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# IMPROVEMENT OF METHODS FOR DESCRIPTION OF A THREE-BUNKER COLLECTION CONVEYOR

### Oleh Pihnastyi, Svitlana Cherniavska

The object of current research is a multi-section transport conveyor. The actual control problem of the transport system flow parameters with given criteria quality is being solved. Algorithms for optimal control of the flow of material coming from the input accumulating bunkers into the collection section of the conveyor have been synthesized, ensuring the filling of the accumulative tank in the minimum time. An admissible control of the flow of material from the accumulating bunkers is found, which allow filling the accumulative tank, taking into account the given distribution of the material along the section of the collection conveyor at the initial and final moments of the filling time with minimal energy consumption. The synthesis of algorithms for optimal control of the material flow from accumulating bunkers became possible due to the determination of differential connections in the optimal control problem based on an analytical distributed model of a transport conveyor section. The distinctive features of the obtained results are that the allowable controls contain restrictions on the value of the maximum allowable load of the material on the conveyor belt and take into account the initial and final distribution of the material along the collection conveyor section. Also, as a feature of the obtained results should be call the consideration of the variable transport delay in the transport conveyor control model. The application area of the results is the mining industry. The developed models will make it possible to synthesize algorithms for optimal control of the flow parameters of the transport system for a mining enterprise, taking into account the transport delay in the incoming of material at the output of the conveyor section. The condition for the practical use of the results obtained is the presence in the sections of the transport conveyor of measuring sensors that determine the belt speed and the material amount in the accumulating bunkers.

Keywords: PiKh-model, speed control, transport delay, accumulating bunker, similarity criteria.

### **1. Introduction**

A transport conveyor serving a mining industry enterprise is a high-tech dynamic distributed system [1] that consists of a large number of sections separated from each other by accumulating bunkers [2–4]. With the normative value of the loading factor for the material of the conveyor section equal to 0.7, the specific transportation costs are up to 20% of the material extraction cost [14]. Reducing the loading factor of the conveyor belt with material leads to a non-linear increase in specific transportation costs. These costs can constitute the main part of the cost of extracting the material, making mining unprofitable. The constant requirements for increasing the competitiveness of mining production substantiate the relevance of scientific topics devoted to building models of the transport system for the synthesis of algorithms for optimal control of the flow parameters of the transport conveyor. To reduce the transport costs of a conveyor section, algorithms have been developed for optimal

control of the belt speed [5-7] and the input material flow [8-10] taking into account the energy management methodology [11-13]. The use of research results at existing enterprises allows to reduce the cost of mining and reduce carbon dioxide emissions into the atmosphere [15].

# 2. Analysis of Literature Data and Statement of Problems

The scheme of the collection conveyor with three accumulating bunkers is quite often used when analyzing the flow of material in a transport system. At the same time, for this conveyor scheme, there are no models that take into account the variable transport delay and the uneven distribution of material along the transport route. For example, in [15], a simulation model with a constant transport delay was developed for the power consumption control system. The model demonstrates the energy saving capability of South Africa's Demand Side Management program for conveyor sections with constant section belt speed and constant material flow from the accumulating bunker. In [16], a system dynamics model was developed to synthesize four material flow control policies for a collection conveyor with three bunkers. The presented model does not take into account the transport delay, the main attention is focused on the problem of overflowing bunkers without restrictions on the maximum allowable load on the conveyor belt. In [17], for a scheme of a collection conveyor with 3 bunkers, a model of a transport system was proposed, in which, to coordinate the filling level of the bunkers, constant transport delays were introduced into the control channels, which provide discrete control of the material flow coming from the accumulating bunkers. The question of modeling the transport system for the general case, which assumes the presence of variable transport delays, has remained unresolved. The use of the discrete element method [18], a neural network [19, 20], and specialized software [21] in modeling a collection conveyor with three bins can be considered as suggested ways to overcome these difficulties. However, the proposed solutions to the problem require significant computing resources, which limits their practical use for the synthesis of control systems. This explains the lack of publications containing methods [18-21] for constructing models for a collection conveyor scheme with three accumulating bunkers. Another approach to solving the problem lies in the further development of analytical models of a multi-section transport conveyor. The foundation of the study is the analytical model of the conveyor section [10]. The model is used to describe the transient modes of operation of a transport conveyor section, does not require significant computing resources, and can be further developed to describe the state of the flow parameters of a multi-section conveyor. The first step in such a study is to build an analytical model for a three-bunker collection conveyor scheme. The presented analysis allows us to assert the practical necessity of constructing an analytical model of a collection conveyor with three bunkers for the synthesis of algorithms for optimal control of flow parameters.

### 3. Purpose and objectives of the study

The aim of the study is to improve the analytical methods for describing the transport system for a collection conveyor scheme with 3 bunkers. This will make it

possible to synthesize algorithms for optimal control of the flow parameters of the transport system in order to reduce the energy consumption of the conveyor section.

To achieve the aim, the following problems were set:

- to develop an analytical model of a 3-bunker collection conveyor, taking into account the transport delay;

- to synthesize an algorithm for optimal control of the flow parameters of the transport system for a collection conveyor scheme with 3 bunkers, based on an analytical model.

# 4. Materials and methods of research

The object of this study is a multi-section transport conveyor. It is assumed that taking into account the transport delay makes it possible to increase the accuracy of control and reduce the specific transport costs.

The foundation of the conducted research is the general provisions of the statistical theory of flow production control systems [22]. To describe the flow parameters of the transport conveyor section, a hydrodynamic model of the transport conveyor was used. [23]. The application of the methods of the theory of similarity makes it possible to present the model of the transport system for the collection conveyor scheme with 3 bunkers in a universal form, expanding the scope of the model.

5. The results of the study of the transport system model for the collection conveyor scheme with 3 bunkers

5. 1. Construction of a conveyor model with 3 bunkers, taking into account the transport delay

A transport system was considered, consisting of one main (collective) conveyor and three linear two sectional conveyors with an intermediate bunker (Fig. 1).

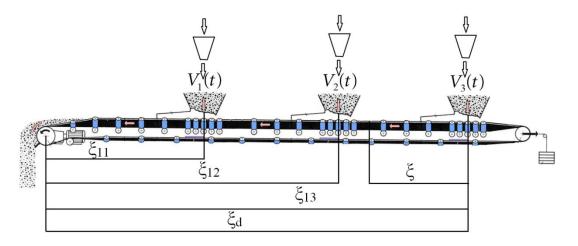


Fig. 1. Scheme of a collection conveyor with 3 bunkers

To describe the transport system, a dimensionless model of a conveyor section was used [10, 23]. Dimensionless parameters were introduced that characterize the state of the parameters of a separate section of the transport system:

$$\begin{aligned} \tau &= \frac{t}{T_{d}}, \quad \xi_{nk} = \frac{S_{nk}}{S_{d0}}, \quad \xi_{d nk} = \frac{S_{d nk}}{S_{d0}}, \\ \gamma_{nk}(\tau) &= \lambda_{nk}(t) \frac{T_{d}}{S_{d0}[\chi]_{0max}}, \quad (1) \end{aligned}$$

$$\begin{aligned} \gamma_{\min nk} &\leq \gamma_{nk}(\tau) \leq \gamma_{\max nk}, \quad g_{0}(\tau) = a_{0}(t) \frac{T_{d}}{S_{d0}}, \\ \theta_{0 nk}(\tau, \xi_{nk}) &= \frac{[\chi]_{0 nk}(t, S_{nk})}{[\chi]_{0max}}, \end{aligned}$$

$$\begin{aligned} \theta_{1 nk}(\tau, \xi_{nk}) &= \frac{[\chi]_{1 nk}(t, S_{nk})}{[\chi]_{0max}} = \\ &= \frac{[\chi]_{0 mk}(t, S_{nk}) a_{nk}(t)}{[\chi]_{0max}} = \theta_{0 nk}(\tau, \xi_{nk}) g_{nk}(\tau), \end{aligned}$$

$$\begin{aligned} \eta_{n}(\tau) &= \frac{N_{m}(t)}{S_{d0}[\chi]_{0max}}, \quad \eta_{m st} = \frac{N_{m st}}{S_{d0}[\chi]_{0max}}, \end{aligned}$$

where  $S_{d\ mk}$  is the length of the *k*-th section of the m-th input conveyor (*m*=1, 2, 3);  $T_d$  is the characteristic time during which the material entering the collection conveyor of length  $S_{d0}$ , reaches the exit point of the collection conveyor and enters the accumulating tank N<sub>0</sub>(t). The flow of material from the output section (*k*=1) *m*-th linear conveyor enters the main conveyor belt at point  $S_0$ . To control the flow of material [ $\chi$ ]<sub>1</sub>  $_{m1}(t, S_{d\ m1})$ , coming from the *m*-th conveyor to the collection conveyor, an accumulating bunker, filled with material by the amount  $N_m(t)$ ,  $N_m \min \langle N_m(t) \langle N_m \max$ . The material flow [ $\chi$ ]<sub>1</sub>  $_{m2}(t, S_{dm2})$  from the previous section (*k*=2) enters the accumulating bunker  $N_m(t)$ . The material level is controlled by changing the flow intensity  $\lambda_{m1}(t)$ . When constructing a model of the *m*-th linear conveyor, we will use the assumptions [17, 18]:

1) section k=1 of the *m*-th linear conveyor is a guide section. The length of the section  $S_{d \ m1}$  is much less than the length of the section of the collection conveyor,  $\xi_{d \ m1} \rightarrow 0$ ;

2) the value of the material flow  $[\chi]_{1\ m2}(t,\ S_{dm2})$ , entering the bunker  $N_m(t)$  is known;

3) conveyor belt speed  $a_0(t)$  is constant.

Taking into account the indicated assumptions, the equation that determines the state of the flow parameters of the m–th linear conveyor takes the form [17, 18]

$$\frac{dn_m(\tau)}{dt} = \theta_{1m}(\tau) - \gamma_m(\tau), \quad n_m(0) = n_{mst},$$

$$n_{mmin} \le n_m(\tau) \le n_{mmax}, \quad (2)$$

$$\begin{split} &\gamma_{\min mt} \leq \gamma_{mt}(\tau) \leq \gamma_{\max mt}, \quad \theta_{1m}(\tau) = \theta_{1m2}(\tau,\xi_{dm2}), \\ &\gamma_{m}(\tau) = \gamma_{mt}(\tau), \quad m = 1...3. \end{split}$$

To describe the state of the flow parameters of the collection conveyor, the equation was used:

$$\begin{split} &\frac{\partial \Theta_{0}(\tau,\xi)}{\partial \tau} + g_{0}(\tau) \frac{\partial \Theta_{0}(\tau,\xi)}{\partial \xi} = \sum_{m=1}^{3} \delta \left( \xi - (\xi_{d} - \xi_{0m}) \right) \gamma_{m}(\tau), \\ &\Theta_{0}(0,\xi) = \psi(\xi), \qquad (3) \\ &\Theta_{0}(\tau,\xi) \leq \Theta_{0max}, \quad \Theta_{0}(\tau,\xi) = \Theta_{001}(\tau,\xi_{01}), \quad \xi = \xi_{01}, \\ &\xi_{d} = \xi_{d01} = 1, \ \Theta_{1}(\tau,\xi) = \Theta_{0}(\tau,\xi) \ g_{0}(\tau), \end{split}$$

where  $\psi(\xi)$  is the linear dimensionless density of the material at time  $\tau=0$ ;  $\delta(\xi)$  is the Dirac function.

The solution of equation (3) determines the linear density of the material at the point of the collection conveyor with the coordinate  $\xi$  at the time  $\tau$ , has the form [24]:

$$\begin{aligned} \theta_{0}(\tau,\xi) &= H(\xi - G(\tau))\psi(\xi - G(\tau)) + \\ &+ \sum_{m=1}^{3} \begin{pmatrix} H(\xi - (\xi_{d} - \xi_{0m})) - \\ -H(\xi - (\xi_{d} - \xi_{0m}) - G(\tau)) \end{pmatrix} \frac{\gamma_{m}(\tau_{\xi m})}{g_{0}(\tau_{\xi m})}, \end{aligned}$$
(4)  
$$G(\tau) &= \int_{0}^{\tau} g_{0}(\alpha) d\alpha, \quad \tau_{\xi m} = G^{-1}(G(\tau) - \xi + (\xi_{d} - \xi_{0m})), \qquad (5)$$

where  $H(\xi)$  is the Heaviside function. The flow of material  $\theta_1(\tau, \xi)$  at the output of the collection conveyor  $\xi = \xi_d = 1$  can be determined through the linear density of the material  $\theta_0(\tau,\xi)$  and the speed of the belt  $g_0(\tau)$ 

$$\begin{aligned} \theta_{1}(\tau,1) &= g_{0}(\tau) H (1 - G(\tau)) \psi (1 - G(\tau)) + \\ &+ g_{0}(\tau) \sum_{m=1}^{3} (H(\xi_{1m}) - H(\xi_{1m} - G(\tau))) \frac{\gamma_{m}(\tau_{1m})}{g_{0}(\tau_{1m})}, \\ &\tau_{1m} = G^{-1} (G(\tau) - \xi_{0m}). \end{aligned}$$

For a constant speed of movement of the speed  $g_0(\tau)=g_0$  is

$$G(\tau) = g_0 \tau, \quad \tau_{1m} = G^{-1}(g_0 \tau - \xi_{0m}) = \tau - \Delta \tau_{1m},$$

$$\Delta \tau_{1m} = \xi_{0m} / g_0 \quad \Delta \tau_{10} = \xi_d / g_0,$$

$$\begin{aligned} \theta_{1}(\tau,1) &= g_{0}H\left(g_{0}\left(\Delta\tau_{10}-\tau\right)\right)\psi\left(1-g_{0}\tau\right) + \\ &+ \sum_{m=1}^{3}\left(1-H\left(\frac{1}{g_{0}}\left(\Delta\tau_{1m}-\tau\right)\right)\right)\gamma_{m}(\tau-\Delta\tau_{1m}). \end{aligned}$$

The value of the transport delay  $\Delta \tau_{10}$  corresponds to the time interval during which the material at the input of the collection conveyor section reaches the output of the section and moves into the accumulating tank  $N_0(t)$ . Since the collecting conveyor does not contain an input bunker, the furthest point where material can enter is the entry point of the third bunker. This point was chosen as the origin of coordinates, obtaining the identical equality  $\lfloor_{0m}=\rfloor_d=1$ . It should be noted that the choice of the  $T_d$  value is arbitrary. It determines the scale of the dimensionless parameters. For a constant belt speed, the conveyor sections  $T_d$  was chosen from the condition  $T_d=S_{d0}/a_0$ ,  $g_0=1$ , and, accordingly, the expression for the output flow takes the form

$$\theta_{10}(\tau) = \theta_1(\tau, 1) = H(\Delta \tau_{10} - \tau) \psi(1 - \tau) +$$
  
+ 
$$\sum_{m=1}^{3} (1 - H(\Delta \tau_{1m} - \tau)) \gamma_m(\tau - \Delta \tau_{1m}).$$
(6)

As a next step, an equation was added that determines the states of the material in the accumulating tank  $n_0(t)$ 

$$\frac{dn_{0}(\tau)}{dt} = \theta_{10}(\tau), \quad 0 \le n_{0}(\tau) \le n_{0\text{max}}, \quad n_{0}(0) = 0.$$
(7)

Combining the Equations (2), (6), (7)

$$\frac{dn_{m}(\tau)}{dt} = \Theta_{1m}(\tau) - \gamma_{m}(\tau), \quad n_{m}(0) = n_{mst},$$

$$n_{mmin} \leq n_{m}(\tau) \leq n_{mmax}, \quad (8)$$

$$\frac{dn_{0}(\tau)}{dt} = \Theta_{10}(\tau), \quad n_{0}(0) = 0,$$

$$0 \leq n_{0}(\tau) \leq n_{0max}, \quad m = 1, 2, 3,$$

$$\Theta_{10}(\tau) = H(1 - \tau)\psi(1 - \tau) +$$

$$+ \sum_{m=1}^{3} (1 - H(\Delta\tau_{1m} - \tau))\gamma_{m}(\tau - \Delta\tau_{1m}),$$

$$\gamma_{\min m} \leq \gamma_{m}(\tau) \leq \gamma_{\max m},$$

a model of the transport system, taking into account the introduced restrictions, was obtained,  $\xi_{dm1} \rightarrow 0$ . The system of equations (8) contains delays that are constant in magnitude

 $0\!<\!\Delta\tau_{_{11}}\!<\!\Delta\tau_{_{12}}\!<\!\Delta\tau_{_{13}}.$ 

Thus, at the time  $\tau < \Delta \tau_{11}$  the output flow of material is determined by the rest of the material along the collection conveyor  $\psi(\xi)$ :

 $\theta_{10}(\tau) \!=\! \psi(1\!-\!\tau), \ 0\!<\!\tau\!<\!\Delta\tau_{11}.$ 

For a time interval  $\tau < \Delta \tau_{11}$ , it is impossible to change the value of the flow  $\theta_{10}(\tau)$  by controlling the intensity of the material flow  $\gamma_1(\tau)$ . For the next time interval, the expression for the material flow is:

 $\boldsymbol{\theta}_{10}\!\left(\boldsymbol{\tau}\right)\!=\!\boldsymbol{\psi}\!\left(\boldsymbol{1}\!-\!\boldsymbol{\tau}\right)\!+\!\boldsymbol{\gamma}_{1}\!\left(\boldsymbol{\tau}\!-\!\boldsymbol{\Delta}\!\boldsymbol{\tau}_{11}\right)\!,\quad\!\!\boldsymbol{\Delta}\!\boldsymbol{\tau}_{11}\!\leq\!\boldsymbol{\tau}\!<\!\boldsymbol{\Delta}\!\boldsymbol{\tau}_{12}.$ 

The value of the output flow can be controlled by changing the value of the flow intensity  $\gamma_1(\tau)$ . In this case, the change in the value of the output flow occurs with a delay  $\Delta \tau_{11}$ . The minimum value of the output flow is limited by the value  $\psi(1-\tau)$ . For the next time interval, the expression for the value of the output flow takes into account the incoming material from the second main conveyor with the intensity  $\gamma_2(\tau)$  and the transport delay  $\Delta \tau_{12}$ 

$$\theta_{10}(\tau) = \psi(1 - \tau) + \gamma_1(\tau - \Delta \tau_{11}) + \gamma_2(\tau - \Delta \tau_{12}),$$

 $\Delta \tau_{12} \leq \tau < \Delta \tau_{13}.$ 

It is allowed to regulate the value of the output flow when changing the intensities  $\gamma_1(\tau)$ ,  $\gamma_2(\tau)$  with transport delays  $\Delta \tau_{11}$ ,  $\Delta \tau_{12}$ . An exception is the requirement to regulate the output flow in the range

$$0\!\leq\!\theta_{10}\!\left(\tau\right)\!\leq\!\psi\!\left(1\!-\!\tau\right)\!.$$

At  $\tau < \Delta \tau_{13}$ , the transport system operated in a transient mode, for which the possibility of regulating the output flow by changing the intensity  $\gamma_m(\tau)$  was limited or completely absent. When  $\Delta \tau_{13} < \tau$ , the value of the output flow is expressed through the values of the intensities  $\gamma_m(\tau)$  of the flow of material from the accumulating bunkers

$$\theta_{10}(\tau) = \gamma_1(\tau - \Delta \tau_{11}) + \gamma_2(\tau - \Delta \tau_{12}) + \gamma_3(\tau - \Delta \tau_{13}),$$

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\Delta \tau_{13} \leq \tau.
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The output flow can be controlled over the entire range of allowable values of the function  $\theta_{10}(\tau)$ . When constructing a control system for the output flow  $\theta_{10}(\tau)$ , it is required to change the values of the intensities  $\gamma_m(\tau)$  of the material flow ahead of  $\Delta \tau_{1m}$ .

The linear density of the material on the conveyor belt  $\theta_0(\tau,\xi)$  must not exceed the maximum allowable value  $\theta_{0max}$ . The restriction should be fulfilled for an arbitrary

moment of time  $\tau$  and coordinates  $\xi=1-\xi_{1\kappa}$ , in which the material enters the collection conveyor from the c *k*-th linear conveyor

$$\begin{split} & \theta_0 \left( \tau, 1 - \xi_{1k} \right) = H \left( 1 - \xi_{1k} - G(\tau) \right) \psi \left( 1 - \xi_{1k} - G(\tau) \right) + \\ & + \sum_{m=1}^3 \begin{pmatrix} H \left( \xi_{1m} - \xi_{1k} \right) - \\ -H \left( \xi_{1m} - \xi_{1k} - G(\tau) \right) \end{pmatrix} \frac{\gamma_m \left( \tau - \left( \Delta \tau_{1m} - \Delta \tau_{1k} \right) \right)}{g_0 \left( \tau - \left( \Delta \tau_{1m} - \Delta \tau_{1k} \right) \right)} \leq \\ & \leq \theta_{0max} = \frac{\theta_{1max}}{g_0(\tau)}. \end{split}$$

The last inequality for the case of constant belt speed  $g_0=1$  of the collection conveyor can be rewritten in the form

$$\begin{split} \gamma_{3}(\tau) &\leq \theta_{1max}; \end{split} \tag{9} \\ \gamma_{2}(\tau) + \gamma_{3} \left( \tau - \left( \Delta \tau_{13} - \Delta \tau_{12} \right) \right) &\leq \theta_{1max}, \\ \gamma_{3}(\alpha) &= \psi(-\alpha) \quad \Pi p \mathbf{H} \quad \alpha < 0; \\ \gamma_{1}(\tau) + \gamma_{2} \left( \tau - \left( \Delta \tau_{12} - \Delta \tau_{11} \right) \right) + \\ + \gamma_{3} \left( \tau - \left( \Delta \tau_{13} - \Delta \tau_{11} \right) \right) &\leq \theta_{1max}, \\ \gamma_{2}(\alpha) &= 0, \quad \gamma_{3}(\alpha) = \psi(1 - \Delta \tau_{12} - \alpha) \quad \Pi p \mathbf{H} \quad \alpha < 0. \end{split}$$

The resulting expressions make it possible to determine the value of the output material flow of the collection conveyor with known values of the input material flows  $\gamma_m(\tau)$  from the accumulating bunkers.

# 5. 2. Synthesis of the optimal control algorithm for the flow parameters of the transport system

The problem of the minimum time  $\tau_{load}$  for filling the accumulating tank  $n_0(\tau)$  with the capacity  $n_{0\text{max}}$  is considered. The material flow speed is controlled by bunker gates for small-sized material or feeders for large-sized material. The performance of the shutter or feeder  $u_m(\tau)$  is set by changing the size of the outlet of the hopper or the operating parameters of the feeder. The problem of optimal control of the flow parameters of the transport system was formulated as follows: it is required to determine the optimal control of the intensity of the material flow  $u_m(\tau)=\underline{\gamma_m(\tau)}$ , coming from the bunker  $n_m(\tau)$  to the collection conveyor, which leads to a minimum

$$\tau_{load} \rightarrow \min,$$
 (10)

with differential connections

$$\frac{dn_m(\tau)}{dt} = \theta_{1\,m}(\tau) - u_m(\tau), \tag{11}$$

$$\frac{dn_{0}(\tau)}{dt} = H(1-\tau)\psi(1-\tau) + \sum_{m=1}^{3} (1-H(\Delta\tau_{1m}-\tau))u_{m}(\tau-\Delta\tau_{1m})$$

restrictions on phase variables

$$n_{mmin} \le n_m(\tau) \le n_{mmax}, \quad n_{mmin} = 0, \tag{12}$$

### control restrictions

$$u_{3}(\tau) \leq \theta_{1\max}; \tag{13}$$

where  $u_3(\alpha) = \psi(-\alpha)$  by  $\alpha < 0$ ;

$$\begin{split} & u_1(\tau) + u_2(\tau - (\Delta \tau_{12} - \Delta \tau_{11})) + \\ & + u_3(\tau - (\Delta \tau_{13} - \Delta \tau_{11})) \leq \theta_{1max}, \end{split}$$

where  $u_2(\alpha) = 0$ ,  $u_3(\alpha) = \psi(1 - \Delta \tau_{12} - \alpha)$  by  $\alpha < 0$ ,

and initial conditions

$$n_0(0) = 0, n_m(0) = n_{ms}, m = 1, 2, 3.$$
 (14)

The quality criterion (9) can be converted to an integral form

$$J = \int_{0}^{\tau_{load}} F_{l} d\tau \rightarrow \min, \quad F_{l} = 1.$$
 (15)

The condition of the maximum principle is obtained as a result of successive transformations. By definition of the quality functional (15) is

$$\frac{dJ}{dt} = F_1.$$

On the other hand, considering  $F_1$  and J as functions of time  $\tau$  and coordinates  $n_0$ ,  $n_m$  for an admissible control

$$\frac{dJ}{d\tau} = \frac{\partial J}{\partial \tau} + \frac{\partial J}{\partial n_0} \frac{dn_0}{d\tau} + \sum_m \frac{\partial J}{\partial n_m} \frac{dn_m}{d\tau} =$$
$$= \frac{\partial J}{\partial \tau} + \psi_0 \frac{dn_0}{d\tau} + \sum_m \psi_m \frac{dn_m}{d\tau},$$

$$\psi_0 = \frac{\partial J}{\partial n_0}, \quad \psi_m = \frac{\partial J}{\partial n_m},$$

it follows that

$$\frac{\partial J}{\partial \tau} = F_1 - \psi_0 \frac{dn_0}{d\tau} - \sum_m \psi_m \frac{dn_m}{d\tau}.$$
 (16)

Equation (16) is the Hamilton-Jacobi equation with the Hamilton function

$$H = -F_1 + \psi_0 \frac{dn_0}{d\tau} + \sum_m \psi_m \frac{dn_m}{d\tau}.$$
 (17)

After substituting the differential constraint equation (11) into function (17), the Hamiltonian function with control delay was obtained

$$H = -F_{1} + \psi_{0}(\tau) \begin{pmatrix} H(1-\tau)\psi(1-\tau) + \\ +\sum_{m=1}^{3} (1-H(\Delta\tau_{1m}-\tau)) \times \\ +\sum_{m=1}^{3} \psi_{m}(\tau) (\theta_{1m}(\tau) - u_{m}(\tau)). \end{pmatrix}$$
(18)

Taking into account (18), the quality criterion (15) was written as

$$J = \int_{0}^{\tau_{load}} \left( \psi_{0}(\tau) \begin{pmatrix} H(1-\tau)\psi(1-\tau) + \\ +\sum_{m=1}^{3} (1-H(\Delta\tau_{1m}-\tau)) \times \\ +\sum_{m=1}^{3} \psi_{m}(\tau) (\theta_{1m}(\tau) - u_{m}(\tau)) - H. \right) d\tau \rightarrow \min.$$
(19)

After replacing the variabl  $\beta = (\tau - \Delta \tau_{1m})$  and allowing the representation for the function  $\psi_0(\tau)$  outside the control area  $\tau > \tau_{load}$  in the form  $\psi_0(\tau) = 0$ , it was obtained

$$\begin{aligned} & \int_{0}^{\tau_{logal}} \psi_{0}(\tau) \Big( 1 - H(\Delta \tau_{1m} - \tau) \Big) u_{m}(\tau - \Delta \tau_{1m}) d\tau = \\ &= \int_{0}^{\tau_{logal} - \Delta \tau_{1m}} \psi_{0}(\beta + \Delta \tau_{1m}) u_{m}(\beta) d\beta \approx \\ &\approx \int_{0}^{\tau_{logal}} \psi_{0}(\beta + \Delta \tau_{1m}) u_{m}(\beta) d\beta. \end{aligned}$$

$$(20)$$

Substituting the result obtained into (19), the quality criterion for the control problem takes the form

$$J = \int_{0}^{\tau_{load}} \begin{pmatrix} \psi_{0}(\tau) H(1-\tau) \psi(1-\tau) + \\ + \sum_{m=1}^{3} \psi_{0}(\tau + \Delta \tau_{1m}) u_{m}(\tau) + \\ + \sum_{m=1}^{3} \psi_{m}(\tau) (\theta_{1m}(\tau) - u_{m}(\tau)) - H \end{pmatrix} d\tau \rightarrow \min, \quad (21)$$

and, accordingly, Hamiltonian (18) can be represented in the form

$$H = -F_{1} + \psi_{0}(\tau)H(1-\tau)\psi(1-\tau) + + \sum_{m=1}^{3}\psi_{0}(\tau + \Delta\tau_{1m})u_{m}(\tau) + + \sum_{m=1}^{3}\psi_{m}(\tau)(\theta_{1m}(\tau) - u_{m}(\tau)).$$
(22)

Taking into account the restrictions on the phase variables, the optimality conditions for the control problem are written in the form

$$L = H + \sum_{m=1}^{3} \mu_0(\tau) n_m(\tau) + \sum_{m=1}^{3} \mu_1(\tau) (n_{mmax} - n_m(\tau)), \qquad (23)$$
$$\frac{d\psi_m(\tau)}{dt} = -\frac{\partial L}{\partial n_m} = -\mu_{0m} - \mu_{1m}, \ \psi_m(\tau_{load}) = 0,$$
$$\frac{d\psi_0(\tau)}{dt} = -\frac{\partial L}{\partial n_0} = 0.$$

followed by the transformation of the Hamilton function to the form

$$H = -1 + \psi_0(\tau) H(1-\tau) \psi(1-\tau) +$$
  
+ 
$$\sum_{m=1}^{3} (\psi_0(\tau + \Delta \tau_{1m}) - \psi_m(\tau)) u_m(\tau) +$$
  
+ 
$$\sum_{m=1}^{3} \psi_m(\tau) \theta_{1m}(\tau) \rightarrow \max.$$
 (24)

Since the Hamilton function is linear in the control  $u_m(\tau)$ , the maximum of the Hamilton function is reached at the ends of the segment of control change, whence, the optimal control has the form

$$u_m(\tau) \rightarrow u_{mmax}, \quad \psi_0(\tau + \Delta \tau_{1m}) - \psi_m(\tau) \ge 0,$$

$$u_m(\tau) \rightarrow 0, \quad \psi_0(\tau + \Delta \tau_{1m}) - \psi_m(\tau) < 0.$$

From the adjoint system can be found  $\psi_0(\tau), \psi_m(\tau)$ :

$$\Psi_0(\tau) = \Psi_0, \quad \Psi_m(\tau) = \int_0^{\tau} (\mu_{0m}(\alpha) - \mu_{1m}(\alpha)) d\alpha,$$

 $\psi_m(\tau_{load}) = 0.$ 

The joint solution of equations (11), (15), (16), taking into account the restrictions on phase trajectories and control, allows us to determine the optimal program for controlling the flow intensivity from the bunkers.

Of practical interest is the control program for a transport system containing largecapacity bunkers. To simplify the discussion of the results, let us dwell on the case when, at the initial moment of time, the filling level of the input bunkers with material  $n_m(0)=n_{m st}$  allows, during the time  $\tau_{load}$  of the process of filling the storage tank, not to reach the phase limitation  $0 < n_m(\tau) < n_{m st}$ . Then from the solution of equations (23) it follows

$$\begin{split} \psi_{m}(\tau) &= \psi_{m} = 0, \\ \psi_{0}(\tau + \Delta \tau_{1m}) &= H(\tau_{load} - (\Delta \tau_{1m} + \tau))\psi_{0c}, \\ \psi_{0}(\tau) &= \text{const} = \psi_{0c}, \\ H &= -1 + \psi_{0}(\tau) H(1 - \tau) \psi(1 - \tau) + \\ &+ \sum_{m=1}^{3} \psi_{0}(\tau + \Delta \tau_{1m}) u_{m}(\tau) \rightarrow \text{max}. \end{split}$$
(25)

The Hamilton function determines the control  $u_m(\tau)$  of the material flow from the *m*-th bunker (табл. 1) (Table 1) under constraints (12), (13).

#### Table 1

Bunker control modes	(General o	case)
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$N_{2} N_{2}$	Time interval	$u_1(\tau)$	$u_2(\tau)$	$u_3(\tau)$
1	$\tau_{load}$ – $\Delta \tau_{11}$ < $\tau \leq \tau_{load}$	From the control		
2	$\tau_{load} - \Delta \tau_{12} < \tau \leq \tau_{load} - \Delta \tau_{11}$	$u_1(\tau) \rightarrow \max$	constraint	
3	$\tau_{load} - \Delta \tau_{13} < \tau \leq \tau_{load} - \Delta \tau_{12}$	$u_1(\tau) \rightarrow \max$	$u_2(\tau) \rightarrow \max$	conditions
4	$0 < \tau \leq \tau_{load} - \Delta \tau_{13}$	$u_1(\tau) \rightarrow \max$	$u_2(\tau) \rightarrow \max$	$u_3(\tau) \rightarrow \max$

From a practical point of view, the mode of operation of the transport system, for which the requirements are met, is of interest:

a) at the initial time  $\tau=0$  the conveyor belt is empty;

δ) at the end time  $\tau = \tau_{load}$  load the tape is empty;

B) the energy costs for moving the material during the time  $\tau_{load}$  of filling the storage tank should be minimal.

These requirements are expressed in the form of equations:

$$\int_{0}^{1} \theta_{0}(0,\xi) d\xi = 0, \quad \int_{0}^{1} \theta_{0}(\tau_{\text{load}},\xi) d\xi = 0, \quad (26)$$

$$H = -1 + \sum_{m=1}^{3} \Psi_0(\tau + \Delta \tau_{1m}) u_m(\tau) \rightarrow \max.$$
(27)

The considered control mode can be adapted for the problem of filling the tank with a material of a given concentration (mixing the material in the required proportion). Equation (26) characterizes the state of the transport system, in which at the initial and final time the conveyor belt is not filled with material. The condition of minimum energy consumption for moving material along the collection conveyor determines the bunker control strategy in the case when the control problem has more than one solution. In accordance with this strategy, the maximum material flow intensivity is achieved at the first bunker  $u_1(\tau) \rightarrow \max$  (the closest bunker to the section output), then for the second bunker  $u_2(\tau) \rightarrow \max$ , and only then for the third bunker. In this case, conditions (12) must be observed, which limit the maximum load on the belt. The value  $u_m(\tau)$  for the considered control algorithm takes either the maximum allowable value or a value equal to zero (Table 2).

Table 2

Bunker control modes (at the start and end of control, the conveyor belt is not filled with material)

Nº Nº	Time interval	$u_1(\tau)$	$u_2(\tau)$	$u_3(\tau)$
1	$\tau_{load}$ - $\Delta \tau_{11} < \tau \leq \tau_{load}$	0	0	0
2	$\tau_{load} - \Delta \tau_{12} < \tau \leq \tau_{load} - \Delta \tau_{11}$	$u_1(\tau) \rightarrow \max$	0	0
3	$\tau_{load} - \Delta \tau_{13} < \tau \leq \tau_{load} - \Delta \tau_{12}$	$u_1(\tau) \rightarrow \max$	$u_2(\tau) \rightarrow \max$	0
4	$0 < \tau \leq \tau_{load} - \Delta \tau_{13}$	$u_1(\tau) \rightarrow \max$	$u_2(\tau) \rightarrow \max$	$u_3(\tau) \rightarrow \max$

To assess the level of material in the accumulator tank, the location of the bunkers will be determined by the coordinates  $\xi_{11}=1/3$ ,  $\xi_{12}=2/3$ ,  $\xi_{13}=1$ . With a constant belt speed  $g_0=1$  and the accepted location of the bunkers, the transport delay is constant  $\Delta \tau_{11}=1/3$ ,  $\Delta \tau_{12}=2/3$ ,  $\Delta \tau_{13}=1$  and is proportional to the length of the transport route. The amount of material in the tank at an arbitrary point in time is determined by the equation

$$\frac{dn_0(\tau)}{d\tau} = \sum_{m=1}^{3} \left( 1 - H\left( \Delta \tau_{1m} - \tau \right) \right) u_m(\tau - \Delta \tau_{1m}),$$
$$n_0(0) = 0,$$

which can be represented in the following form

$$n_0(\tau) = \int_0^{\tau} \sum_{m=1}^{3} (1 - H(\Delta \tau_{1m} - \beta)) u_m(\beta - \Delta \tau_{1m}) d\beta.$$

The presented solution is used to calculate the loading time of the accumulating tank

$$n_0(\tau_{load}) = \int_0^{\tau_{load}} \sum_{m=1}^3 (1 - H(\Delta \tau_{1m} - \tau)) u_m(\tau - \Delta \tau_{1m}) d\tau.$$
(28)

The solution of equation (28) for different maximum allowable control values was obtained in the form of four options. The results of a numerical experiment based on the developed model (3)–(8) of the transport conveyor are shown Fig. 2.

Variant No 1:  $u_{1\max} = u_{2\max} = u_{3\max}, u_{1\max} \ge \theta_{1\max}$ .

The solution of equation (28) for this variant has the form

$$\boldsymbol{\textit{n}}_{\!\!\!0}\left(\boldsymbol{\tau}\right) \!=\! \left(\!1\!-\!\boldsymbol{\textit{H}}\!\left(\boldsymbol{\Delta}\boldsymbol{\tau}_{11}\!-\!\boldsymbol{\tau}\right)\!\right)\!\boldsymbol{\theta}_{1\text{max}}\!\left(\boldsymbol{\tau}\!-\!\boldsymbol{\Delta}\boldsymbol{\tau}_{11}\right)\!,$$

$$n_0(\tau_{load}) = \theta_{1max}(\tau_{load} - \Delta \tau_{11})$$

$$\boldsymbol{\tau}_{\textit{load}} = \frac{\textit{n}_{0}\!\left(\boldsymbol{\tau}_{\textit{load}}\right)}{\boldsymbol{\theta}_{1\text{max}}} + \Delta\boldsymbol{\tau}_{11}.$$

The solution of equation (28) for this variant has the form (Fig. 2, a,  $\delta$ ).

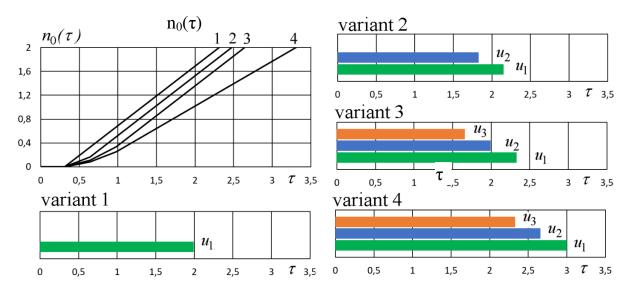


Fig. 2. Transport system control modes: a - filling the accumulating tank with different control options; b - variant 1; c - variant 2; d - variant 3; e - variant 4

Variant No 2:  $u_{1\max}=u_{2\max}=u_{3\max}$ ,  $u_{1\max}+u_{2\max}\ge \theta_{1\max}$ ,  $u_{1\max}\le \theta_{1\max}$ .

The accumulating bunker filling dynamics for the discussed control variant is determined by the expressions:

$$\begin{split} & n_0(\tau) = \left(1 - H(\Delta\tau_{11} - \tau)\right) u_{1\max}(\tau - \Delta\tau_{11}) + \\ & + \left(1 - H(\Delta\tau_{12} - \tau)\right) (\theta_{1\max} - u_{1\max})(\tau - \Delta\tau_{12}), \\ & n_0(\tau_{load}) = u_{1\max}(\Delta\tau_{12} - \Delta\tau_{11}) + \theta_{1\max}(\tau_{load} - \Delta\tau_{12}), \\ & \tau_{load} = \frac{n_0(\tau_{load}) - u_{1\max}(\Delta\tau_{12} - \Delta\tau_{11})}{\theta_{1\max}} + \Delta\tau_{12}. \end{split}$$

The accumulating tank is filled with the first and second bunkers. The third bunker is not functioning (Fig. 2, a, e).

Variant No 3:  $u_{1\max}=u_{2\max}=u_{3\max}$ ,  $u_{1\max}+u_{2\max}+u_{3\max}\ge \theta_{1\max}$ ,  $u_{1\max}+u_{2\max}\le \theta_{1\max}$ .

The flow characteristics of the transport system can be obtained from the expressions

$$\begin{split} & n_{0}(\tau) = \left(1 - H(\Delta\tau_{11} - \tau)\right) u_{1max}(\tau - \Delta\tau_{11}) + \\ & + \left(1 - H(\Delta\tau_{12} - \tau)\right) u_{1max}(\tau - \Delta\tau_{12}) + \\ & + \left(1 - H(\Delta\tau_{13} - \tau)\right) (\theta_{1max} - 2u_{1max})(\tau - \Delta\tau_{13}), \\ & n_{0}(\tau_{load}) = u_{1max}(\Delta\tau_{12} - \Delta\tau_{11}) + \\ & + 2u_{1max}(\Delta\tau_{13} - \Delta\tau_{12}) + \theta_{1max}(\tau_{load} - \Delta\tau_{13}), \\ & \tau_{load} = \\ & = \frac{n_{0}(\tau_{load}) - u_{1max}(\Delta\tau_{13} - \Delta\tau_{11}) - u_{2max}(\Delta\tau_{13} - \Delta\tau_{12})}{\theta_{1max}} + \\ & + \Delta\tau_{13}. \end{split}$$

The accumulating tank is filled with the first, second and third bunker.

Variant No 4:  $u_{1\max} = u_{2\max} = u_{3\max}$ ,  $u_{1\max} + u_{2\max} + u_{3\max} < \theta_{1\max}$ .

The filling level of the accumulating tank and the loading time are determined by the equations

$$\begin{split} n_{0}(\tau) &= \left(1 - H(\Delta\tau_{11} - \tau)\right) u_{1max} \left(\tau - \Delta\tau_{11}\right) + \\ &+ \left(1 - H(\Delta\tau_{12} - \tau)\right) u_{1max} \left(\tau - \Delta\tau_{12}\right) + \\ &+ \left(1 - H(\Delta\tau_{13} - \tau)\right) u_{1max} \left(\tau - \Delta\tau_{13}\right), \\ n_{0}(\tau_{load}) &= u_{1max} \left(\Delta\tau_{12} - \Delta\tau_{11}\right) + \\ &+ 2u_{1max} \left(\Delta\tau_{13} - \Delta\tau_{12}\right) + 3u_{1max} \left(\tau_{load} - \Delta\tau_{13}\right), \\ \tau_{load} &= \\ &= \frac{n_{0}(\tau_{load}) - u_{1max} \left(\Delta\tau_{13} - \Delta\tau_{11}\right) - u_{2max} \left(\Delta\tau_{13} - \Delta\tau_{12}\right)}{u_{1max} + u_{2max} + u_{3max}} + \\ &+ \Delta\tau_{13}. \end{split}$$

The material flow control modes in the *m*-th bunker when calculating the loading time  $\tau_{load}$  of the storage tank are presented in Table 3.

Variant	Time interval	$u_1(\tau)$	$u_2(\tau)$	$u_3(\tau)$
$u_{1\max} \ge \theta_{1\max}$	$\tau_{load} - \Delta \tau_{11} < \tau \leq \tau_{load}$	0	0	0
	$0 < \tau \leq \tau_{load} - \Delta \tau_{11}$	$\theta_{1\max}$	0	0
	$\tau_{load} - \Delta \tau_{11} < \tau \leq \tau_{load}$	0	0	0

Table 3 Bunker control modes  $(u_{1\max}=u_{2\max}=u_{3\max})$ 

$2u_{1\max} \ge \theta_{1\max}$ ,	$\tau_{load} - \Delta \tau_{12} < \tau \leq \tau_{load} - \Delta \tau_{11}$	$u_{1\max}$	0	0
$u_{1\max} < \theta_{1\max}$	$0 < \tau \leq \tau_{load} - \Delta \tau_{12}$	$u_{1\max}$	$\theta_{1\max}$ - $u_{1\max}$	0
$3u_{1\max} \ge \theta_{1\max}$ ,	$\tau_{load} - \Delta \tau_{11} < \tau \leq \tau_{load}$	0	0	0
$2u_{1\max} < \theta_{1\max}$	$\tau_{load} - \Delta \tau_{12} < \tau \leq \tau_{load} - \Delta \tau_{11}$	$u_{1\max}$	0	0
	$\tau_{load} - \Delta \tau_{13} < \tau \leq \tau_{load} - \Delta \tau_{12}$	$u_{1\max}$	$u_{1\max}$	0
	$0 < \tau \leq \tau_{load} - \Delta \tau_{13}$	$u_{1\max}$	$u_{1\max}$	$\theta_{1\max}$ -2 $u_{1\max}$
$3u_{1\max} < \theta_{1\max}$	$\tau_{load} - \Delta \tau_{11} < \tau \leq \tau_{load}$	0	0	0
	$\tau_{load} - \Delta \tau_{12} < \tau \leq \tau_{load} - \Delta \tau_{11}$	$u_{1 \max}$	0	0
	$\tau_{load} - \Delta \tau_{13} < \tau \leq \tau_{load} - \Delta \tau_{12}$	$u_{1\max}$	$u_{1\max}$	0
	$0 < \tau \leq \tau_{load} - \Delta \tau_{13}$	$u_{1\max}$	$u_{1\max}$	$u_{1\max}$

At the initial moment of time, all bunkers are functioning. Since the Hamilton function is linear in control, the value for optimal control is expressed in terms of the maximum or minimum control values, subject to a limit on the maximum allowable density of the material for the conveyor belt.

# 6. Discussion of the results of modeling the collection conveyor

An analytical model of the transport system is proposed, taking into account the features of the movement of material along the technological route of a multi-section collection conveyor (3)–(8). In contrast to the known models of the collection conveyor with 3 bunkers [16, 17], the analytical model takes into account the following fundamental features of existing conveyor-type transport systems. Firstly, the initial distribution of the material along the transportation route, which, unlike existing models, makes it possible to obtain the value of the flow parameters, and, accordingly, form the optimal control during the initial movement of the belt. Secondly, the variable transport delay of the movement of the material along the conveyor section, which makes it possible to synthesize optimal controls for transient modes, which is impossible when using existing stationary models. Thirdly, the influence of the uneven distribution of material along the transportation route on the flow characteristics of the transport system. At present, this is of particular importance due to the urgency of the problem of reducing the specific energy consumption in the extraction of material. Fourthly, restrictions on the maximum allowable linear density of the material along the belt, the speed of the belt and the intensity of the flow of material coming from the accumulating bunkers make it possible to exclude controls that lead to damage to the conveyor section.

The analytical model allows to determine:

- linear density of the material at a given point of the transport route for an arbitrary point in time (4);

- the value of the transport delay of the movement of material between two points of the transport route for an arbitrary point in time (5);

- the value of the output flow of the material of the transport conveyor for an arbitrary moment of time (6) at known intensities of material flows from the accumulating bunkers.

It should be noted that the relative lengths of the sections of the transport conveyor necessary for the calculation, as well as the law of change in time of the speed of the belt of individual sections and the values of the intensities of the flows of materials from the accumulation bunkers, must be known. As a limitation of this study, we should mention the assumption of a constant speed of the belt of individual sections in the synthesis of optimal control algorithms (9). When synthesizing the control algorithm, the control quality criterion (10) was used, which ensures maximum performance when the accumulating tank is filled. The requirement to minimize energy costs (27) for material transportation has narrowed the area of admissible controls.

When constructing an analytical model, the limitations associated with the presence of dynamic stresses in the belt during the operation of the conveyor in transient modes are not taken into account, which may make it impossible to ensure practical or theoretical expectations from the use of the research results.

The practical use of the proposed model consists in the possibility of synthesizing algorithms for optimal control of the flow parameters of the transport system of a mining enterprise for different control quality criteria. The prospect for further research is the synthesis of an optimal control system for a collection conveyor with 3 bunkers at a variable belt speed. This will allow to increase the fill factor of the material section of the collection conveyor.

### 7. Conclusions

1. An analytical model of a collection conveyor with 3 bunkers has been developed. Distinctive features of the presented model are taking into account the variable transport delay and the distribution of material along the transportation route. This gave advantages over the known results obtained using models with constant transport delay and without taking into account the initial / final distribution of material along the transport route. The advantages lie in the possibility of describing not only stationary, but also transient modes of functioning of the transport system. The result obtained is explained by the fact that the basis for constructing the model of the transport conveyor was the statistical theory of the description of production systems, within which the transport conveyor is considered as a dynamic distributed system. As one of the comparative estimates of the result, one should present the error with which the estimated amount of material in the accumulating tank is determined. For an extended collection conveyor with a tank of small capacity, the quantification of the error can be a significant part of its standard capacity.

2. An analytical model of a collection conveyor with 3 bunkers is used to synthesize algorithms for optimal control of the flow parameters of a transport system containing a variable transport delay. Accounting for the variable transport delay has made it possible to significantly expand the region of admissible optimal controls and improve the control accuracy. The main feature of the obtained optimal controls is that the theory of systems with aftereffect is used for the synthesis of controls. This made it possible to use the Pontryagin maximum principle for systems containing the transport delay in phase variables.

### **Conflict of interest**

The authors declare that they have no conflict of interest in relation to this research, including financial, personal, authorship or other nature that could affect the research and its results presented in this article.

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