# Global Imbalances: Should We Use Fundamental Equilibrium Exchange Rates?

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## Abstract

The reduction of global imbalances observed during the climax of crisis is incomplete. In this context, currencies realignments are still proposed to ensure global macroeconomic stability. These realignments are based on equilibrium rates derived from equilibrium exchange rate models. Among these models, we have the fundamental equilibrium exchange rate (FEER) model introduced by Williamson (1994). This approach is often labelled as normative mainly because the return to the equilibrium is not described in the model. If the FEER is not related neither in the short nor in the long to the real exchange rates, we see no clear justification to intervene in foreign exchange markets based on these equilibrium rates. In this case, the FEER is a normative approach and should not be used to reduce global imbalances. This paper provides empirical evidences robust to cross-sectional dependence that the FEER is related to real exchange rate in the long run and thus could be a useful tool to prevent the resurgence of large global imbalances and associated risks.

**JEL Classification:** F31, F41.
**Key words:** Global Imbalances, Equilibrium Exchange Rate, International Monetary Cooperation.

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# 1 Introduction

As witnessed by the evolution of current account balances and net foreign assets, the reduction of global imbalances observed during the climax of crisis is incomplete. Indeed, current account imbalances in flow have been reduced with the global slowdown and the collapse of the world trade in 2009. However, these evolutions of current account imbalances have not been sufficient to reduce net foreign assets positions in stock. After the climax of the crisis, global imbalances in stock (i.e. the net foreign assets positions) represent more than 15% of world GDP in absolute value as we can see in Fig. 1.

Fig. 1: Net foreign assets (in percent of world GDP)
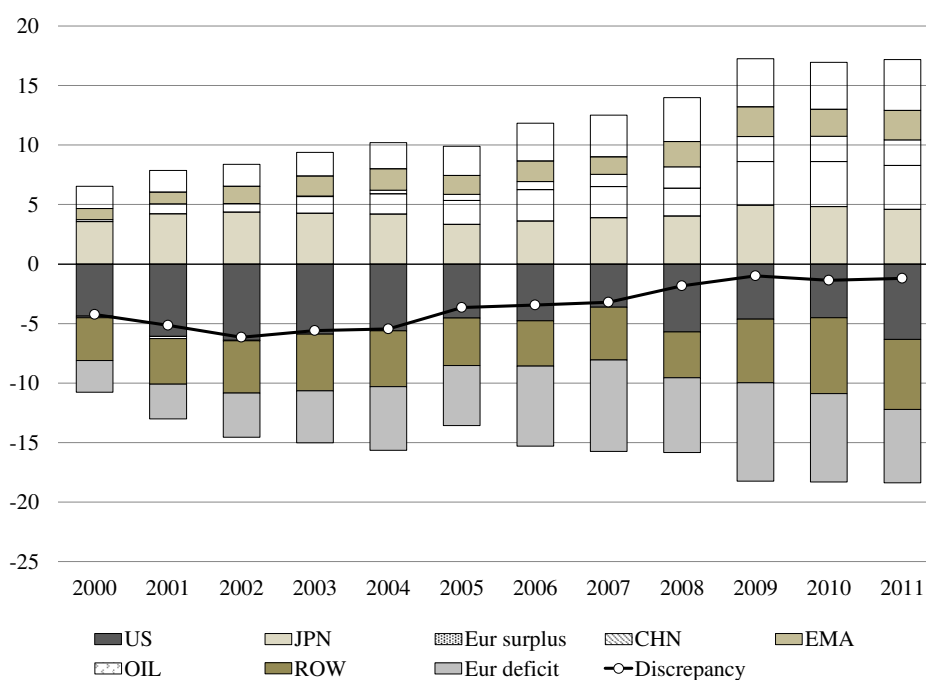


Note: Data are preliminary for 2011. EUR surplus: Austria, Belgium, Denmark, Finland, Germany, Luxembourg, Netherlands, Sweden, Switzerland. EUR deficit: Greece, Ireland, Italy, Portugal, Spain, United Kingdom, Bulgaria, Czech Republic, Estonia, Hungary, Latvia, Lithuania, Poland, Romania, Slovak Republic, Turkey, Ukraine. Emerging Asia: Hong Kong S.A.R. of China, Indonesia, Korea, Malaysia, Philippines, Singapore, Taiwan province of China, Thailand. Oil exporters: Algeria, Angola, Azerbaijan, Bahrain, Republic of Congo, Ecuador, Equatorial Guinea, Gabon, Iran, Kazakhstan, Kuwait, Libya, Nigeria, Norway, Oman, Qatar, Russia, Saudi Arabia, Sudan, Syria, Trinidad and Tobago, United Arab Emirates, Venezuela, Yemen. Rest of the world: remaining countries.

As pointed out by Blanchard and Milesi-Ferretti (2012), the persistence of large current account imbalances and large net foreign assets positions is a threat for the world

economy. Firstly, large current account imbalances increase the systemic risks as countries with large deficits can be subject to sudden stops and their macroeconomic consequences. Secondly, they increase political tensions as a number of countries, which are suspected of unfair competition with undervalued exchange rates, could be threatened by retaliatory measures. Thirdly, in the current context of weak growth in advanced countries, the perpetuation of export-led growth strategies in some emerging countries could be a menace for the global recovery.

Currencies realignments are still proposed to ensure global macroeconomic stability. These realignments are based on equilibrium rates derived from equilibrium exchange rate models. Among these models, we have the fundamental equilibrium exchange rate (FEER) model introduced by Williamson (1994). This approach is often labelled as normative mainly because the return to the equilibrium is not described in the model. If the FEER is not related neither in the short nor in the long to the real exchange rates, we see no clear justification to intervene in foreign exchange markets based on these equilibrium rates. In this case, the FEER is a normative approach and should not be used to reduce global imbalances. This paper provides empirical evidences robust to cross-sectional dependence that the FEER is related to real exchange rate in the long run and thus could be a useful tool to prevent the resurgence of large global imbalances and associated risks.

This paper is organized as follow. Section 2 presents a general framework of the FEER approach. Sections 3 focusses on the empirical results robust to cross-sectional dependence. Section 4 concludes on the usefulness of the FEER approach to reduce global imbalances.

## 2 FEER Methodology

In the literature on equilibrium exchange rates, the FEER approach have several variants. We can quote Cline (2008), Jeong et al. (2010) and Carton and Hervé (2012) for example. These variants differs on the type and size of modelling (general equilibrium, partial equilibrium, reduced form relationship), on the determination of the sustainable current account in the medium term (econometric estimates, judgemental assessment, arithmetic average) and on the trade elasticities (calibration to balance the trade model in volume and value, econometric estimates in a panel setting to ensure consistency of the world trade model).

In spite of all these differences, we present a general framework adapted to describe every FEER approach. We start with a simple current account model based on Clark and MacDonald (1998):

$$CA = -KA \qquad (1)$$

$$CA = ntb + nfar \qquad (2)$$

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$$ntb = b_0 + b_1 q + b_2 y dpot + b_3 y f pot \tag{3}$$

$$nfar = f(q) \tag{4}$$

Where *CA* is the current account balance, *KA* is the capital account, *ntb* is the net trade balance, *nfar* represents returns of net foreign assets, *q* is the real effective exchange rate (when *q* increases, we observe a real effective depreciation), *ydpot* is the domestic full employment output and *yfpot* represents full employments output of foreign economies.

A real effective depreciation and an increase of full employments output of foreign economies improve the net trade balance ($b_1 > 0, b_3 > 0$), an increase of the domestic full employment output deteriorates the net trade balance ($b_2 < 0$).

Combining Equations 1 to 4 gives:

$$CA^* = f(q^{reer}, ydpot, yfpot) = -KA^* \tag{5}$$

Where *CA** is the sustainable current account in the medium term.

To determine the FEER, every approach have to solve the following equation:

$$q^{feer} = f(KA^*, ydpot, yfpot) \tag{6}$$

We obtain the fundamental equilibrium exchange rate ($q^{feer}$), which realizes simultaneously the external and internal equilibrium for all trading partners.

In our approach, we use a two-step procedure to obtain the fundamental equilibrium exchange rate for each trading partners (Jeong et al., 2010). Firstly, we use a partial equilibrium model of world trade for the main countries at the world level (US, China, Japan, Euro area, UK and the Rest of the World). We solve Equation 6 to obtain fundamental equilibrium exchange rates for these countries in a partial equilibrium model of 35 equations. Secondly, we use simple national model in which world demand and world price are exogenous for smaller economies. National estimates are linked with the estimates of the main countries at the world level[1]. In that case the misalignments (i.e. the difference between observed rates and equilibrium rates), written in differential logarithmic ($r = dLogR = (Ri - R^e)/R^e$), are computed as[2]:

$$r = \frac{1}{sx} \cdot \left[ \frac{b}{mx} + \eta m.di - \eta x.d^* \right] \tag{7}$$

Where *b* is the difference between the observed current account and the equilibrium one, as percentage of GDP, *d* and *d** stand for internal and world demand in volume, also

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[1] Notice that the FEER estimates are not obtained country-by-country but in a consistent framework by relying on a world trade model for the main economic areas.

[2] $R^e$ is the equilibrium exchange rate.

written in differential logarithmic, $\eta m$ and $\eta x$ are import and export volume elasticities, $sx$ and $mx$ are coefficients derived from the foreign trade model in which mark-up behaviours are allowed.

Concerning the determination of the sustainable current account in the medium term, following (Chinn and Prasad, 2003), we regress the current account on several medium-term determinants of investment and saving behaviours. The consistency of current account targets is ensured by using the Rest of the World as a residual. At the world level, the sum of current account targets expressed in the same currency is equal to zero. The trade elasticities of the world trade model comes from econometric estimates. These estimates are generally made in a panel setting to ensure that elasticities are mutually consistent[3].

Although, there are several variants of the FEER approach in the literature on equilibrium exchange rates. This simplified framework contains the essential principles which are included in all FEER approaches.

# 3   Empirical Results

The purpose of this section is twofold. First, we estimate FEERs for seventeen industrialized and emerging countries (the United States, the United-Kingdom, the Euro area, Japan, Korea, China, Brazil, India, Mexico, Argentina, Chile, Colombia, Indonesia, Malaysia, Philippines, Thailand and Uruguay) over the period 1982 to 2007 with the methodology described above[4]. Secondly, we test empirically the usefulness of the FEER approach to reduce global imbalances.

After the estimation of FEERs for these seventeen countries over the period 1982-2007, we test the following long-run relationships:

$$reer_{i,t} = \alpha_i + \beta feer_{i,t} + \mu_{i,t} \tag{8}$$

$$feer_{i,t} = \delta_i + \theta reer_{i,t} + \varepsilon_{i,t} \tag{9}$$

Where $feer$ is the fundamental equilibrium exchange rate and $reer$ is the real effective exchange rate[5]. Variables in minuscule represents natural logarithms.

When the time dimension ($T = 26$ in our sample) is superior to the cross-section dimension ($N = 17$ in our sample), we can test the existence of cross-sectional dependencies with a Lagrange multiplier test as pointed out by De Hoyos and Sarafidis (2006). Consequently, we apply an LM test on an ARDL(1,1) specification with fixed effects as in Persyn and Westerlund (2008).

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[3] See Jeong et al. (2010) for more details and complete description of the model and the methodology.

[4] Estimates for emerging countries are presented and discussed in Aflouk et al. (2010).

[5] Source: Bank for International Settlements.

Table 1: Breusch-Pagan LM test of independence

|  | *p*-value |
|---|---|
| Equation (8) | 0.000 |
| Equation (9) | 0.000 |

Source: author's calculations.

As we can see in Table 1, we strongly reject the null hypothesis of cross-sectional independence. In order to take into account cross-sectional dependence, we implement panel unit root tests, panel cointegration tests and a new estimator which allow cross-sectional dependence.

We use the CADF test introduced by Pesaran (2007) to test the unit root properties of the variables in presence of cross-sectional dependence. This test is robust to cross section dependencies by subtracting cross section averages of lagged levels in addition to the standard ADF equation. As shown by Table 2, series are nonstationary I(1) series as a I(1) series achieves stationarity after first differencing.

Table 2: Integration of the variables

|  | Level | First Difference |
|---|---|---|
| *feer* | 0.223 | -4.271 |
|  | (0.588) | (0.000) |
| *reer* | 0.375 | -3.083 |
|  | (0.646) | (0.001) |

Source: author's calculations. Note: *p*-values in parentheses.

To test cointegration, we use the panel and the "mean group" statistics suggested by Westerlund (2007). The existence of negative error-correction term is taken as proof for cointegration. To take into account cross-sectional dependence, critical values need to be obtain through bootstrapping. As we can see in Table 3, variables are cointegrated.

The previous results have established that the variables are integrated and cointegrated in presence of cross-sectional dependence. Now, we use a Cross-Sectionally augmented pooled Mean Group (CPMG) estimator introduced by Pesaran (2006) and implemented recently by Mohaddes et al. (2012) to estimate the long-run relationships in presence of cross-section dependence. In this approach, we augment the PMG estimator (Pesaran

Table 3: Cointegration of the variables

|  | $G\tau$ | $G\alpha$ | $P\tau$ | $P\alpha$ |
|---|---|---|---|---|
| Equation (8) | -2.162 | -6.414 | -6.661 | -4.005 |
|  | (0.001) | (0.013) | (0.070) | (0.031) |
| Equation (9) | -2.481 | -7.460 | -9.441 | -6.548 |
|  | (0.000) | (0.000) | (0.001) | (0.001) |

et al., 1999) with cross sectional average of independent and dependent variables in order to capture the common factors or the heterogeneous time effects.

More precisely, we start with the ARDL(1, 1) model as specified in Equation 10:

$$reer_{i,t} = \delta_{0i} + \delta_{1i}feer_{i,t} + \delta_{2i}feer_{i,t-1} + \lambda_i reer_{i,t-1} + u_{i,t} \tag{10}$$

The error correction equation yield:

$$\Delta reer_{i,t} = \phi_i(reer_{i,t-1} - \theta_{0i} - \theta_{1i}feer_{i,t}) - \delta_{2i}\Delta feer_{i,t} + u_{i,t} \tag{11}$$

Now, we assume that the error term $u_{i,t}$ follow multi-factor error structure:

$$u_{i,t} = \gamma_i f_t + \varepsilon_{i,t} \tag{12}$$

where $f_t$ is a factor of unobserved common shocks. The error terms dependencies across individuals are captured by $f$, whereas the impacts of these factors on each country are governed by the idiosyncratic loadings in $\gamma_i$.

By using Equations 10 and 12 and by averaging across i, we obtain:

$$\overline{reer}_t = \bar{\delta}_0 + \bar{\delta}_1\overline{feer}_t + \bar{\delta}_2\overline{feer}_{t-1} + \bar{\lambda}\overline{reer}_{t-1} + \bar{\gamma}f_t + \bar{\varepsilon}_t \tag{13}$$

Where the variables with a bar denote the simple cross section averages of the corresponding variables in year t. The common factors can be captured through a linear combination of the cross-sectional averages of the dependent variable and of the regressors:

$$\gamma_i f_t = -c_i\bar{\delta}_0 - c_i(\bar{\delta}_1 + \bar{\delta}_2)\overline{feer}_t + c_i(1 - \bar{\lambda})\overline{reer}_{t-1} + c_i\Delta\overline{reer}_t + c_i\bar{\delta}_2\Delta\overline{feer}_t \tag{14}$$

where $c_i = \frac{\gamma_i}{\bar{\gamma}}$. Replacing Equations 12 and 14 in Equation 11 yields the error correction equation:

$$\Delta reer_{i,t} = \phi_i \left( reer_{i,t-1} - \theta_{0i} - \theta_{1i} feer_{i,t} - a_i^* \overline{reer}_{t-1} + b_i^* \overline{feer}_t \right)$$
$$- \delta_{2i} \Delta feer_{i,t} + c_i \Delta \overline{reer}_t + c_i^* \Delta \overline{feer}_t + \varepsilon_{i,t} \tag{15}$$

Where $\phi_i = -(1 - \lambda_i)$; $\theta_{0i} = (\delta_{0i} - c_i \bar{\delta}_0)/(1 - \lambda_i)$; $\theta_{1i} = (\delta_{1i} + \delta_{2i})/(1 - \lambda_i)$; $a_i^* = c_i (1 - \bar{\lambda})/(1 - \lambda_i)$; $b_i^* = c_i (\bar{\delta}_1 + \bar{\delta}_2)/(1 - \lambda_i)$; $c_i^* = c_i \bar{\delta}_2$.

Since the CPMG estimator imposes long-run coefficients to be constant for all individuals, while it allows short run heterogeneity, the error correction models[6] are written:

$$\Delta reer_{i,t} = \phi \left( reer_{i,t-1} - \theta_0 - \theta_1 feer_{i,t} - a^* \overline{reer}_{t-1} + b^* \overline{feer}_t \right)$$
$$- \delta_{2i} \Delta feer_{i,t} + c_i \Delta \overline{reer}_t + c_i^* \Delta \overline{feer}_t + \varepsilon_{i,t} \tag{16}$$

$$\Delta feer_{i,t} = \phi \left( feer_{i,t-1} - \theta_0 - \theta_1 reer_{i,t} - a^* \overline{feer}_{t-1} + b^* \overline{reer}_t \right)$$
$$- \delta_{2i} \Delta reer_{i,t} + c_i \Delta \overline{feer}_t + c_i^* \Delta \overline{reer}_t + \varepsilon_{i,t} \tag{17}$$

The results are presented in Tables 4 and 6. The estimations give clear cut results. They clearly show a positive and significant long-run relationship between fundamental rates and observed rates in presence of cross-sectional dependence. The results are robust to different groups of countries since the results in Tables 5 and 7 are very similar to those for the entire sample.

As pointed out by Saadaoui (2011), in case of cyclical evolution of competitiveness (Equation 8), the half-life[7] is equal to 3.8 years (3 years for emerging countries only). For structural evolution of competitiveness (Equation 9), the half-life is equal to 2.31 years (2.15 years for emerging countries only). When a country experienced a cyclical evolution of its competitiveness, it can slow the return to equilibrium in case of unfavourable evolutions hence a longer half-life[8].

We provide robust empirical evidences that the FEER approach is related in the long run with observed rates even if the dynamic of real exchange rates is not explicitly described in the model. These results confirm the usefulness of the FEER approach to reduce global imbalances. The FEER approach should be used as a tool to prevent the return of large imbalances and associated risks.

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[6] Causality tests have been conducted thanks to the Pooled Mean Group estimator. They clearly show that the causal relationship is bi-directional (Saadaoui, 2011).

[7] The half-lives are computed by using the following formula: $h = -\ln(0.5)/\ln(1 + |\phi|)$. They correspond to the number of periods for a deviation (from the long run equilibrium) to decay by 50%. Here, deviations correspond to misalignments.

[8] See Saadaoui (2011) for a distinction between cyclical and structural evolutions of competitiveness.

Table 4: Long-relationship (Equation 8)

|  | Long-run coefficient (β) | z-stat / p-value |
|---|---|---|
| CPMG | 0.53*** | 7.38 |
| Error-correction term (φ) | -0.20*** | -4.27 |
| Hausman test | 1.13 | 0.77 |
| Number of cross-section | 17 | |
| Number of periods | 26 | |
| Number of observations | 442 | |

Source: author's calculations. Notes: *p*-value for the Hausman test of homogeneity of long run coefficients. The symbol *** indicates statistical significance at the 1% level.

Table 5: Long-relationship (Equation 8) for emerging countries only

|  | Long-run coefficient (β) | z-stat / p-value |
|---|---|---|
| CPMG | 0.63*** | 7.77 |
| Error-correction term (φ) | -0.26*** | -6.06 |
| Hausman test | 3.79 | 0.28 |
| Number of cross-section | 13 | |
| Number of periods | 26 | |
| Number of observations | 338 | |

Source: author's calculations. Notes: *p*-value for the Hausman test of homogeneity of long run coefficients. The symbol *** indicates statistical significance at the 1% level.

Table 6: Long-relationship (Equation 9)

| | Long-run coefficient (θ) | z-stat / p-value |
|---|---|---|
| *CPMG* | 0.64*** | 13.37 |
| *Error-correction term (φ)* | -0.35*** | -6.72 |
| *Hausman test* | 1.57 | 0.66 |
| *Number of cross-section* | 17 | |
| *Number of periods* | 26 | |
| *Number of observations* | 442 | |

Source: author's calculations. Notes: *p*-value for the Hausman test of homogeneity of long run coefficients. The symbol *** indicates statistical significance at the 1% level.

Table 7: Long-relationship (Equation 9) for emerging countries only

| | Long-run coefficient (θ) | z-stat / p-value |
|---|---|---|
| *CPMG* | 0.73*** | 11.29 |
| *Error-correction term (φ)* | -0.38*** | -5.21 |
| *Hausman test* | 2.57 | 0.46 |
| *Number of cross-section* | 13 | |
| *Number of periods* | 26 | |
| *Number of observations* | 338 | |

Source: author's calculations. Notes: *p*-value for the Hausman test of homogeneity of long run coefficients. The symbol *** indicates statistical significance at the 1% level.

# 4 Conclusion

The reduction of global imbalances observed during the climax of crisis is incomplete as witnessed by the evolution of net foreign assets positions. In this context, currencies realignments are still proposed to ensure global macroeconomic stability. These currencies realignments are based on equilibrium (or reference) rates derived from equilibrium exchange rate models. Among these models, we have the FEER approach introduced by Williamson (1994). This approach is often labelled as normative as the exchange rate dynamic is not explicitly described in the model. We provide robust empirical evidences that fundamental rates are related in the long run with observed rates in presence of cross-section dependence. These empirical results are supportive of the usefulness of the FEER approach to reduce global imbalances and associated risks. A return of large imbalances could dampen the global recovery (Blanchard and Milesi-Ferretti, 2012).

In July 12, the IMF has adopted the FEER concept to strengthen its surveillance activities on bilateral and multilateral levels (International Monetary Fund, 2012). In its *Pilot External Sector Report*, the IMF produce a set of deviations between real effective exchange rates and those consistent with fundamental and desirable policies for 28 economies. Even if this new decision does not create new formal obligations, it could be considered as a step in the recognition that members must have mutually consistent objectives to ensure global macroeconomic and macrofinancial stability.

Our empirical results are consistent with the IMF's decision as they support the usefulness of the FEER approach to reduce global imbalances. This decision could be preliminary step towards a larger discussion on the future of the international monetary system.

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