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# The environmental effect of ambient charges in mixed triopoly with diverse firm objectives

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## Abstract

This paper examines a quantity-setting mixed triopoly model comprising a profit-maximizing firm, a partially cooperating firm and a socially concerned firm to reassess the environmental effect of an increase in ambient charges. The paper demonstrates that an increase in the ambient charge can reduce pollutant emissions.

Keywords: ambient charge; Cournot triopoly; partially cooperating firm; pollution; socially concerned firm

JEL classification: C72; D21; Q58

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# 1. Introduction

The analysis by Ganguli and Raju (2012) considers two Bertrand duopoly games to reassess the effect of an increase in ambient charges as a policy measure for reducing industrial non-point source pollution. In the first game, the regulator first announces the ambient charge and then two firms non-cooperatively and simultaneously choose their prices. In this game, the pollution abatement technologies are assumed to be fixed. In the second game, knowing that the ambient charge has been announced by the regulator, two firms non-cooperatively and simultaneously choose their pollution abatement technologies in the first stage and prices in the second stage. Ganguli and Raju demonstrate that in each game an increase in the ambient charge leads to more pollution. In addition, Sato (2017) examines the effect of an increase in ambient charges in a static Cournot duopoly model and shows that an increase in the ambient charge leads to less pollution as opposed to Bertrand duopoly competition.

Most models of economic theory assume that firms maximize profits. Therefore, the behaviour of profit-maximizing firms has been most frequently encountered in the literature on economic theory. However, in the real world, not all firms adopt profit maximizing behaviour. For example, some economic models include partially cooperating firms (Cyert and DeGroot, 1973; Bischi et al, 2010; Matsumoto et al, 2010; Cracau, 2015). Each partially cooperating firm's aim is to maximize the sum of its own profit and certain proportions of the profits of the other firms. In addition, economic market models that incorporate socially concerned firms are sometimes analyzed by economists (Goering, 2007; Kopel and Brand, 2012; Lambertini and Tampieri, 2012; Cracau, 2015; Kopel, 2015; Garca et al, 2019). Each socially concerned firm's aim is to maximize the sum of its own profit and a proportion of consumer surplus.

We examine a quantity-setting mixed triopoly model comprising a profit-maximizing firm, a partially cooperating firm and a socially concerned firm to reassess the environmental effect of an increase in ambient charges.

The remainder of this paper is structured as follows. In Section 2, we describe the model

used. Section 3 presents the main result of this study. Finally, Section 4 concludes the paper.

## 2. The model

We consider three firms: a profit-maximizing firm (firm P), a partially cooperating firm (firm C) and a socially concerned firm (firm S). There is no possibility of entry or exit. In the remainder of this paper, subscripts P, C and S represent firm P, firm C and firm S, respectively. The production quantity of firm  $i(i = P, C, S)$  is represented as  $q_i$ . The inverse demand function is linear:  $P = a - Q$ , where  $P$  represents the market price,  $Q = q_p + q_c + q_s$  is the aggregate demand, and  $a$  is a constant. The total amount of pollution generated by the firms is given by  $E = e(q_p + q_c + q_s)$ , where  $e \in (0, \infty)$  denotes the pollution abatement technology.

Firm  $i$ 's profit is given by

$$\pi_i = (a - Q)q_i - c_i q_i - m(eQ - \bar{E}), \quad (1)$$

where  $c_i \in (0, \infty)$  represents firm  $i$ 's marginal cost of production and  $\bar{E}$  is the environmental standard. If  $eQ < \bar{E}$ , then the regulator of the government will give the firms a subsidy of  $m(\bar{E} - eQ)$ , whereas if  $eQ > \bar{E}$ , then the firms will be penalized by  $m(eQ - \bar{E})$ .

Firm C's objective function is given by

$$V_C = \pi_C + \beta(\pi_P + \pi_S), \quad (2)$$

where  $\beta \in [0, 1]$  denotes the level of cooperation.

Firm S's objective function is given by

$$W_S = \pi_S + \theta CS, \quad (3)$$

where  $CS = \frac{1}{2}Q^2$  represents consumer surplus and  $\theta \in [0, 1]$  is the level of social concern.

We assume that all outputs obtained in Cournot-Nash equilibrium are non-negative. In the next section, we present the result of the mixed triopoly model.

### 3. Main result

From (1), (2) and (3), we can derive the following reaction functions:

$$R_P(q_C, q_S) = \frac{a - c_P - em - q_C - q_S}{2}. \quad (4)$$

$$R_C(q_P, q_S) = \frac{a - c_C - (1 + 2\beta)em - (1 + \beta)q_P - (1 + \beta)q_S}{2}, \quad (5)$$

$$R_S(q_P, q_C) = \frac{a - c_S - em - (1 - \theta)q_P - (1 - \theta)q_C}{2 - \theta}. \quad (6)$$

Solving these reaction functions simultaneously, we have the following equilibrium quantities:

$$q_P^* = \frac{(1 - \theta + \beta\theta)a - (3 - \beta - \theta + \beta\theta)c_P + c_C + (1 - \beta)c_S - (1 - 2\beta - \theta + \beta\theta)em}{4 - 2\beta - \theta + \beta\theta},$$

$$q_C^* = \frac{(1 - 2\beta - \theta)a + (1 + \beta)c_P - (3 - \theta)c_C + (1 + \beta)c_S + (1 - 4\beta + \theta + 2\beta\theta)em}{4 - 2\beta - \theta + \beta\theta},$$

$$q_S^* = \frac{(1 + 2\theta - \beta\theta)a + (1 - \beta - \theta + \beta\theta)c_P + (1 - \theta)c_C - (3 - \beta)c_S - (1 - 2\beta + 2\theta - \beta\theta)em}{4 - 2\beta - \theta + \beta\theta}.$$

When  $e$  is given, the industrial emission quantity can be calculated as follows:

$$e(q_P^* + q_C^* + q_S^*) = \frac{e[(3 - 2\beta)a - (1 - \beta)c_P - c_C - (1 - \beta)c_S - 3em]}{4 - 2\beta - \theta + \beta\theta}. \quad (7)$$

Equation (7) is a function of the policy parameter  $m$ . Therefore, we can represent  $e(q_P^* + q_C^* + q_S^*)$  as a function  $E(m)$ . If  $E(m)$  is differentiated by  $m$ , then:

$$E'(m) = -\frac{3e^2}{4 - 2\beta - \theta + \beta\theta}. \quad (8)$$

We can now present the following proposition.

**Proposition 1:** In the quantity-setting mixed triopoly model,  $E'(m) < 0$ .

We find that the result of this proposition is the same as that obtained from profit-maximizing Cournot duopoly competition.

## 4. Conclusion

We have examined a quantity-setting mixed triopoly model comprising a profit-maximizing firm, a partially cooperating firm and a socially concerned firm, and have demonstrated that an increase in the ambient charge can always lead to less pollution. We have found that the result of this study is the same as that obtained from profit-maximizing Cournot duopoly competition.

## References

- Bischi, G. I., Chiarella, C., Kopel, M., Szidarovszky, F., 2010. *Nonlinear Oligopolies: Stability and Bifurcations*. Heidelberg, Germany: Springer-Verlag Berlin Heidelberg.
- Cracau, D. 2015. The effect of strategic firm objectives on competition. In: Ohnishi, K. (Ed.), *Firms' Strategic Decisions: Theoretical and Empirical Findings, Volume 1* (pp. 170-181). Sharjah, UAE: Bentham Science Publishers.
- Cyert, R. M., DeGroot, M. H., 1973. An analysis of cooperation and learning in a duopoly context. *American Economic Review* 63 (1), 24-37.
- Ganguli, S., Raju, S., 2012. Perverse environmental effects of ambient charges in a Bertrand duopoly. *Journal of Environmental Economics and Policy* 1(3), 289-296.
- Garcfa, A., Leal, M., Lee, S.-H., 2019. Endogenous timing with a socially responsible firm. *Korean Economic Review* 35 (2), 345-370.
- Goering, G. E., 2007. The strategic use of managerial incentives in a non-profit firm mixed

- duopoly. *Managerial and Decision Economics* 28 (2), 83-91.
- Goering, G. E., 2008. Welfare impacts of a non-profit firm in mixed commercial markets. *Economic Systems* 32 (4), 326-334.
- Kopel, M., Brand, B., 2012. Socially responsible firms and endogenous choice of strategic incentives. *Economic Modelling* 29 (3), 982-989.
- Kopel, M., 2015. Price and quantity contracts in a mixed duopoly with a socially concerned firm. *Managerial and Decision Economics* 36 (8), 559-566.
- Lambertini, L., Tampieri, A., 2012. Corporatesocial responsibility and firms' ability to collude. In: Boubaker, S., Nguyen, D. K. (Eds.), *Board directors and corporate social responsibility* (pp. 167-178). London: Palgrave Macmillan.
- Matsumoto, A., Merlone, U., Szidarovszky, F., 2010. Dynamic oligopoly with partial cooperation and antitrust threshold. *Journal of Economic Behavior & Organization* 73 (2), 259-272.
- Ohnishi, K., 2010. Lifetime employment contract and quantity competition with profit-maximizing and joint-stock firms. *Journal of Institutional and Theoretical Economics* 166 (3), 462-478.
- Ohnishi, K., 2021. Pollution, partial privatisation and the effect of ambient charges. MPRA Paper No. 106319, University Library of Munich, Germany.
- Poe, G. L., Schulze, W. D., Segerson, K., Suter, J. F., Vossler, C. A., 2004. Exploring the performance of ambient based policy instruments when nonpoint source polluters can cooperate. *American Journal of Agricultural Economics* 86 (5), 1203-1210.
- Sato, H., 2017. Pollution from Cournot duopoly industry and the effect of ambient charges. *Journal of Environmental Economics and Policy* 6 (3), 305-308.
- Segerson, K., 1988. Uncertainty and incentives for nonpoint pollution control. *Journal of Environmental Economics and Management* 27, 275-285.
- Suter, J. F., Vossler, C. A., Poe, G. L., Segerson, K., 2008. Experiments on damage-based ambient

taxes for nonpoint source polluters. *American Journal of Agricultural Economics* 90 (1), 86-102.

Wang, L. F. S., Lee, J. Y., 2010. Partial privatization, foreign competition, and tariffs ranking. *Economics Bulletin* 30 (3), 2405-2012.

Xepapadeas, A.P., 1991. Environmental policy under imperfect information: incentives and moral hazard. *Journal of Environmental Economics and Management* 20, 113–126.

Xepapadeas, A.P., 1992. Environmental policy design and dynamic non-point source pollution. *Journal of Environmental Economics and Management* 23, 22–39.

Xepapadeas, A.P., 1995. Observability and choice of instrument mix in the control of externalities. *Journal of Public Economics* 56, 485–498.