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Kakarot-Handtke, Egmont

University of Stuttgart, Institute of Economics and Law

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# Geometrical Exposition of Structural Axiomatic Economics (II): Qualitative and Temporal Aggregation

Egmont Kakarot-Handtke\*

#### Abstract

Behavioral assumptions are not solid enough to be eligible as first principles of theoretical economics. Hence all endeavors to lay the formal foundation on a new site and at a deeper level actually need no further vindication. Part (I) of the structural axiomatic analysis submits three nonbehavioral axioms as groundwork and applies them to the simplest possible case of the pure consumption economy. The geometrical analysis makes the interrelations between income, profit and employment under the conditions of market clearing and budget balancing immediately evident. Part (II) applies the differentiated axiom set to the analysis of qualitative and temporal aggregation.

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**Keywords** new framework of concepts; structure-centric; axiom set; supersymmetry; general equilibrium; dimensionless variables; income; profit; distributed profit; retained profit; full employment

<sup>\*</sup>Affiliation: University of Stuttgart, Institute of Economics and Law, Keplerstrasse 17, D-70174 Stuttgart. Correspondence address: AXEC, Egmont Kakarot-Handtke, Hohenzollernstraße 11, D-80801 München, Germany, e-mail: handtke@axec.de

The present paper is the sequel to (2012). Taking the general case of the consumption economy as a point of departure it has been demonstrated in Part (I) how income, profit and distributed profit are interconnected in the reproducible consumption economy with market clearing and budget balancing. The analysis has been confined to one firm and one period. It is now generalized for an arbitrary number of firms and periods.

The minimalistic structural frame that constitutes the pure consumption economy is set up in Section 1. In Section 2 the exemplary mapping of a differentiated microeconomic state onto the structural axiom set is carried out geometrically. The difference between the notion of a behavioral equilibrium and the notion of structural supersymmetry is discussed in Section 3 and some good reasons are provided as to why the latter is preferable. In Section 4 the exemplary mapping of a differentiated period sequence onto the structural axiom set is carried out geometrically. Section 5 concludes.

# 1 Axioms and definitions

The first three structural axioms relate to income, production, and expenditures in a period of arbitrary length. For the beginning the period length is assumed to be the calendar year. Simplicity demands that we have at first one world economy, one firm, and one product.

Total income of the household sector Y in period t is the sum of wage income, i.e. the product of wage rate W and working hours L, and distributed profit, i.e. the product of dividend D and the number of shares N.

$$Y = WL + DN \quad |t \tag{1}$$

Output of the business sector O is the product of productivity R and working hours.

$$O = RL \quad |t \tag{2}$$

Consumption expenditures C of the household sector is the product of price P and quantity bought X.

$$C = PX \quad |t \tag{3}$$

With (4) wage income  $Y_W$  and distributed profit income  $Y_D$  is defined:

$$Y_W \equiv WL \qquad Y_D \equiv DN \quad |t. \tag{4}$$

Definitions determine the logical context of concepts, they add no new content to the axiom set.

#### 2 Qualitative aggregation

The axiom set refers to one single firm. Since the economy is composed of an indefinite – but certainly not infinite – number of firms differentiation is one of the nearest tasks. It is carried out geometrically in Figure 1a (for the formal underpinnings see 2011c, Appendix A).

The four axes represent the positive values of the variables employment L, income Y, consumption expenditures C, output O, and quantity bought X, respectively. The quadrants are numbered according to the axioms they enclose. The bisecting line in the northwestern quadrant mirrors income from the horizontal to the vertical axis.

The business sector is, in the 1st quadrant, split up into three firms with equal shares of the total working hours L. The number of firms and the distribution of the working hours  $L_A$ ,  $L_B$ ,  $L_C$  between them is arbitrary. The different individual wage rates *within* each firm are given by the tangents to the income curve and they are here ordered from the lowest to the highest. The wage incomes  $Y_{WA}$ ,  $Y_{WB}$ ,  $Y_{WC}$  include the remuneration of all managers and executives of the respective firm. For the sake of simplicity the wage structure is assumed to be identical in all three firms. The individual incomes of the employees are graphically cumulated and sum up to total period income Y. Distributed profits have been set to zero.

The productivities  $R_A$ ,  $R_B$ ,  $R_C$  that are given by the slopes of each line segment in the 2nd quadrant are different for each firm. The respective labor inputs and productivities yield the period outputs  $O_A$ ,  $O_B$ ,  $O_C$  as shown on the horizontal axis. The outputs are qualitatively different. The magnitude of the different productivities and outputs depends on the unit of measurement, e.g. ounce, liter, piece, square meter, carat, and so on.

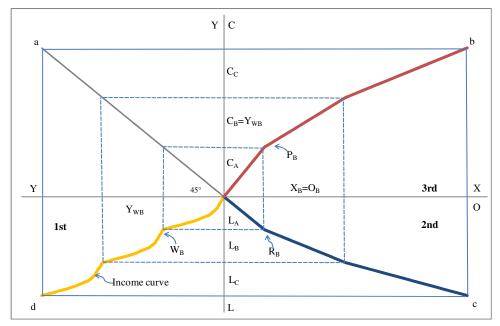
It has to be emphasized that the productivities need not be fix for all levels of labor input, that is, the 2nd axiom is compatible with increasing, constant and decreasing returns. The geometrical representation is a snapshot for the period under consideration.

The 3rd quadrant depicts the price–quantity configurations for each product and the shares  $C_A$ ,  $C_B$ ,  $C_C$  of total consumption expenditures C. The prices  $P_A$ ,  $P_B$ ,  $P_C$ are represented by the slopes of the respective line segments. The quantities bought  $X_A$ ,  $X_B$ ,  $X_C$  from each firm are – here – equal to the quantities produced  $O_A$ ,  $O_B$ ,  $O_C$ . There are no changes of inventory.

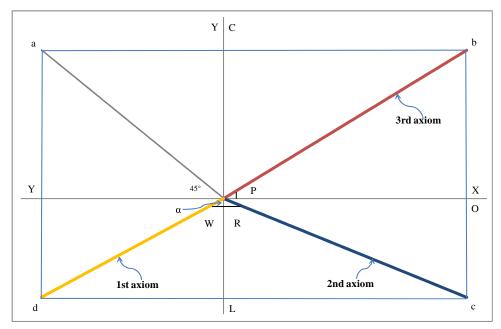
The juxtaposition in the quadrant with the 45° line shows that consumption expenditures  $C_A$ ,  $C_B$ ,  $C_C$  are here exactly equal to wage incomes  $Y_{WA}$ ,  $Y_{WB}$ ,  $Y_{WC}$  for each firm. For the business sector as a whole therefore holds C = Y.

The business sector's financial profit  $\Delta Q_{fi}$  in period *t* is defined with (5) as the difference between the sales revenues – for the economy as a whole identical with total consumption expenditures *C* – and costs – here identical with total wage income  $Y_W$ :

$$\Delta Q_{fi} \equiv C - Y_W \equiv PX - WL \quad |t. \tag{5}$$



(a) Three firms produce and sell three diverse consumption goods under the condition of market clearing and budget balancing



(b) The identical mapping of the coordinates a, b, c, d and the origin from Figure 1a to 1b amounts to the aggregation of the detailed structure of the business and the household sector and yields the graphical representation of the structural axiom set

Figure 1: Qualitative aggregation

This gives for firm A and analogous for the other firms:

$$\Delta Q_{fiA} \equiv C_A - Y_{WA} \equiv P_A X_A - W_A L_A \quad |t. \tag{6}$$

The profit of each firm in Figure 1a is zero by construction. Therefore we have for the economy as a whole at first neither profit nor distributed profit.

The coordinates of points a, b, c, d in Figure 1a and the origin are now mapped to Figure 1b. The details are left behind. The straight lines that now connect the origin with the four identical coordinate points a, b, c, d represent the axiom set. The mapping therefore amounts to the aggregation of the business sector and the household sector, respectively. Aggregation leads formally back to the sole firm that has been the axiomatic point of departure.

The mapping that has been exemplarily carried out in Figure 1 can be generalized for an arbitrary number of firms and agents. For the economy as a whole one has  $X_{ABC} = O_{ABC}$  and C = Y, i.e. the product markets are cleared and the household sector's budget is balanced. This configuration is referred to as supersymmetric outcome in the product market. Supersymmetry is a purely structural property and means not a whit more than that the household sector's consumption expenditure are exactly equal to the period income and the business sector's period output is exactly equal to the quantity bought by the household sector. This market outcome configuration is outstanding among all other possible market outcomes. Supersymmetry is fundamentally different from equilibrium as it does not refer to human behavior or to anonymous market forces. It is established by conditions that highlight one configuration among all logically possible configurations. The beauty of the supersymmetric configuration is that it is reproducible in principle for an indefinite number of periods.

What exactly does the mapping formally entail? The geometrical transformation of the kinked lines in Figure 1a to the straight lines in Figure 1b amounts to the calculation of the respective weighted averages. Thus the wage rate in the 1st quadrant, which is equal to the tangent function of the angle  $\alpha$ , is given by:

$$W \equiv \frac{1}{L} \left( W_A L_A + W_B L_B + W_C L_C \right) \quad |t.$$
<sup>(7)</sup>

Variable  $W_A$  is in turn the average wage rate of firm A and likewise for the other firms.

The productivity in the 2nd quadrant is given by:

$$R \equiv \frac{1}{L} \left( R_A L_A + R_B L_B + R_C L_C \right) \quad |t.$$
(8)

The productivity R is a composite of productivities with diverse dimensions and it is not clear at first sight whether this average, which is geometrically at any time feasible, is economically meaningful.

Finally, the price in the 3rd quadrant is given by:

$$P \equiv \frac{1}{X} \left( P_A X_A + P_B X_B + P_C X_C \right) \quad |t.$$
<sup>(9)</sup>

The composite quantity X is made up of quantities with quite different dimensions, e.g. number of cars, liters of milk, and square meters of carpet:

$$X \equiv X_A + X_B + X_C \quad |t. \tag{10}$$

Recalling the saying that it makes no sense to count together apples and oranges the first thing to consider is that it is by no means self-evident that apples can be counted together in the first place:

... from a strict utilitarian point of view, there is no such thing as a generic commodity. To every individual qua individual, each apple is different ... the self-identity of the commodity, which is the necessary prerequisite of its basis as a cardinal number, is not at all psychologically present. (Mirowski, 1986, p. 205), see also (Mirowski, 2004)

That apples may be counted together already requires an abstraction with a more or less arbitrary bundling of physical characteristics. Thus, when we are not interested in apples and oranges as such there is no objection against lumping together a kilo of each and carrying home two kilos of fruit. In the same manner we can intelligibly speak of a zoo that is inhabited by nine mammals counting together four elephants, three dolphins and two bumblebee bats. Hence, when we introduce the abstract term *unit of output* we can sum up the heterogeneous specific units of  $X_A, X_B, X_C$ . This abstraction makes it possible to calculate the price *P* of Figure 1b as a correspondence of the prices of Figure 1a. Care has to be taken, however, of what this operation entails.

In Figure 2 the line segment  $X_1$  is the result of a straightforward addition of output quantities with diverse dimensions as in (10). Let us assume now that an abstract unit of output has been defined as a unique measuring rod and that all output quantities are expressed in this new standard unit. Measured in this unit the composite output is now  $X_2$  with a unique dimension. In quantitative and qualitative terms, of course, output and quantity bought do not change at all. The change in the unit of measurement affects productivity and price in (7) and (8). Expressed in the standard unit the price is higher and the productivity is lower compared to the initial situation. The salient point is that the new values are geometrically related as follows:

$$P_{1} = \frac{e}{X_{1}} \quad R_{1} = \frac{X_{1}}{f} \quad \Rightarrow \quad P_{1}R_{1} = \frac{e}{f}$$

$$P_{2} = \frac{e}{X_{2}} \quad R_{2} = \frac{X_{2}}{f} \quad \Rightarrow \quad P_{2}R_{2} = \frac{e}{f}$$
(11)

Changes of the unit of measurement do not affect the *product* of price and productivity. The variable that gives rise to the question of measurement simply cancels out. Whenever both variables are used in conjunction it is of no import

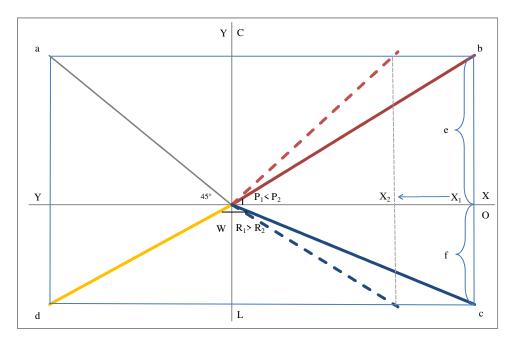


Figure 2: The product of price and productivity is invariant to changes of the unit of measurement

whether we add up heterogeneous or standardized output dimensions. As it happens this is mostly the case. As an example (6) can be rewritten as:

$$\Delta Q_{fi1} \equiv P_1 X_1 - W_1 L_1 \equiv P_1 R_1 L_1 \left( 1 - \frac{W_1}{P_1 R_1} \right) \quad \text{if} \quad O = X \quad |t.$$
 (12)

The profit of firm<sub>1</sub> in no way depends on the measurement of output units, despite the fact that both productivity and price vary with the chosen dimension of output. The crucial determinant of profit is the factor cost ratio  $\rho_F = \frac{W}{PR}$  which is unit-free, i.e. a rational number without dimension.<sup>1</sup> For each firm the factor cost ratio is unity, given the conditions enumerated in the foregoing. Therefore profit is zero. For the economy as a whole as given by the axioms the factor cost ratio is unity, too.

In sum: qualitative aggregation entails that for any microeconomic configuration in period t there exists a correspondence that is formally represented by the first three structural axioms.

# **3** Behavioral equilibrium as a limiting case

But there is something scandalous in the spectacle of so many people refining the analysis of economic states which they give no reason to suppose will ever, or have ever, come about. (?, p. 88)

<sup>&</sup>lt;sup>1</sup> For the search of pure dimensionless constants in physics see (Mirowski, 2004, pp. 158-159)

Equilibrium is the pivotal conception in standard economics. It means, though, quite different things to different people. Weintraub (1991, p. 99-112) explored its varying images and definitions as an instant of a Wittgensteinian language game. Equilibrium may be regarded as a formal construct or a feature of the real world. The realists's critique of the mathematical conception is mostly in the spirit, if not always in the strong words, of Clower:

An intellectually respectable answer should consist of something more than tired clichés; observable economic events derive ultimately not from unspecified coordinating mechanisms, whether invisible hands, price systems, or neowalrasian "auctioneers", but ... from definable actions of real people. (Clower, 1994, p. 806), see also (Chick and Dow, 2001)

The notion of equilibrium invokes a plethora of images: center of gravitation, natural state of rest, balance of opposing forces, best-of-all-worlds, mutual compatibility of individual plans, end of exchanges and readjustments, solution of a model, fixed point, attractor, entropy maximum, and, yes, justice<sup>2</sup> (Freeman, 2007), (Vilks, 1992), (Mirowski, 1989). The crucial point, though, is the identification of equilibrium with reality:

The partition of the nonnegative price-quantity space into equilibrium and disequilibrium points fosters a separation of interest, for nothing can really be said about most of the possible price-quantity configurations whatsoever, except that those pairs will not ever be wanted, desired, or observed. They stand outside analysis, outside economics, outside language. Equilibrium is real, for it is potentially observable. (Weintraub, 1991, p. 144)<sup>3 4</sup>

It deserves mention that no equilibrium has ever been observed (Hahn, 1980, p. 133). The comparison with the classical view provides a paradigmatic instance of the fact that formal progress is perfectly reconcilable with conceptual regress (?, pp. 79-96), (McCloskey, 1994, 133-145). The classical stance was distinctly dynamic:

 $<sup>^2</sup>$  "Commodities exchange ... in proportion to the quantities of labour which have been expended to produce them: this is the law of value which Ricardo formulated, a law of equilibrium and justice." (Halévy, 1960, p. 343)

<sup>&</sup>lt;sup>3</sup> "So far as this limited sense of equilibrium is concerned it is true that we assume the economic system to be always in equilibrium. Nor is it unreasonable to do so. There is a sense in which current supplies and current demands are always equated in competitive conditions. Stocks may indeed be left in the shops unsold; but they are unsold because people prefer to take the chance of being able to sell them at a future date rather than cut prices in order to sell them now. ... In this (analytically important) sense the economic system. ... can be taken to be always in equilibrium." (Hicks, 1939, p. 131)

<sup>&</sup>lt;sup>4</sup> "The second possibility is *to define* equilibrium in such a way that it is always present. Of course it is possible to do this; any outcome can be considered an equilibrium in the sense that agents do what they do instead of doing something else. But such a treatment does not get us very far; the study of what happens when the optimizing plans of different agents are not compatible simply gets renamed as a study of moving equilibria rather than of disequilibrium." (Fisher, 1983, p. 7), original emphasis

One of the conditions oftenest dropped, when what would otherwise be a true proposition is employed as a premise for proving others, is the condition of time. It is a principle of political economy that prices, profits, wages &c. "always find their level;" but this is often interpreted as if it meant that they are always, or generally, *at* their level; while the truth is, as Coleridge epigrammatically expresses it, that they are always *finding* their level, "which might be taken as a paraphrase or ironical definition of a storm." (Mill, 2006, p. 807), original emphasis

Walras, to be sure, held roughly the same view with regard to general equilibrium:

Walras was aware that economic equilibrium does not occur in reality and that in the latter the conditions of his model are insufficiently satisfied .... His proof of existence – at least the attempt to do so – is purely mathematical, namely, of a unique solution of his system of equations. (Klant, 1988, p. 93)

Equilibrium made its appearance in the history of economics only in the midnineteenth century and has undergone extensive revisions in the twentieth century. In this process standard economics 'has lost any claim to having a unique and determinate notion of equilibrium' (Mirowski, 1981, p. 606). In sum: there is a conspicuous lack of good reasons for taking equilibrium as the 'central organizing idea' (Hahn) of theoretical economics. To the contrary:

It is erroneous to posit some equilibrium position – as if it were transcendental, self-subsistent, and commanding – and then consider certain phenomena as disturbances or deviations from it. (Samuels, 1997, p. 78)

The structural axiomatic approach is different from any partial or general equilibrium approach as it does not refer to human behavior or to imaginary market forces that move the economy toward a distinct state either simultaneously or in the undefined long run. To exclude human behavior from the set of structural axioms does, however, not imply that it is excluded from a comprehensive analysis. It is, in a second step, consistently connected with the structural axiom set via an own formal interface (for details see 2011b).

This all said, it is now assumed that, given their preferences, all agents are in their Pareto-optimal position with regard to the structure of wage rates and prices in Figure 1a. This marginalistic behavioral equilibrium has the following properties: overall market clearing, i.e.  $X_{ABC} = O_{ABC}$ , budget balancing, i.e. C = Y, and zero profit in each firm.

The coordinates of the points a, b, c, d in Figure 1b are identical with those in Figure 1a. This implies that the complex conditions of the marginalistic behavioral equilibrium can be mapped onto the geometrical representation of the first three axioms. There is a loss of detailed information but this is not necessarily a disadvantage because for many theoretical questions theses details are not of interest.

In these cases the detailed structure of the marginalistic behavioral equilibrium is implicitly present in the structural axiom set and remains in the background.

The purely geometrical relation between the familiar demand–supply schedules of the product market and the 3rd axiom is visualized in Figure 3. It is important to note, however, that the 3rd quadrant is only a part of the whole picture which is given with the complete structural axiom set. Hence Figure 3 has to be taken as a geometrical bridge to the familiar textbook representations of markets. Formally the demand–supply schedules of the product market are redundant in a structural axiomatic analysis.

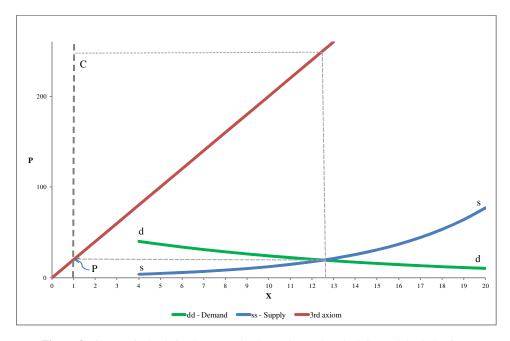


Figure 3: Geometrical relation between the demand-supply schedules and the 3rd axiom

The correspondence that is established with the mapping holds also when the agents are *not* in their marginalistic behavioral equilibrium given their preferences and the structure of wage rates and prices. *All* microeconomic states can be mapped onto the first three axioms. This has important consequences for the relation between the structure-centric axiomatic analysis and the behavior-centric standard analysis. The pairing of structural supersymmetry and marginalistic behavioral equilibrium demonstrates that the former is an objective conception that does not exclude the latter but, by the same token, is by no means restricted to it. Seen from the structural axiomatic perspective a marginalistic general equilibrium is a limiting case. The structural axiom set is truly general.

Aggregation amounts to a surjection of the microeconomic details onto the axiom set that is perfectly neutral with regard behavioral assumptions which purportedly explain how the microeconomic state came to pass. This mapping is always feasible regardless of whether the explanation of the microeconomic state is true or false (cf. Mirowski, 2006).

Now, marginalistic behavioral equilibrium comes in two temporal forms. Simultaneity is the standard form and it plainly has no counterpart in reality (Boland, 1978, pp. 243-244). However, simultaneous behavioral equilibrium may be reinterpreted as an one-period equilibrium with a conveniently chosen period length. The second temporal form has been originally developed by Hicks:

By using the week, we become able to treat a process of change as consisting of a series of temporary equilibria; this enables us still to use equilibrium analysis in the dynamic field. (Hicks, 1939, p. 127)

Hicks's conception has a family resemblance with the structural axiomatic period analysis. It is clearly but one possible interpretation of general equilibrium and not the most popular anyway (Kirman, 2006, p. 256). The fundamental crux of any interpretation is, of course, the incongruity of the notion of simultaneity and the notion of a finite period length, that is, the conceptualization of time:

The notion of time is so primitive and basic an element in man's experience that its neglect by much economic theory constitutes an incredible puzzle. This puzzle is attributable, perhaps, to the almost irresistible lure of formalism – particularly one that cannot adequately handle time. (Rizzo, 1979, p. 1)

# 4 Temporal aggregation

Aggregation is also about the formal relations between the values of the variables of the axiom set over an arbitrary number of periods and the resulting values for all periods taken together. Just in the same manner as in Section 2 the differentiated geometrical representation of a given number of periods – instead of a given number of firms – can be mapped onto the elementary geometrical representation of the axioms that relate now to a longer period. Figure 4 shows the development over three periods (again without distributed profits).

The slopes of the respective line segments in the 1st to 3rd quadrant represent different wage rates W, productivities R and prices P for consecutive periods. In the first – innermost – period consumption expenditures C are greater than total income Y and the quantity bought X is greater than output O, i.e. the household and the business sector draw on existing stocks of money and products which have been here left out of the picture (for details see 2011a). Asymmetry prevails, just as in the real world. The differences of the flow magnitudes are represented by the line segments between the arrows on the horizontal and vertical axis. In period<sub>2</sub> total income exceeds consumption expenditures are again greater than the quantity bought. In period<sub>3</sub> consumption expenditures are again greater than income but output and quantity bought are equal, i.e.  $X_3 = O_3$  and  $C_3 > Y_3$ .

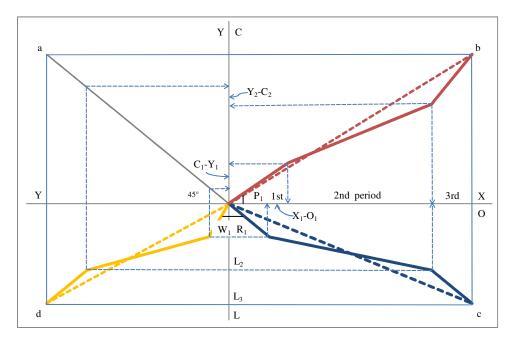


Figure 4: Temporal aggregation of three asymmetric periods with supersymmetry for all periods taken together

The coordinates of the points a, b, c, d are the endpoints of the development over three periods. Since for each period the new origin is given by the endpoint of the previous period the three periods  $t_1, t_2, t_3$  can be geometrically added up to one longer period t with identical end coordinates a, b, c, d. The diverse line segments in each quadrant lead to the same end points as the respective straight lines. This implies that the actual conditions in each period can be mapped onto the geometrical representation of the first three axioms that now refer to the longer period t. The geometrical summation over three periods results in this special case in supersymmetry for the longer period. Hence saving and dissaving as well as the increase and decrease of the stock of products cancel out over the longer time span. The question of how this outcome comes about is left open here because it requires the introduction of behavioral assumptions (for details see 2011b).

The equations that perform the mapping are the same as in Section 2 with the difference that the output is here taken as homogeneous over all periods. So when we start with the Hicksean week as shortest meaningful period length we can map the 52 detailed weekly representations onto the axiom set that relates to a year and then map ten of them onto that of a decennium. The graphics always look the same but for the scales on the axes. This holds for each discrete period length. There is, again, a loss of detailed information about each single period but this is not a disadvantage when a bird's eye view is needed. There is a consistent sequence of periods between the short and the long run that is summed up by mapping. As Kalecki put it:

In fact, the long-run trend is but a slowly changing component of a chain of short-period situations, it has no independent entity; ... (Kalecki, 1971, p. 165)

By their respective endpoints the shorter periods are truly preserved as these endpoints are the starting points for the next step in the development of the economy. The first property to emphasize is that the geometrical representation of the axiom set is self-similar over time. If we could draw an analogue to Figure 4 from the beginning to the end of the economy it would inevitably turn out to be supersymmetric. The second important property is that it is possible to employ Figure 1a in each period of Figure 4. That means that temporal aggregation implies qualitative aggregation.

It is, in principle, possible to shrink the period to an infinitesimal length and thus to perform the formal transition to a continuous analysis. This, indeed, is a quite separate line of inquiry that is not pursued further here.<sup>5</sup>

Temporal aggregation is about the formal relations between the values of the variables of the axiom set for an arbitrary number of periods and the resulting values for all periods taken together. The axiom set has the property that its geometrical representation is self-similar over time, and that means, that it is independent of the chosen period length. Qualitative and temporal aggregation entails that the elementary axiom set is applicable independently of the underlying microeconomic details and independently of the chosen period length.

# 5 Conclusion

The two main results Part (II) of the structural axiomatic analysis are:

• Qualitative aggregation entails that for any microeconomic state in period *t* there exists a correspondence that is formally represented by the first three structural axioms.

<sup>&</sup>lt;sup>5</sup> "By the early 1920s Niels Bohr and a few other physicists suspected that elementary processes in a world of discontinuous entities and states might, as a matter of principle, not allow for a continuous description in space and time ....." (Gingerezer et al., 1997, p. 174)

<sup>&</sup>quot;The Greek philosopher Zenon of Elea had already demonstrated the impossibility of dividing the infinite flow of space and time into infinitesimally small parts. ... The methods of calculus are legitimate in mathematics. However, their application to real situations in economics and elsewhere leads to the negation of the basic existential dichotomy of the finite and the infinite." (Weisskopf, 1955, p. 212)

<sup>&</sup>quot;... physics cannot be based on continous structures." (Brown, 2011, p. 630)

<sup>&</sup>quot;For mathematicians anything goes (other than contradictions). Mathematicians will assume a variable can achieve an infinite or infinitesimal value in order to provide some logically necessary conclusion. But infinities and infinitesimals in the real world are impossible *by definition*." (Boland, 2003, p. 87), original emphasis

<sup>&</sup>quot;... to walk on firm ground we must start with a finite duration." (Georgescu-Roegen, 1971, p. 214)

• Temporal aggregation entails that the structural axiom set is applicable independently of the underlying microeconomic details and independently of the chosen period length.

The structural axiom set is self-similar with regard to the differentiation of the household and business sector as well as to the sequencing of time.

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