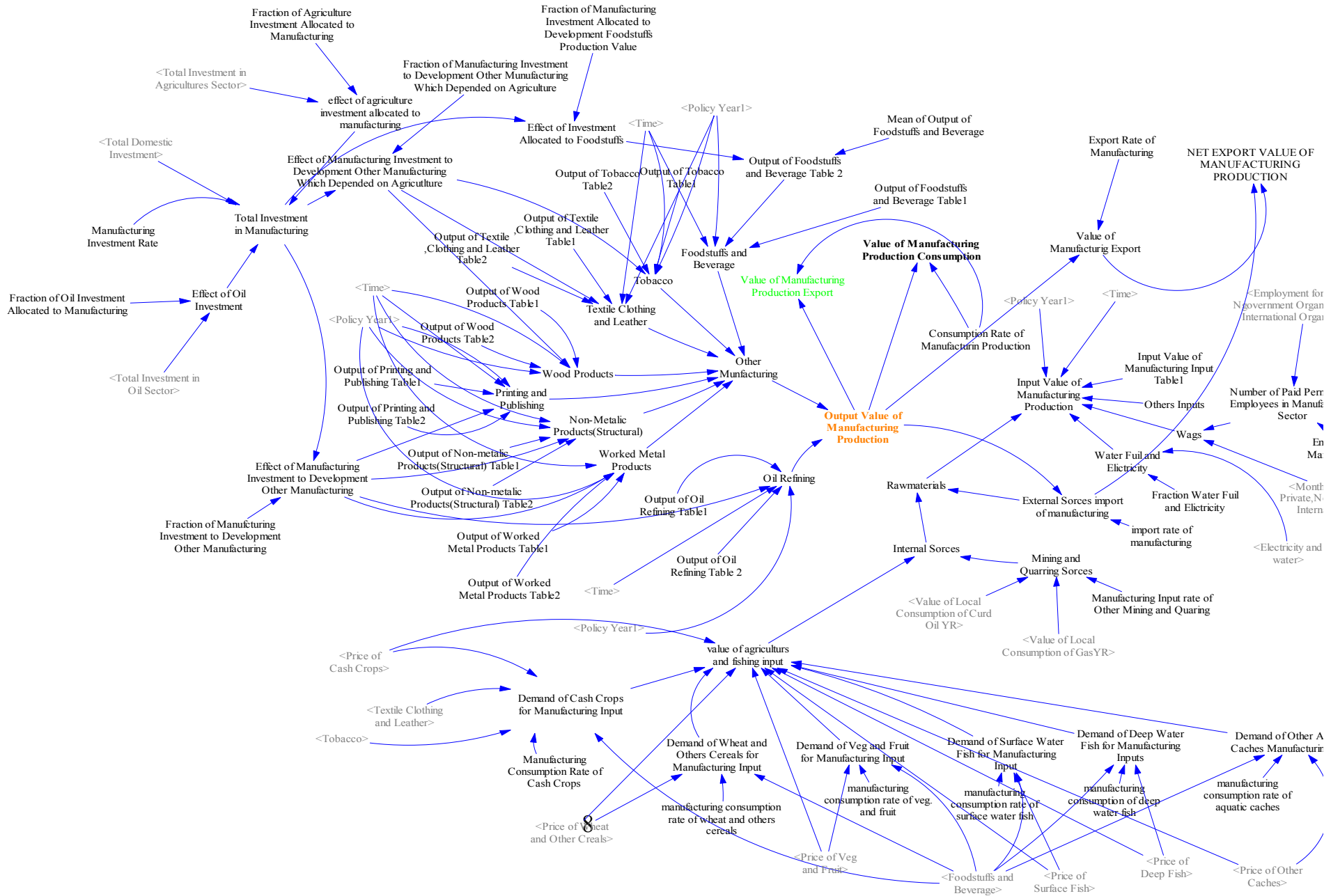
5- Equilibrium Price and Value of Crops View



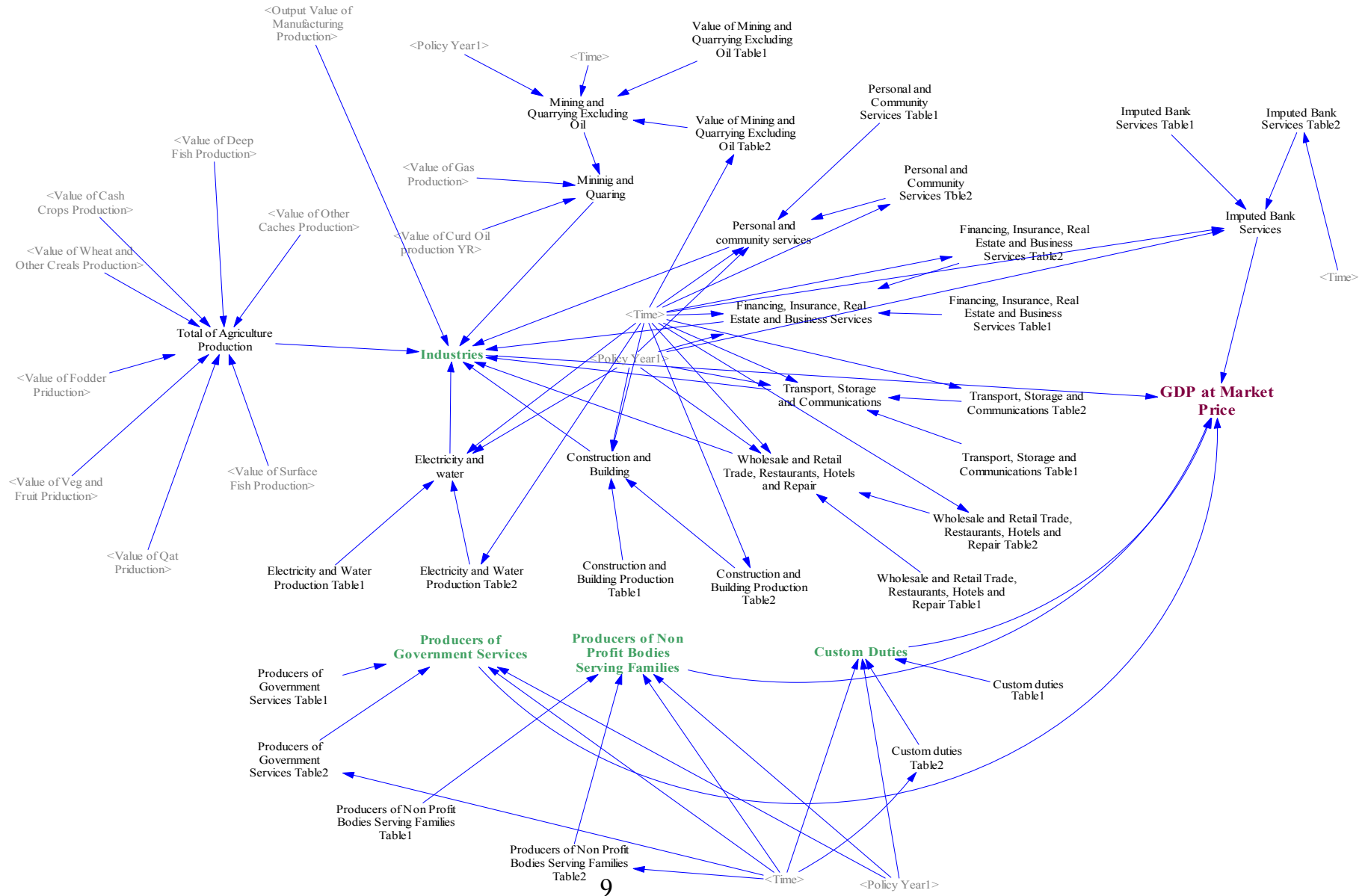
6- Oil and Gas Production View



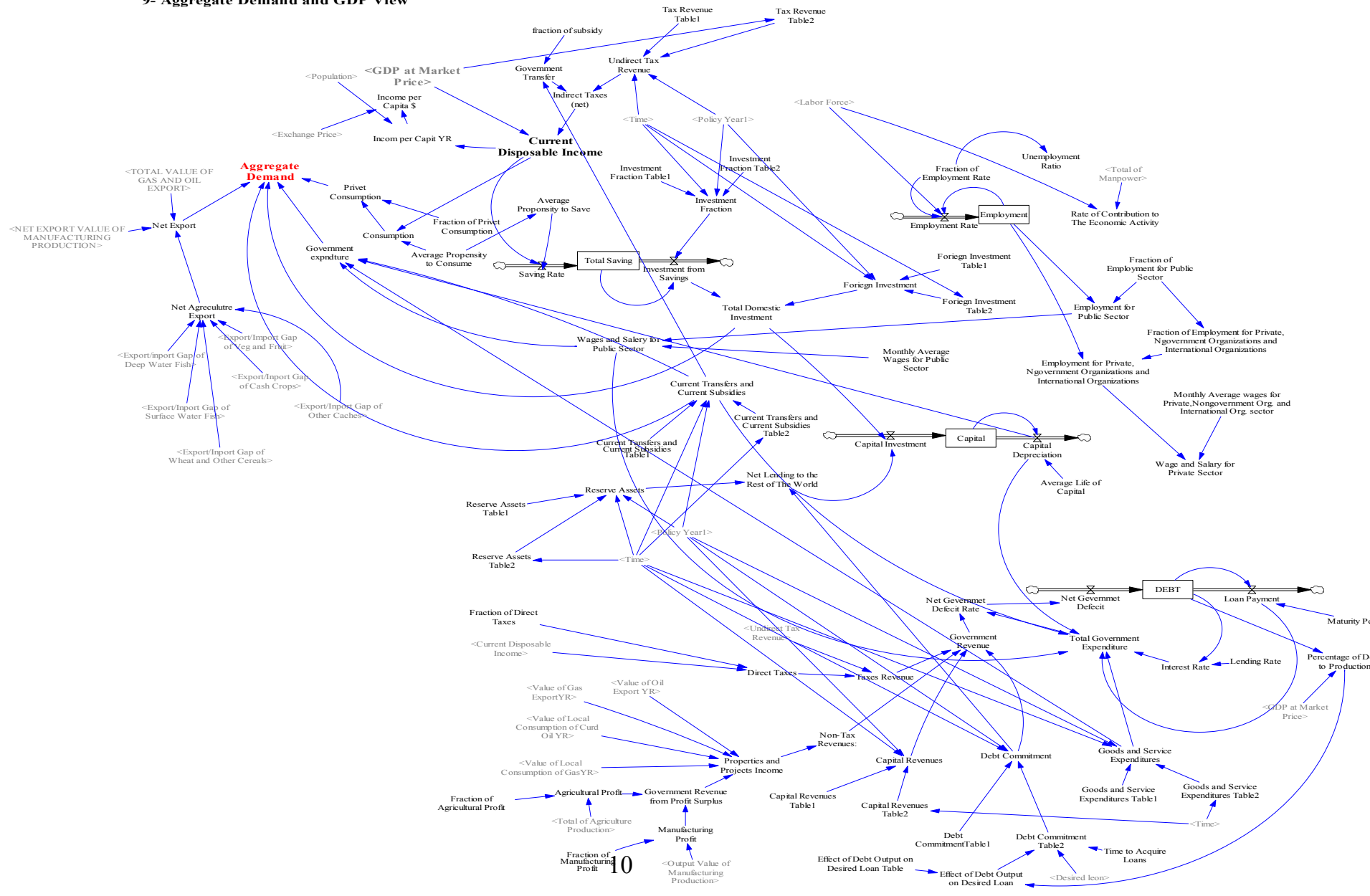
7- Manufacturing Production View



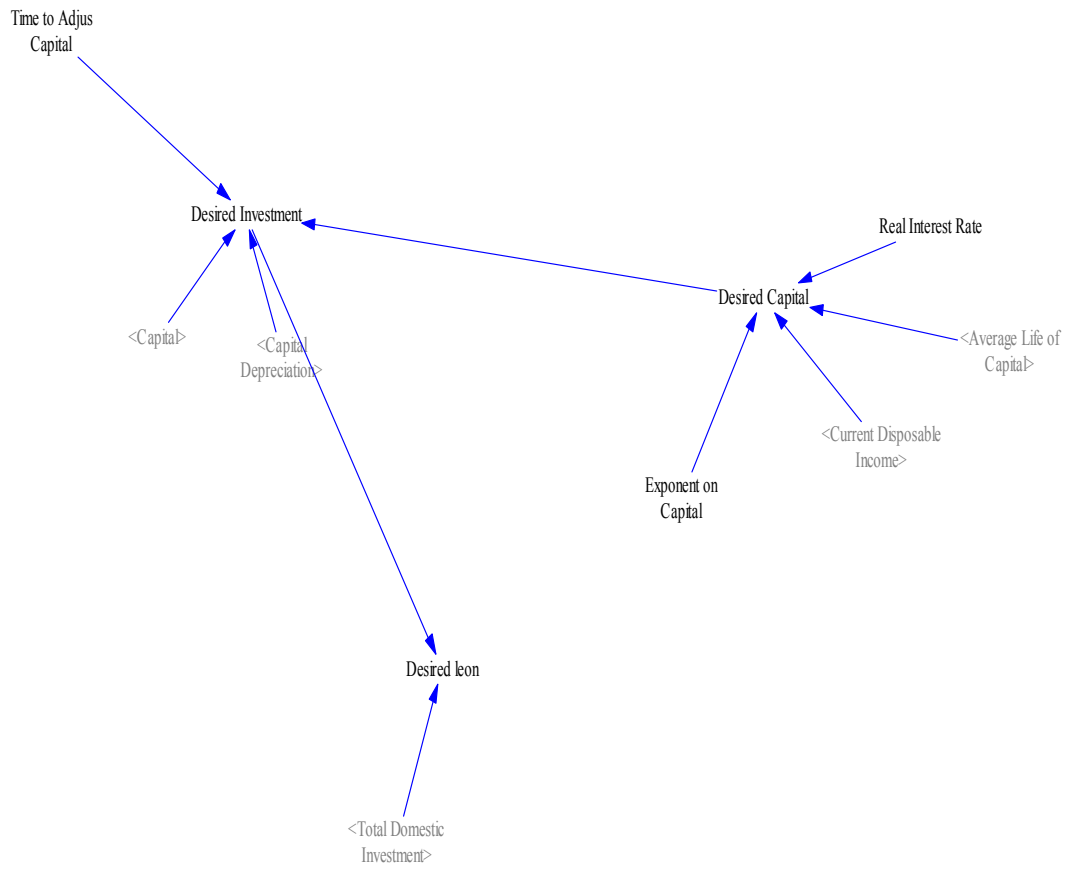
8- Total Production View



9- Aggregate Demand and GDP View



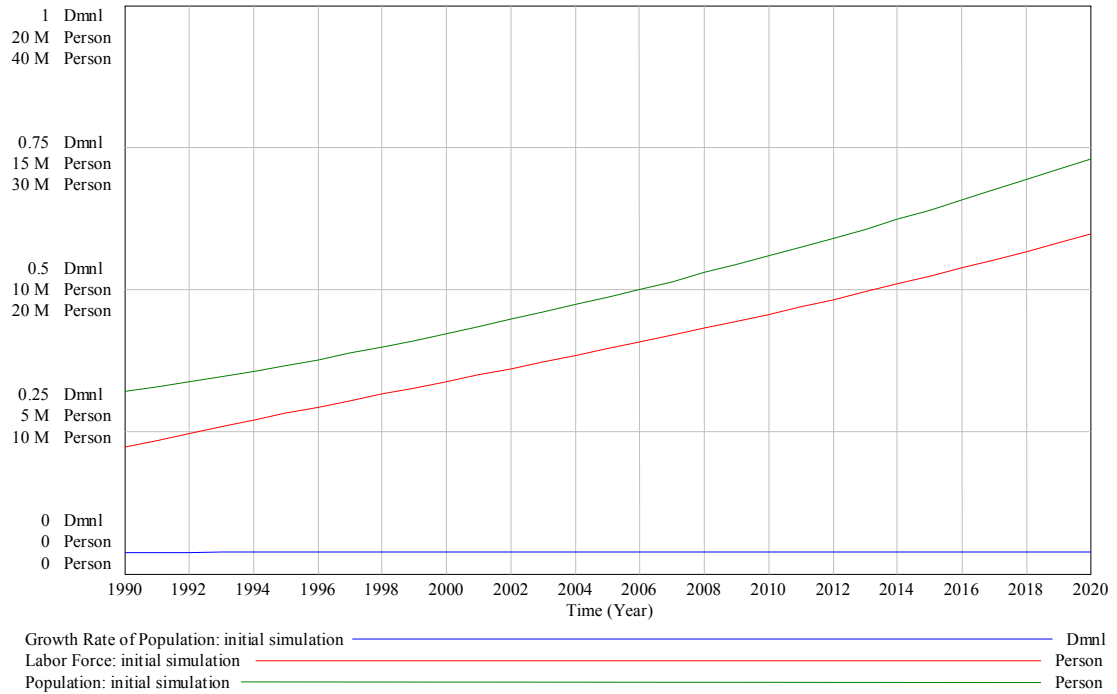
10- Desired View



4. Initial Simulation

It is a state of the system before our policies through 1990-2020

Figure (6-1) Population, Labor Force and Growth Rate of Population



The figure shows growth of population, Labor Force and Growth Rate of Population through 1990-2020 in initial state of the system.

$$\xi_t = \sum_1^n \xi_{nt}, n=1,2,..,4 \text{ see appendix(1)}$$

$$\xi_{1t} = \int_{t_0}^t (b - d - m_{1t})dt + i_1$$

$$\xi_{2t} = \int_{t_0}^t (m_{1t} - d_{2t} - m_{2t})dt + i_2$$

$$\xi_{3t} = \int_{t_0}^t (m_{2t} - d_{3t} - m_{3t})dt + i_3$$

$$\xi_{4t} = \int_{t_0}^t (m_{3t} - d_{4t})dt + i_4$$

$$\frac{\partial \xi_{1t}}{\partial t} = b - (d_{1t} + m_{1t}) = [F * \xi_{2t} * 0.5 / RL] - [(\xi_{1t} * mo_{1t}) + (\xi_{1t} * \frac{(1 - mo_{1t})}{15})]$$

$$\frac{\partial \xi_{2t}}{\partial t} = m_{1t} - (d_{2t} + m_{2t}) = \frac{\xi_{1t} * (1 - mo_{1t})}{15} - \left[(\xi_{2t} * mo_{2t}) + \frac{\xi_{2t} * (1 - mo_{2t})}{30} \right]$$

$$\frac{\partial \xi_{3t}}{\partial t} = m_{2t} - (d_{3t} + m_{3t}) = \frac{\xi_{2t} * (1 - mo_{2t})}{30} - \left[(\xi_{3t} * mo_{3t}) + \frac{\xi_{3t} * (1 - mo_{3t})}{20} \right]$$

$$\frac{\partial \xi_{4t}}{\partial t} = m_{3t} - d_{4t} = \frac{\xi_{3t} * (1 - mo_{3t})}{20} - (\xi_{4t} * mo_{4t})$$

$$b = F * \xi_{2t} * 0.5 / rl$$

Where

ζ_{nt} = population number

F = Total fertility = 5.8 child/wn

i_n = Initial value of population, $n=1,2,..,4$

m_{nt} = Maturation rate, $n=1,2,..,4$, $t=1,2,3,.....,30$

mo_{nt} = Mortality fraction

n = Age group

t = Time, (1990-2020)

d = death rate

b = birth rate

RL = Reproductive Lifetime = 30 years

Table (1) Result of Initial Simulation of Population View

| Time (Year) | Growth Rate of Population (person) | Labor Force (person) | Population |
|-------------|---------------------------------------|----------------------|------------|
| 1990 | 0.0362015 1.28086e+007 | 4.44635e+006 | |
| 1991 | 0.0370693 1.31423e+007 | 4.69488e+006 | |
| 1992 | 0.037761 1.34957e+007 | 4.93718e+006 | |
| 1993 | 0.0383056 1.38674e+007 | 5.1744e+006 | |
| 1994 | 0.0387281 1.42561e+007 | 5.40761e+006 | |
| 1995 | 0.0390499 1.46609e+007 | 5.63772e+006 | |
| 1996 | 0.0392891 1.50809e+007 | 5.86559e+006 | |
| 1997 | 0.0394609 1.55153e+007 | 6.09195e+006 | |
| 1998 | 0.039578 1.59637e+007 | 6.31748e+006 | |

| | | |
|------|---------------------------|--------------|
| 1999 | 0.039651 1.64255e+007 | 6.54279e+006 |
| 2000 | 0.0396888 1.69006e+007 | 6.76845e+006 |
| 2001 | 0.0396987 1.73886e+007 | 6.99496e+006 |
| 2002 | 0.0396867 1.78893e+007 | 7.22279e+006 |
| 2003 | 0.0396578 1.84027e+007 | 7.45236e+006 |
| 2004 | 0.039616 1.89288e+007 | 7.68409e+006 |
| 2005 | 0.0395646 1.94675e+007 | 7.91833e+006 |
| 2006 | 0.0395064 2.0019e+007 | 8.15545e+006 |
| 2007 | 0.0394434 2.05833e+007 | 8.39577e+006 |
| 2008 | 0.0393775 2.11607e+007 | 8.6396e+006 |
| 2009 | 0.03931 2.17513e+007 | 8.88725e+006 |
| 2010 | 0.0392421 2.23554e+007 | 9.13898e+006 |
| 2011 | 0.0391745 2.29731e+007 | 9.39509e+006 |
| 2012 | 0.039108 2.36049e+007 | 9.65584e+006 |
| 2013 | 0.0390431 2.4251e+007 | 9.92148e+006 |
| 2014 | 0.0389802 2.49118e+007 | 1.01923e+007 |
| 2015 | 0.0389195 2.55875e+007 | 1.04684e+007 |
| 2016 | 0.0388613 2.62787e+007 | 1.07503e+007 |
| 2017 | 0.0388056 2.69856e+007 | 1.10379e+007 |
| 2018 | 0.0387525 2.77086e+007 | 1.13317e+007 |
| 2019 | 0.0387021 2.84483e+007 | 1.16319e+007 |
| 2020 | 0.0386543 2.9205e+007 | 1.19386e+007 |

Figure (2-5) Cultivable Area, Cultivated Area and Cultivated Rate

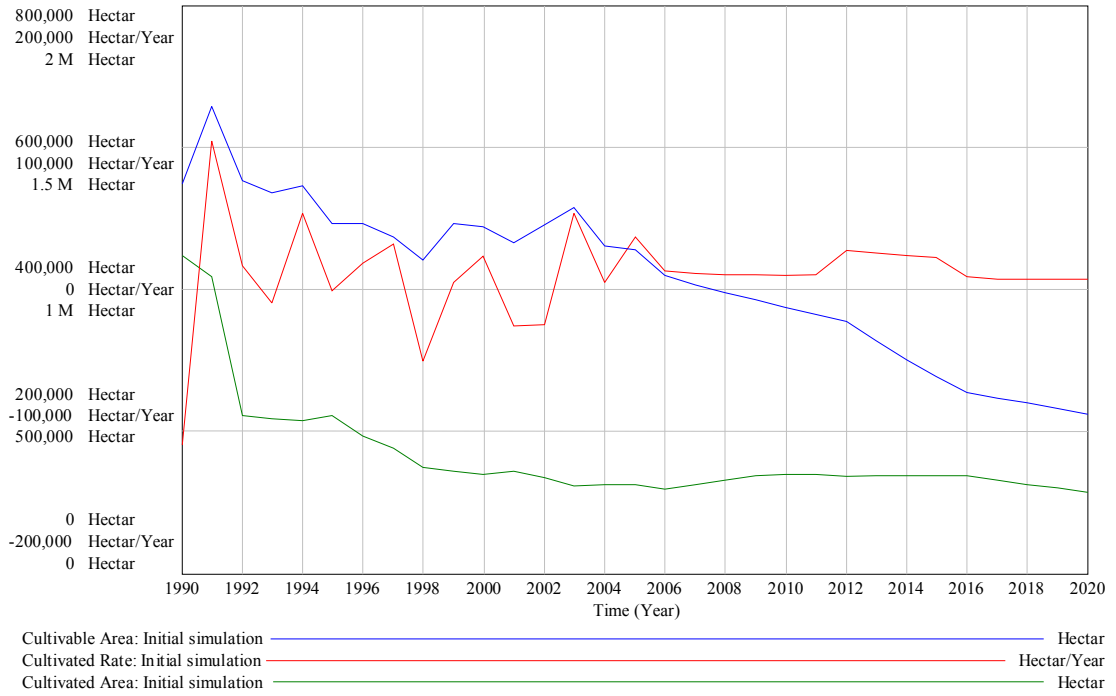


Figure (2-5) Cultivated Area, Crops, Qat, Fodder Area

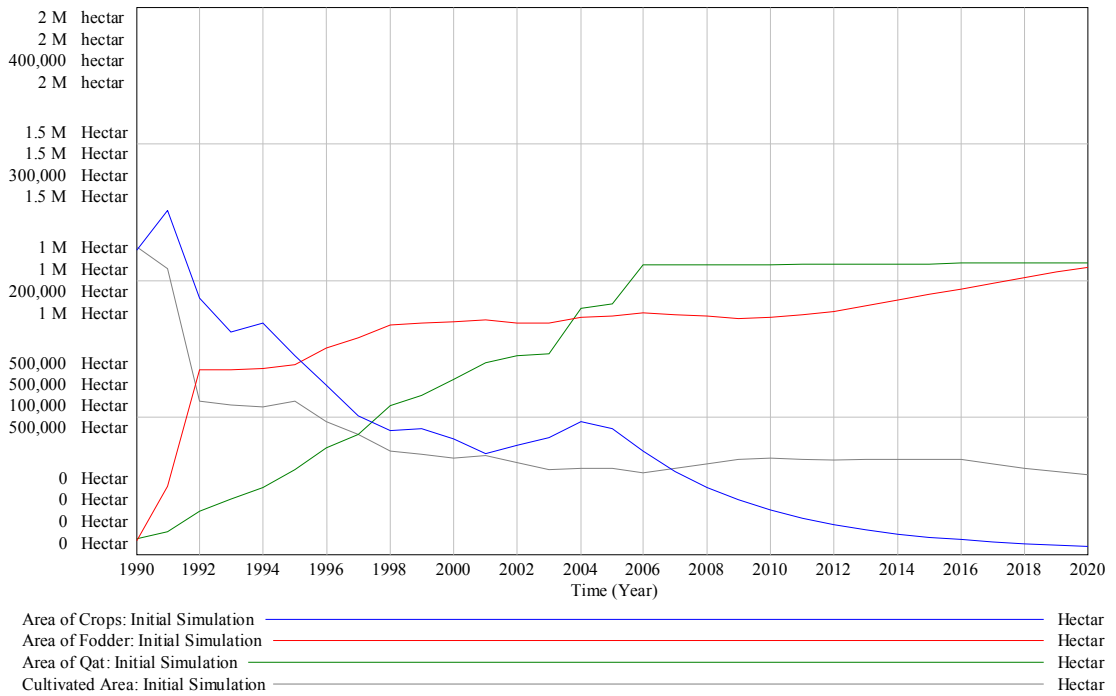
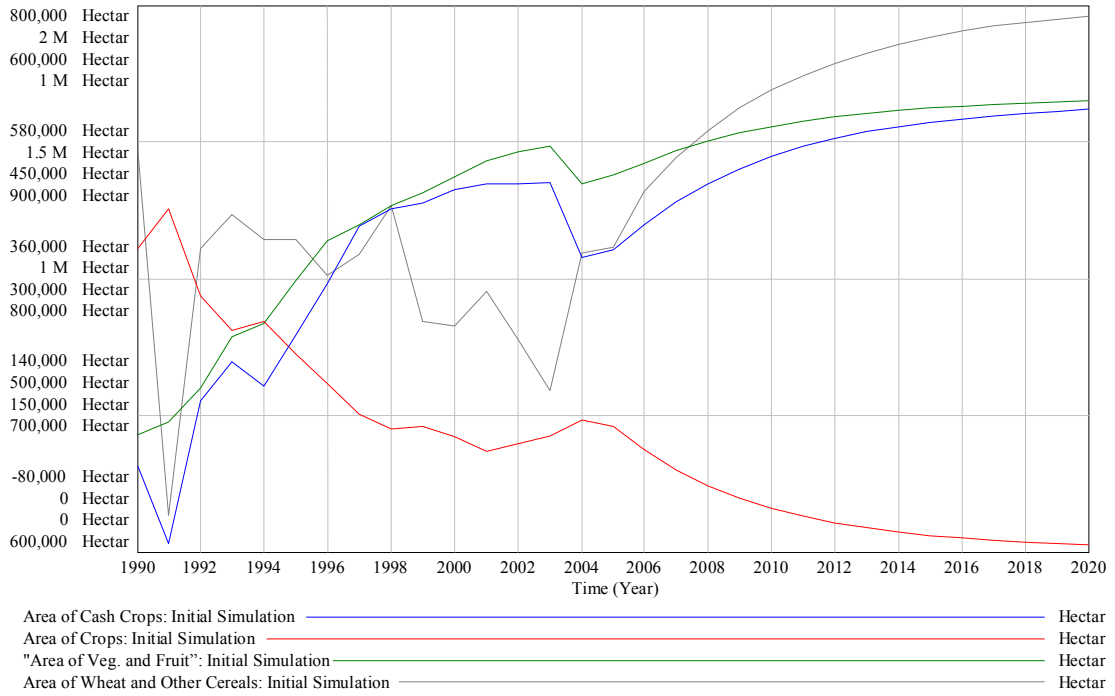


Figure (4-5) Area of Crops, Cash Crops, Wheat and other Cereals, Veg. and Fuit Area



$$cbl_t = - \int [cdr_t + ica] dt \quad \text{See appendix (2)}$$

$$\frac{\partial cbl}{\partial t} = -\psi_{cbl}(cbl_t)$$

$$cd_t = \int_{t_0}^t [cdr_t - (car_t + qar_t + far_t)] dt + icda$$

$$\frac{\partial cd}{\partial t} = (\psi_{cbl}(cbl_t) - ((\psi_{crops}(cd_t) + \psi_{fodder}(cd_t) + \psi_{qat}(cd_t)))$$

$$ca_t = \int_{t_0}^t [car_t - ((ccar_t + vfar_t + wcar_t))] dt + ica$$

$$\frac{\partial ca}{\partial t} = (\psi_{crops}(cd_t) - (\psi_{cashcrops}(ca_t) + \psi_{Veg.andFruit}(ca_t) + \psi_{WheatandCereals}(ca_t)))$$

$$cca_t = \int_{t_0}^t ccar_t dt + icca$$

$$\frac{\partial cca}{\partial t} = \psi_{cashcrops} (ca_t)$$

$$vfa_t = \int_{t_0}^t vfar_t dt + ivfa$$

$$\frac{\partial vfa}{\partial t} = \psi_{veg.andfruit} (ca_t)$$

$$wca_t = \int_{t_0}^t wcar_t dt + iwca$$

$$\frac{\partial wca}{\partial t} = \psi_{wheatandcereals} (ca_t)$$

$$foda_t = \int_{t_0}^t fodar_t dt + ifoda$$

$$\frac{\partial foda}{\partial t} = \psi_{fodder} (cd_t)$$

$$qata_t = \int_{t_0}^t qatar_t dt + iaqta$$

$$\frac{\partial qata}{\partial t} = \psi_{qat} (cd_t)$$

$$\psi_{cbl} = \psi_t(t) \forall t \in T1, \text{ fid } [\psi_{wheat,cereals} (\kappa)] \forall t \in T2]$$

$$\text{fid} = \text{fid}_{table} [\rho_{dcbla} (AGINV)]$$

$$AGINV = \rho_{AGINV} (TINV)$$

Where

cbl=Cultivable Area

cd=Cultivated Area

ca=Area of Crops

cca=Area of Cash Crops

vfa="Area of Veg. and Fruit"

wca=Area of Wheat and Other Cereals

foda=Fodder Area

qata=Qat Area

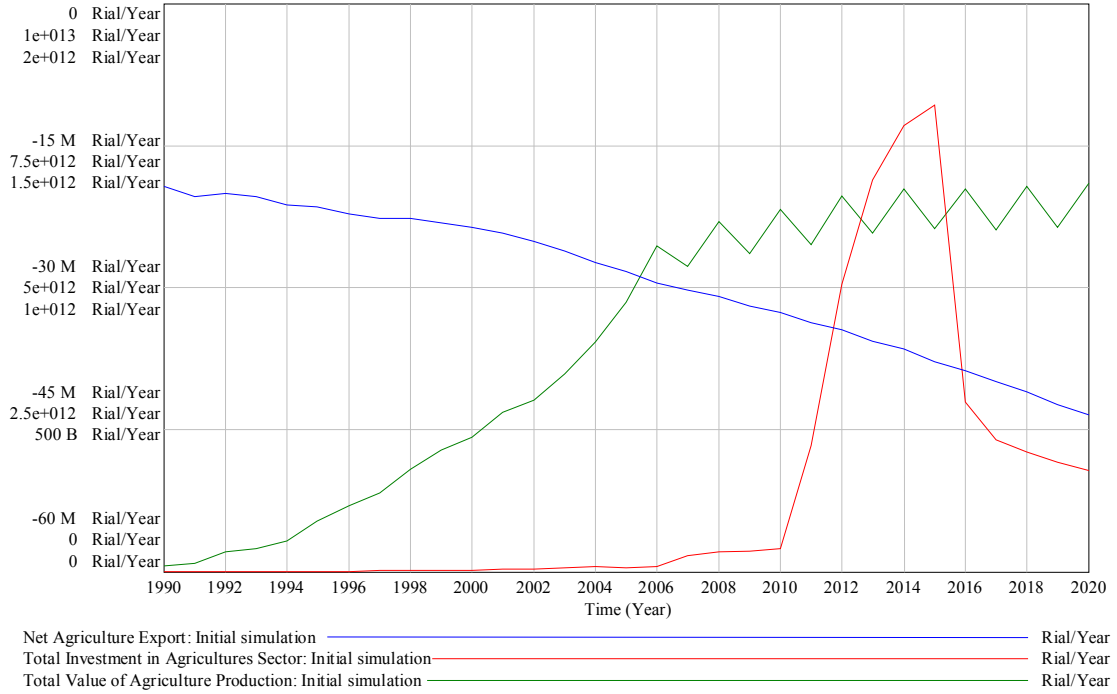
ψ_{group} =Growth Rate of Area

i_{group} =Initial value of Area

T1= Time period before policy year (1990-2005)

$T2$ = Time period after policy year (2006-2020)
 fid = Fraction of Investment Allocated to Development the Cultivated area
 k = Effect of Growth in Cereals Area
 ρ_{dcble} = Coefficient of Development cultivated area
 $AGINV$ = Total Investment in Agricultures Sector
 ρ_{AGINV} = Coefficient of Investment in Agricultures Sector
 $TINV$ = Total Domestic Investment

Figure (5-5) Net agriculture Export, Agriculture Investment and Net Export



Total Values of Agriculture Production = Value of Cash Crops Production + Value of Deep Fish Production + Value of Fodder Production + Value of Other Catches Production + Value of Qat Production + Value of Surface Fish Production + Value of Veg and Fruit Production + Value

$$TVAP_t = \left[\sum_i^h VCP_t + \sum_i^j VFP_t \right] + PVQ_t + PVF_t$$

Where

$TVAP_t$ = Total Values of Agriculture Production

VCP = Value of Crops Production

VFP = Value of Fishing Production

PVQ_t = Production Value of Qat

PVF_t = Production Value of Fodder

h = Number of agriculture Crops

j = Number of fishing kinds

And

$VCP_i = ccprov_t + wcprov_t + vfprov_t$

$$C_{prov_t} = P_t^{cashcrops} * ccpro_t$$

$$ccpro_t = cca_t * ccproy_t$$

$$ccproy_t = ccproy_t(t) \forall t \in T1, [\mu_{ccproy} + (\lambda_1 ctcs) + (\lambda_2 IVMP)]_t \forall t \in T2$$

$$ctcs_t = ctcs(t) \forall t \in T1, \{-3.82565e13 + [1.91976e010(t)]\} \forall t \in T2$$

$$IVMP_t = IVMP_t(t) \forall t \in T1, \sum_t^d MI_t, \forall t \in T2$$

Where

ccprov=C ash Crops Productive Value

wcprov=Wheat and Cereals Productive Value

μ =Productivity Mean of Cash Crops Area

λ_1 = coefficient of Current Transfers and Current Subsidies

λ_2 =Coefficient of Input Value of Manufacturing Production

$$P_t^{cashcrops} = P_t^{cashcrops} (t) \forall t \in T1, \int_{t_0}^t (x_{ccp}_t) dt + iP^{cashcrops} \forall t \in T2$$

$$\frac{\partial ccP}{\partial t} = ccip_t - \left(\int_{t_0}^t (x_{ccp}_t) dt + iP^{cashcrops} \right)$$

$$ccip_t = \left(\int_{t_0}^t (x_{ccp}_t) dt + iP^{cashcrops} \right) * eccdsb_t$$

$$eccdsb_t = (ccdsb_t)^{scp}$$

$$ccdsb_t = \frac{ccd_t}{ccs_t}$$

$$ccd_t = (cctld_t + ccxig_t) * e^{ccde * \ln \left[\frac{\int_{t_0}^t (x_{ccp}_t) dt + iP^{cashcrops}}{ccrP} \right]}$$

$$ccs_t = (ccpro_t) * e^{ccse * \ln \left[\frac{\int_{t_0}^t (x_{ccp}_t) dt + iP^{cashcrops}}{ccrP} \right]}$$

where

- $P_t^{cashcrops}$ = Equilibrium Price of Cash Crops
 $xccp_t$ = Change in Cash Crops Price
 $iP^{cashcrops}$ = Initial Value of Cash Crops
 $ccip_t$ = Cash Crops Indicated Price
 $eccdsb_t$ = Effect of Cash Crops Demand/Supply Balance on Price
 $sccp$ = Sensitivity of Cash crops Price to Demand/Supply Balance=1
 $ccdsb_t$ = Cash Crops Demand/Supply Balance
 ccd_t = Demand of Cash Crops
 ccs_t = Supply of Cash Crops
 $ccrP$ = Reference Cash Crops Price= 306507(Rial)
 $ccde$ = Cash Crops Demand Elasticity= -1
 $ccse$ = Cash Crops Supply Elasticity= 1
 $cctld_t$ = Total Local Demand of Cash Crops
 $ccxig_t$ = Export/Import Gap of Cash Crops
 $ccpro_t$ = Production of Cash Crops
 $ccprov_t$ = Value of Cash Crops Production
 $ccproy_t$ = Productivity of Cash Crops Area

$$NAE_t = \left[\sum_i^h EIGC_i + \sum_i^j EIGF_i \right]_t$$

$$\sum EIGC = EIGCC + EIGWC + EIGVF$$

$$EIGCC_t = ccpro_t - tldcc_t$$

$$tldcc_t = ccdmi_t + ccnid_t$$

$$ccnid_t = \delta(\xi_t)$$

Where

- NAE = Net of Agriculture Export
 $EIGC$ = Export/Import Gap of Crops
 $EIGCC$ = Export/Import Gap of Cash Crops
 $tldcc$ = Total Local Demand of Cash Crops
 $ccdmi$ = Demand of Cash Crops for Manufacturing Input
 $ccnid$ = Normal Individual Demand of Cash Crops
 δ = Normal Consumption Rate of Cash Crops Per Capita

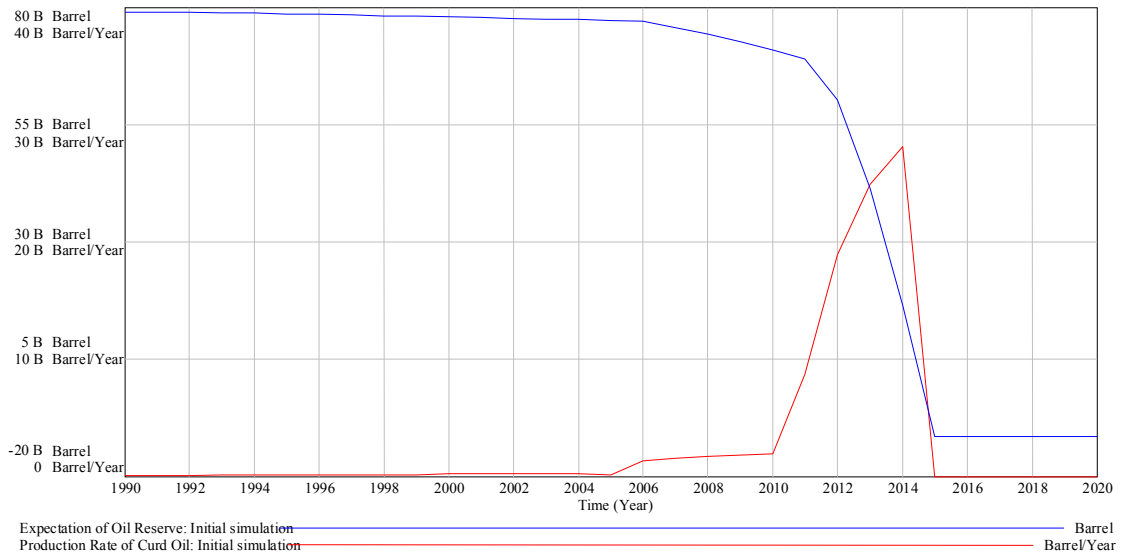
Table (2-5) Result of Initial Simulation of Agriculture View

| Time (Year) | Net Agriculture Export (RIAL) | Net | Total Value of Agriculture |
|-------------|-------------------------------|--------------|----------------------------|
| 1990 | -1.94018e+007 | 2.2379e+009 | 2.16339e+010 |
| 1991 | -2.04054e+007 | 4.14423e+009 | 2.91099e+010 |
| 1992 | -2.01108e+007 | 5.14581e+009 | 7.03195e+010 |
| 1993 | -2.04203e+007 | 1.00906e+010 | 8.31123e+010 |
| 1994 | -2.12863e+007 | 2.16939e+010 | 1.08991e+011 |
| | | | 1.77486e+011 |
| | | | 2.34333e+011 |
| | | | 2.77576e+011 |
| | | | 3.60331e+011 |
| | | | 4.28393e+011 |

| | | |
|------|---------------|--------------|
| 1995 | -2.14961e+007 | 4.7331e+011 |
| | 4.52395e+010 | 5.59893e+011 |
| 1996 | -2.21679e+007 | 6.0323e+011 |
| | 7.39684e+010 | 6.94967e+011 |
| 1997 | -2.26645e+007 | 8.09341e+011 |
| | 7.30805e+010 | 9.48176e+011 |
| 1998 | -2.26415e+007 | 1.14606e+012 |
| | 5.40093e+010 | 1.07753e+012 |
| 1999 | -2.31264e+007 | 1.23264e+012 |
| | 9.076e+010 | 1.12117e+012 |
| 2000 | -2.37045e+007 | 1.27549e+012 |
| | 1.7315e+011 | 1.15159e+012 |
| 2001 | -2.42576e+007 | 1.32298e+012 |
| | 1.43496e+011 | 1.19112e+012 |
| 2002 | -2.51117e+007 | 1.34664e+012 |
| | 1.47531e+011 | 1.20784e+012 |
| 2003 | -2.61757e+007 | 1.34811e+012 |
| | 1.7487e+011 | 1.20163e+012 |
| 2004 | -2.73935e+007 | 1.35617e+012 |
| | 2.20713e+011 | 1.21087e+012 |
| 2005 | -2.83187e+007 | 1.36556e+012 |
| | 3.24606e+011 | |
| 2006 | -2.94818e+007 | |
| | 2.96436e+012 | |
| 2007 | -3.02914e+007 | |
| | 3.4914e+012 | |
| 2008 | -3.09195e+007 | |
| | 3.88253e+012 | |
| 2009 | -3.18942e+007 | |
| | 4.18743e+012 | |
| 2010 | -3.26233e+007 | |
| | 3.99843e+013 | |
| 2011 | -3.37325e+007 | |
| | 8.70036e+013 | |
| 2012 | -3.44854e+007 | |
| | 1.0944e+014 | |
| 2013 | -3.56428e+007 | |
| | 1.20278e+014 | |
| 2014 | -3.65247e+007 | |
| | 1.23263e+014 | |
| 2015 | -3.7741e+007 | 5.19911e+013 |
| 2016 | -3.87025e+007 | |
| | 4.23378e+013 | |
| 2017 | -3.99895e+007 | |
| | 3.82528e+013 | |
| 2018 | -4.09928e+007 | |
| | 3.49218e+013 | |
| 2019 | -4.23264e+007 | |
| | 3.19342e+013 | |

2020 -4.33915e+007
 2.92206e+013

Figure (6-5) Expectation Oil Reserve and Production Rate of Curd Oil (1990-2020)



Figure(7-5) Total Investment in Oil Sector and Total Value of Oil Export

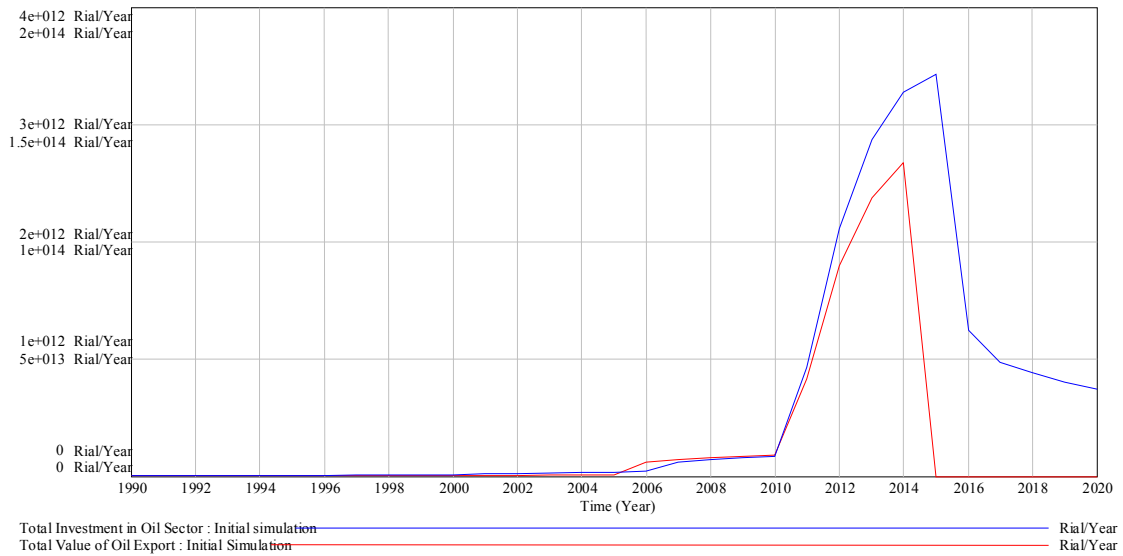
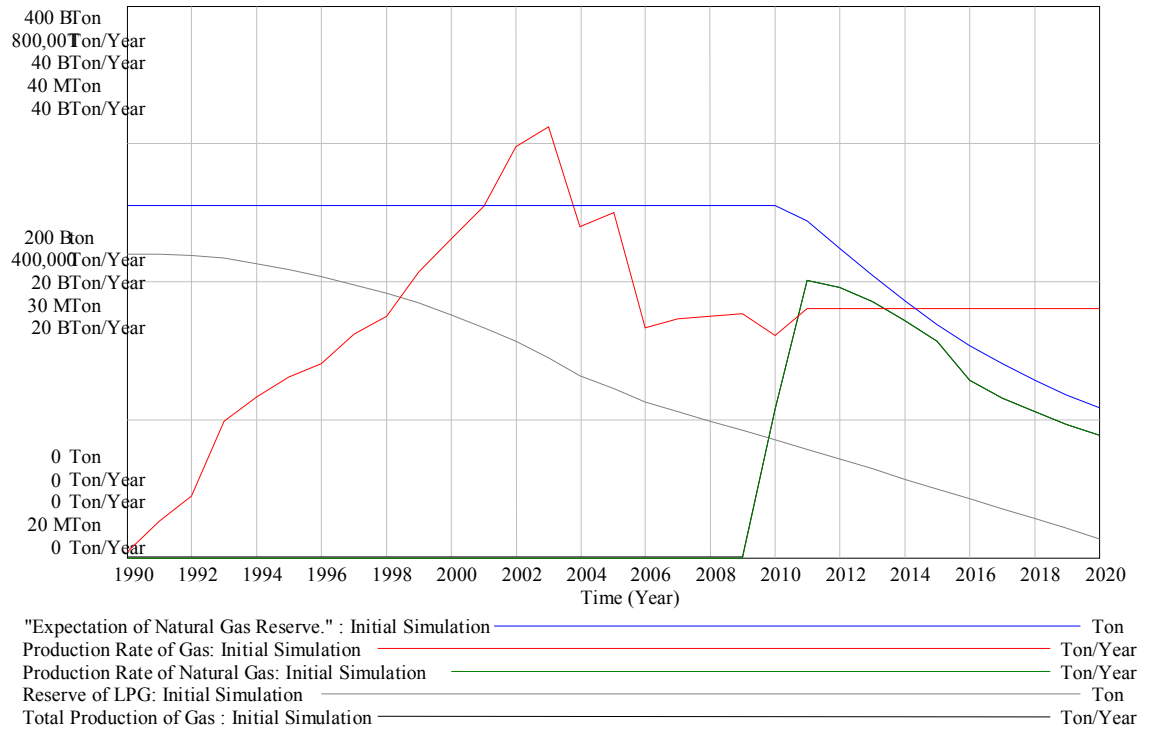


Figure (8-5) Selected Variables



$$EOR_t = - \int_{t_0}^t (prco_t) dt + iEOR, EOR \geq 0$$

$$\frac{\partial EOR}{\partial t} = prco_t : EOR > 0, 0 : EOR \leq 0$$

$$prco_t = \Phi_1(t) * N_1(t) : t \in T1, \Phi_2 * N_2 : t \in T2$$

$$\Phi_2 = \Gamma(TIOS_t)$$

$$N_2 = \Omega(TIOS_t)$$

$$TIOS = \beta_1 * (TINV_t)$$

$$copv_t = prco_t * P_{\$lbarrel}$$

$$P_{\$lbarrel} = P_{\$lbarrel}(t) \forall t \in T1, P_{\$lbarrel}^* \forall t \in T2$$

$$invop_t = \beta_2 * (copv_t)$$

$$ncopv_t = copv_t - invop_t$$

$$gscop_t = \beta_3 * (ncopv_t)$$

$$csop_t = (1 - \beta_3) * ncopv_t$$

$$tlcco_t = \beta_4 * (gscop_t)$$

$$xco_t = ([(1 - \beta_4) * tlcco_t] + csop_t) * xP_{YRIS}$$

$$tlcco_t^* = tlcco_t * xP_{YRIS}$$

$$xP_{YRIS} = xP_{YRIS}(t) \forall t \in T1, xP_{YRIS}^* \forall t \in T2$$

Gas Production

$$RLPG_t = - \int_{t_0}^t (gpr_t) dt + iRLPG$$

$$\frac{\partial RLPG}{\partial t} = gpr_t : RLPG > 0, 0 : RLPG \leq 0$$

$$gpr_t = gpr_t(t) \forall t \in T1, gpr_t^* \forall t \in T2$$

$$gpr_t^* = N_2 * \theta$$

$$\theta = (\theta^* * dprg_t) + dprg_t$$

$$dprg_t = 0 \forall t \in T3, fidgp_t \forall t \notin T3$$

$$fidgp_t = A_2(TIGS 2) \forall t \in T3, A_1(TIGS 1) \forall t \in T2, 0 \forall t \notin T3 \text{ or } T2$$

$$TIGS2_t = TIOS_t$$

$$TIGS1_t = \beta_5 * (TINV_t)$$

$$ENGR_t = - \int_{t_0}^t (ngpr_t) dt + iENGP$$

$$\frac{\partial ENGR}{\partial t} = dprng_t * ENGR_t$$

$$dprng_t = fidgp_t \forall t \in T3, 0 \forall t \notin T3$$

$$TPG_t = (dprg_t + dprng_t) \forall t \in T3, (dprg_t) \forall t \notin T3$$

$$TPGV_t = TPG_t * gP_t$$

$$gP_t = gP_T(t) \forall t \in T1, gP_t^* \forall t \in T2$$

$$NTPGV_t = TPGV_t - (\beta_6 * TPGV_t)$$

$$lcgp_t = lcgp_t(t) \forall t \in T1, (\beta_7 * NTPGV_t) \forall t \in T2$$

$$xgp_t = NTPGV_t - lcgp_t$$

Where

EOR_t = Expectation of Oil Reserve

$prco_t$ = Production Rate of Curd Oil

Φ = Productivity Mean Per Sector

N = Number of Oil Sector

$TIOS$ = Total Investment in Oil Sector

$TINV$ = Total Domestic Investment

$cpov$ = Value of Curd Oil Production

$P_{\$barrel}$ = Price Per Barrel

$Inovp$ = Input Value of Curd Oil Production

$gscop$ = Government Share of Curd Oil Production

$ncopv$ = Net Value of Curd Oil \$

$csop$ = Companies Share

$tlcco$ = Total Local Consumption of Oil

xco = Value of Oil Export YR

$xP_{YR/\$}$ = Exchange Price

β_1 = Investment Rate for Oil Sector

β_2 = Input Rate of Oil

β_3 = Government Share Rate

β_4 = Local Consumption Rate of Oil

$RLPG$ = Reserve of LPG

Gpr = Production Rate of Gas

θ = Productivity of LPG Per Oil Sector

$dprg$ = Development Production Rate of LPG

$fidgp$ = Fraction Investment Which Allocated to Development Gas Production

$TIGS$ = Total Investment in Gas Sector

$ENGR$ = Expectation of Natural Gas Reserve

$ngpr$ = Production Rate of Natural Gas

$dprng$ = Development Production Rate of Natural Gas

TPG = Total Production of Gas

$TPGV$ = Value of Gas Production

gP_t = Price of Gas YR Per Ton

$NTPGV$ = Net Value of Gas Production

$lcpg$ = Value of Local Consumption of Gas YR

xgP = Value of Gas Export YR

β_5 = Total Investment in Gas Sector

β_6 = Input Rate From Gas Production

β_7 = Local Consumption Rate of Gas

Table (3-5) Result of Initial Simulation of Oil View

| Time EOR (Barrel) | (Year) | $Prco$ (Barrel/ Year) | $P_{\$barrel}$ rel | $xP_{YR/\$}$ 13.92 | Xco (Rial/Y rar) | $TIOS$ (Rial/Y ear) |
|------------------------|--------------|--------------------------|-----------------------|-----------------------|-----------------------|------------------------|
| 1990 | 7.9e+010 | 6.81044e+007 | 12 | 22.12 | 5.53803e+ | 2.60546e+0 |
| 1991 | 7.89319e+010 | 7.45916e+007 | 12.5 | 28.5 | 009 | 08 |
| 1992 | 7.88573e+010 | 6.42028e+007 | 14 | 39.54 | 1.00403e+ | 1.98629e+0 |
| 1993 | 7.87931e+010 | 7.78794e+007 | 15.8 | 55.24 | 010 | 09 |
| 1994 | 7.87152e+010 | 1.21451e+008 | 15.2 | 100 | 1.24706e+ | 2.54047e+0 |
| 1995 | 7.85938e+010 | 1.23724e+008 | 16.9 | 129.2 | 010 | 09 |
| 1996 | 7.847e+010 | 1.24505e+008 | 4 | 8 | 2.36279e+ | 3.82768e+0 |

| | | | | | | |
|------|--------------|--------------|------|-------|-----------|------------|
| 1997 | 7.83455e+010 | 1.30495e+008 | 20.3 | 135.8 | 010 | 09 |
| 1998 | 7.8215e+010 | 1.32919e+008 | 8 | 8 | 4.95075e+ | 2.55817e+0 |
| 1999 | 7.80821e+010 | 1.41274e+008 | 18.4 | 55.75 | 010 | 09 |
| 2000 | 7.79409e+010 | 1.5722e+008 | 4 | 161.7 | 1.01574e+ | 4.52344e+0 |
| 2001 | 7.77836e+010 | 1.5786e+008 | 14.9 | 3 | 011 | 09 |
| 2002 | 7.76258e+010 | 1.57738e+008 | 4 | 168.6 | 1.55079e+ | 6.05391e+0 |
| 2003 | 7.7468e+010 | 1.55114e+008 | 18.6 | 3 | 011 | 09 |
| 2004 | 7.73129e+010 | 1.52532e+008 | 7 | 176 | 1.46954e+ | 9.30471e+0 |
| 2005 | 7.71604e+010 | 1.49996e+008 | 27.3 | 183 | 011 | 09 |
| 2006 | 7.70104e+010 | 1.25658e+009 | 9 | 184 | 1.32229e+ | 1.44657e+0 |
| 2007 | 7.57538e+010 | 1.47951e+009 | 24.5 | 191.4 | 011 | 10 |
| 2008 | 7.42743e+010 | 1.64495e+009 | 8 | 2 | 1.97159e+ | 1.43759e+0 |
| 2009 | 7.26294e+010 | 1.77391e+009 | 27.9 | 196 | 011 | 10 |
| 2010 | 7.08554e+010 | 1.86244e+009 | 5 | 196 | 3.25523e+ | 1.36501e+0 |
| 2011 | 6.8993e+010 | 8.68719e+009 | 36.6 | 196 | 011 | 10 |
| 2012 | 6.03058e+010 | 1.88781e+010 | 51.5 | 196 | 2.89751e+ | 1.91628e+0 |
| 2013 | 4.14277e+010 | 2.49123e+010 | 19 | 196 | 011 | 10 |
| 2014 | 1.65154e+010 | 2.80795e+010 | 51 | 196 | 3.29272e+ | 2.14978e+0 |
| 2015 | -1.1564e+010 | 0 | 51 | 196 | 011 | 10 |
| 2016 | -1.1564e+010 | 0 | 51 | 196 | 3.80204e+ | 2.62739e+0 |
| 2017 | -1.1564e+010 | 0 | 51 | 196 | 011 | 10 |
| 2018 | -1.1564e+010 | 0 | 51 | 196 | 4.98408e+ | 3.34398e+0 |
| 2019 | -1.1564e+010 | 0 | 51 | 196 | 011 | 10 |
| 2020 | -1.1564e+010 | 0 | 51 | 196 | 7.14196e+ | 3.28783e+0 |
| | | | 51 | 196 | 011 | 10 |
| | | | 51 | 196 | 5.98548e+ | 3.97449e+0 |
| | | | 51 | 196 | 012 | 10 |
| | | | 51 | 196 | 7.04735e+ | 1.22027e+0 |
| | | | 51 | | 012 | 11 |
| | | | 51 | | 7.83538e+ | 1.41639e+0 |
| | | | 51 | | 012 | 11 |
| | | | 51 | | 8.44966e+ | 1.56685e+0 |
| | | | | | 012 | 11 |
| | | | | | 8.87135e+ | 1.66897e+0 |
| | | | | | 012 | 11 |
| | | | | | 4.13796e+ | 9.27616e+0 |
| | | | | | 013 | 11 |
| | | | | | 8.9922e+0 | 2.11075e+0 |
| | | | | | 13 | 12 |
| | | | | | 1.18664e+ | 2.87182e+0 |
| | | | | | 014 | 12 |
| | | | | | 1.33751e+ | 3.27128e+0 |
| | | | | | 014 | 12 |
| | | | | | 0 | 3.42601e+0 |
| | | | | | 0 | 12 |
| | | | | | 0 | 1.24067e+0 |
| | | | | | 0 | 12 |
| | | | | | 0 | 9.71542e+0 |
| | | | | | 0 | 11 |
| | | | | | | 8.76873e+0 |

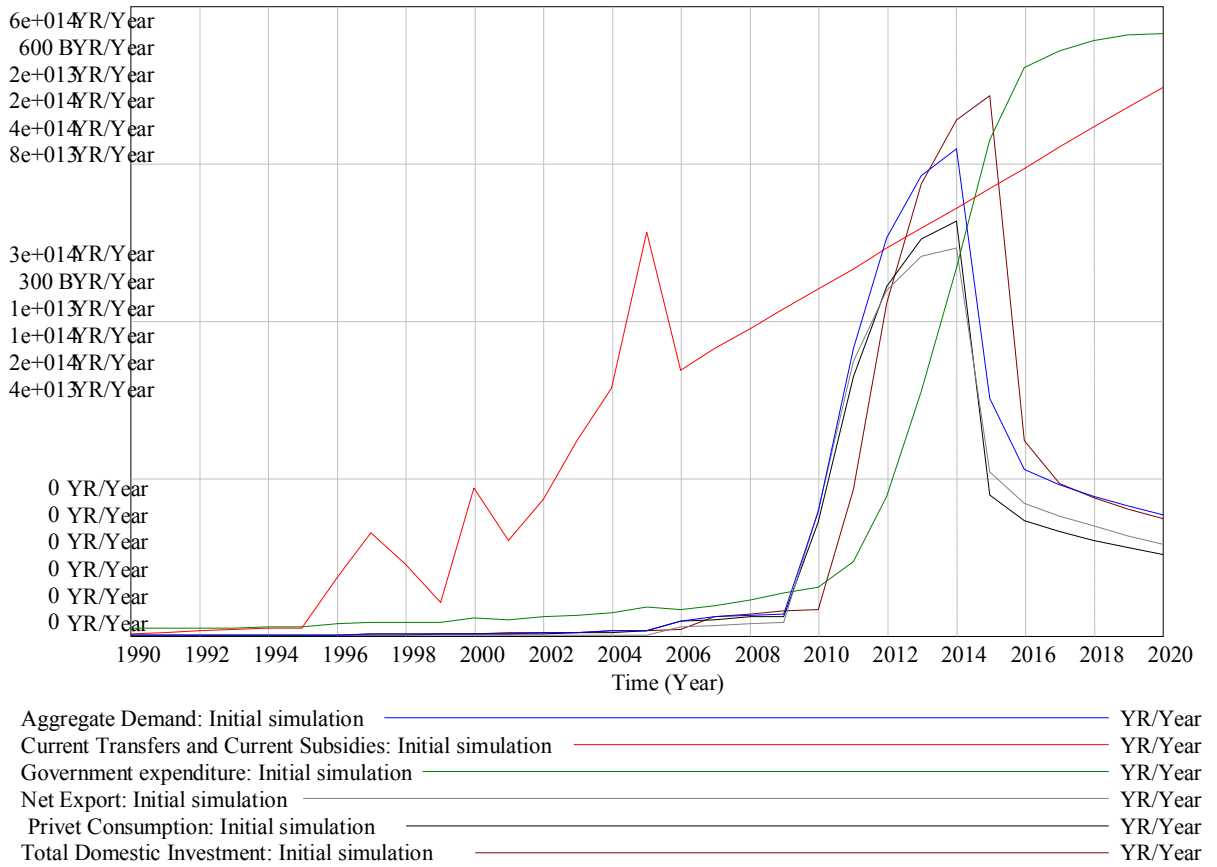
11
8.05739e+0
11
7.40354e+0
11

Table (4-5) Result of Initial Simulation of Gas View

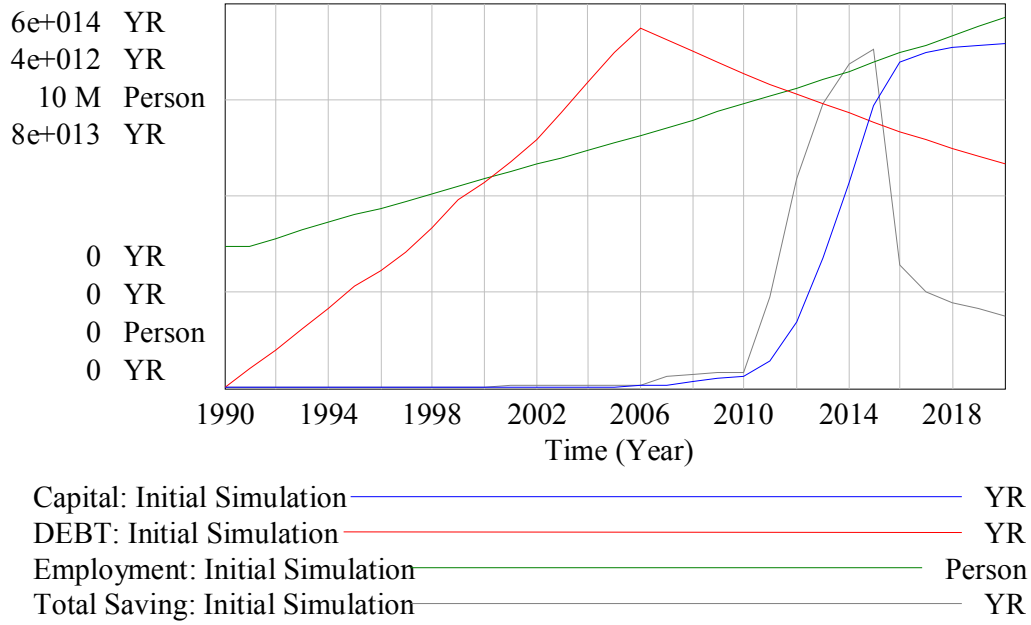
| Time <i>RLPG(Ton)</i> | (Year) | <i>Gpr(Ton/Y ear)</i> | <i>ENGR(Ton)</i> | <i>Ngpr(Ton/Y ear)</i> | <i>xgP(YR/Ye ar)</i> | <i>TVGOE(YR/Ye ar)</i> |
|--------------------------|--------------|---------------------------|-----------------------|----------------------------|--------------------------|----------------------------|
| 1990 | 3.1e+007 | 7433 | 2.54873e+ | 0 | 0 | 2.46647e+009 |
| 1991 | 3.09926e+007 | 51771 | 011 | 0 | 0 | 4.47161e+009 |
| 1992 | 3.09408e+007 | 89200 | 2.54873e+ | 0 | 0 | 5.554e+009 |
| 1993 | 3.08516e+007 | 197069 | 011 | 0 | 0 | 1.06582e+010 |
| 1994 | 3.06545e+007 | 232815 | 2.54873e+ | 0 | 0 | 2.23687e+010 |
| 1995 | 3.04217e+007 | 261178 | 011 | 0 | 190848 | 4.63149e+010 |
| 1996 | 3.01605e+007 | 280080 | 2.54873e+ | 0 | 2.27738e+ | 7.67816e+010 |
| 1997 | 2.98805e+007 | 324270 | 011 | 0 | 006 | 7.60459e+010 |
| 1998 | 2.95562e+007 | 349383 | 2.54873e+ | 0 | 1.94048e+ | 5.68364e+010 |
| 1999 | 2.92068e+007 | 413220 | 011 | 0 | 006 | 9.44774e+010 |
| 2000 | 2.87936e+007 | 462783 | 2.54873e+ | 0 | 4.15683e+ | 1.76925e+011 |
| 2001 | 2.83308e+007 | 508109 | 011 | 0 | 006 | 1.4928e+011 |
| 2002 | 2.78227e+007 | 595025 | 2.54873e+ | 0 | 2.53082e+ | 1.53601e+011 |
| 2003 | 2.72277e+007 | 624813 | 011 | 0 | 006 | 1.83555e+011 |
| 2004 | 2.66029e+007 | 480000 | 2.54873e+ | 0 | 3.83465e+ | 2.26461e+011 |
| 2005 | 2.61229e+007 | 500000 | 011 | 0 | 007 | 3.32642e+011 |
| 2006 | 2.56229e+007 | 331738 | 2.54873e+ | 0 | 1.81089e+ | 2.97198e+012 |
| 2007 | 2.52911e+007 | 346416 | 011 | 0 | 007 | 3.49909e+012 |
| 2008 | 2.49447e+007 | 349914 | 2.54873e+ | 0 | 5.73261e+ | 3.89024e+012 |
| 2009 | 2.45948e+007 | 352598 | 011 | 0 | 007 | 4.19514e+012 |
| 2010 | 2.42422e+007 | 322199 | 2.54873e+ | 1.07555e+0 | 0 | 3.99921e+013 |
| 2011 | 2.392e+007 | 360000 | 011 | 10 | 5.92416e+ | 8.70116e+013 |
| 2012 | 2.356e+007 | 360000 | 2.54873e+ | 2.00894e+0 | 008 | 1.09448e+014 |
| 2013 | 2.32e+007 | 360000 | 011 | 10 | 6.1908e+0 | 1.20286e+014 |
| 2014 | 2.284e+007 | 360000 | 2.54873e+ | 1.95885e+0 | 08 | 1.23272e+014 |
| 2015 | 2.248e+007 | 360000 | 011 | 10 | 1.09766e+ | 5.19993e+013 |
| 2016 | 2.212e+007 | 360000 | 2.54873e+ | 1.85522e+0 | 009 | 4.23458e+013 |
| 2017 | 2.176e+007 | 360000 | 011 | 10 | 1.14622e+ | 3.82607e+013 |
| 2018 | 2.14e+007 | 360000 | 2.54873e+ | 1.71915e+0 | 009 | 3.49297e+013 |
| 2019 | 2.104e+007 | 360000 | 011 | 10 | 1.1578e+0 | 3.19422e+013 |
| 2020 | 2.068e+007 | 360000 | 2.54873e+ | 1.57151e+0 | 09 | 2.92286e+013 |
| | | | 011 | 10 | 1.16668e+ | |
| | | | 2.54873e+ | 1.27976e+0 | 009 | |
| | | | 011 | 10 | 3.55888e+ | |
| | | | 2.54873e+ | 1.1563e+01 | 013 | |
| | | | 011 | 0 | 6.64729e+ | |
| | | | 2.54873e+ | 1.05563e+0 | 013 | |
| | | | 011 | 10 | 6.48158e+ | |
| | | | 2.54873e+ | 9.65335e+0 | 013 | |
| | | | 011 | 09 | 6.13869e+ | |
| | | | 2.54873e+ | 8.83324e+0 | 013 | |

| | | |
|-----------|----|-----------|
| 011 | 09 | 5.68845e+ |
| 2.44117e+ | | 013 |
| 011 | | 5.19993e+ |
| 2.24028e+ | | 013 |
| 011 | | 4.23458e+ |
| 2.04439e+ | | 013 |
| 011 | | 3.82607e+ |
| 1.85887e+ | | 013 |
| 011 | | 3.49297e+ |
| 1.68695e+ | | 013 |
| 011 | | 3.19422e+ |
| 1.5298e+0 | | 013 |
| 11 | | 2.92286e+ |
| 1.40183e+ | | 013 |
| 011 | | |
| 1.2862e+0 | | |
| 11 | | |
| 1.18064e+ | | |
| 011 | | |
| 1.0841e+0 | | |
| 11 | | |

Figure (9-5) Mine Result of Initial simulation of GDP View



Figure(10-5) Main Results for Initial Simulation of GDP View



$$Y_t = PC_t + GE_t + TINV_t + NE_t$$

$$PC_t = \alpha_{PC} * C_t$$

$$C_t = \alpha_c * CDI_t$$

$$CDI_t = GDP_t - NIT_t$$

$$GDP_t = IND_t + PGS_t + PNPSF_t + CDU_t - IBS_t$$

$$NIT_t = ITR_t - gt_t$$

$$ITR_t = ITR_t(t) \forall t \in T1, f(GDP_t) \forall t \in T2$$

$$gt_t = \alpha_{subsidy} * CGTS_t$$

$$GE_t = PWS_t + CGTS_t + CAD_t + GOSE_t$$

$$PWS_t = \mu_{PS} * PEM_t * 12$$

$$CGTS_t = CGTS_t(t) \forall t \in T1, (\alpha_{CGTS} + \beta_{CGTS}(t)) \forall t \in T2$$

$$CAD_t = \frac{CA_t}{\mu_{ALC}}$$

$$CA_t = \int_{t_0}^t (CAI_t - CAD) dt_t + iCA$$

$$\frac{\partial CA_t}{\partial t} = CAI_t - CAD_t$$

$$CAI_t = \max(0, TINV_t + NLRW_t)$$

$$NLRW_t = RA_t + DC_t$$

$$RA_t = RA_t(t) \forall t \in T1, [\alpha_{RA} + \beta_{RA}(t)] \forall t \in T2$$

$$DC_t = DC_t(t) \forall t \in T1, [\max(0, (\frac{DL_t}{tal}) * edodl)] \forall t \in T2$$

$$TINV_t = INFS_t + FINV_t$$

$$INFS_t = \alpha_{INV} * TS_t$$

$$TS_t = \int_{t_0}^t (SR_t - INFS_t) dt + iTS$$

$$\frac{\partial TS_t}{\partial t} = SR_t - INFS_t$$

$$SR_t = (1 - \alpha_C) * CDI_t$$

$$NE_t = NAE_t + NOGE_t + NMPE_t$$

$$DEBT_t = \int_{t_0}^t (NGD_t - LP_t) dt + iDEBT$$

$$\frac{\partial DEBT_t}{\partial t} = NGD_t - LP_t$$

$$NGD_t = (-NGDR_t) \forall NGDR \leq 0, 0 \forall NGDR > 0$$

$$NGDR_t = GR_t - GE_t$$

$$LP_t = \frac{DEBT_t}{mp}$$

$$EMP_t = \int_{t_0}^t EMPR_t dt + iEMP$$

$$\frac{\partial EMP}{\partial t} = EMPR_t$$

$$EMPR_t = (\alpha_{EMP} * LF_t) - EMP_t$$

$$LF_t = (\xi_{2t} + \xi_{3t}) * \alpha_{LF}$$

$$INC_t / capita = \frac{CDI_t}{\xi_t}$$

Where

Y_t = Aggregate Demand

PC_t = Private Consumption

GE_t = Government expenditure

NE_t = Net Export

C_t = Consumption

CDI_t = Current Disposable Income

GDP_t = GDP at Market Price

NIT_t = "Indirect Taxes (net)"

IND_t = Industries

PGS_t = Producers of Government Services

$PNPSF_t$ = Producers of Non Profit Bodies Serving Families

CDU_t = Custom Duties

IBS_t = Imputed Bank Services

ITR_t = Indirect Tax Revenue

gt_t = Government Transfer

$CGTS_t$ = Current Transfers and Current Subsidies

PWS_t = Wages and Salary for Public Sector

CAD_t = Capital Depreciation

$GOSE_t$ = Goods and Service Expenditures

PEM_t = Employment for Public Sector

μ_{PS} = Monthly Average Wages for Public Sector

CA_t = Capital

μ_{ALC} = Average Life of Capital

CAI_t = Capital Investment

$NLRW_t$ = Net Lending to the Rest of The World

RA_t = Reserve Assets

DC_t = Debt Commitment

$INFS_t$ = Investment from Savings

$FINV_t$ = Foreign Investment

TS_t = Total Saving

SR_t = Saving Rate

NAE_t = Net Agriculture Export

$NOGE_t$ = TOTAL VALUE OF GAS AND OIL EXPORT

$NMPE_t$ = NET EXPORT VALUE OF MANUFACTURING PRODUCTION

NGD_t = Net Government Deficit

LP_t = Loan Payment

$NGDR_t$ = Net Government Deficit Rate

GR_t = Government Revenue

mp = Maturity Period

EMP_t = Employment

$EMPR_t$ = Employment Rate

LF_t = Labor Force

$INC/capita$ = Income per Capita YR

Table (5-5) Result of Initial Simulation of GDP View

| Time Aggregate | Privet | Governme | Total | Current | Net Export |
|----------------|--------------|-----------|------------|--------------|--------------|
| Demand | Consumpt | nt | Domestic | Transfers | |
| | ion | expndture | Investment | and Current | |
| 1990 | 3.0009e+011 | 6.31772e+ | 5.21092e+ | 2.27447e+009 | 2.2379e+009 |
| 1991 | 3.6756e+011 | 2.27189e+ | 5.21092e+ | Subsidies | 4.14423e+009 |
| 1992 | 4.45684e+011 | 010 | 009 | 2.27447e+009 | 5.14581e+009 |
| 1993 | 5.43537e+011 | 9.13468e+ | 3.97258e+ | 3.11144e+009 | 1.00906e+010 |
| 1994 | 6.27211e+011 | 010 | 010 | 4.15672e+009 | 2.16939e+010 |
| 1995 | 8.78244e+011 | 1.40541e+ | 5.08094e+ | 5.40557e+009 | 4.52395e+010 |
| 1996 | 1.30038e+012 | 011 | 010 | 6.98038e+009 | 7.39684e+010 |
| 1997 | 1.55029e+012 | 1.91286e+ | 7.65536e+ | 6.8107e+009 | 7.30805e+010 |
| 1998 | 1.63388e+012 | 011 | 010 | 5.5432e+010 | 5.40093e+010 |
| 1999 | 1.81191e+012 | 2.66944e+ | 5.11634e+ | 9.8475e+010 | 9.076e+010 |
| 2000 | 2.41194e+012 | 011 | 010 | 6.8609e+010 | 1.7315e+011 |
| 2001 | 2.60801e+012 | 4.42896e+ | 9.04688e+ | 3.1527e+010 | 1.43496e+011 |
| 2002 | 2.9382e+012 | 011 | 010 | 1.41579e+011 | 1.47531e+011 |
| 2003 | 3.53611e+012 | 6.77097e+ | 1.21078e+ | 9.0597e+010 | 1.7487e+011 |
| 2004 | 4.06942e+012 | 011 | 011 | 1.3104e+011 | 2.20713e+011 |
| 2005 | 5.13349e+012 | 7.54505e+ | 1.86094e+ | 1.8594e+011 | 3.24606e+011 |
| 2006 | 1.40932e+013 | 011 | 011 | 2.3592e+011 | 2.96436e+012 |
| 2007 | 1.77445e+013 | 7.96232e+ | 2.89313e+ | 3.84967e+011 | 3.4914e+012 |
| 2008 | 1.98585e+013 | 011 | 011 | 2.53885e+011 | 3.88253e+012 |
| 2009 | 2.14376e+013 | 9.91471e+ | 2.87519e+ | 2.73083e+011 | 4.18743e+012 |
| 2010 | 1.17981e+014 | 011 | 011 | 2.9228e+011 | 3.99843e+013 |
| 2011 | 2.73017e+014 | 1.27701e+ | 2.73002e+ | 3.11477e+011 | 8.70036e+013 |
| 2012 | 3.78731e+014 | 012 | 011 | 3.30679e+011 | 1.0944e+014 |
| 2013 | 4.37945e+014 | 1.47037e+ | 3.83256e+ | 3.49876e+011 | 1.20278e+014 |
| 2014 | 4.64133e+014 | 012 | 011 | 3.69074e+011 | 1.23263e+014 |
| 2015 | 2.26239e+014 | 1.6446e+0 | 4.29956e+ | 3.88271e+011 | 5.19911e+013 |
| 2016 | 1.59128e+014 | 12 | 011 | 4.07468e+011 | 4.23378e+013 |
| 2017 | 1.43375e+014 | 1.97873e+ | 5.25478e+ | 4.26666e+011 | 3.82528e+013 |
| 2018 | 1.33037e+014 | 012 | 011 | 4.45863e+011 | 3.49218e+013 |
| 2019 | 1.23783e+014 | 2.18949e+ | 6.68795e+ | 4.6506e+011 | 3.19342e+013 |
| 2020 | 1.15453e+014 | 012 | 011 | 4.84258e+011 | 2.92206e+013 |
| | | 2.82304e+ | 6.57565e+ | 5.03455e+011 | |
| | | 012 | 011 | 5.22652e+011 | |
| | | 9.24321e+ | 7.94899e+ | | |
| | | 012 | 011 | | |
| | | 1.05776e+ | 2.44053e+ | | |
| | | 013 | 012 | | |
| | | 1.17025e+ | 2.83278e+ | | |
| | | 013 | 012 | | |
| | | 1.2455e+0 | 3.1337e+0 | | |
| | | 13 | 12 | | |
| | | 7.2769e+0 | 3.33793e+ | | |
| | | 13 | 012 | | |
| | | 1.64769e+ | 1.85523e+ | | |
| | | 014 | 013 | | |
| | | 2.22249e+ | 4.22151e+ | | |
| | | 4.45797e+ | | | |

| | | |
|-----------|-----------|-----------|
| 014 | 012 | 013 |
| 2.52067e+ | 7.7755e+0 | 5.74364e+ |
| 014 | 12 | 013 |
| 2.63348e+ | 1.1688e+0 | 6.54257e+ |
| 014 | 13 | 013 |
| 8.95515e+ | 1.57494e+ | 6.85202e+ |
| 013 | 013 | 013 |
| 7.35082e+ | 1.80227e+ | 2.48134e+ |
| 013 | 013 | 013 |
| 6.66321e+ | 1.85945e+ | 1.94308e+ |
| 013 | 013 | 013 |
| 6.11979e+ | 1.88955e+ | 1.75375e+ |
| 013 | 013 | 013 |
| 5.61623e+ | 1.90684e+ | 1.61148e+ |
| 013 | 013 | 013 |
| 5.17627e+ | 1.91395e+ | 1.48071e+ |
| 013 | 013 | 013 |

Table (6-5)Result of Initial Simulation of GDP View

| Time(Year) | Total | Employment(Pe | Capit(YR) | DEBT(YR) |
|------------|--------------|---------------|--------------|--------------|
| Saving(YR) | | rson) | 1.5074e+010 | 5e+007 |
| 1990 | 1.0136e+010 | 3.69047e+006 | 1.82613e+010 | 2.02294e+011 |
| 1991 | 1.80008e+010 | 3.69047e+006 | 5.4199e+010 | 3.97682e+011 |
| 1992 | 2.37554e+010 | 3.89675e+006 | 1.09031e+011 | 6.10961e+011 |
| 1993 | 3.65486e+010 | 4.09786e+006 | 1.85436e+011 | 8.30743e+011 |
| 1994 | 4.97454e+010 | 4.29476e+006 | 2.28669e+011 | 1.05744e+012 |
| 1995 | 6.94208e+010 | 4.48832e+006 | 2.86642e+011 | 1.22907e+012 |
| 1996 | 1.15178e+011 | 4.67931e+006 | 3.23128e+011 | 1.41747e+012 |
| 1997 | 1.85874e+011 | 4.86844e+006 | 4.53282e+011 | 1.67709e+012 |
| 1998 | 1.97515e+011 | 5.05631e+006 | 7.83599e+011 | 1.95331e+012 |
| 1999 | 2.07066e+011 | 5.24351e+006 | 9.94153e+011 | 2.13841e+012 |
| 2000 | 2.57839e+011 | 5.43052e+006 | 9.89424e+011 | 2.35892e+012 |
| 2001 | 3.84954e+011 | 5.61782e+006 | 1.21999e+012 | 2.585e+012 |
| 2002 | 3.97777e+011 | 5.80582e+006 | 1.52153e+012 | 2.86763e+012 |
| 2003 | 4.2769e+011 | 5.99491e+006 | 1.95223e+012 | 3.17151e+012 |
| 2004 | 5.14584e+011 | 6.18546e+006 | 2.47372e+012 | 3.47837e+012 |
| 2005 | 5.69393e+011 | 6.37779e+006 | 2.9438e+012 | 3.74277e+012 |
| 2006 | 7.34151e+011 | 6.57222e+006 | 5.58025e+012 | 3.61801e+012 |
| 2007 | 2.42634e+012 | 6.76902e+006 | 1.00525e+013 | 3.49741e+012 |
| 2008 | 2.82538e+012 | 6.96849e+006 | 1.49734e+013 | 3.38083e+012 |
| 2009 | 3.1302e+012 | 7.17087e+006 | 2.01216e+013 | 3.26813e+012 |
| 2010 | 3.33526e+012 | 7.37641e+006 | 4.24728e+013 | 3.1592e+012 |
| 2011 | 1.90267e+013 | 7.58536e+006 | 1.04792e+014 | 3.05389e+012 |
| 2012 | 4.34345e+013 | 7.79793e+006 | 2.03165e+014 | 2.95209e+012 |
| 2013 | 5.9133e+013 | 8.01435e+006 | 3.19381e+014 | 2.85369e+012 |
| 2014 | 6.73701e+013 | 8.23483e+006 | 4.40055e+014 | 2.75857e+012 |
| 2015 | 7.05572e+013 | 8.45958e+006 | 5.07078e+014 | 2.66661e+012 |
| 2016 | 2.54581e+013 | 8.68881e+006 | 5.23048e+014 | 2.57773e+012 |
| 2017 | 1.98992e+013 | 8.92271e+006 | 5.30885e+014 | 2.4918e+012 |
| 2018 | 1.79401e+013 | 9.16149e+006 | 5.34869e+014 | 2.40874e+012 |
| 2019 | 1.64666e+013 | 9.40535e+006 | 5.35791e+014 | 2.32845e+012 |
| 2020 | 1.51118e+013 | 9.65447e+006 | | |

5. Discussion

In a complex system we cannot compute every effect and behavior of variables on model. The mathematical approaches to the study of dynamical systems are existed since the days of Newton and Leibniz (Peter Turchin,2005). The most common and incredibly fruitful mathematical tool is the differential equation, which looks like this:

$$X' = f(X)$$

where X is a variable describing some aspect of the system. On the left hand side we see X with a dot on top, which denotes the derivative, or rate of change of X . To the right of the equals sign, $f(X)$ means some function of X . For example, if $f(X) = rX$, then we have an exponential model: $X' = rX$, which assumes that the rate of change of the variable X is directly proportional to the value of the variable X . Even a third order, linear differential equation is unsolvable by inspection. Important situations in management, economics, medicine, and social behavior usually lose reality if

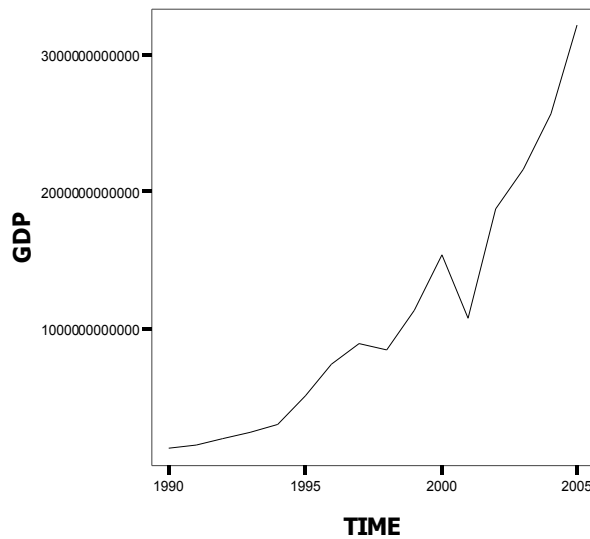
simplified to less than fifth-order nonlinear dynamic systems. Often the model representation must be twentieth order or higher.

The previous model represents the actual system behavior as it is observed in real life. It should be decrease the random error because we can put every variables which we think in the model and we can test every change in it. Values and Parameter values are drawn from all available sources, not merely from statistical analysis of time series. Regression modeling is usually a cross-sectional view of the relationship among variables at a single point in time. The numbers of cases included in a sample provide the variation to construct the parameter estimates. In contrast, simulation modeling (System Dynamics model) is a longitudinal analysis of the variables and their relationship over time. Thus, time is a primary variable as is the effect that variables have on each other. The difference is largely between a cross-sectional and a longitudinal analysis. The methods overlap when time is used as a variable in the regression equation that leads to time-series analysis. The purpose of the two methods is still different, however. The emphasis in regression analysis (linear or non-linear) is to estimate the regression coefficients as indicators of the structure of a system; the emphasis in simulation analysis (System Dynamics) is to use those coefficients in extrapolating the value of variables over time.

Let's take GDP value to comparing between System Dynamics model and linear regression model.

Table (6-1) GDP (Million Rial) at 1990-2005(CSO,2005)

| 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|---------|---------|
| 126489 | 150986 | 192047 | 238332 | 306404 | 511058 | 736385 | 888808 | 849321 | 1132619 | 1538636 | 1076049 | 1878007 | 2160608 | 2563490 | 3208501 |



The above graph shows real historical data of GDP.

We can estimate the parameters from linear function as follow:

$$Y = \alpha + \beta X$$

Where α and β are constant. The kind of relationship between independent and dependent variables is taken from economic theory. The simple regression model in which time is independent variable and GDP is dependent variable, the estimated value of parameters is

$$\alpha = -368083522.87 \quad \beta = 184821.46$$

$$GDP_T = -368083522.87 + 184821.46 (Time) + \varepsilon$$

(-10.28)
(10.31)

Where ε is error term

$R = 0.94$ $DW = 0.82$

That is meaning the time variable determining 94% for the change average of GDP.

It underestimate the true variance.

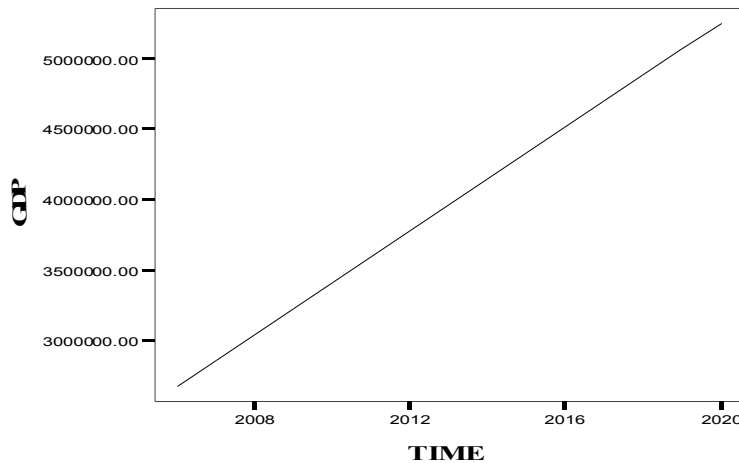
the t values look too good

will reject H_0 when it is true

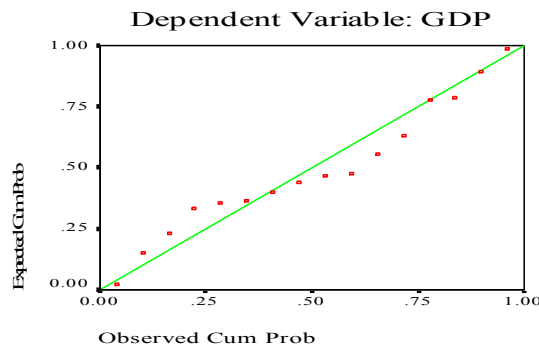
So estimates will be unbiased but inefficient (not least variance).

Statistically this model have autocorrelation problem. Time is often a parameter of the equation because we hope to use the model to forecast a value for a certain time period, but time cannot stand alone as the economic independent variable.

The below graph show the prediction value for GDP through 2005-2020 period



Normal P-P Plot of Regression Standardized Residual



Economic theory was telling us about GDP function as follow:

$GDP = \text{Consumption} + \text{Government expenditure} + \text{Investment} + \text{Net export}$

Table (6-2) GDP Component through 1990-2005

| Year | GDP | CONS | INVES | GEXP | NEXP |
|------|--------|--------|-------|-------|--------|
| 1990 | 126489 | 93298 | 18046 | 22115 | -7330 |
| 1991 | 150986 | 130802 | 24334 | 28800 | -32950 |

| | | | | | |
|------|---------|---------|--------|---------|---------|
| 1992 | 192047 | 154274 | 43026 | 37187 | -42440 |
| 1993 | 238332 | 212810 | 48249 | 45483 | -68210 |
| 1994 | 306404 | 243543 | 64390 | 57585 | -59114 |
| 1995 | 511058 | 428428 | 112713 | 74017 | -104100 |
| 1996 | 736385 | 483433 | 170879 | 97458 | -15385 |
| 1997 | 888808 | 571757 | 221215 | 116832 | -20996 |
| 1998 | 849321 | 576227 | 276465 | 124473 | -127844 |
| 1999 | 1132619 | 770168 | 278493 | 156273 | -72315 |
| 2000 | 1538636 | 797196 | 264274 | 194133 | 124209 |
| 2001 | 1076049 | 1086959 | 325114 | 236313 | 13715 |
| 2002 | 1878007 | 1265702 | 347128 | 279088 | -13911 |
| 2003 | 2160608 | 1448769 | 447822 | 1448769 | -32545 |
| 2004 | 2563490 | 1698053 | 519868 | 1698053 | 23672 |
| 2005 | 3208501 | 2058537 | 594523 | 2058537 | 162500 |

The above table shows real historical data of GDP and macroeconomic variables. We can use multi regression analysis to estimate statistical parameter by using SPSS program:

$$\alpha = 81460.89 \quad \beta_1 = 0.67 \quad \beta_2 = 1.99 \quad \beta_3 = 0.16 \quad \beta_4 = 1.48$$

$$R = 0.98 \quad DW = 3.09$$

$$GDP = 81460.89 + 0.67 (CONS) + 1.99 (INVES) + 0.16(GEXP) + 1.48 (NEXP) + \varepsilon$$

(0.88)
(1.50)
(1.53)
(1.15)

(2.00)

In this model we can't predict through time but we can do if we know any values of independent variables. It is inflexible to change parameters estimator values; we have insignificant estimators for all parameters. If we enter the time into the model we have the follow equation:

$$\alpha = -101923864.74 \quad \beta_1 = 0.45 \quad \beta_2 = 0.95 \quad \beta_3 = 0.29 \quad \beta_4 = 1.55 \quad \beta_5 = 51243.78$$

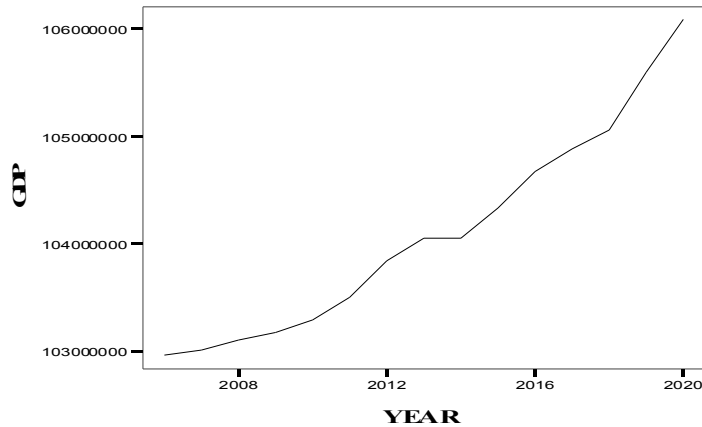
$$R = 0.99 \quad DW = 3.10$$

$$GDP = -101923864.74 + 0.45(CONS) + 0.95(INVES) + 0.29(GEXP) + 1.55(NEXP) + 51243.78 (YEAR) + \varepsilon$$

(-0.85)
(0.85)
(0.53)
(1.38)

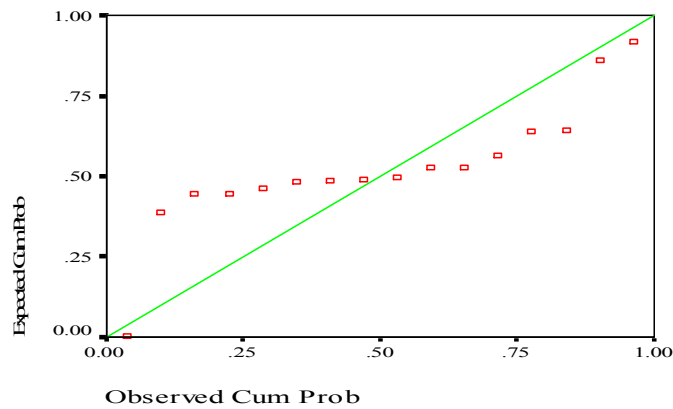
(2.06) (0.85)

Where ε is error term



Normal P-P Plot of Regression Standardized Residual

Dependent Variable: GDP



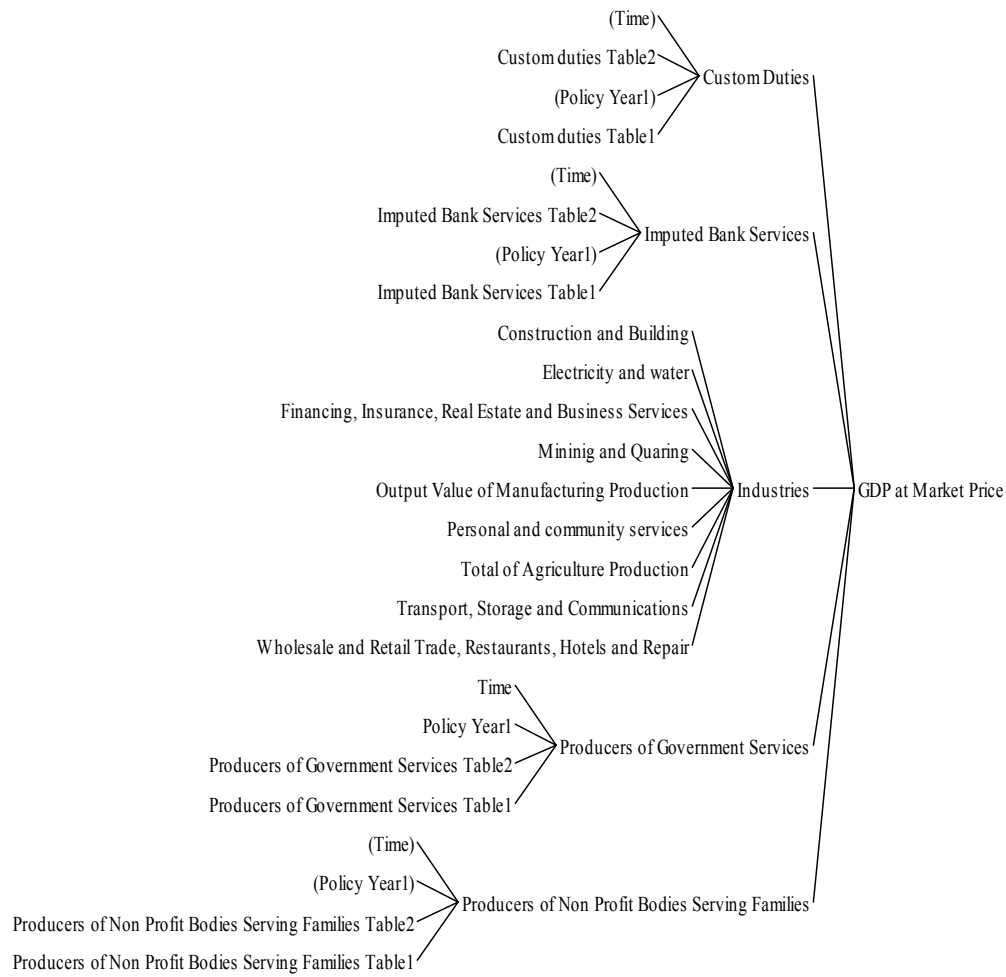
The above graphs show the predicted value of GDP and residuals through 2006-2020 periods. This model tells us about GDP increase forever and 99% of change in GDP value depend only on five variables as function shows, but if we are in need to understand and determine the behavior of the variables and their interactive effect, we must make more analysis and more function with more variables.

6. System Dynamics Model Analysis

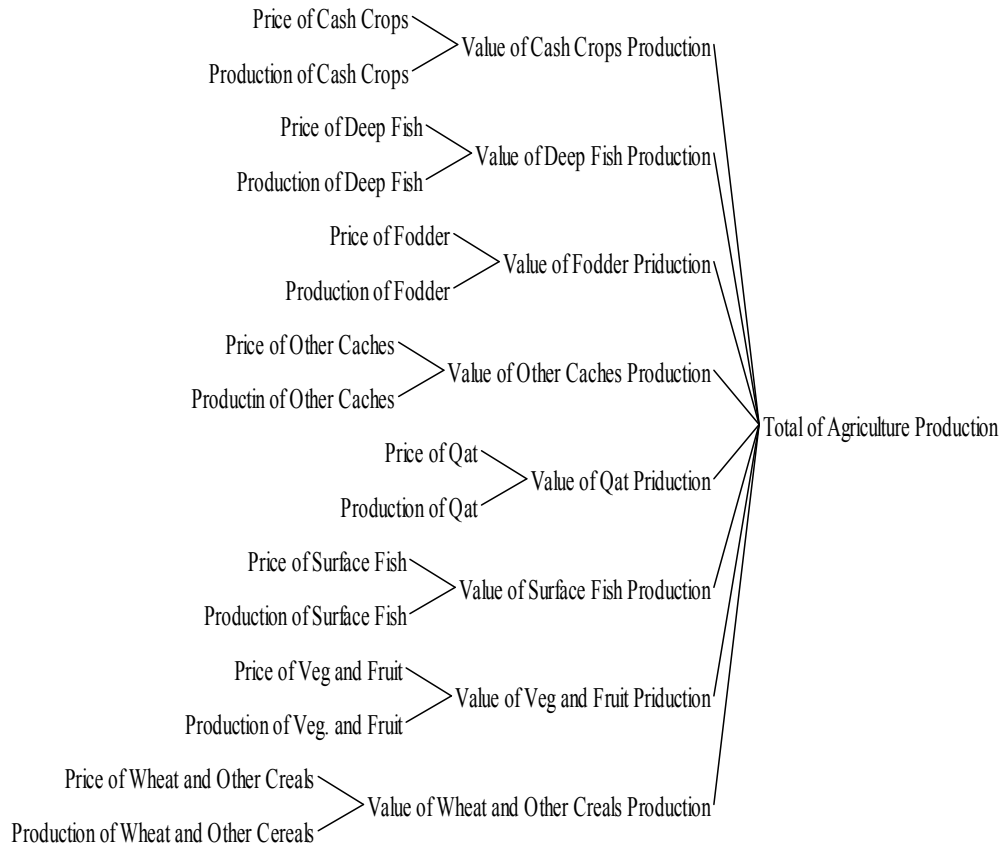
From macroeconomic system dynamic model of Yemen we can see the main difference between System Dynamics model and other linear or non-linear models which we can use in statistical analysis. We have more than 600 variables in our models. The model consists of 4 kinds of variables, Level, rate, lookup and constant. These variables relate to each other by 500 linear and non-linear equations with statistical parameters estimator. All stock equations are integral which depend on accumulation and all flows equation are differential. However, in this study we are not focus on mathematical solutions but we show the theoretical properties for System Dynamic and the main difference than regression analysis .

If we choose one of main variables, for example GDP. The relationship between variables which affect GDP was get from model diagram that shows causal loop. We can add any variables which we think and we can make all possible causal loop. The

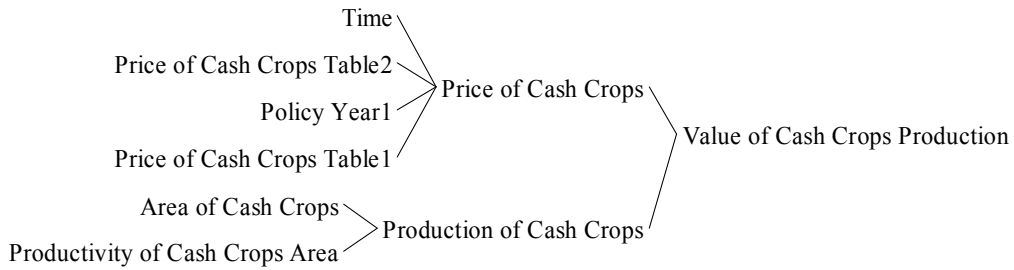
below diagram show all real components of productive sector and the historical data of GDP in the model.



Also we can take one of these components to know its components for example agriculture sector.

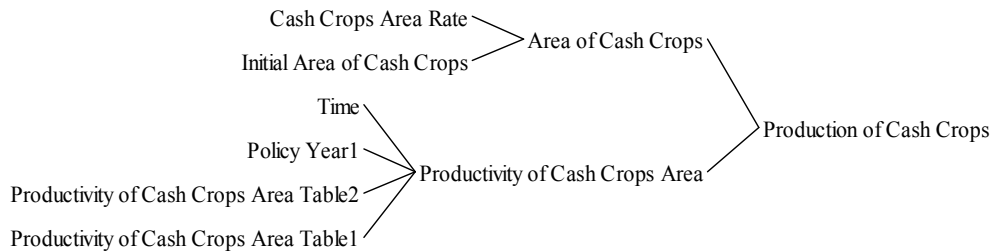


we take one of crops and we see variables and parameters which make effect, for example: Cash Crops.

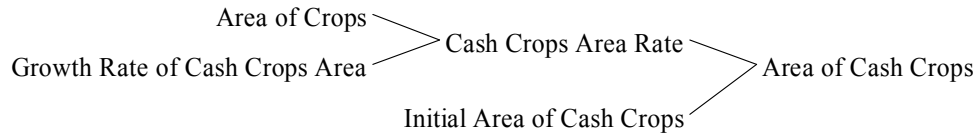


and we take one of these variables and show all possible formula which relating to parameters.

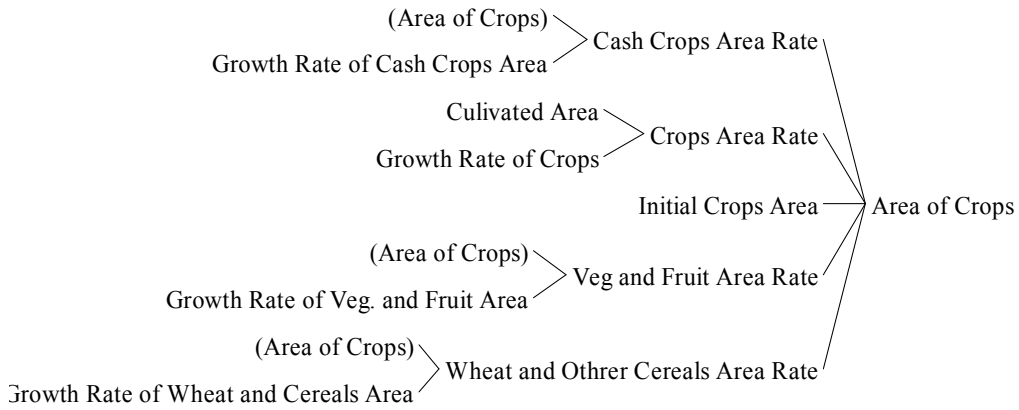
For example: Production of Cash Crops



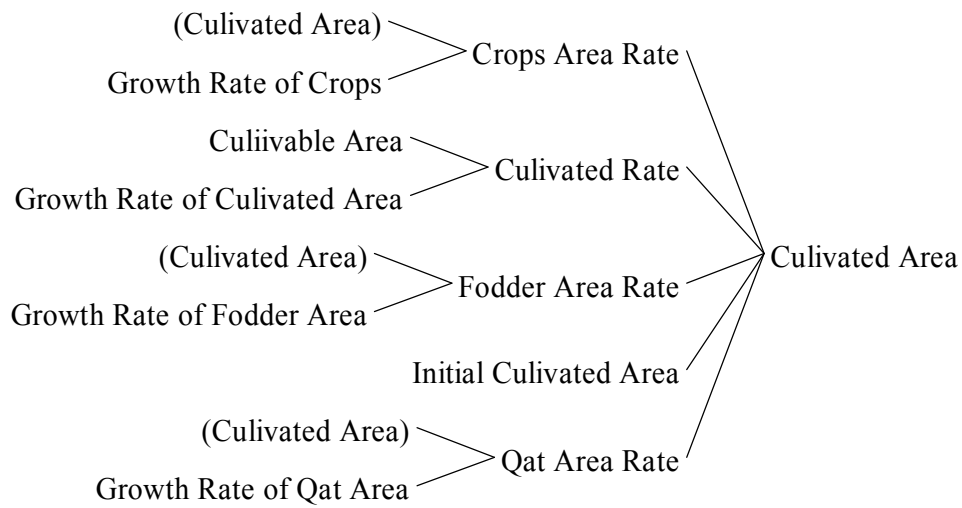
From production of Cash Crops diagram we take Area of Cash Crops variable.



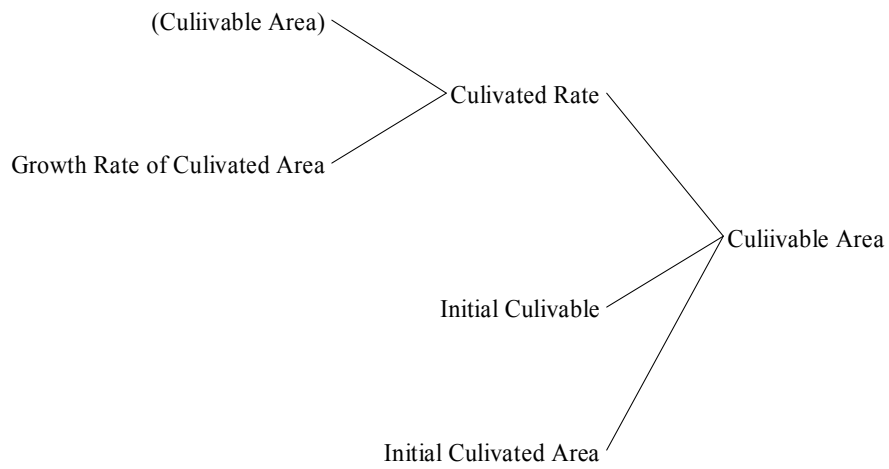
Area of Crops



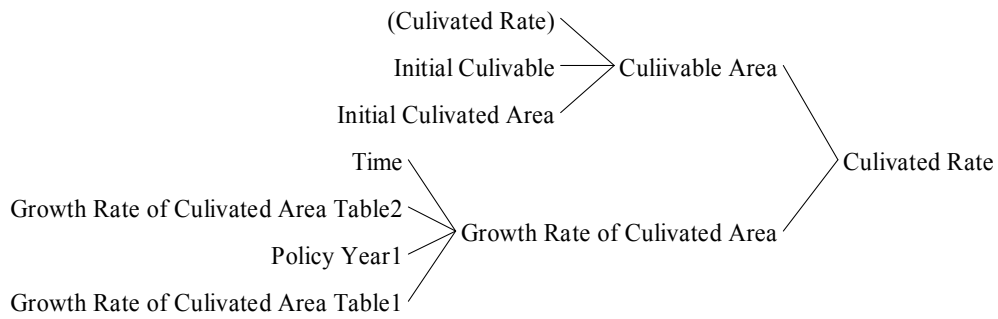
Cultivated Area



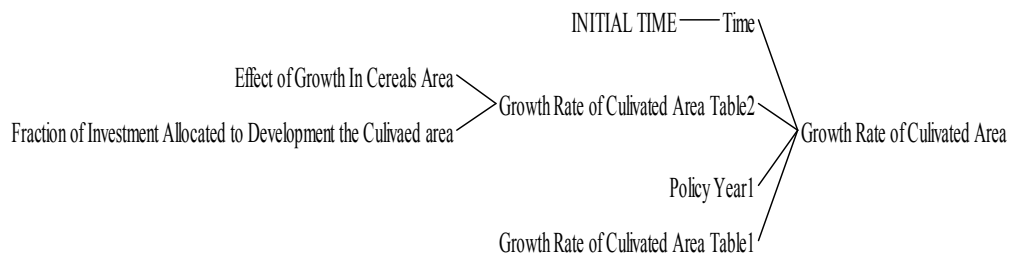
Cultivable Area



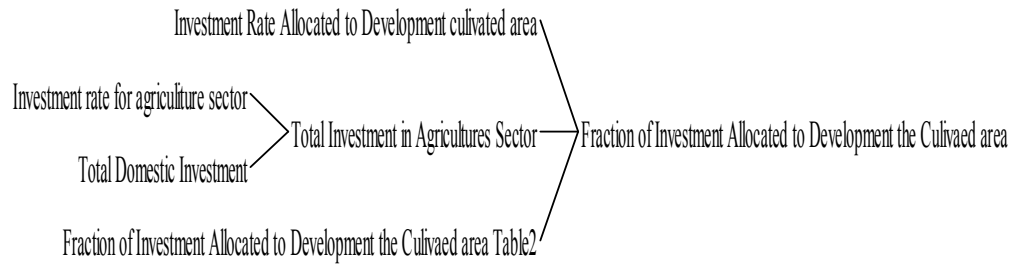
Cultivated Rate



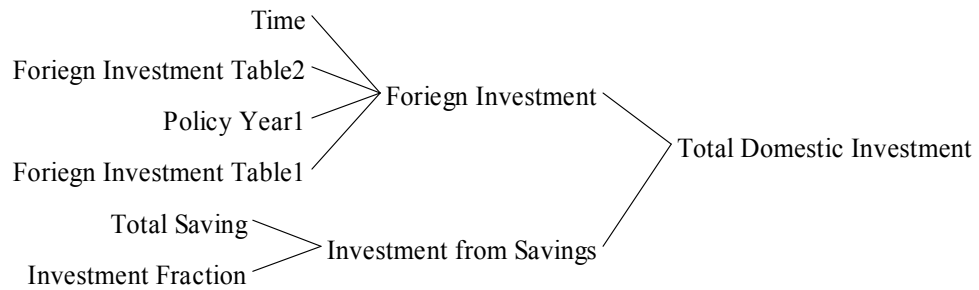
Growth Rate of Cultivated Area



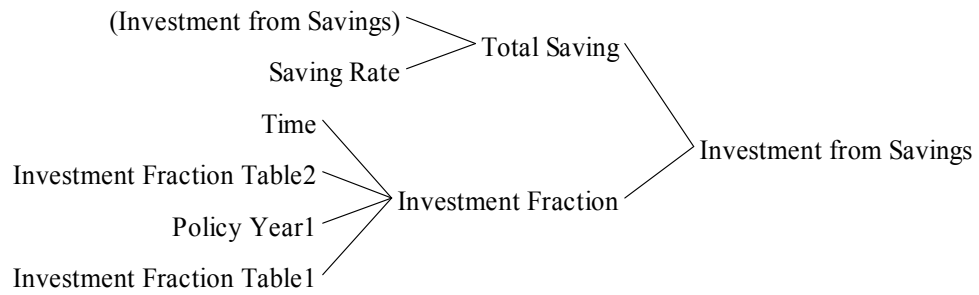
Fraction Investment Allocated to Development the Cultivated Area



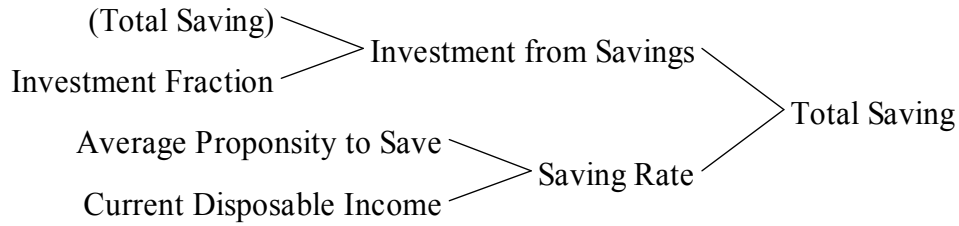
Total Domestic Investment



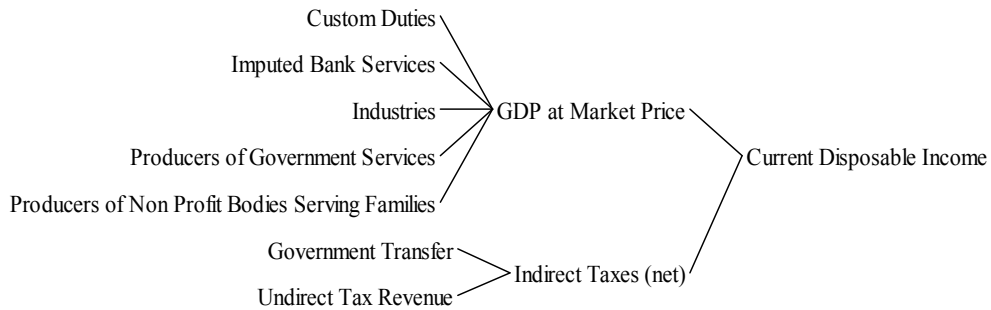
Investment From Saving



Total Saving



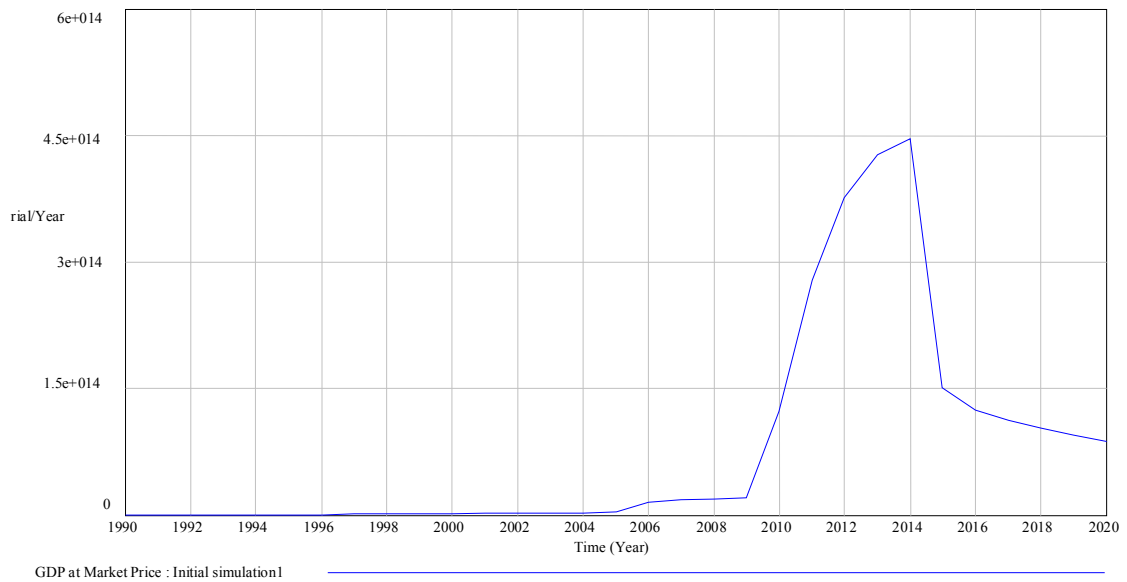
Current Disposable Income



All of previous diagram lead us to beginning step, so more loops we can follow in same way.

In our model the GDP chart presents the historical data and prediction value through 1990-2020 periods.

Figure (6- 1)GDP at Market Price , historical and predicted value (1990-2020)



in above chart we note increase in GDP value until 2014 then beginning to decrease because production value in Yemen depends on oil production and oil production depends on Production Rate of Cured Oil that depends on Expectation of Oil Reserve, this causality relationship is not exist in regression analysis as we see in the three

regression models. So system dynamic is more realistic than regression model and holistic.

7. Sensitivity Analysis

Sensitivity analysis is used to determine how “sensitive” a model is changed according to the change of the parameters value within the model and the changes in the structure of the model. Sensitivity tests help us to understand dynamics of a system. Experimenting with a wide range of values can offer insights into behavior of a system in extreme situations. Discovering that the system behavior greatly changes for a change in a parameter value can identify a leverage point in the model, a parameter whose specific value can significantly influence the behavior mode of the system. in this analysis we focus on parameter sensitivity. we depend on historical data which compute from statistical books. We try to determine economics variables and behavior of the production sector in the future under follows realities

- 1- our model is open model, we can add many of variables.
- 2- we assume the data is true.
- 3- we focus on main productive sectors only as agriculture and oil sector.
- 4- we use OLS method to estimate unknown parameters in all subsystem in the model.
- 5- we use computer program simulation (VENSIM PLE) which used monte-carlo simulation method.

The model is described macroeconomic of Yemen as we thought. In initial state of the model we can see the growth in agriculture sector is limited because the cultivable Area will be decreased and also oil sector, which all production value depend on it, will decrease. It will be ended after many years. So we are in need to discover other sources or develop the source which existent. System Dynamic provide many Scenarios to solve problem and give us many choices to make decision.

In our model, we can see

- 1- Total Fertility is very high
- 2- Cultivable Area is limited
- 3- Consumption of agriculture production is very high
- 4- Growth in fishing sector is very low
- 5- Trading balance is negative
- 6- Most income is oil production income
- 7- Oil production per year is decrease and Expectation of Oil Reserve is limited
- 8- Government expenditure is very high
- 9- DEBT is very high
- 10- Domestic investment is very low

In this section we look at model and explore how sensitive it is to changes in parameters and initial values of stocks.

Let's now look at the behavior of the system when started in equilibrium. We can't choose all variables in the model because they are many, but we focus on main variables to explain behavior of the system.

First Scenario

Let's assume that the Total Fertility change to 5 child/wn and 6.5 child/wn another way at time 1 year. Below Figures show the resulting behavior of the variables which affect parameters.

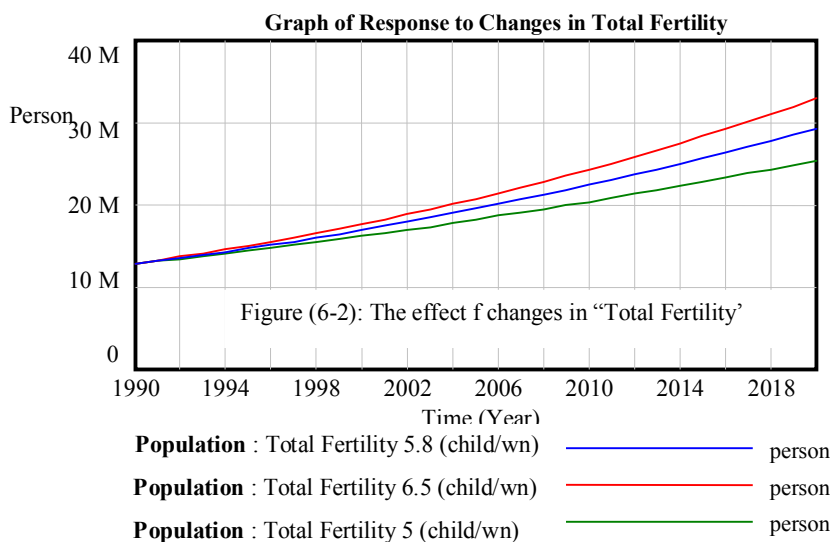


Figure (6-2): The effect f changes in "Total Fertility"

A change in "Total Fertility" creates a simultaneous change in the initial number of population, where "Total Fertility" is low, births rate is low. The result is a number of population in curve 3 growth lower than a number of population in curve 2 and 1.

Graph of Response to Changes in Total Fertility

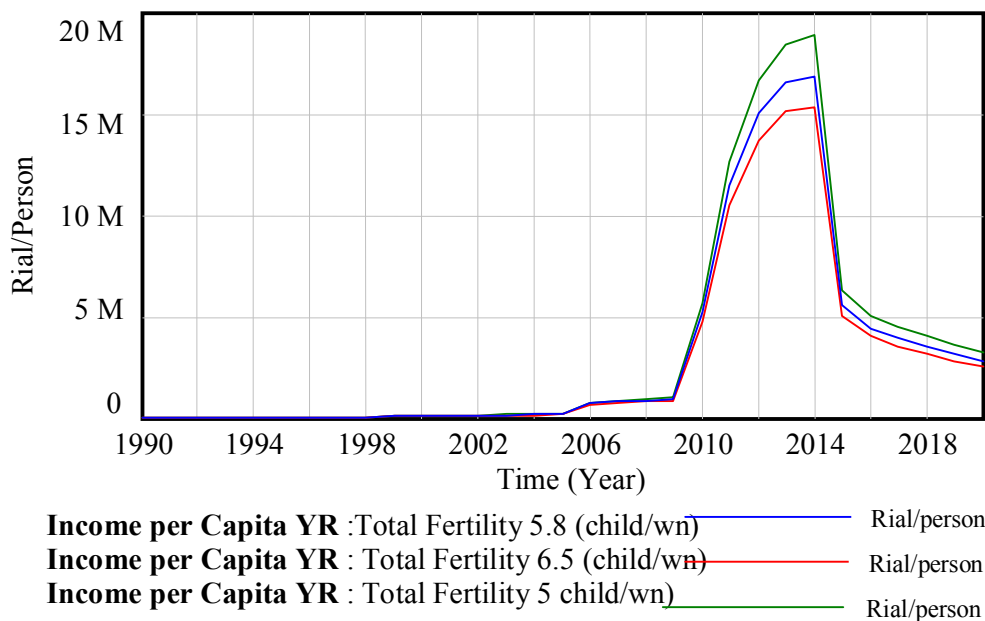


Figure (6-3): The effect of changes in "Total Fertility"

When we divide income to population, income per capita is increase.

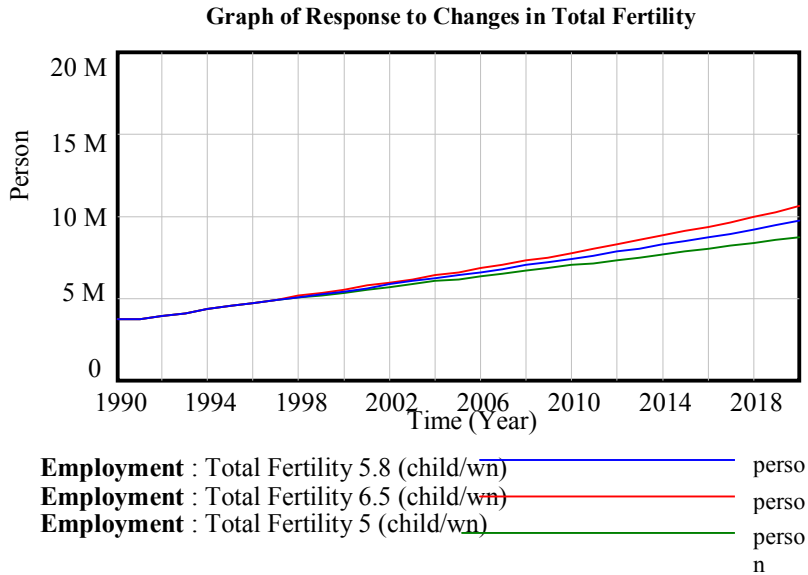


Figure (6-4): The effect of changes in “Total Fertility”

low number of population, a result is low number of employment.

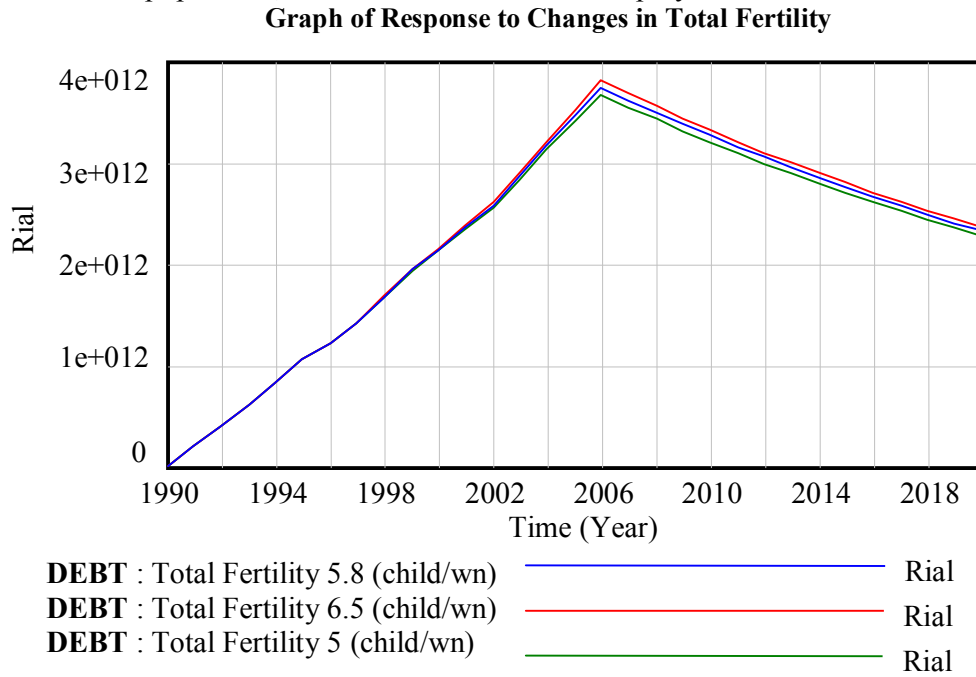


Figure (6-5): The effect of changes in “Total Fertility”

low number in employment, cause low number employment in public sector so low value of government expenditure lead to low debt.

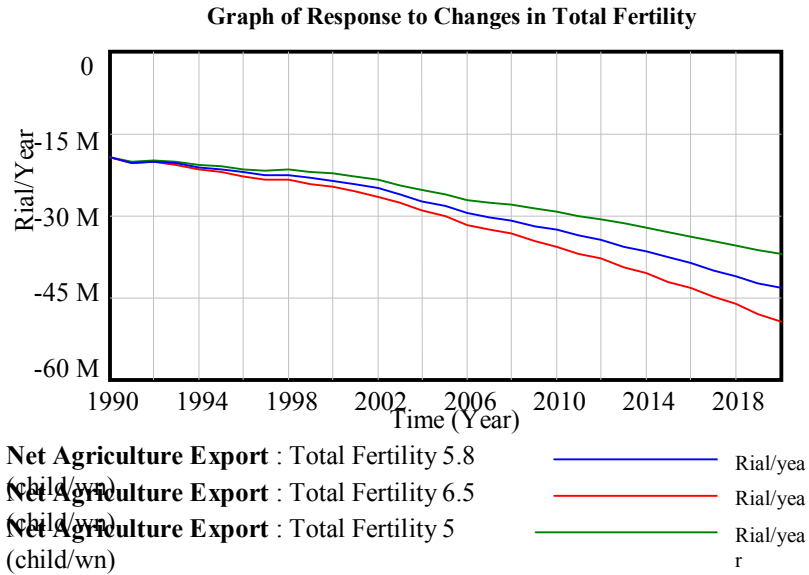


Figure (6-6): The effect of changes in “Total Fertility’

low population, result low local consumption of agriculture production so export value of agriculture production will be increased during the time. Although the three curves do not look exactly the same, these parameter changes do not affect the general mode of behavior of the system. All three curves show a small decrease and increase in the variables right after the step increase or decrease.

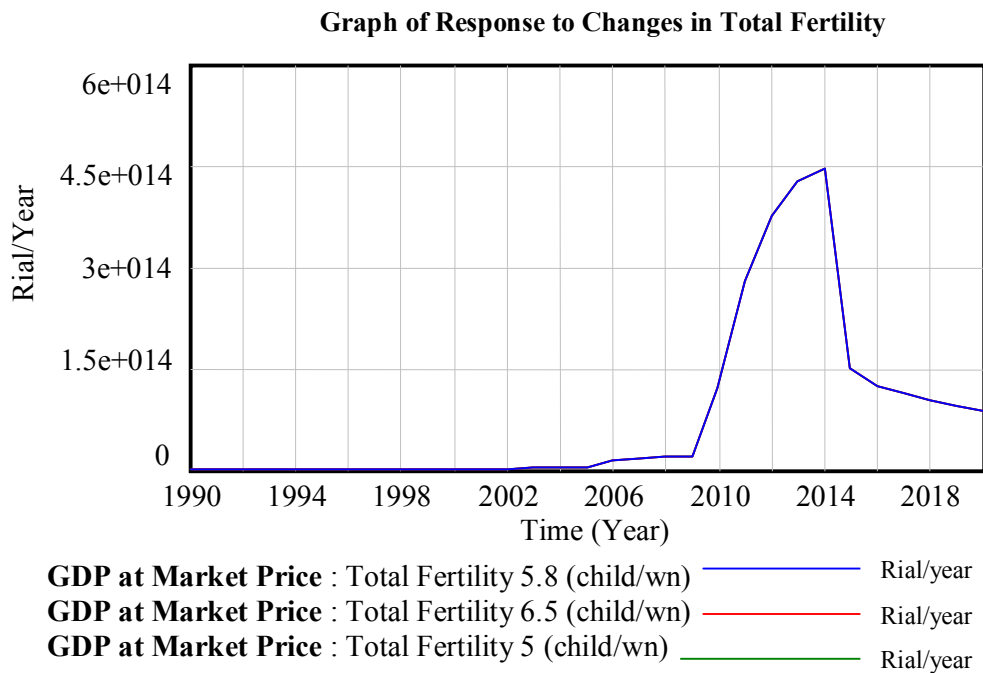


Figure (6-7): The effect of changes in “Total Fertility’

The GDP variable does not respond for change in Total Fertility. we are interested in the behavior of "Aggregate Demand ." and "GDP" What parameters and initial values should be used in a sensitivity analysis of the Yemen macroeconomic model?

We assume that Investment Fraction, Total Fertility, Fraction of private Consumption, Average Propensity to Consume, Investment Rate for Oil Sector and Investment Rate for agriculture Sector are the parameters which we use in sensitivity analysis of our model.

Second Scenario

We change value of parameter during the time as follow:

- 1- Increase of the Investment Fraction to one unit
- 2- Decrease of the Total Fertility to three *child/wn*
- 3- Decrease of the Fraction of Private Consumption to 0.5625
- 4- Decrease of Average Propensity to Consume to 0.6625
- 5- Increase of Investment Rate for agriculture Sector to 0.55
- 6- Decrease of Investment Rate for Oil Sector to 0.025

below graphs show response of the model to change in parameters which we selected in Second Scenario.

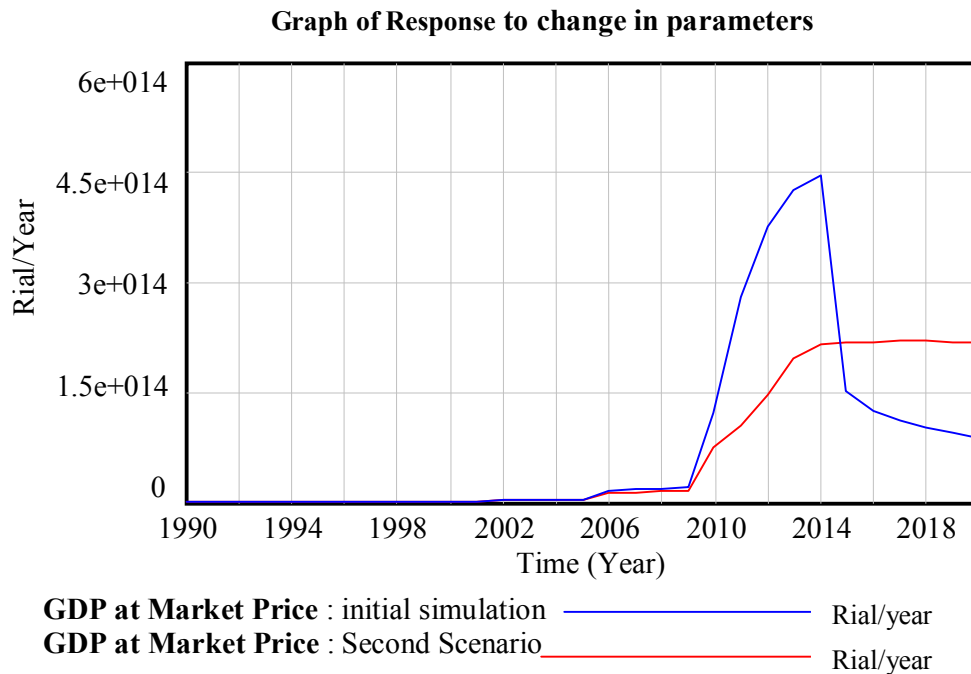
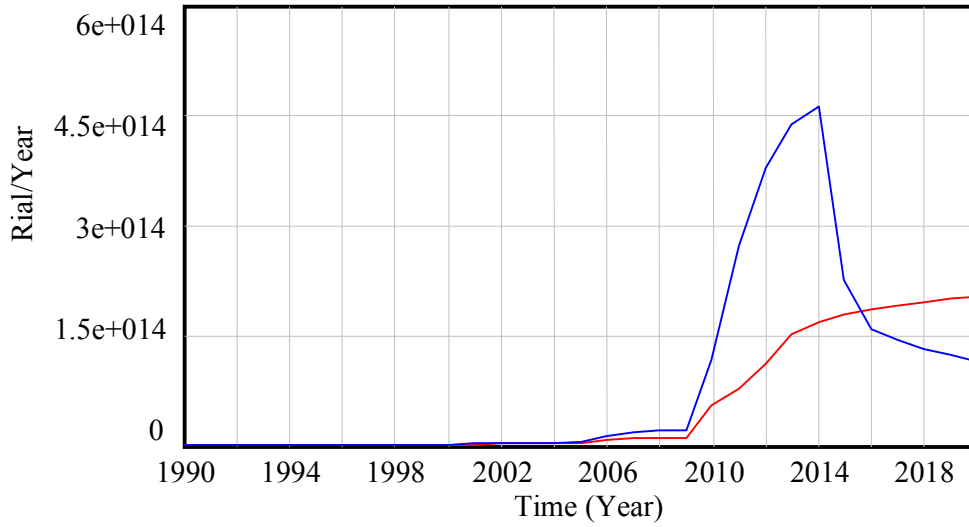


Figure 6-8: The effect of changes in parameters of Second Scenario

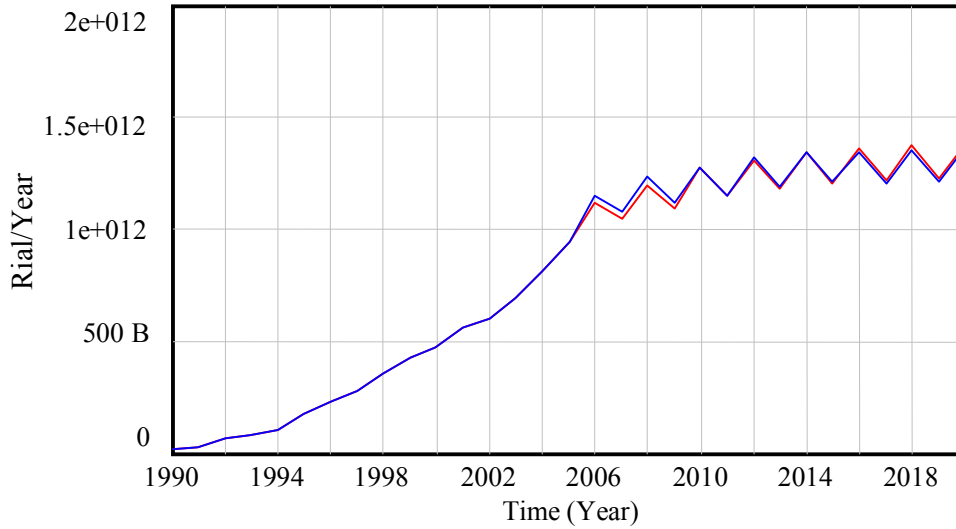
Graph of Response to change in parameters



Aggregate Demand : Initial Simulation — Rial/year
 Aggregate Demand : Second Scenario — Rial/year

Figure 6-9: The effect of changes in parameters of Second Scenario

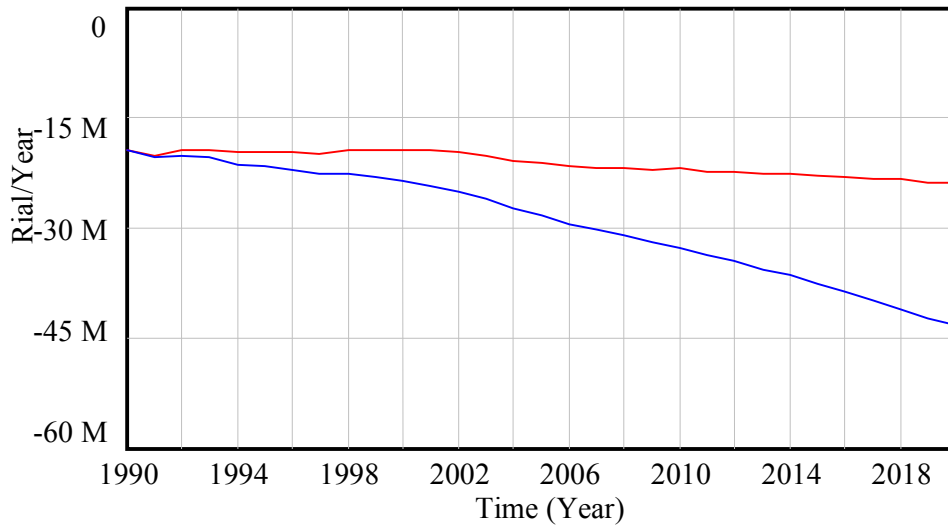
Graph of Response to change in parameters



Total of Agriculture Production : Initial Simulation — Rial/year
 Total of Agriculture Production : Second Scenario — Rial/year

Figure 6-10: The effect of changes in parameters of Second Scenario

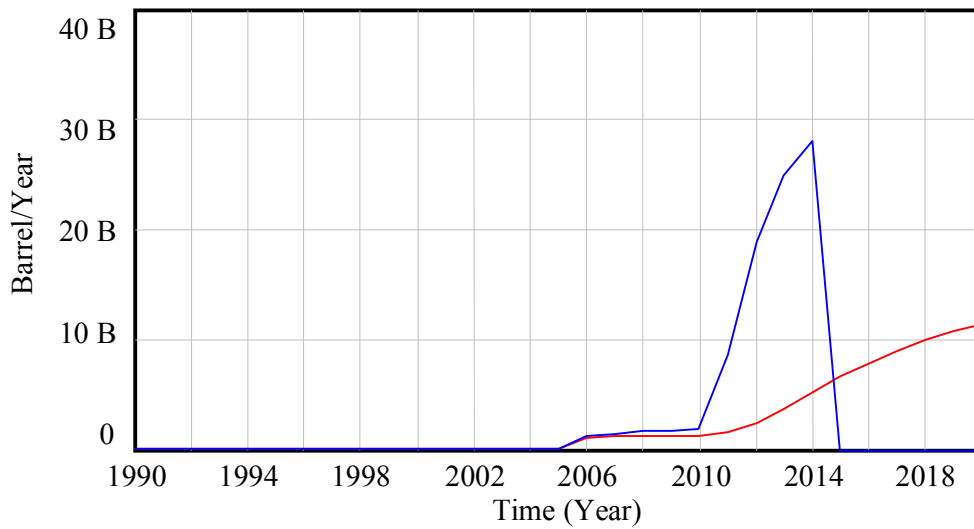
Graph of Response to change in parameters



Net Agriculture Export: Initial Simulation — Rial/year
Net Agriculture Export : Second Scenario — Rial/year

Figure 6-11 : The effect of changes in parameters of Second Scenario

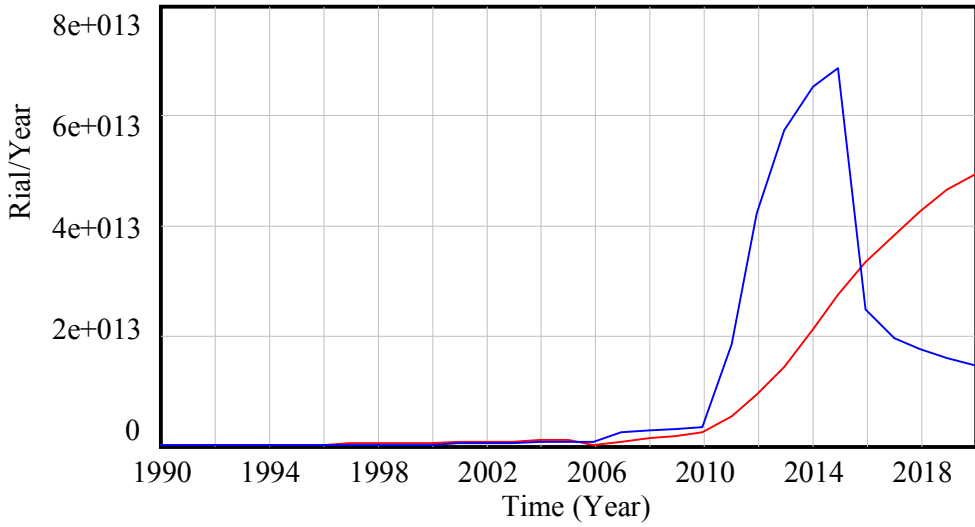
Graph of Response to change in parameters



Production Rate of Curd Oil : Initial Simulation — barrel/year
Production Rate of Curd Oil : Second Scenario — barrel/year

Figure 6-12 : The effect of changes in parameters of Second Scenario

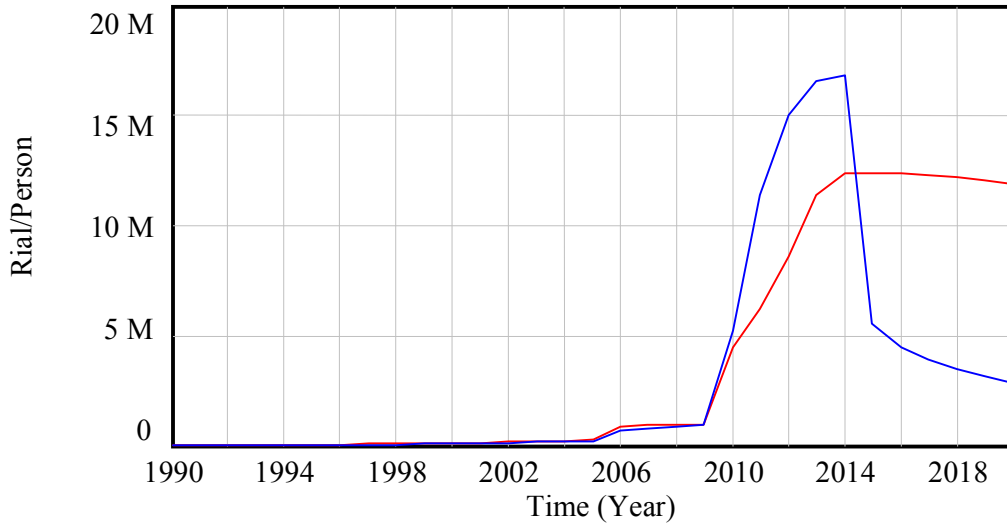
Graph of Response to change in parameters



Total Domestic Investment : Initial Simulation — Rial/year
Total Domestic Investment : Second Scenario — Rial/year

Figure 6-13: The effect of changes in parameters of Second Scenario

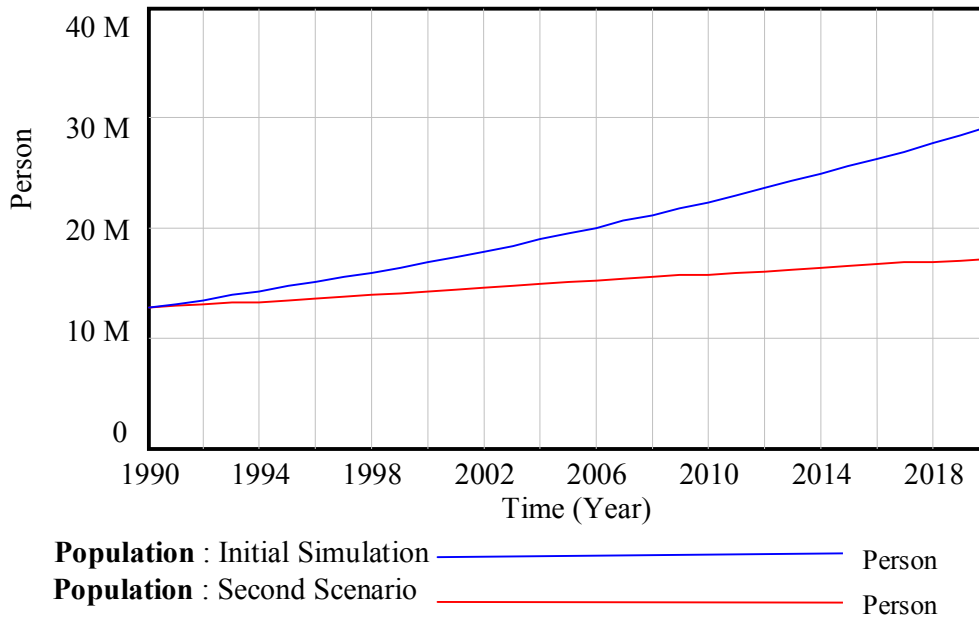
Graph of Response to change in parameters



Income per Capita YR : Initial Simulation — Rial/person
Income per Capita YR : Second Scenario — Rial/person

Figure 6-14: The effect of changes in parameters of Second Scenario

Graph of Response to change in parameters



Figure(6-15) : The effect of changes in parameters of Second Scenario

Sensitivity analysis again showed that changing the value of parameters makes some difference in the behavior of the model, while the general behavior mode is relatively insensitive to parameter changes. Some parameter changes affect the behavior to a larger extent than others. Changes in some parameters affect the equilibrium values. We can make a thousand of scenarios and notes for all change in variables or model behavior easily.

8. Conclusions

We studied System Dynamics models and its implementation on macroeconomics analysis to know the real behavior of complex system and solved the problem which emerge when we can't have more of data and we compared it with another models (regression). It is distinguished from others because it provides wide look for the problems and means of detecting changes in system which we study. Although the system contains more than 600 variables and their major interrelated relations, it is easily to be understood and competence of the controlling the change tools which give us distance of forecasting to a long term and ability to strategically planning.

System Dynamics models can provide better forecasts than traditional approaches. In and of itself, this should allow decision maker to make better decisions. But in addition, the use of System Dynamics models for forecasting allows decision makers to: (1) get an early warning of sectors structural changes, (2) identify key sensitivities and scenarios, and(3) determine appropriate buffers and contingencies for forecast inaccuracies. These benefits can further enhance business performance. Therefore we can define the System Dynamics as a modern type of statistical analysis depends on feedback data and concerns with making nonlinear and two-way relationships between variables interacting with each others to estimate parameters having more specificity and reality.

9. Recommendation

The importance of any statistical models establish from their ability to relating all variables which we think make effect on phenomena that we study, and our ability to change the structure of this model when we need that. also we can evaluate a quality of the statistical model and its ability to prediction for variables behavior when we use efficient estimate method for parameters to get much reality and less standard error with high statistical significance for expected values in the model. System Dynamics model provides us all above mentioned things. Therefore we recommend to use this model in studying all economical phenomenon and build real structure of all subsystem in our model and revise all of macroeconomic policies in Yemen. We need to make strategically planning for a long time for the wealth sources in our country because the result of the initial simulation in our model is very dread as long as we depend on oil production only to provide the economic activity. we must think about next generations and should make good plans by choosing perfect and scientific method to evaluate and analyze the present time to build the wide base for future. System Dynamic model leads us to know the behavior of system components now and in the future, also it enables us to change the economic, social, political, financial and educational policies and know the effects of change in our life.

10. References

1. Dominick S. (1982) Statistics and econometrics, theory and problems. McGraw Hill.
2. Hinkleley, N., Reid L. and Snell, E. (1991) Statistical theory and modeling. Chapman hall.
3. Frederic Barlat, Long-Qing Chen (2004) MONTE CARLO METHODS. Wiley Verlag GmbH.
4. Jonathan Pengelly, February 26, 2002,
5. Anthony S. Campagna, (1974) Macroeconomics Theory and Policy. University of Vermont.
6. Paul Samuelson & William D. Nordhous (1992) Economics. Fourteenth edition
7. Karl E, case, Ray c. fair 1989-1992, Principles of macroeconomic. second edition, prentice hall inc
8. Paul, W. (1989) Macroeconomic from theory to practice,. McGraw Hill,
9. Fernandez-Villaverde, Juan F. Rubio-Ramerez (2004) Estimating Macroeconomic Models: A Likelihood Approach.
10. Central Bank of Yemen (2006) World Economic Situation and Domestic Economic Developments report.
11. Central Statistical Organization (2005) Trade Statistics Indicators book.
12. Kevin Dooley (2002) Simulation Research Methods. Arizona State University.
13. Kristin den Exter (2004) Integrating Environmental Science and Management: The Role of System Dynamics Modeling, PhD Dissertation.
14. Allenna Leonard with Stafford Beer (19994)The system perspective: Methods and Models for the future.
15. Ford, A. (1999) Modeling the Environment: An Introduction to System Dynamics Modeling of Environmental Systems.
16. Craig W. Kirkwood (1998) System Dynamics Methods: A Quick Introduction, College of Business, Arizona State University, Original material copyright, 1998

17. Bernhard J. Angerhofer, Marios C. Angelides (2000) System Dynamics Modeling in supply chain Management: Research Review, Department of Information Systems and Computing, Brunel University, Uxbridge, Middlesex. UK.
18. Rudolf J. Freund, William J. Wilson (1998) Regression analysis, statistical modeling of a response variable. Academic Press.
19. Bill Harris (2000) Applying System Dynamics to Business: An Expense Management Example, <http://facilitatedsystems.com/>
20. Forrester, J. (1989) The Beginning of System Dynamics. System Dynamics Society, Stuttgart, Germany.
21. King, I. (2002) A Simple Introduction to Dynamic Programming in Macroeconomic Models, Department of Economics, University of Auckland. New Zealand.
22. Fernando Bignami, Luca Colombo, Gerd Weinrich (2000) A Dynamic Macroeconomic Model with Stochastic Rationing.
23. Schneider, M. and Spitzer, M. (2004) Forecasting Austrian GDP using the generalized dynamic factor model.
24. Jiuping Xu (2006) Modeling and simulation of a System Dynamics model for country cycle economy, World Journal of Modeling and Simulation Vol. 2, No. 3.
25. Lucia Breierova and Choudhari, M. (2001) An Introduction to Sensitivity Analysis. Massachusetts Institute of Technology.
26. James M. Lyneis (1998) System Dynamics in Business Forecasting: A Case Study of the Commercial Jet Aircraft Industry.
27. Loutfi M., Moscardini, O. and Lawler K., (1995) Using System Dynamics to analyse the Economic Impact of Tourism Multipliers, School of Computing, Engineering and Technology, University of Sunderland, Sunderland, United Kingdom.
28. Goldstein, H. (1999) Multilevel statistical models,, institute of education, multilevel models project. New York.
29. Kleijnen, J. (1990) Sensitivity Analysis of System Dynamics Models: Regression Analysis and Statistical Design.
30. Shoukath Ali. and Ramaswamy, N. (1993) Statistical Methods for Improving Confidence in System Dynamics Models. A case Study on Blood Bank Inventory Management Systems.
31. Lucia Breierova, Mark Choudhari (1996) An Introduction to Sensitivity Analysis Prepared for the MIT System Dynamics. Education Project Under the Supervision of Dr. Jay W. Forrester.
32. John D. Sterman (2000) Business Dynamics, system thinking and modeling for a complex world. McGraw-Hill.