



Munich Personal RePEc Archive

Engaging Central Banks in Climate Change? The Mix of Monetary and Climate Policy

Chen, Chuanqi and Pan, Dongyang and Bleischwitz, Raimund and Huang, Zhigang

Central University of Finance and Economics, University College London

October 2020

Online at <https://mpra.ub.uni-muenchen.de/103750/>
MPRA Paper No. 103750, posted 28 Oct 2020 11:33 UTC

Engaging Central Banks in Climate Change?

The Mix of Monetary and Climate Policy

Chuanqi Chen¹, Dongyang Pan², Raimund Bleischwitz³, Zhigang Huang⁴

Abstract

Given the recent debate on central banks' role under climate change, this research theoretically investigates the mix of monetary and climate policy and provides some insights for central banks who are considering their engagement in the climate change issue. The "climate-augmented" monetary policy is pioneeringly proposed and studied. We build an extended Environmental Dynamic Stochastic General Equilibrium (E-DSGE) model as the method. By this model, we find the following results. First, the making process of monetary policy should consider the existing climate policy and environmental regulation. Second, the coefficients in traditional monetary policy can be better set to enhance welfare when climate policy is given. This provides a way to optimise the policy mix. Third, if a typical form climate target is augmented into the monetary policy rule, a dilemma could be created. This means that it has some risks for central banks to care for the climate proactively by using the narrow monetary policy. At the current stage, central banks could and should use other measures to help the climate and the financial stability.

Keywords: Central Bank, Climate Change, Monetary Policy, Climate Policy, E-DSGE

¹ PhD Candidate, School of Finance, Central University of Finance and Economics & Research Fellow, International Institute of Green Finance (中央财经大学绿色金融国际研究院)

² Corresponding author. PhD Candidate, Institute for Sustainable Resources, University College London & Research Fellow, International Institute of Green Finance, Email: d.pan.17@ucl.ac.uk

³ Professor, Institute for Sustainable Resources, University College London

⁴ Professor, School of Finance, Central University of Finance and Economics

21

1. Introduction

22 Should central banks engage in the climate change issue? In 2015, a report
23 published by the Bank of England⁵ proposed that climate change could pose a risk to
24 financial stability and economic development. Since then, and especially after the
25 signing of the Paris Agreement, climate change and the broader environmental issue
26 have become a factor that central banks are called on to consider. By forming the
27 Network of Central Banks and Supervisors for Greening the Financial System (NGFS)
28 in 2017 and the International Platform on Sustainable Finance (IPSF) in 2019, many
29 central banks are starting to investigate ways to manage risks from climate change and
30 to support a green economic transition. For instance, China’s central bank pioneered
31 the field by supporting “green finance” via monetary policy in 2018⁶. This can be
32 viewed as a kind of “climate-augmented” monetary policy, or “green monetary policy”.
33 However, these arguments and actions do not mean that it is totally justifiable for central
34 banks to engage in the climate change issue without condition. Some experts worry that
35 such engagement could deviate central banks’ market neutrality and overburden their
36 policy tools (violate the Tinbergen Rule). The momentum in policy practice and the
37 debate on the feasibility of the engagement naturally raise the need of research on the
38 monetary policy under climate change considerations.

39 In academia, the exacerbated climate change and environmental challenge has
40 brought new waves of research in the “environmental macroeconomics” (Hassler et al.,
41 2016). Since 2010, some theoretical frameworks have been founded and applied to
42 assess how environmental risks and relevant policies could affect the macro-economy.

⁵ Bank of England’s Prudential Regulation Authority (2015). The impact of climate change on the UK insurance sector. <https://www.bankofengland.co.uk/prudential-regulation/publication/2015/the-impact-of-climate-change-on-the-uk-insurance-sector>

⁶ Source: The People’s Bank of China
<http://www.pbc.gov.cn/goutongjiaoliu/113456/113469/3549913/index.html>

43 The “Environmental Dynamic Stochastic General Equilibrium (E-DSGE)” model has
44 been newly developed as a mainstream method. Angelopoulos (2010), Fischer and
45 Springborn (2011), Heutel (2012), Golosov et al. (2014), Doda (2014), Annicchiarico
46 and DiDio (2015), and Dissou and Karnizova (2016) investigated relationships between
47 greenhouse gas (GHG)/pollutant emissions and business cycles by setting
48 GHG/pollutant as an externality in the economy and determined how environmental
49 policies influence either fluctuation or economic growth. Other researchers have
50 studied the effect of weather on economic volatility. Chen (2014) built a model with
51 weather shocks embedded and found that it had good explanatory power for China’s
52 business cycle. Gallic and Vermandel (2019) found that weather shocks account for a
53 very significant proportion of economic volatility in the long run. Of those policy-
54 related studies, two regimes of environmental policy, namely cap-and-trade (permitting)
55 and taxing, are the main subjects of focus. For example, Golosov et al. (2014) tried to
56 find the optimal level of taxing fossil fuels. Dissou and Karnizova (2016) compared the
57 different implications of reducing CO2 emissions with carbon permits and carbon taxes
58 in place.

59 At first glance, monetary policy and environmental issues are seemingly unrelated.
60 However, such traditional notion starts changing. According to the above research,
61 environment factors and policies are proven to influence either the fluctuation or the
62 growth of the economy, which is exactly what monetary policy cares about. Hence,
63 some researchers have started to investigate the role of central banks and monetary
64 policy under climate change. Pioneering discussions, including Haavio (2010),
65 Campiglio (2016), Ma (2017), McKibbin et al. (2017), and Bolton et al. (2020), have
66 qualitatively explained the linking mechanism between monetary policy and climate
67 change. Particularly, Krogstrup and Oman (2019) point out that the mix of
68 macroeconomic and financial policies for climate change mitigation needs further
69 investigation.

70 Quantitatively, Annicchiarico and DiDio (2017) were the first to use an E-DSGE

71 model to study the mix of monetary and climate policy. They compared three specific
72 mixes and showed that the optimal monetary policies should be tightened slightly when
73 GHG emissions are considered. Economides and Xepapadeas (2018) compared
74 monetary policy both with and without considering climate change in the model and
75 found that the reaction of monetary policy to economic shocks will be affected by
76 climate change. Punzi (2019) introduced borrowing constraints and heterogeneous
77 production sectors into the model to investigate green financing activity and found that
78 only the differentiated capital requirement policy can sustain green financing. Huang
79 and Punzi (2019) incorporated financial friction, according to Bernanke et al. (1999),
80 and found that environmental regulations can accelerate the risks that the financial
81 system faces. Chan (2020) introduced environmental targeting carbon taxation, fiscal,
82 and monetary policies and compared their different effects in terms of improving the
83 environment and welfare.

84 These scholars can be regarded to have started a new discussion on monetary policy
85 and the environment. However, because of the growing global enthusiasm on
86 sustainability, central banks are expected to respond to more concerns about this issue.
87 It includes the macroeconomic and financial stability implications of climate change,
88 the risks of stranded assets, the relationship between monetary policy and both climate
89 change and climate policy, how to encourage green finance, the cost and benefit of
90 “green monetary policy”, and many other aspects.⁷ Many specific concerns have not
91 been touched upon by previous works.

92 In this research, we aim to investigate the relationship between and the mix of
93 monetary and climate policy and provide some insights for central banks who are

⁷ Please refer to the NGFS’s “Technical Supplement” to the “First Comprehensive Report” (https://www.banque-france.fr/sites/default/files/media/2019/08/19/ngfs-report-technical-supplement_final_v2.pdf), “The Macroeconomic and Financial Stability Impacts of Climate Change Research Priorities” (https://www.ngfs.net/sites/default/files/medias/documents/ngfs_research_priorities_final.pdf) and NGFS’s research priorities listed by The International Network for Sustainable Financial Policy Insights, Research, and Exchange (INSPIRE) (<https://www.climateworks.org/inspire/>)

94 considering their engagement in the climate change issue. We will answer three new
95 and relevant questions: (1) Whether and how monetary policy is influenced by climate
96 policy? (2) Whether and how monetary policy can be improved when the climate policy
97 is considered in the framework of analysis and whether there is an optimal monetary
98 policy? and (3) Should a central bank adopt a “climate-augmented” monetary policy or
99 use monetary policy to care for the climate proactively? By answering these questions,
100 we can understand how monetary policy can coordinate with climate policy and some
101 mechanisms of the policy mixing. The above research topic and questions mainly
102 extend that of Annicchiarico and DiDio (2017). We also extend it by working on more
103 research objects: more kinds of policy mixes that are closer to the real-world policy, not
104 only the mixes that contain Ramsey optimised policy.

105 Our method for research is an extended E-DSGE model. The basic DSGE setting
106 is in line with the standard New Keynesian framework. The basic “Environmental”
107 features are introduced following Annicchiarico and DiDio (2017) by incorporating the
108 GHG emissions from production, their negative externality on productivity, and the
109 climate policy that controls emissions, i.e., cap-and-trade or carbon tax. To consider the
110 environmental module in a more comprehensive way, we also introduce some novel
111 environmental features into the model: the concealed emissions, the potential penalty
112 for them, and the effectiveness of enforcement of such penalty. These concealed
113 emission-related features are omitted by traditional E-DSGE models, but actually
114 common in the reality and found to be nontrivial in the model economy.

115 Based on the E-DSGE model, we first mix monetary policy [of Taylor rule type
116 (Taylor, 1993), which is a close approximation of the real-world] with different types
117 of climate policy and compare these different mixes to see if climate policy can
118 influence monetary policy. The impulse responses of major economic and
119 environmental variables to shocks and the conditional welfare and consumption
120 equivalents are calculated. The results show that when monetary policy is mixed with
121 different types of climate policy under different effectiveness of environmental

122 regulation, its dynamic changes. Therefore, the making process of monetary policy
123 should consider the existing climate policy and environmental regulation.

124 We then explore a traditional way to improve the mix of monetary and climate
125 policy. This is to optimise the coefficients in the Taylor rule of monetary policy. The
126 results show that the coefficients can always be better set to enhance welfare when a
127 certain regime of climate policy is considered in the framework. If the cost-push shock
128 is dominant in the economy, optimal coefficients exist. Both the climate policy regime
129 and the effectiveness of environmental regulation can affect the value of the optimal
130 coefficients.

131 Finally, we propose to improve the policy mix by introducing a radically “climate-
132 augmented” monetary policy, which can help determine whether it is good for a central
133 bank to use monetary policy to care for the climate proactively. This is to introduce an
134 emission gap target into the Taylor rule of monetary policy. The results show that the
135 welfare of the economy can be enhanced when monetary policy is augmented by the
136 new target and the coefficient of the target is set in a specific interval. However, under
137 some circumstances, such monetary policy will create a dilemma for central banks. This
138 indicates a risk if we directly use the narrow monetary policy to care for the climate.

139 The novelty of this research lies in three aspects. First, the research topic. Besides
140 being among the first within the emerging discussion and modelling work on monetary
141 policy in the context of climate change, this research investigates three important
142 questions (see above) that are newly emerging in policy making and pioneeringly
143 studies the “‘climate-augmented’ monetary policy” in a formal model. This help answer
144 questions raised by the NGFS. Second, the research scope. Extending Annicchiarico
145 and DiDio (2017) who considered either monetary or climate policy as Ramsey type in
146 the policy mix, we work on mixes with both the two policies non-Ramsey optimised,
147 which can better represent the real-world. Third, the research method. The traditional
148 E-DSGE model is firstly enriched with concealed emission-related features so that its
149 environmental module is more comprehensive and closer to the reality.

150 The paper proceeds as follow. Section 2 describes the extended E-DSGE model.
 151 Section 3 compares the mixes of monetary policy with different climate policies.
 152 Section 4 investigates the optimisation of policy mixes. Sections 5 concludes.

153 2. Model

154 We construct an extended E-DSGE model based on the New Keynesian
 155 framework. GHG emissions from production, their negative externality on productivity,
 156 and environmental policies that control emissions are introduced following
 157 Annicchiarico and DiDio (2017). Innovatively, concealed (illegal) emissions, the
 158 potential penalty for them, and the effectiveness of enforcement of such penalty are set
 159 into the model by extending the enterprise sector and environmental authority. This is
 160 to depict the reality that in many countries the environmental regulation is not very
 161 strict, and firms have some space to emit more than the legal level.

162 The introduction of concealed emission-related features enriches the traditional E-
 163 DSGE models, making it more comprehensive and closer to the reality. Such
 164 introduction is also found to be nontrivial for answering our research questions. The
 165 potential penalty for concealed emissions can be regarded as another dimension of
 166 environmental regulation, in addition to the traditional climate policy (carbon tax or
 167 cap-and-trade).

168 2.1 Household

169 A representative household maximises its expected lifetime utility, which is
 170 determined by consumption C_t and labour L_t and has the form of

$$171 \mathbb{E}_0 \left\{ \sum_{t=0}^{\infty} \beta^t S_t \left(\ln C_t - \mu_L \frac{L_t^{1+\eta}}{1+\eta} \right) \right\} \quad (1)$$

172 where $0 < \beta < 1$ is the discount factor, $\eta \geq 0$ is the inverse of the elasticity of
 173 labour supply, and $\mu_L > 0$ is the coefficient of disutility of labour. S_t represents the

174 stochastic shocks of time-preference, which follows $\ln S_t = \rho_S \ln S_{t-1} + (1 -$
 175 $\rho_S) \ln S + e_{S,t}$ to evolve, where $0 < \rho_S < 1$ and $e_{S,t} \sim i.i.d.N(0, \sigma_S^2)$.

176 The budget constraint of the household is

$$177 \quad P_t C_t + R_t^{-1} B_{t+1} = B_t + W_t L_t + D_t + P_t T_t \quad (2)$$

178 where P_t is the price of final good, B_t and B_{t+1} are the nominal quantity of riskless
 179 bonds at period t and $t + 1$, R_t is the riskless interest rate of the bonds which is
 180 determined by the central bank, W_t is the nominal wage of labour, D_t denotes the
 181 nominal dividend derived from enterprises, and T_t is the lump-sum transfer from
 182 government.

183 At the optimum we have the following first-order conditions

$$184 \quad \beta R_t \mathbb{E}_t \left[\frac{S_{t+1}}{S_t} \frac{C_t}{C_{t+1}} \frac{1}{\Pi_{t+1}} \right] = 1 \quad (3)$$

$$185 \quad L_t^\eta = \frac{W_t}{\mu_L P_t C_t} \quad (4)$$

186 where $\Pi_{t+1} = P_{t+1}/P_t$ is the inflation of period $t + 1$. Equation (1) is the Euler
 187 equation, and equation (2) is the labour supply equation.

188 2.2 Enterprise and the Environment

189 Consistent with the standard New Keynesian framework, the enterprise sector is
 190 formed by final good and intermediate good producers. The final good Y_t is produced
 191 by competitive firms using the Constant Elasticity of Substitution (CES) technology

$$192 \quad Y_t = \left[\int_0^1 Y_{j,t}^{\frac{\theta_t-1}{\theta_t}} dj \right]^{\frac{\theta_t}{\theta_t-1}} \quad (5)$$

193 where $Y_{j,t}$ denotes the intermediate goods produced by monopolistically competitive
 194 firms, and the subscript $j \in [0,1]$ denotes the intermediate good firms of a continuum.
 195 $\theta_t > 1$ is the elasticity of substitution and is also a stochastic process that describes the
 196 cost-push shock (Smets and Wouters (2003)). It follows $\ln \theta_t = \rho_\theta \ln \theta_{t-1} +$
 197 $(1 - \rho_\theta) \ln \theta + e_{\theta,t}$ with $0 < \rho_\theta < 1$ and $e_{\theta,t} \sim i.i.d.N(0, \sigma_\theta^2)$.

198 Final good producers maximise their profit, which is determined by

199
$$P_t Y_t = \int_0^1 Y_{j,t}^{\frac{\theta_t-1}{\theta_t}} dj \quad (6)$$

200 The first-order condition yields the demand function for intermediate goods

201
$$Y_{j,t} = \left(\frac{P_{j,t}}{P_t} \right)^{-\theta_t} Y_t \quad (7)$$

202 and

203
$$P_t = \left[\int_0^1 P_{j,t}^{1-\theta_t} dj \right]^{\frac{1}{1-\theta_t}} \quad (8)$$

204 which implies that the price of final good P_t is also the price level.

205 A typical intermediate good firm has a production function

206
$$Y_{j,t} = \Lambda_t A_t L_{j,t} \quad (9)$$

207 where A_t is the total factor productivity (TFP) factor or technology that follows a
 208 stochastic process $\ln A_t = \rho_A \ln A_{t-1} + (1 - \rho_A) \ln A + e_{A,t}$, in which $0 < \rho_A < 1$
 209 and $e_{A,t} \sim i.i.d. N(0, \sigma_A^2)$. Following Golosov et al. (2014), Λ_t is a damage coefficient
 210 that describes the negative externality of GHG emissions on productivity (TFP damage
 211 coefficient). It is the pivot linking the economy and the environment. Λ_t is determined
 212 by the stock of emissions following

213
$$\Lambda_t = e^{-\chi(M_t - \tilde{M})} \quad (10)$$

214 where M_t is the stock of emissions of period t, \tilde{M} is the level before the industrial
 215 revolution, and $\chi > 0$ measures the intensity of negative externality.

216 According to Heutel (2012), GHG emissions are a by-product of the production
 217 process. The original emissions from production are $Z_{j,t}^{ori}$ which is proportional
 218 (measured by φ) to the volume of output of intermediate firms

219
$$Z_{j,t}^{ori} = \varphi Y_{j,t} \quad (11)$$

220 To dispose of the original emissions, a firm has three channels to use and trade-off:
 221 abate emission, emit legally and pay tax, and conceal emission. A firm can choose to
 222 abate a percentage of $U_{t,j}$ ($0 \leq U_{t,j} \leq 1$) of the original emissions which will bring a
 223 marginal increasing cost of $\phi_1 U_{j,t} \phi_2 Y_{j,t}$, where $\phi_1 = \phi_1' \varphi > 0$ and $\phi_2 > 1$ are cost

224 coefficients. A firm can also choose to legally emit some original emissions. This
225 requires a firm to pay a carbon tax or buy an emission permit in the cap-and-trade
226 system (depending on the climate policy regime) at a price $p_{z,t}$ for every unit of GHG
227 emissions.

228 The novelty of our model is the introduction of **concealed emitting channel and**
229 **related environmental regulation**. Normally, a government or environmental
230 authority cannot detect every source of pollution. So, firms have some space to emit
231 secretly and provide artificially low legal emission data, making their real emission
232 higher than the legal level which they have either paid tax or bought a permit. The secret
233 or concealed emissions will save some costs for either emission abating or legal
234 emitting. Meanwhile, the concealed emissions are subject to potential fine. Although a
235 government may not be able to spot every concealed emission, they usually have some
236 degree of regulation on such emissions and will pose some costs (most commonly
237 penalty or prosecution) to the emitters spotted. A recent example of the concealed
238 emission and the related regulation is the Volkswagen emissions scandal in 2015. The
239 Volkswagen company concealed their cars' excessive emissions by technical
240 manipulation for years. It was detected by chance and then the company has faced a
241 huge amount of fine by governments.

242 To abstract the above, we assume that firms (as a whole) have the concealed
243 emitting channel to dispose of the original emissions; the government spots the
244 concealed emissions with a certain probability (the lower, the weaker the effectiveness
245 of environmental regulation on emissions). If spotted, the government penalises the
246 firm with a certain amount of fine (the fewer, the weaker the effectiveness). To model
247 this, we assume that a firm faces an expected fine volume that equals to $\frac{\psi}{2} V_{t,j}^2 \varphi Y_{j,t}$,
248 where $\varphi Y_{j,t} = Z_{j,t}^{ori}$ is the original emissions; $0 \leq V_{t,j} \leq 1$ is the proportion of
249 concealed emissions in the original emissions; $\psi > 0$ is defined as the "Effectiveness
250 of Enforcement of Environmental Regulation" (EOEER), which is proportional to the

251 probability of the government spotting concealed emissions and the amount of the fine
 252 for every unit of concealed emissions. Using the $\frac{\psi}{2} V_{t,j}^2 \phi Y_{j,t}$ term as the volume of the
 253 fine is derived from a simple intuition: the more concealed emissions that are emitted
 254 and spotted or the more effective the enforcement of environmental regulation, then the
 255 greater the fine. $V_{t,j}$ is quadratic in the term to describe that the total amount of fine is
 256 marginally increasing with regard to $V_{t,j}$ — the more that a firm emits concealedly,
 257 the easier are the emissions to be spotted. A number $\frac{1}{2}$ is put into the term to simplify
 258 calculation.

259 The introduction of concealed emissions and EOEER relaxes the hidden
 260 assumption of the perfect effectiveness of environmental regulation in most previous
 261 E-DSGE models and makes the environmental regulation in our study more
 262 comprehensive and closer to the reality. Such introduction is nontrivial for answering
 263 our specific research questions, as we will show that the differences in EOEER will
 264 make the regimes of climate policy either more similar or more different and further
 265 influence the dynamics of financial and economic variables (see Subsection 3.3). The
 266 potential penalty for concealed emissions can be regarded as another dimension of
 267 environmental regulation, in addition to the traditional climate policy (carbon tax or
 268 cap-and-trade).

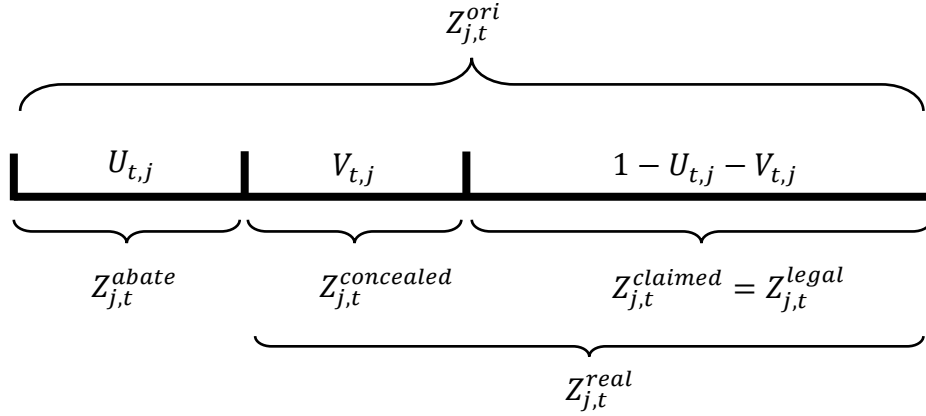
269 The three channels by which firms can dispose of their original emissions, namely
 270 emission abating, legally emitting, and concealedly emitting, have now all been
 271 explained. This is helpful for illuminating the following variables. The real emission
 272 $Z_{j,t}^{real}$ is the amount of GHG that is really emitted to the atmosphere and can be
 273 monitored by the government. It equates to the original emissions $Z_{j,t}^{ori}$ minus the
 274 abated emissions $Z_{j,t}^{abate} = U_{t,j} \phi Y_{j,t}$. The claimed emissions $Z_{j,t}^{claimed}$ is the amount
 275 of GHG emissions that a firm reports to the government concealing its concealed
 276 emissions $Z_{j,t}^{concealed}$. It is the amount of legal emissions $Z_{j,t}^{legal}$ and also the amount

277 of tax or permit that a firm needs to either pay or buy ($p_{Z,t}Z_{j,t}^{legal}$). It equals to the real
 278 emissions minus the concealed emissions. Accordingly, we have

$$279 \quad Z_{j,t}^{real} = Z_{j,t}^{ori} - Z_{j,t}^{abate} = (1 - U_{t,j})\varphi Y_{j,t} = Z_{j,t}^{legal} + Z_{j,t}^{illegal} \quad (12)$$

$$280 \quad Z_{j,t}^{claimed} = Z_{j,t}^{real} - Z_{j,t}^{illegal} = (1 - U_{t,j} - V_{t,j})\varphi Y_{j,t} = Z_{j,t}^{legal} \quad (13)$$

281 The above relationship is illustrated in Figure 1.



282

283

Figure 1: The relationship among emission variables

284

285 Considering the cost of disposing of emissions via the three channels and the sticky
 286 pricing assumption in the standard New Keynesian framework (Rotemberg, 1982), the
 287 objective of an intermediate firm is to maximise

$$288 \quad \mathbb{E}_0 \left\{ \sum_{t=0}^{\infty} \Omega_{0,t} \left[\frac{P_{j,t}}{P_t} Y_{j,t} - TC_{j,t} - \frac{\gamma}{2} \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right)^2 Y_t \right] \right\} \quad (14)$$

289 which is subject to

$$290 \quad TC_{j,t} = \frac{W_t}{P_t} L_{j,t} + \phi_1 U_{j,t}^{\phi_2} Y_{j,t} + p_{Z,t} (1 - U_{j,t} - V_{j,t}) \varphi Y_{j,t} + \frac{\psi}{2} V_{j,t}^2 \varphi Y_{j,t} \quad (15)$$

291 where $\Omega_{0,t} = \beta^t \frac{C_0}{C_t}$ is the stochastic discount factor.

292 The above settings and assumptions yield the following first-order conditions
 293 (more details in Appendix)

$$294 \quad (1 - \theta_t) - \gamma(\Pi_t - 1)\Pi_t + \beta\gamma\mathbb{E}_t \left[\frac{C_t}{C_{t+1}} (\Pi_{t+1} - 1)\Pi_{t+1} \frac{Y_{t+1}}{Y_t} \right] + \theta_t MC_t = 0 \quad (16)$$

295
$$MC_t = \frac{W_t}{\Lambda_t A_t P_t} + \phi_1 U_t^{\phi_2} + p_{Z,t}(1 - U_t - V_t)\varphi + \frac{\psi}{2} V_t^2 \varphi \quad (17)$$

296
$$p_{Z,t} = \frac{1}{\varphi} \phi_1 \phi_2 U_t^{\phi_2 - 1} \quad (18)$$

297
$$V_t = \frac{1}{\psi \varphi} \phi_1 \phi_2 U_t^{\phi_2 - 1} = \frac{p_{Z,t}}{\psi} \quad (19)$$

298 where MC_t is the marginal cost of production, $\gamma > 0$ is the price adjusting cost
 299 coefficient, and $\Pi_t = \frac{P_t}{P_{t-1}}$ denotes inflation. Equation (16) is the New Keynesian
 300 Phillips Curve.

301 **2.3 Monetary and Environmental Authorities**

302 The monetary policy authority (central bank) decides the nominal interest rate
 303 following a traditional Taylor rule

304
$$\frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi}\right)^{\rho_{\Pi}} \left(\frac{Y_t}{Y_t^{na}}\right)^{\rho_Y} \quad (20)$$

305 where Y_t^{na} is the natural output without price stickiness, R and Π are the steady
 306 state of nominal interest rate and inflation, and ρ_{Π} and ρ_Y are the intensity
 307 coefficients for targeting on inflation and output gap, respectively. The Taylor rule type
 308 monetary policy is a closer approximate of the real-world than the Ramsey monetary
 309 policy. We do not consider the latter in this research.

310 The environmental authority decides the climate policy regime. In this research
 311 we analyse two major regimes: cap-and-trade (CA regime) and carbon tax (TX regime).
 312 Under the CA regime, the environmental authority sets an emission cap Z_t^{cap} and
 313 sells emission permits to the market at a price decided by the market competition. In
 314 equilibrium, the total legal emissions Z_t^{legal} equates to Z_t^{cap} . Under the TX regime,
 315 the authority sets a fixed carbon tax level for every unit of legal emissions. The authority
 316 does not set a ceiling for total legal emissions. We also include climate policy regimes
 317 of no control on emissions (NO regime) and of Ramsey optimal control (RM regime)
 318 in the following analysis, but mainly for benchmarking and comparison purpose.

319 Besides choosing the climate policy regime, the environmental authority fines firms if
 320 concealed emissions are spotted. The earnings of the authority, including the income
 321 from selling emission permits or levying a carbon tax and from the fines are transferred
 322 to households directly.

323 2.4 Market Clearing and Aggregation

324 In equilibrium, we have the market clearing condition

$$325 \quad Y_t = C_t + \phi_1 U_t^{\phi_2} Y_t + \frac{\gamma}{2} (\Pi_t - 1)^2 Y_t \quad (21)$$

326 Following Rotemberg (1982), we assume that all the firms are symmetrical. So, the
 327 gross variables share the same form of expressions with individual variables. The total
 328 production function is

$$329 \quad Y_t = \Lambda_t A_t L_t \quad (22)$$

330 The totalities of emissions are

$$331 \quad Z_t^{legal} = \int_0^1 Z_{j,t}^{legal} dj = (1 - U_t - V_t) \varphi Y_t \quad (23)$$

$$332 \quad Z_t^{real} = \int_0^1 Z_{j,t}^{real} dj = (1 - U_t) \varphi Y_t \quad (24)$$

333 The total transfer is

$$334 \quad T_t = p_{z,t} Z_t^{legal} + \frac{\psi}{2} v_t^2 \varphi Y_t \quad (25)$$

335 The total stock of emissions is

$$336 \quad M_t = (1 - \delta_M) M_{t-1} + Z_t^{real} + \tilde{Z} \quad (26)$$

337 where \tilde{Z} is the emissions from nature without human influence, and $0 < \delta_M < 1$ is
 338 the natural rate of decay of GHG stock.

339 2.5 Calibration

340 We calibrate the parameters as follows and list them in Table 1. Following Gali
 341 (2015), the discount factor β is set as 0.99, the elasticity of substitution in steady state
 342 θ is set as 6, and the inverse of the Frisch elasticity η is set as 1. The adjusting cost
 343 coefficient γ , which measures price stickiness, is set as 58.25 so that the stickiness has

344 a duration of three quarters when it is converted into Calvo pricing. The disutility
345 coefficient of labour μ_L is set as 24.9983 so that the steady state of labour is 0.2
346 without monopoly. Following tradition, the persistent coefficients of shocks (including
347 TFP shock, preference shock, and cost-push shock) are set as 0.9, and the Taylor-rule
348 elasticities (coefficients) of monetary policy ρ_π and ρ_Y are set as 1.5 and 0.5,
349 respectively, in Section 3. Following Annicchiarico and DiDio (2017), the scale
350 coefficient of abatement cost ϕ_1 is set as 0.185, and the elasticity ϕ_2 is set as 2.8.
351 The parameter determining the damage caused by emissions on output χ is set as
352 0.000457. Following Heutel (2012), the decay rate of emission stock δ_M is set as
353 0.0021. Following Xu et al. (2016), the coefficient measuring the original emissions per
354 unit of output φ is set as 0.601. As for the EOEER ψ , according to the proportion of
355 the “environmental penalties” collected by the government in total GDP in China,
356 which is approximately 0.01%,⁸ the ψ should be approximately 0.45. This is within
357 the magnitude of 0.1 to 1. For comparison purposes, we need to set a large ψ and a
358 small ψ . Considering the magnitude, the benchmark of ψ (in Subsection 3.1 and 3.2)
359 is set as 1, which is the upper bound of the magnitude, and the value describing a relative
360 ineffective regulation is set as 0.1 (in Subsection 3.3), which is the lower bound.

361

Table 1: Calibrated values of the parameters

Parameter		Value	Target
β	Discount factor	0.99	$\beta = \frac{1}{1+\rho}$, where risk-free (pure time preference) discount rate $\rho \approx 1\%$
η	Inverse of the Frisch elasticity,	1	Literature
μ_L	Disutility coefficient of labour	24.9983	Steady labour time is 0.2 under fully competition market
θ	Elasticity of substitution in steady state	6	Literature
γ	Adjusting cost coefficient of sticky	58.25	Literature

⁸ Source: The State Council of China http://www.gov.cn/xinwen/2019-02/26/content_5368758.htm

	price		
ρ_A	Persistent coefficient of TFP shocks.	0.9	Commonly used value
ρ_S	Persistent coefficient of preference shocks.	0.9	Commonly used value
ρ_θ	Persistent coefficient of cost-push shocks.	0.9	Commonly used value
ϕ_1	Scale coefficient of abatement cost	0.185	Literature
ϕ_2	Elasticity of abatement cost	2.8	Literature
χ	Intensity of negative externality	0.000457	Literature
φ	Emissions per unit of output in the absence of abatement	0.601	Literature
ψ	EOEER	0.1, 1	Proportion of environmental punishment cost in GDP
δ_M	Decay rate of GHG stock	0.0021	Literature
A	TFP in steady state	5.1151	Steady output is 1 under fully competition market
S	Preference in steady state	1	No influence at steady state
ρ_π	Policy Response to Inflation	0.5	Literature
ρ_Y	Policy Response to Output Gap	1.5	Literature

3. The Mixes of Monetary Policy with Different Climate Policies

In this section, we mix the monetary policy with four different types of climate policies: cap-and-trade, carbon tax, no control (with climate policy absent), and Ramsey optimal, and compare the mixes in terms of differences in fluctuation and welfare. We also consider the differences brought by the (in)effectiveness of enforcement of environmental regulation. The comparison in this section will show whether and how the monetary policy will vary when the type of climate policy and the effectiveness of environmental regulation are different. This is an extension of Annicchiarico and DiDio (2017), also a pre-requisite for optimising the policy mixes in Section 4.

3.1 Fluctuation Comparison

Annicchiarico and DiDio (2017) started investigating the mixes of monetary

374 policy and climate policy by considering one policy as the Ramsey type and the other
375 as varying types. They showed that key macroeconomic variables, including labour,
376 emissions, interest rate, and inflation, respond differently to a productivity shock when
377 the policy type differs. Their work is an inspiring start on such issue, meanwhile, can
378 be extended or improved in some respects. First, at least one policy was assumed as the
379 Ramsey type in any mix they studied. This type of policy is the ideal optimisation but
380 difficult to carry out directly in reality. The mix that purely consists of practically
381 realisable policies is not studied. So, such real-world practical policy mixes can be
382 further investigated. Second, the potential ineffectiveness of environmental regulation
383 that could change the dynamics of the economy can be considered additionally. This
384 relaxes the hidden assumption of the perfect effectiveness of environmental regulation.
385 Third, the regimes with “no climate policy” and “Ramsey climate policy” can be
386 introduced into the comparison to serve as benchmarks.

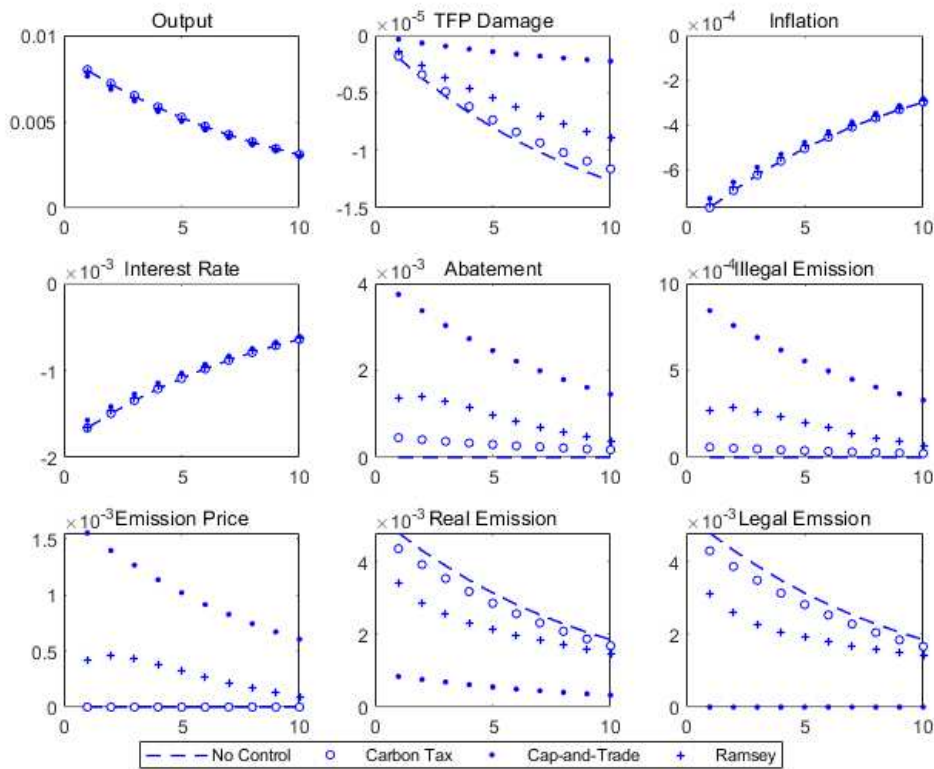
387 We still compare the response of key macroeconomic variables to the productivity
388 shock, but extend the work of Annicchiarico and DiDio (2017) by including the mixes
389 of Taylor rule type monetary policy with four different types of climate policy
390 (constituting four regimes) with consideration of the EOEER. The four types of climate
391 policy include cap-and-trade, carbon tax, no control and Ramsey optimal (see Appendix
392 for equations). The first three and the Taylor rule monetary policy are all commonly
393 implemented in the real-world. In this subsection, we compare the fluctuation of the
394 economy in different regimes via impulse response analysis. To be specific, we give a
395 1% positive TFP shock and then find the dynamics of economic variables. Here, the
396 EOEER ψ is set as 1 as a benchmark. The values of tax level and emission target are
397 set so that all regimes (except for the NO regime⁹) share the same steady state with the
398 case of Ramsey.

⁹ The No Control regime is equivalent to a TX regime with a tax level at 0. This makes the steady state different and predefined.

399 The results of impulse response analysis (absolute deviation from steady states)
400 are shown in Figure 2. It can be found that the responses of endogenous variables to the
401 shock have different paths under the four different regimes. For economic and monetary
402 variables, output under the CA regime increases by less than under the RM regime,
403 whereas output under the TX regime increases by more than under the RM regime. The
404 TFP damage coefficient (Λ_t), inflation, and the resulting interest rate under the CA
405 regime drop less than under the RM regime, whereas under the TX regime the negative
406 changes are larger than is the case under the RM regime. For environmental related
407 variables, abatement, concealed emissions, and emission price under the CA regime rise
408 by more than under the RM regime, whereas, under the TX regime they either change
409 less than under the RM regime or do not change. Legal emissions and real emissions
410 under the TX regime increase by more than under the RM regime, whereas, under the
411 CA regime, real emissions rise by less than under the RM regime, and legal emissions
412 do not change.

413 The differences between regimes (note the scales of the y-axes) are not large,
414 because the environmental-related disruption and costs (for abatement, emissions, and
415 fines) are relatively small under current parameters.¹⁰ The differences could be more
416 significant in the future if the climate change problem becomes more serious. Since it
417 could aggravate the external shock (e.g., severer weather extremes) and increase the
418 emission-related costs.

¹⁰ The standard deviation of Λ_t is less than 0.00027 under the CA and TX regimes. The proportion of environmental-related costs to output (GDP) at steady state is less than 0.7%.



419

420 Figure 2: The dynamics of endogenous variables after a 1% positive TFP shock under
 421 different regimes (EOEER=1)

422

423 To understand the mechanism behind the differences of the changes, we first need
 424 to understand that after a positive TFP shock, **emission prices** and **real emissions** will
 425 rise under the RM regime. When the shock happens, every unit of output will have a
 426 lower cost. This decreases the price level and increases the demand. An increased
 427 demand causes an increased supply or output. When the level of output increases, the
 428 original emissions from production also increase. This can cause a higher marginal
 429 damage to TFP, so the Ramsey optimization requires a higher rate of abatement U_t .
 430 According to equation (18), the **emission price $p_{z,t}$** also needs to be **higher**
 431 **simultaneously** under the RM regime. To dispose of the extra original emissions from
 432 production under the RM regime, firms will be arranged to use all three channels —
 433 namely abating, legally emitting, and concealedly emitting — as all the channels have

434 an increasing marginal cost for society. Hence, abatement, legal emissions, and
435 concealed emissions will all rise. As a result, **real emissions, which equates to the sum**
436 **of legal and concealed emissions, will also rise** under the RM regime.

437 Then, the differences between the CA and TX regimes can be explained. Under
438 the TX regime (and the NO regime), the **emission prices** (for legal emissions) are fixed
439 at the carbon tax level (or 0), irrespective of how much firms emit. After a shock, this
440 is lower than the Ramsey optimal (increased) emission price. The relative lower
441 emission price has three implications: (1) On **output**. As the emission price is fixed, its
442 marginal level is also fixed and equates to the tax level. At optimum, the costs of all
443 three channels for disposing of the original emissions from production share this same
444 marginal level. The costs for disposing of every unit of emissions via concealed
445 emitting and abatement are marginal increasing; hence, the average cost of these two
446 channels is lower than the tax level. Given that the tax level is lower than is the Ramsey
447 optimal emission price, the average cost for disposing of every unit of emission via all
448 three channels is less than is the case under the RM regime. When the unit emission
449 cost is lower, the price level decreases, which causes a higher demand for production
450 output. So, it is higher than is the case under the RM regime. (2) On **real emissions** and
451 the **TFP damage coefficient**. The relatively lower costs of disposing of legal and
452 concealed emissions allow real emissions, which is the sum of legal and concealed
453 emissions, to rise by more than is the case under the RM regime. Real emissions
454 accumulate into emission stock and directly decrease the TFP damage coefficient (N.B.,
455 it is negative). Therefore, the TFP damage coefficient drops by more than it does under
456 the RM regime. (3) On **legal emissions, abatement, and concealed emissions**. With a
457 lower emission price, the legal emissions increase by more than they would under the
458 RM regime. When relatively more original emissions from production are disposed of
459 via the legal emitting channel, a lesser amount of emissions need to be disposed of via
460 the other two channels, namely abating and concealed emitting. This causes the
461 abatement and concealed emissions to increase by less than is the case under the RM

462 regime. (4) On **inflation and interest rate**. A lower than RM regime emission price
463 causes a lower marginal cost of production, and then a lower inflation and lower interest
464 rate in succession. Hence, both the change in inflation and the change in interest rate
465 are lower than their changes under the RM regime.

466 Under the CA regime, the mechanism of change is the antithesis of that under the
467 TX regime. The legal emissions volume is fixed at a target, so it is lower than the new
468 Ramsey optimal (increased) legal emissions' level. After the shock and the rise of
469 original emissions, the concealed emitting and abatement channels need to dispose of
470 more emissions than is the case under the RM regime. This leads to higher marginal
471 disposing costs of these two channels. At optimum, the costs of all three channels for
472 disposing of the original emissions share a same marginal level, hence the emission
473 price (for legal emissions) rises higher than is the case under the RM regime. The higher
474 than RM regime emission price (which is opposite to the lower than RM regime price
475 under the TX regime) has implications for the endogenous variable that are exactly
476 antithetical to those under the TX regime. Therefore, there are differences in the
477 changes between the CA and TX regimes. Meanwhile, we can say that there exists a
478 "price level-offsetting" effect in the CA regime that can better stabilise the economy
479 when a shock happens. This is because the fixed legal emission volume causes a
480 higher/lower price for disposing of emissions and offsets the lowering/heightening price
481 level (and also attenuates monetary policy). Under the TX regime, the fixed carbon
482 price does not have such a function.

483 In general, the above analysis shows that when monetary policy is mixed with
484 different climate policies, the monetary policy itself (interest rate) and the effect of the
485 policies on the economy (other endogenous variables) will differ in facing a TPF shock.
486 Under the TX regime, the monetary policy (interest rate) is strengthened compared with
487 under the RM regime and, meanwhile, the TX regime-type climate policy is looser than
488 is the RM regime-type (real emissions too high and abatement too low). Conversely,
489 under the CA regime the monetary policy is weakened; the CA regime-type climate

490 policy is tighter than is the RM regime-type.

491 The above analysis conveys two key messages: (1) The cap-and-trade regime of
492 climate policy could offset the price fluctuation after shocks and become an attenuator
493 for monetary policy. (2) The making process of monetary policy should consider the
494 existing regime of climate policy, as the dynamic of monetary policy is influenced by
495 the selection of climate policy.

496 3.2 Welfare Comparison

497 To further investigate the above policy mixes, we compare the welfare of the four
498 regimes in addition to the above fluctuation analysis. This will help us find which of
499 the four mixes are better and which are worse.

500 In the comparison, we maintain all parameters, including the coefficients in the
501 Taylor rule and the EOEER, fixed. We set the steady states of the CA and TX regimes
502 equal to that of the RM regime. The steady state of the NO regime comes from the
503 $p_{z,t} = 0$ case of the TX regime. So, the differences in welfare between the CA, TX,
504 and RM regimes are due only to the difference in regime. We follow the welfare
505 criterion of Mendicino and Pescatori (2007) and calculate the conditional welfare of
506 individuals. The expression is

$$507 \quad W_j = \mathbb{E}_t \sum_{m=0}^{\infty} \beta^m \left(\ln C_{j,t+m} - \mu_L \frac{L_{j,t+m}^{1+\eta}}{1+\eta} \right) \quad (27)$$

508 where W_j is the conditional welfare, and $j = \{\text{NO, TX, CA, RM}\}$ means the four
509 regimes of climate policy: no control, carbon tax, cap-and-trade, and Ramsey optimal.

510 To show results more intuitive, we also calculate the consumption equivalent (CE)
511 of each case. CE is the additional fraction of consumption that households under no
512 policy can obtain if a certain policy is introduced for them. Let

$$513 \quad W_{j'} = \mathbb{E}_t \sum_{m=0}^{\infty} \beta^m \left[\ln(1 + CE_{j'}) C_{NO,t+m} - \mu_L \frac{L_{NO,t+m}^{1+\eta}}{1+\eta} \right] \quad (28)$$

514 we have

515
$$CE_{j'} = \exp\{(1 - \beta)(W_{j'} - W_{NO})\} - 1 \quad (29)$$

516 where $j' = \{TX, CA, RM\}$ represents a certain regime of climate policy.

517 The welfares of all four regimes and the corresponding CEs are shown in Table 2.

518 Table 2: Welfare and Consumption Equivalents of the four regimes

	Welfare	CE
NO	-59.469	0
TX	-58.583	0.0088972
CA	-58.585	0.0088727
RM	-58.566	0.0090715

519

520 We can find

521
$$W_{RM} > W_{TX} > W_{CA} > W_{NO} \quad (30)$$

522 and

523
$$CE_{RM} > CE_{TX} > CE_{CA} > CE_{NO} \quad (31)$$

524 Specifically: (1) Any regime with a climate policy has better welfare than has the
 525 NO regime, as any climate policy can somehow reduce emissions, and so does its
 526 externality. (2) The RM regime has the highest welfare and CE of all the regimes. This
 527 is the nature of Ramsey policy. (3) The TX regime is a little better than is the CA regime
 528 in terms of welfare and CE; however, the differences between them are not big.

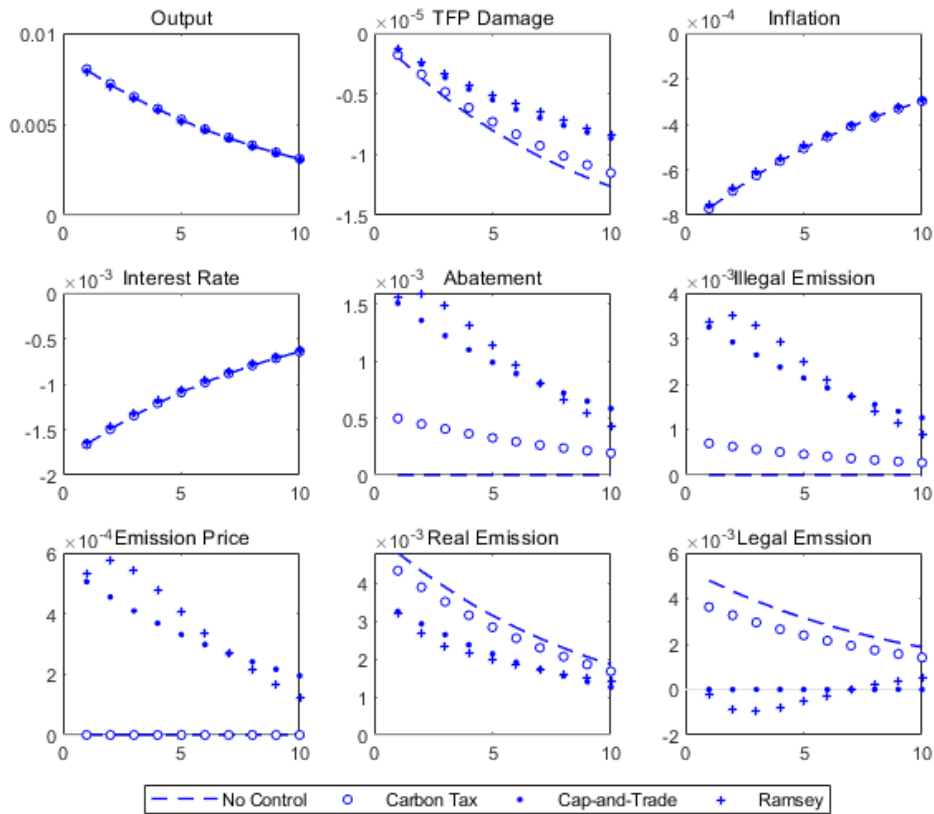
529 In terms of the welfare standard, the TX regime tends to be a better choice among
 530 the three real-world implementable regimes (CA, TX, and NO) when a TFP shock
 531 happens. However, sensitivity analysis indicates that it is not always the best choice.
 532 We find that either when the parameter EOEER is small enough or when the shock is
 533 changed to demand-type, the result $W_{TX} > W_{CA}$ and $CE_{TX} > CE_{CA}$ will reverse to
 534 $W_{TX} < W_{CA}$ and $CE_{TX} < CE_{CA}$. Hence, among the three real-world implementable
 535 regimes, no one is always dominant over others regardless of parameters and shocks,
 536 in terms of the welfare standard.

537 **3.3 The Role of Environment Regulatory Effectiveness**

538 This section investigates whether the effectiveness of enforcement of
539 environmental regulation, in addition to the choice of climate policy type, will also
540 affect the economy and the monetary policy.

541 To do this, we set a lower effectiveness parameter ψ equal to 0.1. This is a much
542 smaller value than the benchmark case in Subsection 3.1, where $\psi = 1$. The small
543 value means that the environmental regulation is less effective. In Figure 3, we show
544 the fluctuation of economy following the same method as in Subsection 3.1. It needs to
545 be noted that the units of some of the vertical axes in Figure 2 and Figure 3 are different.
546 Then, we compare the results in Figure 2 ($\psi = 1$) and in Figure 3 ($\psi = 0.1$) to identify
547 any differences arising from the effectiveness of enforcement of environmental
548 regulation.

549 It can be found, for variables apart from legal and concealed emissions, that when
550 the effectiveness is lower the differences of fluctuation between the CA and TX regimes
551 become smaller — mainly because the variables' paths under the CA regime are more
552 approximate to the paths under the TX regime. Under the TX regime, legal emissions
553 change by more than is the case when environmental regulation is more effective. Under
554 the CA regime, concealed emissions change more. This makes the mixes with different
555 regimes of climate policy become more similar to each other.



556

557 Figure 3: The dynamics of endogenous variables after a 1% positive TFP shock under
 558 different regimes (EOEER=0.1)

559

560 The pivotal reason for the diminishing differences between regimes is that the less
 561 effective enforcement of environmental regulation gives firms more space to dispose of
 562 their emissions via the concealed emitting channel and the “price level-offsetting” effect
 563 in the CA regime is weakened. When ψ is lower, the unit cost for concealed emissions
 564 and the total cost for disposing of every unit of original emissions will decrease. This
 565 allows the steady state share of concealed emissions in original emissions (i.e. V_t) and
 566 original emissions to increase. After a TFP shock under the TX regime, concealed
 567 emissions rise by more than is the case with higher ψ because of the increased steady
 568 state V_t . The path of abatement is almost unchanged because the extra original
 569 emissions after a shock do not change significantly, and the share of abatement for
 570 disposing of every unit of original emissions (i.e., U_t) is not changed according to

571 equation (18), which does not include ψ . Neither does the path of real emissions, whose
 572 share is $1 - U_t$, change significantly, for the same reason. The legal emissions rise by
 573 less because their share in disposing of every unit of original emissions $1 - U_t - V_t$ is
 574 reduced due to an increased V_t . The paths of inflation and interest rate are almost
 575 unchanged due to a fixed $p_{Z,t}$ under the TX regime.

576 After a TFP shock under the CA regime, $p_{Z,t}$ increases by less than is the case
 577 when ψ is higher, as the cost for concealed emissions rises by less.¹¹ The “price level-
 578 offsetting” effect is weakened. This brings more similar changes in the paths of inflation
 579 and the interest rate. Illegal emissions rise by more than is the case with a higher ψ for
 580 the same reason under the TX regime. Abatement increases by less as more original
 581 emissions are disposed of via the concealed emitting channel. Real emissions rise by
 582 more because the concealed emissions increase by more and the legal emissions are
 583 fixed under the CA regime.

584 In addition to the fluctuation analysis, we also calculate and compare the welfare
 585 of each regime after the EOEER is changed to 0.1. We find that the order of welfare
 586 and the consumption equivalent comparison will change to $W_{ET} > W_{TX}$ and $CE_{CA} >$
 587 CE_{TX} . The reason is that consumption, as one of the determinants of welfare, increases
 588 by more under the CA regime than under the TX regime. A lower ψ brings a lower
 589 cost for concealed emissions. Under the CA regime this also brings a lower $p_{Z,t}$. Then,
 590 the price level decreases and demand, production output, and consumption increase.
 591 However, under the TX regime, $p_{Z,t}$ is fixed, and, hence, the price level decreases by
 592 less than is the case under CA. Then, consumption does not rise by so much.¹² The

¹¹ There is a marginal increasing cost for concealed emissions $\frac{\psi}{2} v_{t,j}^2 \phi Y_{j,t}$. When ψ is lower, the steady state cost for concealed emissions is lower. Hence, the cost for concealed emissions rises less here. Meanwhile, the three channels for disposing of original pollution have the same marginal cost (a natural result of economic optimisation); hence $p_{Z,t}$ equals the cost for concealed emissions.

¹² The fluctuation of price also influences welfare, according to Rotemberg (1982). However, the result here means that the influence of consumption on welfare is stronger.

593 output under the CA regime rises more than it does under the TX regime, after a shock,
594 which makes the output gap under the CA regime relatively smaller and the welfare
595 larger.

596 The above analysis shows that the ineffectiveness of enforcement of environmental
597 regulation will make climate policy less effective and that different regimes become
598 more similar. This implies that the difference in the fluctuation of economy and
599 monetary policy between regimes will also change due to the differentiation of EOEER.
600 Therefore, in addition to the regime of climate policy, the EOEER also needs to be
601 considered when designing monetary policy. Otherwise, the dynamics of monetary
602 policy and its effect on the economy will be somewhat different (too strong or too weak)
603 from what is envisaged with only considering the regime of climate policy. Another
604 implication is that, when making monetary policy, developed countries should consider
605 the existing regime of climate policy more carefully than developing countries, as their
606 effectiveness of environmental regulation is often better and the differences between
607 regimes are more significant.

608 **4. The Optimisation of Policy Mixes**

609 From Subsection 3.2, it can be found that, among the three real-world
610 implementable regimes of policy mix (CA, TX, and NO), no one is always dominant
611 over others, in terms of the welfare standard. In this section, we propose to improve or
612 “optimise” these regimes respectively. The first way is to optimise policy coefficients
613 in the traditional Taylor rule of monetary policy. The second and also a novel way is to
614 introduce a radically “climate-augmented” monetary policy. This is to include the
615 emission gap target into the Taylor rule of monetary policy. We will try to find the best
616 coefficient for the new target and determine whether this inclusion can become a
617 desirable practice. The results will give an answer to central banks’ question of
618 “whether it is good for the monetary authority to proactively care for the climate”.

619 **4.1 Optimisation in the Traditional Monetary Policy**

620 The Ramsey optimal monetary policy, which has been investigated by
621 Annicchiarico and DiDio (2017), constitutes the ideally optimal policy mix. However,
622 as this kind of policy assumes that all endogenous variables in the economy can be
623 controlled and adjusted by the authority, it is difficult for policy makers to carry out in
624 reality. We do not work more on it here. For real-world implementable climate policy
625 regimes (CA, TX, and NO), Subsection 3.2 showed that no one is always dominant.

626 In this subsection, our way to improve or to “optimise” the policy mix is to first
627 choose a certain regime that is real-world implementable, then optimise the policy
628 coefficients in them. To do this, we have three potential options. The first is to give a
629 fixed strength of climate policy and optimise the coefficients in the Taylor rule of
630 monetary policy (ρ_Y and ρ_π). The second is to fix the monetary policy coefficients
631 and optimise the climate policy strength. The third is to optimise the climate strength
632 and the monetary coefficients simultaneously. We choose the first method because this
633 research is on the angle of central banks. The second method is on the angle of
634 environmental regulator. The third approach is more comprehensive but is also more
635 complex and difficult for policy makers to coordinate and carry out.

636 To calculate, we first combine different values of monetary policy coefficients
637 with different types of climate policy (CA or TX¹³) under different EOEER and shocks.
638 Shocks include TFP, cost-push, and preference shocks, considering that these three can
639 cover both supply- and demand-side shocks. Then, we derive the welfare and CE of
640 every combination. The policy coefficients ρ_π and ρ_Y that maximise the welfare and
641 CE of a certain combination of climate policy, EOEER, and shock, if exist, is the
642 optimised policy coefficients for it. For simplicity, we only consider the regimes that
643 can solve the model with a unique solution.

644 We find that under a cost-push shock (a positive θ_t shock), there exist optimal

¹³ We do not incorporate the NO regime as Subsection 3.2 showed that it is always an inferior one.

645 monetary policy coefficients for every climate policy and EOEER, as shown in Table
 646 3. This means that if the cost-push shock is dominant in the economy, the central bank
 647 has the best choice of coefficients in the Taylor rule of monetary policy, when climate
 648 policy and EOEER are given.

649 Table 3: Optimal policy coefficients in the Taylor rule of monetary policy under
 650 different climate policies and EOEER (cost-push shock)

φ (EOEER)	Cap-and-Trade		Carbon Tax	
	ρ_{π}	ρ_Y	ρ_{π}	ρ_Y
0.1	3.2335	0.4573	3.4792	0.4591
0.5	2.8024	0.4573	3.4948	0.4593
1	2.6819	0.4589	3.4969	0.4593
10	2.5549	0.4619	3.4984	0.4593
100	2.5418	0.4624	3.4985	0.4591

651

652 Table 3 shows that ρ_Y does not vary significantly across climate policy regimes;
 653 however, ρ_{π} is always larger under the TX regime than under the CA regime. This is
 654 because the emission price in the CA regime changes when a shock happens. When a
 655 cost-push shock (a positive θ_t shock) happens, the price level becomes lower, which
 656 increases demand, production output, and emissions. The higher emissions then lead to
 657 an increase in the price for disposing of emissions under the CA regime (see Subsection
 658 3.1 for details). Hence, the price level under the TX regime (which is fixed) is relatively
 659 lower than is the case under the CA regime. To suppress deflation, a stronger ρ_{π} is
 660 needed. This again shows the “price level-offsetting” effect in the CA regime and the
 661 basic mechanism that differentiates the two climate regimes. Table 3 also shows that
 662 across different EOEER, only ρ_{π} under the CA regime goes lower significantly when
 663 EOEER increases. This is because a higher EOEER pushes up the cost for concealed
 664 emissions and increases the demand for legal emissions. Under the CA regime, the

665 emission permit price $p_{z,t}$ increases more, offsetting the decrease of price level more
666 after the cost-push shock. So, the strength of inflation targeting, ρ_{π} , could be eased.

667 Under TFP or preference shocks, we find that the welfare and CE become higher
668 when ρ_{π} and ρ_Y become larger. This is a common result of the New-Keynesian
669 model. However, this means there are no optimal values of ρ_{π} and ρ_Y if the ranges
670 of the coefficients are not limited and a TFP (or preference) shock is dominant in the
671 economy.

672 To summarise, we find that when climate policy is considered in the framework,
673 the monetary policy can always be improved by adjusting the Taylor rule coefficients.
674 If a cost-push shock is dominant in the economy, optimal coefficients exist. Both the
675 climate policy regime and the EOEER can affect the value of the optimal coefficients.
676 At this point, we can report that when the existing climate policy is brought into the
677 framework of the central bank's policy making, at least three things can be considered
678 to improve the monetary policy: the type (regime) of climate policy, the EOEER, and
679 the coefficient in the Taylor rule of monetary policy.

680 **4.2 The “Climate-Augmented” Monetary Policy**

681 In this subsection, we propose a radical way to improve the traditional policy
682 mixes. This is to change the form of the Taylor rule of monetary policy by incorporating
683 the emission gap target into it and create a so called “climate-augmented” monetary
684 policy. We will search the best coefficient for the new target and determine whether this
685 introduction can become a good practice. This will give an answer to central banks’
686 question of “whether it is good for the monetary authority to proactively care for the
687 climate”.

688 Our method is to add the emission gap as the third target into the traditional
689 inflation and output gap targeting Taylor rule. The emission gap is the relative deviation
690 of current real emissions to the ideal real emissions (we use the steady state real

691 emissions calculated under Ramsey optimal climate policy¹⁴). It is an analogue to the
 692 inflation and output gap target and is a typical form. The new form of the Taylor rule is

$$693 \quad \frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi}\right)^{\rho_{\Pi}} \left(\frac{Y_t}{Y_t^{na}}\right)^{\rho_Y} \left(\frac{Z_{t-1}}{Z}\right)^{\rho_Z} \quad (32)$$

694 where Y_t^{na} is the natural output without nominal price stickiness, R , Π , and Z are
 695 the steady states of nominal interest rate, inflation rate, and real emissions, respectively.
 696 Z_{t-1} represents the current real emissions. We assume that the authority uses Z_{t-1} , not
 697 Z_t , to represent the current real emissions since real emissions includes the concealed
 698 emissions which often cannot be detected during the period of policy making (period
 699 t). The emission gap target is not a replication of the output gap target as we use the
 700 real emissions in it, not the original emissions who are proportional to output. Real
 701 emissions incorporate abatement and is the ultimate factor that influences the
 702 environment and, thus, can directly reflect the climate objective. ρ_Z is the intensity
 703 coefficients for targeting on the emission gap. This new form of Taylor rule makes the
 704 monetary policy proactively care for the climate.

705 Then, we set the strength of the traditional target of monetary policy (i.e. the
 706 inflation and the output coefficient) as fixed: $\rho_Y = 0.5$ and $\rho_{\Pi} = 1.5$, and calculate
 707 welfare values of the economy with different ρ_Z and different shocks.¹⁵ ρ_Z takes
 708 every value in the interval that can produce a unique solution for the equilibrium.
 709 Common shocks (TFP, cost-push, and preference) that cover both supply- and demand-
 710 side shocks are introduced respectively. Under a same shock, if the welfare with a ρ_Z
 711 is higher than is the welfare with $\rho_Z = 0$, a ρ_Z that can improve the policy mix is
 712 found. As ρ_Y and ρ_{Π} are fixed and allowing ρ_Z to change is introducing a new

¹⁴ A more intuitive “ideal real emissions” is the carbon budget measured against the 1.5°C (or lower) target. However, the calculation requires some reliable data in natural science which is currently unavailable.

¹⁵ A more comprehensive method is to simultaneously optimise the three targets. We do not do it in this research as our method is enough when we give the condition “the strength of the traditional Taylor rule target of monetary policy is given” in the conclusion.

713 dimension for optimisation, there must be some ρ_Z that can improve the welfare. It
 714 will serve as a supplement of the potentially either over-strong or over-weak ρ_Y and
 715 ρ_Π .

716 Applying the above method, we can find the intervals of ρ_Z that can improve the
 717 welfare, as well as the values of ρ_Z that can enhance the welfare at the greatest extent
 718 (define as “the best value of ρ_Z ”) under different regimes and different shocks. Results
 719 using parameters calibrated in Subsection 2.5 shown in Table 4. When the TFP or cost-
 720 push shock is dominant, the best ρ_Z is negative in both climate regimes. When the
 721 preference shock is dominant, the best ρ_Z lies in the right boundary of possible values,
 722 which means that the higher the ρ_Z , the higher the welfare.

723 Table 4: The interval of ρ_Z that can improve welfare and the best ρ_Z under different
 724 climate policies and shocks (original price stickiness)

Shock	Cap-and-Trade		Carbon Tax	
	Interval	Best	Interval	Best
TFP shock	(-0.866, 0)	-0.453	(-0.174, 0)	-0.091
Cost-push shock	(-0.509, 0)	-0.261	(-0.12, 0)	-0.062
Preference shock	The higher the better			

725

726 However, sensitivity analysis shows that under TFP or cost-push shock, the best
 727 ρ_Z can also be positive under different parameter values. For example, if the price
 728 stickiness parameter γ is large enough [e.g., 10 times larger, which is roughly in line
 729 with Gertler et al. (2019)], the best ρ_Z becomes positive under both regimes with a
 730 cost-push shock, as shown in Table 5.

731

732

733

734

735 Table 5: The interval of ρ_Z that can improve welfare and best ρ_Z under different
 736 climate policies and shocks (price stickiness 10 times larger)

Shock	Cap-and-Trade		Carbon Tax	
	Interval	Best	Interval	Best
TFP shock	(-0.934, 0)	-0.508	(-0.16, 0)	-0.087
Cost-push shock	(0, 1.342)	0.602	(0, 0.184)	0.085
Preference shock	The higher the better			

737

738 We must point out that when the interval of ρ_Z that can improve welfare is
 739 negative, there is a dilemma between the welfare objective and the environmental
 740 objective. Suppose a positive TFP or cost-push shock happens, then the emission gap
 741 is positive due to the lower price level, higher output, and higher emissions. With a
 742 negative ρ_Z , a lower interest rate will be derived, which encourages demand and
 743 production, fulfilling the welfare objective. However, the higher production causes
 744 higher emissions, which is adverse to the environmental objective. On the contrary, if
 745 we change the ρ_Z to a positive value to realise the environmental objective (emission
 746 gap), then it deviates from the interval that can improve welfare. Failing to enhance
 747 welfare is incompatible with the fundamental purpose of a central bank. This is the
 748 potential dilemma that emerges to a central bank if they add the emission gap target into
 749 the traditional monetary policy.

750 The above analysis gives an answer to the question “whether a central bank should
 751 adopt ‘climate-augmented’ (emission gap targeting) monetary policy” or “whether it is
 752 good for the monetary authority to proactively care for the climate”. If the interval of
 753 the new target’s coefficient (ρ_Z) that can improve welfare consists of a positive part, it
 754 is good to do so by adding the emission gap target into the Taylor rule of monetary
 755 policy and setting the targeting coefficient as a value in the positive interval. If the
 756 interval consists of only negative values, it is not good to add the emission gap target

757 into the Taylor rule.

758 Based on the above results and the real-world circumstance, we do not suggest
759 central banks to add the new climate target (the emission gap target) into the Taylor rule
760 of monetary policy without further reviews. Considering that the welfare improving
761 interval of ρ_Z is not fixed and is determined by many uncertain factors including deep
762 parameters, the regime of climate policy, and the type of shock, a central bank cannot
763 assure that the climate augmented Taylor rule monetary policy always does not bring
764 the dilemma between the welfare and the environmental objective. Meanwhile, many
765 central banks in the real-world are already overburdened with multiple targets other
766 than price stability and employment.

767 This subsection shows that, when the strength of the traditional Taylor rule target
768 of monetary policy is given, incorporating the emission gap target into the rule and
769 setting the coefficient of the new target in a specific interval can improve the policy mix
770 in terms of the welfare standard. The best value of the coefficient for emission targeting
771 is found under different situations (given the coefficients for inflation and output gap
772 targeting fixed). However, under some circumstances, this radically “climate-
773 augmented” monetary policy will create a dilemma between the welfare and the
774 environmental objectives, making it less valuable of recommendation for central banks
775 to adopt without further reviews.

776 **4.3 A Discussion**

777 Although the “climate-augmented” (emission gap targeting) monetary policy is
778 found to be controversial above, it does not mean that this kind of monetary policy is
779 useless from other points of view. The DSGE model is used mainly for fluctuation
780 analysis, so the conclusions are based on short-term standards. Climate change can be
781 characterized as a long-term challenge for mankind. Considering that “climate-
782 augmented” monetary policy of certain forms can limit emission and reduce future
783 climate risks, it could become a preferable choice for policy makers in the long-run.

784 From the modelling prospective, the reasons include: First, the steady state welfare
785 could be higher if emission is limited. This can compensate for the welfare loss shown
786 in the fluctuation analysis. Second, a lower climate risk increases economic stability
787 and decreases welfare loss brought by fluctuation.

788 The above results neither means that central banks should not proactively care for
789 the climate by measures other than the narrow monetary policy (interest rate). Climate
790 change can bring physical and transition risks to firms so that can cause financial and
791 economic instability. Safeguarding financial and economic stability is a major mandate
792 of most central banks. They could use macroprudential and other regulatory policy tools,
793 such as environmental stress testing and green asset purchase, and play a coordinating
794 role among regulators and the market to fulfil this mandate in facing climate change.

795 **5. Conclusion**

796 In this paper, we have studied the relationship between and the mix of monetary
797 and climate policy. By using an Environmental Dynamic Stochastic General
798 Equilibrium (E-DSGE) model augmented with a range of emissions including what we
799 call concealed emissions and related regulations, we have compared the mixes of Taylor
800 rule-based monetary policy with different climate policies to find whether and how
801 climate policy will influence monetary policy; this paper optimised the coefficients in
802 the monetary policy rule under certain climate policies; and proposed a “climate-
803 augmented” monetary policy and investigated if and when it can be a good choice for
804 the central bank. All these provide insights for central banks who are considering their
805 engagement in the climate change issue.

806 The main findings consist of three parts. First, the dynamics of monetary policy
807 and the economy are influenced by the selection of regimes of climate policy and the
808 effectiveness of enforcement of environmental regulation (EOEER). The pivotal reason
809 is that the cap-and-trade regime can offset the price fluctuation after shocks, whereas

810 the carbon tax regime cannot. The effectiveness of environmental regulation also plays
811 a role, as it can make climate policy less effective by providing more space for
812 concealed emissions. Therefore, the making process of monetary policy should consider
813 the existing climate policy and environmental regulation. Developed countries should
814 consider the climate policy more carefully than do the developing ones.

815 Second, the coefficients in the traditional Taylor rule of monetary policy can always
816 be better set to enhance welfare when a certain regime of climate policy is considered
817 in the economy. If the cost-push shock is dominant in the economy, optimal coefficients
818 exist. Both the climate policy regime and the effectiveness of environmental regulation
819 can affect the value of the optimal coefficients. We can summarise from the above that,
820 under the framework with climate factors, at least three aspects can be considered to
821 improve the monetary policy: the type (regime) of climate policy, the effectiveness of
822 enforcement of environmental regulation, and the coefficients of the inflation and
823 output gap targets in the Taylor rule of monetary policy.

824 Third, the welfare of the economy can be enhanced by adding the target of emission
825 gap into the rule of monetary policy and setting the coefficient of the new target in a
826 specific interval, when the strength of the traditional Taylor rule target of monetary
827 policy is given. The best value of the coefficient for targeting can be found under
828 different scenarios. However, under some circumstances, this radically “climate-
829 augmented” (emission gap targeting) monetary policy is likely to create a dilemma
830 between the welfare and the environmental objectives. If we do not want central banks
831 to take the risk of such dilemma, it is better not to introduce the climate target into the
832 monetary policy rule without further reviews. Central banks could and should use
833 measures other than the narrow monetary policy (interest rate) to proactively care for
834 the climate.

835 The above findings give insights to the initial question of this paper “Should central
836 banks engage in the climate change issue?” — The making process of monetary policy
837 should consider the existing climate policy; otherwise, the dynamic of monetary policy

838 and its effect on the economy will be different from what is originally envisaged.
839 However, it is not recommended for central banks to add the climate (emission gap)
840 target into the narrow monetary policy at the current stage, as this may create a dilemma
841 for them.

842 This research can be extended in several aspects. For example: (1) Set the EOEER
843 as a shock to study the “transition risk” brought by climate change and the tightening
844 process of environmental regulation (e.g., China’s environmental inspection). (2) Set a
845 dynamic rule (e.g., the Taylor rule) for climate policy. (3) Improve the form of climate
846 target in the monetary policy rule (e.g., use an ideal real emission that is in line with the
847 1.5°C climate target). (4) Introduce more types of shocks (e.g., climate change shock
848 after the tipping point). (5) Introduce more financial fractions and constraints (e.g. zero
849 lower bound of interest rate) to describe the role of monetary policy more precisely. (6)
850 Along with the monetary policy, introduce and study more policy tools and measures
851 that central banks can use to mitigate climate risk and support the green economic
852 transition [e.g., identifying green financing and differentiating reserve rate requirements,
853 re-lending and collateral requirements (Pan, 2019), green asset purchase and credit
854 guidance]. (7) Find whether the three-target “climate-augmented” monetary policy is
855 better than the traditional two-target policy when all the Taylor rule coefficients in them
856 are simultaneously optimised.
857

859 **Derivation of the New Keynesian Phillips Curve**860 The maximisation problem of firm j is

$$861 \left\{ \begin{array}{l} V_0 = \max \mathbb{E}_0 \left\{ \sum_{t=0}^{\infty} \Omega_{0,t} \left[\frac{P_{j,t}}{P_t} Y_{j,t} - TC_{j,t} - \frac{\gamma}{2} \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right)^2 Y_t \right] \right\} \\ s. t. \left\{ \begin{array}{l} TC_{j,t} = \frac{W_t}{P_t} L_{j,t} + \phi_1 U_{j,t}^{\phi_2} Y_{j,t} + p_{z,t} (1 - U_{j,t} - V_{j,t}) \varphi Y_{j,t} + \frac{\psi}{2} V_{j,t}^2 \varphi Y_{j,t} \\ Y_{j,t} = \Lambda_t A_t L_{j,t} \\ Y_{j,t} = \left(\frac{P_{j,t}}{P_t} \right)^{-\theta_t} Y_t \end{array} \right. \end{array} \right.$$

862 We can rewrite the objective function by the Bellman Equation as

$$863 V_t = \max \left\{ \frac{P_{j,t}}{P_t} Y_{j,t} - TC_{j,t} - \frac{\gamma}{2} \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right)^2 Y_t + \mathbb{E}_t \Omega_{t,t+1} V_{t+1} \right\}$$

864 which yields the Lagrangian function as

$$865 \mathcal{L}_t = \frac{P_{j,t}}{P_t} Y_{j,t} - \left[\frac{W_t}{P_t} \frac{Y_{j,t}}{\Lambda_t A_t} + \phi_1 U_{j,t}^{\phi_2} Y_{j,t} + p_{z,t} (1 - U_{j,t} - V_{j,t}) \varphi Y_{j,t} + \frac{\psi}{2} V_{j,t}^2 \varphi Y_{j,t} \right] \\ 866 - \frac{\gamma}{2} \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right)^2 Y_t + \mathbb{E}_t [\Omega_{t,t+1} V_{t+1}] + \lambda_{j,t} \left[\left(\frac{P_{j,t}}{P_t} \right)^{-\theta_t} Y_t - Y_{j,t} \right]$$

867 where $\Omega_{t,t+1} = \beta \frac{C_t}{C_{t+1}}$ is the stochastic discount factor. So, we can obtain the FOC for868 $U_{j,t}$ and $V_{j,t}$

$$869 p_{z,t} = \frac{\phi_1 \phi_2}{\varphi} U_{j,t}^{\phi_2 - 1}$$

$$870 V_{j,t} = \frac{p_{z,t}}{\psi}$$

871 and derive

$$872 MC_{j,t} = \frac{W_t}{P_t} \frac{1}{\Lambda_t A_t} + \phi_1 U_{j,t}^{\phi_2} + p_{z,t} (1 - U_{j,t} - V_{j,t}) \varphi + \frac{\psi}{2} V_{j,t}^2 \varphi$$

873 The FOCs for $P_{j,t}$ and $Y_{j,t}$ derive

$$874 1 - \theta_t - \gamma \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right) \frac{P_{j,t}}{P_{j,t-1}} + \beta \gamma \mathbb{E}_t \left[\left(\frac{P_{j,t+1}}{P_{j,t}} - 1 \right) \frac{P_{j,t+1}}{P_{j,t}} \frac{C_t}{C_{t+1}} \frac{Y_{t+1}}{Y_t} \right] + \theta_t MC_{j,t} = 0$$

876 **Taylor Rule Monetary Policy Mix Cap-and-Trade Climate Policy**

$$\left. \begin{aligned}
& \beta R_t \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} \frac{1}{\Pi_{t+1}} \right] = 1 \\
& (1 - \theta_t) - \gamma(\Pi_t - 1)\Pi_t + \beta\gamma \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} (\Pi_{t+1} - 1)\Pi_{t+1} \frac{Y_{t+1}}{Y_t} \right] + \theta_t MC_t = 0 \\
& MC_t = \frac{W_t}{\Lambda_t A_t P_t} + \phi_1 \tilde{U}_t^{\phi_2} + p_{Z,t}(1 - U_t - v_t)\varphi + \frac{\psi}{2} v_t^2 \varphi \\
& L_t^\eta = \frac{W_t}{\mu_L P_t C_t} \\
& Y_t = C_t + \phi_1 U_t^{\phi_2} Y_t + \frac{\gamma}{2} (\Pi_t - 1)^2 Y_t \\
& Z = (1 - U_t - v_t)\varphi Y_t + \tilde{Z} \\
& M_t = (1 - \delta_M)M_{t-1} + (1 - U_t)\varphi Y_t + \tilde{Z} \\
& Y_t = \Lambda_t A_t L_t \\
& p_{Z,t} = \frac{1}{\varphi} \phi_1 \phi_2 U_t^{\phi_2 - 1} \\
& v_t = \frac{1}{\psi \varphi} \phi_1 \phi_2 U_t^{\phi_2 - 1} = \frac{p_{Z,t}}{\psi} \\
& \frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi} \right)^{\rho_\pi} \left(\frac{Y_t}{Y_t^{na}} \right)^{\rho_Y}
\end{aligned} \right\}$$

878 **Taylor Rule Monetary Policy Mix Carbon Tax Climate Policy**

$$\left. \begin{aligned}
& \beta R_t \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} \frac{1}{\Pi_{t+1}} \right] = 1 \\
& (1 - \theta_t) - \gamma(\Pi_t - 1)\Pi_t + \beta\gamma \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} (\Pi_{t+1} - 1)\Pi_{t+1} \frac{Y_{t+1}}{Y_t} \right] + \theta_t MC_t = 0 \\
& MC_t = \frac{W_t}{\Lambda_t A_t P_t} + \phi_1 U^{\phi_2} + p_Z(1 - U - v)\varphi + \frac{\psi}{2} v^2 \varphi \\
& L_t^\eta = \frac{W_t}{\mu_L P_t C_t} \\
& Y_t = C_t + \phi_1 U^{\phi_2} Y_t + \frac{\gamma}{2} (\Pi_t - 1)^2 Y_t \\
& M_t = (1 - \delta_M)M_{t-1} + (1 - U)\varphi Y_t + \tilde{Z} \\
& Y_t = \Lambda_t A_t L_t \\
& p_Z = \frac{1}{\varphi} \phi_1 \phi_2 U^{\phi_2 - 1} \\
& v = \frac{1}{\psi \varphi} \phi_1 \phi_2 U^{\phi_2 - 1} = \frac{p_Z}{\psi} \\
& \frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi} \right)^{\rho_\pi} \left(\frac{Y_t}{Y_t^{na}} \right)^{\rho_Y}
\end{aligned} \right\}$$

880 **Taylor Rule Monetary Policy Mix No Control Climate Policy**

881 No control policy is a special case of the carbon tax policy with $p_Z = 0$. The

882 equation system is all the same as with the “Taylor Rule Monetary Policy Mix Carbon

883 Tax Climate Policy” except that p_Z is set as 0.

884 **Taylor Rule Monetary Policy Mix Ramsey Optimal Climate Policy**

$$\begin{aligned}
 & \mathbb{E}_t \sum_{t=0}^{\infty} \beta^t \left(\ln C_t - \mu_L \frac{L_t^{1+\eta}}{1+\eta} \right) \\
 & \left. \begin{aligned}
 & \beta R_t \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} \frac{1}{\Pi_{t+1}} \right] = 1 \\
 & (1 - \theta_t) - \gamma(\Pi_t - 1)\Pi_t + \beta\gamma \mathbb{E}_t \left[\frac{C_t}{C_{t+1}} (\Pi_{t+1} - 1)\Pi_{t+1} \frac{Y_{t+1}}{Y_t} \right] + \theta_t MC_t = 0 \\
 & MC_t = \frac{W_t}{\Lambda_t A_t P_t} + \phi_1 U_t^{\phi_2} + p_{Z,t}(1 - U_t - v_t)\varphi + \frac{\psi}{2} v_t^2 \varphi \\
 & L_t^\eta = \frac{W_t}{\mu_L P_t C_t} \\
 & Y_t = C_t + \phi_1 U_t^{\phi_2} Y_t + \frac{\gamma}{2} (\Pi_t - 1)^2 Y_t \\
 & M_t = (1 - \delta_M) M_{t-1} + (1 - U_t)\varphi Y_t + \tilde{Z} \\
 & Y_t = \Lambda_t A_t L_t \\
 & \frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi} \right)^{\rho_\pi} \left(\frac{Y_t}{Y^{na}} \right)^{\rho_Y}
 \end{aligned} \right\} \text{s. t.}
 \end{aligned}$$

886

887

Reference

- 889 Angelopoulos, K., Economides, G., & Philippopoulos, A. (2010). What is the best
890 environmental policy? Taxes, permits and rules under economic and environmental
891 uncertainty. CESifo Working Paper Series No. 2980.
- 892 Annicchiarico, B., & Di Dio, F. (2015). Environmental policy and macroeconomic
893 dynamics in a new Keynesian model. *Journal of Environmental Economics and*
894 *Management*, 69, 1-21.
- 895 Annicchiarico, B., & Di Dio, F. (2017). GHG emissions control and monetary policy.
896 *Environmental and Resource Economics*, 67(4), 823-851.
- 897 Bernanke, B. S., Gertler, M., & Gilchrist, S. (1999). The financial accelerator in a
898 quantitative business cycle framework. *Handbook of macroeconomics*, 1, 1341-
899 1393.
- 900 Bolton, P., Despres, M., Pereira da Silva, L. A., Samama, F., & Svartzman, R. (2020).
901 The green swan: Central banking and financial stability in the age of climate change.
902 Bank for International Settlements
- 903 Chan, Y. T. (2020). Are macroeconomic policies better in curbing air pollution than
904 environmental policies? A DSGE approach with carbon-dependent fiscal and
905 monetary policies. *Energy Policy*, 141, 111454.
- 906 Chen, G., Chao, J., Wu, X., & Zhao, X. (2014). Rare disaster risk and the
907 macroeconomic fluctuation in China. *Economic Research Journal*, 2014(8), 54-66.
908 (Originally in Chinese: 陈国进, 晁江锋, 武晓利, 赵向琴, 罕见灾难风险和
909 中国宏观经济波动[J]. *经济研究*, 2014(8):54-66.)
- 910 Campiglio, E. (2016). Beyond carbon pricing: The role of banking and monetary policy
911 in financing the transition to a low-carbon economy. *Ecological Economics*, 121,
912 220-230.
- 913 Doda, B. (2014). Evidence on business cycles and CO2 emissions. *Journal of*
914 *Macroeconomics*, 40, 214-227.
- 915 Dissou, Y., & Karnizova, L. (2016). Emissions cap or emissions tax? A multi-sector
916 business cycle analysis. *Journal of Environmental Economics and Management*, 79,
917 169-188.
- 918 Economides, G., & Xepapadeas, A. (2018). Monetary policy under climate change.
919 Bank of Greece Working Paper No. 247.

- 920 Fischer, C., & Springborn, M. (2011). Emissions targets and the real business cycle:
921 Intensity targets versus caps or taxes. *Journal of Environmental Economics and*
922 *Management*, 62(3), 352-366.
- 923 Gali, J. (2015). *Monetary policy, inflation, and the business cycle: an introduction to*
924 *the new Keynesian framework and its applications*. Princeton University Press.
- 925 Gallic, E., & Vermandel, G. (2019). Weather shocks. Working Paper, HAL Id: halshs-
926 02127846.
- 927 Gertler, M., Kiyotaki, N., & Prestipino, A. (2019). A macroeconomic model with
928 financial panics. *The Review of Economic Studies*, 87(1), 240-288.
- 929 Golosov, M., Hassler, J., Krusell, P., & Tsyvinski, A. (2014). Optimal taxes on fossil
930 fuel in general equilibrium. *Econometrica*, 82(1), 41-88.
- 931 Haavio, M. (2010). Climate change and monetary policy. *Bank of Finland Bulletin Vol.*
932 *84*.
- 933 Hassler, J., Krusell, P., & Smith Jr, A. A. (2016). Environmental macroeconomics. In
934 *Handbook of macroeconomics (Vol. 2, pp. 1893-2008)*. Elsevier.
- 935 Heutel, G. (2012). How should environmental policy respond to business cycles?
936 Optimal policy under persistent productivity shocks. *Review of Economic Dynamics*,
937 15(2), 244-264.
- 938 Huang, B., Punzi, M. T., & Wu, Y. (2019). Do banks price environmental risk?
939 evidence from a quasi natural experiment in the People's Republic of China. ADBI
940 Working Paper No. 974.
- 941 Krogstrup, S., & Oman, W. (2019). Macroeconomic and financial policies for climate
942 change mitigation: a review of the literature. IMF Working Paper WP/19/185.
- 943 Ma, J. (2017). Establishing China's green financial system. China Financial Publishing
944 House. (Originally in Chinese: 马骏, 2017, 《构建中国绿色金融体系》, 中国金
945 融出版社, 2017年10月)
- 946 McKibbin, W. J., Morris, A. C., Panton, A., & Wilcoxon, P. (2017). Climate change and
947 monetary policy: Dealing with disruption. *Brookings Climate and Energy*
948 *Economics Discussion Paper*.
- 949 Mendicino, C., & Pescatori, A. (2004). Credit frictions, housing prices and optimal
950 monetary policy rules. Working Paper n.42/2004 Università Roma Tre.
- 951 Pan, D. (2019). The Economic and environmental effects of green financial policy in
952 China: A DSGE approach. SSRN Working Paper 3486211.
- 953 Punzi, M. T. (2019). Role of bank lending in financing green projects: A dynamic

954 stochastic general equilibrium approach. Handbook of Green Finance: Energy
955 Security and Sustainable Development, 1-23.

956 Rotemberg, J. J. (1982). Sticky prices in the United States. *Journal of Political Economy*,
957 90(6), 1187-1211.

958 Smets, F., & Wouters, R. (2002). An estimated stochastic dynamic general equilibrium
959 model of the euro area: International Seminar on Macroeconomics. European
960 Central Bank Working Paper No. 171.

961 Taylor, J. B. (1993). Discretion versus policy rules in practice. *Carnegie-Rochester*
962 *conference series on public policy*, Vol. 39, 195-214.

963 Xu, W., Xu, K., & Lu, H. (2016). Environmental policy and China's macroeconomic
964 dynamics under uncertainty – based on the NK model with distortionary taxation.
965 MPRA Working Paper No. 71314