

A Contribution to the Positive Theory of Indirect Taxation

Canegrati, Emanuele

London School of Economics and Political Science

5 December 2007

Online at https://mpra.ub.uni-muenchen.de/6116/ MPRA Paper No. 6116, posted 05 Dec 2007 15:23 UTC

A Contribution to the Positive Theory of

Indirect Taxation

Emanuele Canegrati a*

^aSTICERD,

London School of Economics and Political Science,

Houghton Street, London, WC2A 2AE, UK

November 25, 2007

Abstract

In this paper I analyse a probabilistic voting model where self-interested governments set their taxation policies in order to maximise the probability of winning elections. Society is divided into groups which have different preferences for the consumption of goods. Results show how candidates are captured by the most powerful groups, which not necessarily represent the median voter but may be located at more extreme positions. The introduction of a probabilistic voting model characterized by the presence

^{*}Corrisponding author (E-mail: e.canegrati@lse.co.uk). I am particularly grateful to Mario Gilli, Torsten Persson, Frank Cowell and all the partecipants to the STICERD seminars at the London School of Economics for useful comments. All errors are mine.

of single-minded groups overrules the classic results achieved by the median voter theorem, because it is no longer the position on the income scale to drive the equilibrium policy but the ability of groups to focus on their most preferred goods, instead. This ability allows them to achieve a strong political power which candidates cannot help going along with, because they would lose elections otherwise.

JEL Classification: D11, H24, H53

Keywords: Probabilistic Voting Theory, Single-mindedness, Indirect Taxation, Public Expenditure

1 Introduction

Taxation has been a much-discussed topic in the economic literature. From previous contributions we know that the maximum efficiency is achieved via lump-sum taxes, because they nullify the excess burden of taxation. Nevertheless, such a taxation is not desirable because considered unjust. Thus, in order to achieve equity goals, benevolent governments must accept that taxpayers distort their economic choices in order to escape the burden of taxation. As a consequence market failures, such as a reduction in the labour supply, arise.

In democratic societies, allocation choices for the public sector are made through voting, and through the actions of elected representatives. Economic outcomes must be evaluated in such a broader context, one that allows for the possibility of setting tax rates at candidate discretion, together with the collective nature of existing political institutions that must be relied on to take decisions on fiscal issues.

Depending on whether the political decision-making mechanism is considered by the analysis or not, the literature on taxation has divided in two main streams of research: the normative and the positive approach.

The normative approach seeks efficiency-oriented solutions considering the existence of a benevolent social-planner who avoids any concern regarding the collective action. A tenet achieved by this analysis states that a tax system is efficient if it minimizes the total excess burden of raising a given amount of revenues. A typical application of this approach is the inverse elasticity rule associated with Ramsey (1927) who analysed an economy with sales taxes im-

posed on different commodities. This work concludes affirming that, in order to minimise the excess burden, higher tax rates should be levied on commodities which have a relatively inelastic demand in the range of the demand function with respect to commodities whose demands are more elastic, so as to raise a given total revenue while avoiding, as far as possible, the excess burdens associated with the substitution away from commodities whose after-tax price has risen. Furthermore, a version of Ramsey's rule modified by Diamond (1975) envisions a planner who takes distributional goals into account, derived from a welfare function where weights are attached to the welfare of different individuals. In order to maximise social welfare the planner equalizes distributionally weighted marginal excess burdens per dollar raised across available tax bases.

Otherwise, the *positive approach* studies collective choice processes and their influence on political and economic outcomes. Works which belong to this second strand do not only focus on market failures but also on political failures. Two recent works (Polo, 1998; Svensson, 1997) focalise on the role of political competition where candidates propose policy platforms in order to maximise the probability of winning elections (or the number of votes), under uncertainty about voters' political preferences. Since individuals aim to maximise their utility influenced by public policies, they react positively to an increase in the amount of public goods and negatively to the payment of taxes and to welfare losses caused by taxation. The maximisation of the probability of winning is achievable if politicians design an equilibrium tax structure which equalises the change in opposition per marginal tax dollar raised across groups.

It is essential to understand equilibrium outcomes produced by well-functioning political processes, and to examine how such outcomes change when imperfections become part of the collective action. This implies that we need a model of collective choice as our starting point that allows to study and demonstrate the existence and stability of political equilibria and to examine the nature of specific equilibrium policies or outcomes. Probabilistic voting Theory is able to accomplish this goal, since the resulting Nash equilibria amongst parties are Pareto-optimal. (Hettich and Winer 1999, Chapter 4.) However, the need of taking this basic analytical step is not tied to the use of a particular framework; rather, it arises from the fundamental nature of normative analysis itself. Imperfections in private markets have their counterparts in failures of the political process. As a consequence, we must focus on the operation of the collective decision mechanism in order to identify those features that cause it to operate imperfectly. Not only must we begin by modelling a political process that leads to an optimal allocation of resources, but it is also necessary to determine tailored tax policies that will be part of the political equilibrium. Once this has been accomplished, we can then extend the examination to specific imperfections of collective decision-making and trace out their implications for structure of tax policies. Few authors writing on taxation have concerned themselves with this research programme but unless it is carried out, economists cannot accomplish an analysis of tax policy failures that has the same force as does the well-known work on private market imperfections.

Finally, once we introduce also equity goals in the analysis we must deal

with welfare state programmes which transfer resources amongst groups. A question naturally arises: to what extent do voters' preferences influence these programmes? A standard model of redistributive taxation may be found in Romer (1975), Roberts (1977) and Meltzer and Richard (1981); if we suppose that individual productivity differs and so does the availability of leisure, it can be demonstrated that political candidates commit to the policy preferred by the median voter. In equilibrium, taxes are higher the greater is the distance between median and mean income, a specific measure of income inequality. Nevertheless, in these models the single-peakedness condition, which is necessary for an equilibrium to exist, is very likely to fail, as the authors demonstrated.

In this paper I will analyse how self-interested governments set their taxation policies in a probabilistic voting model. Candidates are pure voter-seekers and aim to maximise the probability of winning elections. Society is divided into groups who assign different weights to consumption of goods, based on their preferences; that is they have different levels of single-mindedness. Results show how in equilibrium candidates must satisfy the most powerful groups, which not necessarily represent the median voter, or the middle class, but may be located at extreme positions on the income scale. The introduction of a probabilistic voting model characterized by single-minded groups breaks the classic result of median voter models because it is no longer the position on the income scale which drives the choice of candidates but the ability of groups to focus on issues they prefer, instead. This ability enables them to achieve a strong political power which candidates cannot help going along with, because they would lose the elections, otherwise. Escaping the more single-minded groups is impossible to politicians, as long as they are prisoner of their own self-interest. In this vicious circle, the role of taxation reduces only to protect private interests. Results of this model represent the antithesis of classic normative models. Taxation loses its pro-active role as a mechanism to redistribute resources from the rich to the poor or to supply public goods and becomes only a key to win elections, no matter if this means protecting even the richest components of society.

Results of this model would provide also a possible answer for the existence of the indirect taxation. This is an old issue addressed by Atkinson and Stiglitz (1976) who demonstrated that the optimal direct-cum-indirect tax problem puts all commodity taxes to zero and raises everything through income tax. More recent works by Laroque (2005) and Kaplow (2006) demonstrated that Atkinson and Stiglitz's result is even stronger because there appears to be no role for taxes on commodities even in the presence of a not optimally designed tax structure. Then, why Governments are so reluctant to abolish indirect taxation? If we consider that direct taxation is progressive in practice whilst indirect taxation is mildly regressive¹ it might be perfectly possible to see the interest of powerful interest groups to prevent a substantial shift from indirect to direct taxation. If more single-minded groups find amongst the richest component of society and are not favourable to increase the weight of direct taxation with respect to indirect taxation, Governments could not undertake this reform. As a consequence income distribution is less egalitarian.

 $^{^{1}}$ see Jones (2007) and Keen (2007)

The paper is organised as follows: section two introduces a model of indirect taxation, section three extend the model allowing for endogenous public expenditure and section four concludes.

2 A model of indirect taxation

Legend of symbols		
h = 1,, H	social groups	
$\int f^h$	group's size	
j = D, R	political candidates	
i=1,,n	goods	
\mathbf{x}_i^h	consumption of goods	
ψ^h_i	preference for goods/level of single-mindedness	
ξ^h	idiosyncratic stochastic variable	
ς	non-idiosyncratic stochastic variable	
$q_i^j \!= p_i \!+\! t_i^j$	consumption price = production price + tax rate	
s ^h	density function of idiosyncratic variable/political power of a group	
d	density function of non-idiosyncratic variable	
λ^h	marginal utility of income	
α^{j}	marginal probability of winning of D for group h	
ϕ^{h}_{oi}	effect of a variation in price of good o on the compensated demand of good i for group h	
$\chi_i^{h,j}$	distributive characteristic	
φ^h	preferences for public good	
G^{j}	public good	

I consider a society divided into H groups, indexed by h = 1, ..., H. Groups have size f^h and their members are exactly alike. Two political candidates, j = D, R, run for an election. Both candidates have an ideological label (for example, Democrats and Republicans), exogenously given. Voters' welfare depends on two components: the first is deterministic and it is represented by the consumption of goods, whilst the second is stochastic and derives from personal attributes of candidates.

Each individual in group h derives his consumption from n goods x_i^h , indexed by i = 1, ..., n. Consumption is a function of the tax policy chosen by candidates and it is perfectly observable. The deterministic component of welfare may be written in a logarithmic fashion, $\sum_{i=1}^{n} \psi_i^h \log x_i^h$, where ψ_i^h represents the weight that group h attaches to good i.

The stochastic component is denoted by $D^R \cdot (\xi^h + \varsigma)$, where the indicator function

$$D^{R} = \begin{cases} 1 & if \ R \ wins \\ 0 & if \ D \ wins \end{cases}$$

The random variable $\varsigma \leq 0$ reflects candidate *R*'s popularity amongst voters and it is realized between the announcement of policies and elections. It is not idiosyncratic and it is uniformly distributed as

$$\varsigma \sim U\left[-\frac{1}{2}, \frac{1}{2}\right]$$

with mean zero. Otherwise, $\xi^h \stackrel{<}{>} 0$ represents an idiosyncratic random variable

which measures voters' preferences for D. It is not perfectly observable by candidates and it is uniformly distributed as

$$\xi^h \sim U\left[-\frac{1}{2s^h}, \frac{1}{2s^h}\right]$$

again with mean zero and density s^h .

Therefore, a representative individual in group h maximizes the following utility function:

$$U^{h} = \sum_{i=1}^{n} \psi_{i}^{h} \log x_{i}^{h} + D^{R} \cdot \left(\xi^{h} + \varsigma\right)$$

$$\tag{1}$$

under the following budget constraint

$$\sum_{i=1}^{n} q_i^j x_i^h = M^h \tag{2}$$

where M^h is the income of any individual in group h. I denote by $q_i^j = p_i + t_i^j$ the consumption price of good i, by p_i the fixed production price² and by t_i^j the unit excise tax levied by candidate j on good i. Hence, $\overrightarrow{x} = [x_1, ..., x_n] \in X \subset \mathbb{R}^n$ denotes the vector of the consumption of goods, $\overrightarrow{q^j} = \left[q_1^j, ..., q_n^j\right] \in Q^j \subset \mathbb{R}^n$ the vector of consumption prices, $\overrightarrow{p} = [p_1, ..., p_n] \in P \subset \mathbb{R}^n$ the vector of tax rates.

I introduce two important definitions:

Definition 1 group A is said to be more single-minded than group B with re-

 $^{^{2}}$ In this model I do not take into account the impact of taxation on production.

spect to good *i* if the weight assigned by A to *i* is greater than the weight assigned by B. That is, if $\psi_i^A > \psi_i^B$.

This definition states that groups, in attributing different weights to the consumption of goods, are less or more likely to substitute a good with another³ depending on preferences they have for every good. As a consequence, there exist some goods whose consumption is more defended by groups, because its reduction would affect individuals' welfare in a more tangible way.

Definition 2 group A is said to be more politically powerful than group B if its density is higher than B's. That is if $s^A > s^B$.

In this case the political power of a group must be intended as the ability of influencing candidates' choices, when they have to take decisions over a policy. In traditional probabilistic voting models this power is expressed by a density function which captures the distribution of the electorate.

2.1 The demand for goods

Individuals maximize 1 subject to 2. For any group the Lagrangian function is

$$\mathcal{L}^{h} = \sum_{i=1}^{n} \psi_{i}^{h} \log x_{i}^{h} + D^{R} \cdot \left(\xi^{h} + \varsigma\right) + \lambda^{h} \left(M^{h} - \sum_{i=1}^{n} q_{i}^{j} x_{i}^{h}\right)$$

The set of first order conditions is

 $^{^3{\}rm For}$ a complete discussion on the Single Mindedness Theory see Canegrati (2006) and Mulligan and Sala-i-Martin (1999)

$$\begin{pmatrix} \frac{\partial \mathcal{L}^{1}}{\partial x_{1}^{1}} & \dots & \frac{\partial \mathcal{L}^{H}}{\partial x_{1}^{H}} \\ \vdots & \ddots & \vdots \\ \frac{\partial \mathcal{L}^{1}}{\partial x_{n}^{1}} & & \frac{\partial \mathcal{L}^{H}}{\partial x_{n}^{H}} \\ \frac{\partial \mathcal{L}^{1}}{\partial \lambda^{1}} & & \frac{\partial \mathcal{L}^{H}}{\partial \lambda^{H}} \end{pmatrix} = \begin{pmatrix} \frac{\psi_{1}^{1}}{x_{1}^{1}} = \lambda^{1}q_{1}^{j} & \dots & \frac{\psi_{1}^{H}}{x_{1}^{H}} = \lambda^{H}q_{1}^{j} \\ \vdots & \ddots & \vdots \\ \frac{\psi_{n}^{1}}{x_{n}^{1}} = \lambda^{1}q_{n}^{j} & & \frac{\psi_{n}^{H}}{x_{n}^{H}} = \lambda^{H}q_{n}^{j} \\ \frac{\sum_{i=1}^{n} q_{i}^{j}x_{i}^{1}}{x_{n}^{1}} = M^{1} & & \sum_{i=1}^{n} q_{i}^{j}x_{i}^{H} = M^{H} \end{pmatrix}$$

The resolution of first order conditions yields Marshallian demand functions $x_i^{h*} = \frac{\psi_i^h M^h}{q_i^j}$ and the indirect utility functions

$$V\left(x\left(q_{i}^{j}, M^{h}\right)\right) = \sum_{i=1}^{n} \psi_{i}^{h} \log \frac{\psi_{i}^{h} M^{h}}{q_{i}^{j}} + D^{R} \cdot \left(\xi^{h} + \varsigma\right)$$

2.2 Political Competition

I consider now the problem of candidates. What distinguishes this contribution from previous taxation models in Political Economy is the existence of a new setting where probabilistic voting and single-mindedness theory fuse together. In the classic theory of optimal taxation governments had always been considered as benevolent planners, who aimed to maximise a social welfare function whose characteristics depended on preferences for equity. Hence, preferences of society were perfectly mirrored by policy-maker's preferences. Weights attached to the utility of different agents were higher for the poorest and lower for the richest.

In this model politicians are considered as voter-seekers who aim to maximise the probability of winning elections by choosing an optimal policy vector $\overrightarrow{t^{j}}$. Each voter in group h votes for R if and only if R's policy provides him with a greater utility than that provided by D. That is, a generic voter ι votes for D if and only if:

$$V^{h}\left(\overrightarrow{t^{R}}\right) + \xi^{\iota,h} + \varsigma \ge V^{h}\left(\overrightarrow{t^{D}}\right) \qquad \forall \iota \qquad (3)$$

where $V^h\left(\vec{t^j}\right)$ represents the indirect utility function which individuals in group h derive under the vector of policies chosen by candidate j. Within each group there is a fraction of *swing voters*, denoted by $\hat{\iota}$, represented by those individuals who do not have a particular preference for D or R. For these voters equation 3 holds with equality:

$$\xi^{\hat{\iota},h} = V^h\left(\vec{t^D}\right) - V^h\left(\vec{t^R}\right) - \varsigma \tag{4}$$

Otherwise, voter ι votes for D if $\xi^{\iota,h} < \xi^{\hat{\iota},h}$ and for R if $\xi^{\iota,h} > \xi^{\hat{\iota},h}$. Swing voters are pivotal, since even a small change in the policy vector makes them no longer indifferent to candidates and then they vote for one of two.

The probability of winning elections for candidate j is written as⁴

$$p^{j}\left(\overrightarrow{t^{j}}, \overrightarrow{t^{-j}}\right) = \frac{1}{2} + \frac{d}{s} \sum_{h=1}^{H} f^{h} s^{h} \left[V\left(\overrightarrow{t^{j}}\right) - V\left(\overrightarrow{t^{-j}}\right) \right]$$
(5)

 $^{^{4}}$ For a complete derivation of the probability of winning in a probabilitic voting model, see Canegrati (2006) or Persson and Tabellini (2000).

where
$$V\left(\overrightarrow{t^{j}}\right) := V\left(p_{i} + t_{i}^{j}, M^{h}\right)$$
 and $s := \sum_{h} s^{h} f^{h}$.

Axiom 3 the density function of a group is twice differentiable and monotonically increasing in the consumption of goods. That is $s^h = s(x_1^h, ..., x_n^h)$, with $\frac{\partial s^h}{\partial x_i^h} > 0.$

This axiom brings something new with respect to traditional probabilistic voting models, where the density function was always treated as a constant. This idea to make the density function depend on consumption of goods is new and deserve to be explained. The classic literature on probabilistic voting models (Persson and Tabellini (2000), Lindbeck and Weibull (1987), Coughlin (1992)) has always assumed that political preferences of voters for candidates have a distribution where the density function is a constant. Instead, in this model, the density function is increasing in the level of consumption which in turn is affected by the vector of policies. Candidates realize that, should they change their policy vector, the density function of groups, and thus their political power, would change. Hence, I suggest the existence of a nexus amongst governments' choices, voters' consumption and political power of groups which eventually affects elections' outcome.

Furthermore, as suggested by Lindbeck and Weibull (1987), I assume that

Remark 4 there exists a balanced-budget constraint

$$\sum_{h} f^{h} \sum_{i} t^{j}_{i} x\left(q^{j}_{i}, M^{h}\right) = 0 \tag{6}$$

which coerces the government to redistribute, via transfers, all the tax revenues collected.

This assumption allows us to treat the model as **purely redistributive**, with the advantage of clearly showing the redistribution effects, neglecting any concern about the existence of public expenditure. In turn, equation 6 states that all the revenues collected via taxation are used to redistribute wealth amongst groups. As a consequence, if some groups are better off by the achievement of a net transfer, some others must necessarily be worse off, because they have to bear the payment of these transfers.

Finally, notice how this political game is a two-person, constant-sum and symmetric game where a pair of policies is an equilibrium pair if and only if it is a saddle point for

$$\Gamma = \left(T^D, T^R; p^D, 1 - p^D\right)$$

2.3 The equilibrium

To solve the problem I write the Lagrangian function for D (the same holds for R):

$$\mathcal{L}^{D} = \frac{1}{2} + \frac{d}{s} \sum_{h} f^{h} s^{h} \left[V\left(\vec{t^{D}}\right) - V\left(\vec{t^{R}}\right) \right] + \mu^{D} \left(\sum_{h} f^{h} \sum_{i} t^{D}_{i} x\left(q^{D}_{i}, M^{h}\right) \right)$$
(7)

The set of first order conditions is:

$$\begin{cases} \frac{\partial \mathcal{L}^{D}}{\partial q_{1}^{D}} = \frac{\partial}{\partial q_{1}^{D}} \left(\frac{1}{s}\right) d\sum_{h} f^{h} s^{h} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{1}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{1}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{1}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{1}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{D}}\right) - V\left(\overrightarrow{t^{R}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{H}}\right) - V\left(\overrightarrow{t^{H}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{H}}\right) - V\left(\overrightarrow{t^{H}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{H}}\right) - V\left(\overrightarrow{t^{H}}\right)\right] + \frac{d}{s} \sum_{h} f^{h} \frac{\partial s^{h}}{\partial q_{n}^{D}} \left[V\left(\overrightarrow{t^{H}}\right) - V\left(\overrightarrow{t^{H}}\right)\right]$$

In this game, the existence of an equilibrium is guaranteed by the concavity of the utility functions. This proof which exploits the concavity assumptions was adopted in a voting model by Hinich et al. (1973). An easy proof is also provided by Coughlin (1985), for special cases of redistributive models.

Proposition 5 In a constant-sum game an equilibrium is achieved via a convergence of policy; that is: $\overrightarrow{t^{D}*} = \overrightarrow{t^{R}*}$.

Proof. First of all, we have defined Γ as a constant-sum game, since $p^R\left(\vec{t^D}, \vec{t^R}\right) = 1 - p^D\left(\vec{t^D}, \vec{t^R}\right)$. Suppose now that the pair $\left(\vec{t^D}\diamond, \vec{t^R}\diamond\right) \in T \times T$ is an equilibrium of the game. Suppose also that $\vec{t^D}\diamond \neq \vec{t^R}\diamond$. We know from 5 that $p^D\left(\vec{t^R}, \vec{t^R}\right) = \frac{1}{2}$, because $V\left(\vec{t^R}\right) = V\left(\vec{t^R}\right)$ and thus $\frac{d}{s}\sum_{h=1}^{H} f^h s^h \left[V\left(\vec{t^j}\right) - V\left(\vec{t^{-j}}\right)\right] = 0$. Therefore, by the definition of a Nash Equilibrium it must be

$$p^{D}\left(\overrightarrow{t^{D}}, \overrightarrow{t^{R}}\right) > p^{D}\left(\overrightarrow{t^{R}}, \overrightarrow{t^{R}}\right) = \frac{1}{2}$$

$$\tag{8}$$

By the definition of a constant-sum game we also know that $p^R\left(\vec{t^D}, \vec{t^D}\right) = 1 - p^D\left(\vec{t^D}, \vec{t^D}\right) = \frac{1}{2}$ and again by the definition of a Nash Equilibrium, it must be

$$p^{R}\left(\overrightarrow{t^{R}}, \overrightarrow{t^{D}}\right) > p^{R}\left(\overrightarrow{t^{D}}, \overrightarrow{t^{D}}\right) = \frac{1}{2}$$

$$\tag{9}$$

Since $p^R\left(\overrightarrow{t^R\diamond}, \overrightarrow{t^D\diamond}\right) = 1 - p^D\left(\overrightarrow{t^R\diamond}, \overrightarrow{t^D\diamond}\right)$, this implies that $p^D\left(\overrightarrow{t^R\diamond}, \overrightarrow{t^D\diamond}\right) < \frac{1}{2}$. By 8, this implies that $p^D\left(\overrightarrow{t^R\diamond}, \overrightarrow{t^D\diamond}\right) > \frac{1}{2}$, a contradiction. Therefore, $\overrightarrow{t^D\diamond} = \overrightarrow{t^R\diamond}$.

Corollary 6 In equilibrium, $V\left(\vec{t^D}\diamond\right) = V\left(\vec{t^R}\diamond\right)$.

Proof. By the meaning of Proposition 5, $\vec{t^D} = \vec{t^R}$. Therefore, $V\left(\vec{t^D}\right) = V\left(\vec{t^R}\right)$.

Exploiting Corollary 6, we may re-write the first order conditions in the following manner:

$$\begin{cases} \frac{\partial \mathcal{L}^{D}}{\partial q_{1}^{D}} = \frac{d}{s} \sum_{h} \frac{\partial V^{h}}{\partial q_{1}^{D}} f^{h} s^{h} + \mu^{D} \left(\sum_{o} t_{o}^{D} \sum_{h} f^{h} \frac{\partial x_{o}^{h}}{\partial q_{o}^{D}} + x_{o}^{h} \right) = 0 \qquad o \neq i \end{cases}$$

$$\vdots$$

$$\frac{\partial \mathcal{L}^{D}}{\partial q_{n}^{D}} = \frac{d}{s} \sum_{h} \frac{\partial V^{h}}{\partial q_{n}^{D}} f^{h} s^{h} + \mu^{D} \left(\sum_{o} t_{o}^{D} \sum_{h} f^{h} \frac{\partial x_{o}^{h}}{\partial q_{o}^{D}} + x_{o}^{h} \right) = 0$$

$$\frac{\partial \mathcal{L}^{D}}{\partial \mu^{D}} = \sum_{h} f^{h} \sum_{i} t_{i}^{D} x \left(q_{i}^{D}, M^{h} \right) = 0$$

From Roy's Identity we know that $\frac{\partial V^h}{\partial q_i^D} = -\lambda^h x_i^h$ where λ^h is the marginal utility of income. Applying Slutzky decomposition we obtain the Slutzky matrix

$$D_{q^{j}}x\left(q^{j},M^{h}\right) = D_{q^{j}}h\left(q^{j},U^{h}\right) - D_{M^{h}}x\left(q^{j},M^{h}\right)x\left(q^{j},M^{h}\right)^{\top}$$

An element of the matrix is $\frac{\partial x_i^h}{\partial q_i^D} = \frac{\partial (x_i^h)^c}{\partial q_i^D} - \frac{\partial x_i^h}{\partial M^h} x_i^h$, where $\frac{\partial (x_i^h)^c}{\partial q_i^D}$ is the change in the Hicksian demand with a change in price, representing the substitution effect, and $\frac{\partial x_i^h}{\partial M^h} x_i^h$ is the income effect. Under the hypothesis of normal goods $\frac{\partial x_i^h}{\partial q_i^D} < 0$, for every *i*. Substituting these two expressions in the set of first order conditions we obtain:

$$\frac{\partial \mathcal{L}^{D}}{\partial q_{i}^{D}} = -\sum_{h} \left(\lambda^{h} f^{h} s^{h} \frac{d}{s} + \mu^{D} f^{h} \sum_{o} t_{o}^{D} \frac{\partial x_{o}^{h}}{\partial M^{h}} \right) x_{i}^{h} + \mu^{D} \left(\sum_{o} t_{o}^{D} \sum_{h} f^{h} \xi_{oi}^{h} + x_{o}^{h} \right) = 0$$

$$\tag{10}$$

Expression

$$\alpha^{h,D} := \lambda^h f^h s^h \frac{d}{s} + \mu^D f^h \sum_o t^D_o \frac{\partial x^h_o}{\partial M^h}$$

denotes the marginal probability of winning of D for group h. It measures the weight that D attaches to group h as a function of its political power, represented by two parameters: density and size. A suitable interpretation for this expression is the following: redistribution transfers are a function of the weight that candidates attribute to groups, which depends on the effect that a change in the utility of the group, due to a change in the policy vector, has on the probability of winning at the margin. Hence, groups are assigned with a weight which is higher the more single-minded the group. Furthermore, $\phi_{oi}^{h} := \frac{\partial (x_{i}^{h})^{c}}{\partial q_{o}^{D}}$ represents the effect of a variation in price of good o on the compensated demand of good i for group h. Equation 10 may be re-written as follows:

$$\frac{\partial \mathcal{L}^D}{\partial q_i^D} = -\sum_h \alpha^h x_i^h + \mu^D \left(\sum_o t_o^D \sum_h f^h \phi_{oi}^h + x_o^h \right) = 0 \tag{11}$$

Dividing both sides by μ^D and x_i^h and re-arrange terms we finally obtain:

$$-\frac{\sum_{o} t_{o}^{D} \sum_{h} f^{h} \phi_{oi}^{h}}{x_{i}^{h}} = -\frac{\Delta x_{i}^{ch}}{x_{i}^{h}} = \frac{\mu^{D} - \chi_{i}^{h}}{\mu^{D}}$$
(12)

 $\forall i$

 $\chi_i^{h,D} := \frac{\sum_h \alpha^h x_i^h}{x_i^h} \text{ represents what in the literature is known as the ditributive characteristic of good i for group h and for candidate D. <math>-\frac{\Delta x_i^{ch}}{x_i^h}$ represents approximately the proportional variation in the compensated aggregate demand of good i.

Proposition 7 The distributive characteristic is higher the higher is the amount of good consumed by groups which receive a higher weight by candidates, that is the more single-minded.

Proof. the distributive characteristic of good *i* for group *h* and for candidate *D* is obtained by multiplying the marginal probability of winning of candidate *j* for group *h* by consumption of a good by group *h* with respect to the total consumption of good *i*. Notice that $\chi_i^{h,D}$ is increasing in $\alpha^{h,D}$, being $\frac{\partial \chi_i^{h,D}}{\partial \alpha^{h,D}} = 1$. We also know that $\alpha^{h,D}$ increases with respect to an increase in the group's

density,

$$\frac{\partial \alpha^h}{\partial s^h} = \lambda^h f^h \frac{d}{s} \left(1 - \frac{\overbrace{f^h s^h}}{s} \right) > 0$$

By Axiom 3 we know that the density function is monotonically increasing in the consumption of goods. Finally, the first order derivative of the Marshallian functions is increasing in the level of single-mindedness, since $\frac{\partial x_i^{h*}}{\partial \psi_i^h} = \frac{M^h}{q_i^i} > 0$.

Therefore, more single-minded groups provide the candidates with a higher marginal probability of winning, which translates the consumption of goods in higher level of distributive characteristics. We have found a precise linkage between single-mindedness and distributive characteristic summarised by the following scheme:

$$single-mindedness\ (\uparrow)\Longrightarrow consumption\ of\ good\ (\uparrow)\Longrightarrow$$

 $density\ function\ (\uparrow) \Longrightarrow distributive\ characteristic\ (\uparrow)$

Proposition 8 The optimal tax structure induces a lower reduction in the consumption of those goods which are the most preferred by more single-minded groups. **Proof.** a reduction in consumption is captured by the left-hand side of 12, which is negative. This expression is lower the lower is the right-hand side, which is lower the smaller the difference between μ^j and $\alpha^{h,j}$. By proposition 7 we know that the distributive characteristic is higher the higher the single-mindedness of a group and hence the right-hand side reduces as well.

To what extent do taxation of goods obtained in this political economy framework differ from the classic taxation à la Ramsey? To answer, we must compare the many-person Ramsey's rule (Diamond, 1975) with equation 12. In the former, optimal tax rates induce a lower reduction in the consumption of those goods which are more consumed by the poor, because this category of individuals are assigned with a higher weight by society. Instead, in 12, the weight attached by candidates does not only depend on individuals' income but also on groups' political power. That is, the more powerful groups obtain a higher political consideration by candidates. As a consequence, candidates do not only take equity goals into account, as in the classic Ramsey rule. This attitude represents the real political failure of this model compared to a traditional model taken from the optimal theory of taxation. The difference between the traditional Ramsey rule $-\frac{\sum_{a}^{t} c_{a} \sum_{b}^{\phi} \phi_{a}^{i}}{\mu} = \frac{\mu - \chi_{b}^{i}}{\mu}$ and 12 can be calculated taking the difference of the two expressions. This difference, equal to

$$\lambda^{h} \left(\frac{\partial W}{\partial V^{h}} - f^{h} s^{h} \frac{d}{s} \right) + \mu^{j} \left(1 - f^{h} \right) \sum_{o} t_{o}^{j} \frac{\partial x_{o}^{h}}{\partial M^{h}}$$

is higher the lower f^h and s^h ; this means that the less single-minded groups receive a lower weight by candidates, whilst under Ramsey the social weight assigned by the Government depends on the effect which an increase in the utility of group h has on the social welfare at the margin, $\frac{\partial W}{\partial V^h}$. This weight is generally higher for the poorest as long as the Social Welfare Function is strictly concave. I remark that 12 does not say that candidates totally neglect the welfare of the poor because $\alpha^{h,j}$ is higher the higher is the marginal utility of income, λ^h , which is higher for the poorest⁵. Notice also that the classic Ramsey rule and 12 coincide if $\frac{\partial W}{\partial V^h} = f^h s^h \frac{d}{s}$; that is, *if the importance attributed by* society to the increase in the welfare of group h is exactly equal to the political importance attributed by candidates to the same group. In this case, and only in this case, the normative and the positive approaches achieve the same results. Nevertheless, a tenet taken by the theory of optimal taxation still holds: in equilibrium, the policy chosen by candidates is characterised by different tax rates, even though the redistribution does not take place between the rich and the poor but between the strongest and the weakest groups. The following table compares results obtained under the classic Ramsey rule and 12.

⁵The marginal utility of income is always decreasing in the level of income.

	Classic Ramsey rule	Single-mindedness rule
General formula	$-\frac{\sum\limits_{o}^{t_o} \sum\limits_{h} \phi_{oi}^h}{x_i^h} = \frac{\mu - \chi_i^h}{\mu}$	$-\frac{\sum\limits_{o}^{t_{o}}\sum\limits_{h}^{D}f^{h}\phi^{h}_{oi}}{x^{h}_{i}} = \frac{\mu^{D} - \chi^{h}_{i}}{\mu^{D}}$
Distributive characteristic	$\frac{\sum\limits_{h} \left(\lambda^{h} + \mu \sum\limits_{o} t_{o} \frac{\partial x_{o}^{h}}{\partial M^{h}}\right) x_{i}^{h}}{x_{i}^{h}}$	$\frac{\sum\limits_{h} \left(\lambda^{h} f^{h} s^{h} \frac{d}{s} + \mu^{D} f^{h} \sum\limits_{o} t^{D}_{o} \frac{\partial x^{h}_{o}}{\partial M^{h}}\right) x^{h}_{i}}{x^{h}_{i}}$
Distortion on consumption	yes	yes
Political failure	no	yes
Achievement of equity goals	yes	depending on the location of single-minded groups on the income scale
Better off groups	poor	more single-minded
Worse off groups	rich	less single-minded
Highest weight assigned	poor	more single-minded

3 Endogenous public expenditure

I analyse now an extension of the previous model considering a Government which must choose both the tax rates and the provision of a public good. The introduction of public goods in probabilistic voting models with single-minded groups raises two fundamental questions:

- 1. to what extent is the optimal provision of public goods influenced by distortionary taxation?
- 2. to what extent is the traditional Samuelson rule modified when the Government is not benevolent but aims to maximise the probability of winning elections?

The problem of the individual may be re-written in the following log-linear fashion:

$$\max_{\{x_i^h\}} \sum_{i=1}^n \psi_i^h \log(x_i^h) + \varphi^h \log G^j + D^R \cdot \left(\xi^h + \varsigma\right)$$

$$s.t.\sum_{i=1}^{n} q_i^j x_i^h = M^h$$

where G^{j} denotes the per-capita level of provision of a public good chosen by candidates and φ^{h} the idiosyncratic preference of group h for the provision of the public good, or in other words, the mindedness of the group for the amount of the public good. The production of this good is entirely financed by taxes levied on tax-payers. Thus, individuals' choices are influenced by the amount of the public good. On the one hand, G reduces the individuals' disposable income, since the higher G the higher the taxes which individuals must pay to balance their budget; in turn, public expenditure crowds out private consumption. On the other hand, the arising substitution effect depends on the degree of complementarity or substitutability between private and public goods; the effect of a change in the amount of public good on private goods is higher the higher is the degree of complementarity between private and public goods.

Solving the individual maximization problem we obtain the Marshallian functions $x_i^{h*} = \frac{\psi_i^h M^h}{q_i^j}$ and the Indirect Utility Function

$$U\left(x_{i}^{h*},G^{j}\right)=V\left(x\left(q_{i}^{j},M^{h}\right),G^{j}\right)$$

The Government's budget constraint is:

$$C\left(G^{j}\right)\sum_{h}f^{h} = \sum_{h}f^{h}\sum_{i}t_{i}^{j}x\left(q_{i}^{j},M^{h}\right)$$

where $C(G^j)$ denotes the per-capita cost function of the public good. I assume that $C(G^j)$ is a twice differentiable function, with $C_{G^j} := \frac{\partial C(G^j)}{\partial G^j} > 0$ and $C_{G^jG^j} := \frac{\partial^2 C(G^j)}{\partial^2 G^j} > 0$; that is, the production of the public good has marginal decreasing costs. Furthermore, C_{G^j} measures the Marginal Rate of Transformation (MRT) and in order to emphasise this fact I will define $C_{G^j} := MRT^j$.

Secondly, I solve the candidate's problem, which is the same as before, modified only by the presence of the public good. I denote the new candidate policy vector by $\eta^j = \left[t_1^j, ..., t_n^j, G^j\right] \in \Phi^j \subset \mathbb{R}^{n+1}$ and I write the Lagrangian function:

$$\mathcal{L}^{j} = \frac{1}{2} + \frac{d}{s} \sum_{h} f^{h} s^{h} \left[V\left(\eta^{j}\right) - V\left(\eta^{-j}\right) \right] + \mu^{j} \left(\sum_{h} f^{h} \sum_{i} t_{i}^{j} x\left(q_{i}^{j}, M^{h}\right) - C\left(G^{j}\right) \sum_{h} f^{h} \right)$$
(13)

First, notice that the optimal tax rate 12 does not change even in the presence of public expenditure which finances public goods. Instead

Proposition 9 the marginal rate of transformation is equal to the sum of idiosyncratic preferences for the public good of groups weighted by their size and density.

Proof. The first order conditions for 13 are:

$$\frac{\partial \mathcal{L}^{j}}{\partial q_{1}^{j}} = \frac{d}{s} \sum_{h} \frac{\partial V^{h}}{\partial q_{1}^{j}} f^{h} s^{h} + \mu^{j} \left(\sum_{o} t_{o}^{j} \sum_{h} f^{h} \frac{\partial x_{o}^{h}}{\partial q_{1}^{j}} + x_{o}^{h} \right) = 0$$

$$\vdots$$

$$\frac{\partial \mathcal{L}^{j}}{\partial q_{n}^{j}} = \frac{d}{s} \sum_{h} \frac{\partial V^{h}}{\partial q_{n}^{j}} f^{h} s^{h} + \mu^{j} \left(\sum_{o} t_{o}^{j} \sum_{h} f^{h} \frac{\partial x_{o}^{h}}{\partial q_{n}^{j}} + x_{o}^{h} \right) = 0 \qquad (14)$$

$$\frac{\partial \mathcal{L}^{j}}{\partial G^{j}} = \frac{d}{s} \sum_{h} \frac{\partial V^{h}}{\partial G^{j}} f^{h} s^{h} - \mu^{j} \left(MRT^{j} \sum_{h} f^{h} \right) = 0 \qquad (15)$$

Since in equation 15 $\frac{\partial V^h}{\partial G^j} = \frac{\varphi^h}{G^j}$ we obtain a final version of the equation which refers to the choice of public good:

$$\frac{d\sum_{h}\varphi^{h}f^{h}s^{h}}{sG^{j}\sum_{h}f^{h}} = \mu^{j}\left(MRT^{j}\right)$$
(16)

To provide an example, suppose now that $C(G^j) = (G^j)^2$, with $MRT^j = 2G^j$. Equation 16 becomes

$$\frac{d\sum_{h}\varphi^{h}f^{h}s^{h}}{sG^{j}\sum_{h}f^{h}} = 2\mu^{j}G^{j}$$
(17)

which, solved with respect to G^j yields:

$$G^{j*} = \left(\frac{d\sum \varphi^h f^h s^h}{2s\mu^j \sum_h f^h}\right)^{\frac{1}{2}}$$
(18)

This expression clearly shows how the provision of public good depends on the mindedness of groups, that is on the idiosyncratic parameter φ^h .

In this expression μ^{j} represents the marginal cost of public funds, defined as the social cost of spending one extra dollar on any given public good and it measures the distortionary effect of taxation.

Proposition 10 The provision of public good is strictly increasing in the singlemindedness of the group, weighted by its density and size and decreasing in the marginal cost of public fund.

Proof. Performing some comparative statics we see that

$$\frac{\partial G^{j*}}{\partial \varphi^h} = \frac{1}{2} \left(\frac{d \sum_h \varphi^h f^h s^h}{2s \mu^j \sum_h f^h} \right)^{-\frac{1}{2}} \frac{d f^h s^h}{2s \mu^j \sum_h f^h} > 0$$

29

$$\begin{split} \frac{\partial G^{j*}}{\partial s^h} &= \frac{1}{2} \left(\frac{d\sum_h \varphi^h f^h s^h}{2s\mu^j \sum_h f^h} \right)^{-\frac{1}{2}} \frac{df^h \varphi^h}{2s\mu^j \sum_h f^h} > 0\\ \frac{\partial G^{j*}}{\partial f^h} &= \frac{1}{2} \left(\frac{d\sum_h \varphi^h f^h s^h}{2s\mu^j \sum_h f^h} \right)^{-\frac{1}{2}} \frac{d}{2s\mu^j} \frac{\varphi^h s^h \sum_h f^h - \sum_h \varphi^h f^h s^h}{\left(\sum_h f^h\right)^2} > 0\\ \frac{\partial G^{j*}}{\partial \mu^j} &= -\frac{1}{2} \left(\frac{d\sum_h \varphi^h f^h s^h}{2s\mu^j \sum_h f^h} \right)^{-\frac{1}{2}} \frac{df^h s^h}{2s(\mu^j)^2 \sum_h f^h} < 0 \end{split}$$

Otherwise, the Ramsey rule does not change with respect to the previous case and the reason is simple. If the Ramsey rule detects the most efficient way to finance a certain level of expenditure, for every level of expenditure, all the more so it must detect the most efficient way to finance the level of expenditure when this is chosen in an optimal way to finance G. Of course, tax rates differ depending on the level of G, since higher level of G entails higher level of tax revenues, but the optimal tax rate structure does not change with respect to the previous case.

Therefore, the provision of public good is higher the higher the presence of more single-minded groups which ask for it. With respect to the classic Samuelson rule, a model with single-minded groups states that the provision of public goods is not only inefficient because of the presence of distortionary taxation, but also because of the political failure which society falls into, due to the presence of powerful interest groups which candidates must satisfy.

4 Conclusions

In this paper I analysed how voter-seeking candidates decide their indirect taxation policies in a Probabilistic Voting model. Results say that candidates are captured by the most powerful (single-minded) groups, which not necessarily coincide with the median voter, but may represent even the richest components of society. These results are at odds with the classic results achieved exploiting the median voter theorem, because it is no longer the median position on the income scale which determines the equilibrium policies chosen by candidates, but the ability of groups to focus on their more preferred issues, instead.

Finally, this model provides a possible explanation to the existence of indirect taxation, since we perfectly know how the optimal direct-*cum*-indirect tax problem puts all commodity taxes to zero and raises everything through income tax (Atkinson and Stiglitz, 1976). Instead, this model may suggest how there could be an interest by powerful single-minded groups to prevent a substantial shift from indirect to direct taxation. Since the indirect taxation is mostly regressive whilst direct taxation mostly progressive, richest single-minded groups would not favour this shift. The direct-*cum*-indirect tax problem can be perfectly studied using Probabilistic Voting and Single-mindedness theory; I hope this could be done in future works.

References

- Auerbach, A. (1985) The Theory of Excess Burden and Optimal Taxation, in Handbook of Public Economics, Vol. I, Elsevier.
- [2] Atkinson, A. B. and Stiglitz (1976) The Design of tax Structure: Direct versus Indirect Taxation. the Journal of Public Economics 6, pp. 55-75.
- [3] Beckmann, K. (2002) How Leviathan Taxes, Constitutional Political Economy, Vol.13, pp. 265-273.
- [4] Boadway, R. W. and Bruce, N. (1984), Welfare Economics, Basil Blackwell
- [5] Canegrati, E. (2006) The Single-Mindedness Theory: Micro-foundation and Applications to Social Security Systems, mimeographed
- [6] Coughlin, P. (1985) Elections with Redistributional Reputations. Prepared for the 1985 Carnegie-Mellon conference on Political Economy.
- [7] Coughlin, P. (1992) Probabilistic Voting Theory, Cambridge University Press
- [8] Diamond, P. (1975) A Many-Person Ramsey Rule, Journal of Public Economics Vol.4, pp.335-42
- [9] Gahvari, F. (2006) On the Marginal Cost of Public Funds and the Optimal Provision of Public Goods, Journal of Public Economics, Vol. 90 pp.1251-1262
- [10] Gentry, W. Optimal Taxation, Columbia University, mimeo

- [11] Hettich, W. & Winer, S. (1999), Democratic Choice and Taxation: A Theoretical and Empirical Analysis, Cambridge University Press
- [12] Hinich, M, Ledyard, J and Ordershook, P. (1973) A Theory of Electoral Equilibrium: A Spatial Analysis Based on the Theory of Games, Journal of Politics, 35; pp. 154-193
- [13] Jones, F. (2007) The Effects of Taxes and Benefits on Household Income 2005/2006. Non-journal article, Office for National Statistics, http://www.statistics.gov.uk/CCI/article.asp?ID=1804
- [14] Kaplow, L. (2006) On the Undesirability of Commodity Taxation even when Income taxation is not Optimal, Journal of Public Economics, 90, pp. 1235-1250.
- [15] Keen, M. (2007) Vat Attacks! IMF Working Paper WP/07/142, International Monetary Fund.
- [16] Laroque, G.R. (2005) Indirect Taxation is Superfluous under Separability and Taste Homogeneity: A simple Proof, Economics Letters 87, pp. 141-144
- [17] Lindbeck, A. & Weibull, J. (1987), Balanced-budget redistribution as the outcome of political competition. Public Choice 52(3): 273-297
- [18] Meltzer, A. & Richard, S. (1985) A Positive Theory of in-kind Transfers and the Negative Income Tax, Public Choice 47, pp.231-265
- [19] Mulligan C. B. & Sala-i-Martin: Social Security, Retirement and the Single-Mindness of the Electorate, (1999) NBER Working Paper 9691

- [20] Persson, T. & Tabellini, G. (2000), Political Economics: Explaining Economic Policy, MIT Press
- [21] Polo, M. (1998) Electoral Competition and Political Rents, IGIER, Milan, mimeo
- [22] Ramsey , F. P. (1927) A Contribution to the Theory of Taxation, Economic Journal, Vol.37, pp. 47-61
- [23] Roberts, K. (1977) Voting over Income Tax Schedules, Journal of Public Economics 8, pp: 392-340
- [24] Romer, T. (1975) Individual Welfare, Majority Voting and the Properties of a Linear Income Tax, Journal of Public Economics 7, pp:163-168
- [25] Saez, E. (2002) The desirability of commodity taxation under non-linear income taxation and heterogeneous tastes, Journal of Public Economics Vol. 83, pp.217-230
- [26] Svensson, J. (1997) The Control of Public Policy: Electoral Competition, Polarization and Primary Elections, The World Bank, Washington D.C. mimeo