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# THE IMPERFECTIONS OF CONDITIONAL PROGRAMS AND THE CASE FOR UNIVERSAL BASIC INCOME \*

Luís Guimarães† Diogo Lourenço‡

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#### **Abstract**

What is the impact of replacing conditional welfare programs with a Universal Basic Income (UBI) that costs the same? We answer this question using a general-equilibrium model with incomplete markets that accounts for three imperfections of conditional programs: incomplete take-up, illegitimate transfers, and administrative costs. We find that these imperfections, particularly incomplete take-up, substantially affect welfare. We also find that replacing the conditional programs with a UBI would increase capital stock, employment, and output, and lower inequality. Yet, the welfare effect of a UBI is not clear-cut. Aggregate welfare would fall in our benchmark, but a moderately larger UBI would be preferable to an equal expansion of conditional programs, especially for the least educated.

*Keywords*: Universal Basic Income; Welfare System; Take-up; Illegitimate Transfers; Administrative Costs; Labor Market Flows.

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<sup>&</sup>lt;sup>†</sup>Queen's University Belfast and cef.up. E-mail address: l.guimaraes@qub.ac.uk.

<sup>&</sup>lt;sup>‡</sup>University of Porto, School of Economics and Management and cef.up. E-mail address: dlourenco@fep.up.pt.

# 1 Introduction

There are several ideas for bolstering the capacity of welfare systems to alleviate poverty and inequality. One that has enjoyed noteworthy attention is the introduction of a universal basic income (UBI). The introduction of a fixed, universal, unconditional transfer would entail direct and general equilibrium effects on inequality, output, and welfare. In this paper, we illuminate these effects. We investigate the impact of replacing conditional welfare programs with a UBI that costs the same, i.e., is expenditure-neutral.<sup>1</sup>

To these ends, we build and discipline a model with heterogeneous agents and incomplete markets to resemble the US economy. Since we seek to illuminate the impact of replacing existing conditional programs with a UBI, we account for their magnitude and incentive structure. But our main contribution is to incorporate three key aspects of conditional programs as they are, demarcating our model from the ideal configuration assumed in the literature. In particular, we incorporate incomplete take-up, illegitimate transfers, and administrative costs. We find that explicitly modelling these imperfections substantially alters the estimated impacts of an expenditure-neutral UBI.

Incomplete take-up occurs when conditional programs do not reach all the eligible. It is a common and sizeable phenomenon. Focusing on US programs, the take-up rate is well below 100%, being closer to 80% for the *Earned-Income Tax Credit* (EITC) and the *Supplemental Nutrition Assistance Program* (SNAP), and as low as 60% for the *Supplemental Security Income* (SSI) and 45% for *Unemployment Insurance* (UI).<sup>2</sup> We model take-up parsimoniously by assuming that claims follow a random process, and that claim rates are typically less than unity and differ with level of education.

Illegitimate transfers occur when conditional programs offer relief to those not entitled to it. They are a significant phenomenon too, reaching up to 10% of the value of SNAP and SSI transfers, and as much as 25% of the EITC's. We model illegitimate transfers by allowing a fraction of a program's total transfers to go to ineligible claimants and to overpay eligible recipients.

Finally, in addition to incomplete take-up and illegitimate transfers, conditional programs require resources for screening and monitoring. Administrative or overhead costs can be as little as 1% of the total spent on transfers, as in the EITC, but they can also be sizable, reaching more than 6% of spending on SNAP, 10% on UI, and 12% on SSI transfers. We model these costs by allowing a

<sup>&</sup>lt;sup>1</sup>In the literature, a UBI may refer to any universal income, as in this paper, or only to a universal income large enough to cover basic expenses. It may be seen as a substitute for existing welfare programs, completely or partially, or merely as a complement. For more details, see Van Parijs and Vanderborght (2017), Calsamiglia and Flamand (2019), and Hoynes and Rothstein (2019).

 $<sup>^2</sup>$ We define take-up rate as the fraction of the eligible that receives the benefit. Claim rate, on the other hand, is the fraction of a group that, irrespective of eligibility, applies for a welfare benefit. See Section 4.2 for the sources of the estimates in this and the next two paragraphs.

proportion of what the government spends on conditional programs to benefit no one.<sup>3</sup>

A UBI, on the other hand, would be mostly free of those imperfections. Since it is a universal transfer, it is bound to achieve near complete take-up. <sup>4</sup> Illegitimate payments should also be several orders of magnitude smaller than in existing programs, mostly limited to duplicate payments or cases of identity theft. Finally, the trivial administrative costs of the EITC, a relatively complex tax credit, indicate that a UBI's administrative costs should be negligible. Still, a UBI would suffer from challenges of its own. Even though it promises to reach all those in the dead angle of conditional programs, it is a blunt instrument that does not discriminate rich from poor. Consequently, it would inefficiently transfer to those that value transfers relatively less. Its unconditionality would also make it useless for nudging behavior. Conditional and unconditional programs thus suffer from distinct, albeit significant, challenges. Under standard assumptions, in a stripped-down version of our full model, we show analytically that the three imperfections of conditional programs lower welfare. In fact, the eligible for conditional programs might be better off with a UBI even if the transfer they receive falls on average.

To improve the full model's fit to the US economy, enabling its use as a laboratory for policy experiments, it features consumers that are heterogeneous along five dimensions: accumulated assets, labor market state, benefit claimant status, fixed level of education, and stochastic human capital. Moreover, consumers are constrained by their success in matching with firms in a frictional labor market and by taxes and transfers set by the government.

In our first set of experiments, we quantify the welfare significance of the imperfections of conditional programs, i.e., of the benchmark welfare system, which resembles that of the US. We remove each imperfection separately and then all three together. We find that illegitimate payments have quantitatively negligible effects on welfare, while those of administrative costs are moderate. Incomplete take-up, on the other hand, is associated with a welfare loss of noteworthy magnitude vis-a-vis a perfect system. Its correction would be equivalent to a permanent increase of 1.9% in consumption, almost 9% for those with the lowest level of education. Those with less education tend to claim relief at a relatively low rate and are, simultaneously, poorly protected by their assets against fluctuations in income. They are therefore especially affected by the inability of conditional programs to reach all the eligible. Abstracting from the imperfections of conditional programs, especially incomplete take-up, risks considerably overestimating the welfare loss of introducing a UBI.

<sup>&</sup>lt;sup>3</sup>These three imperfections are not independent of each other. For instance, whilst the EITC has lower administrative or overhead costs than the SNAP or the SSI, a much greater proportion of the value of its transfers is illegitimate. In this paper, we are not concerned with perfecting the existing system or with the trade-offs involved in reforming it. For that, see Kleven and Kopczuk (2011) and Finkelstein and Notowidigdo (2019).

<sup>&</sup>lt;sup>4</sup>Being unconditional, a UBI could be passively received and, being universal, no stigma should be attached to receiving it. Hence, a UBI addresses two important causes of incomplete take-up: application costs and stigma (Moffitt, 1983).

We quantify this loss and investigate other consequences of replacing the benchmark welfare system with an expenditure-neutral UBI (worth approximately 1500 USD per year). We find that such a replacement would increase job search effort, capital accumulation, and, consequently, output. It would also raise wages and lower wealth inequality. Indeed, transfers in the benchmark depend on consumers' idiosyncratic states, such as wealth or labor market state, disincentivizing work and wealth accumulation, especially among the poorest. As a UBI is less distortionary, economic activity rises. Further, since an expenditure-neutral UBI spends the same but reaches more recipients, the amount going to the worse off falls. For precautionary reasons, they are incentivized to save more than in the benchmark, whilst the better off are incentivized to save less, contributing to the fall in wealth inequality. Still, despite promoting economic activity and curbing inequality, an expenditureneutral UBI would lower welfare by an average of 0.7% of consumption-equivalent units. Mostly, this is due to the poor and nonemployed becoming less well-insured. Yet, decomposing the welfare impact by level of education leads to the noteworthy conclusion that the least educated, who are disproportionately poor and nonemployed, are not those most negatively affected by a UBI. If, on average, transfers to these consumers fall the most with a UBI, eligible consumers that got no transfer in the benchmark system due to incomplete take-up now get relief from the UBI transfer, a relief that is especially valuable given their low income and assets.

Finally, given the calls for making the social safety net more generous, in another set of experiments, we investigate the performance of expenditure-neutral UBIs if they were to replace welfare systems of alternative scales. We find that if the welfare system is large enough (allowing for a UBI of approximately 2150 USD per year), replacing it with a UBI would increase aggregate welfare, especially for the least educated. Scaling up the benchmark welfare system amplifies its distortions to labor supply and asset accumulation, as well as the inequality between consumers that take up benefits and those that do not. A UBI increases welfare by alleviating distortions and reaching those in the dead angle of conditional programs.

We study two extensions of the benchmark model. The first is motivated by the observation that in welfare systems of greater generosity, the prospective advantages of claiming benefits, and therefore take-up rates, should be greater than in the benchmark. While in the benchmark model we assume fixed claim rates, in this extension we endogenize them by explicitly modeling claims as resulting from a cost-benefit analysis weighing the benefits of prospective transfers against the myriad costs that participation entails, including the time and hassle of the application process, stigma, privacy concerns, etc. (e.g., Moffitt, 1983; Finkelstein and Notowidigdo, 2019). This extension allows us to test the robustness of our result that a UBI performs better than conditional welfare systems larger enough than the benchmark. The key result stands: even accounting for growing incentives to claim,

a UBI of 2300 USD would perform better than an equivalent expansion of the benchmark welfare system. The second extension is motivated by noticing that flows into and out of the labor force depend on the incentive structure generated by conditional programs. In the benchmark model, only the flows from out of the labor force into employment are endogenous. In this extension, we endogenize all flows into and out of the labor force. We find that the benchmark welfare system is even more distortionary than the benchmark model indicates. Moreover, the welfare gains of replacing a conditional welfare system of sufficient generosity with a UBI are robust, as a UBI of 2000 USD would suffice to increase welfare relative to the expanded benchmark system.<sup>5</sup>

Our work contributes to the literature assessing the introduction of a UBI. Among the contributions furthering this goal are those studying existing programs that, like a UBI, offer universal cash transfers. Noteworthy examples are the Alaska Permanent Fund Dividend (Jones and Marinescu, 2022, Watson, Guettabi and Reimer, 2020, Kozminski and Baek, 2017, Berman, 2018), or the universal cash transfer implemented in Iran (Salehi-Isfahani and Mostafavi-Dehzooei, 2018). Other contributions result from the numerous trials and pilot projects across the world (e.g., Haushofer and Shapiro, 2016, Verho, Hämäläinen and Kanninen, 2022). Still, despite generating relevant evidence, enlightening decision-makers and offering proofs-of-concept, there are important questions that the study of existing programs or of pilots cannot illuminate (Hoynes and Rothstein, 2019). Existing programs typically differ from a UBI in crucial details. For instance, the Alaska Permanent Fund Dividend is not tax-funded. Pilots, in turn, usually have a clear and relatively short duration and, therefore, are not intended to create a long-term expectation that transfers will endure. Some are not redistributive but instead create net inflows from the outside. Finally, the number of beneficiaries and the magnitude of average and total transfers are too small to induce sizable general equilibrium effects.

An approach like ours is better suited to address the questions we pose. Our work is closest to contributions using general equilibrium models to study tax and transfer systems (such as Boar and Midrigan, 2022, Dyrda and Pedroni, 2023, Ferriere et al., 2023, Heathcote, Storesletten and Violante, 2017, or McKay and Reis, 2016), especially to those looking specifically at UBI. There is a growing number of these, displaying increased diversity in emphases and modeling choices. Daruich and Fernández (2024), Ferreira, Peruffo and Cordeiro Valério (2021), Guner, Kaygusuz and Ventura (2023), and Ludu-

<sup>&</sup>lt;sup>5</sup>We also show that our key results are robust to several alternative modeling and calibration choices.

<sup>&</sup>lt;sup>6</sup>Since 1982, the Alaska Permanent Fund has paid a yearly dividend, usually well above 1000 USD, to virtually every Alaska resident. As for Iran, in late 2010 it replaced several existing subsidies with a sizable, universal cash transfer worth more than a quarter of the median per capita household income. A smaller example is the dividend paid to all adult members of the Eastern Band of Cherokee Indians, distributing part of the profits from the operation of a casino inaugurated in 1997 (Akee et al., 2010, Akee et al., 2018). The number of beneficiaries is relatively small, in the hundreds, even though gross transfers have been as high as 6000 USD in a year.

<sup>&</sup>lt;sup>7</sup>An example is that implemented by the Finnish authorities. In 2017 and 2018, about 2000 unemployed persons in Finland saw their conditional unemployment insurance replaced by an unconditional monthly transfer worth 631 USD.

vice (2021), for instance, are especially concerned with modeling family structure and family-level decision making. Like us, Fabre, Pallage and Zimmermann (2014), Jaimovich et al. (2022), and Rauh and Santos (2022) instead put a greater emphasis on the role of labor market frictions. In their turn, Conesa, Li and Li (2023) and Mukbaniani (2021) emphasize the hierarchical importance of different types of needs and the role of a UBI in covering basic consumption necessities.

We make two major contributions to this literature. First, and most importantly, we are the first to explicitly model incomplete take-up and illegitimate transfers. Abstracting from these imperfections, the literature generally concludes that introducing a UBI decreases welfare, even if its size is much greater than that of existing programs. We show, however, that those imperfections have welfare consequences of noteworthy magnitude and would favor UBI under standard assumptions. Consequently, the estimates of the welfare loss of introducing a UBI to replace a perfect welfare system offer only an upper bound to the welfare loss of replacing the extant, imperfect, system. Moreover, accounting for imperfections leads to more nuanced results than those in the literature. In particular, the impact on welfare is neither universal, as the most educated would benefit from a UBI in our benchmark, nor robust, as the welfare impact of introducing an expenditure-neutral UBI hinges on the generosity of the system.

Second, we model flows across three labor market states: employed, unemployed, and out of the labor force (OLF). To the best of our knowledge, no other paper assessing the tax and transfer system does this. Rauh and Santos (2022), for example, abstract from the OLF, while Jaimovich et al. (2022) allow newborn consumers to remain OLF, but no subsequent transitions into the labor market. By incorporating flows across all three states, we account for the risks of losing a job and leaving the labor force. We also account for the impact of transfers differentiated by labor market state, a common feature in real-life programs. Finally, if a labor market state were left out, the universal transfer in the model would be implicitly conditional to belonging to the modeled states.

<sup>&</sup>lt;sup>8</sup>A few papers address incomplete take-up by adjusting the calibration. For example, Heathcote, Storesletten and Violante (2017) and Rauh and Santos (2022) calibrate their tax and transfer functions accounting for incomplete take-up, but do not model it. They thus implicitly assume that all eligible individuals get the same transfer as the average recipient with similar characteristics, as opposed to there being eligible individuals that get nothing. Within the UBI literature, there are two papers that do model imperfections, including administrative costs. Fabre, Pallage and Zimmermann (2014) contrast a UBI with unemployment insurance that suffers from moral hazard problems and incurs in administrative costs. They find that the optimal unemployment insurance (UI) is preferred to the optimal UBI because UBI is a blunt instrument. Yet, in modeling unemployment insurance, they assume that all the unemployed receive UI if unemployed for no fault of their own. In a robustness check, Daruich and Fernández (2024) calculate the magnitude of administrative costs necessary to reverse their benchmark results and conclude that it is implausibly high. As for the literature on the effects of UI in a macroeconomic setting, take-up is modeled by Birinci and See (2023) and Kekre (2023). Kekre proposes a parsimonious approach as in our benchmark, while Birinci and See offer a model with endogenous take-up, similar to that in our extension. Neither studies the welfare consequences of incomplete take-up.

<sup>&</sup>lt;sup>9</sup>Our paper, therefore, relates to contributions outside the tax and transfer literature, such as Cairó, Fujita and Morales-Jiménez (2022), or Krusell et al. (2017; 2020), who also build models accounting for flows across the three labor market states.

In Section 2, we examine a simple endowment economy, a stripped-down version of the full model, which evinces the welfare consequences of the imperfections of conditional programs. We then lay out our full model in Section 3 and describe and explain our calibration strategy in Section 4. We present our experiments and measure the welfare costs associated with the imperfections of the benchmark welfare system in Section 5 and the impact of replacing it with a UBI in Section 6. Section 7 shows that our findings are robust in two extensions of the full model. We conclude in Section 8.

# 2 A Simple Endowment Model

#### 2.1 Environment

Consider an endowment economy whose consumers have the same preferences, measured by a utility function  $u(\cdot)$ , but differ in their exogenously fixed endowment  $y \in \{y_L, y_H\}$ ,  $y_H > y_L$ . To alleviate this inequality, a government runs a conditional welfare program transferring from those with endowment  $y_H$  to the rest. This conditional program suffers from three imperfections. First, take-up is incomplete: all consumers with  $y_L$  are eligible, but only a fraction  $0 < \psi < 1$ , the exogenously fixed take-up rate, does receive a transfer. Second, not all transfers are legitimate: some end up going to those with endowment  $y_H$ . Third, there are administrative costs: screening claimants and monitoring recipients divert a fraction  $t \ge 0$  of the amount collected from those with  $y_H$ .

# 2.2 The Costly Imperfections of Conditional Programs

Let  $T_L(T_H)$  denote the average transfer to those with low (high) endowment. Each low-endowment recipient gets  $T_L/\psi$ . The welfare burden of incomplete take-up may be measured by:

$$\Xi \equiv u(y_L + T_L) - \left[ \psi u \left( y_L + T_L / \psi \right) + (1 - \psi) u(y_L) \right]. \tag{1}$$

**Proposition 1** Let  $u(\cdot)$  be a strictly increasing, strictly concave, continuously differentiable function with a strictly convex first-order derivative,  $0 < \psi < 1$ ,  $y_L > 0$ , and  $T_L > 0$ . Then:

 $i) \Xi > 0$ 

ii)  $\Xi$  decreases with  $\psi$ 

iii)  $\Xi$  increases with  $T_L$ 

*iv)*  $\Xi$  *decreases with*  $y_L$ 

**Proof** See Appendix A.1.

Proposition 1 shows that, under standard assumptions, the welfare outcome of a conditional welfare program is worse when take-up is incomplete. This is true among the eligible and, consequently, in the aggregate. The welfare loss is greater, the lower the take-up rate, as the consumption inequality among low-endowment consumers increases. Furthermore, more generous programs, i.e., with greater  $T_L$ , have, in this setting, better welfare outcomes among the eligible. They are also better in the aggregate as long as  $y_L + T_L/\psi$  is less than the endowment of high-endowment consumers net of taxes and transfers, a further assumption we make throughout this section. Proposition 1, however, shows that the welfare burden due to incomplete take-up grows with the generosity of the program, as a higher  $T_L$ , for a given  $\psi$ , increases the consumption inequality among low-endowment consumers. As for  $y_L$ , it lessens the satisfaction that any given transfer brings to its recipients. Consequently, if it is higher, less is lost by those the program does not reach.

Turning to illegitimate transfers, the more trickles up to the high-endowment consumers,  $T_H$ , the lower the  $T_L$ , which diminishes the welfare effects of the conditional program. Finally, the more is diverted to the wasteful running of the conditional program,  $\iota$ , the less actually reaches recipients.

#### 2.3 UBI vs. Imperfect Conditional Programs

A UBI promises to reach those in the dead-angle of conditional programs at a negligible administrative cost. Yet, it is a blunt instrument that does not discriminate high-endowment from low. Consequently, barring implausibly high administrative costs, those with a low endowment would receive a lower average transfer with an expenditure-neutral UBI. This, however, need not imply that they would become, on average, worse off.

To see this, let  $\xi$  measure by how much average transfers could be reduced without welfare loss if take-up were complete, i.e., to be such that:

$$u(y_L + (1 - \xi)T_L) = \psi u(y_L + T_L/\psi) + (1 - \psi)u(y_L). \tag{2}$$

**Proposition 2** *Under the assumptions of Prop. 1:* 

 $i) \Xi > 0 iff \xi > 0$ 

*ii*)  $0 < \xi < 1$ 

iii)  $\xi$  decreases with  $\psi$ 

iv)  $\xi$ .  $T_L$  increases with  $T_L$ . If the utility function displays constant absolute or relative risk aversion, then  $\xi$  increases with  $T_L$ 

v) If the utility function displays constant absolute risk aversion, then  $\xi$  does not vary with  $y_L$ . If it displays constant relative risk aversion, then  $\xi$  falls with  $y_L$ 

## **Proof** See Appendix A.2.

 $\xi$  is a strictly positive magnitude. Consequently, if the introduction of an expenditure-neutral UBI lowers average transfers to low-endowment consumers by less than  $\xi$ , i.e., if  $UBI > (1 - \xi)T_L$ , then these consumers would benefit, on average, from the unconditional program. In this case, the welfare gains of the eligible, but formerly non-recipient, consumers would more than compensate the welfare loss of the eligible, and formerly recipient, consumers resulting from the reduction in the average value of transfers.

Proposition 2 establishes that a UBI's welfare performance, relative to the existing program, is better when take-up is low, when the size of the existing welfare program is greater, and when those in the dead-angle of conditional programs have less.

The performance of a UBI also rises with  $T_H$  and  $\iota$ . A higher  $T_H$  means that the conditional program, like the UBI, also transfers to those that do not need, while saving on administrative costs associated with conditionality allows a higher average transfer.

In the literature, the imperfections of conditional welfare programs are mostly neglected. Under the assumption of a perfect welfare system ( $\psi=1$ ,  $T_H=0$ ,  $\iota=0$ ), an expenditure-neutral UBI stands little chance of increasing the welfare of low-endowment consumers. To see this, notice that, in a perfect system,  $UBI < T_L + T_H = T_L$ , as the UBI also reaches high-endowment consumers. Consequently  $u(y_L + UBI) < u(y_L + T_L)$ . Only if the introduction of a UBI were associated with a substantial increase in  $y_L$  would low-endowment consumers benefit. A rise in  $y_L$  is expected insofar as conditional welfare programs tend to be more distortionary. Yet, the extant literature and the results of the full model show that the order of magnitude of such distortions is too low.

The findings in this section hinge on assumptions ubiquitous in macroeconomic models. <sup>10</sup> They are relevant to all models that shed light on the advantages and disadvantages of a UBI relative to extant conditional welfare programs. They highlight that whether an expenditure-neutral UBI increases welfare depends on how programs function in practice, warts and all. Hence, since existing estimates of the welfare losses of a UBI abstract from the imperfections of extant programs, they offer upper bounds for that loss. In the next section, we develop a much richer model of an economy as a laboratory to quantify the welfare and macroeconomic effects of an expenditure-neutral UBI. A key message from this richer model is that the results in this section are quantitatively relevant: neglect-

<sup>&</sup>lt;sup>10</sup>Assumed, for example, by any model with constant relative risk aversion or exponential utility.

ing the imperfections of the welfare system implies a sizable overestimation of the welfare losses of a UBI. In fact, an expenditure-neutral UBI can increase welfare.

#### 3 Model

We build an artificial economy in continuous time with incomplete markets and without aggregate uncertainty (such as Aiyagari, 1994; Bewley, 1986; Huggett, 1993). As in the economy of Krusell, Mukoyama and Şahin (2010), heterogeneous consumers meet and bargain with firms in a labor market characterized by matching frictions. The government collects taxes on consumption and on capital and labor incomes to finance spending and transfers. We study the economy's stationary general equilibrium.

#### 3.1 Consumers

The economy is populated by a measure one continuum of infinitely-lived, risk-averse, dynastic consumers perpetually in working age. <sup>11</sup> They are heterogeneous along five dimensions: accumulated assets, a; labor market state, n; benefit claimant status, b; exogenously-given fixed level of education, z; and stochastic human capital resembling work experience,  $\zeta$ .

# 3.1.1 Objective Function

Consumers choose consumption,  $c_t$ , and, if nonemployed, job search effort,  $s_t$ , to maximize lifetime utility:

$$\mathbb{E}_0 \int_0^\infty e^{-\rho_z t} u(c_t, s_t) \mathrm{d}t,\tag{3}$$

where  $\mathbb{E}$  is the expectation operator, t denotes time,  $u(\cdot)$  is instantaneous utility (such that  $u_c(\cdot) > 0$ ,  $u_{cc}(\cdot) < 0$ ,  $u_s(\cdot) < 0$ ,  $u_s(\cdot) < 0$ , and  $\rho_z$  is a discount rate dependent on consumers' level of education.<sup>12</sup>

<sup>&</sup>lt;sup>11</sup>As discussed by Hubmer, Krusell and Smith. (2021), the choice of dynastic consumers implicitly defines a bequest function. As there are no clear microeconomic estimates of such functions, our assumption conveniently introduces the bequest motive, which is typically disregarded in other papers studying the effects of a UBI.

<sup>&</sup>lt;sup>12</sup>This assumption allows us to better capture the wealth differences among workers of different levels of education. Other papers in the literature also allow for heterogeneous discount rates: e.g., Krusell and Smith (1998), Krueger, Mitman and Perri (2016), Hubmer, Krusell and Smith. (2021), and Rauh and Santos (2022). See also Falk et al. (2018) for experimental evidence.

#### 3.1.2 Budget Constraint and Asset Holdings

A consumer's choices are constrained by a budget:

$$\dot{a}_t = \bar{w}_t(a, n, b, z, \zeta) + T_t(a, n, b, z, \zeta) + (1 - \tau_a)(r_t - \delta)a_t - (1 + \tau_c)c_t, \tag{4}$$

where  $r_t$  and  $\delta$  refer to the gross return and depreciation rate of capital,  $\tau_a$  is the capital income tax, and  $\tau_c$  is the consumption tax.  $\bar{w}_t$  is net labor income, which refers to after-tax wages in the case of employed consumers or, in that of the nonemployed, to home production in the amount  $h(z,\zeta)$  (as in Boerma and Karabarbounis, 2021). The are transfers received. Taxation and transfers are discussed in Section 3.2.

The assets accumulated by a consumer, a, are claims on the total assets in the economy. These, as in Krusell, Mukoyama and Şahin (2010), are composed of aggregate capital, K, and the value of firms,  $\Omega$ , both with an equal equilibrium return of  $r - \delta$ , due to arbitrage. Asset holdings observe a lower-bound, or borrowing limit, dependent on the level of education:

$$a_t \ge a_z.$$
 (5)

#### 3.1.3 Labor Market State

The labor market is segmented by level of education and stochastic human capital  $(z,\zeta)$ . In each segment, consumers can be employed (e), unemployed (u), or out of the labor force (OLF, o). The indicator function  $n^x$ ,  $x \in \{e, u, o\}$ , denotes labor market state.

Job-search effort affects the likelihood of finding a job. Its intensity is given by  $s(a, n^x, b, z, \zeta) f(z, \zeta)$ .  $s(a, n^x, b, z, \zeta)$  denotes the search effort of the unemployed (x = u) or the OLF (x = o), while  $f(z, \zeta)$  is the job-finding rate per unit of search effort in the segment (endogenized in Section 3.4.1). Since OLF consumers do, in fact, find jobs without actively looking, we distinguish them from unemployed consumers by assuming that they search passively if moving to employment would increase lifetime utility. Hence,  $s(a, n^o, b, z, \zeta) \in \{s_o^z, 0\}$ , where  $s_o^z > 0$  measures passive search effort and depends on the level of education z.

Finally, we assume that a constant exogenous fraction,  $m_{eu}^z$ , of employed consumers with level of education z become unemployed. Similarly, there are exogenous flows from employment and un-

<sup>&</sup>lt;sup>13</sup>Home production is a perfect substitute for the market good. It is included because the evidence in Boerma and Karabarbounis suggests that it significantly affects inequality.

<sup>&</sup>lt;sup>14</sup>Consumers are not allowed to own equity of an individual firm. Also, assuming that arbitrage holds frees us from tracking portfolio compositions.

employment to out of the labor from and from out of the labor force to unemployment. We denote their intensities by  $m_{eo}^z$ ,  $m_{uo}^z$ , and  $m_{ou}^z$ , all varying with z.

#### 3.1.4 Stochastic Human Capital

Consumers are further constrained by the stochastic processes for human capital. As in the literature (Ljungqvist and Sargent, 1998; Kehoe, Midrigan and Pastorino, 2019), they tend to accumulate human capital when employed and lose it when nonemployed. To capture this, we use bounded Ornstein-Uhlenbeck processes for stochastic human capital,  $\zeta$ :

$$d\zeta = \theta_{\zeta}(\zeta_e - \zeta(t))dt + \sigma_{\zeta}dW(t), \tag{6}$$

$$d\zeta = \theta_{\zeta}(\zeta_o - \zeta(t))dt + \sigma_{\zeta}dW(t), \tag{7}$$

where Eq. (6) applies to employed consumers and Eq. (7) to the nonemployed. These stochastic processes observe exogenously-imposed upper and lower bounds,  $\bar{\zeta}$  and  $\underline{\zeta}$ .  $\theta_{\zeta}$  is the rate of mean reversion,  $\sigma_{\zeta}$  denotes volatility, and  $\mathbb{W}(t)$  is a standard Brownian motion.  $\zeta_e$  and  $\zeta_o < \zeta_e$  are the long-term means of the respective (unbounded) process.

#### 3.2 Government

Consumers' budgets depend on taxes and transfers set by the government. These are detailed in this section.

#### 3.2.1 Revenues

The government obtains revenues by collecting flat taxes on consumption and capital income, and progressive taxes on labor income. In particular, we follow Benabou (2002) and Heathcote, Storesletten and Violante (2017) and assume that labor income taxes are

$$w(a,b,z,\zeta)-(1-\tau_n)w(a,b,z,\zeta)^{1-\lambda_n},$$

which implies that net labor income for employed consumers is

$$\bar{w}(a, n^e, b, z, \zeta) \equiv (1 - \tau_n) w(a, b, z, \zeta)^{1 - \lambda_n}, \tag{8}$$

where  $\lambda_n$  governs the degree of progressivity, while  $\tau_n$  governs the level. Home production ( $\bar{w}(a,n^u,b,z,\zeta)=\bar{w}(a,n^o,b,z,\zeta)=h(z,\zeta)$ ) is not taxed.

<sup>&</sup>lt;sup>15</sup>If tax rates are flat  $(\lambda_n = 0)$ , then  $\tau_n$  is the labor income tax rate.

#### 3.2.2 Expenses

These revenues are spent on unproductive government spending, *G*, and on transfers and ancillary administrative costs.

There are four conditional programs in the model, mimicking, in a stylized way, various real-world counterparts. First, there are employed benefits subsidizing the labor supply of consumers whose labor income is not too high. Second, there is standard unemployment insurance (UI) for consumers that become unemployed after a long enough period of employment and that have not received UI for too long. Third, there are other unemployed benefits for the unemployed poor who do not receive UI. Finally, there are OLF benefits directed at poor OLF consumers. We use  $b_l^j$  as an indicator function denoting benefit-claiming status, where the superscript  $j \in \{e, ui, u, o, \emptyset\}$  corresponds to employed benefits, e, unemployment insurance, e, other unemployed benefits, e, out of the labor force benefits, e, and no benefits, e; the subscript e0 only applies to employed benefits to denote eligibility for UI. We denote the corresponding value of transfers by e1.

Real-life conditional benefit programs are characterized by incomplete, and sometimes very low, take-up: only a fraction of the eligible do receive a transfer. We model incomplete take-up in a parsimonious way, abstracting from its causes. Regarding employment, other unemployment, and OLF benefits, we assume that claims follow a random process. Only a proportion  $\psi_x^z$  of those that move to any labor market state  $x \in \{e, u, o\}$  or lose eligibility for UI claim the respective benefits. The claim rate is then  $\psi_x^z$ , dependent on the level of education. Besides claiming, to receive benefits consumers must also fulfill categorical or means-testing conditions on income or wealth. For instance, those entitled to unemployment insurance are not entitled to other unemployed benefits.

The take-up rate of each type of benefit is then given by the proportion of those that are eligible and that do receive it. Insofar as the claim rate is less than one ( $\psi_x^z < 1$ ), then so is the take-up rate. These two rates are, however, different: claimants have the incentive to behave in a way that grants them eligibility, e.g., by choosing not to search for jobs or by not accumulating assets.

Regarding UI, employed consumers with level of education z become eligible at rate  $p_{ui}^{e,z}$ , capturing incomplete take-up and that eligibility requires a sufficiently long period of employment as well as

<sup>&</sup>lt;sup>16</sup>In modeling UI, the literature typically abstracts from the time it takes to gain and lose eligibility, instead assuming that all the unemployed receive UI. McKay and Reis (2016) and Rauh and Santos (2022) are noteworthy exceptions. In their contributions, UI expires after a sufficiently long unemployment spell. We go further and also account for the fact that eligibility is not gained immediately once an employment spell begins.

<sup>&</sup>lt;sup>17</sup>In Section 7.1, we offer a version of our model with endogenous take-up. We choose the parsimonious model as our benchmark because our goal is not to explain incomplete take-up, but to understand its macroeconomic and welfare implications in the benchmark system. In modeling take-up, Moffitt (1983) is seminal. More recent examples include Kleven and Kopczuk (2011) and Finkelstein and Notowidigdo (2019). Unlike ours, these contributions do not seek to elucidate the macroeconomic effects of incomplete take-up.

the satisfaction of an earnings test. If eligible consumers become unemployed, they always claim, and get, UI transfers. Consumers receiving these transfers lose eligibility at rate  $p_{ui}^u$ , which only depends on the duration of unemployment.

Besides incomplete take-up, real-life programs suffer from two additional imperfections: illegitimate transfers and administrative costs. Illegitimate transfers include over-payments to eligible consumers and payments to ineligible consumers. We model this phenomenon by assuming that all claimants receive some payment, however small, that they are not entitled to. As for administrative costs, they are simply modeled as a fraction,  $\iota_j$  where  $j \in \{e, ui, u, o\}$ , of the total value of transfers in the program.

Finally, in addition to the four conditional benefits, the model includes an unconditional transfer directed at all consumers, a universal basic income, *UBI*. All consumers receive the same UBI transfer, i.e., there is complete take-up. We also assume that there are no illegitimate transfers or administrative costs.

The transfers a consumer receives are, then, given by  $T(a, n, b_l^j, z, \zeta) = UBI + B(a, n, b_l^j, z, \zeta)$ .

# 3.2.3 The Balanced Budget

The government runs a balanced budget:

$$\sum_{z} \sum_{b} \int_{\zeta}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} \left[ w(a,b,z,\zeta) - (1-\tau_{n}) w(a,b,z,\zeta)^{1-\lambda_{n}} \right] g(a,n^{e},b,z,\zeta) dad\zeta$$

$$+ \tau_{c} \sum_{z} \sum_{b} \sum_{n} \int_{\underline{\zeta}}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} \left[ c(a,n,b,z,\zeta) - h(n,z,\zeta) \right] g(a,n,b,z,\zeta) dad\zeta + \tau_{a}(r-\delta)(K+\Omega) =$$

$$(1+\iota_{e}) \left( \bar{B}_{e,ui}^{e} + \bar{B}_{e,\varnothing}^{e} \right) + (1+\iota_{ui}) \bar{B}_{ui}^{u} + (1+\iota_{u}) \bar{B}_{u}^{u} + (1+\iota_{o}) \bar{B}_{o}^{o} + UBI + G,$$

$$(9)$$

where  $g(\cdot)$  is the density function of the consumers' distribution detailed in Section 3.6.1, and  $\bar{B}^x_{j,l} \equiv \sum_z \int_a^\infty B(a,n^x,b^j_l,z,\zeta)g(a,n^x,b^j_l,\zeta,t)\mathrm{d}a$  are transfers to consumers in labor market state  $n^x$  and benefit status  $b^j_l$ . The left-hand side of Eq. (9) sums government revenues from labor income, consumption, and capital income taxes. Since home production is consumed but not taxed, we subtract it from consumption. The right-hand side of Eq. (9) sums government transfers and related administrative costs, as well as unproductive government expenditures. Transfers include employed benefits, which depend on wages and thus on whether consumers are eligible for UI. Transfers also include those related to UI, other unemployed benefits, OLF benefits, and UBI.

#### 3.3 Firms

Consumers rely on firms for employment and production. There are two types of firms in the model. Intermediate producers, or labor firms, hire consumers to produce labor services. These are, in turn, sold to final-good producers to produce the final good that is consumed or invested.

#### 3.3.1 Labor Firms

Labor firms open vacancies in a segment of the labor market of their choice, and a free-entry condition is satisfied in each segment. Each labor firm employs at most one consumer. When vacant, it pays the flow cost  $\kappa_z$ , which varies with the level of education of the consumers in the segment. When matched with a consumer characterized by level of education z and stochastic human capital  $\zeta$ , the firm produces  $y_z e^{\zeta}$  units of labor services, where  $y_z$  is a productivity factor varying with education. It also pays a wage,  $w(a, b, z, \zeta)$ , that is bargained as described in Section 3.4.2 and depends on the consumer's idiosyncratic state.

Labor services are sold to final-good producers at the competitive price  $p_L$ . Labor firms are homogeneous, but their profits depend on the consumer (worker) they are matched with, since this affects both production and wages. Consequently, the labor firm's value, J, depends on the state  $(a, b, z, \zeta)$  of the consumer. Labor firms discount future profits at rate  $r - \delta$ , and are worthless in equilibrium if the match breaks.

For illustration, we present the case of a firm employing a consumer receiving employed benefits but not yet eligible for unemployment insurance. In this case, the value of the firm is given by the following Hamilton-Jacobi-Bellman (HJB) equation:

$$(r-\delta+m_{eu}^z+m_{eo}^z)J(a,b_{\varnothing}^e,z,\zeta)=y_ze^{\zeta}p_L-w(a,b_{\varnothing}^e,z,\zeta)+\partial_aJ(a,b_{\varnothing}^e,z,\zeta)\dot{a}(a,n^e,b_{\varnothing}^e,z,\zeta)\\ +\theta_{\zeta}(\zeta_e-\zeta)\partial_{\zeta}J(a,b_{\varnothing}^e,z,\zeta)+\frac{\sigma_{\zeta}^2}{2}\partial_{\zeta\zeta}^2J(a,b_{\varnothing}^e,z,\zeta)+p_{ui}^{e,z}\left[J(a,b_{ui}^e,z,\zeta)-J(a,b_{\varnothing}^e,z,\zeta)\right]. \tag{10}$$

The left-hand side accounts for the possibility that the match breaks up if the consumer becomes unemployed ( $m_{eu}^z$ ) or OLF ( $m_{eo}^z$ ). On the right-hand side, the first two terms correspond to flow profit, while the third term accounts for the impact that a change in the consumer's asset holdings would have on the bargaining solution and, consequently, on the value of the firm. The subsequent two terms account for changes in human capital, while the last term accounts for changes in benefit status, as eligibility for unemployment insurance tends to increase wages. This last term differentiates the HJB of a labor firm employing a consumer ineligible for unemployment insurance from that of the others (see Appendix B.2 for all possible HJB equations giving labor firm values).

#### 3.3.2 Final-good Producers

Final-good producers rent capital, K, from consumers and buy labor services, L, from labor firms to produce the final good, Y. Their production function is Y = AF(K, L), where A is total-factor productivity. We assume perfect competition, which implies that:

$$r = AF_K$$

$$p_L = AF_L$$
.

where  $F_K$  and  $F_L$  are the marginal products of K and L.

#### 3.4 Labor Market

Consumers and labor firms meet in a frictional labor market segmented by level of education and stochastic human capital,  $(z,\zeta)$ .

#### 3.4.1 Matching Function

Within each segment, a standard Cobb-Douglas matching function,  $M(U,v) \equiv \chi_z v(z,\zeta)^{1-\eta} U(z,\zeta)^\eta$ , determines the number of matches as a function of total job search effort, U, and vacancies, v, in the segment. Here,  $\eta$  is the elasticity of the matching function with respect to U, while  $\chi_z$  is the matching efficiency, which depends on z. Hence, the vacancy-filling rate is  $q(z,\zeta) \equiv \chi_z \theta(z,\zeta)^{-\eta}$  and the job-finding rate of a unit of search effort is  $f(z,\zeta) \equiv \chi_z \theta(z,\zeta)^{1-\eta}$ , where  $\theta(z,\zeta) \equiv \frac{v(z,\zeta)}{U(z,\zeta)}$  measures labor market tightness as the ratio of vacancies to total search effort in the segment. Total search effort is  $U(z,\zeta) \equiv \sum_{n \in \{n^u,n^o\}} \sum_b \int_a^\infty s(a,n,b,z,\zeta) g(a,n,b,z,\zeta) da$ .

#### 3.4.2 Wage Bargaining

Matched consumers and labor firms bargain over wages according to Kalai's (1977) bargaining, i.e., until

$$(1-\phi)\Big[W(a,n^e,b,z,\zeta)-\tilde{W}(a,n^u,b,z,\zeta)\Big]=\phi J(a,b,z,\zeta),$$

where  $\phi$  represents consumers' bargaining power, the share of the total surplus of the match accruing to them. This equation also solves the Nash bargaining problem under risk neutrality, which is common in the literature.  $W(a,n,b,z,\zeta)$  stands for the lifetime utility of a consumer in state  $(a,n,b,z,\zeta)$ , while  $\tilde{W}(a,n^u,b,z,\zeta)$  stands for the consumers' outside option. The latter is either  $W(a,n^u,b^{ui},z,\zeta)$  for consumers entitled to unemployment insurance, since they always claim it, or  $\psi_u W(a,n^u,b^u,z,\zeta)$ +

 $(1-\psi_u)W(a,n^u,b^\varnothing,z,\zeta)$  for the others, as only a fraction  $\psi_u$  claim other unemployed benefits. <sup>18</sup> The closed-form wage equations are found in Appendix B.3.

#### 3.5 Consumers' Problem

The consumer's maximization problem can be summarized by HJB equations corresponding to each of the nine labor-benefit states. As presented above, these states are the combination of  $n^x$  and  $b_l^j$  where  $x \in \{e, u, o\}$ ,  $j \in \{e, ui, u, o, \varnothing\}$ , and  $l \in \{ui, \varnothing\}$ , the latter only relevant to the employed (x = e). When convenient, we use  $X_{j,l}^x$  as shorthand for any function X depending on the entire vector of idiosyncratic states,  $(a, n^x, b_l^j, z, \zeta)$ .

We illustrate the consumers' maximization problem with the case of an unemployed consumer receiving unemployment insurance and leave the other cases to Appendix B.1. The HJB of this consumer is

$$\begin{split} \rho_{z}W_{ui}^{u} &= \max_{c,s} \left\{ u(c,s) + \partial_{a}W_{ui}^{u} \left[ h(z,\zeta) + B_{ui}^{u} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c \right] \right. \\ &+ sf(z,\zeta) \left[ \psi_{e}^{z}W_{e,ui}^{e} + (1-\psi_{e}^{z})W_{\varnothing,ui}^{e} - W_{ui}^{u} \right] + p_{ui}^{u} \left[ \psi_{u}^{z}W_{u}^{u} + (1-\psi_{u}^{z})W_{\varnothing}^{u} - W_{ui}^{u} \right] \\ &+ m_{uo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1-\psi_{o}^{z})W_{\varnothing}^{o} - W_{ui}^{u} \right] + \theta_{\zeta}(\zeta_{o} - \zeta)\partial_{\zeta}W_{ui}^{u} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{ui}^{u} \right\}. \end{split}$$

$$(11)$$

The HJB shows that the flow value depends on instantaneous utility, changes in asset holdings, the possibility of finding jobs, the risk of losing UI eligibility, the risk of moving out of the labor force, and the risk of changes in stochastic human capital. In the cases of changes in labor market state and loss of UI eligibility, there is the additional risk of benefit claiming. In light of all these risks, the consumption-saving decision is determined by the First-Order condition (FOC) with respect to c:

$$u_c(c_{i,l}^x, s_{i,l}^x) = \partial_a W_{i,l}^x, \tag{12}$$

which is the same for all consumer types. This equation implies that the marginal value of consumption must be as high as the marginal value of saving. Moving to the job search effort decision, the FOC is:

$$u_s(c_{ui}^u, s_{ui}^u) = f(z, \zeta) \left[ \psi_e^z W_{e, ui}^e + (1 - \psi_e^z) W_{\varnothing, ui}^e - W_{ui}^u \right]. \tag{13}$$

This equation implies that the marginal disutility of searching must equal the marginal expected gain of searching. It takes a similar form for unemployed consumers who do not receive UI. OLF

<sup>&</sup>lt;sup>18</sup>The latter outside option also applies to consumers that find jobs when out of the labour force to avoid unnecessarily complicating the model.

consumers, however, as referred above, do not choose the intensive margin of job search effort: their job search effort is positive (and fixed) if  $\psi_e^z W_{e,\varnothing}^e + (1-\psi_e^z) W_{\varnothing,\varnothing}^e > W_j^o$  for  $j \in \{o,\varnothing\}$ . *Ceteris paribus*, OLF consumers that receive benefits tend to enjoy higher lifetime utility than those not receiving them  $(W_o^o > W_\varnothing^o)$ . This, in turn, lowers incentives to passively search for jobs, increasing the chances they remain OLF.

#### 3.6 Stationary Equilibrium

#### 3.6.1 Kolmogorov Forward Equations

The Kolmogorov Forward (Fokker-Planck) equations describe the evolution of the joint density function  $g_{j,l}^x \equiv g(a, n^x, b_l^j, z, \zeta)$ . Like the consumers' HJB, it is also a system of nine equations, detailed in Appendix B.4. The Kolmogorov Forward equations in the state  $(n^u, b^{ui})$ , for instance, is:

$$\begin{split} \partial_{t}g_{ui}^{u} &= -\partial_{a}\left[\dot{a}_{ui}^{u}g_{ui}^{u}\right] - \left[s_{ui}^{u}f(z,\zeta) + p_{ui}^{u} + m_{uo}^{z}\right]g_{ui}^{u} \\ &+ m_{eu}^{z}\left(g_{e,ui}^{e} + g_{\varnothing,ui}^{e}\right) - \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{ui}^{u}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{ui}^{u}\right], \end{split} \tag{14}$$

This equation highlights movements along the asset dimension, labor market state, benefit status, and stochastic human capital. The density function aligns with the population size normalization,  $\sum_{z}\sum_{n}\sum_{b}\int_{\zeta}^{\bar{\zeta}}\int_{a}^{\infty}g(a,n,b,z,\zeta)\mathrm{d}a\mathrm{d}\zeta=1.$  In the stationary equilibrium, it satisfies  $\partial_{t}g(\cdot)=0$  for all  $(a,n,b,z,\zeta)$ .

#### 3.6.2 Market Clearing

The asset market clears continuously in the model because the sum of all the assets owned by consumers equals the sum of aggregate capital, K, and the value of firms,  $\Omega$ :

$$\sum_{z} \sum_{b} \sum_{n} \int_{\zeta}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} a g(a, n, b, z, \zeta) da d\zeta = K + \Omega.$$
 (15)

As only labor firms obtain profits in equilibrium, their value is

$$\Omega \equiv \sum_{z} \sum_{h} \int_{\zeta}^{\bar{\zeta}} \int_{a}^{\infty} J(a, b, z, \zeta) g(a, n^{e}, b, z, \zeta) da d\zeta, \tag{16}$$

where we use the fact that the density of labor firms equals that of employed consumers, as each firm employs a single consumer.<sup>19</sup>

Each segment of the labor market converges to equilibrium as labor firms open vacancies until the

<sup>&</sup>lt;sup>19</sup>In equilibrium,  $\Omega$  also equals  $\frac{d}{r-\delta}$ , where dividends, d, equal the difference between the sum of profits and the sum of hiring costs,  $\sum_z \sum_b \int_{\zeta}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} (y_z e^{\zeta} p_L - w(a,b,z,\zeta)) g(a,n^e,b,z,\zeta) \mathrm{d}a \mathrm{d}\zeta - \sum_z \int_{\underline{\zeta}}^{\bar{\zeta}} \kappa_z \nu(z,\zeta) \mathrm{d}\zeta$ .

free-entry condition is satisfied:

$$\kappa_{z} = \frac{q(z,\zeta)}{U(z,\zeta)} \sum_{j \in \{e,\varnothing\}} \psi_{j}^{z} \int_{\underline{a}}^{\infty} \left[ J(a,b_{ui}^{j},z,\zeta) s_{ui}^{u} g_{ui}^{u} + J(a,b_{\varnothing}^{j},z,\zeta) \left( s_{u}^{u} g_{u}^{u} + s_{\varnothing}^{u} g_{\varnothing}^{u} + s_{o}^{o} g_{o}^{o} + s_{o}^{o} g_{\varnothing}^{o} \right) \right] da, \quad (17)$$

where  $\psi_j^z = \psi_e^z$  if j = e and  $\psi_j^z = 1 - \psi_e^z$  if  $j = \varnothing$ . This equation posits that the flow cost of an open vacancy,  $\kappa_z$ , equals the expected flow value. The latter, in turn, depends on the vacancy-filling rate and the expected value of a filled vacancy. This expectation relies on the density function g and on the variation in search intensity among consumers. Furthermore, this expectation accounts for the changing value of the matched firm across consumers' idiosyncratic states.

Finally, the market for labor services also clears:

$$L = \sum_{z} \sum_{h} \int_{\zeta}^{\bar{\zeta}} \int_{a}^{\infty} y_{z} e^{\zeta} g(a, n^{e}, b, z, \zeta) da d\zeta.$$
 (18)

The formal definition of the stationary equilibrium is in Appendix B.5.

# 4 Calibration

To calibrate the model, we looked at monthly US data for the population aged 25-64. We used data from the *Current Population Survey* (CPS), *Survey of Income and Program Participation* (SIPP), and others, as well as information from reports by accredited bodies and other papers. All values are in 2018 dollars. The calibrated model performs well in internal and external validation exercises.

#### 4.1 Consumers and Firms

Table 1 lists the calibration choices related to consumers and firms.

Consumers' utility function is  $u(c,s) = \log(c) - \pi \frac{z}{u} \frac{s^2}{2}$ , where the second term only applies to the unemployed. Consumers can have one of four fixed and exogenous levels of education: less than high school (LHS), high school (HS), some college (SC), and college or more (C). The proportion of each was calibrated to equal the equivalents in CPS data (2010-2019). Regarding stochastic human capital, we normalize its lower bound to  $\zeta = 0$  and set its upper bound to  $\bar{\zeta} = 4$  to be arbitrarily large. We also impose that the long-term mean of the (unbounded) stochastic human capital process for the nonemployed converges to the lower bound, i.e.,  $\zeta_o = \underline{\zeta}$ . We adapt the calibration in Jaimovich et al. (2022) of a discrete-time auto-regressive process for stochastic human capital to our continuous-time setting to calibrate  $\sigma_{\zeta}$  and  $\theta_{\zeta}$ . We then use  $\zeta_e$  to approximate the earnings distribution in SIPP

 $<sup>^{20}</sup>$ We assume that the passive job search effort of OLF consumers has no utility relevance.

**Table 1:** Benchmark Calibration: Consumers and Firms

Parameters							
Description	LHS	HS	SC	С	Source/Target		
Preferences & Borrowing							
Discount rate $(100\rho^z)$ :	1.01	0.93	0.89	0.53	Return on $K$ ; education wealth		
Minimum assets (a):	-1.00	-1.39	-1.61	-2.69	Small Debt Levels Allowed		
Production							
Capital Share ( $\alpha$ ):		0.	30		Standard		
Capital depreciation rate $(\delta)$ :		0.	01		Investment-Output ratio		
Skill efficiency units $(y^z)$ :	1	1.04	1.03	1.45	Skill premium CPS		
Home production ( $h^{\nu}$ ):		0.	17		Fall Consumption UI Recipients		
Size of each group (%):	8.00	29.68	27.76	34.56	CPS Averages		
Total-Factor Productivity ( <i>A</i> ):		0.15			Normalize mean wages		
Experience							
Maximum log experience $(\bar{\zeta})$ :		4.	00		Exogenous		
Minimum log experience ( $\zeta$ ):		0.	00		Exogenous		
Rate of mean reversion $(100\theta_{\zeta})$ :	0.95				Jaimovich et al.		
Volatility ( $\sigma_{\zeta}$ ):	0.11				Jaimovich et al.		
Long term $\zeta$ of employed $(\zeta_e)$ :		1.	65		Earnings Distribution SIPP		
Long term $\zeta$ of nonemployed $(\zeta_o)$ :	0.00				Exogenous		
Matching & Bargaining							
Matching function elasticity $(\eta)$ :	0.72				Petrongolo and Pissarides		
Bargaining Power ( $\phi$ ):		0.72			Standard		
Matching efficiency ( $\chi^z$ ):	0.24	0.25	0.26	0.27	Job-finding probability CPS		
Vacancy-posting costs ( $\kappa^z$ ):	0.93	1.22	1.24	1.36	Normalize market tightness		
<b>Labor Market Flows</b>							
Job-destruction probability (100 $m_{eu}^z$ ):	2.26	1.33	1.06	0.62	Flows CPS		
Flows from E to OLF ( $100m_{eo}^z$ ):	3.82	2.27	2.00	1.61	Flows CPS		
Flows from U to OLF ( $100m_{uo}^z$ ):	22.60	18.90	17.90	15.80	Flows CP		
Flows from OLF to U ( $100m_{ou}^z$ ):	1.36	1.77	2.15	1.71	Flows CPS		
JSE disutility $(\pi_u^z)$	2.19	3.01	3.06	3.31	Normalize JSE		
Passive JSE of OLF $(s_o^z)$	0.12	0.14	0.17	0.20	Flows CPS		

data (2019).<sup>21</sup> Finally, we allow small amounts of debt to capture the empirical fact that there are individuals with negative net worth. Maximum borrowing increases with the level of education in proportion to skill premiums.

We assume that final-good producers combine capital and labor services using a Cobb-Douglas production function:  $Y = AK^{\alpha}L^{1-\alpha}$ . As is common in the literature (e.g., Krusell, Mukoyama and Şahin, 2010), we target a capital share of 30%, an investment-output ratio of 23%, and an annual real rate of return on capital of 4%. We also target the ratios of mean wealth among consumers of each level of education in 2019 (US Federal Reserve Board, 2020). All these targets imply  $\alpha = 0.3$ , a depreciation rate of capital  $\delta = 0.012$ , and discount rates  $\rho_1 = 0.0101$ ,  $\rho_2 = 0.0092$ ,  $\rho_3 = 0.0089$ , and  $\rho_4 = 0.0053$ , which agree with Falk et al. (2018) in that patience increases with education. To calibrate total-factor productivity, A, we normalize the average wage (57500 USD in 2018 CPS) to one. For the labor productivity factor,  $y_z$ , we target skill premiums in CPS data (2010-2019).

We use CPS data (1978-2012) to discipline labor market flows. We follow Shimer (2012) and Krusell

<sup>&</sup>lt;sup>21</sup>These parameters are calibrated internally together with others, as detailed below. In most instances, no single parameter reaches a target. But, in describing our calibration choices, we relate the parameter with the intended target.

et al. (2017) to obtain average gross worker flows for each level of education and use them to calibrate exogenous flows ( $m_{eu}^z$ ,  $m_{eo}^z$ ,  $m_{uo}^z$ , and  $m_{ou}^z$ ). We also use these average gross flows to calibrate the matching efficiency,  $\chi_z$ , and OLF passive job search effort,  $s_o^z$ , such that the model matches average unemployed and OLF job-finding rates. The average job search effort of the unemployed and average labor market tightness are normalized to one for each level of education by calibrating the scale of the disutility of job search effort,  $\pi_u^z$ , and vacancy-posting costs,  $\kappa_z$ . The elasticity of the matching function is  $\eta=0.72$ , which agrees with the evidence in Petrongolo and Pissarides (2001). Consumers' bargaining power is also  $\phi=0.72$  as it commonly equals  $\eta$  in the calibration of matching models (e.g., Shimer, 2005).

Finally, we use home production to capture the average 8.2% fall in consumption observed in the first month of recipiency among UI recipients (Ganong and Noel, 2019). We assume  $h(z,\zeta) = h^{\nu}(y_z e^{\zeta}) p_L$ , consistent with the evidence in Boerma and Karabarbounis (2021) that home productivity increases with market productivity, and set  $h_{\nu} = 0.165$  to meet that target.

#### 4.2 Government

Table 2 lists the calibration choices related to taxes, benefit programs, and government spending.

We assume that the consumption tax rate is 5.5% and the capital income tax rate is 30% (similar to those in McKay and Reis, 2016). We use the estimates in Guner, Kaygusuz and Ventura (2014) to calibrate the labor income tax function. Specifically, we focus on the case without tax credits for any household, since we include tax credits in benefit programs. We thus set  $\tau_n = 0.088$  and  $\lambda_n = 0.031$ .

We calibrate the four conditional benefit programs in the model by using information for six US cash or near-cash programs: the *Earned Income Tax Credit* (EITC), the *Advanced Child Tax Credit* (ACTC), the *Child Tax Credit* (CTC), *Unemployment Insurance* (UI), *Supplemental Nutrition Assistance Program* (SNAP), and *Supplemental Security Income* (SSI).<sup>23</sup> These programs have motley categorical and means-testing requirements, differing among them and often by State. It is beyond the scope to capture the idiosyncrasies of each of those programs. Our stylized surrogates merely aim to approximate real-world counterparts.

The EITC, ACTC, and CTC are tax credits. They are, implicitly, employment subsidies, creating prowork incentives (Hoynes and Rothstein, 2019). Since taxes in the model are calculated on a monthly basis and paid instantaneously while employed, we look at these tax credits to calibrate employed

<sup>&</sup>lt;sup>22</sup>As the estimates in Guner, Kaygusuz and Ventura (2014) rely on normalized household income, we rescale labor income in the model assuming that mean household income is 75000.

<sup>&</sup>lt;sup>23</sup>We exclude programs with transfers in kind, such as Medicaid. Our selection covers the lion's share of cash or near-cash welfare programs in the US (Hoynes and Rothstein, 2019). In a robustness check found in Appendix D.2, we consider a scenario that includes the *Temporary Assistance for Needy Families* (TANF) program.

Table 2: Benchmark Calibration: Government

		Parar	neters		
Description	LHS	HS	SC	C	Source/Target
<b>Employed Benefits</b>					
Guaranteed Benefit:	0.03			Total CTC & ACTC transfers	
Subsidy Rate:	0.34			EITC Single 1 child	
Tax Rate:	0.16			EITC Single 1 child	
Phase-out point:		0.	.32		EITC Single 1 child
Maximum Legitimate Transfer:		0.	.08		Total EITC transfers
Maximum Assets:		18	3.26		EITC Single 1 child
Illegitimate Transfer (if $a = 0$ ; 100x):		0.	.96		Taxpayer Advocate
Claim Rate ( $\psi_e^z$ ):	0.60	0.42	0.46	0.41	EITC Recipients PSID
Administrative Costs ( $\iota_{be}$ ):		0.	.01		Taxpayer Advocate
Unemployment Insurance					
Replacement Rate:		0.	.50		Standard
Cap (% bench. wage):		0.	.57		Average UI transfers
Illegitimate Transfer (if $a = 0$ ; 100x):		4.	.13		US Department of Labor
Entitlement $(p_{ui}^{e,z})$ :	0.03	0.05	0.05	0.33	% of Unemployed receiving UI
Expiration $(p_{ui}^u)$ :		0.	.17		Average Duration
Administrative Costs ( $\iota_{bui}$ ):		0.	.10		Whittaker, Isaacs and Overbay
Other Unemployed Benefits					
Guaranteed Benefit:			.11		Unemp. Share SSI & SNAP in PSID
Maximum Assets:			.63		SSI & SNAP Rules
Illegitimate Transfer (if $a = 0$ ; 100x):		0.	.49		Taxpayer Advocate
Claim Rate $(\psi_u^z)$ :	0.39	0.49	0.65	0.86	SSI & SNAP Unemp. Recip. PSID
Administrative Costs ( $\iota_{bu}$ ):		0.	.09		Social Security Admin.; Dep. of Agriculture
OLF Benefits					
Guaranteed Benefit:			.08		OLF Share SSI & SNAP in PSID
Maximum Assets:			.63		SSI & SNAP Rules
Illegitimate Transfer (if $a = 0$ ; 100x):			.45		Taxpayer Advocate
Claim Rate $(\psi_o^z)$ :	0.36	0.47	0.46	0.43	SSI & SNAP OLF Recip. PSID
Administrative Costs ( $\iota_{bo}$ ):		0.	.09		Social Security Admin.; Dep. of Agriculture
Taxes & Government Spending					
Labor income tax level $(100\tau_n)$ :	8.80			Guner, Kaygusuz and Ventura	
Labor income tax progressivity (100 $\lambda_n$ ):	3.10			Guner, Kaygusuz and Ventura	
Capital income tax $(100\tau_a)$ :	30.00			Standard	
Consumption tax rate (100 $\tau_c$ ):			.50		Standard
Government Spending ( $100g_y$ ):		8.	.97		Balanced Budget

benefits,  $b^e$ .<sup>24</sup> Figure C1 in Appendix C illustrates the schedule of  $b^e$ . It is modeled in line with the workings of the EITC: it increases with earned income according to a subsidy rate until it reaches a maximum transfer. This value is received until earnings reach a phase-out point. For earnings higher than this point, the benefit falls with earned income according to a tax rate until it reaches zero for earnings high enough.

In calibrating  $b^e$ , we rely on the EITC schedule for a household with one adult and one dependent. In this case, the subsidy rate is 34%, the tax rate 15.98%, and the phase-out annual income 18661.7 USD (0.32 in model units). We further impose that eligible claimants must have less than 3500 USD (0.06 in model units) in annual capital income. We calibrate the maximum transfer so that total transfers match 69.4 Bn USD of average real yearly spending on EITC (calculated based on the IRS's

<sup>&</sup>lt;sup>24</sup>In practice, these programs also have nonemployed beneficiaries. This can happen if, for instance, a household member obtained earnings in a previous tax year. We abstract from these complications. See Guner, Kaygusuz and Ventura (2023) or Luduvice (2021) for contributions modeling such details.

SOI Bulletins for 2009-2019). Further, since the ACTC and CTC have high income and wealth limits, we assume that the 71 Bn USD of average yearly spending (2009-2017) on these credits are transferred evenly to all claimants of  $b^e$ , whether eligible for the EITC or not.

To calibrate illegitimate transfers, we take a leaf from Taxpayer Advocate (2019) who estimate that about 25% of the total value of EITC transfers is not distributed in accordance with the program's rules. We assume that this amount is distributed among all claimants, regardless of eligibility, according to the decay rule  $e^{-0.02a}$ . In other words, those with fewer assets tend to obtain higher illegitimate transfers as wealthier consumers are more easily screened out. We also assume that the administrative costs of employed benefits are 1% of the total value of transfers, the estimate for the EITC (Taxpayer Advocate, 2019).

Finally, about 28 million taxpayers benefited from the EITC yearly in 2010-19, of which 22.22% were couples. Hence, we scale the claim rates,  $\psi_e^z$ , to reach 33.8 million recipients in the model. To distinguish the claim rates of consumers with different levels of education, we use SIPP data (2017-2019) to estimate the share of EITC beneficiaries of each level of education among employed individuals.

Unemployment insurance has the clearest empirical counterpart. We impose  $p_{ui}^u=1/6$ , so that receiving unemployment insurance lasts approximately six months on average. We set  $p_{ui}^{e,z}$ , the rate at which employed consumers become eligible for unemployment insurance, by targeting the respective recipiency rate (the share of unemployed consumers of each level of education receiving unemployment insurance). We obtain these estimates by rescaling those in Forsythe and Yang (2021) until we reach the average recipiency rate of 28% reported by the BLS. We also follow a calibration strategy for calculating benefits that is common in the literature. We set a replacement rate of 50% but impose a ceiling calibrated to match average total transfers of 24.4 Bn USD during 2017-2019. Finally, every worker receiving unemployment insurance gets an extra amount, also decaying with assets according to  $e^{-0.02a}$ . This amount is calibrated to capture the 8.5% of total transfers misaligned with program rules, as per the US Department of Labor's estimates. Administrative costs are set at 10%, the proportion of total transfers equivalent to the average yearly federal funding for the administration of this program in 2014-2019 (Whittaker, Isaacs and Overbay, 2022).

SSI and SNAP offer recipients a guaranteed benefit and tax earnings heavily (at 50% and 30%). We use information on these programs to calibrate other unemployed benefits and OLF benefits.<sup>26</sup> We impose two eligibility requirements: consumers must be in the appropriate labor market state and, like the real SNAP and SSI, their assets cannot exceed 3000 USD (0.05 in model units). To calibrate claim

 $<sup>^{25}</sup>$ Average transfers in this period were 28.2 Bn USD, but almost 14% of recipients were either younger than 25 or older than 64.

<sup>&</sup>lt;sup>26</sup>In the model, all nonemployed consumers have zero earned income, so the transfer is always the maximum.

rates, we target the recipiency rates of unemployed and OLF consumers per level of education receiving SNAP, SSI, or both in SIPP data (2017-2019). Consumers with the lowest levels of education are the most likely to receive these benefits (see Data column in Table C2 in Appendix C). To calibrate the guaranteed benefit, we target the average real total transfers of SSI and SNAP (70.5 Bn USD) from 2011 to 2019 to those aged 25-64. We split them between the two benefits in the model to match the average share of the value of SSI and SNAP transfers directed at the unemployed (91.6%) and OLF (8.4%) in SIPP data (2017-2019). Finally, we assume that illegitimate transfers (again decaying with assets) amount to 8% of the value of all transfers (Taxpayer Advocate, 2019) and administrative costs to 8.7% (US Social Security Administration, 2022, US Department of Agriculture, 2022).

Total spending in benefit schemes is 2.55% of the average wage, i.e., 1470 USD. Government spending is the residual that balances the budget: it is a share  $g_v = 8.97\%$  of output.

#### 4.3 Internal & External Validation

The calibrated model matches empirical targets well. Tables C1 and C2 in Appendix C show this for the job-finding rates of unemployed and OLF consumers, for skill premiums, for wealth differences in skill, for investment-related targets, and for benefit-related targets. The two leftmost columns of Table 3 compare the earnings distribution in SIPP data (2019) with that delivered by our model. The differences are small.

Table 3: Earnings and Wealth Inequality

	Ear	nings	We	Wealth		
	_Data_	Model	Data	Model		
Q1	0.00	1.30	-0.50	-0.79		
Q2	2.70	4.74	0.80	0.76		
Q3	13.52	10.47	3.40	5.31		
Q4	24.10	21.39	9.00	16.63		
Q5	59.60	62.11	87.40	78.09		

*Note*: This table contrasts the five quintiles of the earnings distribution in 2019 SIPP data and the wealth distribution in the Survey of Consumer Finances 2018 with those in the model.

Table 3 also offers a measure of external validation. The two rightmost columns contrast the share of each quintile of the wealth distribution in the Survey of Consumer Finances (2019) with that in the model. The model offers a good approximation.

The Alaska Permanent Fund Dividend (APFD) is another source of external validation. It is a transfer to all Alaska residents, with few exceptions (see Jones and Marinescu, 2022 for a detailed discussion).

 $<sup>^{27}</sup>$ SIPP identifies the household members that benefit from a program. We use these data to calculate the recipiency rates. Moreover, as, in practice, employed individuals can also be beneficiaries, we reweight the shares of the unemployed and OLF such that the share of beneficiaries in the model is the one we calculate using SIPP data (2017-2019). In calculating these shares, we rule out those with net worth (excluding net holdings in housing and automobiles) higher than 3000 USD and those with yearly earnings exceeding 12000 USD.

It is, therefore, close to the UBI in the model, albeit not tax-financed.<sup>28</sup> According to Jones and Marinescu, the APFD slightly increases employment, but it increases the share of part-time work by 1.8pp. This indicates a small reduction in hours worked. To judge how close our model is to the estimates in Jones and Marinescu, we introduce a UBI worth 2.5% of mean wages (1430 USD; close to the average APFD in real terms since 1982) without adjusting taxes. Our model implies a 0.58pp reduction in employment, close to the findings in Jones and Marinescu and in line with other papers that perform a similar experiment (Luduvice, 2021; Jaimovich et al., 2022).

The evidence in Elsby and Shapiro (2012) and Ortego-Marti (2016, 2017) supports our calibration strategy for the stochastic processes of human capital accumulation and, in particular, our choice of  $\zeta^e$ . Elsby and Shapiro report a difference in log earnings between an experienced and an inexperienced full-time, full-year worker to have been, in 2001-07, approximately 1.02 for LHS workers and 1.2 for workers with College or more. In our model, consumers are ageless and experienced. We produce a counterpart to their estimates by simulating  $\zeta$  over a 12-month period for two types of consumer employed throughout: one starting with  $\zeta = \zeta$  and another with the average  $\zeta$  of the employed with the respective level of education. The model counterparts are very close to the estimates in Elsby and Shapiro. We obtain 0.98 for LHS consumers and 1.24 for those with College or more, the difference between these two magnitudes being explained by the higher average  $\zeta$  of the latter. Additionally, Ortego-Marti offers evidence that, upon nonemployment, each month without a job lowers subsequent earnings by about 0.0122 log points on average, with a higher loss for more educated consumers. In our model, spending a month nonemployed implies that  $\zeta$  falls by 0.0132 on average for those with College and 0.0107 for those with LHS, in line with the evidence.

As presented above, we target the average fall in consumption of unemployment insurance recipients in the first month of recipiency estimated in Ganong and Noel (2019). Yet, Ganong and Noel also offers the path of consumption for those that remain nonemployed up to ten months after the first month of recipiency. We use this evidence to externally validate our calibration. We simulate the path of consumption for those who become unemployed and recipients of UI. Then, we restrict our attention to those who remain recipients of UI for six months and lose recipiency immediately after. Figure D1 in Appendix D shows that our model broadly agrees with the path estimated in Ganong and Noel. Moreover, the consumption paths of the relatively rich (at the time of losing the job) and the rest agree with the variation reported in Ganong and Noel as those relatively rich are better able to smooth consumption.

Finally, we further validate our model by studying the claim rates of consumers with different levels

<sup>&</sup>lt;sup>28</sup>Also, the transfer value varies yearly, even if it has usually been higher than 1000 current USD since 1996.

of education. Empirically, the recipiency rate of a given program falls with the level of education, as conditional programs usually target the worse off. Matching these rates for SSI and SNAP, our model estimates that the claim rates and, consequently, the take-up rates of LHS consumers are the lowest. Since a relatively high proportion of LHS consumers is eligible, take-up rates similar to those of more educated consumers would entail much higher recipiency rates than we find in the data. This implication of our model dovetails the evidence in Tempelman and Houkes-Hommes (2016) and Finkelstein and Notowidigdo (2019), who find that the poorest do not display the highest take-up rates. Poverty is associated with multifaceted barriers, such as poorer health, limited social integration, or lower educational attainment, all of which complicate the application process (Tempelman and Houkes-Hommes). Additionally, there is evidence that the poorest often underestimate the benefits of applying (Finkelstein and Notowidigdo). Indeed, poverty is linked with cognitive burdens that can impair performance and reasoning (Bertrand, Mullainathan and Shafir, 2004; Mani et al., 2013).

# 5 The Burdensome Imperfections of Conditional Programs

A major contribution of our paper is to explicitly model key imperfections of current welfare programs: incomplete take-up, illegitimate transfers, and administrative costs. In Proposition 1, we showed that, under typical assumptions, they are associated with welfare losses vis-a-vis a perfect welfare system. In this section, we quantify these losses. We run a set of experiments in which we remove each imperfection separately and then all three together.<sup>30</sup> The latter case is that of a near-perfect welfare system, the one assumed by almost all contributions in the related literature. In these experiments, the total expenditure on welfare programs remains the same.<sup>31</sup>

Table 4 shows that the three imperfections are not equally consequential in terms of welfare.<sup>32</sup> Removing illegitimate transfers has a negligible effect. Removing administrative costs is more significant, especially for consumers with less than high school, but the overall effect is moderate. The most significant imperfection is clearly incomplete take-up. Solving this imperfection would be equivalent to a permanent increase in consumption of 1.93%.

<sup>&</sup>lt;sup>29</sup>The same is not true for the EITC because our model abstracts from a few of the categorical restrictions that apply in practice. For example, the asset limit for couples equals that of singles, which penalises eligibility for the most educated, who are more likely to be married.

<sup>&</sup>lt;sup>30</sup>To conduct our experiments, we use the finite-difference method described in Achdou et al. (2021) to solve for two deterministic steady-states of the model: the benchmark and the counterfactual.

 $<sup>^{31}</sup>$  To ensure this, we rescale employed benefits, other unemployed benefits, and OLF benefits by adjusting the maximum transfer until expenditures on each program equal their respective new target. For unemployment insurance, we rescale expenditures by adjusting both the replacement rate (capped at 90%) and the maximum transfer. Regarding complete take-up, we set  $\psi_e^z = \psi_u^z = \psi_o^z = 1$  for all z. In the case of unemployment insurance, we approximate complete take-up by dividing the benchmark  $p_{ui}^{e,z}$  by 0.45, an estimate of the take-up rate of this program (Lachowska, Sorkin and Woodbury, 2022). In the cases with complete take-up, we also rescale illegitimate transfers so that their total remains approximately the same. This implies lower average transfers with complete take-up and higher transfers without administrative costs.

<sup>&</sup>lt;sup>32</sup>See Appendix B.6 for details on the welfare measure.

Table 4 also shows that the worse off, here the least educated, bear the brunt of these imperfections. Moving to a perfect welfare system would generate an aggregate consumption-equivalent variation (CEV) of 2.58%. Yet, echoing Proposition 1, this figure rises to 10.99% for consumers with less than high school. As for the better-off, i.e., those with at least a college degree, a perfect welfare system would be equivalent to a relatively small permanent increase in consumption of 0.44%.

**Table 4:** Welfare impact of conditional programs' imperfections

	No Illeg. Transfers	No Admin	100% Take-up	Perfect
CEV Aggregate	0.00	0.38	1.93	2.58
CEV Aggregate CEV LHS	0.12	1.22	8.86	10.99
CEV HS	-0.06	0.62	3.91	5.02
CEV SC	-0.02	0.45	1.79	2.61
CEV C	0.04	0.14	0.24	0.44

*Note:* This table shows the consumption-equivalent variation (CEV, welfare change) of ameliorating the extant welfare system by eliminating each of the three imperfections (first three columns) and all three together (fourth). The first line reports the average CEV, while the other lines decompose it by level of education.

The imperfections of conditional welfare programs are clearly consequential. As discussed, a UBI would be mostly free of these imperfections. Yet, its unconditionality brings problems of its own, including the fact that the worse off would get less relief on average. In the next section, we throw light on the welfare and macroeconomic consequences of introducing a UBI.

# 6 The Effects of Introducing an Expenditure-Neutral UBI

What are the effects of replacing a suite of conditional programs with a universal basic income that costs the same? To answer this, we solve for two deterministic steady-states of our model: one with conditional benefit programs and without UBI transfers, and another with the converse. In all our experiments, we impose that the government spends the same amount on the welfare system and on other spending in both steady-states.<sup>33</sup>

In the first experiment, a UBI replaces the benchmark welfare system, which is composed of four imperfect conditional programs. Then, we investigate whether size matters, as indicated by Proposition 2, by replacing welfare systems of different generosity with a UBI that costs the same. In Appendix D, we complement these experiments by showing that alternative calibrations and the inclusion of the transitional dynamics between steady-states barely affect our main findings.

#### 6.1 Output Increases, while Inequality and Welfare Fall

Table 5 summarizes the main results of the first experiment.

 $<sup>^{33}</sup>$ Expenditures may be the same, but differences in economic activity, such as changes in capital income, may affect tax revenues. If so, the government adjusts  $\tau_n$  to balance the budget.

Replacing the four benefit programs with an expenditure-neutral UBI substantially increases both the capital stock and labor services. This leads to an increase in output of 1.12%. Average wages also increase, whereas both wealth and earnings inequalities fall. The wealth Gini coefficient, for instance, drops from 0.764 to 0.727 (Table D3 in Appendix D offers the breakdown per quintile of wealth and earnings).

Table 5: Effects on economic activity, inequality, and welfare

	Change (%)
Output	1.12
Capital	2.87
Labor Services	0.38
Average Wage	0.50
Wealth Gini	-4.83
CEV	-0.73
Change in Transfers	
Average	0.10
Average among Poor	-1.15

*Note:* This table shows key effects of replacing the benchmark welfare system with an expenditure-neutral UBI. The first five lines report indicators of economic activity and of wealth inequality. These are followed by the consumption-equivalent variation, a measure of welfare change. The last two lines report the change in average transfers and in average transfers to the poor (i.e., those with less than 10000 USD in assets).

Still, introducing an expenditure-neutral UBI is equivalent to a permanent loss of 0.73% of consumption. In other words, it lowers welfare. The last line in Table 5 helps to explain these seemingly paradoxical results. Average transfers to the poorest consumers (those with net worth below 10000 USD) fall by 1.15% of benchmark wages, i.e., by more than 30% of their original value. As the poorest consumers value a dollar of transfer relatively more, the fact that they get smaller transfers significantly impacts welfare. In the benchmark, this effect is strong enough to compensate for the facts that (i) average wages and employment increase, (ii) the introduction of a UBI leads to an increase in the amount available for transfers, as there are no administrative costs, and (iii) a few poor consumers that received no benefits due to incomplete take-up now get a UBI transfer.

Table 6 deepens these results. It shows that college-educated consumers prefer a UBI because their wealth or earnings are usually too high for them to be eligible for conditional benefits. Less educated consumers, on the other hand, tend to lose with a UBI, as they become less well-insured in the worst idiosyncratic states. Interestingly, however, the least educated are not those losing the most with the introduction of a UBI despite enjoying the largest average transfers in the baseline system. This can be explained by noticing Proposition 2, and that the least educated are also those with the lowest claim rates, especially for the two programs that bring the most relief to the poor: other unemployed and OLF benefits. Moreover, they have the lowest endowments, which magnifies the losses of incomplete take-up. Hence, albeit smaller, a UBI reaches all those in need, which partly compensates for

the fall in average transfers.

Table 6: Breakdown by level of education

	LHS	HS	SC	С
CEV	-1.35	-1.38	-1.83	0.20
Employment	4.27	0.15	0.15	0.07
Unemployment	-0.66	-0.06	-0.06	-0.03
Average Wage	-3.32	0.89	0.85	0.89
Job-finding rate	-0.22	0.20	0.26	0.08
Unemployed JSE	-0.72	1.41	1.66	1.50
OLF JSE	30.15	-	-	-
Change in Transfers				
Average	-0.94	-0.13	-0.15	0.74
Average among Poor	-1.70	-1.04	-1.13	-0.93

*Note:* This table decomposes the effects of replacing the benchmark welfare system with an expenditure-neutral UBI by levels of education. The first line reports the consumption-equivalent variation (welfare change). The following six lines report changes in labor market outcomes and job search effort (JSE). The last two lines report the change in average transfers and in average transfers to the poor (i.e., those with less than 10000 USD in assets).

The distortions caused by conditional programs help to explain the increase in capital stock and labor services that a UBI generates. The most generous benefits are only available to nonemployed consumers. This distorts job search effort to such an extent that a substantial fraction of those with less than high school prefer to reject any job offer when they are out of the labor force, instead claiming benefits. Moreover, the most generous benefits also require virtually no asset holdings. There arises the semblance of a *poverty trap*, as the poorest individuals (especially those with low potential for high wages) prefer not to accumulate assets to foster eligibility. Consequently, removing such limits leads to an increase in the capital stock and to more assets being held by the lowest quintiles of the wealth distribution. The substantial reduction in wealth inequality is further explained by precautionary savings as in Luduvice (2021) and Rauh and Santos (2022). Since the average transfers received while poor are lower with a UBI, consumers seek to increase their asset holdings to smooth consumption. They also tend to search more intensively for jobs. The opposite tends to be true for college-educated consumers. With a UBI they have fewer incentives to accumulate assets, also lowering wealth inequality.

In sum, this experiment suggests that replacing the current welfare system fosters economic activity and lowers inequality, but that it also lowers welfare. In our experiments, we find that the increase in economic activity always accompanies the introduction of a UBI. Its negative welfare impact, on the other hand, is not robust, as shown in the next section.

<sup>&</sup>lt;sup>34</sup>Table 6 shows a high increase in passive OLF job search effort with UBI, which indicates that more consumers with LHS search passively for jobs.

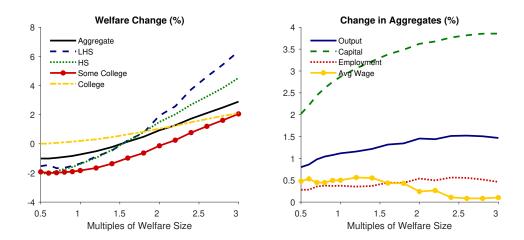
#### 6.2 UBI's Relative Performance Improves with Welfare System Generosity

In recent years, there have been calls to make the social safety net more generous. This begs the question we investigate in this section: how would an expenditure-neutral UBI perform if it replaced a welfare system with a different scale than that of the benchmark?<sup>35</sup>

To answer this question, we proceed in three steps. First, we change the budget of each program proportionately by adjusting the maximum transfer.<sup>36</sup> Second, we update the level of labor income taxes,  $\tau_n$ , to balance the government budget. Third, we compute the expenditure-neutral UBI that replaces the four programs. The results are in Figure 1.

The left panel of Figure 1 evinces that the relative performance of a UBI depends on the scale of the welfare system it is replacing. The solid black line shows that small changes to the scale of the benchmark system have little impact, but that the consumption-equivalent variation of introducing a UBI turns positive if replacing a welfare system 1.6 times larger than the benchmark (UBI would be approximately 2150 USD per year). If the welfare system is 2.1 times the benchmark, all education groups are better off with a UBI (UBI would be approximately 2900 USD per year). <sup>37</sup>

Figure 1: Replacing Welfare Systems of Various Scales with a UBI



*Note:* This figure plots the welfare effects of replacing welfare systems of various scales with expenditure-neutral UBIs. The scale of the welfare system (x-axis) goes from half to three times that of the benchmark. A scale of one is the benchmark reported above. Unemployment insurance is not rescaled. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in the average gross wage.

<sup>&</sup>lt;sup>35</sup>Also, a UBI is often used to refer to an income high enough to cover basic expenses. For instance, during the 2020 presidential campaign, Andrew Yang proposed a UBI of 12000 USD per year, about nine times what we have considered so far. This further motivates our experiments, as they allow us to distinguish the impact of increasing the total value of transfers from that of changing the rationale of their distribution.

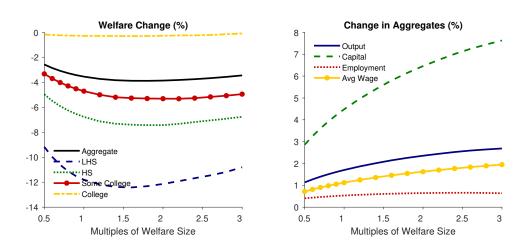
<sup>&</sup>lt;sup>36</sup>We do not do this for unemployment insurance because it is difficult to increase spending with this program without exceeding the 100% replacement rate. We did, however, experiment to the extent possible with a replacement rate of 90%. The results do not change qualitatively.

<sup>&</sup>lt;sup>37</sup>We also find that a scaled-up welfare system, up to three times the benchmark, is welfare-enhancing. In other words, the introduction of a UBI that costs three times the benchmark system would increase welfare.

The right-hand panel in Figure 1 helps explain these results. Like our first experiment, replacing the benchmark welfare system with an expenditure-neutral UBI enhances economic activity. However, this effect grows stronger with the generosity of the system, as it amplifies the distortions brought by conditional programs. In other words, the relative positive impact of a UBI on job search effort, on the accumulation of assets, and, consequently, on output, grows with the generosity of the welfare system. Additionally, the rise in economic activity generates higher government revenues, which demands a lower  $\tau_n$ . This further boosts job search effort, as the net average wage increases (even if the average gross wage falls, as Figure 1 shows). The increase in aggregate income and lower taxes make it possible for consumers to consume more over their lifetimes.

This said, we find, yet again, that imperfections are key. Figure 2 shows the results of doing a similar exercise, only now with welfare systems free of incomplete take-up, illegitimate transfers, and administrative costs. It shows that an expenditure-neutral UBI would not improve welfare even if replacing a welfare system three times larger than the benchmark. In this case, no education group would be better off with a UBI, with the costs falling overwhelmingly on the least educated. This is true even though a UBI would have an even greater positive impact on economic activity, as the less imperfect welfare system demotivates job search effort and asset accumulation even more. Crucially, however, such a welfare system better insures consumers against the worst idiosyncratic states, such as leaving the labor force or suffering a negative human capital shock.

Figure 2: Replacing Welfare Systems Free of Imperfections and of Various Scales with a UBI



*Note:* This figure shows the results of repeating the experiments in Figure 1, only now abstracting from incomplete take-up, illegitimate transfers, and administrative costs. The scale of the welfare system (x-axis) goes from half to three times the benchmark size. A scale of one delivers the same results as in the last column of Table D4. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in the average gross wage.

We thus find that this insurance effect is stronger than the distortionary effect if we scale a welfare system that does not suffer from imperfections, but it is weaker if the system does. In further ex-

periments, we buttress our finding that incomplete take-up is key: a model with complete take-up but with illegitimate transfers and administrative costs delivers a pattern similar to that of Figure 2, while one with incomplete take-up and no other imperfection delivers a pattern similar to Figure 1 (see Figures D2 and D3 in Appendix D). In other words, the outcomes in Figure 1 are partly driven by the increased inequality between claimants and non-claimants resulting from scaling-up conditional programs.<sup>38</sup> This echoes Proposition 2. A more generous benchmark system amplifies the burden of its imperfections and, thus, replacing it with a UBI increases welfare, especially for the worse off.

These results highlight a key finding of our paper. Other studies argue that the optimal UBI would entail a larger welfare system, but that it would not enhance welfare over the optimal conditional welfare system (Ferriere et al., 2023) or even over the benchmark (Guner, Kaygusuz and Ventura, 2023). Yet, contrasting Figures 1 and 2 suggests that such findings may partly turn on abstracting from imperfections, especially incomplete take-up.

Our experiments also disentangle the relevance of the scale of a welfare system from that of the incentive structure it creates. Papers such as Conesa, Li and Li (2023), Daruich and Fernández (2024), Jaimovich et al. (2022), Luduvice (2021) or Rauh and Santos (2022), do not compare a sizable UBI with a welfare system of similar scale, but only with the benchmark.<sup>39</sup> In our experiments (not reported), we find that scaling up the benchmark system would increase welfare, which elucidates the importance of scale. We also find that if the scaling up exceeds 60%, a UBI would be preferable to the scaled-up system, and therefore to the benchmark. This reveals the importance of the incentive structure and how it interacts with scale.

# 7 Extensions & Alternative Setups

#### 7.1 Endogenous Claim Rates

In our benchmark model, claim rates differ by welfare program and consumers' level of education. Yet, they do not change with consumers' other characteristics nor, more importantly, with the generosity of the welfare system. In this section, we examine a version of our model in which claim rates are endogenous. We show that an expenditure-neutral UBI still increases aggregate welfare when replacing welfare systems moderately larger than the benchmark.

In this version of the model, claims are modeled as a two-step process that aims at capturing the main causes of incomplete take-up: imperfect information, stigma, and application costs (Currie, 2006; Ko

<sup>&</sup>lt;sup>38</sup>Appendix D.2 shows that the gains of replacing a generous welfare system with a UBI are robust to different calibrations. <sup>39</sup>Jaimovich et al. (2022), Luduvice (2021), and Rauh and Santos (2022) find that a sizable UBI would increase welfare over the benchmark, while Conesa, Li and Li (2023) and Daruich and Fernández (2024) find the opposite.

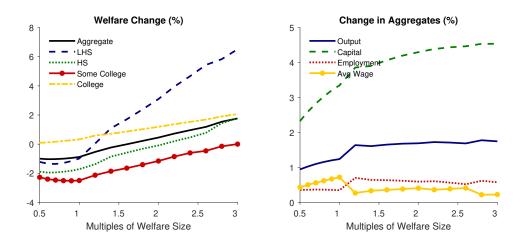
and Moffitt, 2022).<sup>40</sup> The  $\psi_x^z$  are now interpreted as the proportion of those that, upon moving to any labor market state  $(x \in \{e, u, o\})$  or losing eligibility for UI, *could* claim the respective benefits. This captures imperfect information as well as other eligibility constraints not considered in the model. The potential claimants that choose to claim a benefit are then subject to a cost  $C_x^z c$ , where c is a draw from a distribution  $c_x(c)$ . This cost captures the disutility of stigma and application costs. In this version of the model, consumers only claim a benefit if it is indeed worth their while. For example, consumers that move out of the labor force would claim OLF benefits if  $W(a, n^o, b^o, z, \zeta) - C_o^z c > W(a, n^o, b^o, z, \zeta)$ , which, conditional on c, depends on standard wealth, income, and substitution effects. All else remains the same.

To illustrate this version of the model, we assume that  $\zeta_x(c)$  is a log-normal distribution with mean zero and standard deviation  $\sigma_x$ . We assume that claim rates of other unemployed and OLF benefits are fully determined by costs ( $\psi_u^z = \psi_o^z = 1$  for all z) and use  $C_u^z$  and  $C_o^z$  to match recipiency rates. We also assume that costs are proportional to the time spent applying for SNAP benefits, setting  $\sigma_u = \sigma_o = 1.0345$  to match the ratio of the mean and median time needed for an application (Ponza et al., 1999). As for employed benefits, we calibrate them by using  $C_e^z$  to target the ratios of recipiency rates as well as the number of EITC recipients. As the IRS's estimates of household participation in the EITC is 78% and there are categorical restrictions for recipiency beyond those considered in the model, we additionally calibrate  $\psi_e^z$  so that application costs deter only 22% of eligible consumers. Finally, we set  $\sigma_e = 1$ , which implies that claim rates tend to increase 4.5 pp with a 1000 USD annual increase in generosity, similar to the estimates in Plueger (2009).

Our findings are summarized in Figure 3. We highlight three. First, the change to the model affects the benchmark results only slightly. The CEV for LHS and College-educated consumers is slightly higher, while it is smaller for the rest. This stems from two counteracting forces: claim rates become relatively larger for those who need the programs the most, conditional on education, but claiming benefits is now costly. Second, welfare changes are less sensitive to the size of the welfare system than in the baseline, especially for more educated consumers and for relatively large welfare systems. This results from the fact that more generous welfare systems raise the benefits of claiming and thus increase claim rates. Third, a UBI continues to increase aggregate welfare for a sufficiently large welfare system. The cutoffs have increased from 2150 USD to 2300 USD per year, but the main result stands.

 $<sup>^{40}</sup>$ As we do not adjust unemployment insurance as we change the size of the welfare system, we only adapt the claim rate process for employed, other unemployed, and OLF benefits.

Figure 3: Model with Endogenous Claim Rates



*Note:* This figure plots the welfare effects of replacing welfare systems of various scales with expenditure-neutral UBIs. The scale of the welfare system (x-axis) goes from half to three times that of the benchmark. A scale of one is the benchmark reported above. Unemployment insurance is not rescaled. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in the average gross wage.

## 7.2 Endogenizing OLF flows

In our benchmark model, labor force participation flows are mostly driven by exogenous shocks. OLF consumers decide whether to passively look for jobs, but the flows from out of the labor force to unemployment as well as those into the OLF state are driven by Poisson processes. This begs the question of whether our benchmark model fully captures the distortions caused by welfare programs on the labor supply. Hence, in this section, we investigate a version of our model in which all the flows to and from out of the labor force are endogenous.

The shocks bringing consumers out of the labor force,  $m_{eo}^z$  and  $m_{uo}^z$ , can be interpreted as the result of a cost of participating in the labor market that is large enough to compel them to leave. Symmetrically, the shock  $m_{ou}^z$  can be interpreted as the result of a cost compelling all nonparticipants to actively look for jobs. We model this interpretation in a simple way. When agents face the shocks  $m_{eo}^z$  and  $m_{uo}^z$ , they draw a cost of remaining in the labor force, denoted by  $c_p$ , from the probability density functions  $\varphi_e^z(c_p)$  and  $\varphi_u^z(c_p)$ . Similarly, when agents face the shock  $m_{ou}^z$ , they draw a cost of remaining out of the labor force,  $c_o$ , from  $\varphi_o^z(c_o)$ . Moreover, we assume that when consumers draw  $c_p$  or  $c_o$  they become aware of whether they will be welfare claimants conditional on the change in their labor market state. With probability  $\psi_x^z$ , they become claimants if they move. Optimal decision making, therefore, requires that consumers only leave or enter the labor force if it is worth their while. For example, unemployed consumers drawing  $c_p$  move out of the labor force if  $W(a, n^u, b, z, \zeta) - c_p < W(a, n^o, b^o, z, \zeta)$  when they are claimants of OLF benefits and if

 $W(a, n^u, b, z, \zeta) - c_p < W(a, n^o, b^{\varnothing}, z, \zeta)$  when they are not.

To illustrate this extension, we assume that  $\varphi_e^z(\cdot)$ ,  $\varphi_u^z(\cdot)$ , and  $\varphi_o^z(\cdot)$  are discrete probability distributions in which there is 1/2 chance of drawing one of two possible outcomes,  $\{0,\infty\}$ . All consumers that draw  $\infty$  move, but of those that draw 0, only those that are better off in the alternative labor market state will move. We recalibrate the model using  $m_{eo}^z$ ,  $m_{uo}^z$ , and  $m_{ou}^z$  to match the respective flows in the data.

Figure 4 summarizes the results. As expected, the distortions to the labor supply in this extension are larger than in the benchmark model. Replacing the conditional welfare programs with an expenditure-neutral UBI would increase labor supply three times more than in the benchmark. The changes to capital and output are also more substantial. Looking at welfare, however, there are only small changes in the aggregate. This said, we find a substantial change for the least educated, whose CEV increases by 1.83%, contrasting with the loss of 1.35% in the benchmark. If the greater distortions in this extension contribute to this result, the main reason for the fall is the greater persistence in being a welfare claimant, especially when OLF. In the several versions of our model, many LHS consumers claiming OLF benefits would prefer to remain OLF. In this extension, consumers have more agency to remain OLF. Consequently, outflows from this state are smaller in this extension. Given the recipiency rates in the data, this necessitates a correlative fall in the claim rate of OLF benefits,  $\psi_o^z$  (0.145 in this extension and 0.361 in the benchmark), to reduce the inflows. In other words, in the status quo, few of those with an LHS education that leave the labor force benefit from OLF benefits.

Welfare Change (%) Change in Aggregates (% 15 6 Aggregate 5 ·LHS · Capita ···HS ····· Employm 10 Some College Avg Wage College 2 5 0 -1 -5 -2 0.5 1.5 2 2.5 0.5 1.5 2 Multiples of Welfare Size Multiples of Welfare Size

Figure 4: Model with Endogenous OLF Flows

*Note:* This figure plots the welfare effects of replacing welfare systems of various scales with expenditure-neutral UBIs. The scale of the welfare system (x-axis) goes from half to three times that of the benchmark. A scale of one is the benchmark reported above. Unemployment insurance is not rescaled. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in the average gross wage.

We also find that the welfare gains from replacing the benchmark welfare system with an expenditure-

neutral UBI increase with the generosity of the system. This important result is, therefore, robust. In particular, a UBI exceeding 2000 USD per year would increase aggregate welfare.

## 8 Concluding Remarks

Our paper suggests that the gains and losses of a UBI are not black and white. First, economic activity, measured by capital accumulation, employment, and output, is increased with the introduction of a UBI, as it alleviates the distortions of conditional programs. Second, a UBI leads to less inequality, as consumers are more motivated to accumulate assets, be it because they are not penalized in their eligibility for welfare programs, or because they are no longer as well insured against idiosyncratic risks. Third, an expenditure-neutral UBI lowers welfare in our benchmark because the poor tend to receive smaller average transfers. The fall in welfare is, however, neither robust nor universal. It is not robust because it hinges on the scale of the welfare system: the bigger the system, the costlier its distortions and imperfections. It is not universal because it varies by level of education. Those with a college education benefit from a UBI in our benchmark and, for larger systems, the least educated are the group benefiting the most.

A major contribution of our paper is in taking up the challenge of modeling three real-world imperfections of extant conditional programs: incomplete take-up, illegitimate transfers, and administrative costs. We find that these imperfections impose a heavy welfare burden. Abstracting from them – particularly incomplete take-up – is therefore consequential: an expenditure-neutral UBI does not stand a chance against perfect conditional programs. Yet, once imperfections are taken into account, a UBI is preferable to the benchmark welfare system if generous enough. <sup>41</sup>

The imperfections of conditional programs are also relevant in assessing related alternatives to the current system, such as a Negative Income Tax (NIT). The NIT is a combination of a flat transfer (UBI) with a flat income tax rate. Insofar as an NIT entails replacing imperfect conditional programs with a UBI, estimates of the welfare loss (gain) of an NIT that ignore those imperfections should be treated as an upper (lower) bound. For example, Guner, Kaygusuz and Ventura (2023) find that the optimal NIT is better than the benchmark welfare system, while Boar and Midrigan (2022) find that the optimal NIT is almost as welfare-improving as the optimal system with progressive income and wealth taxes. Yet, both contributions, as well as others in the literature, abstract from the imperfections of conditional welfare programs, which weakens the case for an NIT.

Finally, our findings illuminate much beyond the impacts of replacing conditional programs with

<sup>&</sup>lt;sup>41</sup>Our model includes a wealth of substantial features besides those imperfections. Still, there are alternative modeling choices that we did not consider, for instance, that of explicitly modelling overlapping generations or household composition. Propositions 1 and 2 indicate that our central results should be robust. This warrants further research.

an unconditional one. They remind us that a policy option may seem best in a perfect setting, but that practical implementation often raises issues with first-order importance. Indeed, conditional programs with complete take-up and no illegitimate transfers would be much preferred to a simple UBI, as they would reach perfectly all those and just those they target. But this is not so in practice. Such a deviation from the ideal could well reverse the preferable policy choice.

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# **Appendix**

## A Proofs Endowment Economy

## **A.1** Proof of Proposition 1:

i) Follows directly from the strict concavity of  $u(\cdot)$ ,  $0 < \psi < 1$ , and  $T_L > 0$ .

ii) 
$$\frac{\delta\Xi}{\delta\psi} = -u(y_L + T_L/\psi) + \psi \cdot \frac{T_L}{\psi^2} \cdot u'(y_L + T_L/\psi) + u(y_L) = u(y_L) - u(y_L + T_L/\psi) - u'(y_L + T_L/\psi)[y_L - (y_L + T_L/\psi)] < 0,$$

since  $0 < \psi < 1$ ,  $T_L > 0$ , and  $u(\cdot)$  strictly concave.

iii) 
$$\frac{\delta\Xi}{\delta T_L} = u'(y_L + T_L) - \frac{\psi}{\psi} \cdot u'(y_L + T_L/\psi) = u'(y_L + T_L) - u'(y_L + T_L/\psi) > 0,$$

since  $y_L + T_L < y + T_L/\psi$ , as  $0 < \psi < 1$  and  $T_L > 0$ , and  $u(\cdot)$  strictly concave.

iv) 
$$\frac{\delta\Xi}{\delta y_L} = u'(y_L + T_L) - \psi . u'(y_L + T_L/\psi) - u'(y_L) + \psi . u'(y_L) = u'(y_L + T_L) - [\psi . u'(y_L + T_L/\psi) + (1 - \psi) . u'(y_L)] < 0,$$

since  $0 < \psi < 1$ ,  $T_L > 0$ , and  $u'(\cdot)$  strictly convex.

#### **A.2** Proof of Proposition 2:

i) Let  $x \in \mathbb{R}$  be such that

$$u(y_L + T_L - x) = \psi u (y_L + T_L / \psi) + (1 - \psi) u(y_L)$$

Since  $u(\cdot)$  is continuous, x exists. Since  $u(\cdot)$  is strictly increasing, x is unique. Without loss of generality,  $x = \xi T_L$ , for some  $\xi \in \mathbb{R}$ .

 $\Xi > 0 \iff u(y_L + T_L) > u(y_L + T_L - x) \iff y_L + T_L > y_L + T_L - x$ , since  $u(\cdot)$  strictly increasing.

But 
$$y_L + T_L > y_L + T_L - x \iff x > 0 \iff \xi > 0$$
, since  $T_L > 0$ .

- ii)  $\xi > 0$  follows trivially from Prop. 1 (i) and Prop. 2 (i). Suppose  $\xi \ge 1$ . Then  $u(y_L + (1 \xi)T_L) \le u(y_L) \implies u(y_L + T_L/\psi) \le u(y_L)$ , which contradicts  $u(\cdot)$  strictly increasing,  $T_L > 0$  or  $0 < \psi < 1$ .
- iii) Let  $\psi' > \psi$ . From Prop. 1 (ii) follows that

$$u(y_L + T_L) - \left[\psi'u(y_L + T_L/\psi') + (1 - \psi')u(y_L)\right] < u(y_L + T_L) - \left[\psi u(y_L + T_L/\psi) + (1 - \psi)u(y_L)\right] \iff$$

 $\left[\psi'u\left(y_L + T_L/\psi'\right) + (1 - \psi')u(y_L)\right] > \left[\psi u\left(y_L + T_L/\psi\right) + (1 - \psi)u(y_L)\right] \iff u(y_L + (1 - \xi')T_L) > u(y_L$ 

iv) Let  $T'_L > T_L$ . Since  $u(\cdot)$  strictly increasing,  $u(y_L + T'_L/\psi) > u(y_L + T_L/\psi) \iff \psi u(y_L + T'_L/\psi) + (1 - \psi)u(y_L) > \psi u(y_L + T_L/\psi) + (1 - \psi)u(y_L) \iff u(y_L + (1 - \xi')T'_L) > u(y_L + (1 - \xi)T_L)$ . Then,  $y_L + (1 - \xi')T'_L > y_L + (1 - \xi)T_L$ . Consequently,  $y_L + T'_L > y_L + T_L \iff (y_L + T'_L) - (y_L + (1 - \xi)T_L) > (y_L + T_L) - (y_L + (1 - \xi')T'_L) \iff \xi'T'_L > \xi T_L$ 

To prove the second claim in (iv) and to prove (v), take a second-order Taylor approximation of each side of Eq. 2:

$$u(y_L + T_L) - u'(y_L + T_L)\xi T_L + \frac{1}{2}u''(y_L + T_L)\xi^2 T_L^2 = u(y_L + T_L) + \frac{1}{2}u''(y_L + T_L)T_L^2(1/\psi - 1) \Leftrightarrow$$

$$-u'(y_L + T_L)\xi T_L + \frac{1}{2}u''(y_L + T_L)\xi^2 T_L^2 = \frac{1}{2}u''(y_L + T_L)T_L^2(1/\psi - 1) \Leftrightarrow$$

$$-u'(y_L + T_L)\xi + \frac{1}{2}u''(y_L + T_L)\xi^2 T_L = \frac{1}{2}u''(y_L + T_L)T_L(1/\psi - 1) \Leftrightarrow$$

$$\xi - \frac{1}{2} \frac{u''(y_L + T_L)}{u'(y_L + T_L)} \xi^2 T_L = -\frac{1}{2} \frac{u''(y_L + T_L)}{u'(y_L + T_L)} T_L \left(\frac{1}{\psi} - 1\right)$$
(A1)

Assume that the utility function displays constant absolute risk aversion (CARA). Let  $\theta = -\frac{u''(y_L + T_L)}{u'(y_L + T_L)} > 0$ . In this shorthand, Eq. A1 becomes:

$$\xi + \frac{1}{2}\theta \xi^2 T_L = \frac{1}{2}\theta T_L \left(\frac{1}{\psi} - 1\right) \Leftrightarrow$$
$$\xi = \frac{1}{2}\theta T_L \left(\frac{1}{\psi} - 1 - \xi^2\right)$$

Taking the derivative of both sides with respect to  $T_L$ , noticing that, given CARA,  $\frac{\partial \theta}{\partial T_L} = 0$ , yields:

$$\frac{\partial \xi}{\partial T_L} = \frac{1}{2}\theta \left(\frac{1}{\psi} - 1 - \xi^2\right) - \theta T_L \xi \frac{\partial \xi}{\partial T_L} \Leftrightarrow \frac{\partial \xi}{\partial T_L} (1 + \theta \xi T_L) = \frac{1}{2}\theta \left(\frac{1}{\psi} - 1 - \xi^2\right)$$

As  $0 < \xi < 1$  (Prop. 2 (ii)),  $T_L > 0$ , and  $\theta > 0$ ,  $\frac{1}{\psi} - 1 - \xi^2$  and  $1 + \theta \xi T_L$  are both positive magnitudes. Consequently,  $\frac{\partial \xi}{\partial T_L} > 0$  (iv). Taking the derivative of Eq. A1 with respect to  $y_L$  makes it straightforward to see that  $\frac{\partial \xi}{\partial y_L} = 0$  (v).

Assume that the utility function displays constant relative risk aversion (CRRA). Let  $\theta \equiv -\frac{u''(y_L + T_L)}{u'(y_L + T_L)}(y_L + T_L)$ 

 $T_L$ ). In this shorthand, Eq. A1 becomes:

$$\xi = \frac{1}{2}\theta \frac{T_L}{y_L + T_L} \left( \frac{1}{\psi} - 1 - \xi^2 \right)$$

Taking the derivative of both sides with respect to  $T_L$ , noticing that, given CRRA,  $\frac{\partial \theta}{\partial T_L} = 0$ , yields

$$\frac{\partial \xi}{\partial T_L} \left( 1 + \theta \xi \frac{T_L}{y_L + T_L} \right) = \frac{1}{2} \theta \frac{\partial \frac{T_L}{y_L + T_L}}{\partial T_L} \left( \frac{1}{\psi} - 1 - \xi^2 \right)$$

Since  $0 < \xi < 1$ ,  $y_L > 0$ ,  $T_L > 0$ , and  $\theta > 0$ ,  $\frac{\partial \xi}{\partial T_L}$  must be positive (iv). Taking the derivative of Eq. A1 with respect to  $y_L$  makes it straightforward to see that  $\frac{\partial \xi}{\partial y_L} < 0$  (v).

# **Online Appendix**

### B Further Details of the Model

Throughout this appendix, we use  $X_{j,l}^x$  as shorthand for any function X depending on the entire vector of idiosyncratic states,  $(a, n^x, b_l^j, z, \zeta)$ , where  $x \in \{e, u, o\}$ ,  $j \in \{e, ui, u, o, \varnothing\}$ , and  $l \in \{ui, \varnothing\}$ , the latter only relevant to the employed (x = e). In the case of wages,  $w(a, b_l^j, z, \zeta)$ , and the value of firms,  $J(a, b, z, \zeta)$ , we use the shorthand  $w_l^j$  and  $J_l^j$ .

## **B.1** Consumers' HJB Equations

Here we present all possible HJB equations describing a consumer's problem.

The HJB of an employed consumer claiming employed benefits and eligible for unemployment insurance is given by:

$$\rho_{z}W_{e,ui}^{e} = u(c_{e,ui}^{e}, 0) + \partial_{a}W_{e,ui}^{e} \left[ (1 - \tau_{n})(w_{ui}^{e})^{1 - \lambda_{n}} + B_{ui}^{e} + UBI + (1 - \tau_{a})(r - \delta)a - (1 + \tau_{c})c_{e,ui}^{e} \right]$$

$$+ m_{eu}^{z} \left[ W_{ui}^{u} - W_{e,ui}^{e} \right] + m_{eo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1 - \psi_{o}^{z})W_{\varnothing}^{o} - W_{e,ui}^{e} \right] + \theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}W_{e,ui}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{e,ui}^{e}.$$
(B1)

The HJB shows that the flow value depends on instantaneous utility, which is only a function of consumption because consumers only search for jobs when nonemployed. The flow value also depends on changes in asset holdings (i.e., on the budget constraint). Note that the benefits  $B^e_{ui}$  depend on whether the consumer is eligible for unemployment insurance because it affects the wage. Moreover, the flow value depends on the risk of moving to unemployment and receiving unemployment insurance, on the risk of moving out of the labor force and, if moving, whether OLF benefits are claimed. Finally, the flow value depends on stochastic changes in human capital.

The HJB of an employed consumer claiming employed benefits and ineligible for unemployment insurance is:

$$\begin{split} \rho_{z}W_{e,\varnothing}^{e} &= u(c_{e,\varnothing}^{e},0) + \partial_{a}W_{e,\varnothing}^{e} \left[ (1-\tau_{n})(w_{\varnothing}^{e})^{1-\lambda_{n}} + B_{\varnothing}^{e} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{e,\varnothing}^{e} \right] \\ &+ p_{ui}^{e,z} \left[ W_{e,ui}^{e} - W_{e,\varnothing}^{e} \right] + m_{eu}^{z} \left[ \psi_{u}^{z}W_{u}^{u} + (1-\psi_{u}^{z})W_{\varnothing}^{u} - W_{e,\varnothing}^{e} \right] + m_{eo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1-\psi_{o}^{z})W_{\varnothing}^{o} - W_{e,\varnothing}^{e} \right] \\ &+ \theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}W_{e,\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{e,\varnothing}^{e}. \end{split}$$
 (B2)

There are two major differences relative to Eq. (B1). One is the additional term accounting for the impact of becoming eligible for unemployment insurance (UI) on the flow value. Another is the term to account for the claiming risk when moving to unemployment without being eligible for UI.

The HJBs of an employed consumer not earning employed benefits are:

$$\begin{split} \rho_{z}W_{\varnothing,ui}^{e} &= u(c_{\varnothing,ui}^{e},0) + \partial_{a}W_{\varnothing,ui}^{e} \left[ (1-\tau_{n})(w_{ui}^{\varnothing})^{1-\lambda_{n}} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{\varnothing,ui}^{e} \right] \\ &+ m_{eu}^{z} \left[ W_{ui}^{u} - W_{\varnothing,ui}^{e} \right] + m_{eo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1-\psi_{o}^{z})W_{\varnothing}^{o} - W_{\varnothing,ui}^{e} \right] + \theta_{\zeta}(\zeta_{e}-\zeta)\partial_{\zeta}W_{\varnothing,ui}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{\varnothing,ui}^{e}, \\ & \rho_{z}W_{\varnothing,\varnothing}^{e} = u(c_{\varnothing,\varnothing}^{e},0) + \partial_{a}W_{\varnothing,\varnothing}^{e} \left[ (1-\tau_{n})(w_{\varnothing}^{\varnothing})^{1-\lambda_{n}} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{\varnothing,\varnothing}^{e} \right] \\ &+ p_{ui}^{e} \left[ W_{\varnothing,ui}^{e} - W_{\varnothing,\varnothing}^{e} \right] + m_{eu}^{z} \left[ \psi_{u}^{z}W_{u}^{u} + (1-\psi_{u}^{z})W_{\varnothing}^{u} - W_{\varnothing,\varnothing}^{e} \right] + m_{eo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1-\psi_{o}^{z})W_{\varnothing,\varnothing}^{o} - W_{\varnothing,\varnothing}^{e} \right] \\ &+ \theta_{\zeta}(\zeta_{e}-\zeta)\partial_{\zeta}W_{\varnothing,\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{\varnothing,\varnothing}^{e}. \end{split}$$
(B4)

The main difference relative to Eqs. (B1) and (B2) (respectively) is that these consumers do not claim employed benefits, which affects their budget constraints.

The HJB of an unemployed consumer claiming other unemployed benefits is:

$$\begin{split} \rho_{z}W_{u}^{u} &= u(c_{u}^{u}, s_{u}^{u}) + \partial_{a}W_{u}^{u} \left[ h(z,\zeta) + B^{u} + UBI + (1 - \tau_{a})(r - \delta)a - (1 + \tau_{c})c_{u}^{u} \right] \\ &+ s_{u}^{u}f(z,\zeta) \left[ \psi_{e}^{z}W_{e,\varnothing}^{e} + (1 - \psi_{e}^{z})W_{\varnothing,\varnothing}^{e} - W_{u}^{u} \right] + m_{uo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1 - \psi_{o}^{z})W_{\varnothing}^{o} - W_{u}^{u} \right] \\ &+ \theta_{\zeta}(\zeta_{o} - \zeta)\partial_{\zeta}W_{u}^{u} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{u}^{u}. \end{split} \tag{B5}$$

Compared with Eq. (11), this equation has one less term as, contrary to those earning unemployment insurance, consumers receiving other unemployed benefits do not lose eligibility while unemployed. The same applies to the HJB of an unemployed consumer claiming no conditional benefits:

$$\begin{split} \rho_z W^u_\varnothing &= u(c^u_\varnothing, s^u_\varnothing) + \partial_a W^u_\varnothing \left[ h(z,\zeta) + UBI + (1-\tau_a)(r-\delta)a - (1+\tau_c)c^u_\varnothing \right] \\ &+ s^u_\varnothing f(z,\zeta) \left[ \psi^z_e W^e_{e,\varnothing} + (1-\psi^z_e) W^e_{\varnothing,\varnothing} - W^u_\varnothing \right] + m^z_{uo} \left[ \psi^z_o W^o_o + (1-\psi^z_o) W^o_\varnothing - W^u_\varnothing \right] \\ &+ \theta_\zeta (\zeta_o - \zeta) \partial_\zeta W^u_\varnothing + \frac{\sigma^2_\zeta}{2} \partial^2_{\zeta\zeta} W^u_\varnothing, \end{split} \tag{B6}$$

which also has a simpler budget constraint.

Finally, the HJBs for consumers out of the labor force (OLF) are:

$$\begin{split} \rho_{z}W_{o}^{o} &= u(c_{o}^{o},0) + \partial_{a}W_{o}^{o} \left[ h(z,\zeta) + B^{o} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{o}^{o} \right] \\ &+ s_{o}^{o}f(z,\zeta) \left[ \psi_{e}^{z}W_{e,\varnothing}^{e} + (1-\psi_{e}^{z})W_{\varnothing,\varnothing}^{e} - W_{o}^{o} \right] + m_{ou}^{z} \left[ \psi_{u}^{z}W_{u}^{u} + (1-\psi_{u}^{z})W_{\varnothing}^{u} - W_{o}^{o} \right] \\ &+ \theta_{\zeta}(\zeta_{o} - \zeta)\partial_{\zeta}W_{o}^{o} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{o}^{o}, \end{split} \tag{B7}$$

$$\rho_{z}W_{\varnothing}^{o} = u(c_{\varnothing}^{o}, 0) + \partial_{a}W_{\varnothing}^{o} \left[ h(z, \zeta) + UBI + (1 - \tau_{a})(r - \delta)a - (1 + \tau_{c})c_{\varnothing}^{o} \right]$$

$$+ s_{\varnothing}^{o} f(z, \zeta) \left[ \psi_{e}^{z}W_{e,\varnothing}^{e} + (1 - \psi_{e}^{z})W_{\varnothing,\varnothing}^{e} - W_{\varnothing}^{o} \right] + m_{ou}^{z} \left[ \psi_{u}^{z}W_{u}^{u} + (1 - \psi_{u}^{z})W_{\varnothing}^{u} - W_{\varnothing}^{o} \right]$$

$$+ \theta_{\zeta}(\zeta_{o} - \zeta)\partial_{\zeta}W_{\varnothing}^{o} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{\varnothing}^{o},$$
(B8)

Even though OLF consumers choose whether to search for jobs, they only choose on the extensive margin and searching for jobs does not affect their utility since we assume that the search happens passively. Other than this, all other changes relative to Eqs. (B5) and (B6) are to account for the fact that the flows between the two labor market states reverse direction.

For completeness, we reproduce the HJB of an unemployed consumer receiving unemployment insurance found in the main text:

$$\begin{split} \rho_{z}W_{ui}^{u} &= u(c_{ui}^{u}, s_{ui}^{u}) + \partial_{a}W_{ui}^{u} \left[ h(z,\zeta) + B_{ui}^{u} + UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{ui}^{u} \right] \\ &+ s_{ui}^{u}f(z,\zeta) \left[ \psi_{e}^{z}W_{e,ui}^{e} + (1-\psi_{e}^{z})W_{\varnothing,ui}^{e} - W_{ui}^{u} \right] + p_{ui}^{u} \left[ \psi_{u}^{z}W_{u}^{u} + (1-\psi_{u}^{z})W_{\varnothing}^{u} - W_{ui}^{u} \right] \\ &+ m_{uo}^{z} \left[ \psi_{o}^{z}W_{o}^{o} + (1-\psi_{o}^{z})W_{\varnothing}^{o} - W_{ui}^{u} \right] + \theta_{\zeta}(\zeta_{o} - \zeta)\partial_{\zeta}W_{ui}^{u} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta\zeta}^{2}W_{ui}^{u} \right\}. \end{split} \tag{B9}$$

#### **B.2** Labor Firms' HJB

The HJB of a firm employing a consumer eligible for unemployment insurance is:

$$(r - \delta + m_{eu}^z + m_{eo}^z)J_{ui}^e = ze^{\zeta}p_L - w_{ui}^e + \partial_a J_{ui}^e \dot{a}_{e,ui}^e + \theta_{\zeta}(\zeta_e - \zeta)\partial_{\zeta} J_{ui}^e + \frac{\sigma_{\zeta}^2}{2}\partial_{\zeta\zeta}^2 J_{ui}^e,$$
 (B10)

which mainly differs from Eq. (10) because it does not include the last term. The two HJBs remaining, of firms employing consumers not claiming employed benefits, are, respectively, the same as (B10) and (10) except that the consumer's claimant status is either  $b_{ui}^{\varnothing}$  and  $b_0^{\varnothing}$ .

#### **B.3** Wage Equations

Using the consumers' HJB equations in Appendix B.1 and  $J(a, b, z, \zeta)$  in Section 3.3, the wage of an employed consumer claiming employed benefits and entitled to unemployment insurance satisfies:

$$w_{ui}^{e} \left[ (1 - \phi) \frac{\partial_{a} W_{e,ui}^{e} (1 - \tau_{n}) (w_{ui}^{e})^{-\lambda_{n}}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} + \phi \frac{1 - \partial_{a} J_{ui}^{e} (1 - \tau_{n}) (w_{ui}^{e})^{-\lambda_{n}}}{r - \delta + m_{uo}^{z} + m_{eo}^{z}} \right]$$

$$= (\phi - 1) \frac{u(c_{e,ui}^{e}, 0) + \partial_{a} W_{e,ui}^{e} \left[ B_{ui}^{e} + UBI + (1 - \tau_{a}) (r - \delta) a - (1 + \tau_{c}) c_{e,ui}^{e} \right]}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}}$$

$$+ (\phi - 1) \frac{-(\rho_{z} + m_{eo}^{z}) W_{ui}^{u} + m_{eo}^{z} \left[ \psi_{o} W_{o}^{o} + (1 - \psi_{o}) W_{\emptyset}^{o} \right]}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} + (\phi - 1) \frac{\theta_{\zeta} (\zeta_{e} - \zeta) \partial_{\zeta} W_{e,ui}^{e} + \frac{\sigma_{\zeta}^{2}}{2} \partial_{\zeta\zeta}^{2} W_{e,ui}^{e}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}}$$

$$+ \phi \frac{p_{L} z e^{\zeta} + \partial_{a} J_{ui}^{e} \left[ B_{ui}^{e} + UBI + (1 - \tau_{a}) (r - \delta) a - (1 + \tau_{c}) c_{e,ui}^{e} \right]}{r - \delta + m_{uo}^{z} + m_{eo}^{z}} + \phi \frac{\theta_{\zeta} (\zeta_{e} - \zeta) \partial_{\zeta} J_{ui}^{e} + \frac{\sigma_{\zeta}^{2}}{2} \partial_{\zeta\zeta}^{2} J_{ui}^{e}}{r - \delta + m_{uo}^{z} + m_{eo}^{z}}.$$
(B11)

The wage of a consumer claiming employed benefits but ineligible for unemployment insurance is:

$$\begin{split} w_{\varnothing}^{e} \bigg[ (1-\phi) \frac{\partial_{a} W_{e,\varnothing}^{e}(1-\tau_{n})(w_{\varnothing}^{e})^{-\lambda_{n}}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} + \phi \frac{1-\partial_{a} J_{\varnothing}^{e}(1-\tau_{n})(w_{\varnothing}^{e})^{-\lambda_{n}}}{r - \delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \bigg] \\ = (\phi - 1) \frac{u(c_{e,\varnothing}^{e}, 0) + \partial_{a} W_{e,\varnothing}^{e} \bigg[ B_{\varnothing}^{e} + UBI + (1-\tau_{a})(r - \delta)a - (1+\tau_{c})c_{e,\varnothing}^{e} \bigg] + p_{ui}^{e,z} W_{e,ui}^{e}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \\ + (\phi - 1) \frac{-(\rho_{z} + m_{eo}^{z} + p_{ui}^{e,z}) \left[ \psi_{u} W_{u}^{u} + (1-\psi_{u}) W_{\varnothing}^{u} \right] + m_{eo}^{z} \left[ \psi_{o} W_{o}^{o} + (1-\psi_{o}) W_{\varnothing}^{o} \right]}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \\ + (\phi - 1) \frac{\theta_{\zeta}(\zeta_{e} - \zeta) \partial_{\zeta} W_{e,\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2} \partial_{\zeta\zeta}^{2} W_{e,\varnothing}^{e}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}}} \\ + \phi \frac{\mu_{L} z e^{\zeta} + \partial_{a} J_{\varnothing}^{e} \left[ B_{\varnothing}^{e} + UBI + (1-\tau_{a})(r - \delta)a - (1+\tau_{c})c_{e,\varnothing}^{e} \right] + p_{ui}^{e,z} J_{ui}^{e}}{r - \delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}}} + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta) \partial_{\zeta} J_{\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2} \partial_{\zeta\zeta}^{2} J_{\varnothing}^{e}}{r - \delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}}}. \end{split}$$
(B12)

The wage of a consumer not claiming employed benefits and eligible or ineligible for unemployment

insurance are, respectively:

$$\begin{split} w_{ui}^{\varnothing} \left[ (1-\phi) \frac{\partial_{a} W_{\varnothing,ui}^{e}(1-\tau_{n})(w_{ui}^{\varnothing})^{-\lambda_{n}}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} + \phi \frac{1-\partial_{a} J_{ui}^{\varnothing}(1-\tau_{n})(w_{ui}^{\varnothing})^{-\lambda_{n}}}{r-\delta + m_{uo}^{z} + m_{eo}^{z}} \right] \\ = (\phi-1) \frac{u(c_{\varnothing,ui}^{e},0) + \partial_{a} W_{\varnothing,ui}^{e}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} \left[ UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{\varnothing,ui}^{e}} \right]}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} \\ + (\phi-1) \frac{-(\rho_{z} + m_{eo}^{z})W_{ui}^{u} + m_{eo}^{z}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} + (\phi-1) \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}W_{\varnothing,ui}^{e} + \frac{\sigma_{\zeta}^{z}}{2}\partial_{\zeta\zeta}^{2}W_{\varnothing,ui}^{e}}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} \\ + \phi \frac{p_{L}ze^{\zeta} + \partial_{a}J_{ui}^{\varnothing} \left[ UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{\varnothing,ui}^{e}}{r-\delta + m_{uo}^{z} + m_{eo}^{z}} + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}V_{\varnothing,ui}^{u} + \frac{\sigma_{\zeta}^{z}}{2}\partial_{\zeta\zeta}^{2}J_{ui}^{\omega}}{r-\delta + m_{uo}^{z} + m_{eo}^{z}} \right]} \\ = (\phi-1) \frac{u(c_{\varnothing,\varnothing}^{e},0) + \partial_{a}W_{\varnothing,\varnothing}^{e}(1-\tau_{n})(w_{\varnothing}^{\varnothing})^{-\lambda_{n}}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z}} + \phi \frac{1-\partial_{a}J(a,b_{\varnothing}^{\varnothing},z,\zeta)(1-\tau_{n})(w_{\varnothing}^{\varnothing})^{-\lambda_{n}}}{r-\delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{u}}} \\ = (\phi-1) \frac{u(c_{\varnothing,\varnothing}^{e},0) + \partial_{a}W_{\varnothing,\varnothing}^{e} \left[ UBI + (1-\tau_{a})(r-\delta)a - (1+\tau_{c})c_{\varnothing,\varnothing}^{e} \right] + p_{ui}^{e,z}W_{\varnothing,ui}^{e}}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \\ + (\phi-1) \frac{-(\rho_{z} + m_{uo}^{z} + p_{uo}^{e,z}) \left[ W_{u}W_{u}^{u} + (1-\psi_{u})W_{\varnothing}^{u} \right] + m_{eo}^{z} \left[ \psi_{o}W_{o}^{o} + (1-\psi_{o})W_{\varnothing}^{o} \right]}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \\ + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}W_{\varnothing,\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta}^{2}W_{\varnothing,\varnothing}^{e}}{\rho_{z}^{2}\partial_{\zeta}^{2}(\zeta_{\zeta}W_{\varnothing,\varnothing}^{e})} + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}W_{\varnothing,\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta}^{2}(\zeta_{\zeta}W_{\varnothing,\varnothing}^{e})}{\rho_{z} + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}} \\ + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}U_{\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta}^{2}(J(a,b_{\varnothing}^{\varnothing},z,\zeta)})}{r-\delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}}} + \phi \frac{\theta_{\zeta}(\zeta_{e} - \zeta)\partial_{\zeta}U_{\varnothing}^{e} + \frac{\sigma_{\zeta}^{2}}{2}\partial_{\zeta}^{2}(J(a,b_{\varnothing}^{\varnothing},z,\zeta)})}{r-\delta + m_{uo}^{z} + m_{eo}^{z} + p_{ui}^{e,z}}} \\ (B14)$$

## **B.4** Density Functions

The density of employed consumers claiming employed benefits and eligible for unemployment insurance evolves according to the Kolmogorov forward equation (KFE):

$$\partial_{t}g_{e,ui}^{e} = -\partial_{a}\left[\dot{a}_{e,ui}^{e}g_{e,ui}^{e}\right] - \left[m_{eu}^{z} + m_{eo}^{z}\right]g_{e,ui}^{e} + s_{ui}^{u}f(z,\zeta)\psi_{e}g_{ui}^{u} + p_{ui}^{e}g_{e,\varnothing}^{e} - \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{e} - \zeta)g_{e,ui}^{e}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{e,ui}^{e}\right].$$
(B15)

Looking at the left-hand side, this equation shows the effect of savings, flows out of employment, flows from those earning unemployment insurance who find jobs, and changes in stochastic human capital.

The KFE of an employed consumer claiming employed benefits but not eligible for unemployment

insurance is:

$$\begin{split} \partial_{t}g_{e,\varnothing}^{e} &= -\partial_{a}\left[\dot{a}_{e,\varnothing}^{e}g_{e,\varnothing}^{e}\right] - \left[m_{eu}^{z} + m_{eo}^{z} + p_{ui}^{e}\right]g_{e,\varnothing}^{e} \\ &+ \psi_{e}f(z,\zeta)\left(s_{u}^{u}g_{u}^{u} + s_{\varnothing}^{u}g_{\varnothing}^{u} + s_{o}^{o}g_{o}^{o} + s_{\varnothing}^{o}g_{\varnothing}^{o}\right) \\ &- \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{e} - \zeta)g_{e,\varnothing}^{e}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{e,\varnothing}^{e}\right]. \end{split} \tag{B16}$$

There are mainly three differences between Eqs. (B15) and (B16). One is that the flows of those that become eligible for unemployment insurance are reversed. The other two are related to flows from nonemployment. Whereas those claiming unemployment insurance (UI) remain eligible for UI as soon as they find jobs, the unemployed that do not claim UI must start employment without that eligibility. A fraction  $\psi_e$  of the latter group move to the state  $(a, n^e, b^e_{\varnothing}, z, \zeta)$  when they find jobs. Finally, those OLF that find jobs are never eligible for UI and, again, a fraction  $\psi_e$  of them move to the state  $(a, n^e, b^e_{\varnothing}, z, \zeta)$  when they do.

The last two KFEs for employed consumers are for those that do not claim employed benefits whether or not eligible for UI. The KFEs are, respectively:

$$\partial_{t}g_{\varnothing,ui}^{e} = -\partial_{a}\left[\dot{a}_{\varnothing,ui}^{e}g_{\varnothing,ui}^{e}\right] - \left[m_{eu}^{z} + m_{eo}^{z}\right]g_{\varnothing,ui}^{e}$$

$$+s_{ui}^{u}f(z,\zeta)(1-\psi_{e})g_{ui}^{u} + p_{ui}^{e}g_{\varnothing,\varnothing}^{e}$$

$$-\partial_{\zeta}\left[\theta_{\zeta}(\zeta_{e}-\zeta)g_{\varnothing,ui}^{e}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{\varnothing,ui}^{e}\right],$$

$$\partial_{t}g_{\varnothing,\varnothing}^{e} = -\partial_{a}\left[\dot{a}_{\varnothing,\varnothing}^{e}g_{e,\varnothing}^{e}\right] - \left[m_{eu}^{z} + m_{eo}^{z} + p_{ui}^{e}\right]g_{\varnothing,\varnothing}^{e}$$

$$+(1-\psi_{e})f(z,\zeta)\left(s_{u}^{u}g_{u}^{u} + s_{\varnothing}^{u}g_{\varnothing}^{u} + s_{o}^{o}g_{o}^{o} + s_{o}^{o}g_{\varnothing}^{o}\right)$$
(B18)

The only relevant difference between these last two equations and Eqs. (B15) and (B16) is the separation between those who claim and those who do not claim employed benefits.

 $-\partial_{\zeta}\left[\theta_{\zeta}(\zeta_{e}-\zeta)g_{\varnothing,\varnothing}^{e}\right]+\frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{\varnothing,\varnothing}^{e}\right].$ 

The KFEs of unemployed consumers that claim other unemployed benefits or claim no benefits are:

$$\partial_{t}g_{u}^{u} = -\partial_{a}\left[\dot{a}_{u}^{u}g_{u}^{u}\right] - \left[s_{u}^{u}f(z,\zeta) + m_{uo}^{z}\right]g_{u}^{u}$$

$$+\psi_{u}\left[p_{ui}^{u}g_{ui}^{u} + m_{eu}^{z}\left(g_{e,\varnothing}^{e} + g_{\varnothing,\varnothing}^{e}\right) + m_{ou}^{z}\left(g_{o}^{o} + g_{\varnothing}^{o}\right)\right] \qquad (B19)$$

$$-\partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{u}^{u}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{u}^{u}\right],$$

$$\partial_{t}g_{\varnothing}^{u} = -\partial_{a}\left[\dot{a}_{\varnothing}^{u}g_{\varnothing}^{u}\right] - \left[s_{\varnothing}^{u}f(z,\zeta) + m_{uo}^{z}\right]g_{\varnothing}^{u}$$

$$+(1 - \psi_{u})\left[p_{ui}^{u}g_{ui}^{u} + m_{eu}^{z}\left(g_{e,\varnothing}^{e} + g_{\varnothing,\varnothing}^{e}\right) + m_{ou}^{z}\left(g_{o}^{o} + g_{\varnothing}^{o}\right)\right] \qquad (B20)$$

$$-\partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{\varnothing}^{u}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{\varnothing}^{u}\right].$$

These two equations only differentiate between those who claim and those who do not claim other unemployed benefits. They are both affected by savings, flows to other labor market states, flows from those who lose eligibility for UI, flows from other labor market states, and changes in stochastic human capital.

Finally, the KFE for OLF consumers are

$$\begin{split} \partial_{t}g_{o}^{o} &= -\partial_{a}\left[\dot{a}_{o}^{o}g_{o}^{o}\right] - \left[s_{o}^{o}f(z,\zeta) + m_{ou}^{z}\right]g_{o}^{o} \\ &+ \psi_{o}\left[m_{eo}^{z}\left(g_{e,ui}^{e} + g_{\varnothing,ui}^{e} + g_{e,\varnothing}^{e} + g_{\varnothing,\varnothing}^{e}\right) + m_{uo}^{z}\left(g_{ui}^{u} + g_{u}^{u} + g_{\varnothing}^{u}\right)\right] \\ &- \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{o}^{o}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{o}^{o}\right], \end{split} \tag{B21}$$

$$\begin{split} \partial_{t}g_{\varnothing}^{o} &= -\partial_{a}\left[\dot{a}_{\varnothing}^{o}g_{\varnothing}^{o}\right] - \left[s_{\varnothing}^{o}f(z,\zeta) + m_{ou}^{z}\right]g_{\varnothing}^{o} \\ &+ (1 - \psi_{o})\left[m_{eo}^{z}\left(g_{e,ui}^{e} + g_{\varnothing,ui}^{e} + g_{e,\varnothing}^{e} + g_{\varnothing,\varnothing}^{e}\right) + m_{uo}^{z}\left(g_{ui}^{u} + g_{u}^{u} + g_{\varnothing}^{u}\right)\right] \\ &- \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{\varnothing}^{o}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{2}\left[\sigma_{\zeta}^{2}g_{\varnothing}^{o}\right]. \end{split} \tag{B22}$$

These two equations only differentiate between those who claim and those who do not claim OLF benefits. They are both affected by savings, flows to other labor market states, flows from other labor market states, and changes in stochastic human capital.

For completeness, we reproduce the density function of unemployed consumers receiving unemployment insurance found in the main text:

$$\begin{split} \partial_{t}g_{ui}^{u} &= -\partial_{a}\left[\dot{a}_{ui}^{u}g_{ui}^{u}\right] - \left[s_{ui}^{u}f(z,\zeta) + p_{ui}^{u} + m_{uo}^{z}\right]g_{ui}^{u} \\ &+ m_{eu}^{z}\left(g_{e,ui}^{e} + g_{\varnothing,ui}^{e}\right) - \partial_{\zeta}\left[\theta_{\zeta}(\zeta_{o} - \zeta)g_{ui}^{u}\right] + \frac{1}{2}\partial_{\zeta\zeta}^{z}\left[\sigma_{\zeta}^{z}g_{ui}^{u}\right], \end{split} \tag{B23}$$

#### **B.5** Stationary Equilibrium: Definition

The stationary equilibrium is composed of a set of prices  $\{r, p_L, w(a, b, z, \zeta)\}$ , controls  $\{c(a, n, b, z, \zeta), s(a, n, b, z, \zeta)\}$ , value functions  $\{V(a, n, b, z, \zeta), J(a, b, z, \zeta)\}$ , quantities  $\{K, L, \Omega, U(z, \zeta), f(z, \zeta), q(z, \zeta)\}$ , labor market tightness  $\theta(z, \zeta)$ , and density function  $g(a, n, b, z, \zeta)$  such that:

- 1. The value function  $W(a, n, b, z, \zeta)$  and the controls satisfy the maximization problems in Eqs. (11) and (B1-B8).
- 2. The value function  $J(a, b, z, \zeta)$  satisfies Eqs. (10) and (B10).
- 3. Factor prices r and  $p_L$  equal the marginal products of capital and labor for final-good producers.
- 4. The wage function agrees with the solutions to Kalai's bargaining in Eqs. (B11-B14).

- 5. The density function satisfies Eqs. (14), (B15-B22) and  $\partial_t g(a, n, b, z, \zeta) = 0$ .
- 6. The value of firms  $\Omega$  satisfies Eq. (16).
- 7. The markets for assets, labor services, and vacancies clear, i.e., Eqs. (15), (17), and (18) are satisfied.
- 8. (a) In the benchmark, government spending G guarantees a balanced budget in line with Eq. (9).
  - (b) In the experiments, the level of labor income taxes  $\tau_n$  guarantees a balanced budget in line with Eq. (9).

#### **B.6** Welfare Measure

We measure the welfare change if the economy is reformed from benchmark regime B to an alternative regime A by computing the required variation in lifetime consumption that would be just enough for each consumer to prefer regime A to B. In particular, we define

$$W^{B}(a, n, b, z, \zeta, \lambda) \equiv \mathbb{E}_{0} \int_{0}^{\infty} e^{-\rho_{z} t} u((1 + \lambda) c(a, n, b, z, \zeta)) dt,$$

where  $\lambda$  is a permanent relative change to consumption. Then, we find  $\lambda$  for each consumer such that

$$W^{B}(a, n, b, z, \zeta, \lambda) = W^{A}(a, n, b, z, \zeta)$$
 (B24)

If  $\lambda > 0$ , the policy increases the consumer's welfare. Accordingly, we compute the aggregate consumption equivalent variation (CEV) using:

$$\sum_{z} \sum_{b} \sum_{n} \int_{\zeta}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} W^{B}(a, n, b, z, \zeta, \lambda) g^{B}(a, n, b, z, \zeta) dad\zeta = 
\sum_{z} \sum_{b} \sum_{n} \int_{\zeta}^{\bar{\zeta}} \int_{\underline{a}}^{\infty} W^{A}(a, n, b, z, \zeta) g^{B}(a, n, b, z, \zeta) dad\zeta,$$
(B25)

where  $g^B(\cdot)$  corresponds to the equilibrium density function in the benchmark and  $\lambda$  measures the CEV that equals both sides.

When accounting for the transition between steady-states (Appendix D.3), we replace  $W^A(a, n, b, z, \zeta)$  with the value function upon impact. There is little difference between the value function with a UBI upon impact and in the long run. So, our measure of CEV for the steady-state is very close to that of the transition in Appendix D.3.

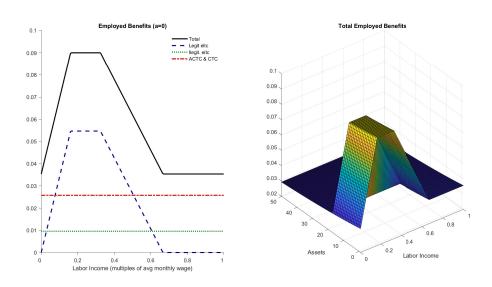
## C Internal Validation

This Appendix offers insight into how well our model matches the empirical targets.

Table C1: Summary of Internal Validation I

	Data/Target	Model
Unemployed Job-finding rate		
College	27.00	27.09
Some College	25.90	26.00
High School	24.80	24.95
Less than High School	23.90	23.94
OLF Job-finding rate		
College	5.38	5.37
Some College	4.42	4.40
High School	3.38	3.36
Less than High School	2.23	2.23
Skill Premium		
College Vs Some College	1.67	1.67
Some College Vs High School	1.14	1.14
High School Vs Less High School	1.40	1.40
Mean Wealth Ratio		
Mean Wealth Ratio C-SC	4.04	4.04
Mean Wealth Ratio C-HS	4.98	4.98
Mean Wealth Ratio C-LHS	11.03	11.03
Investment		
I/Y	23.00	23.00
Annualized return on capital	4.00	4.00

Figure C1: Employed Benefits Structure



*Note:* The left panel shows how the total and the three components of employed benefits change with labor income for consumers with zero assets. The right panel shows how total employed benefits change with assets and labor income. The fall of illegitimate transfers with assets drives the curvature seen on the right panel for given income.

Table C2: Summary of Internal Validation II

	Data	Model
Employed benefits		
Total Transfers	1.46	1.46
Illeg. Transfers	0.20	0.20
Recipients (%)	20.24	20.24
Share Recipients LHS	39.80	39.80
Share Recipients HS	24.86	24.86
Share Recipients SC	25.08	25.08
Unemployment Insurance		
Total Transfers	0.25	0.25
Illeg. Transfers	0.02	0.02
Recipiency Rate LHS	13.25	13.25
Recipiency Rate HS	23.19	23.19
Recipiency Rate SC	24.85	24.85
Recipiency Rate C	38.10	38.10
Other Unemployed Benefits		
Total Transfers	0.06	0.06
Illeg. Transfers	0.00	0.00
Recipiency Rate LHS	24.64	24.64
Recipiency Rate HS	20.87	20.87
Recipiency Rate SC	23.67	23.67
Recipiency Rate C	8.92	8.92
OLF Benefits		
Total Transfers	0.67	0.67
Illeg. Transfers	0.05	0.05
Recipiency Rate LHS	37.05	37.05
Recipiency Rate HS	27.25	27.25
Recipiency Rate SC	23.84	23.84
Recipiency Rate C	8.80	8.80

*Note:* This table contrasts moments in the data with the equivalents in the model. Recipiency rates are expressed as a fraction of those in the respective labor market state. The share of recipients of employed benefits is the recipiency rate of employed benefits of consumers of a given level of education divided by the recipiency rates for all levels of education.

## D Further Results

#### D.1 External Validation: Comparison with Ganong and Noel (2019)

We use home production to target the fall in consumption of UI recipients observed on the month of the first UI payment, as estimated in Ganong and Noel (2019). Their data, however, offers a detailed pattern of the consumption behavior of UI recipients throughout the unemployment spell. We produce a model counterpart by (i) simulating the path of consumption for those who become unemployed and recipients of UI and (ii) restricting our attention to those who remain recipients of UI for six months and lose recipiency immediately after. We compare the two in Figure D1.

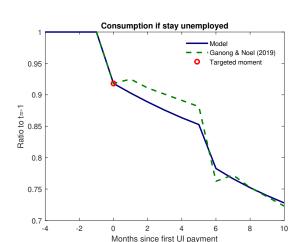


Figure D1: Comparison of model with estimates in Ganong and Noel (2019)

#### D.2 Robustness to Alternative Calibrations

To gauge the robustness of our main results, we studied several alternative calibration choices, that we discuss below. We summarize the findings in Table D1. This table shows the CEV for the baseline level of UBI in the upper panel and the threshold UBI (the level above which the CEV becomes positive) in the lower panel. Regardless of the calibration choice, there is always a threshold above which an expenditure-neutral UBI increases welfare for all education groups. Moreover, barring an implausibly extreme scenario for the claim rates, the thresholds are close to those in the benchmark. It is also noteworthy that they are much smaller than the UBI proposed by Andrew Yang and others.

- In the benchmark calibration, we assume that the home production function is  $h(z,\zeta) = h^{\nu}(y_ze^{\zeta})p_L$ , i.e., that home production is proportionate to market production. We now posit instead that  $h(z,\zeta) = h^f + h^{\nu}(y_ze^{\zeta})p_L$ , where  $h^f = 0.025$  measures fixed home production, while  $h^{\nu}$  remains calibrated to match the fall in consumption of UI recipients ( $h^{\nu} = 0.113$ , contrasting with  $h^{\nu} = 0.173$  in the benchmark calibration). This alternative calibration leads to higher home production for the least productive (typically less educated), and lower for the rest. Proposition 2 of Section 2 indicates that replacing the conditional welfare system with a UBI should be less appealing to those with higher home production, as a higher endowment protects against the imperfections of conditional programs. This is what we report in Table D1: the CEV of introducing a UBI falls for those with high school or less, and rises for the rest. The threshold UBI increases by about 500 USD for those with less than high school and by about 100 USD in the aggregate.
- SNAP and SSI eligibility typically requires that recipients have less than 3000 USD in assets. Yet,

Table D1: Summary of Robustness Checks

	CEV Baseline UBI				
	Agg.	LHS	HS	SC	C
Benchmark Calibration	-0.73	-1.35	-1.38	-1.83	0.20
Fixed Home Production	-0.76	-1.93	-1.48	-1.78	0.25
High Asset Limit $B_u \& B_o$	-0.67	-2.01	-1.16	-1.62	0.18
Low Asset Limit B <sub>e</sub>	-0.75	-1.26	-1.33	-1.81	0.11
Benchmark Cal.+TANF	-0.62	-0.85	-1.15	-1.74	0.22
Much Higher Claim Rates	-2.05	-5.61	-3.78	-2.96	-0.27
Lower Claim Rates	-0.39	-0.73	-1.00	-1.37	0.42
	Threshold UBI				
	Agg.	LHS	HS	SC	C
Benchmark Calibration	~2148	~2165	~2168	~2867	<815
Fixed Home Production	~2251	~2636	~2296	~2958	<815
High Asset Limit $B_u \& B_o$	~2181	~2714	~2106	~2838	<815
Low Asset Limit $B_e$	~2168	~2107	~2126	~2825	~1041
Benchmark Cal.+TANF	~2104	~1965	~2112	~2816	<840
Much Higher Claim Rates	~3902	~4236	~4035	~4390	~2568
Lower Claim Rates	~1791	~1799	~1951	~2426	<815

such restrictions vary by state and have numerous exceptions. As an alternative calibration, we increase the asset limit of other unemployed and OLF benefits to 10000 USD. We also restrict our attention to a wider group of households in SIPP data, which implies that our claim rates  $\psi_u^z$  and  $\psi_o^z$  target higher recipiency rates. We find that the least educated are the most sensitive to this change. Still, the effects are overall small, especially in the aggregate.

- The maximum return on capital compatible with EITC eligibility is 3500 USD, which we target in our benchmark calibration. Yet, this maximum is set for the household, irrespective of composition. We therefore consider an alternative in which we limit the maximum return on capital to 2625. We find that this increases the claim rates of all education groups, but especially of those with a college education, the most likely to be married in the data. This alternative has little effect in the aggregate. In the benchmark system, it benefits those with a college education at the expense of everyone else.
- In our benchmark calibration, we do not consider the *Temporary Assistance for Needy Families* (TANF). This program offers training and other forms of assistance to needy families, including transfers. It is intended to promote employment. As an alternative calibration, we increase employed benefits by 8 Bn USD. This change slightly increases the benefit of introducing a UBI for all education groups, with a disproportionate effect on the least educated.
- We consider an extreme alternative calibration for the claim rates of other unemployed and OLF benefits. In this alternative, we do not restrict our attention to those with low earnings or

low assets in SIPP data. Instead, we impose that recipients with high assets or earnings in the data also correspond to poor nonemployed consumers in the model. The targeted recipiency rates are at least 50% higher, and usually double, those in the benchmark. Hence, claim rates  $\psi^z_u$  and  $\psi^z_o$  are substantially higher. As this implies a far less imperfect conditional welfare system, an expenditure-neutral UBI would lead to large welfare losses. Yet, even in this extreme case, if the welfare system were generous enough, a UBI would still be welfare increasing. The thresholds are about double those in the benchmark but still far lower than the 12000 USD proposed by Andrew Yang.

• The empirical recipiency rates of other unemployed and OLF benefits targeted in the benchmark calibration are those of SNAP and SSI rescaled by the proportion of those that are employed and satisfy the asset and earnings restrictions. We do this because a few SNAP and SSI recipients are employed in practice, but we assume that they are nonemployed in the model. In this robustness check, we do not rescale the recipiency rates. Evidently, the claim rates fall in this case, implying a more imperfect benchmark welfare system. This leads to a substantial reduction in the costs of introducing a UBI and also a meaningful fall in the threshold UBI.

## **D.3** Robustness to Transitional Dynamics

In this section, we look at the transitional dynamics from the moment that the expenditure-neutral UBI is unexpectedly introduced. To do so, we must consider that prices,  $\{r_t, p_{L,t}, w_t(a,b,z,\zeta)\}$ , and quantities,  $\{K_t, L_t, \Omega_t, U_t(z,\zeta), f_t(z,\zeta), q_t(z,\zeta)\}$ , change over time. Moreover, the value functions,  $W(\cdot)$  and  $J(\cdot)$  also change over time, which implies that we must add the terms  $\partial_t W_t(a,n,b,z,\zeta)$  and  $\partial_t J_t(a,b,z,\zeta)$  to the respective equations for all  $(a,n,b,z,\zeta)$ . Again, we follow Achdou et al. (2021) in building the algorithm. However, we face the additional challenge that the value of firms jumps as the change is introduced. We handle this by using interpolation and adjusting the density functions of those with assets close to the maximum so that the aggregate capital stock is unchanged when the UBI is introduced.

Table D2 shows that accounting for the transition between steady-states has a negligible effect on our conclusions. The welfare effects of the policy upon impact and in the long-run are almost indistinguishable.

### **D.4** Other Tables and Figures

Table D2: Welfare Impact: Transition vs Long Run

	Aggregate	LHS	HS	SC	С
CEV Steady-state	-0.73	-1.35	-1.38	-1.83	0.20
<b>CEV Transition</b>	-0.72	-1.39	-1.38	-1.81	0.22

*Note:* This table reports the consumption-equivalent variation (welfare change, CEV) in the aggregate and decomposed by levels of education of our UBI experiment. The first line reports the CEV when we only compare the long-run values in both welfare systems. The second line reports the CEV when we compare the long-run values in the benchmark system with those immediately upon the introduction of a UBI.

Table D3: Inequality

	Earnings		Wealth	1
	Benchmark	UBI	Benchmark	UBI
Q1	1.30	1.43	-0.79	-0.69
Q2	4.74	4.88	0.76	1.92
Q3	10.47	10.54	5.31	6.90
Q4	21.39	21.32	16.63	17.59
_Q5	62.11	61.83	78.09	74.30

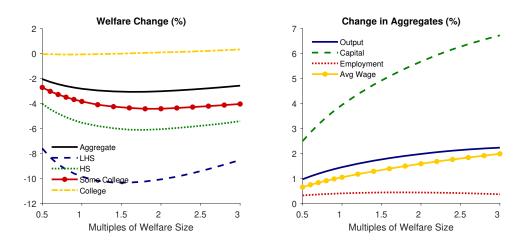
*Note:* This table contrasts the five quintiles of the earnings and wealth distributions implied by the model with the benchmark welfare system and the model with an expenditure-neutral UBI.

**Table D4:** Welfare impact of replacing improved welfare systems with a UBI

	Benchmark	No Illeg. Transfers	No Admin	100% Take-up	Perfect
CEV Aggregate	-0.73	-0.74	-1.12	-2.83	-3.51
CEV LHS	-1.35	-1.48	-2.55	-9.87	-11.73
CEV HS	-1.38	-1.33	-2.01	-5.55	-6.67
CEV SC	-1.83	-1.81	-2.29	-3.84	-4.69
CEV C	0.20	0.17	0.06	-0.07	-0.28

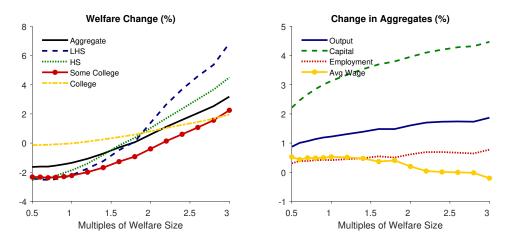
*Note:* This table shows the consumption-equivalent variation (welfare change) of replacing different welfare systems with an expenditure-neutral UBI. The first column repeats the benchmark results for convenience. The next three columns report the welfare consequences of replacing a system that transfers the same total amount but is free of one kind of imperfection. The last column that of replacing a welfare system without any such imperfections. The first line reports the average CEV, while the other lines decompose it by level of education.

Figure D2: Replacing Welfare Systems with Complete Take-up and of Various Scales with a UBI



*Note:* This figure shows the results of repeating the experiments in Figure 1, only now abstracting from incomplete take-up. The scale of the welfare system (x-axis) goes from half to three times the benchmark size. A scale of one delivers the same results as in the second rightmost column of Table D4. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in average gross wage.

**Figure D3:** Replacing Welfare Systems of Various Scales without Administrative Costs and Illegitimate Transfers with a UBI



*Note:* This figure shows the results of repeating the experiments in Figure 1, only now abstracting from administrative costs and illegitimate transfers. The scale of the welfare system (x-axis) goes from half to three times the benchmark size. The left panel reports the average consumption-equivalent variation for all consumers and consumers grouped by education. The right panel reports changes in indicators of economic activity and in average gross wage.