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# Advances in the Agent-based Modeling of Economic and Social Behavior

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# Abstract

In this survey we discuss advances in the agent-based modeling of economic and social systems. We present the state of the art in the heuristic design of agents and the connections to the results from laboratory experiments on agent behavior. We further discuss how large-scale social and economic systems can be modeled and highlight novel methods and data sources. At last we present an overview of estimation techniques to calibrate and validate agent-based models.

*Keywords:* agent-based models, heuristic design, model calibration, behavioral economics, computational social science, computational economics JEL: B41, C60, D90, E70, G17, G40, L20

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# 1. Introduction

Agent-based models (ABMs<sup>1</sup>) are a way to model and simulate the behavior and interactions of heterogeneous individuals and organizations and to infer regularities that govern their behavior as a whole. While first models were developed in the 70s, ABMs were only popularized in the 90s when computational methods became more readily available. By today, agentbased modeling has been applied to a large number of scientific fields and it continues to be an exciting and popular approach for a number of reasons:

- 1. The availability of computational power to model large-scale social interaction;
- 2. The possibility to use decision rules to model behavior (behavioral heuristics) instead of mathematical optimization;
- 3. The evolution of highly applicable network theory to facilitate interaction patterns between agents;
- 4. The importance of the stability of human-devised systems (such as financial system);
- 5. The popularity of behavioral labs that provide blueprints for designing agent-based models;
- 6. The current neglect within the agent-based community of the importance of estimation and calibration of agent-based models.

This survey highlights the above listed concepts and provides some applications of modeling economic and social behavior that have seen a significant development in the last decade. Our goal is to provide an overview of the state of the art and explore some of the potentials of the agent-based approach along these lines.

 $<sup>^1\</sup>mathrm{In}$  the following we use ABM as the abbreviation for agent-based model and agent-based modeling.

First, in section 2, we will see how advances in agent-based models have led to much more detailed simulations of social behavior and social systems and how this has contributed to a better understanding of how agents' behavior and interactions lead to structure on the aggregate level. A significant part of this section is devoted to the granularity of data and data types that can be used in agent-based models. In section 3 we discuss the use of heuristics in defining adaptive behavior of boundedly rational agents such as households, financial investors, banks, and/or firms by sourcing from some of the most recent agent-based models within the fields of economics and finance. In section 4 we present how economic networks can be used to describe the interactions of agents, for example when these represent organizations, such as firms or banks. This section focuses on advances of structure identification in economic networks and brings forth some recent examples of explicit incorporation of networks into agent-based models. In what follows, section 5 highlights one particular case where networks have proven very useful, namely in the analysis of systemic stability of the financial sector. Here idiosyncratic actions can become coordinated and lead to aggregate fluctuations and macro level instabilities. The section presents a compilation of agent-based models that study connectivity within a banking system, emerging systemic risk, and address the risk mitigation via macroprudential rules (such as leverage ratios, liquidity ratios, equity ratios) and tax policies. Section 6 is motivated by the fact that behavioral economics has only recently entered the literature about computational methods. This section describes the contribution of experimental and behavioral economics to agent-based modeling in dealing with the behavior and interaction of heterogeneous agents. It is focused on the need to combine computational economics with the capacity of controlled laboratory experiments to study the effects of psychological, cognitive, emotional, cultural, and social factors on decision making in order to bring the agent-based models closer to experimental data. Finally, section 7 elaborates on the development of estimation methodology for agent-based models. While many agent-based models aim to reproduce certain stylized facts of economic systems their validation too often stays on a rather rudimentary level. This section therefore surveys methods for the empirical validation and estimation of agent-based models and their parameters.

#### 2. Agent-based Models and Computational Social Science

Computational Social Science (CSS) is receiving enormous momentum in recent years thanks to the availability of large-scale datasets in various forms and the accessibility of computational platforms to social scientists. Broadly speaking, CSS aims to use computational methods and large-scale data to examine existing social theories, develop new theories, and improve our understanding of human behavior in scale. Despite its broad perspective, CSS in recent years focused heavily on data-driven methodologies (Lazer et al., 2020), and the community of agent-based modelers has been largely neglected. Indeed, agent-based modeling combined with data-driven methodologies can be extremely instrumental in deepening our understanding of social behavior and guide us towards their explanation (Conte and Paolucci, 2014). Models allow to examine the macro-level outcomes that arise from social and psychological theories and empirical data can be used to validate the models. This is important because there can be many social or psychological theories for a social phenomena that result in different behavioral outcomes (Lorenz et al., 2020). ABM in social science consists of multiple components that can be characterized as follows:

1. Agents with their perceptions and decision-making capacity. Agents are commonly comprised of individuals or social groups that have a set of complex psychological traits and socio-demographic attributes. These attributes can be fixed or dynamic. Epstein argues that we should consider cognitively plausible agents in ABM (Epstein, 2014). An example of such approach is the work by Sircova and colleagues that used cross-cultural survey analysis combined with discussions in focus groups to assess the big five personality traits in different countries and use that to calibrate the level of cooperation among agents when resources are limited (Sircova et al., 2015).

- 2. Environment. Agents are often in an environment where they interact with others and the interaction might impact their action. In his seminal work, Watts showed that when a norm-adoption mechanism is applied on a social network, the size of the adoption cascade is heavily dependent on the structure of social network, since agents do not interact homogeneously with each other (Watts, 2002).
- 3. Rules and actions. While interaction between agents can be adjusted by a plausible network, the rules of interaction with other agents and decision making process are deduced from social and psychological theories or observations. For example, the Granovetter threshold theory – people follow a norm as long as a certain threshold of people in their neighborhood follow it – is often used to study the dynamics of norm adoption in a society.
- 4. *Macro structure*. Macro-level structure emerges as a consequence of the micro-level behavior of the agents over time and the macroscopic outcomes may vary significantly from micro behavior (see Schelling, 1971, for an early segregation model). This transition from micro to macro allows ABM to be a powerful explanatory tool. By tuning the parameters on the micro-level, the macro-level effect can be examined.

Depending on the purpose of the model, different levels of granularity and data are needed. Edmonds (2017) categorized the purpose of modeling into seven categories, namely prediction, explanation, description, theoretical exploration, illustration, analogy, and social interaction. They offer a practical approach to assess the validity and risks associated with any of these purposes. Understanding the purposes associated with the ABM in CSS will enable an interdisciplinary team to understand and appreciate the usefulness of the model and assess the validity and the scope of the results in a more reliable manner.

ABMs have been developed in great detail in areas of sociology, in the analysis of social influence, cooperation, social norms, the emergence of conventions and cultural, and opinion dynamics, to name a few. While there are good reviews on ABMs in sociology (Bianchi and Squazzoni, 2015; Conte and Paolucci, 2014), an overview of data resources that could help modelers to move towards data-driven directions is still lacking. In what follows, we will discuss potential data sources that can be used in data-driven ABM.

Surveys. Publicly available surveys such as the European Social Survey (ESS) are the most common approach for initialization of the models or validations. For example, Åberg and Hedström (2011) used unemployment data combined with socio-demographic information of urban neighborhood to explain the impact of social influence on youth unemployment. In another example Grow and Van Bavel (2015) use ESS to model the relationship between assortative mating and gender inequality in higher education.

Digital media. Social media data sets are exceedingly being used by the CSS community to extract information about the ideology and attitude of users and how they shape and evolve over time. For example, sentiment analysis on social media platforms can help infer the users' political and ideological leaning, which will inform the agent's cognition and behavioral properties (Waldherr and Wettstein, 2019). Analyzing the agents' actions over time could be harvested to infer behavioral aspects such as opinion dynamics and polarization.

Network data. Information on who follows whom or friendship networks in online social networks can be used to create more realistic interaction scenarios. This information combined with recent advances in identifying gender or ethnicity of the users from the names or images (Karimi et al., 2016) can be used to identify how different groups of people interact based on their socio-demographic attributes. For example, by accounting for homophily in social interactions based on empirical evidence, one can model the spread and adoption of norms between majority and minority groups more realistically (Kohne et al., 2020).

Timing of social interactions can also significantly influence diffusion processes (Karimi and Holme, 2013), and thus, temporal networks are hugely instrumental in building realistic models of social interactions over time for studying dynamical processes such as the spread of information, norms, culture, cooperation, coordination, and innovation diffusion (Holme, 2015).

*Crowd-sourced data.* Conducting large-scale surveys and focused groups using online participation enables researchers to achieve large-scale data to calibrate ABM models or evaluate the outcomes in a viable manner (Behrend et al., 2011). For example, by asking people about their local neighborhood and their estimate about a prevalence of a certain minority group, one can estimate the perception bias of people based on their social network (Lee et al., 2019) and use this information to model disinformation spreading or mitigation strategies to prevent formation of biases.

Call data and wearable sensors. Found data such as data on mobile phone calls combined with socio-demographic information of the users or the regions can be used to model the information network and explore various dynamical aspects of human society such as the spread of disease (Gozzi et al., 2020). In more controlled settings, wearable sensors such as sociopattern sensors can be deployed or used to infer the communication structure in face-toface interactions and study how it could impact performance of students at schools (Fournet and Barrat, 2014).

*Scholarly databases.* Large-scale scholarly publications such as Web of Science or DBLP database can be used to model how scholars move and find new collaborators, how ideas spread, and how a new field of research emerges.

Urban mobility and census data. Publicly available data on urban mobility can be used to model communication and movement of people in space and time, e.g., to study how offenders communicate and move in a city (Rosés et al., 2018). Combining census data, panel data and mobility data could help to better model inequality and racial segregation in cities (Crooks, 2010).

# 3. Heuristics and Modeling

In this section we will walk through elementary heuristics in some recent agent-based models in economics and finance. We use the notion of the heuristic as a strategy that ignores part of the information to ease the process of decision making (Gigerenzer and Gaissmaier, 2011). An extensive survey of action rules (behavioral heuristics) in agent-based models can be found in Dosi et al. (2020).

Heuristics in financial models have long been centered around learning and adaptation in a multi-agent setting and how this interferes with the financial market as a whole (see for instance LeBaron, 2002). Financial agents perform trades in financial assets and interact with each other either directly via social learning processes, or indirectly, via the price mechanism. Anufriev and Hommes (2012) develop heuristics to explain coordination of individual behavior as observed in laboratory financial markets. Agents in financial models range from passive automations without cognitive functions (i.e. zero-intelligence agents) to active data-gathering decision makers with learning capacity (i.e. agents with microfunded rules of behavior, such as in Iori and Porter, 2018). Financial agents are still developed as optimizers of some objective (or criteria), such as debt/equity ratio (Fischer and Riedler, 2014), utility, profit, or other criteria. Optimization algorithms rely on well defined objective functions, usually of additive or exponential form, of weighted combinations of the criteria under consideration (An, 2012).

Learning in financial models can be based on probabilistic learning (Lux,

2009b), where people choose between prospects based upon probabilistic alternatives involving risk, such as in Polach and Kukacka (2019). In addition, "probabilistic" agents with adaptive learning might be constructed, such that they adopt strategies based on relative performance to some benchmark or, alternatively, source from an evolving pool of strategies, formed by a mix of chartist and fundamentalist features (Mandes and Winker, 2017) with anchoring (Polach and Kukacka, 2019) and herding (Vidal-Tomás and Alfarano, 2020). Probabilistic learning has traditionally been implemented in the Bayesian way, while adaptive learning rests upon an evolutionary computation with components of genetic algorithms and artificial neural networks. Heuristics in financial models and institutions are focused on simple rules for modeling the flow of funding between cash providers, dealers, and hedge funds as exemplified by Bookstaber et al. (2018).

A wide variety of behavioral heuristics have been developed for modeling agents in economic settings. For instance, Vallino (2014) applies a simple trial-and-error heuristic on procedural rationality of agents in a public choice setting where agents utilize common pool resources (i.e. forests) by adopting their utilization strategies upon changes they observe in the availability of the resources. These agents are boundedly rational (i.e., they do not optimize their objective functions) and operate as satisficers (Simon, 1959) within endogenous institutional setting. Then, there is a trust game simulation experiment (Gazda et al., 2012) of adaptive agent's behavior, where agents are placed in an exogenous and static institutional framework. Authors use a set of behavioral components and ad-hoc heuristics to define agents' actions. Both examples are implemented in the highly applicable NetLogo environment.

Delli Gatti et al. (2011) argue in favor of agent-based models with many types of agents with a small set of behaviors for each type. According to the authors, heuristic rules, in principle, push the heterogeneity of ad-hoc rules to infinity. The authors further stress that agents, in reality, adopt a small portion of behavioral rules and they do not behave in isolation, but via rules for social interaction (i.e. direct or indirect, local or global) with other agents, through learning and mimicking. As a result, agents regularly reformulate expectations about their future states and decisions, and/or impact own or others' preferences and/or available choices.

Gurgone et al. (2018) build on the approach suggested by Delli Gatti et al. (2011) by (i.) adding a model of the interbank market in which loans and interest rates are determined endogenously and (ii.) specifying the sectoral structure of the economy. Their model consists of households, firms, banks, a government and a central bank. Relations in the model are implemented by heuristic rules via some binding equations. For instance, households follow a rule of thumb to determine consumption (linear in relation to available resources); firms hire labor in a 4-step heuristic and set their liquidity needs in advance (i.e. demand for loans becomes a Markov process); Firms charge mark-up prices for their products defined by mark-up rule based on their market share; wages are adopted rule-based, taking into account a linear combination of moving average(s) of inflation and unemployment; relations between government, central bank, banks and firms are determined on financial markets and banking sector via heuristic rules for the provision of liquidity, borrowing constraints, repayment rules, tax collection rules; banks use probabilistic approach (i.e. logistic default probability based on borrower's leverage) to model risk of their borrowers and they use balance-sheet heuristics to monitor liquidity needs and regulatory requirements (i.e. prudential rules).

EURACE (Holcombe et al., 2013) is a large scale agent-based model of European economy related to labor markets, industry evolution, and credit markets. The model consists of nine types of agents (firms, households, investment goods producers, malls, banks, clearing houses, government, central bank, and Eurostat) that operate in various interrelated markets with institutional agents who assess economic indicators and transmit this information back to economic agents. Behavioral heuristics in the model refer to movement, communication, work, consumption decisions, learning, investment decisions, and speculations on financial markets. Agents are boundedly rational with limited capacity for information assimilation. They use simple rules and can learn to adapt to a changing economic environment. For instance, firms plan inventories based upon expectations of future sales obtained by regressions on historical sales; labour is hired via a set of search-match heuristics applied on firms and households; pricing of consumption goods is based on simple mark-up rules; consumers purchasing decisions are random and probabilistic in nature driven by purchasing probabilities they attach to different products based on prices; central bank uses simple heuristics and Basel rules (i.e. via a Deferred Settlement System) to provide liquidity that banks need to finance loans to firms; etc.

Heuristics have a critical impact on the behavior of agents in the model. They need to be carefully implemented such that they capture main behavioral attributes of agents under consideration to facilitate their decision making within a particular institutional setting. Moreover, according to Dosi et al. (2020) heuristics may provide a more accurate and robust tool for modeling action also within in an uncertain environment than sophisticated techniques

### 4. Economic Networks

The financial crisis of 2008 has led to a drastic rise in the awareness of the importance of network properties of economic systems. The structure of economic networks plays an important role for the robustness of the global economy, for understanding structural change and shocks, and for identifying conflicts between global efficiency and individual interests (Schweitzer et al., 2009). For ABMs this means that besides modeling the behavior of agents we have to model realistic networks of interactions where these are relevant for the dynamics of the system. This is not an easy endeavor since this mostly necessitates the use of large-scale data sets, which are only gradually becoming available, together with large-scale simulations. This section therefore will to a large extend focus on advances of structure identification in economic networks before pointing to a few agent-based approaches that incorporate network structure explicitly.

Small to medium scale social networks have been studied in sociology for a long time and have uncovered basic properties of social interactions (see Freeman, 2004, for an overview). Larger scale systems have however only been analyzed after the increase of computing capacity in the 90s, and in fact notable studies from that time included the analysis of the structure of the world wide web (Albert et al., 1999). One application of this new approach were studies on cascades (Watts, 2002). In economics such cascade models (which are very similar to models for epidemics, see, e.g. Eubank et al. (2003)) have been augmented for the analysis of contagious effects in financial markets. This part however will be discussed in more detail in section 5. Here, we will discuss some recent developments that aim at describing economic networks in general.

By today networks have become accepted as mainstream research topics in economics, as they have been identified as decisive influences on economic growth (Acemoglu et al., 2012; Jackson et al., 2017). Even some textbooks have focused on networks in economics (Jackson, 2008; Easley and Kleinberg, 2010). Nevertheless, it is necessary to understand that much of today's research is actually based on previous works in sociology, physics and computer science. For example, networks of firms have been analyzed by Uzzi (1996) and Gulati and Gargiulo (1999) from a sociologist's perspective. Also, the analysis of corporate boards and firm networks (Kogut and Walker, 2001) overlaps with research in management science (Devos et al., 2009; Zona et al., 2018), corporate finance (Duchin et al., 2010; Herskovic, 2018), and interdisciplinary research in physics and computer science (Battiston and Catanzaro, 2004; Vitali et al., 2011).<sup>2</sup>

There are several approaches where known agent-based models have been extended to incorporate network structures between agents explicitly, for example in herding models (Alfarano and Milaković, 2009), economic games (Wilhite, 2014), or Schelling's well known segregation model (Fagiolo et al., 2007; Schelling, 1971). These approaches show under which circumstances network structure influences macroscopic outcomes, yet they do not answer which of the proposed structures we find in reality, how they formed, and how they might develop in the future.

The agent-based approaches to economic networks are also a response to the limitations of traditional macroeconomic models (DSGE) in explaining interaction effects, especially with the financial sector, and crises, in particular of course that of 2008 (LeBaron and Tesfatsion, 2008; Dosi and Roventini, 2019). Hence, when it comes to modeling larger economic systems there are currently two overlapping approaches. On the one side there are classical ABMs that describe economic systems where the agents' behavior is mostly calibrated to empirical data, one noticeable example is the model for the European economy by Deissenberg et al. (2008). While many models include a matching of agents in different markets the resulting network structure of these matches is typically not of major importance (see Dawid and Delli Gatti, 2018, for an overview).

On the other hand there are models for specific parts of economic systems which are often completely data-driven, for example describing the production network of a country like Japan (Krichene et al., 2019). Further examples are the analysis of world trade (Fagiolo et al., 2009) and sector-based input-output networks (Cerina et al., 2015; Klimek et al., 2019). While for many economic networks data of bilateral flows or exposures is available,

<sup>&</sup>lt;sup>2</sup>Further important research outside the scope of this overview has been done by analyzing supply chains and logistics as well as by applying Game Theory to models of network formation.

some markets have been modeled indirectly via the use of time series data and the derivation of correlation-based networks. An example for the latter is the analysis of the dependencies in financial markets for which many different approaches exist (Musmeci et al., 2015; Tumminello et al., 2005; Raddant and Kenett, 2021; Diebold and Yilmaz, 2014; Billio et al., 2012)

Arguably, most of these contributions are not ABMs, they are empirical studies on economic networks. This distinction is however sometimes superficial. The reason is that when we want to estimate the effects that have led to a particular network structure we typically revert back to simulation based inference of these effects, for example in exponential random graph models or the stochastic actor based approach (Strauss and Ikeda, 1990; Wasserman and Pattinson, 1996; Snijders, 2001). Hence, we estimate which behavior on the level of agents has likely led to an observed outcome with respect to network structure.

Noticeably, there is one specific field of research where the agent-based modeling of agents' behavior and connectivity is mostly done jointly, namely in describing the relationships of firms with financial institutions. While the analysis for the case of Italy (De Masi and Gallegati, 2011) is still mostly an empirical study, there are more elaborate models for the case of Spain (Lux, 2016) and an explicit agent-based model for the case of Japan (Bargigli et al., 2020) where network structure becomes one of the key calibration targets.

#### 5. Agent-based Models and Financial Stability

The financial system is a classic example of a complex system. Its dynamic is difficult to predict due to the interconnectedness and interdependences of its parts which give rise to nonlinearities, tipping points, adaptation and feedback loops, among other features. Many empirical financial phenomena, such as fat tailed return distributions, booms and bursts cycles in asset price, volatility clustering, runs on funding, asset fire sales, and financial crisis are difficult to explain by traditional economic models based on the conjecture that the actions of fully rational agents are driven by market fundamentals. ABMs instead are built on the assumption that agents are boundedly rational, interacting and heterogenous. Agents idiosyncratic actions can become coordinated, either via direct reciprocal interactions or by indirect reaction to common signals, and lead to large aggregate fluctuations and macro level instabilities. By simulating how banks, investors regulators, and other players interact with each other, and with the real economy, ABMs have been instrumental in gaining a deeper understanding of how extreme events in real-world financial markets can arise.

Earlier ABM work has focused predominantly on the role of the microstructure of exchanges (execution policies, order types, execution fees, etc), market transparency, and the interaction among heterogeneous strategies, on the volatility of stock prices and the dynamics of order flows. ABMs simulations have shown that stock market models do not generally select the rational, fundamentalist strategy and that simple technical trading rules, such as chartist strategies, as well as herding behavior, may survive. These direct and indirect interactions, by acting as a coordination device of agents trading decisions, can lead to wild price fluctuations in asset prices and memory effects in order flows.

ABMs have been helpful not only to identify the mechanisms that lead to instabilities in financial markets, but also to evaluate policies designed to mitigate them. Pellizzari and Westerhoff (2009) for example have studied the effect of transaction taxes in an agent-based model in which central dealership or continuous double auction are used as a clearing mechanism. Their work show that in the former case, the volatility of the market can be significantly reduced via the imposition of a transaction tax, however in the second setting the tax would reduce market liquidity neutralizing any improvement in price stability. Ladley et al. (2015) have shown that centralising markets can lead to higher price volatility and less resilience to shocks because it increases the equilibrium proportion of unskilled traders. Kovaleva and Iori (2015) have studied the effects of pre-trade quote transparency on market quality in an artificial limit order market where traders react to the unbalance in demand and supply posted in the limit order book. Their simulations show that full quote transparency leads to high transaction costs that dampen trading volume. While the exogenous restrictions of displayed depth does not improve market quality, endogenous restrictions by means of iceberg orders are effective in balancing the limit order book, reducing transaction costs, maintaining higher liquidity, low volatility, and overall enhancing price discovery.

In recent years a large part of the ABM financial literature has shifted to the study of systemic risk and in particular to the analysis of the extent to which default cascades are affected by the connectivity among banks. The inter-bank credit market is an important means through which commercial banks cover short-falls in liquidity. By borrowing from banks with surplus liquidity, banks which face a temporary shortfall can survive as a result of inter-bank credit. This represents risk-sharing and, in and of itself, should help keep down the incidence of failures in the system. While there is an ex ante sense in which inter-bank credit can play a stabilizing role several studies have emphasized the ex post destabilizing implications of one banks failure as the inter-bank credit system is susceptible to contagion. In an early paper, Iori et al. (2006) have shown that when banks are more heterogeneous in their characteristics (either in size or appetite for risk), increasing interbank connectivity initially decreases the probability of an individual bank default to occur. However, if defaults occur they are more likely to initiate large default cascades. Thus, the relationship between the level of interconnectedness in the interbank markets and financial contagion is non-monotonic. Gai and Kapadia (2010) have further shown that increasing the connectivity of the banking network the system become more resilient to contagion triggered by the default of a random bank, but more fragile following the failure of highly connected nodes. A number of authors have explored the role of the interbank network structure on contagion (Nier et al. (2007), Karimi and Raddant (2016), Georg (2013), Krause and Giansante (2012), Lenzu and Tedeschi (2012)) and compared how defaults propagate on scale-free, random, small world and core periphery networks under different modeling assumptions. Battiston et al. (2012) have developed a novel methodology to quantify the unrolling of distress between lenders and borrowers even before a borrowers default, as creditors who are exposed to distressed debtors suffer a deterioration of their credit quality. In addition to direct knock-on effects, the market impact of liquidating overlapping portfolios, in non-perfectly liquid markets, can amplify financial instabilities triggered by distressed banks. The liquidation pressure, typically driven by binding leverage constraints, can in fact lead to fire sales and create new contagion channels, as shown by Caccioli et al. (2014) and Aymanns and Farmer (2015). A third source of contagion has been identified in liquidity hoarding (Anand et al., 2013). A number of authors have in fact shown, using multi-layered networks, that the interaction of these different contagion channels can substantially amplify the effect of each individual one (Klimek et al., 2015; Montagna and Kok, 2016).

An increasing number of agent-based models have considered the interrelation between the financial market and the real economy, and explored the potential for ABMs to test the effectiveness of micro and macroprudential polices, such as Basel II and Basel III. Ashraf et al. (2017) have studied the role of loan-to-value ratios and static capital-adequacy regulation showing that less strict micro-prudential bank regulations allow the economy to recover faster from a crisis. Cincotti et al. (2012) have shown that lower capitaladequacy ratios can spur growth in the short-run, but lead to more serious economic downturns in the long-run as the number of bankruptcies of highly leveraged banks and firms grow, leading to credit rationing. Their simulations show that dynamic adjustment of capital requirements is generally more successful than fixed tight capital requirements in stabilizing the economy and improving the macroeconomic performance. Popoyan et al. (2017) and Krug et al. (2015) have shown that the components of Basel III are non-additive: the inclusion of an additional lever does not always improve the performance of the macroprudential regulation and their joint impact is more effective than the sum of their individual contributions. (Assenza et al., 2018) have tested two macro-prudential policies, a modification of the maximum leverage ratio and the required liquidity ratio and shown that the former is more effective than the latter in terms of reducing the frequency of crises. However, no difference emergence as far as the duration of the crises is concerned. Gurgone et al. (2018) allow banks to set endogenously their leverage and capital targets (within the bounds imposed by regulators) and as a result, when financial downturns occur, banks tend to amplify them by withholding liquidity from the interbank and credit markets and by seeking higher interest rates on the funds which they make available. This financial amplification mechanism (see also Delli Gatti et al., 2010) is exacerbated by the pro-cyclical effects of the prudential regulations. Alternative resolution mechanisms of banking crises have been investigated by Klimek et al. (2015) who find that liquidation is the best policy during expansions, whereas bail in achieve better financial and economic stability during recessions. Poledna and Thurner (2016) have proposed the introduction of a tax on individual transactions, proportional to their marginal contribution to overall systemic risk. Their simulations demonstrates that such Systemic Risk Tax leads to a self-organized restructuring of the financial network essentially eliminating the risk of banks collapsing. Notably, the restructuring occurs without loss of transaction volume and efficiency. On the contrary, when a Tobin tax or Basel III capital surcharges are imposed on SIFIs, the ABM leads to an increases the cost of credit to the real economy.

Overall these studies have shown that Agent Based Models are powerful tools to understand the mechanism that lead to observed stylized fact in financial markets and to explain the unfolding of systemic risk in financial systems. By running a large number of simulations, changing the behavioural rules and the model parameters, ABM can generate a rich set of data to evaluate the consequences of shocks, that can emerge endogenously or be imposed exogenously, and explore the effect of stabilization policies under counterfactual scenarios. Particularly for macro-finance applications, where data are scarce and experiments are limited, ABM offer invaluable computational laboratories for evaluating what-if scenarios. ABMs have so far mostly been used to generate insights and qualitative descriptions of scenario that may occur rather than quantitative forecasts. However, there have been some successful examples of forecasting with empirically calibrated financial agent-based models such as the work of Braun-Munzinger et al. (2018) on the corporate bonds markets. ABM Simulation results can vary dramatically depending on which assumptions are used. As granular data sets of financial transactions are starting to be collected, it will become possible to test the realism of the behavioral assumptions and of the rules of interactions in the agent-based models. A careful calibration of these models to micro level market data will enable the full potential of ABMs, as effective tools for assisting policy makers and market participants in their decision-making processes, to be exploited.

# 6. Controlled Laboratory Experiments

Behavioral economics brings psychological foundations to economics aiming at better explaining economic phenomena. The emphasis of behavioural economics is basically on the effects that psychological, cognitive, emotional, cultural, and social factors have on individual as well as collective decision making (see, e.g., Thaler, 2016). Traditionally, behavioural economics has largely relied on evidence generated by controlled laboratory experiments with human subjects, where all those behavioural aspects are naturally considered (see, e.g., Smith, 1989).

Contrary to the paradigm of rationality, experimental economics has

shown that the heterogeneity of human subjects (e.g. different risk attitude, preferences or cultural background), their different degrees of bounded rationality and cognitive capabilities strongly influence their decisions. ABM builds upon a similar background, namely the pre-analytical vision that the assumption of heterogeneous interacting agents with different and given degrees of bounded rationality better captures micro-level properties of (macro) economic phenomena. ABM and experimental economics share, therefore, the departure from the representative rational optimizing agent as a fundamental building block for the analysis of economic phenomena. Whereas ABM assumes the heterogeneity of economic agents, controlled human subject experiments unavoidably deal with it. It is, thus, natural combining these two approaches, studying potential synergies and complementaries in dealing with the behavior and interaction of heterogeneous agents. Despite the long tradition of the experimental and ABM approaches to describe economic phenomena, it is only recently that several contribution employed the findings of controlled experiments on the determinants of human behavior in the design of artificial agents in ABM. Fewer are, instead, the contributions of ABM in complementing experimental economics.

We claim that an interesting new literature has recently emerged, attempting to combine experimental and computational methodologies, thereby taking advantage of the synergies between them. Based on this literature in particular Duffy (2006) describes the common characteristics shared by ABM and controlled human subjects experiments: (i.) a bottom-up modeling approach, contrary to top-down representative agent models, which naturally cope with heterogeneous agents; (ii.) complex interactions among agents, assuming that the aggregate behavior of interacting agents does not necessarily coincide with the behavior of the individual; and (iii.) agents which posses various degrees of bounded rationality.

In this vein, Contini et al. (2006) list several examples of the complementarities between ABM and human subjects experiments. ABM can help explaining the behavior observed in human subject experiments and, at the same time, experimental data can be employed in calibrating and validating ABM. Conducting controlled laboratory experiments with human subjects imply the existence of budget and time constraints, that imposes limits to the number of participants (agents) and periods, that do not apply to ABM simulations. When designing a laboratory experiment, a calibrated simulation can guide the experimentalist on the sensitivity of the subjects behavior to changes in the key parameters of the experimental design (see, e.g., Arifovic and Petersen, 2017). Additionally, ABM simulations can be used for replicating human-based experiments using the experimental initial conditions, for increasing the number of periods and/or the number subjects, or for giving the opportunity to conduct a robustness test of the experimental findings.

Taking stock of that, however, we find that in most of the contributions, the combination of experimental and ABM simulations focused on explaining experimental data using ABM simulations, whereas we do not find many examples where experimental data served to complement the ABM findings. We think that one of the reason lies in the higher flexibility of computational agent-based models as compared to experimental settings, given the strong constrains in dealing with controlled human subjects experiments. Additionally, we should consider that nowadays ABMs have become much more complex than experimental settings, embracing large macro-simulations of the entire economy.

Despite their simplicity, controlled laboratory experiments allow for collecting data that in the real world are not available, like expectations formation or cognitive abilities or biases of human subjects that can be used to endow artificial agents in ABMs with more realistic characteristics and behavior following, for example, adapting learning rules.

#### 7. Estimation of Agent-Based Models

Agent-based models have been developed for different purposes. Historically, some of the first examples of disaggregated models of economic systems have been microsimulations (pioneered, e.g., by Orcutt et al., 1961) that were mainly developed as decision support system for economic policy. While these models are usually carefully calibrated using empirical distributions of agents' characteristics (such as the age structure of a population to forecast the development of pension expenditures), they have not been subject to rigorous econometric validations. Indeed, the idea of estimation seems alien to this class of models as they are dominated by both institutional detail and a close mapping of certain empirical attributes of the population that are deemed important for a certain type of policy question.<sup>3</sup> There are typically few behavioral relationships and those that exist are well-represented by statistical averages over the large underlying populations (e.g., retirement age, divorce rates etc.). In contrast, the more recent branch of theoretically motivated ABMs that emerged since the 1990s have a different relationship with data: With few exceptions, the motivation of these ABMs has been the desire to explain via behavioral assumptions certain stylized facts that more aggregate, traditional models had left unexplained. The guiding idea of this literature is that certain salient features of our economic reality can only be explained as the outcome of a process of self-organization of the activity of a large ensemble of interacting, heterogeneous agents (see, e.g., Gallegati and Kirman, 2012). The first brand of such models has mainly addressed the well-known but mysterious stylized facts of financial markets such as the particular broad distribution of returns (fat tails) and the extremely large correlation in all measures of their range of fluctuations (clustered volatility), see also Lux (2009b).

<sup>&</sup>lt;sup>3</sup>The International Journal of Microsimulation might be consulted for an overview over this rich universe of agent-based models for policy applications that almost constitutes a parallel world to the more theoretical ABMs developed in academia.

Slightly later, a related literature on macroeconomic ABMs has been developed (e.g. Dawid and Delli Gatti, 2018) which addresses macroeconomic stylized facts such as the distribution of booms and recessions, and crosscorrelations between key macroeconomic variables. Other areas of intense ABM research include industrial dynamics (e.g. Axtell, 2018), and the emergence of stratified distributions of income and wealth (Chakraborti, 2011). With the orientation at measurable stylized facts, empirical validation and estimation of their parameters should be a top priority of the ABM community. Indeed, the justification of the relatively heavy apparatus of models with a multitude (or at least multiple groups) of agents rests on its capacity to explain data better than traditional approaches using structural equations without micro foundations, or the representative agent models that have been particularly popular in macroeconomics. In some areas, it seems easy to score as goal for ABMs as, for instance, important and well-documented regularities such as the size distribution of firms and the Pareto-type distribution of income and wealth defy any attempt of their explanation without disaggregated agents. Other stylized facts like those of financial data had in the pre-ABM literature only be explained in a tautological way: If returns are fat tailed and come with clustered volatility, so must have been the distribution of news on which they are based. More demanding is the task in macroeconomics where there exist well-established models at least for the cross-sectional patterns characteristic of business cycles (although the performance of the traditional DSGE models is not really considered satisfactory, see also Stiglitz (2018)).

Estimation of ABMs is, for most models of the currently available literature, methodologically straight forward, but practically often difficult. In terms of statistical methodology, the possibility of identification of parameters is guaranteed because most ABMs as they exist are Markov processes (a fact emphasized by Aoki, 1998). The nonlinearities inherent in an ABM framework also typically guarantee that problems such as colinearity are not an issue, at least in principle. However, the proliferation of parameters in many ABMs can easily lead to near-colinearity or parameters, that fail to exert much influence on any statistic used in an estimation algorithm (see the experiments in Lux and Zwinkels, 2018). Rigorous estimation should therefore, be a most welcome device to impose discipline on ABM modeling, and estimation results should be brought to good use in model development (e.g., when irrelevant parameters are encountered in an estimation).

The focus on stylized facts as a motivation to develop ABMs in the first place, suggests an empirical approach that uses the available knowledge on interesting statistics of the data: This has often made the generalized Method of Moments (GMM) or Simulated Method of Moments (SMM) the methodology of choice.<sup>4</sup> Examples include Jang (2015), Grazzini and Richiardi (2015), Chen and Lux (2018) or Franke and Westerhoff (2012). Simulation-based estimation seems to suggest itself since the explanatory power of ABMs is mostly explored via Monte Carlo simulations anyway. GMM and SMM also dispense with the necessity of a closed-form solution or numerical approximation for the likelihood which is almost never available in ABMs (an exception is the model estimated in Lux 2009a, 2012). The major drawback of GMM/SMM is a much lower efficiency of the resulting estimates than under a maximum likelihood approach. If the likelihood can be formulated but not solved explicitly, stochastic approximations of the likelihood via a sequential Monte Carlo algorithm or particle filter would be a possibility (see also Lux, 2018). In this approach, a swarm of candidate parameter vectors is updated through the iterated computation of their likelihood values via importance sampling and the averaging over the active particles in each time step provides the approximation of the likelihood function. Again, this approach is computation-intensive as it uses simulations of a large number of replications of the model (with different parameter values), but it provides a higher effi-

 $<sup>^4\</sup>mathrm{A}$  more complete review of estimation techniques for ABMs can be found in Lux and Zwinkels (2018).

ciency of the so attained parameter estimates than GMM/SMM. Since in this framework, the ABM is interpreted as a state-space model with both hidden variables and measurable variables, another advantage is that the particle filter allows to identify the dynamic evolution of hidden variables. These could be the distribution of expectations, strategies or attributes among agents, and would often be of immediate economic interest. Sequential Monte Carlo can be used in frequentist estimation as well as in a Bayesian context (see also Berschinger and Mozzhorin, 2020; Lux, 2020).

#### 8. Outlook and Future Directions

There are numerous promising avenues for research on agent-based models, some have already been touched upon in the previous sections. A particular strength of ABM has always been its flexibility towards the application to new problems. While certain classes of models have been established in fields like macroeconomics or financial markets, ABM has always been a transdisciplinary methodology that can be adapted to problems with different rules, interaction mechanisms and behavioral phenomena.

A current example are data-driven models that have been developed for the COVID-19 pandemic. Here ABMs can be an effective tool to model human interactions and disease dynamics over space and time and offer realistic predictions in terms of the scale of an outbreak or the effectiveness of different interventions (Goldstein et al., 2020; Squazzoni et al., 2020).

ABMs can also be used to study problems that result from the increased use of AI, for example the societal impact of ranking algorithms, recommender systems and its possible reinforcements of social inequalities and biases. In situations in which the given data is noisy or biased, ABMs can be used to generate priors to produce scenarios for machine learning algorithms in a semi-supervised manner to reduce errors and prevent the amplification of distortions. Also, once artificial agents have been designed based on the behavior of human subjects, they can be implemented in large scale simulators (see Dosi et al., 2020). Such synergy between ABM and experimental methodology is at its infancy and, in our opinion, constitutes an exciting avenue of future research.

Further research is also needed on the estimation of ABMs, since not too much is known about the pros and cons of different methods. Available models have mostly allowed for at least the formulation and stochastic approximation of a likelihood function. When models become more complex, such approximations will often not be feasible anymore. In such cases, a promising tool - besides GMM/SMM - should be Approximate Bayesian Computation (ABC). This framework uses measurements (moments) of the data other than the likelihood (Sisson et al., 2005; Toni et al., 2008), and allows to approximate the posterior distribution of the parameters via a rejection sampling or Markov Chain Monte Carlo algorithm (see also Csillry et al., 2010).

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### References

Åberg, Y., Hedström, P., 2011. Youth unemployment: a self-reinforcing process? In: Demeulenaere, P. (Ed.), Analytical sociology and social mechanisms. Cambridge University Press.

- Acemoglu, D., Carvalho, V., Ozdaglar, A., Tahbaz-Salehi, A., 2012. The network origins of aggregate fluctuations. Econometrica 80 (5), 1977–2016.
- Albert, R., Jeong, H., Barabási, A.-L., 1999. Diameter of the world-wide web. Nature 401, 130–131.
- Alfarano, S., Milaković, M., 2009. Network structure and N-dependence in agent-based herding models. Journal of Economic Dynamics and Control 33, 78–92.
- An, L., 2012. Modeling human decisions in coupled human and natural systems: Review of agent-based models. Ecological Modelling 229, 25–36.
- Anand, K., Gai, P., Kapadia, S., Brennan, S., Willison, M., 2013. A network model of financial system resilience. Journal of Economic Behavior & Organization 85, 219–235.
- Anufriev, M., Hommes, C., 2012. Evolution of market heuristics. Knowledge Engineering Review 27 (2), 255–271.
- Aoki, M., 1998. New approaches to macroeconomic modeling: evolutionary stochastic dynamics, multiple equilibria, and externalities as field effects. Oxford University Press.
- Arifovic, J., Petersen, L., 2017. Stabilizing expectations at the zero lower bound: Experimental evidence. Journal of Economic Dynamics and Control 82, 21 – 43.
- Ashraf, Q., Gershman, B., Howitt, P., 2017. Banks, market organization, and macroeconomic performance: an agent-based computational analysis. Journal of Economic Behavior & Organization 135, 143–180.
- Assenza, T., Cardaci, A., Delli Gatti, D., Grazzini, J., 2018. Policy experiments in an agent-based model with credit networks. Economics E-Journal 47.

- Axtell, R., 2018. Endogenous firm dynamics and labor flows via heterogeneous agents. In: Hommes, C., LeBaron, B. (Eds.), Handbook of Computational Economics. Vol. 4. North-Holland, Amsterdam.
- Aymanns, C., Farmer, J. D., 2015. The dynamics of the leverage cycle. Journal of Economic Dynamics and Control 50, 155–179.
- Bargigli, L., Riccetti, L., Russo, A., Gallegati, M., 2020. Network calibration and metamodeling of a financial accelerator agent based model. J Econ Interact Coord 15, 413–440.
- Battiston, S., Catanzaro, M., 2004. Statistical properties of corporate board and director networks. European Physical Journal B 38, 345–352.
- Battiston, S., Puliga, M., Kaushik, R., Tasca, P., Caldarelli, G., 2012. Debtrank: Too central to fail? financial networks, the fed and systemic risk. Scientific reports 2, 541.
- Behrend, T. S., Sharek, D. J., Meade, A. W., Wiebe, E. N., 2011. The viability of crowdsourcing for survey research. Behavior research methods 43 (800).
- Berschinger, N., Mozzhorin, I., 2020. Bayesian Estimation And Likelihoodbased Comparison Of Agent-based Volatility Models. Journal of Economic Interaction and Coordination, in press.
- Bianchi, F., Squazzoni, F., 2015. Agent-based models in sociology. Wiley Interdisciplinary Reviews: Computational Statistics 7 (4), 284–306.
- Billio, M., Getmansky, M., Lo, A. W., Pelizzon, L., 2012. Econometric measures of connectedness and systemic risk in the finance and insurance sectors. Journal of Financial Economics 104 (3), 535–559.

- Bookstaber, R., Paddrik, M., Tivnan, B., 2018. An agent-based model for financial vulnerability. Journal of Economic Interaction and Coordination 13 (2), 433–466.
- Braun-Munzinger, K., Liu, Z., Turrell, A., 2018. An agent-based model of corporate bond trading. Quantitative Finance 18 (4), 591–608.
- Caccioli, F., Shrestha, M., Moore, C., Farmer, J. D., 2014. Stability analysis of financial contagion due to overlapping portfolios. Journal of Banking & Finance 46, 233–245.
- Cerina, F., Zhu, Z., Chessa, A., Riccaboni, M., 2015. World input-output network. PLoS ONE 10 (7), e0134025.
- Chakraborti, A., 2011. Econophysics Review: II. Agent-Based Models. Quantitative Finance 11, 1013–1041.
- Chen, Z., Lux, T., 2018. Estimation of Sentiment Effects in Financial Markets: A Simulated Method Of Moments Approach. Computational Economics 52, 711–744.
- Cincotti, S., Raberto, M., Teglio, A., 2012. Macroprudential policies in an agent-based artificial economy. Revue de l'OFCE (5), 205–234.
- Conte, R., Paolucci, M., 2014. On agent-based modeling and computational social science. Frontiers in Psychology 5, 668.
- Contini, B., Leombruni, R., Richiardi, M., 2006. Exploring a new expace: The complementarities between experimental economics and agent-based computational economics. Journal of Social Complexity 3, 13–22.
- Crooks, A. T., 2010. Constructing and implementing an agent-based model of residential segregation through vector GIS. International Journal of Geographical Information Science 24 (5), 661–675.

- Csillry, K., Blum, M., Gaggiotti, O., Franois, O., 07 2010. Approximate Bayesian Computation (ABC) in Practice. Trends in Ecology & Evolution 25, 410–8.
- Dawid, H., Delli Gatti, D., 2018. Agent-Based Macroeconomics. In: Hommes, C., LeBaron, B. (Eds.), Handbook of computational economics. Vol. 4. Elsevier.
- De Masi, G., Gallegati, M., 2011. Banks firms topology in Italy. Empirical Economics 43(2), 851–866.
- Deissenberg, C., van der Hoog, S., Dawid, H., 2008. EURACE: A massively parallel agent-based model of the European economy. Applied Mathematics and Computation 204 (2), 541–552.
- Delli Gatti, D., Desiderio, S., Gaffeo, E., Cirillo, P., Gallegati, M., 2011. Macroeconomics from the Bottom-up. Vol. 1. Springer Science & Business Media.
- Delli Gatti, D., Gallegati, M., Greenwald, B., Russo, A., Stiglitz, J. E., 2010. The financial accelerator in an evolving credit network. Journal of Economic Dynamics and Control 34 (9), 1627–1650.
- Devos, E., Prevost, A., Puthenpurackal, J., 2009. Are interlocked directors effective monitors? Financial Management 38, 861–887.
- Diebold, F. X., Yilmaz, K., 2014. On the network topology of variance decompositions: Measuring the connectedness of financial firms. Journal of Econometrics (182), 119–134.
- Dosi, G., Napoletano, M., Roventini, A., Stiglitz, J. E., Treibich, T., 2020. Rational heuristics? Expectations and behaviors in evolving economies with heterogeneous interacting agents. Economic Inquiry 58 (3), 1487– 1516.

- Dosi, G., Roventini, A., 2019. More is different ... and complex! The case for agent-based macroeconomics. J Evol Econ 29, 1–37.
- Duchin, R., Matsusaka, J. G., Ozbas, O., 2010. When are outside directors effective? Journal of Financial Economics 96, 195–214.
- Duffy, J., 2006. Agent-based models and human subject experiments. In: Tesfatsion, L., Judd, K. L. (Eds.), Handbook of Computational Economics, 1st Edition. Vol. 2. Elsevier.
- Easley, D., Kleinberg, J., 2010. Networks, Crowds, and Markets. Cambridge UP.
- Edmonds, B., 2017. Different modelling purposes. In: Edmonds, B., Meyer, R. (Eds.), Simulating Social Complexity. Understanding Complex Systems. Springer.
- Epstein, J. M., 2014. Agent\_Zero: Toward neurocognitive foundations for generative social science. Princeton University Press.
- Eubank, S., Guclu, H., Kumar, V. A., Marathe, M., Srinivasan, A., Toroczkai, Z., Wang, N., 2003. Modelling disease outbreak in realistic urban social networks. Nature 429, 180–184.
- Fagiolo, G., Reyes, J., Schiavo, S., Mar 2009. World-trade web: Topological properties, dynamics, and evolution. Phys. Rev. E 79, 036115.
- Fagiolo, G., Valente, M., Vriend, N. J., 2007. Segregation in networks. Journal of Economic Behavior & Organization 64, 316–336.
- Fischer, T., Riedler, J., 2014. Prices, debt and market structure in an agentbased model of the financial market. Journal of Economic Dynamics and Control 48, 95–120.
- Fournet, J., Barrat, A., 2014. Contact patterns among high school students. PloS one 9 (9), e107878.

- Franke, R., Westerhoff, F., 2012. Structural Stochastic Volatility In Asset Pricing Dynamics: Estimation And Model Contest. Journal of Economic Dynamics and Control 36 (8), 1193–1211.
- Freeman, L., 2004. The Development of Social Network Analysis. Empirical Press, Vancouver.
- Gai, P., Kapadia, S., 2010. Contagion in financial networks. Proceedings of the Royal Society A: Mathematical, Physical and Engineering Sciences 466 (2120), 2401–2423.
- Gallegati, M., Kirman, A., 2012. Reconstructing economics: Agent based models and complexity. Complexity Economics 1, 5–31.
- Gazda, V., Gróf, M., Horváth, J., Kubák, M., Rosival, T., 2012. Agent based model of a simple economy. Journal of Economic Interaction and Coordination 7 (2), 209–221.
- Georg, C.-P., 2013. The effect of the interbank network structure on contagion and common shocks. Journal of Banking & Finance 37 (7), 2216–2228.
- Gigerenzer, G., Gaissmaier, W., 2011. Heuristic decision making. Annual review of psychology 62, 451–482.
- Goldstein, G.-P., Morgunov, A., Nangalia, V., Rotkirch, A., 2020. Universal masking is urgent in the covid-19 pandemic: Seir and agent based models, empirical validation, policy recommendations. arXiv:2004.13553.
- Gozzi, N., Tizzoni, M., Chinazzi, M., Ferres, L., Vespignani, A., Perra, N., 2020. Estimating the effect of social inequalities in the mitigation of covid-19 across communities in santiago de chile. medRxiv 2020.10.08.20204750.
- Grazzini, J., Richiardi, M., 2015. Estimation of Ergodic Agent-Based Models by Simulated Minimum Distance. Journal of Economic Dynamics and Control 51, 148–165.

- Grow, A., Van Bavel, J., 2015. Assortative mating and the reversal of gender inequality in education in Europe: An agent-based model. PloS one 10 (6), e0127806.
- Gulati, R., Gargiulo, M., 1999. Where do interorganizational networks come from? American Journal of Sociology 104 (5), 1439–1493.
- Gurgone, A., Iori, G., Jafarey, S., 2018. The effects of interbank networks on efficiency and stability in a macroeconomic agent-based model. Journal of Economic Dynamics and Control 91, 257–288.
- Herskovic, B., 2018. Networks in production: asset pricing implications. Journal of Finance 73 (4), 1785–1818.
- Holcombe, M., Coakley, S., Kiran, M., Chin, S., Greenough, C., Worth, D., Cincotti, S., Raberto, M., Teglio, A., Deissenberg, C., et al., 2013. Largescale modeling of economic systems. Complex Systems 22 (2), 175–191.
- Holme, P., 2015. Modern temporal network theory: a colloquium. The European Physical Journal B 88 (234).
- Iori, G., Jafarey, S., Padilla, F., 2006. Systemic risk on the interbank market. Journal of Economic Behavior & Organization 61(4), 525542.
- Iori, G., Porter, J., 2018. Agent-based modeling for financial markets. In: The Oxford Handbook of Computational Economics and Finance. Oxford University Press.
- Jackson, M., Rogers, B., Zenou, Y., 2017. The economic consequence of social-network structure. Journal of Economic Literature 55 (1), 49–95.
- Jackson, M. O., 2008. Social and Economic Networks. Princeton U.P.
- Jang, T.-S., 2015. Identification of Social Interaction Effects in Financial Data. Computational Economics 45, 207–238.

- Karimi, F., Holme, P., 2013. Threshold model of cascades in empirical temporal networks. Physica A: Statistical Mechanics and its Applications 392 (16), 3476–3483.
- Karimi, F., Raddant, M., 2016. Cascades in real interbank markets. Computational Economics 47 (1), 49–66.
- Karimi, F., Wagner, C., Lemmerich, F., Jadidi, M., Strohmaier, M., 2016. Inferring gender from names on the web: A comparative evaluation of gender detection methods. In: Proceedings of the 25th International conference companion on World Wide Web. pp. 53–54.
- Klimek, P., Poledna, S., Farmer, J. D., Thurner, S., 2015. To bail-out or to bail-in? answers from an agent-based model. Journal of Economic Dynamics and Control 50, 144–154.
- Klimek, P., Poledna, S., Thurner, S., 2019. Quantifying economic resilience from input-output susceptibility to improve predictions of economic growth and recovery. Nature Communications 10, 1677.
- Kogut, B., Walker, G., 2001. The small world of Germany and the durability of national networks. American Sociological Review 66 (3), 317–335.
- Kohne, J., Gallagher, N., Kirgil, Z. M., Paolillo, R., Padmos, L., Karimi, F., 2020. The role of network structure and initial group norm distributions in norm conflict. In: Computational Conflict Research. Springer, Cham, pp. 113–140.
- Kovaleva, P., Iori, G., 2015. The impact of reduced pre-trade transparency regimes on market quality. Journal of Economic Dynamics and Control 57, 145162.
- Krause, A., Giansante, S., 2012. Interbank lending and the spread of bank failures: A network model of systemic risk. Journal of Economic Behavior & Organization 83 (3), 583–608.

- Krichene, H., Fujiwara, Y., Chakraborty, A., Arata, Y., Hiroyasu, I., Terai, M., 2019. The emergence of properties of the Japanese production network: How do listed firms choose their partners? Social Networks 59, 1–9.
- Krug, S., Lengnick, M., Wohltmann, H.-W., 2015. The impact of Basel III on financial (in) stability: an agent-based credit network approach. Quantitative Finance 15 (12), 1917–1932.
- Ladley, D., Lensberg, T., Palczewski, J., Schenk-Hoppé, K., 2015. Fragmentation and stability of markets. Journal of Economic Behavior & Organization 119, 466–481.
- Lazer, D. M., Pentland, A., Watts, D. J., Aral, S., Athey, S., Contractor, N., Freelon, D., Gonzalez-Bailon, S., King, G., Margetts, H., et al., 2020. Computational social science: Obstacles and opportunities. Science 369 (6507), 1060–1062.
- LeBaron, B., 2002. Short-memory traders and their impact on group learning in financial markets. Proceedings of the National Academy of Sciences 99 (suppl 3), 7201–7206.
- LeBaron, B., Tesfatsion, L., 2008. Modeling macroeconomies as open-ended dynamic systems of interacting agents. The American Economic Review 98 (2), 246–250.
- Lee, E., Karimi, F., Wagner, C., Jo, H.-H., Strohmaier, M., Galesic, M., 2019. Homophily and minority-group size explain perception biases in social networks. Nature human behaviour 3 (10), 1078–1087.
- Lenzu, S., Tedeschi, G., 2012. Systemic risk on different interbank network topologies. Physica A: Statistical Mechanics and its Applications 391 (18), 4331–4341.

- Lorenz, J., Neumann, M., Schröder, T., 2020. Individual attitude change and societal dynamics: Computational experiments with psychological theories. PsyArXiv 10.31234/osf.io/ebfvr.
- Lux, T., 2009a. Rational Forecasts or Social Opinion Dynamics? Identification of Interaction Effects in a Business Climate Survey. Journal of Economic Behavior & Organization 72, 638–655.
- Lux, T., 2009b. Stochastic behavioral asset pricing models and the stylized facts. In: Hens, T., Schenk-Hopp, K. (Eds.), Handbook of Financial Markets: Dynamics and Evolution. North-Holland, Ch. 3, pp. 161–215.
- Lux, T., 2012. Estimation of an agent-based model of investor sentiment formation in financial markets. Journal of Economic Dynamics and Control 36, 1284–1302.
- Lux, T., 2016. A model of the topology of the bank-firm credit network and its role as channel of contagion. Journal of Economic Dynamics and Control 66, 36–53.
- Lux, T., 2018. Estimation Of Agent-based Models Using Sequential Monte Carlo Methods. Journal of Economic Dynamics and Control 91, 391–408.
- Lux, T., 2020. Bayesian Estimation of Agent-based Models via Adaptive Particle Markov Chain Monte Carlo. Working Paper, University of Kiel.
- Lux, T., Zwinkels, R. C., 2018. Empirical Validation of Agent-Based Models. In: Hommes, C., LeBaron, B. (Eds.), Handbook of Computational Economics. Vol. 4. Elsevier, pp. 437–488.
- Mandes, A., Winker, P., 2017. Complexity and model comparison in agent based modeling of financial markets. Journal of Economic Interaction and Coordination 12 (3), 469–506.

- Montagna, M., Kok, C., 2016. Multi-layered interbank model for assessing systemic risk. ECB Working Paper.
- Musmeci, N., Aste, T., Di Matteo, T., 2015. Relation between financial market structure and the real economy: Comparison between clustering methods. PLoS ONE 10 (3), e0116201.
- Nier, E., Yang, J., Yorulmazer, T., Alentorn, A., 2007. Network models and financial stability. Journal of Economic Dynamics and Control 31 (6), 2033–2060.
- Orcutt, G., Greenberger, M., Korbel, J., Rivlin, A., 1961. Microanalysis of Socioeconomic Systems: A Simulation Study. Harper and Row, New York.
- Pellizzari, P., Westerhoff, F., 2009. Some effects of transaction taxes under different microstructures. Journal of Economic Behavior & Organization 72, 850–863.
- Polach, J., Kukacka, J., 2019. Prospect theory in the heterogeneous agent model. Journal of Economic Interaction and Coordination 14 (1), 147–174.
- Poledna, S., Thurner, S., 2016. Elimination of systemic risk in financial networks by means of a systemic risk transaction tax. Quantitative Finance 16 (10), 1599–1613.
- Popoyan, L., Napoletano, M., Roventini, A., 2017. Taming macroeconomic instability: Monetary and macro-prudential policy interactions in an agent-based model. Journal of Economic Behavior & Organization 134, 117–140.
- Raddant, M., Kenett, D. Y., 2021. Interconnectedness in the global financial market. Journal of International Money and Finance 110, 102280.
- Rosés, R., Kadar, C., Gerritsen, C., Rouly, C., 2018. Agent-based simulation of offender mobility: integrating activity nodes from location-based

social networks. In: Proceedings of the 17th International Conference on Autonomous Agents and MultiAgent Systems. pp. 804–812.

- Schelling, T., 1971. Segregation in networks. Journal of mathematical Sociology 1, 143–186.
- Schweitzer, F., Fagiolo, G., Sornette, D., Vega-Redondo, F., Vespignani, A., White, D. R., 2009. Economic networks: The new challenges. Science 325, 422–425.
- Simon, H. A., 1959. Theories of decision-making in economics and behavioral science. The American economic review 49 (3), 253–283.
- Sircova, A., Karimi, F., Osin, E. N., Lee, S., Holme, P., Strömbor, D., 2015. Simulating irrational human behavior to prevent resource depletion. PloS one 10 (3), e0117612.
- Sisson, S., Fan, Y., Tanaka, M., 2005. Sequential Monte Carlo Without Likelihoods. Proceedings of the National Academy of Sciences of the United States of America 104, 17601765.
- Smith, V. L., March 1989. Theory, experiment and economics. Journal of Economic Perspectives 3 (1), 151–169.
- Snijders, T. A. B., 2001. The statistical evaluation of social network dynamics. Sociological Methodology 31, 361–395.
- Squazzoni, F., Polhill, J. G., Edmonds, B., Ahrweiler, P., Antosz, P., Scholz, G., Chappin, É., Borit, M., Verhagen, H., Giardini, F., et al., 2020. Computational models that matter during a global pandemic outbreak: A call to action. Journal of Artificial Societies and Social Simulation 23 (2).
- Stiglitz, J., 2018. Where modern macroeconomics went wrong. Oxford Review of Economic Policy, 34, 70106,.

- Strauss, D., Ikeda, M., 1990. Pseudolikelihood estimation for social networks. Journal of the American Statistical Association 95, 204–212.
- Thaler, R. H., July 2016. Behavioral economics: Past, present, and future. American Economic Review 106 (7), 1577–1600.
- Toni, T., Welch, D., Strelkowa, N., Ipsen, A., Stumpf, M., 2008. Approximate Bayesian Computationscheme For Parameter Inference And Model Selection In Dynamical Systems. Journal of the Royal Society Interface J6, 187202.
- Tumminello, M., Aste, T., Di Matteo, T., Mantegna, R. N., 2005. A tool for filtering information in complex systems. PNAS 102 (30), 10421–10426.
- Uzzi, B., 1996. The sources and consequences of embeddedness for the economic performance of organizations: The network effect. American Sociological Review 61 (4), 674–698.
- Vallino, E., 2014. The tragedy of the park: an agent-based model of endogenous and exogenous institutions for forest management. Ecology and Society 19 (1).
- Vidal-Tomás, D., Alfarano, S., 2020. An agent-based early warning indicator for financial market instability. Journal of Economic Interaction and Coordination 15 (1), 49–87.
- Vitali, S., Glattfelder, J. B., Battiston, S., 2011. The network of global corporate control. PlosOne 6(10), e25995.
- Waldherr, A., Wettstein, M., 2019. Bridging the gaps: using agent-based modeling to reconcile data and theory in computational communication science. International Journal of Communication 13, 3976–3999.

- Wasserman, S., Pattinson, P., 1996. Logit models and logistic regressions for social networks: I. An introduction to markov graphs and p\*. Psychometrika 61 (3), 401–425.
- Watts, D. J., 2002. A simple model of global cascades on random networks. Proceedings of the National Academy of Sciences 99 (9), 5766–5771.
- Wilhite, A., 2014. Network structure, games, and agent dynamics. Journal of Economic Dynamics and Control 47, 225 238.
- Zona, F., Gomez-Mejia, L. R., Withers, M. C., 2018. Board interlocks and firm performance: towards a combined agency-resource dependence perspective. Journal of Management 44 (2), 586–618.