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1. Definition

The Barnett critique states that there is an internal inconsistency between the theory that is implied by simple sum monetary aggregation (perfect substitutability among components) and the economic theory that produces the models within which those aggregates are used. That inconsistency causes the appearance of unstable demand and supply for money. The incorrect inference of unstable money demand has caused serious harm to the field of monetary economics. The appearance of instability of the demand for money function disappears, if the relevant neoclassical microeconomic aggregation and index number theories are used to produce the monetary aggregates, which then would nest properly within the money demand functions. In fact, studies of the demand for money function using competently produced monetary aggregates and state-of-the-art demand system modeling methodology have found the demand for money function to be more stable and more easily modeled than the demand for most other consumer goods. See, e.g., Barnett and Serletis (2000, chapters 2, 7, 9, 16, 17, 18, 24), Barnett and Chauvet (2011, chapters 1, 4, 7), and Barnett (2012, pp. 92-110).

The term “Barnett Critique” was coined and defined in a British paper published by the St. Louis Federal Reserve Bank, “Empirical Evidence on the Recent Behavior and Usefulness of Simple-Sum and

Weighted Measures of the Money Stock” (Chrystal and MacDonald (1994). By conducting empirical tests with the St. Louis Federal Reserve’s reduced form policy equation (originated by Andersen and Jorden (1968)), Chrystal and MacDonald compared the statistical properties of differently defined monetary aggregates, including simple sum and Divisia aggregates, among others. Chrystal and MacDonald found that the Divisia aggregates, derived and advocated by Barnett (1980), performed best and recommended that Divisia monetary aggregates be produced and supplied by the Federal reserve at all levels of aggregation, from narrow to broad, so that researchers can test thoroughly the performance of these indicators.

Since 1980, economies throughout the world have experienced substantial monetary and financial innovation. As the structure of financial innovation has been expanding, internal consistency of monetary aggregation with economic theory is growing in importance. Divisia aggregation is directly derived from economic theory and assures consistency with economic theory at all levels of aggregation. An international library of Divisia monetary and financial aggregation research and data are maintained online by the Center for Financial Stability (CFS) in New York City.

2. History

September 26th, 1983 could be remembered as the date on which an unusual controlled experiment of the Barnett critique was conducted. On that same day, Milton Friedman and William A. Barnett both went on the record by publishing their conflicting views and forecasts in major magazines, providing opposite conclusions about the likelihood of inflation and recession, based on analogous data sources, differing only by the method of aggregation. In a “A Case of Bad Good News,” Friedman wrote in *Newsweek* magazine (p. 84) that a huge spike in the growth rate of the M2 money supply had occurred, would surely cause inflation, and would be followed by a recession caused by overreaction of the Federal Reserve to the inflation. The last conclusion, of “unavoidable recession,” was a uniquely monetarist view. Not all economists agreed with that inclusion. For example, economists of the Real Business Cycle school did not agree that an overreaction of monetary policy would cause a recession. They would have agreed with an unavoidable spike of inflation caused by a huge spike in the growth rate of money, but not subsequent changes in real variables, such as unemployment and output. According to that view, the Federal Reserve has no control over real variables, only nominal. At the time

of Friedman's dramatic article in *Newsweek*, there had been a huge spike in the growth rate of simple sum M2.

According to the Barnett Critique, Friedman should have used a properly measured index number for M2, such as Divisia, Fisher ideal, Paasche, or Laspeyres. In his article in *Forbes* magazine on that exact same day, Barnett wrote (p. 196) in his article, with the title "What Explosion?", that there had been no spike in Divisia M2; there would be no surge in inflation and no recession from a Federal Reserve overreaction to an inflation surge that will not occur.

In retrospect, it would be interesting to ask now whether Barnett might have found a spike in a broader Divisia monetary aggregate, such as Divisia M4, currently favored by the Center for Financial Stability. We have done so in Figure 1. Comparing the monthly rate of growth of simple sum M2 and of the broad Divisia M4, an unusual spike in the growth rate of simple sum M2 was identified at the beginning of 1983 but not of Divisia M4. Based on Figure 1, the growth rate of simple sum M2 spiked to 3% a month. Annualized, that would have been about 36% a year, the alarming growth rate Milton Friedman saw and warned about. That would indeed have been an unusual rate of growth of the money supply. However, Divisia M4 displayed no evidence of such a spike at all, further confirming Barnett's finding with Divisia M2 in the *Forbes* article.

There was no surge in inflation or recession following the non-inflation. History proved that Barnett's conclusion was right, and Friedman's was wrong, although the huge surge in simple sum M2 seem by Friedman did indeed occur. Barnett explained that the reason for the misleading spike in simple sum M2 was a change in regulation. The Federal Reserve had just permitted banks to introduce a new type of monetary asset, Money Market Deposit Accounts (MMDA), which, at that time, were yielding a higher market interest rate than other assets included in M2. Many economic agents transferred money into those new high-yielding accounts with the source of funds often coming from outside M2 as, for example, from money market mutual funds and Treasury bills, being held largely for investment motives, while yielding high unregulated market interest rates.

The transfer of investment motivated funds into MMDA accounts in banks caused the simple sum aggregates to surge, since deposits entered into the newly permitted MMDA accounts were added into the simple-sum monetary aggregates without weights, despite the fact that MMDAs deposits were largely motivated by their interest rate yields, as opposed to currency and demand deposits, which did not yield interest and were being held for their monetary services in transactions. However, since

MMDAs were yielding very high-interest rates, their user cost prices, reflecting the opportunity cost from foregone interest, were very low. Divisia monetary aggregates remove the investment motive. Those new monetary innovations, priced at their low user cost prices, smoothly integrated into the Divisia monetary aggregates without creating a spike. The excessive weighting of MMDAs in the simple sum monetary aggregates was the reason that the simple sum and Divisia growth rates at the time of the innovation were so drastically different.

The introduction of MMDAs was not a supply-side phenomenon. The Federal Reserve was not suddenly pumping up the money supply. The Federal Reserve had permitted entry of a new account type, permitting banks to compete with money market mutual funds. The result was a demand-side phenomenon. People were moving funds into those new assets at banks. The Federal Reserve itself was not increasing the money supply.

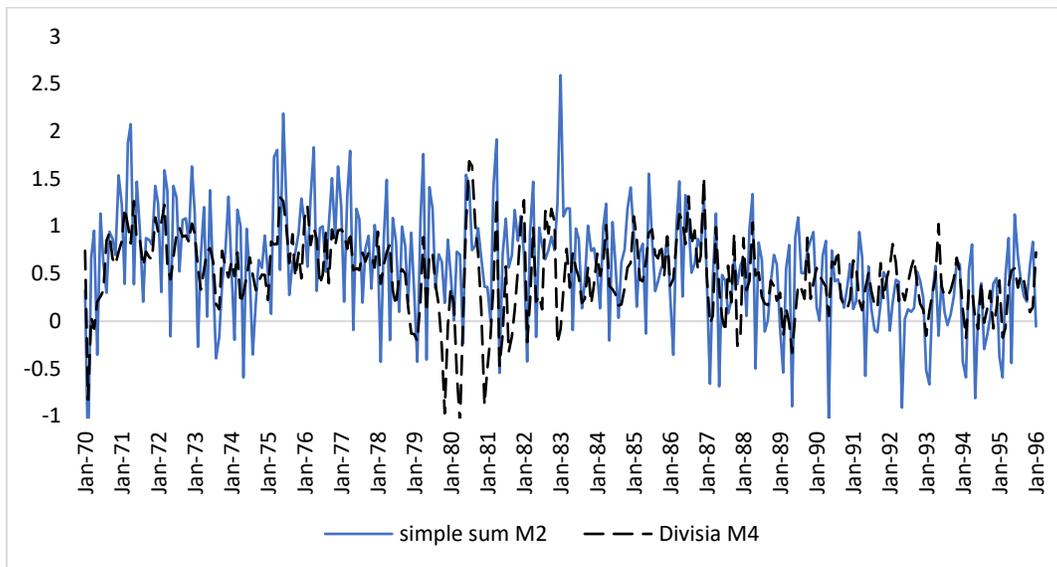


Figure 1. Monthly percentage growth rates of simple sum M2 and Divisia M4

The Barnett Critique defines the “high road” to be research that insists on internal coherence (consistency) among data, theory, and econometrics. In contrast, along the low road researchers can play fast and loose with data, theory, and econometrics. A consequence of low road research is paradoxes, puzzles, and controversies at every turn. Unfortunately, many empirical monetary economists have taken the low road. The basic point to be made by the Barnett Critique is that low-road

research inherently contains internal logical inconsistency. The origin of many controversies in monetary economics was the internal inconsistency of the formulas used to produce the data with the theory producing the models within which the data were used.

Does internal consistency matter? In the 1950s, monetary aggregates initially included only assets yielding no interest. Simple sum aggregation implies that all of its components are perfect substitutes having identical prices. That implicit assumption was satisfied by the earliest monetary aggregates, since the user cost price of all of the components was the same alternative rate of return on capital. The component assets had no own rates of interest of their own. However, if components have different user cost prices but are nevertheless perfect substitutes, there will be a corner solution. Economic agents will buy only the cheapest among the perfectly substitutable component assets. The asset having the lowest user cost prices (foregone interest) will be the assets having the highest own rate of interest.

Now that most component monetary assets yield interest, simple sum monetary aggregation implies a corner solution with only the highest yielding component remaining in existence. The other components logically cannot exist, since no one would hold them. Currency and non-interest-bearing demand deposits cannot exist. Their appearance in the economy and in the Federal Reserve's monetary aggregates must be an illusion. Assuming perfect substitutability consistent with simple sum aggregation, non-negotiable certificates of deposit can exist, since their yield is often higher than the yields on other components of simple sum monetary aggregates. In short, the simple sum monetary aggregates imply that we all are suffering from delusions, since we all believe that other monetary assets, such as currency and demand deposits, exist and are being held by many consumers --- including ourselves. That is an implication of the simple sum monetary aggregation. The simple sum aggregates, based on incompetent index number and aggregation theory, should not be used within macroeconomic models based on competent economic theory.

3. Divisia Monetary Aggregates

The Divisia index was originated by Francois Divisia (1925) as a line integral in continuous time for perishable consumer goods. The growth rate of the Divisia index is a weighted average of component growth rates. The weights in the growth rate aggregate are the expenditure shares of the components with user cost pricing at each instant of time. But the level of the index is not a weighted average of the

levels of the components. The level is a deeply nonlinear line integral. The Divisia index is directly derived from optimizing consumer behavior. There is no approximation error. But economic data are not available in continuous time. Discrete time approximations to the Divisia index have third order remainder terms in the changes.

To discretize the continuous time Divisia index, it is necessary to decide where to measure the share weights in the growth rate index within the discrete time interval. Tornqvist (1936) proposed using the average of the share at the beginning and the share at the end of the discrete time period. The resulting index is chained, not fixed base, since the average shares move over time. Henri Theil (1967) also advocated that discretization. Based on the research of Tornqvist and Theil, the resulting index often is called the Tornqvist-Theil Divisia index, or the Tornqvist-Theil index. Barnett simply calls it the "Divisia index in discrete time," since the Tornqvist weighting is now universally accepted as providing the best discretization and resembles the Simpson's rule approximation to the continuous-time line integral.

Another highly regarded index is the "Fisher ideal" index. That index consists of the geometric mean of the Laspeyres index and the Paasche index. The Fisher ideal index is used in many fields. The Commerce Department in the U.S. uses it in producing data for the national accounts. An important property of the Fisher ideal is self-duality: the dual to the Fisher ideal quantity index is the Fisher ideal price index. In practice, the difference between the growth rate of the Fisher ideal index and of the discrete time Divisia index is less than the roundoff error in the component data.

Compared to the Fisher ideal index, Divisia has two advantages. First, the formula of the Fisher index, as the geometric mean of two different indexes, is highly nonlinear and therefore difficult to explain to the people without expertise in index number theory. On the other hand, the Divisia index in growth rate form is much easier to explain as the share weighted average of component growth rates. Second is the relationship to its continuous time form. The original Divisia index in continuous time, under normal neoclassical optimality assumptions, is always exactly true, not an approximation. Divisia derived his index directly from the first-order conditions for constrained utility maximization under perfect certainty. Therefore, under perfect certainty, the continuous time Divisia index is a direct implication of microeconomic theory, so long as the existence assumption (weak separability of the components from other goods) is satisfied.

On the other hand, the Tornqvist-Theil index is a statistical index number, as is the Fisher ideal index. Hence the Divisia index in discrete time is an approximation. As with all discrete time statistical

index numbers, the Tornqvist-Theil index has an error term. That error term is third order in the component changes. That error is negligible, since it is a chained index aggregating typically over small monthly changes. The Fisher ideal and Tornqvist-Theil indexes are both second-order approximations in discrete time, with third-order remainder terms usually ignored in the data. Since the Divisia index in continuous time is exact, we can characterize the Tornqvist-Theil index as a second-order approximation to Francois Divisia's continuous time index.

Erwin Diewert (1976) defined the class of "superlative index numbers" as those producing a second order approximation to the unknown exact aggregator function. He proved that both the Tornqvist-Theil and Fisher ideal indexes are in that class. When used to measure aggregate monetary services in accordance with Barnett's formulas (1980), both indexes produce almost identical velocity of money and monetary growth.

Barnett (1978,1980) derived the user-cost price formula needed to apply aggregation and index number theory to monetary aggregation. In particular, Barnett (1980) proposed the discrete time Divisia monetary aggregates or the nearly identical Fisher ideal index to measure demand-side monetary services, using economic aggregation and index number theory. Barnett, Offenbacher, and Spindt (1984) applied the resulting formula for the Divisia monetary aggregates to show that they perform far better than the corresponding simple sum aggregates relative to the tests being used at that time to compare monetary aggregates. As observed in that paper, Barnett's Divisia monetary aggregates are elements of Diewert's class of superlative quantity index numbers. While simple sum implies the same weighting of each component monetary asset, Divisia properly weights each monetary asset in accordance with aggregation and index number theory. Divisia monetary aggregates should be strictly preferable to the simple sum aggregates, since the component monetary assets are not perfect substitutes. The aggregation theoretic derivation assumes only that the weak separability condition necessary for the existence of a quantity aggregator function holds. Without such existence, there is nothing to be approximated by aggregation and index number theory.

As derived by Barnett (1978,1980), the real user cost (equivalent rental price) of a monetary asset among n such assets is

$$\pi_{it} = \frac{R_t - r_{it}}{1 + R_t},$$

where r_{it} is the own rate of return on asset i during period t , and R_t is the risk-free rate of return on a completely illiquid asset (benchmark rate on pure capital) during period t . The Divisia index in growth rate form in continuous time is

$$d \log M_t = \sum_{i=1}^n s_{it} d \log m_{it} ,$$

where $s_{it} = \pi_{it} m_{it} / \boldsymbol{\pi}'_t \mathbf{m}_t$ is the expenditure share on monetary asset i and m_{it} is real balances of monetary asset i during period t , with $\boldsymbol{\pi}'_t = (\pi_{1t}, \pi_{2t}, \dots, \pi_{nt})$ and $\mathbf{m}'_t = (m_{1t}, m_{2t}, \dots, m_{nt})$.

4. Credit-Card Augmented Divisia Monetary Aggregates

Credit-Card augmented Divisia monetary aggregates measure the money supply including credit card transaction services. Barnett, Chauvet, Leiva-Leon, and Su (2016) and Barnett and Su (2016) introduced the new monetary aggregates, including credit card transaction volume services. These new Divisia aggregates are provided to the public by the CFS along with the original Divisia aggregates not including credit card services. Credit cards had never before been included in simple sum measures of the money supply, despite the fact that credit cards clearly provide transaction services. The reason is accounting conventions. Accounting, and therefore simple sum aggregation, do not permit adding liabilities to assets. But using economic theory instead of accounting, monetary and credit card services can be entered into a derived utility function to reflect the fact that money and credit cards provide similar services, such as liquidity and transactions services. In particular, credit cards provide deferred payment services not provided by money. The theory permits the measurement of the joint services of credit cards and money in accordance with index number theory. Index number theory measures service flows and is based on microeconomic aggregation theory, not accounting.

The real user cost of credit card services, derived in Barnett and Su (2016), is

$$\tilde{\pi}_{jt} = \frac{e_{jt} - R_t}{1 + R_t} ,$$

where R_t is the risk-free rate of return on a completely illiquid asset (benchmark rate on pure capital) during period t , and e_{jt} is the interest rate charged on credit card j balances. There are two categories of consumers using credit cards. The first category is consumers who pay interest to the credit card

company, and another category is consumers who do not pay interest, since they always repay their credit card debt before interest becomes due. In the simplest representative consumer model aggregated over consumers, e_{jt} is averaged over both those consumers who maintain rotating balances, while thereby paying interest on contemporaneous credit card transactions, and those consumers who pay off such credit card transactions before the end of the period, while thereby not paying explicit interest on the credit card transactions. The representative consumer's utility function for the current period does not include rotating balances for transactions in prior periods to avoid double counting of transactions services. The CFS data include transaction services, measured by their reported "volumes," for the four ($j = 1, \dots, 4$) credit card companies, Visa, MasterCard, Discover, and American Express.

The credit-card augmented Divisia monetary aggregate is a function of monetary asset services and credit card services. The aggregation-theoretic approach produces the credit-card augmented structural aggregate, $M_t = M(\mathbf{m}_t, \mathbf{c}_t)$, derived from optimizing behavior of consumers, where $\mathbf{c}'_t = (c_{1t}, c_{2t}, c_{3t}, c_{4t})$ is the transaction volumes on the representative consumer's credit cards from Visa, MasterCard, Discover, and American Express. The growth rate of the Divisia index, $M(\mathbf{m}_t, \mathbf{c}_t)$, is the share-weighted average of the growth rates of the components. The credit card quantities to include in the augmented Divisia index formula are the monthly credit card transactions volumes, not the credit card balances, which include rotating balances from previous period transactions.

The credit-card augmented Divisia index, which exactly tracks the aggregator function in continuous time, is the following:

$$d \log M_t(\mathbf{m}_t, \mathbf{c}_t) = \sum_{i=1}^n s_{it} d \log m_{it} + \sum_{j=1}^4 \tilde{s}_{jt} d \log c_{jt} .$$

The share, s_{it} , is the expenditure share of monetary asset i in the total services of monetary assets and credit cards, while the share, \tilde{s}_{jt} , is the expenditure share of credit card j services in the total services of monetary assets and credit cards. In the computation of s_{it} , the relevant user cost prices are π_{it} , while in the computation of \tilde{s}_{jt} , the relevant user cost prices are $\tilde{\pi}_{jt}$.

On the supply side, the manner in which the monetary services are produced is highly relevant to the transmission mechanism of monetary policy and to the indicator value of the resulting service flows. In recent decades, transaction and liquidity services have been augmented dramatically by the growth of privately supplied unregulated monetary services from bank-supplied credit cards and from the

services provided by unregulated shadow banking. Barnett and Su (2018) employed a production model of financial firms, which produce services through financial intermediation, and investigated supply-side aggregation when financial firms produce both monetary services and credit card transactions services. They derive the conditions under which a joint supply-side aggregate over monetary and credit card transactions services exists. The existence condition for a supply-side inside-money aggregator function is blockwise weak separability within bank technology, and for a demand-side inside-money aggregator function is blockwise weak separability within tastes.

The user cost formula for supplied monetary assets differs from the demand-side user cost formula, when there is a regulatory wedge produced by the existence of reserve requirements yielding no interest. The existence of non-interest-bearing required reserves imposes an implicit tax on banks. This has been the case during most of US Federal Reserve history. Under those circumstances, Barnett (1987) derived the user cost price received by banks for providing and servicing monetary asset type i to be

$$\pi_{it} = \frac{(1 - k_i)R_t - r_{it}}{1 + R_t},$$

where k_i is the required reserve ratio on monetary asset i . The implicit tax on banks is the foregone interest on uninvested required reserves.

Very recently there has been a change in Federal Reserve policy, resulting in required reserves set at zero with payment of interest on reserves. It is not yet clear whether required reserve ratios will remain at zero permanently.

5. Relevant Literature

Following appearance of the Barnett critique, considerable literature has found that Divisia is a far more appropriate money measure than simple sum for use within economic models. Divisia stabilizes those models and provides better model performance. For example, Belongia and Ireland (2014) found that a Divisia monetary aggregate tracks the true aggregate almost perfectly, following a wide variety of macroeconomic shocks, both real and nominal. Keating and Smith (2019) confirmed that a constant Divisia monetary aggregate growth rate rule would outperform all other rules using simple sum monetary aggregates or the monetary base, while a constant simple sum monetary growth rate rule would cause very high welfare loss.

In multiple research papers, Divisia outperforms simple sum in prediction ability. For example, Barnett, Chauvet, and Leiva-Leon (2016) found that a model containing information on real economic activity, inflation, interest rates, and Divisia monetary aggregates produces the most accurate real time nowcasts of nominal GDP growth. Schunk (2001) similarly provides the forecasting performance of Divisia monetary aggregates with a four-variable vector autoregression including real GDP, GDP deflator, Treasury bill rate, and monetary aggregates. Ellington (2018) evaluates the relative empirical benefits of Divisia monetary aggregates and finds a strong link between Divisia money and economic activity over the business cycle, with that link substantially less prominent when using simple sum monetary aggregation. These studies also confirm the forecasting ability of Divisia aggregates by using out-of-sample forecasts of economic activity. Hundreds of papers have been published about the Barnett critique throughout the world in over 40 countries. A convenient source is the international library maintained online by the Center for Financial Stability (CFS) in New York City.

Barnett has authored or coauthored a very large number of papers published on the validity of the Barnett critique in solving problems associated with the use of simple sum monetary aggregation in modeling and in policy. Many of the most important of those studies have been reprinted in two books, Barnett and Serletis (2000) and Barnett and Chauvet (2011), with presentation and discussion of that research made widely available to the general public in Barnett (2012).

6. Conclusion

Ongoing economic and financial innovations are continuing to produce substitutes for currency and demand deposits relevant to the economy's liquidity, transactions services, and other services normally associated with money. As a result, simple sum aggregation and the Barnett critique are increasing in relevancy and in understanding evolving defects in macroeconomic modeling and policy. Internal consistency among aggregation theoretic assumptions and structure and the assumptions and structure relevant to the models within which the data are used is critically important. These considerations need to be taken into consideration and correctly utilized at the beginning of the data generation process to avoid cumulative misunderstandings and errors in subsequent research and policy. Getting this right at the start would avoid the need for future research on the sources of induced instability in functions resulting from internal inconsistencies between data generation and modeling methodology. The currently fashionable view that money should be ignored, since central bank measures are so poor, is likely to produce serious long-term costs to the profession and to economies throughout the world.

The Center for Financial Stability (CFS) provides Divisia monetary aggregates data for the United States. This site incorporates the most recent advances of the Barnett critique and supplies the results without charge to the public. The Divisia data without credit-card augmentation normalize levels to equal 100 in January 1967, while the credit-card augmented Divisia monetary aggregates and credit-card augmented Divisia inside money aggregates normalize levels to equal 100 in July 2006. The CFS supplies its Divisia monetary aggregates at eight levels of aggregation, DM1, DMZM, DM2M, DM2, DALL, DM3, DM4-, and DM4. Moreover, CFS produces the broad money aggregates such as Divisia M4, while the Federal Reserve no longer provides broad aggregates, such as M3 and M4, since the Federal Reserve has recognized that adding distant substitutes for money to transaction balances involves seriously defective weighting of the component monetary services.

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