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Earnings Dynamics of Men and Women in Finland: Permanent Inequality versus Earnings Instability^{*}

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Abstract

I decompose the variance of earnings of Finnish male and female workers to its permanent and transitory components and study their evolution between the years 1998 and 2007. I find that the increasing earnings inequality of men and women is driven by both transitory and permanent components of earnings. In addition, I find considerable differences in earnings dynamics between men and women that have been largely neglected in previous studies of earnings dynamics. The inequality among men is dominated by the permanent component. Conversely, permanent and transitory components are of comparable magnitudes to women. As a corollary, men face more stable income paths but with larger permanent earnings differences. Women, on the other hand, face more instable earnings profiles but have smaller permanent differences in earnings.

The correlation between initial earnings inequality and the growth in earnings inequality is found to be positive for both sexes, implying a divergence of earnings profiles towards end of the working career. In addition, earnings instability has risen for both sexes.

JEL codes: J31, J62

Keywords: Earnings distribution, earnings dynamics, permanent inequality, transitory inequality, variance decomposition

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1 Introduction

Growing earnings inequality has been a common phenomenon in most of the developed countries since the 1970s. The need to understand this phenomenon has spurred a great deal of research.

Traditional studies of earnings inequality in Finland as well as studies for other countries have concentrated on measuring cross-sectional earnings inequality and its year-to-year changes. Concentrating on cross-sectional inequality hides an important element of economic inequality, namely the mobility of individuals within the earnings distribution.

More recent studies on earnings dynamics stress the importance of decomposing earnings inequality into permanent and transitory components. These two components have a different impact on long run income differences and consequently have different welfare implications. If the rise in yearly income inequality is driven by the transitory component, it may suggest that earnings have become more risky. This, in turn, may decrease welfare if individuals are not able to completely smooth out income fluctuations. This might happen if earnings shocks are either very large or very persistent. On the other hand, if the rise in yearly income inequality is due to the changes in returns to education or other fixed worker attributes, it implies an increased inequality in career earnings as well. If the yearly income inequality is driven by the transitory component, we should observe more year-to-year mobility within the income distribution. This leads to an increase of inequality in the short term but not in the long run. If the permanent component dominates the transitory component, it implies that low earnings are a permanent rather than an isolated experience.

Examples of factors contributing to permanent component of earnings include changes in returns to education, skill, on-the-job training, or other factors that are relatively fixed from the point of view of an individual worker.¹

In this paper, I decompose year-to-year variance of earnings into permanent and transitory components and study their evolution over time by fitting an error component model to observed second moments of individual earnings processes using Finnish data. My data are based on filed tax reports, so measurement errors due to misreporting are arguably substantially smaller than they would be if the data was survey-based.

The vast majority of existing studies decomposing earnings inequality into transitory and permanent components only concentrates on males, making the implicit assumption that the earnings inequality of male workers is a good measure for overall earnings inequality.² The main contribution of this paper to existing literature is that I present measures of permanent and transitory components of earnings separately for men and women. This echoes the observations of Napari (2008), who reports substantial differences in fields of education between men and women and also substantial segregation of occupations and firms into those dominated by

¹It should be stressed that income volatility may or may not be equivalent to economic risk. As discussed in Blundell *et al.* (2008), earnings volatility does not necessarily translate into changes in welfare. Whether changes in income volatility have welfare implications depends on whether changes are anticipated and whether individuals are able to insure themselves against the instability of earnings.

²A notable exception is Ziliak *et al.* (2011), who reports measures of permanent and transitory earnings inequality separately for men and women as well as different educational groups, but does not limit their study to people working.

males and those by females, as noted by Korkeamäki & Kyyrä (2006). Consequently, the picture of earnings inequality based only on males might be misleading. To get comparable figures for men and women, I limit my sample to working males and females and compare their earnings dynamics.

In addition, no existing paper decomposes Finnish earnings inequality into permanent and transitory components. Therefore, I am able to compare earnings dynamics experienced by Finnish workers to earnings dynamics experienced by workers in countries with very different labor market institutions, e.g., Canada, U.K., and the U.S. Finally, my earnings data spans years between 1988 and 2007, allowing me to study relatively recent developments of earnings dynamics.

The current paper is heavily influenced by a series of papers studying the earnings dynamics in other countries. Pioneering studies in this field include Gottschalk & Moffitt (1994), Moffitt & Gottschalk (2002), Baker (1997), and Haider (2001), all of which have been highly influential in studying earnings dynamics in the U.S. by applying GMM estimation techniques. Following in their footsteps, Baker & Solon (2003) and Dickens (2000) present a similar decomposition for Canada and the U.K., respectively. Due to the larger data they have at their disposal, they are able to fit considerably more general models than the ones based on U.S. data. More recent papers using European registry based data fit variants of Baker & Solon (2003) and Dickens (2000). These include Gustavsson (2008), who studies a long Swedish panel from 1960 to 1990 and Ramos (2003) who studies British earnings data from the 1990s and Cappellari (2004), who studies Italian earnings data between 1970 and 1990. Even though the exact model specifications as well as time periods under consideration vary from country to country, the general finding in the aforementioned papers is that there are significant differences between countries in terms of earnings dynamics. This motivates replicating the analysis using data from other countries.

It turns out that increasing earnings inequality is driven by both, permanent and transitory components, but their contribution is different for men and for women. For men, permanent inequality dominates the transitory inequality. For women, they are of similar magnitude. In addition, permanent earnings differences vary substantially between cohorts. Male cohorts are more equal in terms of their permanent earnings compared to women. There has also been a trend increase in earnings instability of both sexes during the observation period.

This paper is structured as follows: Section 2 describes the data and the sample selection criteria. Section 3 introduces the model of earnings dynamics and outlines the estimation method. Section 4 provides results and visualizes them. Section 5 offers conclusions.

2 Data and sample selection

The data used consists of a panel of a one-third random sample of Finnish census. It covers the years 1988-2007.

The measure of earnings used in this paper is yearly work earnings before taxes. Earnings are calculated from individual tax files. To ensure comparability between years, all earnings are deflated to EUR 2007 using the Consumer Price Index. By definition, yearly earnings are given by hourly wage multiplied by the hours worked. Therefore, earnings inequality

reflects two dimensions of inequality, inequality in productivity and inequality in hours worked. Consequently, the variance of yearly earnings is higher than the variance of hourly wages unless the covariance of wages and hours worked is negative and large (Abowd & Card, 1989).

My measure of earnings inequality is the variance of log yearly earnings. This is the standard in papers studying earnings dynamics. The motivation for the choice of inequality measure is that the mathematical properties of variance are well established. In addition, the correlation between the variance of log earnings and other widely used inequality measures is very close to 1. The downside of this choice is that it is not measure-free. Thus, the choice of currency units and base year affects the measure of total earnings inequality. Nonetheless, the measure only affects the *level* of inequality, but not the *changes*. Moreover, the decomposition is unaffected by the measure.

Registry data has some advantages over survey data. Since earnings information is collected as a part of the administrative process, non-response and incorrect answers can be ruled out resulting in extremely reliable data on earnings.³ Attrition from the data can happen only by migration or death. A possible caveat of using a long time series derived from tax registries is that variable definitions may vary over time. Even though the definition of total taxable income has changed as tax laws have changed during the period of 1988-2007, the definition of taxable earnings has remained stable.

Concentrating only on work earnings naturally hides some of the income differences prevalent in the society, because the total income of individuals is defined as a sum of earnings, capital income, income transfers recieved and taxes paid. Supplementing earnings data by including capital incomes is not feasible due to limited data. Moreover, including income transfers and paid taxes would introduce problems because changes in tax laws and social security eligibility rules would severely limit the length of the time series. Another reason to prefer the measure of income chosen in this paper is that it is broadly equivalent to other papers published, thus facilitating international comparisons.

A minor caveat in the data for the purposes of this paper is that earnings of over 200,000 Euros are top-coded due to statistical secrecy laws. This group is small (between .01 % and .05% of yearly observations), so their effect to estimates is arguably small.

2.1 Sample selection criteria

The sample selection criteria are adopted from Haider (2001). The motivation for these criteria is to ensure that earnings dynamics of people who are working are not confounded by people who are switching between work and non-work.

The target group in my sample is prime age working males and females aged between 26 and 60 who are observed for at least six years. I assume that by age 26, people have mostly finished their educations.

I include person-year observations only if the main type of activity of a person is "working". In other words, I exclude students, the unemployed, the retired, and other people outside of the workforce. I limit my attention to people who are working because my interest is in earnings

 $^{^{3}}$ Gottschalk & Huynh (2010) show that earnings inequality decompositions based on PSID most likely overstate both earnings mobility and earnings inequality because of non-classical measurement errors.

dynamics of people who are consistently above the extensive margin. I also exclude working people with zero yearly earnings.

After applying the sample selection criteria, I am left with a "revolving unbalanced panel" (following the terminology in Haider, 2001). The panel is unbalanced because all cohorts are not observed for all years. The length of the panel varies between 6 and 20 years, depending on the cohort. Using an unbalanced panel breaks the collinearity between year, age, and cohort, making it possible to identify all of them separately. Since people are included only if they fulfill the criteria of selection, they may enter and exit the panel. This feature makes the panel revolving.

Applying a revolving unbalanced panel overcomes problems related to compositional changes in the workforce related to the business cycle. If workers with instable earnings only enter the workforce during an economic boom, they are not included in the data, as long as other sample selection criteria are not fulfilled. For example, assume that a person fulfills the age criteria of selection and is working in years 1988 and 1990–1994, total of 6 years. In this case, the earnings observations of the person only contribute to the estimation of earnings dynamics in the years he is observed. Another person, who is working for only 5 years, does not contribute to the estimation at all.

Since it might be likely that individuals with very volatile earnings are also more likely to permanently exit the panel, the approach chosen here introduces potential bias to the estimates. Correcting for attrition is not feasible because the data lacks instruments for selection. Still, the approach chosen here is less restrictive than analyses based on fully balanced panels. In addition, including only people with no breaks in their earnings histories would probably overstate the contribution of permanent earnings component. Using a revolving panel also allows much larger sample sizes compared to a balanced panel.

Previous papers studying the covariance structure of earnings concentrate only on males. This is because changes in female workforce participation might confound estimates of earnings instability of women. I use a revolving unbalanced panel, which overcomes this problem at least partially. Furthermore, the labor force participation rate of Finnish women is very high (Pissarides *et al.*, 2003), which means that endogenous participation is less of a problem than in some other countries.

Even though sample selection criteria somewhat differ from other studies due to different structure of data used, they are consistent within the observation period, thus enabling comparisons between years. Comparisons between countries, on the other hand, might be subject to criticism.

I categorize people in two year birth cohorts and follow each cohort through time. Studies based on smaller data have been forced to pool all cohorts together due to small sample sizes. This naturally hides some of the heterogeneity of earnings dynamics between cohorts.

The total size of the sample used in the analysis is given in Table 1. The sample sizes are considerably larger than those used by other researchers. For example, the total sample size in Haider (2001) is 32,105 individuals and sample size in Gustavsson (2008) is 76,709 individuals.

2.2 Covariance structure of earnings by cohort

In Figure 1, I plot the observed earnings variance for workers selected by the selection criteria given above. For both sexes, the variance decreases between years 1988-1991, and thereafter it goes up until it peaks around 1994. After 1994 earnings inequality goes down somewhat but remains high until the end of the sample period. The variances plotted in Figure 1 are somewhat higher than those observed in most other similar studies. This might be because I cannot discriminate between full-time and part-time workers. Moreover, in studies based on filed income tax reports, earnings are censored from below, because income below the tax limit is not observed. This is not the case in this paper.

To grasp the essential features of earnings dynamics, it is useful to inspect the autocorrelation profiles of earnings by year and cohort. I have calculated yearly variance as well as autocovariances between years for people who are observed in both years. For cohorts which are observed for the full twenty years this adds up to $21 \times 20/2 = 210$ unique covariance elements and less for other cohorts. In total, unique elements of covariance matrices add up to 3,066 covariance elements.

Figure 2 presents the yearly variances and covariances between yearly earnings for selected cohorts of men and women. Figure 2 demonstrates that there are substantial differences in variances as well as autocovariances of male and female earnings. This suggests that there are considerable differences in earnings dynamics of men and women, making it reasonable to estimate separate models for men and women. In addition, comparison of years reveals strong year effects. These are especially apparent during the recession of the early 1990s. The difference of variance and first autocovariance is relatively large. In addition, autocovariances remain positive even at long lags, indicating that there are considerable permanent earnings differences. Finally, the variance and the autocovariance values are larger for the oldest cohort even at longer lags, which suggests the presence of cohort effects in permanent component of earnings.

An alternative way to study cohort covariances is to keep the year fixed and plot covariances by age. This is done for three selected years in Figure 3. Comparing years reveals that income variances and covariances have risen with time for men as well as for women, which indicates that earnings inequality has increased during the panel time and at least part of this rise is due to rise in permanent earnings differences. The variances are higher for young women than for young men, but as people grow older, the higher growth in variances of male earnings causes men to overtake women in terms of earnings inequality. The difference between the variance and autocovariances of earnings is at its largest for young women, indicating that high earnings inequality of young women is driven by transitory differences. For men, the difference between variance and covariances remains almost constant with respect to age.

To summarize, in addition to being able to disentangle permanent and transitory income differences, the preferred model for earnings inequality should allow cohort as well as year effects. The model should also allow for the variances of permanent and transitory components to change as people age.

3 Model and estimation

In this section, I introduce the econometric model and the estimation methodology. I estimate an error-components model with permanent and transitory components. The model allows individuals to permanently differ in their mean earnings as well as the earnings growth rate. The transitory component is modeled as an AR(1) process. As a result, even transitory shocks are allowed to exhibit persistence and take more than a year to dampen.

3.1 Econometric model

Let Y_{ibt} denote log earnings in year t of person i born in year b. Individual earnings can be expressed as deviations from means, or

$$Y_{ibt} = \mu_{bt} + y_{ibt}.$$

Since my interest lies in the second moments of the distribution of Y_{ibt} , it suffices to write a model for de-meaned wages y_{ibt} . Expressing μ_{bt} as cohort-age means captures average year, age, and cohort effects in a more flexible fashion than using regression models with cohort-specific polynomials. The simplest possible model for y_{ibt} is

$$y_{ibt} = p_t \alpha_{ibt} + \lambda_t \varepsilon_{ibt} \tag{1}$$

where the two are orthogonal to each other. Equation (1) can be seen as a Mincerian earnings equation of relative earnings, where α_{ibt} stands for the observed characteristics of individuals and ε_{ibt} is the error term. p_t and λ_t are year-specific factor loadings. Applying variance operator to both sides yields

$$var(y_{ibt}) = p_t^2 \sigma_\alpha^2 + \lambda_t^2 \sigma_\varepsilon^2.$$
⁽²⁾

Equation (2) gives the basic intuition of variance decomposition. $p_t \sigma_{\alpha}^2$ denotes the variance of the permanent component of earnings, and $\lambda_t \sigma_{\varepsilon}^2$ denotes the variance of the transitory component. An increase in either component increases the dispersion of earnings, but an increase in $\lambda_t \sigma_{\varepsilon}^2$ also implies that churning within the earnings distribution increases.

Even though Equation (2) is intuitive, it may be too restrictive for two reasons. First, the variance of transitory shocks may exhibit age-related heteroskedasticity because workers in the start of their careers may have more instable earnings.⁴ In addition, different cohorts may have different skills or other characteristics that affect the variability of their earnings. To incorporate these features, the following generalization of Equation (1) is used

$$y_{ibt} = q_c p_t u_{ibt} + \varepsilon_{ibt},\tag{3}$$

where

$$u_{ibt} = \alpha_i + \beta_i x, \tag{4}$$

$$\varepsilon_{ibt} = \rho \varepsilon_{ibt-1} + \lambda_t \nu_{ibt}, \tag{5}$$

⁴Meghir & Pistaferri (2004) report significant heteroskedasticity in earnings instability using U.S. data, albeit using a different model. Baker & Solon (2003) and Gustavsson (2008) reach similar conclusions using Canadian and Swedish data, respectively.

where α_i , β_i and ν_i are random variables with distributions:

$$\begin{bmatrix} \alpha_i \\ \beta_i \end{bmatrix} \sim \left(\begin{bmatrix} \bar{\alpha} \\ \bar{\beta} \end{bmatrix}, \begin{bmatrix} \sigma_{\alpha}^2 & \sigma_{\alpha\beta} \\ & \sigma_{\beta}^2 \end{bmatrix} \right)$$
(6)

and

$$\nu_{ibt} \sim \left(\bar{\nu}, \gamma_0 + \gamma_1 x + \gamma_2 x^2\right). \tag{7}$$

x is defined as the potential experience of each cohort in year t, i.e., x = t - b - 26.

In Equation (4) u_{ibt} is a random growth term. It describes the permanent component of earnings. σ_{α}^2 reflects variance of earnings profiles of individuals at the age of 26, and the variance in σ_{β}^2 reflects the deviation of individual-specific growth rate from the average growth rate of each cohort (the average growth rate is captured in μ_{bt}). p_t and q_c are year and cohort factor loadings, respectively.

The transitory component of earnings in (5) is given by a mean-reverting AR(1) process. λ_t are year-specific factor loadings on the innovation ν_{ibt} . This specification assumes that an earnings shock takes more than one year to dampen out and that earnings shocks accumulate over time. In addition, Equation (7) allows transitory variance to be a quadratic function of age. Transitory and permanent components of earnings are assumed to be orthogonal to one another. To make identification possible, I have normalized p_{1988} and λ_{1989} and $q_{1951-1952}$ to 1.

Equations (3)–(7) generate non-stationarity to the variances of earnings processes through time-varying factor loadings for the permanent and the transitory components, p_t and λ_t . Another source of non-stationarity is the polynomial form of the variance of transitory shocks. The intuition remains the same: a rise in p_t or q_c increases permanent inequality of workers, whereas a rise in λ_t increases the shuffling of workers.

In line with the model specifications in Baker & Solon (2003) and Gustavsson (2008), the polynomial form of $var(\nu_{ibt})$ recognizes that earnings instability may vary between individuals because they are at different stages of their careers. Yearly factor loadings for permanent and transitory components also give insights in to forces driving changes in income distribution.

The motivation of formulation in Equation (4) is both theoretical and empirical. It has been successfully applied in, e.g., Haider (2001), Ramos (2003), and Cappellari (2004) who demonstrate that in addition to allowing heterogeneity in mean earnings, the slope of earnings and the covariance of the two are important in capturing the dynamics of earnings. In most previous studies, the covariance term $\sigma_{\alpha\beta}$ is found to be negative. This is consistent with the on-the-job training hypothesis (see, e.g., Lillard & Weiss, 1979; Hause, 1980; and Baker, 1997), which states that individuals may accept lower earnings in the beginning of their career, since they anticipate that their earnings will rise at a high enough rate and for a long enough time that they will be compensated for the low earnings at the beginning of their career. On the other hand, if $\sigma_{\alpha\beta}$ is found to be positive, it is consistent with a schooling-matching hypothesis, in which more skilled workers are endowed with more education, which raises their initial earnings and face faster earnings growth as the quality of the match is revealed to their employers (Cappellari, 2004). In addition to the specification in Equations (3)–(7) usually known as "random growth specification" I have also experimented with other specifications. Particularly, another widely used specification for the permanent component is the so-called "random walk specification" (e.g., Gustavsson, 2008). This model is given by $u_{ibt} = u_{ibt-1} + \xi_{it}$, where ξ_{it} is a white noise process. The main difference between the two formulations is that the random growth specification allows the correlation of the intercept and slope terms to be nonzero, whereas the random walk specification. Trials with the random growth specification always resulted in a statistically significant estimate for $\sigma_{\alpha\beta}$. I interpret this as a sign that a random walk model is inconsistent with the observed covariance structure of earnings. Random walk and random growth specifications have different implications in terms of age-derivative of cross-sectional variances. Under the random growth specification, the variance of earnings increases linearly with age, whereas under the random growth specification, the growth of permanent earnings inequality is either convex or concave, depending on the sign of $\sigma_{\alpha\beta}$ (Guvenen, 2009).⁵

3.2 Estimation

Direct estimation of a model based on equations (3)-(7) is inefficient because it means estimating α_i and β_i for each individual with only a small number of observations. Since I am interested in the second moments of earnings distribution, I estimate them directly. To accomplish this, I write down the variance of earnings on year t for cohort b implied by (3):

$$var(y_{ibt}) = q_c^2 p_t^2 \left[\sigma_\alpha^2 + x^2 \sigma_\beta^2 + 2x \sigma_{\alpha\beta} \right] + \rho^2 var(\varepsilon_{ibt-1}) + \lambda_t^2 var(\nu_{ibt}).$$
(8)

Respectively, a general covariance element between year t earnings and year t - h (h > 0) earnings is given by⁶

$$cov(y_{ibt}, y_{ibt-h}) = q_c^2 p_t p_{t-h} \left[\sigma_{\alpha}^2 + x(x-h) \sigma_{\beta}^2 + (2x-h) \sigma_{\alpha\beta} \right] + \rho^h var(\varepsilon_{ibt-h}).$$
(9)

The term $var(\varepsilon_{ibt})$ is calculated by backtracking the recursion in Equation (5) until the first sample year of each cohort. Since earnings time series are relatively short, consequent covariances depend on the variance of initial shock that flaws the standard time series analysis assumption of zero initial conditions. I follow suggestions of MaCurdy (1982; 2007), and treat the variances of initial shocks as extra parameters to be estimated. This parameter also takes into account the earnings differences accumulated before the start of sample.⁷

⁵Since random walk and random growth specifications do not necessarily rule each other out, some researchers (e.g. Baker & Solon, 2003 and Ramos, 2003) incorporate both into the same model. In my data, this specification either does not converge or results in negative variance estimates.

⁶Identification of earnings instability is made possible only by the off-diagonal elements of the covariance matrix. Intuition for this that a high correlation between earnings at t and earnings at t - h implies that instability is low and vice versa.

⁷Initial variance parameters have different interpretation depending on whether the earnings trajectories of cohorts are left-censored. For a cohort which has been 26 years old before 1988, the initial variance is a measure of transitory variance accumulated before 1988, whereas for a cohort which is observed for the first time after 1988, the initial variance is a measure of labor market conditions at the time of labor market entry.

Since the panel is revolving, an individual can only contribute to the covariance matrix if he or she is observed in years t and t - h. The sample covariances are thus calculated as the earnings covariance of people who are observed in both years. Consequently, people who have a higher attachment to the labor market contribute more to the empirical covariance matrices, which leads to a sample selection problem of some degree, that cannot be completely overcome by unbalanced revolving panel construction. This is a common caveat in papers of this genre.

The estimation boils down to minimizing the distance between cohort earnings covariances implied by the model and the empirical autocovariances calculated from the data. I stack each unique covariance matrix elements into vector **C**. Estimation is done by GMM, i.e., by minimizing the distance between observed autocovariances **C** and those implied by the model $\mathbf{F}(\theta)$, where θ is a vector of 87 parameters to be estimated. In practice, I minimize the standard GMM criterion function

$$H = \left[\mathbf{C} - \mathbf{F}(\theta)\right]' \mathbf{W} \left[\mathbf{C} - \mathbf{F}(\theta)\right].$$
(10)

Altonji & Segal (1996) demonstrate that using the asymptotically optimal GMM weighting matrix, i.e., choosing $\mathbf{W} = \left[\mathbf{F}(\theta)' \mathbf{F}(\theta)\right]^{-1}$, can lead to very large finite-sample bias. This is due to correlation of sampling errors in second and fourth moments leading to $\left[\mathbf{F}(\theta)' \mathbf{F}(\theta)\right]^{-1}$ being very close to singular. Following the bulk of the income covariance literature, I have chosen identity matrix as the weighting matrix. This approach is called the Equally Weighted Minimum Distance (EWMD) estimation (Chamberlain, 1984). Using the identity matrix as the weighting matrix gives consistent but generally inefficient estimates.⁸

The asymptotic standard errors of vector θ are given by:

$$var(\theta) = (\mathbf{D}'\mathbf{D})^{-1} \mathbf{D}' \mathbf{\Omega} \mathbf{D} (\mathbf{D}'\mathbf{D})^{-1},$$

where $\mathbf{D} = \frac{\partial \mathbf{F}}{\partial \theta}$ and $\Omega = [\mathbf{C} - \mathbf{F}(\theta)]' \mathbf{Q} [\mathbf{C} - \mathbf{F}(\theta)]$ are evaluated at the solution $\theta = \hat{\theta}$. \mathbf{Q} is a block diagonal matrix of ones, thus setting covariances between cohorts zero.

4 Estimation results

4.1 Parameter estimates

Figure 4 decomposes total inequality into its permanent and transitory components. The decomposition is based on equation (8). The term $p_t^2 \left[\sigma_{\alpha}^2 + x^2 \sigma_{\beta}^2 + 2x \sigma_{\alpha\beta}\right]$ accounts for the permanent component of earnings and term $\rho^2 var(\varepsilon_{ibt-1}) + \lambda_t^2 var(\nu_{ibt})$ accounts for the transitory component.

The contribution of permanent earnings inequality to total inequality larger for men than for women in almost all years. This implies that permanent inequality among men is larger than among women. The permanent inequality among men has remained roughly similar

⁸Using the identity matrix as the weighting matrix makes estimation of (10) equivalent to regressing vector **C** to vector **F** (θ) by nonlinear least squares.

except for the recession years 1991 and 1992. Even though the magnitudes of different components are distinct between sexes, the dynamics of the two components of earnings inequality have been roughly similar for both sexes for the entir.

The transitory components of earnings inequality of men and women are highly correlated, albeit transitory inequality is higher for women than for men. To see which parameters drive the patterns observed in Figure 4, Tables 2 and 3 present the estimates of the parameters of permanent and transitory components. I discuss both parameters in turn.

A first look at Tables 2 and 3 shows that most parameters are accurately estimated in spite of the model being flexibly parameterized and including year, cohort, and experience effects.

Table 2 reports the parameters of permanent earnings differences. The level term σ_{α}^2 is statistically significantly larger for men than for women. The slope term σ_{β}^2 and the correlation term $\sigma_{\alpha\beta}$ are of similar magnitude for both sexes. Moreover, the estimated correlation between the intercept and slope terms is positive. This means that people who have higher initial earnings also have larger earnings growth. As a result, permanent earnings distribution becomes increasingly unequal over the life cycle. Cappellari (2004) reports a similar finding for Italy, but other studies I am aware of (e.g., Haider, 2001; Baker & Solon, 2003; Baker, 1997) report a negative parameter estimate.

For men, year loadings on permanent earnings component are almost constant except for the two deepest recession years. For women, there is a downward trend in yearly loading indicating that the variability in returns to fixed characteristics has decreased during the end of the 1990s and early 2000s. Year loading on the permanent component are often interpreted as prices of fixed characteristics of individuals, keeping cohort effects constant.

Next, I turn to estimates for the cohort loadings on the permanent component q_c . The most intuitive interpretation for cohort loadings of permanent component is that they are a measure of the dispersion of skills within a cohort. An alternative interpretation for q_c is that they reflect very persistent shocks that affect cohorts differently even if the skill dispersion of cohorts does not change. An example of these shocks is long-term effects of graduating in a recession (see e.g., Kwon *et al.*, 2010, and Oreopoulos & von Wachter, 2008).

Coinciding with the decrease in yearly factor loadings for women is the increase in cohort loadings of the permanent component of earnings. This implies that earnings inequality for all women has decreased after the 1990s, but at the same time, younger cohorts are more unequal than older cohorts. In other words, as younger cohorts have become more skilled, within cohort inequality has increased but at the same between-cohort inequality has decreased. For men, the inequality time trend is of opposite sign: younger cohorts are more equal than older.

Finally, I turn to the estimates for the transitory component reported in Table 3. I discuss the parameter of the AR-process first. The persistence of transitory shocks is considerably lower in Finland in comparison to most other studies. Baker & Solon (2003), Dickens (2000), and Haider (2001) report estimated autocorrelation values in the range of 0.6 and 0.95, but they concentrate on full- time working males. In contrast, Ramos (2003) does not discriminate between full-time and part-time workers and finds $\hat{\rho}$ values in the range of 0.29 and 0.41, which are considerably closer to my estimates. This suggests that the variation in hours worked substantially reduces the persistence of transitory earnings shocks.

Three lines at the bottom of Table 3 give the parameters of age-heteroskedasticity. The age profile of the variance of transitory shocks, visualized in Figure 5, is strikingly different

between men and women. For men, γ_1 and γ_2 do not statistically significantly differ from zero, which implies that there is no age-related heteroskedasticity in variance of transitory shocks. For women, on the other hand, the variance of transitory shocks is decreasing and convex. For women under 30, the variance of transitory shocks is over double that of men. Also, regardless of cohort, initial earnings shocks are considerably higher for women than for men. This observation is roughly consistent with Lundberg & Rose (2000), who find that motherhood decreases the supply of labor of those married women who are attached to the labor market but not their wages.

Year loadings on transitory component of earnings λ_t also exhibit different trends for men and women.⁹ For men, they rise and peak in the year 1994. Thereafter, they decline somewhat but still remain above one until year 2007. For women, there is almost a constant rising trend from 1988 to 2007.

Adding cohort loadings to transitory component always resulted in convergence problems. This suggests that cohort effects on the transitory component over-parameterize the model. Therefore, earnings instability seems to be symmetric for all cohorts after accounting for initial conditions. Earnings instability seems to be more related to labor market conditions prevailing in the society rather than to differences in human capital within cohorts. Nonetheless, for both sexes, the contribution of rising earnings instability is substantial. This gives strong evidence that earnings have become more instable.

Making comparisons to other countries is somewhat suspect, because separating prevailing differences in labor market conditions from differences in data is not straightforward. The most comparable study to the current one in terms of data is Ramos (2003), who studies male earnings inequality in the U.K. between 1991 and 1999. In comparison to Ramos' findings, the permanent earnings differences among British men seem larger than those of Finnish men, regardless of birth year.

A potentially interesting comparison can be made to Sweden, another Nordic country with a similar institutional setting to Finland. Gustavsson (2008) fits a model for Sweden that spans years 1960-1990. Comparing the end of Gustavsson's sample to the beginning of my sample reveals large differences. My estimates for the contribution of the transitory component to total inequality are substantially larger than the estimates presented in Gustavsson's study. This discrepancy is at least partly explained by differences in sample composition – especially by the fact that Gustavsson limits to full-time workers.

4.2 Decomposition analysis: cohorts and years

The parameter estimates only give a partial clarification on the evolution of earnings dynamics. As discussed in the previous subsection, there is substastial heterogeneity between cohorts and years. The total inequality is a compound of age, cohort, and year effects. To get further insight on these differences, this subsection introduces the decomposition for various years and cohorts.

Figure 6 plots the decomposition of earnings differences for 3 different cohorts: those born in 1943-1944, 1955-1956 and those born in 1967-1968.¹⁰ Comparing the two pictures reveals

⁹To identify both λ_t and the initial variance parameters σ_c^2 , λ_{1988} is left unrestricted.

¹⁰Plotting other cohorts produces similar pictures.

that the permanent earnings differences between cohorts are considerably higher among men than among women. Secondly, the permanent earnings differences between cohorts are larger among men than among women. The dynamics of permanent earnings differences resemble one another for all cohorts. Permanent earnings differences have risen between 1988 and 2007, regardless of gender and cohort.

Turning to cohort differences in transitory earnings inequality, the transitory differences among men are very small. The transitory earnings differences are almost identical, apart from the initial earnings differences of the youngest cohort. Conversely, the transitory earnings differences among women are decreasing: earnings instability of young women is considerably larger than that of older women.

Figure 6 suggests that permanent earnings differences have grown regardless of age, which suggests earnings inequality driven by increasing year loadings. Figure 7 gives an alternative view of earnings differences: it looks the differences in a single year, but includes all cohorts. Again, we observe a growing permanent inequality as people age. The age-permanent inequality gradient is especially strong for men. The earnings instability is decreasing in age for both sexes. In addition, we see that the earnings instability has grown, regardless of age.

The underlying assumption in the preceding discussion is that the model is correctly specified and all parameters are strongly identified. The following section discusses evidence that speaks in favor of strong identification.

4.3 Identification

A note on the identification of models of second moments of earnings is in order. Generally, weak identification can arise if the moment condition is small but not zero at a range of values differing from the true parameter value θ_0 . Stock & Wright (2000) show that the asymptotic theory devised for identified models is invalid for weakly identified models. As a result, parameter estimates of weakly identified models are inconsistent, and the calculated covariance matrix does not converge to the true covariance matrix, resulting in invalid estimates for standard errors. Furthermore, even if most parameters are strongly identified parameters. In the context of this paper, weak identification may arise if ρ is close to 1. If $\rho \approx 1$, the transitory component is very close to being permanent. This causes problems in identification, since both the transitory and the permanent components reflect relatively permanent earnings inequality, making it difficult to distinguish them from one another, especially, if panel length is short.

Doris *et al.* (2010) gives Monte Carlo evidence on the ranges of parameter values that lead to biased estimates. According to Tables 2a and 3 in their paper, a model estimated using eight panel years of observations and $\rho = .8$ is sufficient to give unbiased results. Since my panel length is well over that for most cohorts (median panel length in my data is 17 years) and my estimates of ρ are well below .8, I am confident about the strong identification of the models estimated. In addition, linear time trends in any factor loading might also weaken the identification. Such trends are not present in my data.

I have not applied Newey's (1985) specification test to assess the goodness of fit because the general finding in earnings dynamics literature is that the null hypothesis of correctly specified model is virtually always rejected. According to Baker & Solon (2003), these tests have inflated sizes when the amount of overidentifying restrictions is as large as in this case (3,066 moment conditions used to identify 87 parameters).

Another possible caveat, according to warnings in Baker & Solon (2003) and Shin & Solon (2011), is that an arbitrary change in parametric model may lead to different conclusions. I have experimented with a wide selection of specifications and find this concern misplaced for two reasons. First, random walk and random growth specifications for the permanent component of earnings give quite similar results (estimates for the random growth specification are not reported). Secondly, more complex specifications for the transitory and permanent components fail to converge. These two facts suggest that my preferred model correctly captures the relevant aspects of income dynamics.

5 Summary and conclusions

Previous research has shown that earnings inequality has risen in Finland during the last two decades. This paper decomposes yearly Finnish log earnings inequality of the working population into its permanent and transitory components separately for men and for women. The econometric analysis is based on the second moments of log-earnings using the minimum distance estimation method of Chamberlain (1984).

I find that the increase in earnings inequality within men as well as within women is driven by both the permanent and the transitory components, but the contributions of these components are of different magnitude for men and women. The permanent component of earnings inequality is larger in magnitude for men than for women. The age-derivative of permanent earnings inequality of men and women is similar, indicating that the relative differences in permanent earnings stay similar throughout the careers of men and women. In addition, the correlation between initial earnings inequality and the growth in earnings inequality is found to be positive for both males and female, implying a divergence of earnings profiles and increasing permanent earnings differences towardt the end of the working career. As a corollary, men face more stabile income paths but with larger permanent earnings differences. Women, on the other hand, face more instable earnings profiles but have smaller permanent differences in earnings.

In addition, the contribution of transitory shocks to inequality has risen considerably for both sexes. This strongly suggests that earnings have become more instable during the last 20 years.

Since the measure of income used in this paper is pre-tax earnings, contributions of taxes and public transfers to total inequality are not observed. Since Finland has a highly redistributive social insurance system, a complementary analysis concentrating on usable income instead of pre-tax earnings is called for.

Finding ultimate causes for changes in persistent and transitory inequality is beyond the scope of this paper, but some tentative explanations can be devised. First, a possible explanation to the rise in permanent earnings inequality is changes in returns to education. Since there are no clear trends in year loadings, it seems unlikely that such upward trending returns to education have played a strong role in the time period. Increasing cohort effects on permanent female earnings inequality suggest that younger working women face higher permanent

earnings inequality than older women. It seems more plausible that this is due to high employment participation of young women rather than changing returns to skills because there is no such trend for cohorts of men.

Finally, lessons from this paper suggest that the standard approach of concentrating only on males might hide potentially important aspects of earnings dynamics prevalent in the society.

References

- Abowd, John M, & Card, David. 1989. On the Covariance Structure of Earnings and Hours Changes. *Econometrica*, **57**(2), 411–45.
- Altonji, Joseph, & Segal, Lewis. 1996. Small-Sample Bias in GMM Estimation of Covariance Structures. Journal of Business and Economic Statistics, 14(3), 353–366.
- Baker, Michael. 1997. Growth-Rate Heterogeneity and the Covariance Structure of Life-Cycle Earnings. *Journal of Labor Economics*, **15**(2), 338–75.
- Baker, Michael, & Solon, Gary. 2003. Earnings Dynamics and Inequality among Canadian Men, 1976-1992: Evidence from Longitudinal Income Tax Records. *Journal of Labor Eco*nomics, 21(2), 267–288.
- Blundell, Richard, Pistaferri, Luigi, & Preston, Ian. 2008. Consumption Inequality and Partial Insurance. The American Economic Review, 98(5), pp. 1887–1921.
- Cappellari, Lorenzo. 2004. The Dynamics and Inequality of Italian Men's Earnings. *Journal* of Human Resources, **39**(2), 475 499.
- Chamberlain, Gary. 1984. Panel data. Chap. 22, pages 1247–1318 of: Griliches, Zvi, & Intriligator, Michael D. (eds), Handbook of Econometrics. Handbook of Econometrics, vol. 2. Elsevier.
- Dickens, Richard. 2000. The Evolution of Individual Male Earnings in Great Britain: 1975-95. *The Economic Journal*, **110**(460), 27–49.
- Doris, Aedin, O'Neill, Donal, & Sweetman, Olive. 2010 (May). *Identification of the Covariance Structure of Earnings Using the GMM Estimator*. IZA Discussion Papers 4952. Institute for the Study of Labor (IZA).
- Gottschalk, Peter, & Huynh, Minh. 2010. Are Earnings Inequality and Mobility Overstated? The Impact of Nonclassical Measurement Error. *The Review of Economics and Statistics*, **92**(2), 302–315.
- Gottschalk, Peter, & Moffitt, Robert. 1994. The Growth of Earnings Instability in the U.S. Labor Market. Brookings Papers on Economic Activity, 25(1994-2), 217–272.
- Gustavsson, Magnus. 2008. A New Picture of Swedish Earnings Inequality: Persistent and Transitory Components, 1960-1990. *Review of Income and Wealth*, **54**(3), 324–349.

- Guvenen, Fatih. 2009. An Empirical Investigation of Labor Income Processes. Review of Economic Dynamics, 12(1), 58–79.
- Haider, Steven J. 2001. Earnings Instability and Earnings Inequality of Males in the United States: 1967-1991. *Journal of Labor Economics*, **19**(4), 799–836.
- Hause, John C. 1980. The Fine Structure of Earnings and the On-the-Job Training Hypothesis. Econometrica, 48(4), pp. 1013–1029.
- Korkeamäki, Ossi, & Kyyrä, Tomi. 2006. A gender wage gap decomposition for matched employer-employee data. *Labour Economics*, 13(5), 611–638.
- Kwon, Illoong, Milgrom, Eva Meyersson, & Hwang, Seiwoon. 2010. Cohort Effects in Promotions and Wages: Evidence from Sweden and the United States. J. Human Resources, 45(3), 772–808.
- Lillard, Lee A., & Weiss, Yoram. 1979. Components of Variation in Panel Earnings Data: American Scientists 1960-70. *Econometrica*, **47**(2), pp. 437–454.
- Lundberg, Shelly, & Rose, Elaina. 2000. Parenthood and the earnings of married men and women. Labour Economics, 7(6), 689 – 710.
- MaCurdy, Thomas. 2007. Chapter 62 A Practitioner's Approach to Estimating Intertemporal Relationships Using Longitudinal Data: Lessons from Applications in Wage Dynamics. Handbook of Econometrics, vol. 6, Part 1. Elsevier.
- MaCurdy, Thomas E. 1982. The use of time series processes to model the error structure of earnings in a longitudinal data analysis. *Journal of Econometrics*, **18**(1), 83 114.
- Meghir, Costas, & Pistaferri, Luigi. 2004. Income Variance Dynamics and Heterogeneity. *Econometrica*, **72**(1), 1–32.
- Moffitt, Robert A., & Gottschalk, Peter. 2002. Trends in the Transitory Variance of Earnings in the United States. *The Economic Journal*, **112**(478), C68–C73.
- Napari, Sami. 2008. The Early-career Gender Wage Gap among University Graduates in the Finnish Private Sector. *LABOUR*, **22**(4), 697–733.
- Newey, Whitney K. 1985. Generalized method of moments specification testing. *Journal of Econometrics*, **29**(3), 229 256.
- Oreopoulos, Philip, & von Wachter, Till. 2008. The Short- and Long-Term Career Effects of Graduating in a Recession: Hysteresis and Heterogeneity in the Market for College Graduates. IZA Discussion Papers 3578. Institute for the Study of Labor (IZA).
- Pissarides, Christopher, Garibaldi, Pietro, Olivetti, Claudia, Petrongolo, Barbara, & Wasmer, Etienne. 2003 (Apr.). *Women in the Labour Force: How Well is Europe Doing?* Open Access publication. Sciences Po.

- Ramos, Xavier. 2003. The Covariance Structure of Earnings in Great Britain, 1991-1999. Economica, 70(278), 353–374.
- Shin, Donggyun, & Solon, Gary. 2011. Trends in men's earnings volatility: What does the Panel Study of Income Dynamics show? *Journal of Public Economics*, **95**(7-8), 973 982.
- Stock, James H., & Wright, Jonathan H. 2000. GMM with Weak Identification. *Econometrica*, 68(5), 1055–1096.
- Ziliak, James P., Hardy, Bradley, & Bollinger, Christopher. 2011. Earnings Volatility in America: Evidence from Matched CPS. *Labour Economics*.

Cohort	Years observed	Age in initial year	Sample size (men)	Sample size (women)
1933-1934	1988-1994	55	2 882	3 673
1935 - 1936	1988-1996	53	$5\ 169$	6 579
1937 - 1938	1988-1998	51	7 383	8 954
1939 - 1940	1988-2000	49	8 595	9 987
1941 - 1942	1988-2002	47	10 398	11 736
1943 - 1944	1988-2004	45	11 593	12 877
1945 - 1946	1988-2006	43	16 817	18 481
1947 - 1948	1988-2007	41	18 760	19 801
1949 - 1950	1988-2007	39	18 026	19 311
1951 - 1952	1988-2007	37	17 735	18 784
1953 - 1954	1988-2007	35	17 643	18 982
1955 - 1956	1988-2007	33	18 377	18 926
1957 - 1958	1988-2007	31	17 610	17 769
1959-1960	1988-2007	29	18 060	17562
1961 - 1962	1988-2007	27	18 447	16 932
1963 - 1964	1989-2007	26	18 720	16 700
1965 - 1966	1991-2007	26	17 945	15 930
1967 - 1968	1993-2007	26	17 688	$15 \ 357$
1969-1970	1995-2007	26	$16\ 057$	$13 \ 476$
1971 - 1972	1997-2007	26	$15 \ 095$	12 209
1973 - 1974	1999-2007	26	14 248	11 343
1975 - 1976	2001-2007	26	$13 \ 482$	9548
Total			$320\ 729$	314 916

Table 1: Cohorts included in the analysis. Note: Age is defined by older of the two birth cohorts.



Figure 1: Yearly earnings inequality (measured by variance of log earnings of workers) of men (solid line) and women (dashed line).





Figure 2: Autocovariances of yearly log earnings for selected cohorts.

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Women



Figure 3: Autocovariances of log yearly earnings for selected years.

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Figure 4: Decomposition of the variance of log earnings among men (left panel) and among women (right panel) measured in percentages. Predicted variance is calculated as the sum of persistent and transitory components.

	\mathbf{Men}		Women	
	Parameter	S.E.	Parameter	S.E.
p_{1988}	1		1	
p_{1989}	1.017	0.010	0.983	0.011
p_{1990}	1.014	0.009	0.944	0.010
p_{1991}	0.737	0.019	0.811	0.009
p_{1992}	0.754	0.019	0.813	0.008
p_{1993}	1.071	0.016	0.913	0.012
p_{1994}	1.102	0.016	0.937	0.009
p_{1995}	1.094	0.018	0.907	0.012
p_{1996}	1.079	0.016	0.908	0.016
p_{1997}	1.063	0.014	0.892	0.015
p_{1998}	1.058	0.017	0.907	0.016
p_{1999}	1.067	0.020	0.898	0.016
p_{2000}	1.054	0.016	0.904	0.013
p_{2001}	1.043	0.014	0.894	0.015
p_{2002}	1.043	0.015	0.893	0.015
p_{2003}	1.063	0.014	0.889	0.012
p_{2004}	1.067	0.013	0.876	0.011
p_{2005}	1.044	0.013	0.855	0.012
p2006	1.028	0.013	0.854	0.013
p2007	1.017	0.015	0.825	0.012
q1933-1934	0.977	0.016	0.777	0.010
$q_{1935-1936}$	1.054	0.012	0.846	0.007
$q_{1937-1938}$	1.076	0.009	0.847	0.005
$q_{1939} = 1940$	1.005	0.007	0.876	0.004
$q_{1941} = 1942$	1.049	0.005	0.904	0.003
$q_{1943} = 1942$	1.047	0.004	0.940	0.003
$q_{1045-1046}$	1.033	0.003	0.938	0.002
$a_{1945} - 1940$ $a_{1047} - 1048$	1.034	0.002	0.958	0.001
$q_{1949} = 1940$ $q_{1949} = 1950$	1.004	0.001	0.971	0.001
$a_{1949} = 1950$ $a_{1951} = 1952$	1		1	
<i>q</i> ₁₀₅₂ 1054	1.000	0.001	1.014	0.001
$q_{1955} = 1954$ $q_{1055} = 1056$	1.004	0.002	1.059	0.002
$q_{1955} = 1950$ $q_{1057} = 1058$	1.026	0.004	1.097	0.003
$q_{1957} = 1958$ $q_{1959} = 1960$	1.010	0.005	1.148	0.005
$q_{1959} = 1900$ $q_{1061} = 1062$	1 037	0.007	1 187	0.007
q1901-1902 q1062 1064	1.001	0.009	1 192	0.001
q1965-1964 q1965-1964	0.992	0.000	1 217	0.012
$q_{1965} = 1966$	0.952	0.011	1 223	0.012
$q_{1907} = 1908$	0.922	0.015	1.220	0.018
q1909-1970 q1071 1070	0.022	0.017	1.260	0.010
q1971-1972 q1972 1974	0.863	0.020	1.200	0.020
91973-1974 (1075 1076	0.005 0.774	0.020	1 1 2 9 4	0.051
$\frac{41975 - 1976}{\sigma^2}$	0.114	0.020	0.002	0.000
σ^2	1.5 ± 10^{-5}	8×10^{-6}	2.093 2.0×10^{-5}	6×10^{-6}
0 b	1.0 + 10 0 004	2×10^{-4}	2.3×10 0.004	$1 + 10^{-4}$
0 ab	0.004	∠ * 10 ⁻	0.004	1 * 10

Table 2: Estimated parameters of permanent component of earnings.

	Men		Women	
	Parameter	S.E.	Parameter	S.E.
λ_{1988}	(unrestricted)		(unrestricted)	
λ_{1989}	1		1	
λ_{1990}	1.057	0.018	1.043	0.019
λ_{1991}	1.279	0.067	1.086	0.024
λ_{1992}	1.380	0.066	1.156	0.024
λ_{1993}	1.384	0.050	1.207	0.028
λ_{1994}	1.487	0.060	1.273	0.031
λ_{1995}	1.413	0.057	1.276	0.032
λ_{1996}	1.395	0.063	1.254	0.036
λ_{1997}	1.349	0.065	1.244	0.037
λ_{1998}	1.366	0.079	1.277	0.039
λ_{1999}	1.335	0.068	1.297	0.043
λ_{2000}	1.331	0.075	1.290	0.047
λ_{2001}	1.290	0.072	1.287	0.047
λ_{2002}	1.288	0.073	1.214	0.051
λ_{2003}	1.243	0.071	1.203	0.062
λ_{2004}	1.239	0.076	1.230	0.057
λ_{2005}	1.253	0.071	1.271	0.054
λ_{2006}	1.312	0.080	1.319	0.050
$\frac{\lambda_{2007}}{-2}$	1.302	0.073	1.308	0.045
$\sigma_{1933-1934}$	0.023	0.009	0.008	0.005
$\sigma_{1935-1936}$	0.003	0.009	0.023	0.004
$\sigma_{\bar{1}937-1938}^{\sigma_{\bar{1}}937-1938}$	0.007	0.009	0.029	0.004
$\sigma_{1939-1940}$	0.054	0.007	0.035	0.004
$\sigma_{1941-1942}^{\sigma_{1}}$	0.097	0.008	0.055	0.004
$\sigma_{1943-1944}^{-2}$	0.101	0.007	0.071	0.004
$\sigma_{1945-1946}$	0.109	0.007	0.088	0.004
$\sigma_{1947-1948}$	0.132	0.006	0.117	0.004
$\sigma_{1949-1950}$	0.123	0.006	0.120	0.003
$\sigma_{1951-1952}$	0.128	0.005	0.150	0.003
$\sigma_{1953-1954}$	0.113	0.005	0.188	0.003
$\sigma_{1955-1956}$	0.106	0.004	0.216	0.003
$\sigma_{1957-1958}^{2}$	0.103	0.004	0.220	0.003
$\sigma_{1959-1960}$	0.117	0.004	0.218	0.003
$\sigma_{1961-1962}^2$	0.135	0.003	0.230	0.002
$\sigma_{1963-1964}^2$	0.141	0.004	0.227	0.004
$\sigma_{1965-1966}^2$	0.210	0.004	0.254	0.002
$\sigma_{1967-1968}^2$	0.323	0.005	0.357	0.002
$\sigma_{1969-1970}^2$	0.281	0.003	0.361	0.002
$\sigma^2_{1971-1972}$	0.246	0.003	0.318	0.003
$\sigma^2_{1973-1974}$	0.255	0.004	0.362	0.004
$\sigma^2_{1975-1976}$	0.205	0.005	0.318	0.007
ρ	0.223	0.012	0.226	0.009
γ_0	0.112	0.013	0.249	0.015
γ_1	-0.001	0.001	-0.011	0.001
γ_2	$9 * 10^{-6}$	$2.7 * 10^{-5}$	$2 * 10^{-4}$	$3 * 10^{-5}$

Table 3: Estimated parameters of transitory variance of earnings.



Figure 5: Variance of transitory shocks of men and women as a function of age.



Figure 6: Decomposition of earnings inequality for three selected cohorts into permanent (black lines) and transitory (gray lines) components for men (left panel) and women (right panel).



Figure 7: Decomposition of earnings inequality for three selected years into permanent (black lines) and transitory (gray lines) components for men (left panel) and women (right panel).