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 $28 \ {\rm November} \ 2006$

Online at https://mpra.ub.uni-muenchen.de/952/ MPRA Paper No. 952, posted 29 Nov 2006 UTC

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November, 2006

Abstract

This essay analyzes the long-run economic effects of HIV/AIDS in Kenya, with emphasis on fertility, education and child labor. Human capital, which is built up through formal education and parental child-rearing, is the only input in production. Two aspects are central to the analysis: First, a mature AIDS epidemic causes massive premature adult mortality, thereby destroying existing human capital and reducing the labor force on a large scale. Second, the transmission of human capital to future generations is weakened, as children are left orphaned and surviving adults are correspondingly burdened. As a consequence, per capita income decreases and communities can less afford to raise and educate children as they did before the outbreak of the disease. The underlying theoretical model, in which it is assumed that parents raise and educate children for both financial and altruistic reasons, is calibrated using data for the period 1920 to 2000. The long-run effects of the disease. which depend heavily on parents' expectations about future mortality rates, are estimated for the years 2000-2040. Both human capital and per capita income grow significantly more slowly after the outbreak of the epidemic, while the incidence of child labor doubles for some periods. The level of fertility falls in the immediate aftermath of the outbreak, but can be significantly higher when the epidemic has reached a mature phase, depending on parents' expectations. Governmental interventions in the health sector in the early phase of the epidemic can strongly mitigate its adverse effects.

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The author thanks the German Academic Exchange Service (DAAD) for support.

1 Introduction

Kenya declared the HIV/AIDS epidemic a national disaster in 1999, 15 years after the first HIV/AIDS case had been reported. By that time, more than half a million Kenyans were estimated to have died of the disease, and some 2.5 million adults were infected. Other countries in Sub-Saharan Africa had reacted to the epidemic more than a decade earlier – notably Kenya's neighbor Uganda, which had declared AIDS a national disaster in 1986. Expectations in Kenya in 1999 were grim: the death rate was projected to rise from 560 persons per day in 2000 to 760 by 2005.¹ While governmental interventions following the 1999 declaration seem to have borne some fruit, and the death rate had even been reduced to 300 per day by 2003,² the epidemic has not yet been brought under complete control.

Most new infections occur among young people, particularly women aged 15 to 24 and men aged 30 and younger.³ As 70 per cent of all Kenyan children are born to mothers vounger than 30, high HIV/AIDS prevalence rates in this age group will strongly affect the way families raise and educate children. As the parents become ill, family income is reduced, either because they cannot work or because of the stigma towards those infected, who have difficulty finding employment. The high costs of treatment further increase the burden on the household's income. Children raised in families affected by HIV/AIDS often enjoy less parental guidance and care, and their education suffers, as they may have to work to support their parents and siblings. As therapies are often too costly, most victims die within 8-10 years of being infected, leaving their children orphans. By 2003, 37% of all orphans were AIDS orphans, up from an estimated 3% in 1990 and 22% in 1995.⁴ Even the education of those children whose parents are not ill suffers, as their teachers are often too sick to conduct their classes. The Kenya Teachers Service Commission reports that deaths among teachers more than tripled between 1995 and 1999, rising from 450 to 1500 per year.⁵ On average, 1.4% of all teachers are expected to die of HIV/AIDS yearly between 2000 and $2010.^{6}$

As women of child-bearing age are strongly affected by the disease, and may transmit

¹Source: $http://www.standwithafrica.org/hiv_aids/reality1.php$

²Source: http://www.aegis.com/news/afp/2003/AF031233.html

³Source: http://www.unaids.org/EN/Geographical + Area/by + country/kenya.asp

⁴Sources: 1990 and 1995 figures: 'Children on the Brink',2002, U.N.AIDS, UNICEF and USAID collaboration. 2003 figure: 'Children on the Brink', 2004, U.N.AIDS, UNICEF and USAID collaboration ⁵Source: 'Education and HIV/AIDS: A window of hope', The World Bank, 2002

⁶Source: ibid.

the virus on giving birth, the total number of children raised by a family is also expected to change. Yet only 30% of all women know that taking anti-retroviral drugs during late pregnancy can reduce the risk of Mother-To-Child-Transmission, according to the 'Kenya Demographic and Health Survey' conducted in 2003. Two different effects are possible: on the one hand, with potential mothers falling ill and dying and higher child mortality due to HIV/AIDS, completed familiy size could fall. On the other hand, families might respond to the rise in mortality by having more children, enough of whom would then survive to take care of their parents when these cannot care for themselves, either due to HIV/AIDS or to old age.

Several studies have projected the impact of the epidemic in Kenya, focusing on economics, the health and education sectors, the development of the population size or specific population groups, like orphans or women. While macroeconomic empirical studies in the 1990s (e.g. Bloom and Mahal (1997)) suggest that the effects of the HIV/AIDS epidemics on the economies of Sub-Saharan African countries are small, more recent work suggests that the effects on specific countries or regions may be very damaging. Bell, Devarajan and Gersbach (2003), for example, simulate the South African economy for the years 1990-2080 and show that the effects of the epidemic will indeed be strong, with a distinct possibility of a collapse of the economy in the absence of government action. Arndt and Lewis (2000) use a shorter simulation period, namely, 1997-2010, and find that both total and per capita GDP are substantially lower in the face of the epidemic, compared to the counterfactual without HIV/AIDS. Bollinger, Stover and Nalu (1999) review several studies of the impact of AIDS in Kenva, and analyze the economic impact of the epidemic on that country's households, agriculture, firms and macroeconomy. They conclude by recommending measures aimed at mitigating the effects of the disease and emphasise the importance of governmental commitment to addressing HIV-related problems, and treating the disease as a 'national priority'.

Ferreira and Pessoa (2003) consider a continuous-time model with premature mortality due to HIV/AIDS where an individual's decision about schooling depends on her life expectancy. They arrive at the conclusion that HIV/AIDS has a strong impact on longterm growth, as individuals reduce formal education when their life expectancy falls. The model is applied to several African countries, and the authors show that schooling falls, on average, by half, while income falls by about a quarter in the presence of the HIV/AIDS epidemic. Corrigan, Glomm and Mendez (2004) consider a 2-generation OLG model where individuals can die prematurely before the start of the last period of life. They consider several scenarios, depending on the duration and strength of HIV/AIDS mortality shock. Growth rates in all scenarios fall when the epidemic breaks out, and recover if the shock is not permanent, that is, if morality rates subsequently return to their pre-epidemic level. The authors provide an extended version of their initial model in Corrigan, Glomm and Mendez (2005), where individuals live for up to three periods. The process of human capital formation is not only dependent on the parents' survival, but also on the time the child spends pursuing formal education rather than working. In addition to deciding about their own consumption and savings, parents, who are assumed to be altruistic, now also decide about their offsprings' schooling and consumption. If an individual is infected with the HIV virus, he also decides about spending on medical treatment, and does not save. The effects of the HIV/AIDS epidemic are large, reducing the current income after 10 generations by 5-45% of potential NO-AIDS income, depending of the scenario.

Young (2005) analyses South Africa, calibrating a Beckerian model of household behavior to Household Survey and Demographic and Health Survey Data. He then simulates various scemarios concerning household response to HIV/AIDS, and finds that per capita income can be larger in the presence of the epidemic, as fertility, and thereby the future labor force, are reduced, and this effect dominates the reduction in schooling orphans experience.

Bell et al. (2004) employ a three-generation OLG model to simulate the effects of the disease in Kenya up to 2050. Unlike the South African case, they find that the Kenyan economy is not threatened with a collapse, but GDP in the AIDS case is lower by about 40% in 2040 compared to the counterfactual without AIDS, and population is lower by about a third. Kenya's long-term problems are attributed to three interrelated factors: first, the 'weakening of the mechanisms through which human capital is transmitted from one generation to the next'; second, a sharp drop in the productivity of human capital in the decade following 1990; and third, the HIV/AIDS epidemic. To analyze the effects of these mechanisms on the Kenyan economy, Bell et al. (2004) focus on household decisions concerning education.

The purpose of the present essay is to extend their analysis by incorporating households' fertility decisions, as it seems realistic to assume that families react to exogenous shocks to mortality by adjusting not only the level of schooling, but also the number of children

they intend to have in the first place. The essay will draw upon Bell et al. (2004), particularly where the model's structure and the data are concerned.

The essay is structured as follows: Section 2 gives a historical overview and discusses the data used. The model is introduced in section 3, and its calibration is presented in section 4. Several variations of projections of the Kenyan economy until 2040 are discussed in sections 5 and 6, while the issue of public policy is taken up in section 7. The issue of formulating and measuring social welfare in the presence of premature adult mortality is addressed in section 8. The main results are stated in section 9, with conclusions in section 10.

2 Historical Overview and Data: 1920-2000

At the beginning of the 20th century, Kenya was a British Protectorate officially called 'British East Africa'. Inland colonization by white settlers began around 1901, when the railway line connecting Mombasa and Lake Victoria was completed. By 1920, 9000 settlers were living in Kenya, and by 1950 their number had increased nearly 10-fold.⁷ Control over nearly all economic activity was concentrated in their hands, and the indigenous population was either employed as workers on the coffee farms, or engaged in mostly low-productivity traditional occupations. Legislation prevented the African population from purchasing and owning property in the highly fertile Kenyan Highlands and from taking part in government. It was only in 1944, that the first African became a member of the Colony's Legislative Council.⁸ The inequalities in economic and political power led to unrest, culminating in the Mau Mau Uprising between 1952 and 1960. While the uprising was suppressed by British troops, some of the Mau Mau's aims – like land reform – were attained in subsequent years.

In 1963, Kenya gained independence, and Jomo Kenyatta became its first president. He was succeeded by Daniel Arap Moi in 1978, who stayed in power until 2002. After Independence, several reforms were undertaken, especially in the spheres of land policy, the educational system, and the political system. Many of these reforms – particularly those regarding education – can be observed in the time series used in this essay, to which we now turn.

 $[\]label{eq:source_result} \ensuremath{^7\text{Source. http://www.lonelyplanet.com/destinations/africa/nairobi/printable.htm} \\ \ensuremath{^7\text{Source. htm}} \\ \ensuremath{^7\text{Sour$

⁸Source: http://www.kenyalogy.com/eng/info/histo12.html

Decadal data on the economies' output and demography for the years 1950 to 2000 are used, as well as data on the average years of schooling from 1920 onwards. A detailed discussion of the time series and revisions is given in Bell et al. (2004), on which this section draws. For the remainder of the essay, the round years will be used as time points, whereby the variable t = 1, 2, 3..., 14 denotes the number of decades elapsed since the year 1900, so that t = 10 denotes the decade starting in the year 2000.

2.1 Population

During the period of interest, five censuses were conducted in Kenya, in the years 1948, 1962, 1969, 1979 and 1989. The United Nations Population Division, the World Bank (in the form of the World Development Indicators, WDI) and the Penn World Tables (PWT) provide secondary data on the Kenyan population and its structure. For the purposes of the calibration, data for the years 1950-1990 are used, with estimates for the nearest round date in the case of the Census figures.

The WDI does not report the total population for 1950, and its data for 1960 onwards are identical to the UN's, as are the PWT data. However, the population in the PWT for 1950 is higher than both the UN and Census data by 3.6% and 7.7% respectively. Bell et al. (2004) reconstruct the early part of the series and reject the PWT's estimates for that year.

Both the UN Population Division and the Censuses provide data on the age distribution. Except for the first and last group, which include infants aged 0-5 and people aged 65 and older, respectively, all 8 age groups span 10 years, their mid-points being 10, 20, 30, 40, 50 and 60. Age-groups will be denoted by the index a = 0, ..., 7 and the size⁹ of an age group in period t will be denoted by N_t^a . As both estimates are problem-ridden, a revised series was derived, in which the implicit age-specific death rates (defined below) are higher for those 35 and older than those implicit in of the original UN data. As a consequence, old cohorts are smaller, while young cohorts are relatively larger than the U.N.'s. Denote the mortality rate in age group *i* over the period t to t + j - i, (j > i) in period t by $q_t^{i,j}$. The age-specific death rate for age group *a* is defined as the probability that a member of age group *a* will not survive to become a member of age group (a + 1)10 years later, and will be denoted by $q_t^{a,a+1}$. Mortality rates can then be computed from

⁹The unit of N_t^a and of all other population data in the essay is 10^3 .

Table 1: Population Tables										
age group/year	1950	1960	1970	1980	1990	2000				
0-4	1040	1541	2294	3482	4458	4696				
5-14	1606	2317	3371	4951	7182	9006				
15-24	1192	1491	2167	3179	4715	6875				
25-34	882	1097	1381	2019	2979	4447				
35-44	634	784	983	1248	1833	2731				
45-54	441	542	677	857	1099	1634				
55-64	240	349	432	545	698	911				
65+	125	201	238	351	511	864				
		Sourco: Ro	11 ot 11 (9)	004)						

Table 1: Population Tables

Source: Bell et al. (2004)

the population tables as follows:

$$q_t^{i,j} = 1 - \frac{N_{t+(j-i)}^j}{N_t^i}.$$

In the remainder of the essay, the probability that a member of age group a = 2 reaches age group a = 4 will play a major role. It will be denoted by κ_t :

$$\kappa_t \equiv 1 - q_t^{3,5} = \frac{N_{t+2}^5}{N_t^3}.$$
(1)

2.2 Output

Both the Penn World Tables and the World Development Indicators provide data on aggregate output, with the PWT time series starting in 1950 and the WDI 10 years later. The PWT contains data on per capita GDP in constant purchasing power units with the base year 1995, as well as population data. As discussed in the previous section, the PWT population estimate for 1950 is implausibly high; so that total GDP for that year is derived using the revised estimate instead. The two series do not differ significantly for the following years, and the PWT series is chosen, being the longer of the two. As the purpose of the analysis is to derive long-term effects, short-term shocks to GDP are smoothed by forming 5-year moving averages. As can be seen from table 2, the Kenyan economy experienced a period of fast growth after Independence, but also a marked slowing down after 1990, with per capita GDP actually falling. For the remainder of the paper, GDP will be denoted by Y_t .

Year	1950	1960	1970	1980	1990	2000				
GDP (10^7)	436	642	1089	2014	3076	3633				
Average annual GDP growth (%)	_	3.9	5.4	6.3	4.3	1.7				
2	D 11	1 (20	0.1)							

Table 2: GDP in Kenya, 1950-200)()
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Source: Bell et al. (2004)

2.3 Educational Attainment

The educational system in Kenya underwent several major changes in the last century. The Department of Education was founded in 1911, but only 3% of the country's African population had enjoyed any formal education by 1925 (Thias and Carnoy, 1972). Primary education was financed and organised by the communities and missionaries, and no common curriculum existed. Until Kenya gained independence in 1963, the African population received mostly technical and vocational training, as recommended by the Fraser Report of 1909. The Ominde Commission, set up in 1964, led to changes in the schooling system which aimed at increasing enrolments in secondary education. Up to 1966, primary and secondary education spanned 8 and 4 years respectively. Primary education was reduced to 7 years after 1966, but was extended again to 8 years in 1985, with all schools using the same curriculum. By 1973, school fees had been abolished for the first 6 years of primary education, following UNESCO's proposals. This led to high enrolment rates, particularly so in 1974 and 1979. As a consequence, the government hired a substantial number of new teachers, many of them poorly trained, thereby possibly reducing the quality – albeit not the quantity – of educational inputs. To finance these additional teachers, schools introduced a plethora of new, compulsory, fees, such as building and equipment levies. According to Nkinyangi (1982), "the cost of schooling as much as quadrupled in some ditricts" ¹⁰ after the levies were introduced. While some of these fees were abolished in subsequent years, primary schooling only became genuinely free in 2003.

Two data sets are used to determine the average years of completed schooling: the Censuses mentioned in section 2.1 and reports by the ministry of education. A very detailed description of the method is given in Bell et al. (2004), the results of which are set out in table 3. The variable e_t denotes the average years of schooling of the school-age cohort in period t, expressed as a fraction of a 12-year schooling period.

¹⁰Nkinyanngi (1982), pp 204.

Table 3: Educational Attainment									
Year	Year 1920 1930 1940 1950 1960 1970 1980 19								
Education e_t 0.047 0.080 0.134 0.201 0.367 0.458 0.520								0.570	
Source: Bell et al. (2004)									

$\mathbf{2.4}$ **School Fees**

Several surveys have studied household spending, and found that households spend about 3-5.5% of their total income on schooling. A summary of the studies' findings is given in table 4. School fees amounted to about 50% of total spending on education in 1994, and were abolished by 2003. As data on household income and expenditures is available until 1990, the costs of sending one child to school for one period, σ_t , can be computed from:

$$\sigma_t e_t N_t^1 = 0.04 \ Y_t \Leftrightarrow$$

$$\sigma_t \equiv 0.04 \ Y_t / (e_t N_t^1) \quad \forall t \le 9.$$
(2)

As e_t, N_t^1 and Y_t are endogenous after 1990, σ_t cannot be computed using the equation above for t > 9. Instead, it will be assumed that all school-going costs remained constant after 1990, with the exception of school fees, which were abolished. From this, we set:

$$\sigma_t = \sigma_9/2 \quad \forall t > 9. \tag{3}$$

Survey	School Fees	Spending on Education
Rural Household Survey Nyanza	2.2	
Province 1970/71		
Urban Houshehold Budget Survey		5.5^{a}
1993/94		
Welfare Monitoring Survey II 1994	1.4^{b}	2.9^{b}
Welfare Monitoring Survey II 1994	2.0^{c}	4.0^{c}
Welfare Monitoring Survey III 1997		5.5

Table 4: Household Spending on Education: Surveys

^a Recreation and Education

^b Mean Household Expenditure

^c Mean Household Expenditure - with Enrolled Children

3 The Model

The basic model describes household decisions concerning the bearing and rearing of children in the presence of premature adult mortality, for example, due to HIV/AIDS.

It is assumed that households consist of three generations, namely, children, parents and grandparents, each of whom is endowed with one unit of time. Children divide their time between working and learning, where the fraction of time assigned to education will be denoted by $e \in [0, 1]$. Surviving parents work full-time, as do grandparents until the age of 65. It is assumed that parents receive the income of the entire family, including that accruing to the grandparents, and then redistribute this income according to some set of social rules, which are described below.

For simplicity, it is assumed that parents (father and mother) are identical with respect to both their levels of human capital and their mortality rates. They raise and educate children in order to increase their own current consumption and to finance their old age. As investment in physical capital is ruled out by assumption,¹¹ and grandparents work part-time only, they also rely on transfers from their children to finance their consumption. A fixed fraction $\chi \in (0, 1)$ of the family's income is transferred to the grandparents. There are no bequests. Raising children is costly, and the better educated parents are, the more they spend on raising their children. School fees, which make up about half of the total costs of primary education in Kenya, were abolished only in 2003.

The temporal structure of the model is as follows: When they reach age group a = 2 young adults form couples and decide on the number of children they intend to have and raise. They also enter into a binding contract on the education these children are to receive when they reach school-going age. If parents have perfect foresight about child mortality and if there is 'replacement fertility', as in Bell, Devarajan and Gersbach (2003), then a decision about fertility is equivalent to deciding about N_t^1 , and we will take N_t^1 as the corresponding decision variable for the remainder of the essay. When parents are in age groups a = 2 and a = 3 their children go to school according to the decision made at birth, as stated in the contract; their level of schooling is e_t , and the level of human capital

¹¹While households in Kenya can save, for example by purchasing land or other assets, most of this saving is precautionary saving. Retirement is not financed by savings, as shown by Hoddinott (1992): Old-age consumption is financed mostly through agricultural income, transfers from children, wages and business income. Other sources of income, such as pensions - which could be interpreted as a form of saving - make up at most 5.2% of the total income for poor and middle-income households, and 30% for richest decile. This suggests that pensions and other forms of savings are not available for the poor.

(measured in efficiency units of labor) they attain upon reaching adulthood is denoted by $\lambda_{t+1}(e_t)$. In period t + 1, the children start working themselves, and have their own children. When their parents reach age group a = 5 in period t + 2, they start receiving transfers from the younger generations. Therefore, the total number of 'young couples' in period t will be $(N_t^2 + N_t^3 + N_t^4)/2$, while the total number of 'old couples' in period t + 2will be $(N_{t+2}^5 + N_{t+2}^6 + N_{t+2}^7)/2$.

It is assumed that the efficiency of a grown-up depends on the time she spent at school, the average efficiency of her parents and the productivity of the educational process [see Bell et al. (2004)]. If an individual does not spend any time at school, she will attain the basic minimum level of efficiency $\lambda = 1$. It is assumed that adults in the two youngest age groups (i.e. a = 2 and a = 3) are involved in educating children, and that the educational technology is isoelastic with parameter ϵ , as in Bell et al. (2004). The children which are going to school in period t attain the following level of human capital in period t + 1:

$$\lambda_{t+1} = 2z_t e_t^{\epsilon} \left(\frac{N_t^2 \lambda_t + N_t^3 \lambda_{t-1}}{N_t^2 + N_t^3} \right) + 1, \qquad z_t, \epsilon > 0 \tag{4}$$

where $z_t (> 0)$ can be thought of as the strength of the mechanism for the inter-generational transmission of knowledge. The growth rate of the adults' level of efficiency in the case of full-time schooling is:

$$g_{\lambda} \equiv \frac{\lambda_{t+1} - \lambda_t}{\lambda_t} = 2z_t \left(\frac{N_t^2 + N_t^3 \frac{\lambda_{t-1}}{\lambda_t}}{N_t^2 + N_t^3}\right) + \frac{1}{\lambda_t} - 1.$$
(5)

Note first that the growth rate will always be positive if previous generations enjoyed no schooling whatsoever, that is,¹² if $\lambda_t = \lambda_{t+1} = 1$. The growth rate g_{λ} will be positive even for high levels of efficiency if z_t is greater than 0.5. If, however, z_t is lower than 0.5, the growth rate will depend on the level of λ_t : If λ_t is sufficiently close to one, g_{λ} will be positive, whatever be the level of λ_t , as $1/\lambda_t$ is then sufficiently close to one.¹³ If the adults' level of efficiency is growing, however, the term in brackets will be lower than 1, while $1/\lambda_t$ will be falling, so that g_{λ} will eventually be zero or negative. A steady-state in λ can arise if z_t is stationary, with the steady-state level of efficiency being $\lambda^* = 1/(1 - 2z_t)$. Note that in a steady-state with respect to λ , population growth plays no role, as the term in brackets in (5) will be 1 in all periods when $\lambda_t = \lambda_{t+1}$. The temporal structure

¹³For
$$\lambda_t = 1$$
, g_{λ} is always positive, as $2z_t \left(\frac{N_t^2 + N_t^3 \frac{\lambda_{t-1}}{\lambda_t}}{N_t^2 + N_t^3}\right) + \frac{1}{1} - 1 > 0$

¹²This result is valid not only for the case of full-time schooling, but also for all $e_{t+1} > 0$.

of the population pyramid, however, is important, as it influences the choice of e_t , and therefore also determines whether stationary value of λ can be reached.

Income is generated through the production of a single, non-storable good. Let the efficiency of a school-age child be fixed at μ . Assume, further, that those younger than 5 and older than 65 years of age, that is, age groups a = 0 and a = 7, do not work at all. Therefore, ignoring unemployment, the total labor supply (measured in efficiency units) of an extended family in period t will be:

$$L_t = \underbrace{N_t^2 \lambda_t + N_t^3 \lambda_{t-1} + N_t^4 \lambda_{t-2} + N_t^5 \lambda_{t-3} + N_t^6 \lambda_{t-4}}_{\text{adult labor}} + \underbrace{N_t^1 (1 - e_t) \mu}_{\text{child labor}}$$
(6)

The production function is assumed to exhibit constant returns to scale with respect to labor (measured in efficiency units). Given the long-term character of the model, assessing the effects of land use in the production function is essential. However, data on land use, development and quality is not available. While a data series on arable land is available at the FAO, and reaches back to 1960, it does not include any information on the quality of the land used, and no data are available for the years before 1960, nor are projections for the future. To keep matters simple, therefore, we assume that the amount of land available is constant, and shared by all adults. We also assume that households are autarchik.

$$Y_t \equiv \frac{\alpha_t}{(N_t^2 + N_t^3 + N_t^4 + N_t^5 + N_t^6)^A} \cdot L_t = \theta_t \cdot L_t$$

$$= \theta_t \cdot (N_t^2 \lambda_t + N_t^3 \lambda_{t-1} + N_t^4 \lambda_{t-2} + N_t^5 \lambda_{t-3} + N_t^6 \lambda_{t-4} + N_t^1 (1 - e_t) \mu),$$
(7)

where $A \ge 0$, $\alpha_t > 0$. The factor $\theta_t \left(= \frac{\alpha_t}{(N_t^2 + N_t^3 + N_t^4 + N_t^5 + N_t^6)^A} \right)$, denotes the amount of output produced with one unit of efficient labor. It has two components: its denominator $(N_t^2 + N_t^3 + N_t^4 + N_t^5 + N_t^6)^A$ captures the fact that the total amount of land is fixed, and divided among all families equally. α_t describes the general level of economic productivity. It can change over time, for example, as a result of economic policy or macroeconomic shocks.

The only active decision-makers in the present setting are the (young) parents, and the decisions they make determine their level of consumption in the last phase of life, as well as the level of efficiency their offspring will attain as adults. For simplicity, assume that the parents' decisions do not influence mortality rates.

Assume that raising infants is free, so that the level of consumption of a family which has

infants only is not influenced by their fertility decisions. Therefore, when making fertility decisions in period t, parents, who are in age groups a = 2, 3 consider their (expected) level of consumption while their children are going to school (denoted by $c_{1,t}$) and later, when they themselves are old, whereby only consumption in the first period of old age is considered for simplicity (denoted by $c_{2,t+2}$). The adults also possess altruism, which expresses itself not only through the expenditures on educating and raising children, but also in their concern for the children's future welfare. For simplicity, it is further assumed that the utility function is additively separable, whereby the level of utility of adults who die prematurely is normalized to zero. Following Bell et al. (2004), we choose the form:

$$E_t U(c_{1,t}, c_{2,t+2}, e_t, N_t^1) = \beta_0 ln(c_{1,t}) + \beta_1 \kappa_t ln(c_{2,t+2}) + \frac{2N_t^1 \kappa_{t+1}}{N_t^2 + N_t^3} \left(1 - \lambda_{t+1}(e_t)^{-\eta}\right)$$
(8)

where κ_{t+k} , k = 0, 1 is the parents' subjective estimate thereof at time t.

Note that by choosing

$$\phi = \frac{2N_t^1 \kappa_{t+1}}{N_t^2 + N_t^3} \left(1 - \lambda_{t+1} (e_t)^{-\eta} \right)$$

as the subutility function with respect to altruism and the education production function in (4), equilibria with $\lambda_t = 1$ and $e_t = 0 \forall t$ (poverty traps) are excluded by construction if $\epsilon < 1$. To see this, differentiate the subutility function with respect to e_{t+1} , and evaluate this derivative for $e_t = 0$:

$$\lim_{e_t \to 0} \frac{\partial \phi}{\partial e_t} = \infty \quad \forall \epsilon < 1, \quad \forall \eta.$$

As will be shown in the following section, the model can only be calibrated by choosing $\epsilon < 1$, so that poverty traps are indeed excluded. The step in the calibration needed to determine ϵ is independent of the choice of functional form for preferences, so that the result $\epsilon < 1$ will be valid even if the utility function took a different form. Therefore, as long as the subutility function ϕ satisfies the condition $\lim_{e_t \to 0} \frac{\partial \phi}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \lambda_{t+1}}{\partial e_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \phi}{\partial \theta_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \lambda_{t+1}} \frac{\partial \phi}{\partial \theta_t} = \lim_{e_t \to 0} \frac{\partial \phi}{\partial \theta_t} \frac{\partial \phi}{\partial \theta_t} + \lim_{e_t \to 0} \frac{$

Consider a family that raises N_t^1 children in period t. Each pair of adults in the groups

a = 2, 3, 4 receives the same fraction of the family's total income:

$$\frac{Y_t}{(N_t^2 + N_t^3 + N_t^4)/2} = \theta_t \cdot \frac{2(N_t^2\lambda_t + N_t^3\lambda_{t-1} + N_t^4\lambda_{t-2} + N_t^5\lambda_{t-3} + N_t^6\lambda_{t-4})}{(N_t^2 + N_t^3 + N_t^4)} + \theta_t \cdot \frac{2N_t^1(1 - e_t)\mu}{(N_t^2 + N_t^3 + N_t^4)}.$$

A fixed fraction $\chi \in [0, 1]$ of the total output produced by adults is allocated to the grandparents (a = 5, 6, 7), who consume it. Assume that each child consumes $b\lambda_t$ units per decade, and that one unit of schooling costs σ_t per child. Then the consumption of a young couple in period t is:

$$c_{1,t} = 2\theta_t (1-\chi) \frac{(N_t^2 \lambda_t + N_t^3 \lambda_{t-1} + N_t^4 \lambda_{t-2} + N_t^5 \lambda_{t-3} + N_t^6 \lambda_{t-4})}{(N_t^2 + N_t^3 + N_t^4)}$$
(9)

+
$$2\theta_t(1-e_t)\mu \frac{N_t^1}{(N_t^2+N_t^3+N_t^4)} - 2b\lambda_t \frac{N_t^1}{(N_t^2+N_t^3+N_t^4)} - 2\sigma_t e_t \frac{N_t^1}{(N_t^2+N_t^3+N_t^4)}$$

The share χ is divided equally among all old members of the family:

$$c_{2,t+2} = 2\theta_{t+2}\chi \cdot \frac{(N_{t+2}^2\lambda_{t+2} + N_{t+2}^3\lambda_{t+1} + N_{t+2}^4\lambda_t + N_{t+2}^5\lambda_{t-1} + N_{t+2}^6\lambda_{t-2})}{N_{t+2}^5 + N_{t+2}^6 + N_{t+2}^7}.$$
 (10)

When deciding about N_t^1 and e_t parents can observe all relevant historical and current values of N, λ and e, particularly λ_t and e_t , and the mortality rates in period t. They also form expectations about future mortality rates, and hence expectations about N_{t+k}^a for $a = 2, \ldots, 7$, and k = 1, 2, 3, 4.

Assume that parents have perfect foresight about all the $q_t^{i,j}$ in all future periods $t + 1, t + 2, \ldots$. They can also observe or deduce the levels of efficiency λ_{t-2} , λ_{t-1} and λ_t associated with age groups a = 5 and a = 6 in period t + 2. All the other values needed to determine $c_{2, t+2}$, namely, N_{t+2}^2 and N_{t+2}^3 as well as λ_{t+2} are unknown. The level of N_{t+2}^3 can be determined from N_t^1 , which is endogenous, using $N_{t+2}^3 = (1 - q_t^{1,3})N_t^1$. Similarly, $N_{t+2}^2 = N_{t+1}^1(1 - q_{t+1}^{1,2})$. However, the level of N_{t+1}^1 is not known to the parents when they make their decisions. Therefore, parents must make conjectures about the future number of school-going children and about e_{t+1} , which will determine λ_{t+2} . Given the complexity of this structure, assume that parents use a simplifying rule: they expect the level of schooling to be stationary:

$$E_t e_{t+1} = e_{t-1}, (11)$$

and the number of school-age children raised by couples in a = 2 and a = 3 in period t + 1 to be stationary too:

$$E_t \left(\frac{2N_{t+1}^1}{N_{t+1}^2 + N_{t+1}^3} \right) = \frac{2N_{t-1}^1}{N_{t-1}^2 + N_{t-1}^3}$$

$$\Leftrightarrow \quad E_t N_{t+1}^1 = N_t^1 \cdot \frac{E_t N_{t+1}^2 + E_t N_{t+1}^3}{N_{t-1}^2 + N_{t-1}^3} \equiv N_t^1 \psi_t.^{14}$$
(12)

Note that N_{t+1}^2 appears in ψ_t , which is endogenous, as $N_{t+1}^2 = N_t^1(1-q_t^{1,2})$. For simplicity, however, the ratio ψ_t will be computed from the population tables (e.g. table 1).

Using (4), (9) and (10), the couple's expected utility can be rewritten as a function of N_t^1 and e_t as well as $E_t e_{t+1}$ and $E_t N_{t+1}^1$ alone. Its optimization problem at time t is then formulated as follows:

$$\max_{e_t, N_t^1} E_t U(e_t, N_t^1; E_t e_{t+1}, E_t N_{t+1}^1, \cdot) \text{ subject to } N_{min} \le N_t^1 \le N_{max}$$
(13)
and $0 \le e_t \le 1$

This yields two first-order conditions as functions of $E_t e_{t+1}$ and $E_t N_{t+1}^1$:

$$\frac{\partial E_t U(\cdot; E_t e_{t+1}, E_t N_{t+1}^1)}{\partial N_t^1} \quad \text{and} \quad \frac{\partial E_t U(\cdot; E_t e_{t+1}, E_t N_{t+1}^1)}{\partial e_t}.$$

Together with (11) and (12) these yield, for an interior solution,

$$\frac{\partial E_t U(\cdot)}{\partial N_t^1} \bigg|_{E_t e_{t+1} = e_{t-1}, E_t N_{t+1}^1 = N_t^1 \psi_t} = 0 \quad \text{and} \quad \frac{\partial E_t U(\cdot)}{\partial e_t} \bigg|_{E_t e_{t+1} = e_{t-1}, E_t N_{t+1}^1 = N_{t-1}^1 \psi_t} = 0, \quad (14)$$

which, in turn, yield the optimal levels of N_t^1 and e_t .

Note that in the present setup, there is no time-inconsistency regarding the parents' decisions about e_t , as their expectations about mortality rates are correct by assumption if there is no HIV/AIDS shock. That is, when their children reach school-going age, parents have no incentives to depart from the binding contract on e_t which they made at

¹⁴An alternative specification, namely $E_t e_{t+1} = e_t$, and respectively $E_t \left(\frac{2N_{t+1}^1}{N_{t+1}^2 + N_{t+1}^3}\right) = \frac{2N_t^1}{N_t^2 + N_t^3}$ is not well-defined, and could lead to non-unique solutions. Assume, for example, that parents expect future fertility rates to be high and education to be low, and therefore choose a high fertility and low schooling themselves, so that the expectations are satisfied. If, however, parents had assumed that fertility would be low and education would be high, and would themselves had chosen a high level of e_t and a low level of N_t^1 , the expectations again would have been satisfied. The specification above, therefore, would have been satisfied in both cases, and an additional rule would be required to choose between all possible solutions.

child-birth. If, however, the parents' expectations about mortality rates prove to be incorrect, that is, if there is an unexpected mortality shock like the outbreak of the HIV/AIDS epidemic after the children are born but before they reach school-going age, it is unlikely that the contractual level of e_t is still optimal, from the parents' point of view. Therefore, e_t might be open to renegotiation.

4 Calibration

The model presented in the previous section is calibrated to the data from section 2. The data on output, population and education can be used to derive the adult's level of efficiency λ_t in each past generation, the children's level of efficiency μ , the factors ϵ, z_t, A and α_t , which characterize the education and production functions, respectively, the social rules governing transfers to the old and to children, χ and b, and the parameters of the subutility functions, β_0 , β_1 and η . This will be done in two steps: first, national aggregates will be used to compute $A, \epsilon, \mu, z_t, \alpha_t$ and λ_t . Second, the calibration of preferences will yield the values of β_0 , β_1, b, χ and η .

Step 1

The first step of the calibration is identical to the one employed in Bell et al. (2004). As noted in section 2.3, only 3% of all adult Africans had enjoyed any education by 1925. Therefore, it seems safe to assume that in 1910, before the Department of Education was established, the general population had no education at all and their level of efficiency was $\lambda_1 = 1$, that is, the minimum possible. Following Bell et al. (2004), λ_2 is set to 1.01. Using this as an initial condition and equation (4) yields a set of 8 equations describing the dynamics of the adults' level of efficiency:

$$\lambda_t = 2z_{t-1}e_{t-1}^{\epsilon} \left(\frac{N_{t-1}^2 \lambda_{t-1} + N_{t-1}^3 \lambda_{t-2}}{N_{t-1}^2 + N_{t-1}^3}\right) + 1, \quad t = 3, \dots, 10$$
(15)

While no data on e_{10} are available yet, it seems reasonable to assume $e_{10} = 0.621$ (see Bell et al. [2004]). The second condition used in the calibration gives the age groups' contribution to GDP, as stated in equation (7):

$$Y_t = \theta_t (N_t^2 \lambda_t + N_t^3 \lambda_{t-1} + N_t^4 \lambda_{t-2} + N_t^5 \lambda_{t-3} + N_t^6 \lambda_{t-4} + N_t^1 (1 - e_t) \mu), \quad t = 5, \dots, 10$$
(16)

where $\theta_t = \frac{\alpha_t}{(N_t^2 + N_t^3 + N_t^4 + N_t^5 + N_t^6)^A}$. The system described by (15) and (16) consists of 14 equations and 25 unknowns: α_t for $t = 5, \ldots, 10$, λ_t and z_t for $t = 3, \ldots, 10$ as well as

 μ , A and ϵ , which are assumed to have stayed constant over time. As the system is underdetermined, solving it is only possible by making assumptions about the values of some of the variables.

Beginning with 1940, adults had enjoyed at least one year of schooling on average (see table 3), which suggests that the measures undertaken in the education sector in the early phase of the century had started to bear fruit. Therefore, the first shift in z_t is assumed to have taken place in 1940. The second shift came after Kenya abolished school fees and reformed the educational system, that is, for the decade starting 1980. While per capita GDP grew until 1990, it started to fall thereafter. Hence, we assume that α stayed constant until t = 9, and dropped once, in t = 10. With these assumptions, the total of 14 variables associated with z_t and α_t is reduced to 5:

$$z_2 = z_3, \quad z_4 = z_5 = z_6 = z_7, \quad z_8 = z_9 = z_{10}$$

 $\alpha_5 = \alpha_6 = \alpha_7 = \alpha_8 = \alpha_9, \quad \alpha_{10}$

To anchor the system, it is still necessary to choose two more variables. To simplify the calculation, ϵ and A are chosen exogenously, as the equations are linear in all other parameters. Solutions where $\epsilon < 0.47$ or $\epsilon > 0.62$ are not considered, as they yield either negative values of one of the parameters, or $\mu > 1$, that is, the labor efficiency of a child is higher than that of an adult who did not enjoy any schooling. The exact value of ϵ chosen should reflect the parents' decisions regarding schooling. As these decisions are determined by their preferences, we now turn to their calibration.

Year	1920	1930	1940	1950	1960	1970	1980	1990			
e_t	0.047	0.080	0.134	0.201	0.367	0.458	0.520	0.570			
N_t^1				1606	2317	3371	4951	7182			
$2N_t^1/(N_t^2+N_t^3)$				1.55	1.79	1.90	1.91	1.87			

Table 5: Households' choices of e_t and N_t^1

Step 2

Table 5 presents the households' decisions concerning education and fertility for the years 1950 to 1990. As can be seen, an interior solution existed during the whole period¹⁵

Source: Bell et al. (2004)

¹⁵If the household decisions were corner solutions, this would imply that the social rule on N_{min} required each family to raise at least 1.55 children. As such a high value of N_{min} is rather restrictive, it seems

and the two conditions in (14) can be used to recover the preference parameters. For any given value of ϵ and ensuing values of μ , λ_t , z_t and α_t , five parameters need to be determined through a calibration of the preferences, namely, η , χ , b, β_0 and β_1 . For computational reasons, solving the system is only possible if one chooses η exogenously, using a grid search method. The other variables are calibrated using (14) for the years 1970 and 1990. A plethora of results exists for the different values of ϵ and η : from all the possible results, one with $\beta_0/\beta_1 \leq 1.01^{20} = 1.22$ and $c_{1,t}/c_{2,t} \approx 1$, t = 7,9 is chosen. The first condition (i.e. $\beta_0/\beta_1 \leq 1.01^{20}$) considers the the rate of pure impatience of individuals. While there are no studies estimating this rate for Kenya, the rate is between 0.25 and 0.5% p.a. in the U.S., according to Fullerton and Rogers (2003) and Altig et al. (1996). Consequently, we will irgnore all solutions where the pure impatiance lies above 1% p.a. in Kenya. The second condition, namely $c_{1,t}/c_{2,t} \approx 1$, implies that families choose a fairly smooth path of consumption in the two periods of life, apart from the eventuality of premature death, which is captured by the term κ_{t+1} in (8). For all values of A < 0.04 and A > 0.17, no solutions satisfying the conditions above exist. Similarly, if $\epsilon < 0.47$, the calibration yields $\mu > 1$, that is, a child's level of labor efficiency is higher than that of an adult who enjoyed no schooling whatsoever, which does not seem realistic.

A continuum of results satisfying all conditions above exists. To keep the number of solutions manageable, we have chose a stepwidth of 0.01 for A, ϵ and η , which reduces the number of solutions to 27. The summary statistics of all 27 solutions are set out in table 6.

Parameter	Min	Max	Average
A	0.06	0.17	0.10
ϵ	0.52	0.54	0.53
η	0.57	2.06	1.44
μ	0.35	0.69	0.54
χ	0.08	0.18	0.13
Time Preference a	0.49	0.99	0.72
Drop ^b in α_t	18.28	19.13	18.64
Drop^c in z_t	43.18	45.92	44.79
Drop^d in λ_t	10.09	15.41	13.32

Table 6: Calibration results: summary statistics

a In % per year.

^b Defined as $-(\alpha_{10} - \alpha_9)/\alpha_9$ in %

^c Defined as $-(z_8 - z_7)/z_7$ in % ^d Defined as $(\lambda_8 - \lambda_9)/\lambda_8$ in %

reasonable to assume that 1.55 children per family, as raised in 1950, constitutes an interior solution.

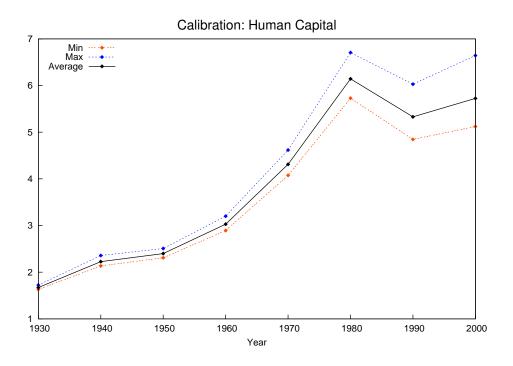


Figure 1: Calibration Results (All Calibrations)

Min., Max., and Average refer to the minimum, maximum and average value λ_t takes over all calibrations.

A value of A between 0.06 and 0.17 implies that, even if α_t stays constant, the productivity of one unit of efficient labor $(\alpha_t/(\sum_{a=2}^6 N_t^a)^A)$ has fallen as population has grown. Working-age population (age groups 2–6) has more than tripled between 1950 and 1990, which implies a reduction in productivity of 7% to 21% during that period. In all solutions satisfying the conditions above, we get $\mu \in [0.35, 0.69]$ that is, a child's labor efficiency is lower by at least 30% than the efficiency of an uneducated adult. The transfer to the grandparents amounts to 8-18% of the total income from adult labor. This is somewhat lower than the grandparents' share of the population $(\frac{N_t^5 + N_t^6 + N_t^7}{\sum_{a=0}^7 N_t^a} \approx 0.12$ for $t \leq 9$).

There were two sharp falls in the efficiency associated with the educational technology, one in the 1930s and another in the 1970s, after the Kenyan government had started to reform the school system yet again. The transmission factor z_t fell by about 45% during the 1970s, and settled at a value just above 0.5, ($z_9 \in [0.53, 0.61]$ in all solutions). With z_t sharply reduced, the growth rate of λ slows too; indeed, the young adults' level of efficiency falls between 1980 and 1990. The economy experiences another shock over the period 1990 – 2000, as α_t falls by about 19%. This shock has two effects: first, labor income is reduced. Second, raising children becomes relatively more expensive. Recalling (9), note that the costs incurred in raising children depend on b, λ_{t+1} and N_{t+1}^1 only,¹⁶ and not on α_{t+1} , which was constant during the years used in the calibration of b. As a consequence, the ratio b/α_t was constant too for t = 7 and t = 9. By 2000, however, the ratio rises as α_t falls, so that raising children is now relatively more expensive.

While the projections are computed for all 27 calibrations, we will present the results of one specific calibration in detail to illustrate the processes underway. The aggregate results of all other calibrations will also be set out. The parameters of the calibration chosen for a detailed description are set out in table 7, while the average values of the parameters are reported in figure 1 and table 24 in the appendix. As can be seen from tables 7 and 24, the calibration chosen for detailed description is, to some extent, the 'average' calibration.

Table 7: Calibration Results Exogenous:									
A = 0.10	$\epsilon = 0.53$	$\eta = 1.46$							
	Endogenous:								
$\mu = 0.538$	$\chi = 0.133$	b = 273.94							
$\beta_0 = 1.8801$	$\beta_1 = 1.6132$								
t	λ_t	z_t	α_t						
2	1.01	1.6791	-						
3	1.6688	1.6791	_						
4	2.2192	1.0188	_						
5	2.3917	1.0177	1357						
6	3.0183	1.0177	1357						
7	4.2922	1.0177	1357						
8	6.1094	0.5613	1357						
9	5.2868	0.5613	1357						
10	5.6710	0.5613	1104						

Table 7: Calibration Results

To summarize, the calibration is done in two steps: the first determines the parameters of the technologies and historical values of λ , while the second deals with the preference parameters. To derive the parameter values we have imposed two sets of restrictions:

¹⁶If the costs incurred in raising children were a function of α , the factor describing labor productivity would drop out of the utility function, as this is logarithmic in form. As a consequence, all decisions on children would be independent of α , which does not seem realistic.

first $\mu \leq 1$, $\beta_0/\beta_1 \leq 1.02^{20}$, with $\beta_0 \geq \beta_1$, and $c_{1,t}/c_{2,t} \approx 1$, which have economic reasons and are independent of the data employed or the country/problem analyzed. The second set of restrictions imposed concerns z_t and α_t . These restrictions are specific to the data set used, and hence to the country/historical experience it reflects. Changing any of the restrictions will lead to significant changes in the calibration results, if any can be derived at all. Koukoumelis (2005) shows that the calibration will, in general, be sensitive to even small measurement errors in Y_5 , the 1950 GDP level. He also shows that the degree of sensitivity to errors in Y_5 can be reduced by choosing a different set of restrictions regarding z_t . In the present paper, we have kept the original restriction in Bell et al. (2004) in order to ensure that the calibrations are comparable.

5 Projections: The Base Case

5.1 Preliminaries

Using the results of the calibrations presented in the previous section, the household decisions regarding completed fertility and education are determined under several scenarios. First, there is the benchmark case without HIV/AIDS, which is the counterfactual. Second, there the AIDS scenario in which the HIV/AIDS epidemic breaks out, and families fully recognize its effects during the 1990s, and adapt their earlier decisions about education accordingly (Scenario 1). We assume that fertility decisions have already been fully implemented by the time children are at school. Third, there is the case in which parents fail to take notice of the epidemic's effects until the late 1990s (Scenario 2). In all cases, the projections start with N_9^1 and e_9 , that is, the first decisions are made in period t = 8and implemented/revised in period t = 9.

5.1.1 Data

To compute the projections, data on mortality rates for 2000 onwards are needed. For both scenarios, revised projections based on those made by the US Bureau of Census are used, following Bell et al. (2004). The population pyramids for both cases are given in tables 8 and 9. The implicit survival rates κ_t and mortality rates $(1 - \kappa_t)$ are set out in table 10. Survival rates for the second age group (age 15 to 24) are lower by up to 30 percentage points if the epidemic breaks out, and mortality rates are at least 1.9 times higher in the case of AIDS. At the peak of the epidemic, mortality rates are more than 3 times higher than their respective values in the case without AIDS during four consecutive decades.

	Table 8: Projections: Population Tables without AIDS										
	1990	2000	2010	2020	2030	2040	2050	2060	2070		
0-4	4458	4696	4602	4503	4537	4398	4336	4336	4336		
5-14	7182	9006	9550	8995	8965	8968	8715	8715	8715		
15-24	4715	6875	8666	9236	8744	8759	8807	8601	8644		
25-34	2979	4447	6526	8277	8878	8458	8525	8624	8475		
35-44	1833	2731	4116	6098	7809	8454	8129	8269	8442		
45-54	1099	1634	2463	3755	5628	7290	7982	7761	7982		
55-64	698	911	1379	2115	3280	4998	6581	7323	7234		
65+	511	864	1294	1969	3131	5266	8395	8395	8395		
			n	D.11	+ 1 (2)	004)					

Table Q. Duciestian . р. .1..... Tables with and AIDC

Source: Bell et al. (2004)

Table 9: Projections: Population Tables with AIDS

				1					
	1990	2000	2010	2020	2030	2040	2050	2060	2070
0-4	4458	4556	3874	3436	3238	3038	2972	2972	2972
5-14	7182	8612	8416	7197	6578	6258	5971	5971	5971
15-24	4715	6839	8209	8040	6945	6429	6186	5902	5902
25-34	2979	4187	5780	6912	6997	6360	6182	5948	5676
35-44	1833	2410	3052	4136	5266	5873	5878	5713	5498
45-54	1099	1487	1760	2173	3125	4372	5352	5357	5207
55-64	698	906	1149	1361	1746	2666	3956	4843	4847
65+	511	821	1087	1362	1693	2353	3657	3657	3657
			Sou	urce: Bell	et al (2	004)			

Source: Bell et al. (2004)

Table 10: Survival rates κ_t and mortality rates $(1 - \kappa_t)$ in the benchmark cases

		1990	2000	2010	2020	2030	2040
NO AIDS	κ_t	0.827	0.844	0.862	0.881	0.899	0.918
AIDS	κ_t	0.591	0.519	0.541	0.633	0.765	0.842
NO AIDS	$1 - \kappa_t$	0.173	0.156	0.138	0.119	0.101	0.082
AIDS	$1 - \kappa_t$	0.409	0.481	0.459	0.367	0.235	0.158

 κ_t is the probability that an adult in age group a = 3 will survive 20 years, to reach age

group a = 5.

 N_t^1 is derived endogenously in the present model, in contrast to the projections in tables 8 and 9. Yet the implicit survival probabilities underlying these tables are used to compute the number of adults in each age group in future periods, and therefore new age pyramids:

$$N_{t+i}^{1+i} = N_t^1 \cdot (1 - q_t^{1,1+i}), \quad i \ge 1$$
(17)

where $q_t^{1,i}$ is the probability that a member of age group 1 in period t will not survive to become a member of age group 1+i in period t+i. Equation (17) enables the calculation of the diagonals of the population table, namely, values for $N_{t+1}^2, N_{t+2}^3, N_{t+3}^4, \ldots$, starting with N_t^1 , which is endogenous. Those values of the age pyramid which cannot be computed using (17), for example N_9^2 or N_{11}^4 , are taken from table 9.

One last step is necessary before turning to the projections, namely, the determination of N_{min}^1 and N_{max}^1 . As the number of school-going children depends on the number of families, one must define N_{min}^1 and N_{max}^1 relative to family size. We choose N_{min}^1 so as to allow stationarity with respect to population size. As some children and adults always die prematurely, even without an AIDS epidemic, the replacement fertility rate will lie somewhat above 1. In the light of these data, N_{min}^1 is set to

$$N_{min}^{1} = 1.05 \cdot \frac{N_{t}^{2} + N_{t}^{3}}{2} \quad \forall t$$

in every period t. Variations in N_{min}^1 will be discussed in section 6.1. It turns out that the value of N_{max}^1 plays a minor role in all but one variation. Historically, the highest number of children raised (a = 1) per family according to the above definition was 1.91 during the 1980s. Therefore, we choose N_{max}^1 slightly higher, so that $2N_t^1/(N_t^2 + N_t^3) \leq 1.95$ or

$$N_{max}^1 = 1.95 \cdot \frac{N_t^2 + N_t^3}{2} \ \forall t.$$

This implies that, in a steady state, the total population can double within about 20 years if all families choose $N_t^1 = N_{max}^1$. We also assume that the number of children cannot drop from N_{max}^1 to N_{min}^1 within one period. If the family's optimum yields $2N_t^1/(N_t^2 + N_t^3) > (1.95 + 1.05)/2 = 1.5$ in some period t, then the minimum number of children in the following period, t+1, is set to $N_{min}^1 = [1.05/2 + N_t^1/(N_t^2 + N_t^3)] \cdot (N_{t+1}^2 + N_{t+1}^3)/2$ instead of $N_{min}^1 = 1.05(N_{t+1}^2 + N_{t+1}^3)/2$. Only in period t+2 does N_{min}^1 take the restricted value of $N_{min}^1 = 1.05(N_{t+2}^2 + N_{t+2}^3)/2$. Consider, for example, t = 9, where $2N_9^1/(N_9^2 + N_9^3) = 1.87 > 1.5$. This yields, in period t = 10 : $N_{min}^1 = [(1.05 + 1.87)/2] \cdot (N_{10}^2 + N_{10}^3)/2 = 0$

 $1.46 \cdot (N_{10}^2 + N_{10}^3)/2$ instead of $N_{min}^1 = 1.05 \cdot (N_{10}^2 + N_{10}^3)/2$, that is, N_{min}^1 is higher by nearly 40%.

5.1.2 Procedure

For each year, the solution to the household maximization problem, that is, the optimal values of N_t^1 and e_t , is computed. Both interior solutions, i.e. solutions to (14), and a total of 8 corner solutions are calculated in order to find the optimum, including interior solutions with respect to only one variable, that is, solutions in which N_t^1 is at the corner, while e_t solves the corresponding first-order condition in (14), and vice versa. λ_{t+1} and the relevant values of the age pyramid are calculated using (4) and (17), and these values are then used to determine the household optima for the following periods. The projections are limited to 2040.

As noted before, Kenya abolished fees for primary education in 2003, which reduced the costs of schooling by about half. This reduction came surprisingly, as part of a campaign promise of a newly elected government, and it cannot be assumed that parents anticipated it during the 1990s, that is, when they made and implemented their fertility decisions. As a consequence, we will proceed as follows to determine the optimal levels of e_{10} and N_{10}^1 : first, we determine e_{10} and N_{10}^1 assuming that $\sigma_{10} = \sigma_9$. In a second step, we assume that parents observe the abolishment of school fees and revise their decision on e_{10} .

The following sections will discuss the results of the model simulations with the calibration in table 7 in detail. The summary of simulation outcomes with the other calibrations' results are reported in tables 25 to 29 in the appendix.

5.2 The Benchmark Cases

5.2.1 The NO AIDS case

The results for the first benchmark case, that is, the scenario without an HIV/AIDS epidemic, are set out in table 11.

The variable y_t denotes GDP per capita, and is computed from the last two columns. Total population, measured in 1000s, is stated in the last column. With $N_{min}^1 = 0.525(N_t^2 + N_t^3)$, a value of 1.05 in the fourth column of the table indicates a corner solution with respect to N_t^1 . Similarly, a value of 1.46 for t = 10 also denotes a corner solution, as described in section 5.1.1. In the first benchmark case, parents reduce fertility during the 1990s

year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8256	1.46	0.93	1242	3730	30023	26.13
11	6.97	8160	1.13	1.00	1530	5480	35814	26.44
12	8.17	10216	1.32	1.00	1641	7341	44746	26.78
13	9.51	12606	1.44	1.00	1787	9955	55701	27.56
14	11.02	15217	1.39	1.00	2005	13791	68772	28.46

Table 11: Benchmark Case: NO AIDS

sharply, from 1.87 children per family to 1.46 children a decade later. This has two reasons: first, as school fees are abolished, the costs of education are reduced by half, so that parents now increase education. Second, the productivity parameter α_t drops by 19%, from its 1990 value of 1357 to 1104 in 2000.¹⁷ As a consequence, raising children is now relatively more expensive, the value of *b* remaining unchanged, and parents must reduce N_t^1 in order to be able to finance child-raising.¹⁸ By 2010, all children start enjoying full-time schooling, and parents find it worthwhile to invest in having more children once again. As a consequence, N_t^1 , $t \geq 11$ all lie above N_{min}^1 , while $e_t = 1.0 \ \forall t \geq 11$.

5.2.2 Scenario 1: Revision of e_9

The HIV/AIDS epidemic does not (measurably) change the adult population structure for 1990, the first year of interest, as can be seen from tables 8 and 9. It does, however, change the parents' expectations, concerning both future mortality rates and population pyramids. Fewer of them will survive to old age, so that consumption in that phase of life becomes effectively less important than consumption while they are young, as the weight attached to $c_{2,t+2}$, $\beta_1 \kappa_t$, falls. The interior solution is $N_9^1 = 4453$ and $e_9 = 0.70$, that is, parents would like to reduce fertility and increase schooling compared to the NO AIDS case, which, in turn would reduce income from child labor ($4453 \cdot (1 - 0.70) <$ $7182 \cdot (1 - 0.57)$). However, school-children in the 1990s have already been born, so that parents cannot choose N_9^1 as they wish. They can, however, revise their choice of e_9 downwards, which yields $e_9 = 0.42$. Total GDP in 1990 is slightly higher than in the NO AIDS case, due to the increase in child labor. After 1990, the level of schooling grows, albeit slowly. Child labor disappears by 2020, a full decade later that in the NO AIDS

 $^{^{17}}$ The fact that the size of the labor force has also increased reduces the labor productivity – and therefore increases the relative child-raising costs – by another 4%.

¹⁸Note that this result would not hold if the child-raising costs were defined as $N_t^1 b \lambda_t \cdot \alpha_t / \sum_{a=2}^6 N_t^a$ rather than $N_t^1 b \lambda_t$.

case. In the first benchmark case, GDP grows, on average, by 3% annually between 1990 and 2040, and by only 1.7% annually in the AIDS scenario. Total GDP in the NO AIDS case is higher by 90% than in the AIDS case for 2040. Population is always lower with the epidemic, by 40% in 2040. It grows by 2.2% annually on average in the NO AIDS case over the period 1990 – 2040, and by only half that rate in the AIDS case. Compared to the US Bureau's projections in tables 8 and 9, total population in 2040 as predicted by the present model is higher by 22% in the NO AIDS case and by 11% in the AIDS case. Per capita GDP falls between 1990 and 2000 in the NO AIDS benchmark case, due to the

year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8040	1.46	0.57	1186	3434	28944	21.91
11	5.26	7058	1.05	0.91	1352	4163	30799	22.17
12	6.47	6928	1.05	1.00	1484	4817	32464	23.36
13	7.60	7829	1.25	1.00	1583	5655	35717	25.33
14	8.94	9186	1.33	1.00	1754	7268	41445	26.98

Table 12: Scenario 1: AIDS, Revision of e_9

drop in α_t in 2000. After this initial reduction of about 5%, per capita GDP grows in all decades thereafter; however, the growth rate is low – only 1.2% annually, on average. In the AIDS case, y_t is higher in 1990 compared to the NO AIDS case, by about 1%. This is due to the fact that children work more. Per capita GDP falls between 1990 and 2000, and the drop is twice as large as in the NO AIDS case. y_t grows slowly after 2010, and, by 2010, GDP per capita in the AIDS case is no greater than its level in the NO AIDS case. By 2040, per capita GDP in the AIDS case is 12% lower than it would have been if the epidemic had not broken out.

5.2.3 Scenario 2: Delayed Expectations

If households do not realize the outbreak of the epidemic until the late 1990s, they cannot revise their decisions about education, so that $e_9^{Scenario\,2} = e_9^{NOAIDS} = 0.57$. Consequently, λ_{10} is higher than in Scenario 1 (5.67 > 4.97), which has two effects: first, households can produce more, and are therefore richer. Second, education is more profitable, as $z_{10}(N_{10}^2\lambda_{10} + N_{10}^3\lambda_9)/(N_{10}^2 + N_{10}^3)$ is higher.¹⁹ As a consequence, parents can now invest more in education, so that e_t is somewhat higher in scenario 2 in all periods, and full-time

¹⁹Note that N_{10}^2 , N_{10}^3 as well as λ_9 and z_{10} are identical in both scenarios, so that the size of term above is determined by λ_{10} alone.

year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8040	1.46	0.59	1255	3634	28944	22.05
11	5.69	7058	1.05	1.00	1446	4452	30799	22.38
12	7.38	6928	1.05	1.00	1632	5299	32464	23.64
13	8.35	8034	1.28	1.00	1735	6251	36023	25.65
14	9.87	9400	1.35	1.00	1939	8135	41964	27.33

Table 13: Scenario 2: Delayed Expectations

schooling is attained earlier than in the first scenario. Parents being wealthier (higher λ_t), they can also invest more in fertility after 2020, that is, when mortality rates fall. All variables are higher in the second scenario compared to the first (Population by about 1%, GDP by 12%, and GDP per capita and human capital by 10%), but still lower than in the NO AIDS case (Population by 39%, GDP by 41%, GDP per capita by 3%, human capital by 10%).

Therefore, from both an individual²⁰ and an aggregate point of view, scenario 2 yields better results, with a weaker impact of the epidemic, than the first scenario, in which parents revise their decisions about schooling during the 1990s.

6 Variations: Parameters

To test how sensitive the results derived above are to the assumptions made, some variations in the latter will now be presented. The variations will concern the choice of N_{min}^1 , and alternative paths for $\{\sigma_t\}_{t=9,10,\ldots}, \{\alpha_t\}_{t=9,10,\ldots}$ and $\{z_t\}_{t=9,10,\ldots}$. In all variations, it will be assumed that parents perfectly foresee all future changes in parameters, even if they do not immediately foresee the course of the HIV/AIDS epidemic.

6.1 Variation 1: The level of N_{min}^1

The first major assumption concerned the minimum number of children parents can choose to have, which was set by the condition $N_{min}^1 = 1.05 \cdot (N_t^2 + N_t^3)/2$. As a variation, N_{min}^1 is increased slightly, to $N_{min}^1 = 1.1 \cdot (N_t^2 + N_t^3)/2$. The results can be found in table 14. In the NO AIDS case, parents now raise more children than in the benchmark case in all

²⁰The expected levels of utility are also higher in all periods in the second scenario compared to the first.

	NO AIDS									
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47		
10	5.67	8398	1.48	0.91	1235	3734	30239	26.13		
11	6.90	8274	1.13	1.00	1520	5492	36119	26.44		
12	8.13	10250	1.30	1.00	1637	7372	45038	26.76		
13	9.45	12699	1.44	1.00	1777	9970	56102	27.53		
14	10.96	15325	1.39	1.00	1994	13809	69272	28.44		
			AIDS, scena	ario 1: 1	Revision of	e_9				
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35		
10	4.97	8178	1.48	0.56	1179	3437	29155	21.91		
11	5.21	7467	1.10	0.86	1327	4183	31527	22.16		
12	6.28	7533	1.10	1.00	1437	4864	33859	23.34		
13	7.48	8001	1.19	1.00	1574	5823	36982	25.29		
14	8.77	9444	1.30	1.00	1730	7418	42887	26.84		
		AID	OS, scenario	2: Dela	yed Expect	ations				
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47		
10	5.67	8178	1.48	0.58	1248	3638	29155	22.04		
11	5.63	7467	1.10	0.94	1418	4472	31527	22.37		
12	7.15	7533	1.10	1.00	1580	5349	33859	23.62		
13	8.21	8216	1.22	1.00	1724	6431	37302	25.61		
14	9.67	9671	1.32	1.00	1909	8292	43434	27.20		

Table 14: Variation 1: The level of N_{min}^1

years but 1990, but they invest less in schooling; so that the level of efficiency of young adults is somewhat lower in all periods, as is per capita GDP. In 2000, parents choose the minimal level of fertility, and invest in education. By 2010, when children go to school full-time, parents start again to have more children. Total population and GDP are higher in all periods from 2000 onwards, but the difference is small, reaching 0.7% in 2040. The difference in GDP is even smaller, amounting to less than 0.2%.

In the first scenario, wherein parents reconsider their earlier decisions about e_9 when learning about HIV/AIDS, the new value for e_9 chosen remains unchanged, being independent of N_{min}^1 . Compared to the reference case, parents now have more, but worse-educated children until 2020 (see tables 13 and 14), and per capita GDP is lower in all periods. The impact of the epidemic on λ_t and y_t is stronger than in the case where the N_{min}^1 factor is 1.05, as parents can less afford to educate their more numerous children. Its impact on GDP and population, however, is weaker, as parents do not reduce fertility as much when the epidemic breaks out, so that population and GDP do not fall as sharply as in the reference case.

In the second scenario, that is, in the case of delayed expectations, GDP and population are higher than in the reference case (Table 13), as parents have more children from 2000 until 2010. They invest less in education, so that e_t , λ_t and per capita GDP lie below their respective reference values. The effects of the epidemic on GDP and Population, however, are weaker than in the reference case.

6.2 Variation 2: The level of σ_t

The households' decisions on schooling are strongly influenced by the costs of education, σ_t , which were reduced during the 2000s as school fees were abolished. This led to an increase in education, which might have countervailed the effects of the HIV/AIDS epidemic. To disentangle the effects from these two shocks, we will now simulate the household's decisions if school fees had not been abolished. The results are reported in table 15.

In all cases, it takes at least one decade longer to eradicate child labor. The effects are arguably strongest in the first scenario, in which child labor is still present in 2040. When the epidemic breaks out, parents now reduce education much more sharply than they did in the benchmark case: for example, $e_{10} \approx 0.38$ in both scenarios, compared to $e_{10} \approx 0.6$ in the reference cases, which means that children work 50% more. The effects of the epidemic on human capital and GDP per capita are therefore stronger than in the

reference case. For example, in the first scenario, 2040 human capital is lower by about 19% than in the NO AIDS case if school fees are ablosihed, and by 43% if they are not. With schooling being more expensive, parents now prefer to invest in having more children when mortality rates are high. Consequently, population size is higher than in the respective reference cases from 2010 onwards, while the effects of the epidemic on total population are somewhat weaker (see tables 25 and 27).

The reduction of schooling costs contributed strongly to mitigating the effects of the epidemic on all measures but population. Note, however, than an underlying assumption is that, while school fees were abolished, school quality (i.e. z_t) remains unchanged. Schools have to instruct many more pupils,²¹ and loose one important source of funding. Governmental spending on primary education as a share of GDP did not change much either – it actually fell from 7.17% in 2002 to 6.98% in 2003.²² Measured in local currency units, however, public spending on primary education rose sharply from 3322 Million Khs in 2002/2003 to 5967 Million Khs in 2003/2004 - a rise of nearly 80%.²³ To sum up, the assumption that quality of education was unaffected by the abolition of school fees might not hold, and one could expect z_t to have been lower than its calibrated value at least temporatily. However, no data are available allowing us to recalibrate z_t , and the change in the pupil/teacher-ratio as one measure of school quality suggest that it did not change much.

6.3 Variation 3: The level of α_t

The labor productivity factor α_t dropped by 19% in the decade following 1990, from 1357 to 1104, and this reduction is the main reason for the households' decision to reduce fertility from 2000 onwards, even in the absence of the disease – see section 5.2. Assume that α_t recovers after the sharp drop in the 1990s, to some value between α_{10} and α_9 . To be precise, let productivity take the value $\alpha_t = 0.5(\alpha_9 + \alpha_{10})$ after 2000. As in the previous section, it will be assumed that parents foresee changes in α_t perfectly. The results are set out in table 16.

 $^{^{21}}$ According to World Bank Data (WDI 2006), the number of children enrolled in primary education increased by 900000, or 18%, between 2002 and 2003, while the number of teachers increased by 7%. This implies that each teacher had to tutor about 3.5 additional students, on average.

²²Source: Worldbank, WDI 2006

²³Source: Kenya Ministry of Education, http://www.education.go.ke/Statistics/EducationExpenditure.pdf, as of Sept. 22, 2006. The data in the text refers to 'recurring costs'. If development costs are inluded, the rise amounts to nearly 190%.

NO AIDS								
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8256	1.46	0.59	1263	3793	30023	26.03
11	5.69	8662	1.20	0.88	1393	5091	36559	26.05
12	6.96	9413	1.18	1.00	1522	6701	44027	26.34
13	8.14	11294	1.31	1.00	1610	8600	53410	26.91
14	9.52	13317	1.34	1.00	1769	11386	64347	27.83
			AIDS, scena	ario 1:	Revision of	e_9		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8040	1.46	0.37	1199	3471	28944	21.85
11	4.37	7058	1.05	0.54	1279	3939	30799	21.91
12	4.74	7597	1.15	0.62	1245	4166	33453	22.79
13	4.98	9331	1.41	0.67	1176	4540	38604	24.42
14	5.41	10056	1.27	0.81	1226	5494	44798	25.67
		AII	OS, scenario	2: Dela	ayed Expect	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8040	1.46	0.38	1269	3673	28944	21.98
11	4.70	7058	1.05	0.59	1365	4204	30799	22.11
12	5.35	6928	1.05	0.74	1392	4520	32464	23.05
13	5.83	8281	1.32	0.85	1351	4916	36392	24.75
14	6.77	8781	1.24	1.00	1464	6043	41285	26.23

Table 15: Variation 2: The level of σ_t

In the NO AIDS case in 2000, parents would like most to have very few children (as raising them is relatively costly when α_t is low) but to educate these children very well, as future pay-offs from schooling are higher, with α_t expected to rise after 2000. However, due to the social rule on N_{min}^1 each family in 2000 must raise at least 1.46 children, and therefore cannot afford to educate much them above $e_{10}^{base \ case} = 0.93$. Thus, the changes in α_t do not lead to an increase in either N_{10}^1 or e_{10} , as one might expect. By 2010, however, when α_t has recovered substantially, the relative costs incurred in raising children are lower, and parents have more children than in the case of a low level of α_t for t > 10. In all periods following 2010, both total and per capita GDP values are higher than in the benchmark case as α_t is higher.

Human capital levels are equal until at least 2010, and the levels in the variation exceed the levels in the benchmark case after that. Recall that the productivity of education depends on the teachers'/parents' average level of human capital, $(N_t^2 \lambda_t + N_t^3 \lambda_t)/(N_t^2 + N_t^3)$. If there are relatively more young (well-educated) adults in age group a = 2, then the term above will grow, and education will be relatively more productive. Therefore, if parents have more children, and if these children enjoy the same education in both the variation and the benchmark case, the level of human capital of individuals leaving school 2 decades later will be higher. In the present case, $N_{11}^1 = 9996$ in the variation and $N_{11}^1 = 7058$ in the benchmark case. These children finish schooling by 2020, when they become parents themselves, and start teaching N_{12}^1 . This cohort, in turn, finishes school by 2030, and their level of human capital is higher in the variation than in the benchmark case 9.58 > 9.51. This effect can also be observed in the second scenario for λ_{14} .

As a consequence of the increased investment in fertility, total population is now much higher than in all other cases reported, and exceeds the 2040 values projected by the US Bureau of the Census by about 50% and, respectively, 30% in the NO AIDS and AIDS cases. The effects of the epidemic are somewhat stronger than in the benchmark case (see tables 25 and 28), with the differences amounting to max. 4 percentage points.

6.4 Variation 3: The level of z_t

As the adults' choice of e_t is driven, at least in part, by z_t , the last variation presented will address the development of the transmission factor after 2000. Assume that z_t recovers after 1990, and, following Bell et al. (2004), set its value to $z_t = 0.65 \forall t \ge 10$. If parents perfectly foresee this change in the productivity of education, they will raise the level of

			: variation		0 0	2000					
	NO AIDS										
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$			
9	5.29	7182	1.87	0.57	1310	3076	23475	26.61			
10	5.67	8256	1.46	0.93	1242	3730	30023	26.28			
11	6.97	9996	1.38	1.00	1585	6107	38535	26.91			
12	8.17	13000	1.51	1.00	1729	8768	50701	27.46			
13	9.58	16327	1.49	1.00	1932	12695	65718	28.13			
14	11.08	20878	1.48	1.00	2168	18446	85089	28.74			
			AIDS, scena	ario 1: 1	Revision of	e_9					
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$			
9	5.29	7182	1.87	0.42	1324	3107	23475	23.45			
10	4.97	8040	1.46	0.57	1186	3434	28944	22.00			
11	5.26	7058	1.05	1.00	1501	4623	30799	22.55			
12	6.76	7555	1.15	1.00	1634	5457	33390	23.82			
13	7.77	9785	1.49	1.00	1688	6624	39241	25.92			
14	9.21	11788	1.45	1.00	1925	9196	47777	27.51			
		AID	OS, scenario	2: Dela	yed Expect	ations					
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$			
9	5.29	7182	1.87	0.57	1310	3076	23475	26.61			
10	5.67	8040	1.46	0.59	1255	3634	28944	22.14			
11	5.69	7058	1.05	1.00	1611	4962	30799	22.76			
12	7.38	7508	1.14	1.00	1772	5905	33320	24.05			
13	8.35	9992	1.52	1.00	1812	7160	39504	26.17			
14	9.89	12102	1.48	1.00	2069	10017	48404	27.80			

Table 16: Variation 3: Recovery of α_t after 2000

schooling children enjoy during the 1990s, even though z_9 takes a low value; for young adults take into account the education of several future generations when making their decisions, and investing in e_t early is profitable. Therefore, if there is perfect foresight concerning z_t , the results for 1990 will differ from the data. This issue can be solved by assuming either that z_t recovers only later, that is, by 2010, or that parents do not take note of the changes in z_t until they actually take place. To keep matters simple, assume that z_t recovers only late, in 2010, that is: $z_9 = z_{10}$ and $z_{t\geq 11} = 0.65$.

	NO AIDS									
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47		
10	5.67	8256	1.46	0.95	1242	3727	30023	26.20		
11	7.02	8606	1.19	1.00	1506	5495	36475	26.61		
12	9.33	9532	1.20	1.00	1782	7869	44152	27.11		
13	11.70	11345	1.31	1.00	2057	11015	53551	27.96		
14	14.78	13329	1.33	1.00	2468	15913	64479	29.16		
				ario 1:	Revision of	e_9				
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35		
10	4.97	8040	1.46	0.58	1186	3433	28944	21.96		
11	5.29	7058	1.05	1.00	1350	4158	30799	22.27		
12	7.70	6928	1.05	1.00	1590	5162	32464	23.64		
13	9.48	7266	1.16	1.00	1853	6461	34876	25.86		
14	12.24	8121	1.23	1.00	2222	8735	39313	27.72		
		AID		2: Dela	ayed Expect	ations				
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$		
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47		
10	5.67	8040	1.46	0.60	1255	3633	28944	22.10		
11	5.72	7058	1.05	1.00	1449	4462	30799	22.48		
12	8.41	6928	1.05	1.00	1722	5592	32464	23.87		
13	10.22	7402	1.18	1.00	1998	7010	35080	26.12		
14	13.19	8303	1.24	1.00	2403	9543	39717	28.00		

Table 17: Variation 4: Recovery of z_t by 2010

By construction, the results for 1990 remain unchanged compared to the benchmark cases, as z_{11} does not appear in the household's maximization problem when it chooses N_9^1 and e_9 . By 2000, however, parents start taking into account future changes in z_t , and increase education accordingly. Consequently, the adult level of efficiency in 2040 is higher by 34%, while per capita and total GDP are higher by 23% and 15%, respectively compared to the benchmark NO AIDS case.

As expected, the effects of the HIV/AIDS epidemic are slightly weaker than in the case where z_t does not change, as parents invest heavily in education even in the presence of the epidemic. Despite the outbreak of the disease, per capita GDP in 2040 when $z_{t\geq 11} = 0.65$ is higher than in the NO AIDS benchmark case (see table 11), and the difference amounts to about 10-20%. Child labor is now eradicated by 2010 even if parents revise their earlier decisions about e_9 .

7 Policy

Governmental intervention has been necessary, since the outbreak of the HIV/AIDS epidemic in Africa in the 1980s, particularly in the health and education sectors, in order to mitigate its adverse effects. Individuals in developing countries do not have the resources to learn unaided about how the disease is transmitted, and cannot afford the treatment if they become infected. With the number of AIDS orphans estimated to have risen by 30% between 2001 and 2003 alone,²⁴ communities which have taken in orphans in the past are increasingly overwhelmed.

Governmental programs can therefore be classified into three types of measures: preventing the disease from spreading, treating and caring for the ill, and looking after orphans. Preventive measures encompass information campaigns in the media and schools, the distribution of condoms and setting up AIDS test facilities in all affected regions. Before the epidemic breaks out fully, the number of HIV infections typically rises in certain population groups like prostitutes and truck drivers – targeting preventive campaigns at these groups can prove to be highly effective.

After the epidemic breaks out, however, the economy must bear the combined burden of a workforce reduced by illness and death, and the costs of caring for the sick and their families. At this stage, public policies aim at extending the life of the infected through treatment and preventing them from spreading the disease to the healthy. While information campaigns in the media and schools remain important, measures now also consist of

²⁴Source: 'Report on the global AIDS epidemic 2004,' U.N.AIDS, 2004, Page 193

treating HIV-positive pregnant women with drugs to reduce the likelihood of the unborn child also being infected at delivery. With a prevalence rate among Kenyan adults aged 15-49 of 6.7% in 2003,²⁵ that is, more than 1 million AIDS cases to follow, the medical infrastracture needs to be extended, by building additional hospitals and clinics, as well as training and employing more health personnel.

Preventive measures such as information campaigns and condom distribution are relatively cheap – particularly so before a full outbreak of the epidemic, when it is often sufficient to target focus groups. Marseille, Hofmann and Kahn (2002) estimate the costs of prevention at about 8-12 US\$ per case averted. Saving one disability-adjusted-life-year (DALY) through a bundle of measures such as prevention of mother-to-child transmission, supply of condoms for sex workers, control of sexually-transmitted diseases, voluntary counseling and testing as well as blood supply safety, costs an estimated US\$12.50. Treatment costs, for example through highly active antiretroviral therapy (HAART) are much higher: in the developed world, they exceed 10,000 US\$ per patient per year. With the emergence of generic drugs, which are intended for distribution in developing countries only, drug costs amount to 350 US\$ per patient per year. Note, however, that these costs do not include distributing the drugs and payments for medical personnel. As a consequence, Marseille, Hofmann and Kahn estimate the costs of saving a DALY for a cost-effective HAART program to be 395 US\$ per patient yearly.

7.1 Procedure

Intervention in the health sector will aim at reducing mortality rates, both through preventing AIDS from spreading and by treating those who are already ill. In the initial phase of the epidemic, intervention will consist mainly of cost-effective preventive measures. Treatment will gain importance when preventive measures do not bear fruit any more. Denote public spending on health in period t, normalized per sub-family, by G_t , and mortality rates in the presence of the disease (D = 1) by $q_t(D = 1)$. Following Bell et al. (2004), assume the relationship between premature adult mortality in the presence of the disease and public spending on health to be as follows:

$$1 - \kappa_t(G_t; D = 1) \equiv q_t(G_t; D = 1) = d_t - \frac{1}{a_t + c_t e^{-b_t G_t}},$$
(18)

which allows for sufficient curvature (diminishing returns) over a flexible interval. The values of a_t, b_t, c_t and d_t need to be calibrated for each period in which $G_t > 0$. As the

²⁵Source: 'Report on the global AIDS epidemic 2004,' U.N.AIDS, 2004, Page 191

present essay uses the same data as Bell et al. (2004), the results derived there remain valid for present purposes.²⁶ Due to the changes in mortality rates, the population tables

	rabie ie: ille parameter	values of the falletion ql	$(\square_l, \square \square)$
	2000	2010	2020
a_t	0.9073	0.9863	1.3852
b_t	0.0169	0.0187	0.0266
c_t	0.3124	0.3395	0.4768
d_t	1.2152	1.1128	0.8066
	Source:	Bell et al. (2004)	

Table 18: The parameter values of the function $q_t(G_t; D=1)$

need to be recalculated using (18) and table 18. To be able to compute the new values of N_t^a , the public spending program needs to be defined and the age-specific mortality rates $q_t^{a,a+1}$, must be formulated as a function of $q_t(G_t; D = 1)$. For reasons of comparability, the same functional form as in Bell et al. (2004) is chosen. Following Bell et al. (2004), G_t , i.e. the level of spending per family, is defined as:

$$G_t \equiv \frac{P_t}{(N_t^2 + N_t^3 + N_t^4)/2},$$
(19)

with P_t being the level of governmental spending on health. Consider the 30-year spending program:

$$\mathbf{P} = (P_{2000}, P_{2010}, P_{2020}) = (50 \cdot 10^6, 100 \cdot 10^6, 100 \cdot 10^6),$$

where $P_{2000} = 50 \cdot 10^6$ means that 50 million dollars are spent on health every year between 2000 and 2009, and P_{2010} and P_{2020} can be interpreted analogously. Assume that the program **P** is financed through grants from abroad, which are fully funded by international donors. As the grants do not need to be repaid, levying taxes or reshuffling the governmental budget to finance them is not necessary. It is also assumed that the government has no means to extend the program beyond the donors' grants.

The age-specific mortality rates are then defined as follows:

$$q_t^{a,a+1}(G_t; D=1) = q_t^{a,a+1} \cdot \left(1 - \frac{q_t(G_t; D=1)}{q_t(0; D=1)}\right)$$
(20)

As a consequence of the policy program \mathbf{P} , the number of children raised by a family and surviving to old age will now change, and the size of G_t is endogenous because as

²⁶Source: Bell et al. (2004), page 47

Parental decisions are determined in part by their expectations about future mortality rates. In the absence of public spending, parents were assumed to have perfect foresight about mortality rates. To keep matters simple in the case of governmental spending on health, assume parents are more short-sighted: They are aware of the mortality structure if the governmental spending did not take place, and of all future effects of the spending program. However, they do not take into account the effects their own decisions on N_t^1 will have on future values of G_t . Hence, the subjective estimates of κ_t and κ_{t+1} are computed as follows: The current population tables and mortality rates are taken as a basis to calculate G_t from (19) and the new mortality rates $q_t^{a,a+1}(G_t; D = 1)$, from (18) and (20), which, in turn, are used to compute new values for N_t^a from (17) and hence κ_t and κ_{t+1} . All values of N_t^a which are not influenced by the policy program **P** are left unchanged.

7.2 Policy: Results

As the policy program **P** does not affect the NO AIDS case, only the results for the AIDS scenarios are reported. Taking into account the history of policies to deal with AIDS in Kenya, it seems unlikely that households in the 1990s could have foreseen that a program would be implemented in the 2000s. Due to the nature of HIV/AIDS, the effects of such a program on mortality will not make themselves felt immediately, so that it will be assumed that, first, parents during the 1990s do not foresee the program, and second, that even during the 2000s they do not realize its effects, and therefore do not revise their decisions about e_{10} . Young adults in t = 10, however, who decide about N_{11}^1 and e_{11} , realize the programs' effects and make their decisions accordingly. Therefore, even if the government intervenes in the health sector, the outcomes for t = 9 and t = 10 regarding fertility and schooling will remain unchanged. The results are set out in tables 30 to 34 in the appendix. The direct effects of the policy program on the families' decisions can be observed for 2010, that is, the first year in which they react to changes in mortality. Table 19 sets out the adult's level of efficiency in 2010 as well as the qualitative changes in fertility and education: a "+" in the third column states that fertility is higher compared to the case without public spending, a "-" denotes that fertility is lower, and a "0" means that it remains unchanged. The symbols in the last column are interpreted analogously.

As a consequence of the policy program \mathbf{P} , mortality rates are reduced, so that more

1 0		0
λ_t	$rac{N_t^1}{(N_t^2+N_t^3)/2}$	e_t
5.26	0	+
5.69	0	0
5.21	0	+
5.63	0	+
4.37	0	+
4.70	0	+
5.26	+	0
5.69	+	0
5.29	0	0
5.72	0	0
	5.26 5.69 5.21 5.63 4.37 4.70 5.26 5.69 5.29	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

Table 19: The effects of the policy program \mathbf{P} on fertility and education: 2010

Scenario 1: e_9 subject to a binding contract

Scenario 2: e_9 revised by the first group

of the parents will survive to old age. At the same time, more of their children will survive to adulthood and be able to finance their parents in old age. Therefore, consumption in the second stage of adulthood becomes more important in all calculations. To finance it, parents can invest either in education, or in fertility, or in both. Recall that, in most variations and scenarios, parents already choose full-time schooling by 2010. In all cases in which $e_{11}^{G=0} < 1$, parents increase schooling when the policy program is undertaken. Fertility is increased in one case only, namley, if α_t recovers, which also implies a reduction of the relative child-raising costs. The overall effects of the program on λ_t , y_t , Y_t and population will be discussed in detail in section 9.

8 The Effects on Social Welfare

In order to assess the overall effects of the epidemic and the policy program \mathbf{P} , a social welfare function (SWF) is required. The choice of a SWF, however, poses difficulties of its own. It has to capture and value several effects of the epidemic: first, some individuals die prematurely, and are robbed of the opportunity to enjoy their lives and be productive.

Second, some individuals are never born, either because their parents die prematurely or because their parents decide to have fewer children. Third, even those individuals who do not die prematurely often enjoy less schooling than they would have done in the absence of the disease, so that their lifetime income is reduced and their parents' utility from the capacity they attain as adults will fall. There is very little literature on the evolution of welfare when fertility is endogenous. Schweizer (1996) considers an open economy and defines efficiency using the concept of net trade. His welfare measure, however, holds only for economies in a steady state, where population growth is constant over time. As this is not the case in our projections, the measure developed by Schweizer cannot be employed in our framework.

The first step is to decide what unit – monetary or physical – to use. As one of the reasons for introducing a social welfare function is to assess the effects and profitability of the policy program \mathbf{P} , and as the costs of this program are measured in dollars, we will choose a money-metric measure. In general, changes to an individual's level of utility are valued using the concepts of the compensating or equivalent variation (CV and EV), as these capture all individual-level effects described above and assign them a monetary value. The CV measures how much money, in the form of a lumpsum transfer, is required such that and individual's level of utility in the AIDS case with the lump-sum transfer be identical to her level of utility in the NO AIDS case: $U(NO AIDS; \cdot) = U(AIDS, CV > 0; \cdot)$. The EV is the lump-sum an individual is willing to pay in order to avoid the changes in mortality brought about by the HIV/AIDS epidemic and its consequences: $U(NO AIDS, EV < 0; \cdot) = U(AIDS; \cdot)$. The CV and EV measure the effects on individuals. By summing the CV and EV over all relevant individuals²⁷ in some periods, it is possible to assess the overall losses and gains due to the epidemic or an intervention. This aggregation, however, does not include those individuals who are never born, but would have been under other circumstances. The CV and EV can be defined in an analogous way to compute the effects of the policy intervention.

The transfer can be paid or received either in period t, that is, while the children are going to school, or in period t + 2, that is, when the parents reach old age, or in both periods. Note, first, that even though the transfers are lump-sum in form, parents will change N_t^1 and/or e_t . Consider, for example, a family receiving a lump-sum transfer T_t in

 $^{^{27}}$ Aggregating the EV^h over all individuals h rests on the assumption that the marginal utility of income is the same for all individuals. This assumption is easily satisfied within a period, as all individuals are identical. However, the marginal utility of income will be identical between two periods by pure chance only.

period t, and nothing in period t + 2. As there are no capital markets, individuals cannot smooth consumption by saving, and therefore they will change their choice of fertility, schooling or both.²⁸ It is not possible to determine e_t and N_t^1 analytically as functions of the transfer, so that the values of the functions $U(AIDS, CV; \cdot)$ and $U(NO AIDS, EV; \cdot)$ must be determined numerically. In fact, the CV and EV can only be derived using grid search methods,²⁹ which are computationally expensive, as they have to be done separately for each period, variation and scenario.

Note, also, that the CV and EV are likely to differ significantly, as the changes in mortality incurred when the epidemic breaks out are large. The difference stems from the fact that it is not only the the levels of consumption which change, but also the weights of the subutility functions. When computing the CV, we consider the AIDS utility function, when computing the EV, the NO AIDS one. These differ, for instance, in the weight attached to old-age consumption, $\beta_1 \kappa_t$, which is much lower in the case of the CV. Hence, the CV will generally be much larger than the EV as mortality rates rise, and vice-versa.

The EV and CV being hard to compute, we will now turn to other, simpler, measures of welfare. One such measure is income, summed over all relevant individuals and periods. While income measures, to some extent, the utility which accrues to households through its close connection to consumption, it does not measure the utility that arises from the educational attainment of the individual's children (i.e. altruism), and it does not fully measure the disutility arising from premature mortality. The contribution of the altruism term to an individual's level of utility is less than 2% in all years, scenarios and variations analyzed; consumption, especially its distribution over time, and the parents' expectations about mortality determine the rest. Therefore, the major drawback of using income as a measure of welfare is that is does not fully capture the losses and gains arising from changes in mortality rates. If these changes are small, income can be used as an easy to compute measure of welfare.

²⁸This argument also holds if parents receive the transfer when they are old, as borrowing is not possible. While it is possible that there will exist a tuple of transfers T_t, T_{t+2} for which fertility and schooling both remain unchanged, it is very unlikely that these transfers will correspond to a CV or EV

²⁹The procedure, in the case of the EV, is as follows: First, compute the levels of utility attained in the AIDS case. Second, use the NO AIDS utility function to calculate the optimal levels of fertility and education for each transfer T, and the ensuing level of utility. Third, choose that level of T for which utility in the NO AIDS case with the transfer is equal to the level of utility in the AIDS case without the transfer. Steps two and three must be done separately for every year. The procedure in the case of the CV is similar. Both the EV and CV can be calculated analogously when evaluating the policy program **P**.

The results, however, require careful interpretation, for they depend on whether per capita or total income (GDP) is used. Total income can rise in two ways: either the number of individuals rises, while income per head is constant, or the income of each individual rises while the number of individuals remains constant. If parents decide to reduce schooling while increasing fertility, per capita income will be lower – suggesting that individuals might be worse off – while total income might rise – suggesting that an economy-wide indicator has improved. If such a tradeoff does not exist, as is the case when the HIV/AIDS epidemic first breaks out,³⁰ both income per capita and total GDP are arguably acceptable measures of welfare. In the case of the policy program P, however, such tradeoffs are frequent, in some cases per capita GDP falls while total GDP (and population) rise. Therefore, when per capita GDP is the measure of welfare, the policy program seems to have negative consequences. If total GDP is used instead, the program has positive consequences. Which measure, then, is better? Note that when the extended lifetime under the program is taken into consideration, the apparent negative effect of the program measured using per capita GDP dissapears. Consequently, both per capita income and total income can be used to measure the welfare losses incurred when the HIV/AIDS epidemic breaks out and the gains from the program.

One last aspect needs to be discussed, namely, the treatment of those individuals who are born under one program but not under another. The valuation of such individuals and their lives is the issue of a lively discussion in both philosophy and economics, and there is no commonly accepted method or procedure. Most authors who are concerned with AIDS, for instance, Young (2005), do not take such individuals into account. Note that whatever individual measure of welfare is chosen – CV, EV or per capita income – it has to be summed up over all households/individuals who experience the losses and gains in order to capture the full effects to be analyzed. Consider, for instance, the effects of the HIV/AIDS epidemic. When only those individuals who actually lived at some point of time are considered, the losses are underestimated: if there had been no epidemic, parents would have had more and better-educated children, whose hypothetical income and lives involve losses which need to be taken into account when measuring the effects of HIV/AIDS.

In the present paper, we need to estimate the effects of the HIV/ADS epidemic in the ab-

³⁰Both per capita and total GDP are higher in the NO AIDS case compared to either AIDS scenario. The single exception is the period t = 10, in which per capita GDP in the presence of the disease is somewhat higher than in its absence due to a rise in child labor. As the difference amounts to less than 1% in all cases, we will ignore this problem for the rest of the welfare analysis.

sence of the intervention, when there is no tradeoff, and the effects of the policy program **P**, when there is. Two measures of welfare will be employed, both of them based on individual incomes: first, a measure in which unborn individuals are taken into account, and second, one in which they are not. To compute the first measure, we calculate the income, in every period, of every individual alive in that period in the presence of the intervention or shock, and compare it to the total income of every individual in the absence of the intervention/shock. As the income of all individuals in some period is simply the total GDP of that period, the first method compares GDP levels. As argued before, this method is more appropriate when there is no tradeoff between schooling and fertility, that is, when comparing the NO AIDS and AIDS cases. To compute the second measure, we calculate the number of people who have died prematurely, or will do so, because of HIV/AIDS (or, respectively, who would have died if there had been no policy intervention), and assess their lost earnings. This step is somewhat more complicated than computing premature deaths. The simplest way of doing it is to assume that, even if the mortality rates had been different, these individuals would have enjoyed the same education, so that their level of human capital would remain unchanged. In this case, their lost earnings would be $\alpha_t \lambda^a$ for each adult in each decade, where λ^a denotes her level of human capital. It is also possible, however, that the individual would have enjoyed more schooling, and hence a higher level of human capital, if mortality rates had been lower, and vice versa. As it is not possible to compute this hypothetical level of schooling, we will simply assume that λ_t and e_t take the same value as in the case without the HIV/AIDS mortality shock or the governmental intervention, as appropriate. Therefore, when computing the (monetary) losses, we will make two assumptions:

- (A1) The fact that some potential children will never be born as a consequence of HIV/AIDS will be ignored
- (A2) The level of human capital attained by all children will be either
 - (A2a) the same level as in the case where the shock/intervention takes place.
 - (A2b) the same level as in the case where the shock/intervention does not takes place

For all measures employed, we compute the 1990 net present value (NPV) of all losses and gains, and compare it either to the 1990 NPV of total, NO AIDS GDP, or to the 1990 NPV of the cost of the policy intervention \mathbf{P} , to assess the effects of the epidemic or the social profitability of the policy program. In all cases, the calculations are limited to the years 1990 to 2040, so that gains and losses which accrue after 2040 are not included.

9 Results

The effects of the HIV/AIDS epidemic and the policy program \mathbf{P} are discussed in sections 9.1 and 9.2 respectively. We will first present changes in some basic measures of welfare, namely, the adults' level of human capital, λ_t , per capita income, y_t , total GDP, Y_t and population in the last period of the projections (t = 14). Second, we will determine the overall effects of the epidemic and the intervention using the procedures described above.

9.1 No public spending on health

The effects of the HIV/AIDS epidemic on the Kenyan people and economy are substantial, but they also depend on the way households react. The average³¹ levels of several simple measures of welfare as a percentage of their respective NO AIDS levels for the year 2040 are set out in tables 25 - 29 in the appendix, as well as in table 20 below. Figure 2 contains the levels of three measures relative to their NO AIDS levels, for all calibrations. While λ and y describe welfare at the individual level, GDP and population are aggregate measures. The effects of the epidemic on λ , per capita GDP and total GDP are strongest in the case where e_9 is revised in 1990, that is, in the first scenario. The impact of HIV/AIDS on GDP is a heavy one: it is lower by at least 34% in all cases, and up to 55% in the second variation. The effect of the HIV/AIDS epidemic on human capital and per capita GDP is by far strongest in the second variation, in which it is assumed that school fees are not abolished. In that case, parents reduce education sharply as the epidemic breaks out, and child labor persists at least until 2030. This variation is also the only case in which the effects of the epidemic on 2040 population are stronger in the second scenario compared to the first. With education being very expensive, and parents being comparatively poor in the first scenario, they prefer to invest in fertility (as opposed to schooling). As a consequence, total population is not reduced by as much in the first scenario as it is in the second, in which fertility is always lower, and education higher.

In the light of the results above, it is obvious that the abolition of school fees strongly mitigated the effects of the epidemic on all welfare measures, with the exception of total population, in both scenarios. The results of the other variations depart only slightly from those of the benchmark cases, with the differences amounting to no more than 4 percentage points, compared to 4 - 23 percentage points in the second variation.

The overall effects of the epidemic are set out in tables 21 and 22. Table 21 gives the 1990

 $^{^{31}}$ The levels reported in the tables refer to average effects for all 27 calibrations

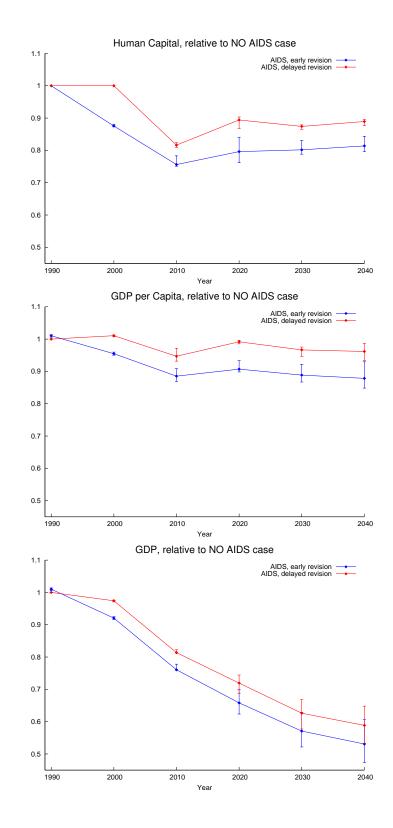


Figure 2: The effects of the HIV/AIDS epidemic expressed as a % of the NO AIDS levels, all calibrations

The bars denote the maximum/minimum values the ratio can take over all calibrations.

	λ	GDP per cap.	GDP Y	Population
		y		
Base Case				
Scenario 1	81	88	53	60
Scenario 2	89	96	59	61
Variation 1 (N_{min}^1)				
Scenario 1	80	87	54	62
Scenario 2	88	96	60	63
Variation 2 $(\sigma_{t\geq 10})$				
Scenario 1	58	70	49	70
Scenario 2	72	83	54	64
Variation 3 ($\alpha_{t\geq 10}$)				
Scenario 1	83	89	50	57
Scenario 2	89	96	55	57
Variation 4 $(z_{t\geq 11})$				
Scenario 1	82	90	55	61
Scenario 2	89	97	60	62

Table 20: The effects of the HIV/AIDS epidemic expressed as a % of the NO AIDS levels in 2040. Average Values

Scenario 1: Revision of e_9

Scenario 2: Delayed Expectations

NPV of the overall losses as a fraction of the 1990 NPV of total NO AIDS GDP when unborn individuals are taken into account, for the base case. The variations are reported in the appendix.

Table 21: Lost income through premature adult mortality, including unborn individuals

Interest Rate	Scenario 1^a	Scenario 2^b
0.0% p.a.	31	26
1.2% p.a.	29	24
5.0% p.a.	21	17

^{*a*} Renegotiation of e_9

 b Delayed Expectations

Average values over all calibrations are reported. All values expressed as a % of the 1990 NPV of total NO AIDS GDP between 1990 and 2040.

Interest Rate	Scena	trio 1^a	Scena	ario 2^b
	(A2a)	(A2b)	(A2a)	(A2b)
0.0% p.a.	11	24	12	19
0.7% p.a.	10	22	11	18
5.0% p.a.	8	18	9	14

Table 22: Lost income through premature adult mortality, excluding unborn individuals

^{*a*} Renegotiation of e_9

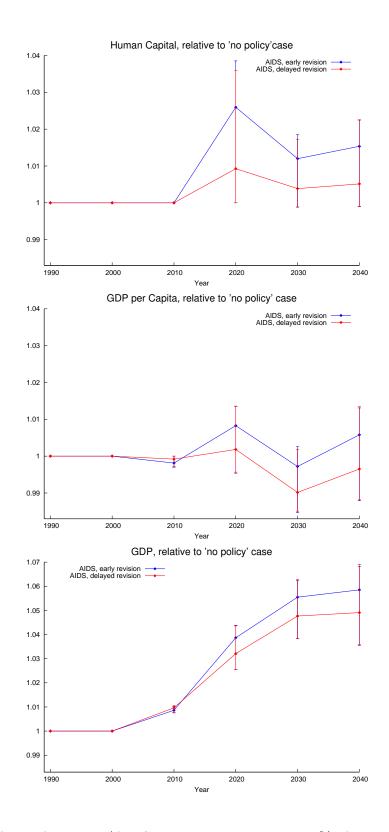
^b Delayed Expectations

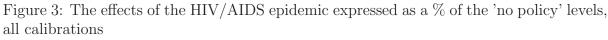
All values expressed as a % of the 1990 NPV of total NO AIDS GDP between 1990 and 2040

Table 22 gives the 1990 net present value (NPV) of the loss of income incurred through premature adult mortality as a fraction of the NPV of total GDP in the period 1990-2040, when unborn individuals are ignored, using assumptions (A2a) or (A2b). Three different annual rates of interest are considered: first, r = 0; second, r = 0.7%, which corresponds to the families' own pure discount rate, as computed from β_0 and β_1 ; and third, r = 5%, which is the interest rate employed in Bell et. al (2004). As expected, the effects of the epidemic are stronger under assumption (A2b), as the levels of lost income per capita are higher in that case. Whichever scenario is chosen the effects of the epidemic range from 8% to 12% of total GDP under assumption (A2a), and 5 to 13 percentage points more under (A2b). Even when the incomes of unborn individuals are ignored, therefore, the society suffers significant economic losses when HIV/AIDS breaks out.

9.2 Public Spending on Health

The effects of the program **P**, expressed as a % of the 2040 NO AIDS level, are set out in table 23. Figure 3 describes three welfare measures relative to their respective levels in the absence of the policy program, for all calibrations. In all variations, all measures of aggregate welfare are higher if the program is undertaken. The results for individual measures of welfare, however, are mixed: they are negative in some cases. To illustrate the changes induced by the policy program **P**, consider the second scenario of the base case, the results of which are reported in table 13 the lower half of table 30. Note that the level of human capital after 2030 in the presence of the program is somewhat lower than in its absence (8.349<8.355), although the levels of schooling are identical in all periods. Recall that the level of human capital of a young adult depends on three variables: first, the quality of schooling (z_t) , second, the amount of time she spends at school (e_t) , and, third, the average level of human capital of her parents/teachers $\left(\frac{N_t^2 \lambda_t + N_t^3 \lambda_{t-1}}{N_t^2 + N_t^3}\right)$. The pol-





The bars denote the maximum/minimum values the ratio can take over all calibrations.

	λ	per capita	GDP Y	Population
		GDP y		
Base Case				
Scenario 1	1.5	0.6	5.8	5.2
Scenario 2	0.5	-0.4	4.9	5.3
Variation 1 (N_{min})				
Scenario 1	2.0	1.1	6.2	5.0
Scenario 2	1.2	0.3	5.4	5.1
Variation 2 $(\sigma_{t\geq 10})$				
Scenario 1	5.3	3.4	6.7	3.2
Scenario 2	5.7	3.3	7.2	3.8
Variation 3 ($\alpha_{t\geq 10}$)				
Scenario 1	0.2	-0.4	7.2	7.7
Scenario 2	0.1	-0.5	7.3	7.8
Variation 3 $(z_{t\geq 11})$				
Scenario 1	0.4	-0.6	4.5	5.1
Scenario 2	-0.1	-1.0	4.1	5.2

Table 23: The average effects of the public spending program \mathbf{P} , expressed as a percentage of the NO AIDS levels in 2040

Scenario 1: e_9 subject to a binding contract

Scenario 2: e_9 revised by the first group

icy program \mathbf{P} does not change either z_t nor e_t – it does, however, change $\frac{N_t^2 \lambda_t + N_t^3 \lambda_{t-1}}{N_t^2 + N_t^3}$: more adults in age group a = 3 survive, so that the ratio of young, well-educated (a = 2)parents to older parents (a = 3) shifts, thereby reducing the average level of human capital of the teachers. The factor $\frac{N_t^2 \lambda_t + N_t^3 \lambda_{t-1}}{N_t^2 + N_t^3}$, which determines λ_{13} , is 7.893 if the program is undertaken, and 7.898 otherwise, and, consequently, λ_{13} is 8.349 in the presence of the program, and 8.355 in its absence. With human capital being lower when \mathbf{P} is undertaken, the program can also have a negative impact on GDP per capita. In this case, another effect of the program also plays a role: with mortality rates reduced, parents assume that more of their children survive. As they cannot invest more in education – all children already enjoy full-time schooling – they have more children: for example, in the case mentioned before, each family has 1.28 children in 2030 in the absence of the program, and 1.32 in its presence. Consequently, the total population is higher, which reduces GDP per capita. As both effects can only be observed if schooling cannot be increased through the policy program, neither of them appears in the case where school fees are not abolished (Variation 2): here, the policy program leads to an increase in schooling, and its effects are strong and positive with respect to all measures of welfare. To sum up, the policy program \mathbf{P} can have negative effects on individual measures of welfare as is shifts the structure of population, and thereby influences the intergenerational transfer of human capital. Note, however, that the negative effects are generally small, and amount to no more than 1.3%. Recall also that mortality rates are reduced in the presence of the program, thereby extending life expectancy and therefore also the expected lifetime income. As a consequnce, the overall effect of the program on individuals might be positive even if per capita GDP is somewhat lower.

To assess the social profitability of the program \mathbf{P} , we employ the methods presented in section 8. Tables 40 and 41 in the appendix report the results when unborn individuals are, and are not, considered, respectively. Assumption (A2) from section 8 now reads as follows:

(A2) The level of human capital attained by all children will be either

- $(A2\hat{a})$ the same level as in the AIDS case with a policy program.
- (A2b) the same level as in the AIDS case without a policy program.

Note that the levels of schooling and human capital are generally higher in the case of Assumption (A2 \hat{a}), so that the effects of the policy program **P** will also be higher in that case.

Even though in some cases the levels of human capital and GDP per capita were lower in the presence of the program than in its absence (see table 23), the program is always profitable, as people live longer. This effect strongly dominates the small reductions in human capital in all cases. Consequently, the discounted gains are at least three times as high as the discounted costs, so that the program is very profitable indeed. Note also that when computing the values in tables 40 and 41, we did not take into account the program's gains which accrue after 2040. More recent evidence suggests that the costs of saving a DALY through HAART might be lower than those employed in the present essay – in this case, the policy program would be even more profitable, as it saves and prolongs more lives.

10 Conclusion

The HIV/AIDS epidemic in Kenya has had, and continues to have, a very damaging impact on the country's economy and population, both at the individual and at the aggregate level. Four factors play a major role in determining the long-term dynamics. First, there is the drop in the inter-generational transmission factor after 1970, which leads to a direct reduction in the formation of human capital and to levels of schooling. Second there is the reduction in labor productivity during the 1990s, as a consequence of which, fertility and total population both fall. Third, there is the increase in mortality rates after the full outbreak of the HIV/AIDS epidemic. Fourth, there is the reduction in education costs during the 2000s. The individuals' reaction to the epidemic depends, first, on when they realize its effects, and second on the social mechanisms governing the way exogenous shocks are dealt with. As has been argued in this essay, changes in the inter-generational transmission factor and the labor productivity factor can mitigate or intensify the epidemic's consequences. Similarly, measures aimed at changing N_{min}^1 can also form part of an anti-AIDS program.

The policy program called \mathbf{P} , which is fully financed by foreign grants, has a positive effect on all aggregate-level welfare measures. In reaction to \mathbf{P} , parents normally increase the level of schooling their children enjoy, and therefore their future income and per capita GDP. Combining \mathbf{P} with measures aimed at influencing N_{min}^1 , α_t and/or z_t , can further mitigate the effects of the epidemic. Note, however, that comparing \mathbf{P} with the other measures discussed in the variations is difficult, as the costs incurred in implementing the changes in the latter are unknown. The gains which accrue if \mathbf{P} is undertaken outweigh many-fold the costs incurred in financing it, even if the overall returns to this investment that occur after 2040 are left out of account.

11 Appendix

I	able 24: Calibration Res	suits: Averages	
A = 0.170(0.03)	$\epsilon = 0.53(0.003)$	$\eta = 1.444(0.41)$	
$\mu = 0.535(0.055)$	$\chi = 0.129(0.029)$	b =	
		282.69(24.85)	
$\beta_0 = 1.7388(0.3968)$	$\beta_1 = 1.5057(0.3444)$		
t	λ_t	z_t	α_t
2	1.01 (0)	$1.6861 \ (0.066)$	_
3	1.6714(0.023)	1.6961 (0.066)	_
4	2.2258(0.054)	1.0198 (0.019)	_
5	2.3984(0.050)	1.0198 (0.019)	1417 (303)
6	3.0289(0.078)	1.0198 (0.019)	1417 (303)
7	4.3109 (0.135)	1.0198 (0.019)	1417 (303)
8	6.1433 (0.240)	0.5631 (0.017)	1417 (303)
9	5.3279(0.286)	0.5631 (0.017)	1417 (303)
10	5.7249(0.365)	0.5631 (0.017)	1152 (244)
	Standard Doviation in	naronthogog	

Table 24: Calibration Results: Averages

Standard Deviation in parentheses.

	, on on one of the	Cabob	
e_9	Average	Min.	Max.
NO AIDS	1.22	1.10	1.36
AIDS	1.11	1.08	1.15
Population	0.60	0.56	0.65
GDP	0.53	0.47	0.61
GDP per capita	0.88	0.85	0.93
Human Capital	0.81	0.80	0.84
ions	Average	Min.	Max.
NO AIDS	1.22	1.10	1.36
AIDS	1.12	1.09	1.18
Population	0.61	0.57	0.66
GDP	0.59	0.53	0.65
GDP per capita	0.96	0.93	0.99
1 1			
	e9NO AIDSAIDSPopulationGDPGDP per capitaHuman CapitalionsNO AIDSAIDSPopulationGDP	NO AIDS1.22AIDS1.11Population0.60GDP0.53GDP per capita0.88Human Capital0.81ionsAverageNO AIDS1.22AIDS1.12Population0.61GDP0.59	e_9 AverageMin.NO AIDS 1.22 1.10 AIDS 1.12 1.10 AIDS 1.11 1.08 Population 0.60 0.56 GDP 0.53 0.47 GDP per capita 0.88 0.85 Human Capital 0.81 0.80 ionsAverageMin.NO AIDS 1.22 1.10 AIDS 1.12 1.09 Population 0.61 0.57 GDP 0.59 0.53

Table 25: Summary of results, all calibrations: The Benchmark Cases

 \overline{a} Ratio of total 2040 population in the simulations to total 2040 population in the US Bureau of Census data, as reported in tables 8 and 9 respectively. $b \frac{Population_{t=14}^{AIDS}}{Population_{t=14}^{NO,AIDS}}, \frac{Y_{t=14}^{AIDS}}{Y_{t=14}^{NO,AIDS}}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{NO,AIDS}}, \frac{\lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{NO,AIDS}}$

s, an camprations.	variation	L	
e_9	Average	Min.	Max.
NO AIDS	1.23	1.11	1.37
AIDS	1.15	1.12	1.19
Population	0.62	0.57	0.67
GDP	0.54	0.48	0.63
GDP per capita	0.87	0.84	0.94
Human Capital	0.80	0.79	0.85
tions	Average	Min.	Max.
NO AIDS	1.23	1.11	1.37
AIDS	1.16	1.13	1.22
Population	0.63	0.59	0.67
GDP	0.60	0.54	0.67
GDP per capita	0.96	0.93	0.99
Human Capital	0.88	0.87	0.90
	e9NO AIDSAIDSPopulationGDPGDP per capitaHuman CapitalionsNO AIDSAIDSPopulationGDPGDP per capita	e_9 AverageNO AIDS1.23AIDS1.15Population0.62GDP0.54GDP per capita0.87Human Capital0.80ionsAverageNO AIDS1.23AIDS1.16Population0.63GDP0.60GDPper capita0.96	NO AIDS 1.23 1.11 AIDS 1.15 1.12 Population 0.62 0.57 GDP 0.54 0.48 GDP per capita 0.87 0.84 Human Capital 0.80 0.79 ions Average Min. NO AIDS 1.23 1.11 AIDS 1.23 0.59 GDP 0.60 0.54

Table 26: Summary of results, all calibrations: Variation 1

^a Ratio of total 2040 population in the simulations to total 2040 population in the US Bureau of Census data, as reported in tables 8 and 9 respectively. $b \frac{Population_{t=14}^{AIDS}}{Population_{t=14}^{NO, AIDS}}, \frac{Y_{t=14}^{AIDS}}{Y_{t=14}^{NO, AIDS}}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{NO, AIDS}}, \frac{\lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{NO, AIDS}}$

rabio 21. Summary of results	, all callorations.	variation 2	-	
Scenario 1: Renegotiation of	e_9	Average	Min.	Max.
Deviation from census data (2040) a	NO AIDS	1.14	1.09	1.23
	AIDS	1.20	1.13	1.31
Effect of the HIV/AIDS epidemic $(2040)^b$	Population	0.70	0.68	0.71
	GDP	0.49	0.47	0.55
	GDP per capita	0.70	0.66	0.79
	Human Capital	0.58	0.54	0.67
Scenario 2: Delayed Expectat	ions	Average	Min.	Max.
Deviation from census data (2040) a	NO AIDS	1.14	1.09	1.23
	AIDS	1.11	1.06	1.18
Effect of the HIV/AIDS epidemic $(2040)^b$	Population	0.64	0.63	0.68
	GDP	0.54	0.50	0.60
	GDP per capita	0.83	0.79	0.89
	Human Capital	0.72	0.68	0.78

Table 27: Summary of results, all calibrations: Variation 2

 \overline{a} Ratio of total 2040 population in the simulations to total 2040 population in the US Bureau of Census data, as reported in tables 8 and 9 respectively. $b \frac{Population_{t=14}^{AIDS}}{Population_{t=14}^{NO, AIDS}}, \frac{Y_{t=14}^{AIDS}}{Y_{t=14}^{NO, AIDS}}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{NO, AIDS}}, \frac{\lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{NO, AIDS}}$

s, an campradions.	variation e	-	
e_9	Average	Min.	Max.
NO AIDS	1.50	1.32	1.71
AIDS	1.29	1.25	1.37
Population	0.57	0.53	0.65
GDP	0.50	0.45	0.60
GDP per capita	0.89	0.86	0.92
Human Capital	0.83	0.81	0.84
ions	Average	Min.	Max.
NO AIDS	1.50	1.32	1.71
AIDS	1.30	1.26	1.37
THE	1.00	1.20	1.01
Population	0.57	0.53	0.65
Population	0.57	0.53	0.65
	NO AIDS AIDS Population GDP GDP per capita Human Capital ions NO AIDS	NO AIDS1.50AIDS1.29Population0.57GDP0.50GDP per capita0.89Human Capital0.83ionsAverageNO AIDS1.50	NO AIDS 1.50 1.32 AIDS 1.29 1.25 Population 0.57 0.53 GDP 0.50 0.45 GDP per capita 0.89 0.86 Human Capital 0.83 0.81 ions Average Min. NO AIDS 1.50 1.32

Table 28: Summary of results, all calibrations: Variation 3

 \overline{a} Ratio of total 2040 population in the simulations to total 2040 population in the US Bureau of Census data, as reported in tables 8 and 9 respectively. $b \frac{Population_{t=14}^{AIDS}}{Population_{t=14}^{NO}AIDS}, \frac{Y_{t=14}^{AIDS}}{Y_{t=14}^{NO}AIDS}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{NO}AIDS}, \frac{\lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{NO}AIDS}$

Table 29. Summary of results	s, an camprations.	variation	L	
Scenario 1: Renegotiation of	e_9	Average	Min.	Max.
Deviation from census data (2040) a	NO AIDS	1.14	1.06	1.30
	AIDS	1.06	1.03	1.11
Effect of the HIV/AIDS epidemic $(2040)^b$	Population	0.61	0.56	0.66
	GDP	0.55	0.49	0.62
	GDP per capita	0.90	0.86	0.94
	Human Capital	0.82	0.81	0.84
	1			
Scenario 2: Delayed Expectat	Ĩ	Average	Min.	Max.
Scenario 2: Delayed Expectat Deviation from census data (2040) a	Ĩ	Average 1.14		
v 1	tions	<u> </u>	Min.	Max.
v 1	ions NO AIDS	1.14	Min. 1.06	Max. 1.30
Deviation from census data $(2040)^{a}$	ions NO AIDS AIDS	1.14 1.07	Min. 1.06 1.04	Max. 1.30 1.12
Deviation from census data $(2040)^{a}$	ions NO AIDS AIDS Population	$ 1.14 \\ 1.07 \\ 0.62 $	Min. 1.06 1.04 0.57	Max. 1.30 1.12 0.66

Table 29: Summary of results, all calibrations: Variation 4

a Ratio of total 2040 population in the simulations to total 2040 population in the US Bureau of Census data, as reported in tables 8 and 9 respectively. ^b $\frac{\text{Population}_{t=14}^{AIDS}}{\text{Population}_{t=14}^{NO AIDS}}, \frac{Y_{t=14}^{AIDS}}{Y_{t=14}^{NO AIDS}}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{NO AIDS}}, \frac{\lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{NO AIDS}}$

Table 30: The Policy Program **P**: Benchmark Case

			AIDS, Scena	ario 1:	Revision of	e_9		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8040	1.46	0.57	1186	3434	28944	21.91
11	5.26	7107	1.05	0.98	1348	4196	31122	22.76
12	6.71	7055	1.05	1.00	1502	5025	33445	23.73
13	7.73	8295	1.29	1.00	1587	6000	37814	25.40
14	9.14	9573	1.33	1.00	1776	7744	43602	27.09
		AID	OS, scenario	2: Dela	yed Expects	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8040	1.46	0.59	1255	3634	28944	22.05
11	5.69	7107	1.05	1.00	1446	4499	31122	22.98
12	7.38	7055	1.05	1.00	1630	5451	33445	23.98
13	8.35	8496	1.32	1.00	1711	6523	38113	25.67
14	9.86	9840	1.35	1.00	1922	8493	44195	27.38

			AIDS, Scena	ario 1:	Revision of	e_9	<u> </u>	
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8178	1.48	0.56	1179	3437	29155	21.91
11	5.21	7518	1.10	0.93	1324	4216	31854	22.75
12	6.51	7670	1.10	1.00	1455	5072	34857	23.70
13	7.61	8466	1.22	1.00	1579	6170	39085	25.36
14	8.97	9834	1.30	1.00	1751	7890	45055	26.95
		AID	OS, scenario	2: Dela	yed Expects	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8178	1.48	0.58	1248	3638	29155	22.04
11	5.63	7518	1.10	1.00	1416	4509	31854	22.96
12	7.34	7670	1.10	1.00	1594	5557	34857	23.97
13	8.32	8681	1.25	1.00	1722	6785	39407	25.66
14	9.83	10077	1.32	1.00	1923	8775	45626	27.29

Table 31: The Policy Program **P**: Variation 1: The level of N_{min}^1

Table 32: The Policy Program **P**: Variation 2: Abolition of school fees

			AIDS, scena	ario 1: 1	Revision of	ε_9		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8040	1.46	0.37	1199	3471	28944	21.85
11	4.37	7107	1.05	0.58	1278	3977	31122	22.48
12	4.89	7684	1.14	0.66	1261	4335	34375	23.15
13	5.19	9517	1.41	0.71	1202	4838	40248	24.51
14	5.72	9968	1.24	0.89	1274	5854	45942	25.83
		AID	,	2: Dela	yed Expects	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8040	1.46	0.38	1269	3673	28944	21.98
11	4.70	7107	1.05	0.64	1363	4243	31122	22.69
12	5.54	7055	1.05	0.79	1407	4707	33445	23.41
13	6.07	8455	1.31	0.90	1381	5253	38052	24.85
14	7.19	8940	1.23	1.00	1515	6488	42819	26.39

		AID	DS, scenario	2: Dela	yed Expect	ations	· · · · · · · · · · · · · · · · · · ·	
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.45
10	4.97	8040	1.46	0.57	1186	3434	28944	22.00
11	5.26	7494	1.11	1.00	1475	4673	31687	23.15
12	6.76	8127	1.18	1.00	1615	5719	35401	24.19
13	7.78	10463	1.47	1.00	1683	7136	42406	25.94
14	9.22	12559	1.44	1.00	1916	9844	51376	27.50
		AID	OS, scenario	2: Dela	yed Expect	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.61
10	5.67	8040	1.46	0.59	1255	3634	28944	22.14
11	5.69	7551	1.12	1.00	1578	5014	31770	23.37
12	7.38	8088	1.17	1.00	1753	6205	35397	24.43
13	8.38	10690	1.50	1.00	1809	7734	42754	26.19
14	9.90	12922	1.47	1.00	2060	10743	52140	27.78

Table 33: The Policy Program **P**: Variation 3: Recovery of α_t

Table 34: The Policy Program **P**: Variation 4: Recovery of z_t

		AID	DS, scenario	2: Dela	yed Expects	ations	, , , , , , , , , , , , , , , , , , , ,	
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.42	1324	3107	23475	23.35
10	4.97	8040	1.46	0.58	1186	3433	28944	21.96
11	5.29	7107	1.05	1.00	1351	4203	31122	22.87
12	7.69	7055	1.05	1.00	1586	5306	33445	23.97
13	9.46	7650	1.19	1.00	1825	6726	36851	25.86
14	12.22	8479	1.23	1.00	2199	9091	41348	27.76
		AID	OS, scenario	2: Dela	yed Expects	ations		
year t	λ_t	N_t^1	$\frac{N_t^1}{(N_t^2 + N_t^3)/2}$	e_t	y_t	$Y_t(10^7)$	Pop.	$E_t U$
9	5.29	7182	1.87	0.57	1310	3076	23475	26.47
10	5.67	8040	1.46	0.60	1255	3633	28944	22.10
11	5.72	7107	1.05	1.00	1449	4509	31122	23.09
12	8.41	7055	1.05	1.00	1718	5747	33445	24.21
13	10.21	7794	1.21	1.00	1969	7297	37066	26.12
14	13.18	8672	1.25	1.00	2378	9935	41774	28.04

Scenario 1: Renegotiation	of e_9	Average	Min.	Max.			
Effect of the Policy Program \mathbf{P} (2040) ^{<i>a</i>}	Population	5.2	4.8	5.6			
	GDP	5.8	3.5	6.8			
	GDP per Capita	0.6	-1.2	1.3			
	Human Capital	1.5	-0.1	2.3			
Scenario 2: Delayed Expecta	Average	Min.	Max.				
Effect of the Policy Program \mathbf{P} (2040) ^{<i>a</i>}	Population	5.3	4.8	5.6			
	GDP	4.9	3.6	6.9			
	GDP per Capita	-0.4	-1.2	1.3			
	Human Capital	0.5	-0.1	2.2			
$ \frac{Population_{t=14}^{AIDS, \mathbf{P}} - Population_{t=14}^{AIDS}}{Population_{t=14}^{AIDS}}, \frac{Y_{t=14}^{AIDS, \mathbf{P}} - Y_{t=14}^{AIDS}}{Y_{t=14}^{AIDS}}, \frac{y_{t=14}^{AIDS, \mathbf{P}} - y_{t=14}^{AIDS}}{y_{t=14}^{AIDS}}, \frac{\lambda_{t=14}^{AIDS, \mathbf{P}} - \lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{AIDS}}. $							

Table 35: The effects of ${\bf P},$ all calibrations: The Benchmark Cases

All values in %

Table 50. The effects of \mathbf{I} , an calibrations. Variation 1								
Scenario 1: Renegotiation	of e_9	Average	Min.	Max.				
Effect of the Policy Program \mathbf{P} (2040) ^a	Population	5.0	4.6	5.5				
	GDP	6.2	3.4	6.6				
	GDP per Capita	1.1	-1.2	1.3				
	Human Capital	2.0	-0.1	2.4				
Scenario 2: Delayed Expects	Average	Min.	Max.					
Effect of the Policy Program \mathbf{P} (2040) ^{<i>a</i>}	Population	5.1	4.6	5.4				
	GDP	5.4	3.5	6.7				
	app a l							
	GDP per Capita	0.3	-1.1	1.4				
	GDP per Capita Human Capital	$\begin{array}{c} 0.3 \\ 1.2 \end{array}$	-1.1 -0.1	$\begin{array}{c} 1.4 \\ 2.3 \end{array}$				
$\frac{a \frac{\text{Population}_{t=14}^{AIDS, \mathbf{P}} - \text{Population}_{t=14}^{AIDS}}{\text{Population}_{t=14}^{AIDS}}, \frac{Y_{t=14}^{AIDS, \mathbf{P}} - Y_{t=14}^{AIDS}}{Y_{t=14}^{AIDS}}$ All values in %	Human Capital	1.2						

Table 36:	The effects	of P	all	calibrations:	Variation	1
T able 00 .	I IIC CHICCUD	ULL,	CULL	camprations.	v ar rauton	т.

Table 37: The effects of \mathbf{P} all calibrations: Variation 2

Table 37: The effects of I	Table 37: The effects of P, all calibrations: Variation 2								
Scenario 1: Renegotiation	of e_9	Average	Min.	Max.					
Effect of the Policy Program \mathbf{P} (2040) ^a	Population	3.2	2.3	5.1					
	GDP	6.7	6.1	7.5					
	GDP per Capita	3.4	1.0	4.2					
	Human Capital	5.3	3.0	6.8					
Scenario 2: Delayed Expect	Average	Min.	Max.						
Effect of the Policy Program \mathbf{P} (2040) ^a	Population	3.8	3.3	5.6					
	GDP	7.2	6.2	7.4					
	GDP per Capita	3.3	1.0	3.9					
	Human Capital	5.7	2.4	6.8					
$\frac{\text{Population}_{t=14}^{AIDS, \mathbf{P}} - \text{Population}_{t=14}^{AIDS}}{\text{Population}_{t=14}^{AIDS}}, \frac{Y_{t=14}^{AIDS, \mathbf{P}} - Y_{t=14}^{AIDS}}{Y_{t=14}^{AIDS}}, \frac{y_{t=14}^{AIDS, \mathbf{P}} - y_{t=14}^{AIDS}}{y_{t=14}^{AIDS}}, \frac{\lambda_{t=14}^{AIDS, \mathbf{P}} - \lambda_{t=14}^{AIDS}}{\lambda_{t=14}^{AIDS}}.$									
All values in $\%$									

Table 50. The cheets of I , an earibrations. Variation 5							
Scenario 1: Renegotiation of	of e_9	Average	Min.	Max			
Effect of the Policy Program \mathbf{P} (2040) ^{<i>a</i>}	Population	7.7	5.9	9.1			
	GDP	7.2	4.9	8.8			
	GDP per Capita	-0.4	-1.0	0.3			
	Human Capital	0.2	0.0	0.9			
Scenario 2: Delayed Expecta	Average	Min.	Max.				
Effect of the Policy Program \mathbf{P} (2040) ^{<i>a</i>}	Population	7.8	5.9	9.1			
	GDP	7.3	4.9	9.0			
	GDP per Capita	-0.5	-0.9	-0.1			
	Human Capital	0.1	0.0	0.2			
$\frac{a}{\frac{\text{Population}_{t=14}^{AIDS, \mathbf{P}} - \text{Population}_{t=14}^{AIDS}}{\text{Population}_{t=14}^{AIDS}}, \frac{Y_{t=14}^{AIDS, \mathbf{P}} - Y_{t=14}^{AIDS}}{Y_{t=14}^{AIDS}}$ All values in %	$\frac{JDS}{t=14}, \frac{y_{t=14}^{AIDS, \mathbf{P}} - y_{t=14}^{AIDS}}{y_{t=14}^{AIDS}}, \frac{y_{t=14}^{AIDS}}{y_{t=14}^{AIDS}},$	$\frac{\lambda_{t=14}^{AIDS, \mathbf{P}} - \lambda_t}{\lambda_{t=14}^{AIDS}}$	$\frac{AIDS}{=14}$.				

Table 38: The effects of \mathbf{P} , all calibrations: Variation 3

Table 39: The effects of **P**, all calibrations: Variation 4

	, an canorations.	variation 4	5	
Scenario 1: Renegotiation	of e_9	Average	Min.	Max.
Effect of the Policy Program \mathbf{P} (2040) ^a	Population	5.1	4.8	5.4
	GDP	4.5	3.4	6.7
	GDP per Capita	-0.6	-1.3	1.3
	Human Capital	0.4	-0.1	2.3
Scenario 2: Delayed Expects	Average	Min.	Max.	
Effect of the Policy Program \mathbf{P} (2040) ^a	Population	5.2	4.8	5.3
	GDP	4.1	3.5	4.4
	GDP per Capita	-1.0	-1.3	-0.9
	Human Capital	-0.1	-0.1	-0.1
$\frac{1}{a} \frac{\text{Population}_{t=14}^{AIDS, P} - \text{Population}_{t=14}^{AIDS}}{\text{Population}_{t=14}^{AIDS}}, \frac{Y_{t=14}^{AIDS, P} - Y_{t=14}^{AIDS}}{Y_{t=14}^{AIDS}}$	$\frac{1DS}{14}, \frac{y_{t=14}^{AIDS, \mathbf{P}} - y_{t=14}^{AIDS}}{y_{t=14}^{AIDS}},$	$\frac{\lambda_{t=14}^{AIDS, \mathbf{P}} - \lambda_t}{\lambda_{t=14}^{AIDS}}$	$\frac{AIDS}{=14}$.	

All values in %

Interest Rate	C.	Scenario 1		S.	Scenario 2				
	Average	Min.	Max.	Average	Min.	Max.			
Base Case				·					
0.0% p.a.	8	6	9	8	7	10			
0.7% p.a.	7	6	8	7	6	9			
5.0% p.a.	5	4	5	4	4	5			
Variation 1: The level of N_{min}^1									
0.0% p.a.	9	6	9	9	7	10			
0.7% p.a.	8	6	8	8	6	9			
5.0% p.a.	5	4	5	5	4	5			
Variation 2:	The level of	f σ_t		·					
0.0% p.a.	8	7	9	9	8	9			
0.7% p.a.	7	7	8	8	7	8			
5.0% p.a.	4	4	5	5	5	5			
Variation 3:	The level of	f α_t							
0.0% p.a.	13	11	15	14	12	16			
0.7% p.a.	12	10	13	13	10	15			
5.0% p.a.	7	6	8	8	6	9			
Variation 4:	The level of	f z_t							
0.0% p.a.	8	6	10	7	7	8			
0.7% p.a.	7	6	9	7	6	7			
5.0% p.a.	4	4	6	4	4	4			

Table 40: The policy program ${\bf P}:$ Profitability^{*a*}, including unborn individuals, all calibrations

^aAll entries expressed as multiples of the 1990 NPV of the costs of \mathbf{P} .

Scenario 1: Revision of e_9

Scenario 2: Delayed Expectations

tions Interest Rate	Scenario 1						Scenario 2					
	$(A2\hat{a})$			$(A2\hat{b})$			$(A2\hat{a})$			$(A2\hat{b})$		
	Avg.	Min.	Max.	Avg.	Min.	Max.	Avg.	Min.	Max.	Avg.	Min.	Max
Base Case												
0.0% p.a.	5	5	5	7	5	7	5	5	5	6	5	8
0.7% p.a.	4	4	5	6	4	7	5	4	5	5	4	7
5.0% p.a.	3	3	3	4	3	4	3	3	3	4	3	5
Variation 1:	The le	vel of	N_{min}^1									
0.0% p.a.	5	5	5	7	4	8	5	5	5	7	5	8
0.7% p.a.	4	4	4	6	4	7	5	4	5	6	4	7
5.0% p.a.	3	3	3	4	3	4	3	3	3	4	3	5
Variation 1:	The le	vel of	σ_t									
0.0% p.a.	4	4	5	7	5	7	5	4	5	8	6	8
0.7% p.a.	4	4	4	6	5	6	4	4	4	7	5	7
5.0% p.a.	3	3	3	4	3	4	3	3	3	4	4	4
Variation 1:	The le	vel of	α_t									
0.0% p.a.	5	5	6	6	5	7	6	5	6	6	5	6
0.7% p.a.	5	5	5	5	5	6	5	5	5	5	5	6
5.0% p.a.	3	3	4	4	3	4	4	3	4	4	3	4
Variation 1:	The le	vel of	z_t									
0.0% p.a.	5	5	5	6	5	8	5	5	6	5	5	6
0.7% p.a.	4	4	5	5	4	7	5	4	5	5	4	5
5.0% p.a.	3	3	3	3	3	5	3	3	4	3	3	3

Table 41: The policy program \mathbf{P} : Profitability^{*a*}, excluding unborn individuals, all calibrations

^aAll entries expressed as multiples of the 1990 NPV of the costs of \mathbf{P} .

Scenario 1: e_9 subject to a binding contract

Scenario 2: e_9 revised by the first group

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