

# Ven der Giessen's reordering algorithm in the program for stochastic simulation of econometric models

Bianchi, Carlo and Calzolari, Giorgio and Doret, Remi IBM Scientific Center, Pisa, Italy

December 1978

Online at https://mpra.ub.uni-muenchen.de/24880/MPRA Paper No. 24880, posted 19 Oct 2010 08:07 UTC

IBM Italy PISA SCIENTIFIC CENTER Z513-5101 December 1978

# VAN DER GIESSEN'S REORDERING ALGORITHM IN THE PROGRAM FOR STOCHASTIC SIMULATION OF ECONOMETRIC MODELS

Carlo Bianchi

IBM Pisa Scientific Center

Giorgio Calzolari IBM Pisa Scientific Center-

Rémi Doret

Student at the «Institut National Polytechnique», Grenoble

IBM Scientific Center Via S. Maria 67 56100 Pisa, Italy

IBM internal use only



This paper describes the application of a reordering algorithm to the equations of econometric models. The algorithm was proposed in 1970 by Van der Giessen [5] and is here applied to the equation format required by the program for stochastic simulation developed at the IBM Scientific Center in Pisa [1], [2].



# CONTENTS

1. INTRODUCTIONp. 7
2. INPUT REQUIREMENTS AND EXECUTION PROCEDURE
2.1. Input data set
2.2. Execution procedure and example of input data set:
the Klein-Goldberger modelp. 9
2.3. The output data setp.11
2.4. Example of output data set:
the reordered Klein-Goldberger modelp.12
3. PERFORMANCESp.14
4, THE PL/1 PROGRAMp.15
4.1. A simplified flow-chartp,16
4.2. Program listingp.18
REFERENCESp.26

#### 1. INTRODUCTION

The program for stochastic simulation of econometric models proposed in [1] uses the Gauss-Seidel solution algorithm, but does not perform any reordering of the model's equations [2,p.8].

In this paper a program to reorder the equations is proposed. It must be used as a pre-processor; its input data set is the card deck (or disk file) containing the equations of the model, as described in [2,pp.8-9]; the output is a new card deck (or disk file) containing the same equations in a new order. The output data set must then be compiled and successively used as in [2].

The input requirements and the execution procedure are described in some details in section (2.), together with an example on the Klein-Goldberger model. A short comment on the performances of the algorithm is given in section (3.).

Details on the algorithm can be found in the paper by Van der Giessen [5]. In any case, several comment lines are inserted in the PL/1 program, whose listing is printed in section (4.2.), after a simplified flow-chart.

#### 2. INPUT REQUIREMENTS AND EXECUTION PROCEDURE

#### 2.1. Input data set

It is a card image file.

Cards must be written in a standard FORTRAN code; in particular:

- FORTRAN statements must be written one per card within columns 7 through 72.
- A statement may be continued on successive cards (up to 19) by placing any character other than blank in column 6 of each continuation card.
- On the first card of a statement column 6 must be blank.
- ~ For comments, the character C is placed in column 1.

## \*\* Statements allowed

- Statements of the form:

```
Y(p) = F(Y(1), ..., Y(n), ...)
```

From now on these statements will be called equations. The subscript of an equation is the first number in parentheses (here p).

The subscript of the variable Y(n) is n.

### - IF statements

IF (test) followed by an equation

For example:

IF(Y(7).GT.Y(10))Y(7)=Y(10)

The subscript of the IF statement is the subscript of the equation.

#### \*\* Other requirements

- Variables to be ordered are always of the form Y(...).

  Their subscripts form a sequence 1,2,3,...,n with n up to 500.
- Other character strings including 'Y' in their expressions may be used in the

data.

- Blanks may be present everywhere in a card (except in column 7 for statements).
- There are no restrictions about the number of comment cards.
- Several equations and IF statements may have the same subscript.

# 2.2. Execution procedure and example of input data set:

the Klein-Goldberger model

In this section the FORTRAN code for the Klein-Goldberger revised model (4) is displayed according to the format in [2,pp.8-9]. This card-image data set is the 12-th file on the tape whose contents are described in [2].

```
SUBROUTINE MODEL (Y, X, NEXO, IREAD, IC, YL, NEND, UMC, A)
                                                                              KLE00010
      IMPLICIT REAL*8 (A-H,O-2)
                                                                              KLE00020
                                                                              KLE00030
      DIMENSION Y(1), X(NEXO, IREAD), YL(NEND, IREAD), UMC(1), A(1)
                                                                              KLE00040
   MODEL KLEIN-GOLDBERGER ECONOMETRICA , 1969, APRIL
                                                                              RLE00050
                                                                              KLE00060
CCC
   MEANING OF ENDOGENOUS VARIABLES Y(I)
                                                                              KLE00070
                                                                              KLE00080
   Y(1) = CD
                                                                               KLE00090
   Y(2) = CN
Y(3) = RR
Y(4) = HB
CCCC
                                                                              KLE00100
                                                                               KLE00110
                                                                               KLE00120
   Y(5) = IM
                                                                               KLE00130
С
   Y(6) = X
                                                                              KLE00140
С
   Y(7) = H
                                                                               KLE00150
C
   Y(8) = WW
                                                                               KLE00160
   Y(9) = W
                                                                               KLE00170
   Y(10) = R
                                                                               KLE00180
   Y(11) = I
                                                                               KLE00190
   Y(12) = D
                                                                               KFE00500
   Y(13) = RS
                                                                               KLE00210
   Y(14) - PC
                                                                              KLE00220
C
   Y(15) = NW
                                                                              KLE00230
C
   Y(16) = Y
                                                                              KLE00240
С
   Y(17) = P
                                                                               KLE00250
C
   Y(18) = SC
                                                                               KLE00260
С
   Y(19) = PGR
                                                                              KLE00270
   Y (20) - PGRR
C
                                                                              KLE00280
                                                                              KLE00290
  MEANING OF EXOGENOUS VARIABLES X(I,IC)
                                                                              KLE00300
                                                                              KLE00310
   X(1, IC) = WG
CCC
                                                                              KLE00320
   X(2,IC) = PM
                                                                              KLE00330
  X(3,1C) = NG
                                                                              KLE00340
   X(4,IC) = NS
C
                                                                              KLE00350
   X(5,IC) = NL
                                                                              KLE00360
                                                                              KLE00370
C
   X(6,IC) = TC
   X(7, IC) - DU
                                                                              KLE00380
   X(\theta,IC) = RD
                                                                              KLE00390
  X(9,IC) = RB-1 (ONLY LAGGED IN THE MODEL)

X(10,IC) = G+B
                                                                              KLE00400
                                                                              KLE00410
C \times (11, IC) = TI
                                                                              KLE00420
```

```
X(12,IC) = T
                                                                                          KLE00430
   X(13,IC) = SUM
                                                                                          KLE00440
   X(14,IC) = CONSTANT
                                                                                          KLE00450
                                                                                          KLE00460
   INVESTMENT FUNCTION (NONRESIDENTIAL)
                                                                                          KLE00470
                                                   3.14
C
      X(11)=.95*YL(11,IC-1)+A(44)*(YL(6,IC-1)-X(1,IC-1))+
-A(45)*YL(10,IC-1)+A(46)*YL(11,IC-1)+A(47)*X(14,IC)+UMC(14)
                                                                                          KLE00480
                                                                                          KLE00490
  DEPRECIATION EQUATION 3.15
                                                                                          KLE00500
C
       Y(12) = A(48) *X(13, IC) + A(49) *X(7, IC) + A(50) *X(14, IC) + UMC(15)
                                                                                          KLR00510
   INTEREST RATE DETERMINATION EQUATION 3.16
                                                                                          KLE00520
       Y(13) = A(51) *X(0,IC) + A(52) *X(9,IC) + A(53) *X(7,IC) +
                                                                                          KLE00530
      -A(54)*X(14,IC)+UMC(16)
                                                                                          KLE00540
  INTEREST RATE STRUCTURE EQUATION 3.10
C
                                                                                          KLE00550
       Y(10) = A(31) + Y(13) + A(32) + YL(10, IC-1) + A(33) + X(14, IC) + UMC(10)
                                                                                          KLE00560
   NATIONAL INCOME NATIONAL PRODUCT IDENTITY 3.18. EXPLIC IN Y
Y(16) = (Y(17) *Y(6) - Y(12) - X(11, IC) - Y(17) *Y(18) -
\mathbf{C}
                                                                                          KLE00570
                                                                                          KLE00580
      -x(6,ic)-x(12,ic))/y(17)
                                                                                          KLE00590
                                                                                          KLE00600
   CONSUMPTION FUNCTION (DURABLES)
       Y(1) = A(1) * (Y(16) - .7*YL(16, IC-1)) + (.7+A(2)) *YL(1, IC-1) + A(3)
                                                                                          KLE00610
      - * x (14, IC) + UMC (1)
                                                                                          KLE00620
  CONSUMPTION FUNCTION (NONDURABLES) 3.2
                                                                                          KLE00630
       Y(2) = A(4) *Y(16) + A(5) *YL(2,IC-1) + A(6) *X(14,IC) + UMC(2)
                                                                                          KLE00640
   INVESTMENT FUNCTION (RESIDENTIAL) 3.3
                                                                                          KLE00650
       Y(3) = A(7) + Y(16) + A(8) + YL(10, IC-1) + A(9) + YL(3, IC-1) + A(10) + X(14, IC)
                                                                                          KLE00660
      -+UMC(3)
                                                                                          KLE00670
   INVESTMENT FUNCTION (INVENTORIES) SCALED BY 10. NORMALIZED FOR H 3.4KLE00680
       Y(4) = (A(11)/10.*(Y(6)-10.*(-YL(4,IC-1)))+A(12)*YL(4,IC-1)
                                                                                          KLE00690
       +A(13)/10*X(14,IC)+UMC(4)/10.)/(1.+A(11))
                                                                                          KLE00700
   IMPORT DEMAND FUNCTION 3.5
                                                                                          KLE00710
       Y(5) = A(14) * Y(6) + A(15) * (X(2,IC) - Y(17)) + A(16) * YL(5,IC-1) +
                                                                                          KLE00720
       -A(17)*X(14,IC)+UMC(5)
                                                                                          KLE00730
  DEFINITION OF REAL GNP
                                 3.17
                                                                                          KLE00740
С
       Y(6) = (Y(1) + Y(2) + Y(11) + Y(3)
                                                                                          KLE00750
      -+10.*(Y(4)-YL(4,IC-1))
                                                                                          KLE00760
      -+x(10,IC)-Y(5)
                                                                                          KLR00770
   PRODUCTION FUNCTION WITH SCALING BY 100 IN H. EXPLIC. FOR NW 3.6 (THE FACTOR 0.230 HAS BEEN EMPIRICALLY CHOSEN FOR CONVERGENCE).
                                                                                          KLEOD 780
                                                                                          KLE00790
       Y(15) = Y(15) + 0.230
                                                                                          KIEDOROO
      -(Y(6)-(X(1,IC)+.95*(YL(6,IC-1)-X(1,IC-1))+A(18)*(Y(11)+Y(3))
                                                                                          KLE00810
      -+A(19)*((Y(15)-X(3,IC)+X(4,IC))-.95*(YL(15,IC-1)-X(3,IC-1)
-+X(4,IC-1)))+A(20)/100.*(Y(7)-.95*YL(7,IC-1))+A(21)*X(14,IC)+
                                                                                          KLE00820
                                                                                          KLE00830
      -UMC(6)))
                                                                                          KLE00840
C HOURS WORKED FUNCTION SCALED BY 100.
                                                                                          KLE00850
      Y(7) \Rightarrow A(22) * 100. * (Y(9) - YL(9, IC-1)) + A(23) * 100. * (X(5, IC) - Y(15) - X(4, ICKLE00860 - 1)) + A(24) * 100. * X(14, IC) + UMC(7) * 100. * XLE00870
  LABOR DEMAND FUNCTION (WAGE SHARE) 3.8 Y(8) = X(1, IC) + A(25) * (Y(6) - X(1, IC)) + A(26) * (YL(8, IC-1) - X(1, IC-1))
C
                                                                                          KLE00880
                                                                                          KLE00890
      -+A(27)*X(14,IC)+UMC(8)
                                                                                          KLE00900
   WAGE RATE DETERMINATION EQUATION 3.9
                                                                                          KLE00910
       Y(9)=YL(9,IC-1)+A(28)+(X(5,IC)-Y(15)-X(4,IC))+
                                                                                          KLE00920
      -A(29)*(YL(17,IC-1)-YL(17,IC-2))+A(30)*X(14,IC)+UMC(9)
                                                                                          KLE00930
   WAGE IDENTITY NORMALIZED FOR P 3.20
                                                                                          KLE00940
       Y(17) = Y(7) + Y(9) + Y(15) / Y(8) / 100.
                                                                                          KT-E00950
   CORPORATE SAVINGS FUNCTION SCALED BY 10.
                                                        3.11. EXPLIC. IN SC
                                                                                          KLE00960
      Y(18) = (A(34) * (Y(17) *Y(14) - X(6,IC)) + A(35) * (YL(17,IC-1) *YL(14,IC-1) *KLE00970 - X(6,IC-1) - YL(17,IC-1) *YL(18,IC-1)) + A(36) *X(14,IC) + UMC(11)) / KLE00980
      -Y(17)
                                                                                          KLE00990
  RENTIER INCOME EQUATION 3.13. EXPLIC IN PGRR
                                                                                          KLE01000
       Y(20) = (A(40) + Y(17) + (Y(11) + Y(3)) + A(41) + (Y(10) - YL(10, IC-1))
                                                                                          KLE01010
  1(20)=(A(40)+1(+7)+(1(+7)+1(3))+A(41)+(1(10)-1L(10,1C-1))
-+A(42)*YL(20,IC-1)*YL(17,IC-1)+A(43)*X(14,IC)+UMC(13))/Y(17)
DEFINITION OF PROFIT 3.19. EXPLIC. IN PGR
Y(19)=(Y(17)*Y(6)-Y(12)-X(11,IC)-Y(17)*Y(8)-Y(20)*Y(17))/Y(17)
                                                                                          KLE01020
                                                                                          KLE01030
                                                                                          KLED1040
  NONCORPORATE INCOME EQUATION 3.12, EXPLIC. IN PC Y(14)=Y(19)-10./Y(17)*
                                                                                          KLE01050
                                                                                          KLE01060
      -(A(37)/10.*Y(17)*Y(6)+A(38)*(YL(19,IC-1)-YL(14,IC-1))*YL(17,IC-1)/KLE01070
      -10.
                                                                                          KLE01080
      -+A(39)/10.*X(14,IC)+UMC(12)/10.)
                                                                                          KLE01090
RETURN
                                                                                          KLE01110
       END
                                                                                          KLE01120
```

To process the reordering algorithm, first of all the first 46 cards of the data set must be dropped, stored into a separate file, as well as the RETURN and END statements. The comment card

#### C......

is mandatory at the end of the data set and must appear nowhere else.

After these preliminary operations, INPUT FORTRAN A1 must be the CMS identifier of the data set [3]; the following VANDERG EXEC procedure

FILEDEF ONE DISK INPUT FORTRAN A1 (RECFM P LRECL 80 BLOCK 80)
FILEDEF TWO DISK OUTPUT FORTRAN A1 (RECFM P LRECL 80 BLOCK 80)
GLOBAL TXTLIB PLILIB
LOAD VANDERG
START

can now be used issuing the CMS command:

vanderg

#### 2.3. The output data set

The output processing is performed by the subroutines ECRIT and IMPRIM (see section 4.). The equations are written following the sequence (put in SEQ) found by Van der Giessen's method.

All the comments preceding a statement in the input file are present in the output file immediately before the statement itself.

Several statements may have the same subscript. In the output file they are written in a block (inserted at the place indicated by SEQ). Inside the block they have the same sequence as their relative order in the input file.

The comment 'END OF RECURSIVE PART' is written after the end of the recursive equations (determined in subroutine RNG), if any.

The comment 'END OF SIMULTANEOUS PART' is put just before the beginning of the post-recursive part (if any).

For further details see the program listing (MAIN and subroutine RNG, section 4.2.).

### 2.4. Example of output data set:

#### the reordered Klein-Goldberger model

The result of the execution of the VANDERG EXEC procedure is the creation of the file whose CMS identifier is OUTPUT FORTRAN, containing the reordered equations and the corresponding comment lines as follows:

```
C INVESTMENT FUNCTION (NONRESIDENTIAL) 3.14
                                                                                               OUT 0 0 0 1 0
        Y(11) = .95*YL(11,IC-1)+A(44)*(YL(6,IC-1)-X(1,IC-1))+
                                                                                                OUT00020
       +A(45)*YL(10,IC-1)+A(46)*YL(11,IC-1)+A(47)*X(14,IC)+UMC(14)
                                                                                                OUT00030
C DEPRECIATION EQUATION 3.15
                                                                                                OUT00040
        Y(12) = A(48) *X(13, IC) + A(49) *X(7, IC) + A(50) *X(14, IC) + UMC(15)
                                                                                                OUT00050
   INTEREST RATE DETERMINATION EQUATION 3.16
                                                                                                00700060
        Y(13) = A(51) + X(8, IC) + A(52) + X(9, IC) + A(53) + X(7, IC) +
                                                                                                OUT00070
C INTEREST RATE STRUCTURE EQUATION 3.10
Y(10)=A(31)*Y(13)+A(32)*YL(10,IC-1)+A(33)*X(14,IC)+UMC(10)
C**** END OF RECURSIVE PART *****
                                                                                                00700080
                                                                                                OUT00090
                                                                                                OUT00100
                                                                                                OUT 0 0 1 1 0
   WAGE RATE DETERMINATION EQUATION 3.9
                                                                                                OUT00120
       Y(9)=YL(9,IC-1)+A(28)*(X(5,IC)-Y(15)-X(4,IC))++A(29)*(YL(17,IC-1)-YL(17,IC-2))+A(30)*X(14,IC)+UMC(9)
                                                                                                OUT00130
                                                                                                OUT00140
C HOURS WORKED FUNCTION SCALED BY 100. 3.7 OUT00150
Y(7)=A(22)*100.*(Y(9)-YL(9,IC-1))+A(23)*100.*(X(5,IC)-Y(15)-X(4,ICOUT00160)
  +))+A(24)*100.*x(14,IC)+UMC(7)*100. OUT00170
INVESTMENT FUNCTION (INVENTORIES) SCALED BY 10. NORMALIZED FOR H 3.40UT00180
C ANYESTMENT FUNCTION (INVENTORIES) SCALED BY 10. NORMALIZED FOR H
Y(4)=(A(11)/10.*(Y(6)-10.*(-YL(4,IC-1)))+A(12)*YL(4,IC-1)
++A(13)/10*X(14,IC)+UMC(4)/10.)/(1.+A(11))
C LABOR DEMAND FUNCTION (WAGE SHARE) 3.8
Y(8)=X(1,IC)+A(25)*(Y(6)-X(1,IC))+A(26)*(YL(8,IC-1)-X(1,IC-1))
++A(27)*X(14,IC)+UMC(8)
                                                                                                OUT00190
                                                                                                00700200
                                                                                                OUT00210
                                                                                                OUT00220
                                                                                                OUT00230
C WAGE IDENTITY NORMALIZED FOR P 3.20
                                                                                                OUT00240
   Y(17)=Y(7)*Y(9)*Y(15)/Y(8)/100.
IMPORT DEMAND FUNCTION 3.5
                                                                                                00700250
С
                                                                                                OUT00260
       Y(5)=A(14)*Y(6)+A(15)*(X(2,IC)-Y(17))+A(16)*YL(S,IC-1)+
+A(17)*X(14,IC)+UMC(5)
                                                                                                Ουτο0270
                                                                                                OTITOGORO
C DEPINITION OF PROFIT 3.19. EXPLIC. IN PGR
Y(19) = (Y(17) *Y(6) -Y(12) -X(11, IC) -Y(17) *Y(8) -Y(20) *Y(17))/Y(17)
                                                                                                OUT00290
                                                                                                OUT00300
C NONCORPORATE INCOME EQUATION 3.12, EXPLIC. IN Y(14)=Y(19)-10./Y(17)*
                                                                                                OUT00310
                                                                                                OUT00320
       +(A(37)/10.*Y(17)*Y(6)+A(38)*(YL(19,IC-1)-YL(14,IC-1))*YL(17,IC-1)/OUT00330
       +10.
                                                                                                OUT00340
       ++A(39)/10.*X(14,IC)+UMC(12)/10.)
                                                                                                OUT00350
C CORPORATE SAVINGS FUNCTION SCALED BY 10. 3.11. EXPLIC. IN SC OUT00360 Y(18)=(A(34)*(Y(17)*Y(14)-X(6,IC))+A(35)*(YL(17,IC-1)*YL(14,IC-1) OUT00370
       +-X(6,IC-1)-YL(17,IC-1)*YL(18,IC-1))+A(36)*X(14,IC)+UMC(11))/
                                                                                                OUT00380
       + Y (17)
                                                                                                OUT00390
C NATIONAL INCOME NATIONAL PRODUCT IDENTITY 3.18. EXPLIC IN Y
                                                                                                OUT00400
       Y(16) = (Y(17) *Y(6) - Y(12) - X(11, IC) - Y(17) *Y(18) - +X(6, IC) - X(12, IC)) /Y(17)
                                                                                                OUT00410
                                                                                                OUT00420
  CONSUMPTION FUNCTION (DURABLES) 3.1
                                                                                                OUT00430
C
        Y(1)=A(1) * (Y(16)-.7*YL(16,IC-1))+(.7+A(2))*YL(1,IC-1)+A(3)
                                                                                                OUT00440
       + *X(14, IC) +UMC(1)
                                                                                                OUT00450
   CONSUMPTION FUNCTION (NONDURABLES) 3.2
                                                                                                OUT00460
        Y(2)=A(4) + Y(16) + A(5) + YL(2, IC-1) + A(6) + X(14, IC) + UMC(2)
                                                                                               OUT00470
    INVESTMENT FUNCTION (RESIDENTIAL) 3.3
                                                                                                OUTO0480
        Y(3)=A(7)+Y(16)+A(8)+YL(10,IC-1)+A(9)+YL(3,IC-1)+A(10)+X(14,IC)
                                                                                                OUT00490
       ++UMC (3)
                                                                                                OUT00500
  DEFINITION OF REAL GNP 3.17
                                                                                                00700510
       Y(6) = (Y(1)+Y(2)+Y(11)+Y(3)
                                                                                                OUT00520
       ++10, *(Y(4)-YL(4, YC-1))
                                                                                                OUT00530
       ++X(10,IC)-Y(5))
                                                                                                OUT00540
   PRODUCTION FUNCTION WITH SCALING BY 100 IN H. EXPLIC. FOR NW 3.6
                                                                                               OUT00550
    (THE FACTOR 0.230 HAS BEEN EMPIRICALLY CHOSEN FOR CONVERGENCE).
                                                                                               00700560
```

```
Y(15)=Y(15)+0.230*
+(Y(6)-(X(1,IC)+.95*(YL(6,IC-1)-X(1,IC-1))+A(18)*(Y(11)+Y(3))
++A(19)*((Y(15)-X(3,IC)+X(4,IC))-.95*(YL(15,IC-1)-X(3,IC-1)
++X(4,IC-1)))+A(20)/100.*(Y(7)-.95*YL(7,IC-1))+A(21)*X(14,IC)+
+UMC(6)))

C RENTIER INCOME EQUATION 3.13. EXPLIC IN PGR
Y(20)=(A(40)*Y(17)*(Y(11)+Y(3))+A(41)*(Y(10)-YL(10,IC-1))
++A(42)*YL(20,IC-1)*YL(17,IC-1)+A(43)*X(14,IC)+UMC(13))/Y(17)
OUT00640
```

The heading statements previously dropped, as well as the RETURN and END statements, must be reinserted.

The data set so obtained (OUTPUT FORTRAN) must be renamed KLEINGOL FORTRAN and compiled; simulation can then be performed as in {2,p.29}.

#### 3. PERFORMANCES

The solution of the non-reordered Klein-Goldberger model for one year (for example 1965), with a relative tolerance 0.1E-06 and assuming the historical values of the endogenous variables as starting values of the Gauss-Seidel procedure, requires 42 iterations.

The solution of the model, reordered as in section (2.4.), requires 18 iterations.

The solution of the Klein-I model, as in [2,pp.8-9], at 1941 requires 25 iterations. After reordering, the same model requires 18 iterations.

The reordering of the Klein-Goldberger model requires about 8 seconds of CPU time on a computer IBM/370 model 168.

#### 4. THE PL/1 PROGRAM

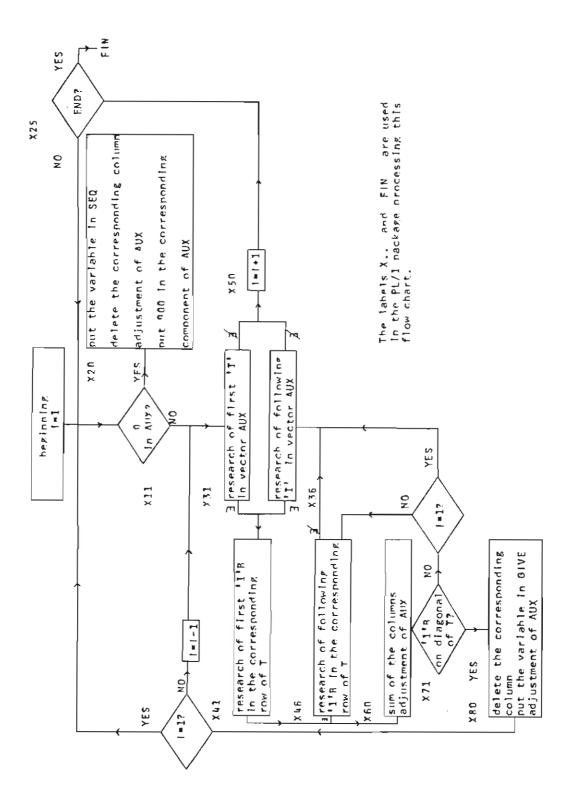
Whenever possible, within the program listing and in the flow-charts the same variables names as in Van der Giessen's paper [5] are maintained.

The program:

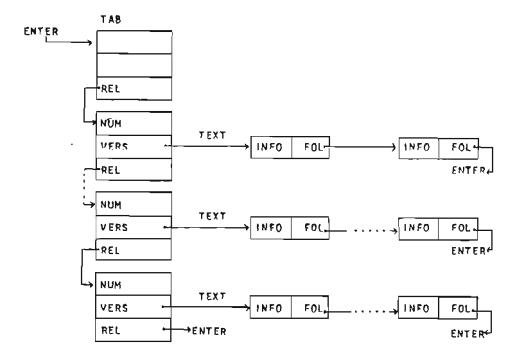
- reads the data set,
- fills the structure matrix T after a syntactic analysis (research of the sequence Y(...)) of each equation,
- stores the cards in a lists structure (see later in this paragraph),
- processes the Van der Giessen's algorithm,
- fills the output file with the new sequence.

Details about each subroutine are given in the listing of the program (see 4.2.).

# 4.1. A simplified flow-chart



In order to have a simple output processing, the cards are stored in this way (a list of lists is used):



The first element of TAB is just created to begin the main list.

In each list TEXT we have a statement (equation or IF statement) with the comment cards coming just before this statement. Each INPO contains one card of the statement. NUM is the subscript of the equation or IF statement.

If several statements have the same subscript, the corresponding row in T depends on all the variables found in all the statements.

#### 4.2. Program listing

```
/* PROPRIETA' DELLA 18M ITALIA */
/* CENTRO SCIENTIFICO DI PISA */
                                                                                                                                                  VA NO 0 0 1 0
                                                                                                                                                  VAN00020
                                                                                                                                                  VAN00030
                   VANDERG: PROC OPTIONS (MAIN);
                                      /*********************/
                                                                                                                                                  VAN00050
                                                                                                                                                  VAN00060
                                                    DECLARATIONS
                                                                                           */
                                                                                                                                                  VAN00070
                                                                                                                                                  VAND0080
                                                                                                                                                  VAN00090
 DCL RANGI POINTER;

DCL (AUX, GI VE, SEQ) (500) PIC'999';

DCL REC (500) PIC'999'; /* USED TO WRITE 'RECURSIVE PART' */

POINTER IN VECTOR 'REC' */

YAN00130

YAN00140

/* THESE ARRAYS ARE USED IN SUBROUTINE RNG */ VAN00150

/* AUX(I) IS FILLED WHITH THE NUMBER OF '1'8 IN ROW I OF MATRIX T*/ VAN00160

/* AT THE END OF VDG ALGORITHM, 'GIVE' IS FILLED WITH THE */ VAN00170

/* VARIABLES TO BE GIVEN /* 'SEQ' IS FILLED WITH THE NEW ORDER OF THE EQUATIONS */ VAN00190

DCL ONE FILE RECORD INPUT:
                                                                                                                                                  VAN00100
  DCL ONE FILE RECORD INPUT;

/* FILE ONE COUNTAINS DATA I.E. THE SET OF EQUATIONS AND COMMENTS*/VANO0210
  DCL TWO FILE RECORD OUTPUT;

/*AFTER PROCESSING FILE TWO CONTAINS THE RESULTS OF REORDERING
DCL COM BIT(1); /* LOGICAL USED FOR THE PRINTING OF COMMENTS */
DCL N PIC'999', /* NUMBER OF EQUATIONS */
I PIC'99', /* POINTER IN LENG */
                                                                                                                                                  VANO0220
                                                                                                                                              */ VAN00230
                                                                                                                                                  VA NO 0 2 4 0
                                                                                                                                                  VA NO 0 2 5 0
                                                                                                                                                  VA NO 0 2 5 0
  CARD CHAR(80); /* CARD USED TO READ DATA */
DCL Z1 PIC'999', EQU CHAR(7000) VARYING;
                                                                                                                                                  VAN00270
                                                                                                                                                  VAN00280
         /* BEFORE EACH 'CALL STUD' EQU CONTAINS ONE EQUATION */
ROW PIC'999', LENG(99) PIC'999', J PIC'999';
/* ROW IS THE INDEX OF ROW IN MATRIX T */
                                                                                                                                                  VAN00290
                                                                                                                                                  VA NO 0 3 0 0
                                                                                                                                                  VAN00310
  /* LENG IS AN ARRAY USED IN SUBROUTINE CREATE */
DCL T (500,500 ) BIT; /* STRUCTURE ARRAY */
/* THE TWO FOLLOWING STRUCTURES FORM LISTS TO STORE EQUATIONS */
                                                                                                                                                  VAN00320
                                                                                                                                                  VAN00330
                                                                                                                                                  VAN00340
  DCL 1 TAB BASED (Q),

2 NUM PIC'999', /* NUM ROW OF AN EQUATION Y(2) = ... -> NUM=2 */

2 VERS POINTER, /* USED TO RECOVER THE FIRST ELEMENT OF TEXT */

2 REL POINTER; /* POINT ON THE FOLLOWING ELEMENT OF TAB */

DCL 1 TEXT BASED(P),
                                                                                                                                                  VA N00350
                                                                                                                                                  VAN00360
                                                                                                                                                  VA NO 0 3 7 0
                                                                                                                                                  VANQ0380
                                                                                                                                                  VA NO 0 3 9 0
            2 INFO CHAR(80), /* INFO IS FILLED WITH 'A LINE OF AN EQUATION' */VANO0400
2 FOL POINTER; /* POINT ON THE FOLLOWING ELEMENT OF TEXT */VANO0410
  DCL (Q, P) POINTER;
                                                                                                                                                  VAN00420
  DCL COUR1 POINTER; /* CURRENT POINTER IN LIST TAB */
DCL COUR2 POINTER; /* CURRENT POINTER IN LIST TEXT */
DCL ENTER POINTER; /* BEGINNING OF THE LIST TAB */
                                                                                                                                                  VAN00430
                                                                                                                                                  VANGGALG
                                                                                                                                                  VANDO450
                                                                                                                                                  VAN00460
                                                                                                                                                  VA NO 0 4 7 0
                                     /****
                                                                                     ****/
                                                                                                                                                  VAN00480
                                                      SUBROUTI NES
                                                                                        */
                                                                                                                                                  VAND0490
                                     /****
                                                                                   ****/
                                                                                                                                                  VANCOSOO
                                                                                                                                                  VAN00510
                                                                                                                                                  VAN00520
                                                                                                                                                  VANO0530
  /* AS IN THE DATA AN EQUATION MAY BE GIVEN ON SEVERAL CARDS */
/* THIS PROCEDURE PUTS ALL THE CARDS COMPOSING AN EQUATION OR IF */
/* STATEMENT IN THE CHARACTER STRING CALLED 'EQU'
/* THE ARRAY 'LENG'

*/
                                                                                                                                                  VAN00540
                                                                                                                                                  VANO 0 5 5 0
                                                                                                                                                  VAN00560
                                                                                                                                                  VAN00570
  /* LENG(1) CONTAINS THE ROW OF THE EQUATION Y(4) =... => LENG(1) =4
/* LENG(1) CONTAINS THE LENGTH (AFTER CANCELLING THE BLANKS)
/* OF THE I-1 CARD OF AN EQUATION OR OF AN IF STATEMENT
                                                                                                                                                  VAN00580
                                                                                                                                                  VAN00590
                                                                                                                                                  VAN00600
  /*********************
                                                                                                                                                  VAN00610
                                                                                                                                                  VANG 0 6 2 0
      CREATE: PROC;
                                                                                                                                                  VAN00630
                                                                                                                                                  VANO0640
  DCL K PIC'99':
                                                                                                                                                  VAN00650
LENG=0;1=2;K=72;
                                                                                                                                                  VAN00660
```

```
/* AFTER CANCELLING THE BLANKS 'K' IS ON THE LAST NONBLANK */
                                                                                                 VAN00570
/* CHARACTER OF A CARD
DO WHILE(SUBSTR(CARD,K,I)=' ');K=K-1;END;
                                                                                                 VANG 0 5 8 0
                                                                                         +/
                                                                                                 VAN00690
      /* WE PUT THE FIRST CARD OF THE EQUATION IN 'EQU'
                                                                                                 VAN00700
EQU-SUBSTR(CARD,7,K-6);
                                                                                                 VAN00710
LENG(2) = K-6; J=K-6;
                                                                                                 VAN00720
READ FILE(ONE) INTO (CARD);
                                                                                                 VAN00730
1 +3;
                                                                                                 VAND0740
/* THE FOLLOWING LOOP FINDS THE REST OF CARDS COMPOSING AN */
/* EQUATION AND PUT THEM IN 'EQU' */
DO WHILE((SUBSTR(CARD,1,1)~*'C')&(SUBSTR(CARD,6,1)~*''));
                                                                                                 VANOD750
                                                                                                 VAN00760
                                                                                                 VANDO 770
   K = 72
                                                                                                 VANOD 7 R O
  DO WHILE(SUBSTR(CARD, K, 1) = 1 1); K=K-1; END;
                                                                                                 VA NO 0.790
   EQU = SUBSTR(EQU,1,3) | | SUBSTR(CARD,7,K-6);
                                                                                                 VANDORDO
   LENG(1) = K-6;
                                                                                                 VA NO 0 8 1 0
   [=[+1;J=J+K-6;
                                                                                                 VA NO 0 8 2 0
   READ FILE(ONE) INTO (CARD);
                                                                                                 VA NO 0 8 3 0
                                                                                                 VA NO 0 8 4 0
   END:
END CREATE;
                                                                                                 VAN00850
                                                                                                 VAN00860
                                                                                                 VA NO 0 8 7 0
/* WHEN WE HAVE FOUND A STRING 'Y(...)', 'COD'LOOKS FOR */
/* THE INDEX BETWEEN PARENTHESES AND PUT IT IN 'Z1' */
                                                                                                 VAN00880
                                                                                                 028000AV
/******
                                                                                                 VAN00900
                                                                                                 VAND0910
      COD: PROC(L);
                                                                                                 VAN00920
                                                                                                 VAND 0930
DCL Z4 CHAR(2);
                                                                                                 VAN00940
DCL (L,K) P1C'9999';
                                                                                                 VAN00950
                                                                                                 VAN00960
/* WE LOOK FOR RIGHT PARENTHESIS OF Y(
DO WHILE(SUBSTR(EQU,K,1) = 1) ; K=K+1; END;
                                                                                                 VAN00970
                                                                                                 VAN00980
                                                                                                 VAND0990
K=K-1;
/* WE ARE BETWEEN THE PARENTHESES OF Y( ) AND WE LOOK FOR */
/* THE FIRST DIGIT OF THE INDEX STARTING FROM THE RIGHT */
DO WHILE(SUBSTR(EQU,K,1)*'');K=K-1;END;
/* WE EXAMINE IF THERE ARE ONE OR TWO DIGITS IN INDEX */
/* AND FILL 'Z1' CONSEQUENTLY */
IF((SUBSTR(EQU,K-1,1)='')|(SUBSTR(EQU,K-1,1)='('))
THEN Z1='00'||SUBSTR(EQU,K, 1);
ELSE IF((SUBSTR(EQU,K-2,1)='')|(SUBSTR(EQU,K-2,1)='('))
THEN Z1='0'||SUBSTR(EQU,K-1,2);
ELSE Z1=SUBSTR(FOU,K-2.3):
                                                                                                 VAN01000
                                                                                                 VAN01010
                                                                                                 VAN01020
                                                                                                 VAN01030
                                                                                                 VAN01040
                                                                                                 VAN01050
                                                                                                 VAN01060
                                                                                                 VAN01070
                                                                                                 VAN01080
       ELSE Z1=SUBSTR(EQU, K-2,3);
                                                                                                 VAN01090
END COD;
                                                                                                 VANOI100
                                                                                                 VAN01110
                                                                                                 VAN01120
/ THIS SUBROUTINE FILLS A ROW OF STRUCTURE ARRAY 'T'
                                                                                                 VAN01130
/* THE EQUATION TO DEAL WITH IS IN 'EQU'
                                                                                                 VANO1140
/************************
                                                                                                 VANO1150
/ *----*/
                                                                                                 VAN01160
     STUD: PROC(M3);
                                                                                                 VAN01170
 *-----
                                                                                                 VAN01180
DCL(M1, M2, M3) PI C'9999', Z2 CHAR(1),
                                                                                                 VAN01190
      COL PIC'999';
/* COD(M3 ) GIVES US THE ROW TO FILL IN MATRIX 'T'
                                                                                                 VAN01200
                                                                                                 VAN01210
CALL COD(M3); ROW=Z1; LENG(1)=ROW; M1=M3+3;
                                                                                                 VAN01220
DO WHILE(M1(J); /* J INDICATES THE END OF 'EQU' */
IF(SUBSTR(EQU,M1,1)='Y') THEN
                                                                                                 VAN01230
                                                                                                 VAN01240
         /* WE HAVE FOUND THE CHARACTER 'Y'. WE LOOK IF THERE IS /* THE FOLLOWING SEQUENCE : Y(....)
                                                                                                 VAN01250
                                                                                                 VA NO 1260
D0;M2=M1+1;
                                                                                                 VAN01270
 DO WHILE (SUBSTR(EQU, M2, 1) = ' '); M2 = M2+1; END; IF( SUBSTR(EQU, M2, 1) = '(') THEN
                                                                                                 VAN01280
                                                                                                VAN01290
                                                                                                VAN01300
    VAN01360
```

```
CALL COD(M1);
                                                                                VAN01370
           CO L=Z1; T(ROW, CO L) = 1 1 B;
                                                                                VANO1386
          M1 =M1+3;
                                                                                VAN01390
         END;
                                                                                VAN01400
                                                                                VAN01410
      END;
                                                                                VAN01420
   END;
M1-M1+1:
                                                                                VAN01430
END;
END STUD;
                                                                                VANDI440
                                                                                VAN01450
                                                                                VAN01460
         ______
                                                                                VAN01470
/ . ' ECRIT' PRINTS THE EQUATION WHOSE INDEX IS DRD(Y(ORD) =....) -/
                                                                                VAN01480
/ + IN THE SAME WAY AS IT WAS GIVEN IN DATA
                                                                                VANDI490
VAN01500
                                                                                VANO1510
   ECRIT: PROC(ORD, RANG);
                                                                                VANDIS20
/ *------/
                                                                                VAN01530
DCL RANG POINTER; /* USED TO PRINT SEVERAL LIST HAVING SAME INDEX */ DCL ORD PIC 999";
                                                                                VANG 154 D
                                                                                VAN01550
COURT-RANG; /* RESEARCH OF INDEX ORD BEGINS AT ADDRESS RANGO/
                                                                                VANG156D
DO WHILE((COURT->NUM"=ORD)&(COURT"=ENTER));
                                                                                VAN01570
COUR1 = COUR1 -> REL;
                                                                                VAN01580
END;
                                                                                VAN01590
IF (COURT-ENTER) THEN GOTO TERM;
                                                                                VAND1600
COUR2 = COUR1 - > VERS;

/* WE ARE ON THE RIGHT ADDRESS, WE WRITE THE FIRST CARD */
WRITE FILE(TWO) FROM(COUR2 -> ) NFO);
                                                                                VAN01610
                                                                                VAN01620
                                                                                VAND1630
           THE FOLLOWING LOOP WRITES THE REST OF TEXT
                                                                                VAN01640
DO WHILE(COUR2->FOL = ENTER);
                                                                                VAN01650
                                                                                VAN01660
  COUR2 = COUR2->FOL;
  WRITE FILE(TWO) FROM(COUR2-> INFO);
                                                                                VAN01670
END;
                                                                                VAN01680
                                                                                VAN01690
TERM: END ECRIT:
                                                                                VAN01708
                                                                                VAN01710
/ THIS SUBROUTINE STORES AN EQUATION IN THE SAME WAY AS
                                                                                VAN01720
/* IT WAS READ IN ORDER TO HAVE A SIMPLE PRINTING. THIS IS
                                                                                VAN01730
/ DONE WITH A LIST STRUCTURE
                                                                                VAND1740
                                                                                VAN01750
                                                                                VAN01760
   ST: PROC;
                                                                                VANO1770
                                                                                VAN01780
/------/
DCL CARD1 CHAR(80),
POS PIC'9999', /* INDICATES POSITION IN STRING 'EQU' */
                                                                                VAN01790
                                                                                VANO1800
    R PI C 99'
                                                                                VAND1810
    / PROCESSING OF THE FIRST CARD OF AN EQUATION OR IF STATEMENT. -/ VAND1820
    /* FIRSTLY WE EXAMINE IF COMMENTS HAVE BEEN ALREADY PUT */VANDIB3D
/* IN A LIST TEXT : IF COM-10'B (NO COMMENTS) WE CREATE A NEW */VANDIB4O
/* LIST TEXT(Y1) OTHERWISE WE CONTINUE THE LIST ALREADY BEGUN(Y2)*/VANDIB5O
CARD1=
         ' ;
                                                                                V M01860
CARD1=
              '||SUBSTR(EQU,1,LENG(2));
                                                                                VANO1870
IF (COM-'0'B ) THEN GOTO Y1;
                                                                                VANO1880
ELSE GOTO Y2;
Y2: COUR1-> NUM=LENG(1);
                                                                                DPRIONAY
                                                                                VAND1900
    ALLOCATE TEXT SET (P);
COUR2->FOL=P;
                                                                                V M01910
                                                                                VAN01920
    P->I NFO =CARD1:
                                                                                VAN01930
    P->FOL=ENTER;
                                                                                VAN01940
     COUR2 -P;
                                                                                VANO1950
    POS = LENG(2)+1;
                                                                                08EIONAV
GOTO Y3;
Y1: ALLOCATE TAB SET (Q);
COUR1->REL=Q;
                                                                                VAN01970
                                                                                VAN01980
                                                                                VAN01990
   Q->REL=ENTER;
                                                                                VAN02000
   Q-> NUM=LENG(1);
                                                                                VANG2010
   COURI-Q;
                                                                                VAN02020
   ALLOCATE TEXT SET(P);
                                                                                VAND2030
   COUR2-P;
                                                                                VAN02040
   Q-> VERS - P:
                                                                                VAN02050
   P->I NFO=CARD1;
                                                                                VAN02050
```

```
P->FOL=ENTER;
                                                                                          VAN02070
    POS=LENG(2)+1;
                                                                                          VAN02080
Y3:R=3;
                                                                                          VANDZOGO
        /* LOOP TO CONTINUE THE LIST 'TEXT' UNTIL THE END OF */
                                                                                          VAN02100
         / THE EQUATION
                                                                                          VAN02110
    DO WHILE (POS(J);
CARD1=' ';
CARD1=' +'||
                                                                                          VAN02120
                                                                                          VAND2130
                    +'||SUBSTR(EQU, POS, LENG(R));
                                                                                          VAN02140
     ALLOCATE TEXT SET(P);
                                                                                          VAN02150
     COUR2->FOL=P;
                                                                                          VAN02160
     P->INFO=CARD1;
                                                                                          VAN02170
     P->FOL=ENTER;
                                                                                          VAN02180
     COUR2=P;
                                                                                          VAN02190
     POS=POS + LENG(R);
                                                                                          VAN02200
     R=R+1;
                                                                                          VAN02210
    END;
                                                                                          VAN02220
END ST ;
                                                                                          VAN02230
                                                                                          VAN02240
VAN02250
/* THIS PROCEDURE RECOGNIZES IF WE ARE ON A STATEMENT */
/* Y( )= OR AN'IF STAT'( IF(....) ).AFTER THERE */
/* IS A SPECIAL TREATMENT FOR EACH KIND OF STATEMENT */
                                                                                          VAN02260
                                                                                          VAN02270
                                                                                          VAN02280
/*****************************
                                                                                          VAN02290
                                                                                          VAN02300
   TESTY: PROC ;
                                                                                          VAN02310
                                                                                          VAN02320
DCL PEQU PIC '9999', /* POINTER IN STRING EQU
NPC PIC '999'; /* USED TO TEST A NUMBER OF PARENTHESIS
IF (SUBSTR(EQU,1,1) = 'Y') THEN
/* WE ARE ON AN 'IF STAT' */
                                                                                          VAN02330
                                                                                          VAN02340
                                                                                          VAN02350
                                                                                          VAN02360
                                                                                          VAN02370
    PEQU=1;
                                                                                          VAN02380
    /* WE LOOK FOR THE LEFT PARENTHESIS OF Y( ) */
DO WHILE(SUBSTR(EQU, PEQU, 1) = *('); PEQU=PEQU+1; END;
                                                                                          VAN02390
                                                                                          VAN02400
   /* PEQU IS ON THE FIRST PARENTHESIS */
NPC=1; PEQU = PEQU + 1;
DO WHILE(NPC=0);
                                                                                          VAN02410
                                                                                          VAN02420
        /* WE LOOK FOR THE END OF TEST IF BY COUNTING THE PARENTHESES */VANO2440
         /* WITH NPC
                                                                                       */VAN02450
       IF (SUBSTR(EQU, PEQU, 1)='(') THEN NPC = NPC +1;
                                                                                         VAN02460
      ELSE IF (SUBSTR(EQU, PEQU, 1) = ')') THEN NPC = NPC -1;
                                                                                         VAN02470
    PEQU=PEQU+1;
                                                                                         VAN02480
    END:
                                                                                          VAN02490
    PEQU = PEQU +1;

/* WE LOOK FOR THE FIRST CHAR 7' FOLLOWING THE END OF TEST */VAN02510

DO WHILE (SUBSTR(EQU,PEQU,I)=''); PEQU = PEQU +1; FND;

VAN02520

IF ((SUBSTR(EQU,PEQU,2)='Y')) THEN

VAN02530

*/VAN02540
                                                                                         VAN02500
           /* THE STAT FOLLOWING IF(..) IS Y( )=.. WF HAVE TO TREAT
/* EQUATION IN STUD(PEQU) PEQU IS NOW ON 'Y' OF Y( )
                                                                                      */VAN02540
                                                                                       */VAN02550
                                                                                         VAN02560
      CALL STUD(PEQU);
    ELSE
                                                                                         VAN02570
              /* THERE IS NOT Y(.)= AFTER 'IF (...)' SO WE HAVE JUST TO */VAN02580
/* STORE THIS STATE WITH 999 IN 'NUM' OF LIST 'TAB' */VAN02590
/* WHICH MEANS THAT THIS STATE WILL BE PRINTED AT THE END */VAN02600
     LENG(1)=999;
                                                                                         VAND2610
                                                                                         VAN02620
   END:
                                                                                         VAN02630
ELSE DO;
           /* THE STATEMENT IS 'Y(..)=.... WE TREAT IT IN STUD (1) */
                                                                                         VAN02640
CALL STUD(1); N=N+1; END;
                                                                                         VAN02650
END TESTY ;
                                                                                         VAN02660
                                                                                         VAN02670
VAN02680
/* ORDERING OF THE EQUATIONS FOLLOWING 'VAN DER GIESSEN METHOD' */
                                                                                         VAN02690
/****************************
                                                                                         VAN02700
/*------/
                                                                                         VAN02710
  RNG: PROC;
                                                                                         VAN02720
/*---*/
                                                                                         VAN02730
DCL IT BIT(1);
DCL A PIC'999', /* POINTER IN VECTOR 'AUX' */
G PIC'999', /* POINTER IN VECTOR 'GIVE' */
                                                                                         VAN02740
                                                                                         VAN02750
                                                                                         VAN02760
```

```
S PIC'999', /* POINTER IN VECTOR 'SEQ' */
K PIC'999', /* POINTER IN THE CURRENT ROW OF 'T' */
(I,J) PIC'999';
                                                                                                VANO2770
                                                                                                VAN02780
                                                                                                VAN02790
                 /* INITIATION OF VECTOR 'AUX' */
                                                                                                VAN02800
A=1:
                                                                                                VAN02810
DO WHILE (A <- N);
                                                                                                VAN02870
G=0; S=1;
                                                                                                VAN02830
DO WHILE(S(=N);
                                                                                                VAN02840
IF(T(A,S)='1'B) THEN G=G+1;
                                                                                                 VAN02850
                                                                                                VAN02860
S=S+1:
END; AUX(A)=G; A=A+1; END;
                                                                                                VAN02870
         /* WE WANT TO SEPARATE THE RECURSIVE OF THE SYSTEM FROM THE */
/* SIMULTANEOUS PART. IN MATRIX 'T', 'RECURSIVE VARIABLES' */
/* HAVE NO '1'B IN THEIR COLUMN.IN THE FOLLOWING LOOP WE */
/* LOOK FOR SUCH VARIABLES AND PUT THEM IN VECTOR 'REC'. */
                                                                                                VAND2880
                                                                                                VAND2890
                                                                                                VAN02900
                                                                                                VAN02910
                                                                                                VAN02920
R1=1: REC(1)=1:
DO A=1 TO N;
                                                                                                VAN02930
G=0; S=1;
                                                                                                VAN02940
DO WHILE(S<=N);
IF (T(S,A)='1'8) THEN Q=G+1;
                                                                                                VAND2950
                                                                                                VAN02960
S=S+1;
                                                                                                VANO2970
END:
                                                                                                VAND2920
IF G=0 THEN DO;
                                                                                                VAN02990
REC(R1)=A; R1=R1+I ; END;
                                                                                                VAN03000
END;
                                                                                                VAN03010
1=1;G=1;S=1;
|T='0'B;
                                                                                                VAN03020
                                                                                                VAND3030
X10:A=1;
                                                                                                VAN03040
              /* X11 TEST TO FIND 'O' IN VECTOR 'AUX' WHICH MEANS THAT
                                                                                              •/VAN03050
              / THE CORRESPONDING VARIABLE MUST BE PUT IN 'SEQ'
                                                                                              -/VAN03060
X11:IF (AUX(A)=0)THEN GOTO X20;
                                                                                                VAN03070
                                                                                                VAN03080
    IF (A(=N)THEN GOTO X11;
                                                                                                VANO309D
          /* WE WENT TO SEPARATE VARIABLES INDEPENDANT FROM ENDOGENOUS */VANO3190
/* VARIABLES FROM THE OTHER VARIABLES. WE KNOW THAT THESE */VANO3110
/* VARIABLES ARE PUT IN 'SEQ' AT THE BEGINNING OF THE ALGO */VANO3120
/* RITHM(IT='0'B).SO WE CAN EASILY FIND THIS SEQUENCE OF */VANO3130
/* VARIABLES AND THEN WRITE A COMMENT OF OUR CHOICE IN THE */VANO3140
/* RIGHT PLACE OF THE OUTPUT FILE */VANO3150
                                                                                                VAN03160
    IF (IT='0'B) THEN
                                                                                                VAN03170
     00;
                                                                                                VAN03180
      IF (S>1) THEN
                                                                                                VAN03190
       00;
       ALLOCATE TAB SET(Q);
                                                                                                VANDEZOD
       COUR1->REL=Q; Q->REL=ENTER; Q->NUM=SEQ(S-1); COUR1-Q; ALLOCATE TEXT SET (P);
                                                                                                VANO3210
                                                                                                VAN03220
       COUR2-P;
                                                                                                VAND3230
       Q->VERS-P
                                                                                                VAH03240
                                                                     ******
       P-> INFO = 'C++++
                                END OF RECURSIVE PART
                                                                                                VAN03250
       P->FOL ENTER;
                                                                                                VAND3260
       END;
                                                                                                VAN03270
                                                                                                VANDI280
    END;
                                                                                                VAN03290
           /* X30 RESEARCH OF THE FIRST I IN VECTOR 'AUX' ./
                                                                                                VAN03300
                                                                                                VAN03310
X31:1F (AUX(A)=1) THEN GOTO X40;
                                                                                                VANO3320
                                                                                                VAN03330
     A=A+1;
    IF (A(=N) THEN GOTO X31;
                                                                                                VANOSSÃO
                                                                                                VAN03350
X50:1=1+1:
                                                                                                VANO3360
     GOTO X25;
            /* X40 RESEARCH OF THE FIRST 1 IN ROW 'A' OF THE MATRIX 'T' */VAN03370
                                                                                                VAND3380
X40:K=1;
X41:15 (T(A,K)-11'B) THEN GOTO X60:
                                                                                                VAND3390
                                                                                                VANO3400
    K=K+1:
    VAN03410
                                                                                                VAN03460
    DOS
```

```
AUX(B)=AUX(B)+1;
                                                                                  VAN03470
    T(B,K)='1'B;
                                                                                  VAN03480
     END;
                                                                                  VAN03490
                                                                                  VAN03500
        /* RESEARCH OF A '1'B IN THE DIAGONAL OF MATRIX 'T'
                                                                                  VAN03510
                                                                                  VAN03520
X71:1F (T(J.J)='1'B) THEN GOTO X80:
                                                                                  VAN03530
   J=J+1;
                                                                                  VAN03540
   IF (J(=N) THEN GOTO X71;
                                                                                  VAND355D
   IF(1=1) THEN GOTO X35;

/* WE HAVE ALREADY FOUND ONE OR MORE '1'B IN ROW A. THEIR
                                                                                  VANO356D
                                                                                  VAN03570
        / TREATMENT HAS BEEN DONE. WE RESEARCH THE FOLLOWING '1'B. ./
                                                                                  VAN03580
X45:K-K+1:
                                                                                  VAND359D
X46:IF(T(A,K)=11'B) THEN GOTO X60;
                                                                                  VAND3600
  K=K+1:
                                                                                  VAN03610
  IF(K<-N) THEN GOTO X48;
                                                                                  VAN03620
         / • WE HAVE ALREADY TREATED ONE OR MORE 'I' IN VECTOR / • AUX. WE RESEARCH THE FOLLOWING 'I'
                                                                                  VAN03630
                                                                                  VAN03640
X35:A=A+1;
                                                                                  VAN03650
X36:1F (AUX(A)=1) THEN GOTO X40;
                                                                                  VAN03660
   A=A+1;
                                                                                  VAN03670
   1F(A<=N) THEN GOTO X36;
                                                                                  VAN03680
    GOTO X50;
                                                                                  VAN03690
       /* WE HAVE FOUND A VARIABLE TO BE GIVEN. SO WE DELETE THE
                                                                                -/VAN03700
       /. CORRESPONDING COLUMN J, WE PUT THIS VARIABLE IN 'GIVE'
                                                                                •/VAN03710
       /* AND ADJUST 'AUX'
                                                                                •/VAN03720
                                                                                  VANO373D
X81:IF(T(A,J)='0'B) THEN GOTO X82;
T(A,J)='0'B;
                                                                                  VAND3740
                                                                                  VAN03750
    AUX(A) = AUX(A) - 1;
                                                                                  VAN03760
X82:A=A+1;
                                                                                  VAN03770
  IF(A<=N) THEN GOTO X81;
                                                                                  VAN03780
   GIVE(G)=J;
                                                                                  VAN03790
                                                                                  VAN03800
    G=G+1:
     IF(I=1) THEN GOTO X10;
                                                                                  VAN03810
   1-1-1;
                                                                                  VAN03820
    GOTO X30 ;
                                                                                  VAN03830
      /+ WE HAVE FOUND A ROW 'A' WITH AUX(A)=0. WE PUT THIS VARIABLE +/VAN03840
/* IN VECTOR 'SEQ', WE DELETE THE CORRESPONDING COLUMN IN +/VAN03850
/* MATRIX 'T' AND ADJUST 'AUX' +/VAN03860
      /+ MATRIX
X20:SEQ(S)=A:
                                                                                  VAN03870
   :000=(A) XUA
                                                                                  VAN03880
   S=S+1;
                                                                                  00880NAV
J=1;
X21:1F (T(J,A)='0'B) THEN GOTO X22;
T(J,A)='0'B;
                                                                                  00650KAA
                                                                                  VAN03910
                                                                                  VAN03920
                                                                                  VAN03930
                                                                                  VAN03940
X22:J=J+1;
VAN63950
                                                                                  VANGTGEO
                                                                                  VAND3970
   ELSE GOTO X10;
                                                                                  DRPEGNAV
FIN: END RNG;
                                                                                  VANOSAGO
                                                                                  VANOAGGO
/* THIS SUBROUTINE SEARCHS IF 'IN' IS ONE OF THE COMPONENTS OF */
/* VECTOR 'REC'. IF YES TROUVE=1 ELSE TROUVE=0 */
                                                                                  VAN04010
                                                                                  VANDAGOO
                                                                                  VANO4030
                                                                                  VANGAGAG
/*-----/
                                                                                  VANOLOSO
    COMP: PROC(IN);
                                                                                  VAND&060
                                                                                  VANOLO70
DCL IN PIC'999',
                                                                                  VANO4080
    R2 PIC'999'
                                                                                  VAN04090
    TROUVE PIC'9';
                                                                                  VAN04100
TROUVE-0; R2-1;
DO WHILE (R2<R1);
                                                                                  VAN04110
                                                                                  VANO4126
IF (REC(R2)=IN) THEN DO; TROUVE=1; R2=R1; END;
                                                                                  VAN04130
ELSE R2+R2+1:
                                                                                  VAN04140
                                                                                  VANOA150
END:
                                                                                  VAN04160
RETURN (TROUVE) ;
```

```
END COMP:
                                                                                VANOL170
                                                                                VAND4180
VANO+190
/* THIS SUBROUTINE WRITES IN THE OUTPUT FILE ALL THE LISTS 'TEXT' */
/* HAVING THE SAME INDEX 'NUM' IN THE LIST 'TAB'. */
                                                                                VAND4200
                                                                                VAHOA710
                                                                                VAND4220
/*-----/
                                                                                 VANDAZ30
    IMPRIM: PROC(INDIC):
                                                                                 VANOA 240
                                                                                 VANDAZ50
DCL INDIC PIC'999';
                                                                                 VAND4260
                                                                                 VANDA270
RANGI-ENTER->REL;
     /* WE LOOK IF THERE IS MORE THAN ONE LIST WITH THE */
/* SAME 'NUM' AND WE CALL ECRIT AS MANY TIMES AS NECESSARY */
                                                                                 VANOA280
                                                                                 VANON 290
DO WHILE (RANG1"-ENTER);
                                                                                 VANOA 100
CALL ECRIT(INDIC, RANGI);
IF (COURT - ENTER) THEN RANGI - COURI -> REL;
                                                                                 VAN04310
                                                                                 VAN04320
ELSE RANGI-ENTER;
                                                                                 VANO4330
                                                                                 VANO4340
END;
END IMPRIM;
                                                                                 VAN04350
                                                                                 VANO 4360
                /-----/
                                                                                 VANO4 370
                                                                                 VANON SEO
                /****
                                                    ****/
                /.
                               MAIN PROCEDURE
                                                       ./
                                                                                VANORTGO
                /****
                                                                                 VANO4400
                                                    ****/
                /-----/
                                                                                 VAN04410
                                                                                 VANON-20
                                                                                VANORA 30
    /- INITIATION -/
ALLOCATE TAB SET(Q);
                                                                                 VANDANAO
                                                                                 VANOA450
ENTER-Q:
couR1=Q:
                                                                                 VAN04460
Q->REL-ENTER;
                                                                                 VANONA70
T-'0'B; N-0;
COM-'0'B;
                                                                                 VANORAGO
                                                                                 VANORAGO
OPEN FILE(ONE) INPUT;
OPEN FILE(TWO) OUTPUT;
                                                                                 VAND4500
                                                                                 VANOA510
                                                                                 VANON520
READ FILE(ONE) INTO (CARD);
/* LOOP TO FIND THE EQUATIONS, STORE THEM AND FILL MATRIX 'T' -/
ON ENDFILE(ONE) GOTO SUIT;
LOOP:IF (SUBSTR(CARD,1,1)-'C') THEN
                                                                                VANDAS 30
                                                                                VANDASAD
                                                                                VANO4550
                                                                                VANDAS60
    100
           / * WE ARE ON A COMMENT CARD.COM-'0'B MEANS THAT ./
                                                                                VANO4570
           / THIS IS THE FIRST COMMENT CARD COMING AFTER ./
/ AM EQUATION OR IF STATEMENT SO WE CREATE ./
                                                                                VANOA580
                                                                                VAN04590
           /. A NEW LIST TEXT AND BEGIN IT WITH THIS CARD ./
                                                                                 VANO4600
                                                                                VANON610
     IF (COM- 'O'B) THEN
                                                                                VANOL670
      DO:
                                                                                VANON630
       ALLOCATE TAB SET(Q);
      COUR1->REL=Q; Q->REL=ENTER; COUR1-Q; COM='1'B;
ALLOCATE TEXT SET(P);
                                                                                VANOAGAD
                                                                                VANO4650
                                                                                VANDAGED
       COURZ-P; Q->VERS-P; P->INFO-CARD; P->FOL-ENTER;
                                                                                VANOA670
       END:
                                                                                VANON580
    ELSE
            /* WE CONTINUE THE 'COMMENT LIST ' ALREADY BEGUN */
                                                                                VAND4690
                                                                                 VANOS 700
       DO;
                                                                                VANO4710
       ALLOCATE TEXT SET(P);
                                                                                VANOA720
       COUR2->FOL-P;
                                                                                 VANO4730
       P-> INFO=CARD;
                                                                                 VAN04740
       P->FOL-ENTER;
                                                                                 VANOA750
       COURZ-P;
                                                                                VANO4750
       END:
                                                                                VAN04770
  READ FILE(ONE) INTO (CARD) ;
                                                                                 VANO4780
    END;
                                                                                VANGA790
  FLSE
      /* WE ARE NOT ON A COMMENT SO WE HAVE TO DO THE WHOLE TREATMENT */VANDABOO
                                                                                VAN04810
    00;
                                                                                VAN04820
    CALL CREATE;
                                                                                VANO4830
  CALL TESTY;
                                                                                VANCASAO
    CALL ST;
COM-'0'B;
                                                                                VANO4850
                                                                                VAN04860
    END;
```

```
GOTO LOOP;
                                                                                                VAN04870
               /* ORDERING OF EQUATIONS */
                                                                                                VAN04880
SUIT: CALL RNG;
                                                                                                VAN04890
          /* WE DO SEQ(N+1)=999 TO PRINT IF STATEMENT WITHOUT */
                                                                                                VAN04900
           /* EQUATION Y(..) .. AFTER TEST IF
                                                                                                VAN04910
    SEQ(N+1)=999;
                                                                                                VAN04920
/* PRINTING OF VECTORS 'GIVE' AND 'SEQ'
PUT SKIP LIST('GIVE', 'SEQUENCE');
PUT SKIP LIST('');
                                                                                                VAN04930
                                                                                                VAN04940
                                                                                                VAN04950
DO I=1 TO N:
                                                                                                VAN04960
PUT SKIP LIST(GIVE(1), SEQ(1));
                                                                                                VAN04970
                                                                                                VAN04980
END;
        /* PRINTING OF THE EQUATIONS WITH NEW ORDERING */
                                                                                                VAND&990
                                                                                                VANOS000
DO I=1 TO N+1;
          /* FIRST WE LOOK IF THE VARIABLE(SEQ(I)) BELONGS TO THE */
/* 'RECURSIVE PART' OF THE SYSTEM.IF YES(COM(SEQ(I))=1 */
/* IT WILL BE WRITTEN LATER,OTHERWISE(COM(SEQ(I))=0) IT */
                                                                                                VAN05010
                                                                                                VAN05020
                                                                                                VAND5030
           / IS WRITTEN AT ONCE.
                                                                                                VAN05040
IF (COMP(SEQ(1))=0) THEN
                                                                                                VAN05050
CALL IMPRIM(SEQ(I));
                                                                                                VANO5060
END;
                                                                                                VAN05070
          /* R1>1 MEANS THAT THERE ARE SOME EQUATIONS IN 'RECURSIVE */ VANO5080
/* PART' OF THE SYSTEM. THESE EQUATIONS ARE IN VECTOR 'REC' */ VANO5090
/* WE PUT THEM IN THE OUTPUT FILE 'TWO' */ VANO5100
IF (RI>1) THEN
                                                                                                VAN05110
DO;
                                                                                                VAN05120
  CARD=' ';
                                                                                                VAN05130
   CARD='C++ END OF SIMULTANEOUS PART ***';
                                                                                                VAN05140
   WRITE FILE(TWO) FROM (CARD);
                                                                                                VAN05150
   DO I-1 TO R1-1;
                                                                                                VAN05160
    CALL IMPRIM(REC(1));
                                                                                                VAN05170
                                                                                                VAN05180
   FND:
                                                                                                VAN05190
END;
CLOSE FILE(ONE);
CLOSE FILE(TWO);
                                                                                                VAN05200
                                                                                                VAN05210
                                                                                                VAN05220
END VANDERG;
```

#### REFERENCES

- [1] Bianchi, C., G. Calzolari and P. Corsi, "A Program for Stochastic Simulation of Econometric Models", Econometrica, 46 (1978), 235-236.
- [2] Bianchi, C., G. Calzolari and P. Corsi, "Stochastic Simulation of Econometric Models: Installation Procedures and User's Instructions", IBM Technical Report G513-3568, Pisa, (1978).
- [3] IBM, "Virtual Machine Facility/370: CMS Command and Macro Reference", GC20-1818, IBM, New York, (1976).
- [4] Klein, L.R., "Estimation of Interdependent Systems in Macroeconometrics", Econometrica, 37 (1969), 171-192.
- [5] Van der Giessen, A.A., "Solving Non-Linear Systems by Computer; a New Method", Statistica Neederlandica, 24 (1970), 41-50.