Political ideology as a source of business cycles

azzimonti marina

university of texas -austin

June 2010

Online at https://mpra.ub.uni-muenchen.de/25937/
MPRA Paper No. 25937, posted 21. October 2010 16:17 UTC
POLITICAL IDEOLOGY AS A SOURCE OF BUSINESS CYCLES

Marina Azzimonti †
This version: June 2010

Abstract

When the government must decide not only on broad public-policy programs but also on the provision of group-specific public goods, dynamic strategic inefficiencies arise. The struggle between opposing groups—that disagree on the composition of expenditures and compete for office—results in governments being endogenously short-sighted: systematic under-investment in infrastructure and overspending on public goods arises, as resources are more valuable when in power. This distorts allocations even under lump-sum taxation. Ideological biases create asymmetries in the group’s relative political power generating endogenous economic cycles in an otherwise deterministic environment. Volatility is non-monotonic in the size of the bias and is an additional source of inefficiency.

JEL Classification: E61, E62, H11, H29, H41, O23
Keywords: Public Investment, Commitment, Probabilistic Voting, Markov Equilibrium, Political Cycles, Time Consistency.

* An earlier version of this paper circulated under the title ‘On the dynamic inefficiency of governments’. I would like to thank Steve Coate, Per Krusell, Fernando Leiva Bertran, Lance Lochner, Leo Martinez, Antonio Merlo, Victor Rios-Rull, Pierre Sarte and Andrzej Skrzypacz as well as participants of the SED Meeting, the Midwest Macroeconomics Meetings, the Public Economic Theory Conference and the Prague-Budapest Spring Workshop in Macroeconomic Theory. I would also like to thank attendants to the department seminar series at the FRB of Richmond and the universities of Rochester, Iowa, and British Columbia for helpful comments. Part of this work was developed while visiting the IIES at Stockholm University and the University of Pennsylvania. All errors are mine.

† University of Texas - Austin. Department of Economics. email:azzimonti@eco.utexas.edu
1 Introduction

Public policy and institutions are found to be relevant factors in explaining the large differences in income per-capita across countries. However, policies that enhance growth and promote development are not always chosen by the government (especially in under-developed economies). Why? A group of explanations attributes it to the instability that results from major political upheaval and coups d’etat. It turns out that even democratic countries, where changes in government follow a stable election process, exhibit large disparities in income and implemented policies. Several authors suggest that this could be the result of failures or frictions in the decision-making process of the public sector. A basic point is that policymakers can engage in rent-seeking activities and may choose inefficient policies in order to increase their probability of re-election so as to get continued access to these office rents. However, one does not need to take such a cynical view of governments. Even governments that are not “intrinsically bad” can, due to the democratic process itself—where re-election is never certain—and the resulting natural lack of commitment, generate bad outcomes. This is the idea pursued in the present paper.

I present a theoretical model where the struggle between groups with different views that alternate in power results in governments being endogenously short-sighted—at least more so than the groups they represent. As a consequence, they tend to overspend and underinvest, reducing output and private consumption. The party in power tries to tie the hands of its successor by strategically manipulating public investment. Political uncertainty, together with the assumption of a fundamental lack of commitment, creates incentives to reduce the amount of public capital available for the next policymaker as a way to restrict his level of spending. I show that the dynamic inefficiency generated by the politician’s short-sightedness is mitigated by the degree of political stability. In addition, asymmetries in the groups’ relative political power—which result from ideological biases in the population—generate endogenous economic cycles. Macroeconomic variables fluctuate in equilibrium, even in the absence of productivity shocks. Analyzing the implications of this second source of inefficiency will be the objective of this paper.

In this economy, the role of the government is to provide public goods and invest in productive public capital, which are financed through lump-sum taxation. There are two groups in the economy that disagree over the composition of spending on public goods but not over its aggregate size or over the level of infrastructure investment. Groups are represented by parties which alternate in power via a democratic process, and election outcomes are uncertain. The degree of political stability (i.e. frequency of turnover) is determined in a voting equilibrium. Agents are forward looking and vote for the party that yields them higher expected utility. I consider a situation where voter’s ideological biases towards one the groups yields its candidates a political advantage over those from the other group, which leads to an asymmetric equilibrium. There is no commitment technology, so promises made during the campaign are non-binding. I characterize time-consistent outcomes as Markov-perfect equilibria. I first derive the incumbent’s optimality condition for a general case and characterize the determinants of political turnover in the equilibrium of a voting model. Thus, the degree of political uncertainty is jointly determined with public policy, so it depends on the primitives that shape it (i.e., on the intensity of ideology, on agent’s preferences, and on technology). I then find an analytical solution under specific functional assumptions in

\footnote{For example, Acemoglu, Johnson, Robinson (2001) study the relationship between property rights and different degrees of development.}

\footnote{Barro (1996) and Easterly and Rebelo (1993) provide evidence that coups reduce growth.}

\footnote{See Persson and Tabellini (1999) for an excellent review of the literature.}

\footnote{An analysis of the earlier models in this literature (e.g. Barro, Nordhaus, and Ferejohn) can be found in Drazen (2000).}
order to derive testable implications from the theory. Finally, I present some empirical evidence supporting the model predictions.

I find that the group that has an advantage in the political dimension (i.e., its candidates are more ‘popular’) wins the elections more often and spends a lower share of output on public consumption, while investing a larger share than its counterpart. The political uncertainty is propagated into the economy and endogenous economic cycles are generated, even though there is no source of uncertainty other than the identity of the policymaker. This decreases welfare relative to the first best not only because it reinforces the dynamic inefficiency (investment is too low), but also because it introduces volatility in macroeconomic variables (output, employment, and consumption). Increases in the ideological bias widen the gap between the policies chosen by the the two groups, as well as their probabilities of being elected. The size of business cycles induced by changes in the bias is non-monotonic because it is affected by changes in policy and probabilities in opposite directions. As a result, economies where the political advantage is low exhibit rapid turnover but small fluctuations in policy as the gap in investment shares is small. At the other extreme, when the biases are large so are the differences in policy, but the most popular party is in power more often and hence fluctuations are small. Volatility is largest for intermediate values of the ideological bias. Using a proxy for investment shares and ideology biases for the US during the period 1929-2006, I show that these two variables tend to comove, providing some support for the theory.

On a more methodological level, this paper provides an optimality equation faced by the government in power that can be used to analyze the trade-offs that arise in the presence of reelection uncertainty. It reveals that there is a wedge between the marginal cost and marginal benefit of investment when compared to the benevolent planner’s solution (so allocations are inefficient). This wedge arises from the existence of intertemporal strategic effects. On the one hand, the government wants to decrease the level of resources available to next period’s policymaker so as to restrict his level of spending. But this will cause a negative effect in the opposition’s investment level, which the incumbent may want to boost if it expects the opposition to invest too little. On the other hand, changes in policy may also modify reelection probabilities, which must be taken into account by forward-looking governments.

**Existing Literature**

This paper contributes to a literature that analyzes the dynamic efficiency of policy choice in representative democracies. It builds on the work by Besley and Coate (1998) and Alesina and Tabellini (1990) who present the first theories of political failure. In Alesina and Tabellini (1990) parties choose to overspend in public goods and to create an excessive level of debt when the outcome of elections is uncertain. In Besley and Coate (1998) parties fail to undertake a public investment that is potentially Pareto improving due to lack of commitment in a two-period model. Our work extends some of their insights to a dynamic infinite-horizon political economy model, particularly relevant for assessing the long-run effects of current policy.

One of the papers most closely related to this is Amador (2008) who also analyzes the inefficiencies generated by a common pool problem in a dynamic infinite horizon model. His basic mechanism, like the one in this paper, is based on the trade-offs described in Alesina and Tabellini (1990). Amador finds that politicians are too impatient behaving as hyperbolic consumers, which results in inefficient overspending and excessive deficit creation. In his paper the alternation of power is exogenous, while it is determined by voting in the current paper. Azzimonti (2010) endogenizes political turnover in a similar environment where the government distorts private investment.

---

5Caballero and Yared (2008), Cuadra and Sapriza (2008), Devereux and Wen (1998) and Ilzetzki (2009) also
in order to finance group specific public goods. Overspending results in equilibrium, but there is no public investment. Battaglini and Coate (2007) introduce productive public goods financed by the government. Instead of focusing on political parties, they assume that policy is decided through legislative bargaining. In their work the probability of being able to choose expenditures is exogenous and only depends on the number of legislators, while it is endogenous here and depends on the level of public investment. Additionally, distortions arise due to the assumption of proportional taxation on labor income in their paper, while I assume those away by focusing on lump-sum taxes (distortions arise because public capital affects the productivity of labor here, while the two are completely independent in their setup). In addition, in these three papers parties are completely symmetric so there are no fluctuations in macroeconomic variables induced by changes of power. The analysis of business cycles generated by ideological biases is a main contribution relative to their work.

This paper also contributes the literature on inefficiencies resulting from the government’s lack of commitment. While existing models with repeated voting find strategic interactions, most of them must rely on numerical methods to characterize the Markov-perfect equilibrium (i.e. Krusell and Rios-Rull 1999). Hassler, Mora, Storesletten, and Zilibotti (2004), on the other hand, find analytical solutions in an overlapping generations setup where policy is decided by majority voting, but assume away political uncertainty. Hassler, Storesletten, and Zilibotti (2007) find that expenditures in a consumable public good can be inefficient, but in a model where two-period lived agents vote over redistributive policy. Unlike in their work, part of the expenditures are devoted to productive investment, which allows us to analyze the effects of policy on economic development.

I also extend existing work by endogenizing the probabilities of reelection in a dynamic setup. A key assumption in this paper is that politicians are citizen candidates that do not have commitment to platforms. As a result, voters expect the incumbent to maximize the utility of the group he represents (disregarding the welfare of other groups). This is opposite to standard result in probabilistic voting models with commitment to platforms, where the politicians maximization problem is equivalent to that of a benevolent planner (see Sleet and Yeltekin, 2008 or Farhi and Werning, 2008). In a recent paper Battaglini (2010) considers an environment where expected ideological biases are persistent and candidates are office seekers with commitment to platforms. He finds that the political equilibrium exhibits excessive debt creation and over spending. Due to the assumption that there is no ex ante bias in favor or against any candidate, the equilibrium is symmetric. Therefore, there are no fluctuations in debt, taxes or macroeconomic variables generated by switches of power (other than those resulting from productivity shocks), which is the focus of this study.

Finally, this paper is related to the literature on ‘partisan cycles’. In contrast to previous models in this literature (like Milesi-Ferreti and Spolaore, 1994, Persson and Svensson, 1989 or more recently Song, 2009), I do not need to assume exogenous differences in preferences over the size of public expenditures in order to generate fluctuations. Parties have the same ex-ante utility over the size of spending on public goods and on the level of investment. In equilibrium one party may spend more and invest less just because it loses more often as a result of an ideological disadvantage.

The organization of the paper is as follows. The model is described the Section 2 and the Markov-perfect equilibrium defined in Section 3. An analytical solution is presented in Section

\[ \text{analyze environments where exogenous political turnover introduces inefficiencies in debt accumulation and the level of taxation in Markov-switching models. See Lagunoff and Bai (2010) for an interesting case where the probabilities are exogenous but depend on the aggregate state of the economy.} \]

\[ \text{Besley, Ilzetzki, and Persson (2010) study the effects of exogenous political instability on fiscal capacity (a durable public good) in a similar environment.} \]
where qualitative and quantitative implications are derived. Section 5 provides some empirical support for the theory and Section 6 concludes.

2 The basic model

2.1 Economic environment

Consider an infinite-horizon economy populated by agents that live in one of two regions, $A$ and $B$, of measure $\mu^J = \frac{1}{2}$, $J = \{A, B\}$. While they have identical income and identical preferences over private consumption, they disagree on the composition of public expenditures since public goods can be region-specific (e.g. parks, museums, environmental protection, public television, etc). Agents also differ in another dimension that is orthogonal to economic policy (religious views, charisma of the politician, etc.). Preferences over this political dimension imply derived preferences over candidates, and will take the form of additive iid preference shocks $\xi$ (to be described in more detail later). The instantaneous utility of agent $j$ in region $J$ at a particular point in time is

$$u(c_j, n_j) + v(g^J_j) + \xi_j,$$

where $u$ and $v$ are increasing and concave in $c$ and $g$, and $u$ is decreasing in $n$, with $v(0) \equiv \bar{v}$, $c_j$ denotes the consumption of private goods, $n_j$ denotes labor, and $g^J$ is the level of discretionary spending on local goods in region $J$. Notice that an agent living in region $A$ derives no utility from the provision of a good in region $B$ (and vice versa), so in principle there will be disagreement in the population over the desired composition of public expenditures, but not on its size, since both types have the same marginal rate of substitution between private and public goods.

There are infinitely many competitive firms that produce a single consumption good and hire labor each period so as to maximize profits, which are distributed back to consumers who own shares of these firms. Firms have access to a Cobb-Douglas technology:

$$F(K_g, n) = AK_g^\theta n^{1-\theta},$$

where $n$ is the aggregate labor supply and $K_g$ is the stock of public capital (i.e. infrastructure, public health, and education, the knowledge produced by the public sector’s R&D and expenditures in national defense or law enforcement). Its level is determined by government investments and acts as an externality in production. The idea behind this specification is that the better the infrastructure (roads, harbors, sewers, etc.), the more educated the population and the stronger the protection of property rights, the higher the productivity of the private sector.

The government raises revenues via lump-sum taxes $\tau$ which are chosen every period, so private consumption is

$$c_j = wn_j + \pi - \tau.$$

Taxes are used to finance the provision of consumable public goods ($g^A$ and $g^B$) and investments on productive public capital ($I_{K_g}$). The cost of producing $g > 0$ units of a local public goods is given by $x(g)$, with $x(0) = 0$. Assuming that there is no debt, the government must balance its budget every period, so its budget constraint reads as:

$$\sum_j x(g^J_j) + I_{K_g} = \tau.$$

Assuming a depreciation rate of $\delta$, public capital evolves according to:

$$K'_g = I_{K_g} + (1 - \delta)K_g.$$
where primes denote next period variables. The assumption of lump-sum taxes is made in order to highlight that inefficiencies in production may arise due to political frictions even when the government has access to non-distortionary financing instruments.

2.2 Planning solutions

Before describing the outcome under political competition (where different parties alternate in power), it is useful to characterize the optimal allocation chosen by a benevolent social planner. The planner chooses \( \{c, K'_g, g^A, g^B\} \) so as to maximize a weighted sum of utilities, where the weight on type \( J \) agents is \( \lambda_J \) (with \( \lambda_A + \lambda_B = 1 \)). All individuals within group \( J \) are treated in a symmetric way since their political shocks are irrelevant for the determination of economic allocations. The planner’s maximization problem follows.

\[
V^*(K_g) = \max \sum_J \mu^J \lambda^J [u(c, n) + v(g^J)] + \beta V^*(K'_g),
\]

subject to the resource constraint:

\[
\sum_J x(g^J) + c + K'_g = F(K_g, n) + (1 - \delta)K_g.
\]

As long as the planner gives a positive weight to each agent, the optimal allocation of public good \( J \) will be such that its marginal utility is proportional to the marginal utility of private consumption.\(^7\)

\[
u_1(c, n)x(g^J) = \zeta_J v(g^J), \quad \text{where } \zeta_J = \frac{\lambda^J}{\sum_J \lambda^J} < 1. \tag{2}\]

By varying \( \lambda^J \) between 0 and 1 it is possible to trace the Pareto frontier that characterizes the optimal provision of public goods. Concavity of \( v \) implies that if type \( A \) agents have a higher weight in the social welfare function, more of their desired public good will be provided (at the expense of type \( B \) agents).

Labor satisfies a standard first order condition where

\[
u_1(c, n)F_2(K_g, n) + u_2(c, n) = 0.
\]

Finally, the planner chooses the level of public capital that equates the marginal costs in terms of foregone consumption to the discounted marginal benefits of the investment.

\[
u_1(c, n) = \beta u_1(c', n')[F_1(K'_g, n') + 1 - \delta]. \tag{3}\]

The planner’s Euler equation is completely independent of the choice of the social welfare function: changes in \( \lambda^J \) do not affect this margin. The results follows from assuming that both agents have the same trade-off between private and public consumption (i.e. \( u \) and \( v \) are equal for all agents).

It is important to note that the planner is constrained to offer all households the same consumption allocation (that is, \( c^A = c^B \)). This is imposed in order to capture the constraint faced by the government in the political equilibrium (where parties cannot tax agents at different rates).\(^8\)

\(^7\)If the planner only cares about the well-being of, say, agent \( A \), it will set \( g^B_t = 0 \) \( \forall t \) and \( g^A_t \) so as to equate the marginal rate of substitution between private and public goods to the marginal cost of providing the goods \( x(g) \).

\(^8\)If we were to assume that \( \lambda^A \mu^A = \lambda^B \mu^B \), the unconstrained social optima would coincide with the result presented above.)
3 Political equilibrium

The role of the government in this economy is to provide public goods and productive public capital. Given the disagreement between groups over which public good should be provided, political parties will endogenously arise in a democratic environment. I analyze a stylized case where there are two parties, A and B, representing each group in the population and competing for office every period. There will be no distinction between a ‘candidate’ and a ‘party’ (all candidates have the same preferences so there is no heterogeneity within a party).

The groups will alternate in power based on a political institution where “ideology” or other non-economic issues play a role. In particular, I use a “probabilistic-voting” setup (see Lindbeck and Weibull (1993)) in order to provide micro-foundations for political turnover: the probability of being in power next period is going to be endogenously determined via an electoral process. A key departure from the traditional probabilistic voting model is that parties do not have commitment to platforms, so announcement made during the political campaign will not be credible unless they are ex-post efficient (that is, once the party takes power). The elected party decides on the level of taxes and the allocation of government resources between spending and investment. Its objective is to maximize the utility of its own type.  

Timing

Each period will be divided into three stages: the Taxation Stage, the Production Stage and the Election Stage.

At the Taxation Stage, the incumbent chooses \( \tau, g_A, g_B \) and \( K'_g \) knowing the state of the economy \( K_g \) and the distribution of political shocks but not their realized values. Hence, policy is chosen under uncertainty. The probability of winning the election can be calculated by forecasting how agents vote given different realizations of the shock.

At the Production Stage agents choose labor supply and levels of consumption taking policy as given, but under uncertainty about the identity of future policymakers. Firms hire labor and distribute profits, and the government implements the policy chosen by the party in power.

After production, consumption, and investment take place, \( \xi' \) is realized. At the Election Stage, agents vote for the party that gives them higher expected lifetime utility. They need to forecast how the winner of the election chooses policy. The assumptions of rationality and perfect foresight imply that agents’ predictions are correct in equilibrium.

3.1 Markov-perfect equilibrium

There is no commitment technology, so promises made by any party before elections are not credible unless they are ex-post efficient. The party in power plays a game against the opposition taking their policy as given. Alternative realizations of history (defined by the sequence of policies up to time \( t \)) may result in different current policies. In principle, this dynamic game allows for multiple subgame-perfect equilibria that can be constructed using reputation mechanisms. I will rule out such mechanisms and focus instead on Markov perfect equilibrium (MPE), defined as a set of strategies that depend only on the current—payoff relevant—state of the economy. Given the sequence of events and the separability assumption between the economic and the political dimensions, the only payoff-relevant state variable is the stock of public capital. In a Markov-perfect equilibrium, policy rules and voting decisions are functions of this state. Since there is no

---

\[ ^9 \text{In that sense this is a partisan model, see Drazen (2000) or Persson and Tabellini (2000) for a description of opportunistic party models.} \]
commitment and no retrospective voting, the values of $g^A$ and $g^B$ chosen by the incumbent are irrelevant in the voting decision. So is the history of ideology shocks, since there is no persistence.

The equilibrium objects that we are interested in are policy functions, allocations, winning probabilities, and value functions. There are three policy functions: the investment rule of incumbent $i$, $h_i(K_g)$, and expenditures in each region-specific good $g^A_{i}(K_g)$ and $g^B_{i}(K_g)$. Agent $j$’s labor supply $n_{ij}(K_g)$ and consumption $c_{ij}(K_g)$ under incumbent $i$’s policies summarize the allocations (firms decisions as well as aggregate consumption and labor supply can be trivially determined from these functions). The probabilities will be denoted by $p_i(K_g)$. The value function—net of political shocks—of agent $j$ when his group is in power will be denoted by $V_j(K_g)$ and when his group is out of power by $W_j(K_g)$. The characterization of the MPE follows, starting from the last stage (the Election stage) to make the exposition clearer.

**Election Stage**

At this stage, agents must decide which party to vote for. The utility derived from political factors, $\xi_j$, has two components: an individual ideology bias (denoted by $\phi^J$) and an overall popularity bias ($\psi$). In particular,

$$\xi_i = (\psi + \phi^J) I_i,$$

where $I$ is an indicator function such that $I_B = 1$ and $I_A = 0$, since the individual specific parameter $\phi^J$ measures voter $j$’s ideological bias towards the candidate from party $B$. I will follow Persson and Tabellini (2000) by assuming that the distribution of $\phi^J$ is uniform and group-specific,

$$\phi^J \sim \left[ -\frac{1}{2\phi^J}, \frac{1}{2\phi^J} \right], \text{ with } J = A, B.$$

These shocks are iid over time, hence ‘candidate specific.’ Each period, a given party presents a candidate and voters form expectations about the candidate’s position on certain moral, ethnic or religious issues, orthogonal to the provision of public goods. Examples are attitudes towards crime (gun control or capital punishment), drugs (i.e. whether to legalize the use of marijuana), immigration policies, pro-life or pro-choice positions, same sex marriage, etc. A value of zero indicates neutrality in terms of the ideological bias, so agents only care about the economic policy, while a positive value indicates that agent $j$ prefers party $B$ over $A$. Since $\phi^J$ can take positive or negative values, there are members in each group that are biased towards both candidates. Therefore, individuals belonging to the same group may vote differently.

The parameter $\psi$ represents a general bias towards party $B$ at each point in time. It measures the average relative popularity of candidates from that party relative to those from party $A$. While the realization of $\phi^J$ is individual-specific, the value of $\psi$ is the same for all agents. $^10$ It captures candidates’ personal characteristics such as honesty, leadership, integrity, charisma, trustworthiness, etc. Candidates with higher values of $\psi$ are preferable by all agents.

The popularity shock is iid over time and can also take positive or negative values. It is distributed according to:

$$\psi \sim \left[ -\frac{1}{2} + \eta, \frac{1}{2} + \eta \right].$$

A positive value for $\eta$ (the expected value of $\psi$) implies that candidates from party $B$ have an average popularity advantage over those from the opposition. On the other hand, $\eta = 0$ implies

$^10$Political scientists refer to this parameter as valence, referring to “issues on which parties or leaders are differentiated not by what they advocate but by the degree to which they are linked in the public’s mind with conditions or goals or symbols of which almost everyone approves or disapproves” (Stokes, 1992).
that parties are symmetric, in the sense that their candidates are expected to be equally popular or charismatic.

Finally, agents are assumed to have perfect information about the candidates, so there are no informational asymmetries in this model. At the election stage, voters compare their lifetime utility under the alternative parties. The maximization problem of voter \( j \) in group \( A \) is given by

\[
\max \left\{ V_A(K_g') , W_A(K_g') + \psi' + \varphi^{jA} \right\},
\]

where \( V_A(K_g') \) denotes the welfare of this agent if a candidate representing his group wins the elections, while \( W_A(K_g') \) is the value of his utility if the candidate representing group \( B \) is elected. The maximization problem of an agent in group \( B \) is analogously defined.

**Determination of probabilities**

Let’s turn now to the intermediate stage between taxation and voting, where the shocks have not yet been realized.

Individual \( j \in A \) votes for \( B \) whenever the shocks are such that

\[
V_A(K_g') < W_A(K_g') + \psi' + \varphi^{jA}.
\]

We can identify the swing voter in group \( A \) as the voter whose value of \( \varphi^{jA} \) makes him indifferent between the two parties

\[
\varphi^A(K_g') = V_A(K_g') - W_A(K_g') - \psi'.
\]

Figure 1 illustrates this point (assuming \( \psi = 0 \) for simplicity). The swing voter is found where the two solid lines intersect. All voters in group \( A \) with \( \varphi^{jA} > \varphi^A(K_g') \) also prefer party \( B \) as can be seen in the graph.

The same type of analysis can be performed for agents in group \( B \), to determine the swing voter in that group. The value of \( \varphi^J \) depends on the difference in utilities of having group \( A \) vs group \( B \) being in office and on the realization of the popularity shock.

Given the assumptions about the distributions of \( \varphi^{jA} \) and \( \varphi^{jB} \) the share of votes for party \( B \) is:

\[
\pi_B = \sum_J \mu^J P (\varphi^{jJ} > \varphi^{j}(K_g'))
\]

\[
= \frac{1}{2} - \sum_J \mu^J \varphi^{jJ} (K_g').
\]

Under majority voting, party \( B \) wins if it can obtain more than half of the electorate; that is, if \( \pi_B > \frac{1}{2} \). This occurs whenever its relative popularity is high enough. There exists a threshold for \( \psi \), denoted by \( \psi^*(K_g') \) such that \( B \) wins for any realization \( \psi > \psi^*(K_g') \). After performing some algebra using the expression above, we find that

\[
\psi^*(K_g') = \frac{1}{\phi} \left( \mu^A \varphi^A \left[ V_A(K_g') - W_A(K_g') \right] + \mu^B \varphi^B \left[ W_B(K_g') - V_B(K_g') \right] \right),
\]

where \( \phi = \mu^A \varphi^A + \mu^B \varphi^B \).

The threshold is given by a weighted sum of the differences in the utility of the swing voter under each party. The weights depend on the dispersion in the ideology shocks and on the amount of supporters that each party has. The higher the heterogeneity within a constituency (\( \varphi^J \)), the bigger the effect these factors have on the election outcomes. Also, the greater the number of
individuals belonging to type $J$, the stronger the group in the determination of the probability. Finally, note that the threshold depends on the level of public capital, though it is not clear in which direction. In principle, this level could increase or decrease with $K'_g$.

Since $\varphi'(K'_g)$ depends on the realized value of $\psi$, ex-ante the share of votes for party $B$ ($\pi_B$) is a random variable. $B$’s probability of winning the election is given by:

$$p_B(K'_g) = P\left(\pi_B > \frac{1}{2}\right) = P(\psi' > \psi^*(K'_g)),$$

which is equivalent to:

$$p_B(K'_g) = \frac{1}{2} + \left[\eta - \psi^*(K'_g)\right]. \quad (5)$$

$A$’s probability of winning the next election is just $p_A(K'_g) = 1 - p_B(K'_g)$.

Recall that $\eta$ represents the popularity advantage of candidates from party $B$ over those from party $A$. So in principle, $B$’s probability increases with $\eta$.

The current level of consumption in private and public capital does not affect the voting decision (i.e. no retrospective voting). Voters do not ‘punish’ politicians/parties for their past behavior but decide instead in terms of future expected policy choices.

**Production Stage**

At this stage firms decide how much labor to hire given wages, and distribute profits back in the form of dividends to agents, who own shares of these firms. Agents choose consumption and leisure, taking wages and government policy (public spending and investment) as given. A competitive equilibrium given policy is defined below, where we omit the stock of public capital $K_g$ from all functions to simplify the notation.

**Definition 1:** A competitive equilibrium given government policy $\Upsilon = \{g^A, g^B, K'_g\}$ is a set of allocations, $\{c_j(\Upsilon), n_j(\Upsilon), \Pi(\Upsilon)\}$, prices $w(\Upsilon)$, and taxes $\tau(\Upsilon)$ such that:

(i). Agents maximize utility subject to their budget constraint. Agent $j$’s labor supply satisfies

$$u_1(c_j(\Upsilon), n_j(\Upsilon))w(\Upsilon) + u_2(c_j(\Upsilon), n_j(\Upsilon)) = 0,$$

where

$$c_j(\Upsilon) = w(\Upsilon)n_j(\Upsilon) + \Pi(\Upsilon) - \tau(\Upsilon).$$

(ii). Firms maximize profits, so $w(\Upsilon) = F_2(K_g, n(\Upsilon))$ and $\Pi(\Upsilon) = F(K_g, n(\Upsilon)) - w(\Upsilon)n(\Upsilon)$.

(iii). Markets clear $n(\Upsilon) = \sum_J \mu^J n_J(K_g, \Upsilon)$.

(iv). The government budget constraint is satisfied.

$$\tau(\Upsilon) = \sum_J x(g^J) + K'_g - (1 - \delta)K_g.$$
firm’s optimal decisions and the government budget constraint into the agent’s budget constraint we obtain consumption as a function of policy,

\[ c(\Upsilon) = F(K_g, n(\Upsilon)) + (1 - \delta)K_g - \sum_J x(g^J) - K'_g, \]  

(6)

with labor as satisfying

\[ u_1(c(\Upsilon), n(\Upsilon))F_2(K_g, n(\Upsilon)) + u_2(c(\Upsilon), n(\Upsilon)) = 0. \]  

(7)

The last two expressions allow us to write agent’s indirect utility, since they summarize the private sector reaction to alternative policies.

**Taxation Stage**

At this stage, the incumbent must decide on the optimal policy knowing that he will be replaced by a different policymaker with some probability. Suppose that \( B \) is the elected party. Given the stock of public capital \( K_g \), his objective function today is:

\[
\max_{g^A, g^B, K'_g \geq 0} u(c, n) + v(g^B) + \xi_j + \beta\{p_B(K'_g)V_B(K'_g) + p_A(K'_g)W_B(K'_g) + E_B(\xi'_j; K'_g)\} 
\]

(8)

where consumption and labor satisfy equations (6) and (7), \( W_B \) denotes the utility of a type \( B \) agent when his party is out of power. \( E_B(\xi'_j, K'_g) \) represents the expected value of tomorrow’s political shock conditional on \( B \) winning the next election (recall that this shock is a relative bias towards a candidate form party \( B \)),

\[
E_B(\xi'_j; K'_g) = \int_{\frac{1}{2} + \eta}^{1+\eta} z \psi(K'_g) dz,
\]

which can be shown to be equal to

\[
E_B(\xi'_j; K'_g) = p_B(\xi'_j) \left[ \frac{1}{2} p_A(K'_g) + \eta \right].
\]

By changing the stock of public capital the incumbent affects not only the economic dimension but also his probability of winning and the expected value of political shocks.  

Since \( g^A \) and \( g^B \) only affect today’s utility, tomorrow’s decisions are independent of the composition of expenditures. If party \( i \) is in power, it will choose \( g^J_i = 0 \), for \( J \neq i \), which further simplifies the problem. Slightly abusing notation, we use \( g_i(K_g) \) to denote the equilibrium amount spent by incumbent \( i \) on the local public good \( i \). The description of the problem is completed by defining the functions \( V_B(K_g) \) and \( W_B(K_g) \):

\[
V_B(K_g) = u(c_B(K_g), n_B(K_g)) + v(g_B(K_g)) + \beta\{p_B(h_B(K_g))V_B(h_B(K_g)) + p_A(h_B(K_g))W_B(h_B(K_g)) + E_B(\xi'_j; h_B(K_g))\} 
\]

(9)

and

\[
W_B(K_g) = u(c_A(K_g), n_A(K_g)) + \]

(10)

11Other papers in the literature usually ignore political shocks because they study two period models, once the shock has been realized. Since \( \xi \) is additive, focusing on net-of-shock welfare is without loss of generality. In this paper, it would not be the case due to the fact that elections are held every period.
\[
\beta\{p_B(h_A(K_g))V_B(h_A(K_g)) + p_A(h_A(K_g))W_B(h_A(K_g)) + E_B(\xi'_j; h_A(K_g))\},
\]

where \( \Upsilon_i(K_g) = \{g_i^A(K_g), g_i^B(K_g), h_i(K_g)\} \) denotes the equilibrium policy functions chosen by incumbent type \( i \), and where \( c_i(K_g) = c(\Upsilon_i(K_g)) \) and \( n_i(K_g) = n(\Upsilon_i(K_g)) \) are the competitive equilibrium values of consumption and labor under the political equilibrium policies.

The choice of expenditures is a static one, affecting only the intra-temporal margin. At the optimum, the government chooses \( g \) so that the marginal cost of providing the good in terms of consumption equals its marginal benefit:

\[
u_1(c_B(K_g), n_B(K_g))x_g(g) = v_g(g). \tag{11}\]

We can see that government spending in the MPE is sub-optimal from the standpoint of an utilitarian social planner by comparing eq. (2) to the equality above. This is the case for two reasons. First, the group out of power gets no provision of their preferred good. Second, there is over-spending in the sense that the marginal rate of private consumption is too low when compared to that of the utilitarian optimum. Even the group in power would prefer a lower level of \( g \) if the difference was invested in productive capital and subsequently used in the provision of its preferred good instead.

The investment decision affects the inter-temporal margin; the costs of increasing public capital are paid today while the benefits are received in the future. The government chooses \( K'_g \) so that the marginal cost in terms of foregone consumption equals expected marginal benefits:

\[
u_1(c_B(K_g), n_B(K_g)) = \beta\{p_B(K'_g)V_B(K'_g) + p_A(K'_g)W_B(K'_g)
+ p_{B1}(K'_g) [V_B(K'_g) - W_B(K'_g)] + E_{B2}(\xi'_j; K'_g)\},
\]

where \( p_{B1}(K'_g) = \frac{\partial p_B(K'_g)}{\partial K'_g} \), and we use the fact that \( p_A = 1 - p_B \).

Even though parties represent their constituencies and have no derived value of being in office, they will try to manipulate the probability of being re-elected (which allows them to implement the desired policy in the future).

As in the planner's first-order condition, the cost of an extra unit of investment in public capital is given by a reduction in current utility via a decrease in consumption \(-u_1(c, n)\). The benefits, on the other hand, now depend on the identity of the party that wins the next election. When \( K'_g \) increases, expected future utility rises from the expansion of resources. Type \( B \) agents enjoy an increase of \( V_B(K'_g) = \frac{\partial v_B(K'_g)}{\partial K'_g} \) utilities if they win the next election (which occurs with probability \( p_B \)) and \( W_B(K'_g) = \frac{\partial W_B(K'_g)}{\partial K'_g} \) otherwise (which occurs with probability \( p_A = 1 - p_B \)). Given that the identity of the decision-maker changes over time, the envelope theorem doesn't hold in this environment, so the traditional Euler equation will not be satisfied. A change in investment today also modifies the problem faced by voters, which in turn affects the probability of being in power next period. A rational incumbent realizes this and thus takes into account the effect of expanding \( K'_g \) on its likelihood of winning. It is reasonable to expect that \( V_B(K'_g) > W_B(K'_g) \), a group is better off while in power. However, the sign of \( p_{B1}(K'_g) \) is, in principle, ambiguous. On the one hand, we expect that the richer the economy, the lower the political turnover (i.e. the probability of an incumbent losing the election decreases, so that the same party tends to stay in power longer). This would imply that by increasing the level of productive capital, the incumbent can tilt the election in its favor, which creates an extra indirect benefit of having more \( K'_g \). On the other hand, if \( p_{B1}(K'_g) \) was negative, the last term represents an indirect cost to investment inducing the incumbent to spend resources on non-productive activities instead. Spending on public capital would decrease not
only current consumption but also future utility via the indirect effect of reducing the probability of winning the next election.

**Politico-economic equilibrium**

We can now define a political equilibrium that takes into account agent’s voting decisions.

**Definition** A Markov-perfect equilibrium with endogenous political turnover is a set of value and policy functions such that:

i. Given the re-election probabilities and CE allocations and prices, the functions \( h_i(K_g), g_i^B(K_g), g_i^A(K_g), V_i(K_g), \) and \( W_i(K_g) \) solve incumbent \( i \)'s maximization problem, given by equations (8), (9), and (10).

ii. Given the re-election probabilities and government policy, the functions \( c_i(K_g) \) and \( n_i(K_g) \) satisfy equations (6) and (7).

iii. Given the optimal rules of the government and CE allocations and prices, \( p_B(K_g) \) solves eq. (5) and \( p_A(K_g) = 1 - p_B(K_g) \).

The definition just imposes consistency between private agents and government’s decisions at every stage (taxation, production, and election).

### 3.2 Differentiable Markov Perfect Equilibrium (DMPE)

In order to further characterize the trade-offs faced by an incumbent when choosing investment, I will focus on differentiable policy functions. Klein, Krusell, and Rios-Rull (2008) made this assumption (in a different context) arguing that there could be in principle an infinitely large number of Markov equilibria. By assuming differentiability, the problem delivers a solution that is the limit to the finite horizon problem. Moreover, it allows us to derive the government optimality condition:

**Proposition 1:** Define

\[
MC = u_1(c_B(K_g), n_B(K_g)),
\]

\[
EMB = \sum_i p_i(K_g)u_1(c_i(K_g'), n_i(K_g')) \left[ F_i(K_g', n_i(K_g')) + 1 - \delta \right],
\]

\[
SDE = -p_A(K_g')x_g(g_A(K_g'))g_{A1}(K_g')u_1(c_A(K_g'), n_A(K_g')),
\]

\[
IDE = h_{A1}(K_g')p_A(K_g')[-u_1(c_A(K_g'), n_A(K_g'))+u_1(c_A(K_g'), n_A(K_g'))], \text{ where } \bar{K}_g' = h_{B1}^{-1}(h_A(K_g')),
\]

\[
SME = p_{B1}(K_g')\left[V_B(K_g') - W_B(K_g')\right] + h_{A1}E_{B2}(\xi'_j; K_g').
\]

Incumbent \( B \)'s first order condition can be written as the sum of these terms

\[
MC = \beta\{EMB + SDE + IDE + SME\}. \tag{12}
\]

**Proof** See Appendix 7.1.

\[12\] Notice that this expression is not an Euler equation due to the fact that the probabilities depend on the value functions themselves.
The left hand side captures the fact that investing in public capital today involves incurring a marginal cost \((MC)\) in terms of current foregone consumption, while the right hand side of equation (12) is composed of the discounted sum of four effects of current actions into future outcomes. Utility is affected directly through the increase in expected marginal benefits and the spending and investment disagreement effects; and indirectly through the strategic manipulation effect.

The first effect in the optimality condition corresponds to the increase in expected marginal benefits \((EMB)\) caused by the increase in current public investment. Under no political uncertainty all other terms are zero, and the \(EMB\) coincides with that faced by a benevolent planner, as seen from equation (3). Because taxes are lump-sum, there are no distortions in the labor supply or other CE conditions. The effect of increasing \(K'\) in future investment would only be of second order and, due to the envelope theorem, there would be no need to keep track of it. The only distortions in this economy arise due to the presence of political uncertainty (i.e. the fact that \(p_i \neq 1\)) and the existence of group-specific public goods. Because parties’ constituencies differ, the reaction of the opposition to a change in \(K'\) will be sub-optimal from the standpoint of party \(B\) (due to the fact that both groups value the future differently) introducing a wedge relative to the first best.

The second term in the optimality condition, the spending disagreement effect \((SDE)\), captures the cost of disagreement in terms of public goods provision. When the incumbent is not re-elected (which happens with probability \(p_A\)), a marginal increase in public capital today changes the opposition’s spending in public goods tomorrow by \(g_{A1}(K'\)\). This reports a cost in terms of foregone consumption next period with no utility benefit since the incumbent derives no utility from that public good. From today’s perspective it is optimal, then, to decrease investment with respect to the certainty case: the current incumbent wants to ‘tie the hands’ of its successor in order to restrict its spending. The disagreement over the composition of public goods together with the political uncertainty deter investment.\(^{13}\)

If parties had the same political power \((p_A = p_B)\), the composition of expenditures would be the only source of disagreement. The center of the conflict would be what to spend the budget on, instead of how much to spend (as analyzed in detail in Azzimonti, 2010). All distortions would be summarized by the \(SDE\). Under asymmetry, there is also disagreement on the levels of spending and investment, as seen in the two effects described next.

The third term in the optimality condition captures the investment disagreement effect \((IDE)\), resulting from the fact that parties would invest differently if in power. To understand the intuition behind this effect, consider the case were party \(B\) is more likely to win an election \((p_B > p_A)\). Because the likelihood of staying in power is larger, the expected marginal benefits of investing one more dollar in public capital are higher than for party \(A\), who would only increase investment next period by \(h_{Ak}(K'\)\). This distorts future investment costs differentially for both parties introducing an additional distortion.

Finally, the last effect in eq. (12) is given by the strategic manipulation effect \((SME)\), that reflects the opportunistic behavior of the party in power. The first term in the SME incorporates marginal increases (or decreases) in the probability of winning the election due to increases in initial resources. Its second term takes into account how changes in today’s public capital alter the expected value of political shocks.

In order to shed some more light on the characterization of Markov perfect equilibria under political uncertainty, it is useful to analyze an example economy, where particular functional forms

\(^{13}\)This effect is similar to that observed in Persson and Svensson (1989). Besley and Coate (1998) find that disagreements over redistribution policies can result in inefficient levels of investment. Milesi-Ferreti and Spolaore (1994) also obtain strategic manipulation, but for an alternative environment. For an infinite horizon economy with symmetric shocks which also exhibits a disagreement effect see Azzimonti (2010).
are assumed and a closed form solution is derived.

4 An application

Under the following two assumptions regarding technology, preferences, and distribution of ideology it is possible to find an analytical solution. In this section, I characterize it and derive qualitative implications from the theory. Next, I discuss their validity by looking at empirical evidence.

Assumption 1: Suppose that:

i Technology is Cobb-Douglas \( F(K_g, n) = AK_g^\theta n^{1-\theta} \) with full depreciation, \( \delta = 1 \).

ii The cost of public goods is linear \( x(g) = g + G \) when \( g \geq 0 \) and \( x(0) = 0 \).

iii Preferences over consumption are of the GHH form

\[ u(c, n) = \log \left( c - \frac{n^{1+\frac{1}{\epsilon}}}{1+\epsilon} \right) \]

where \( \epsilon \) is the elasticity of labor, and

\[ v(g^J) = \log (g^J + G). \]

It is instructive to analyze the Pareto optimal allocations first, obtained by solving equations (2) and (3) presented in Section 2.2. Under the assumptions above the economy collapses to a traditional neoclassical economy, so the standard results apply. There exists a unique equilibrium where the labor supply takes a simple form,

\[ n(K_g) = \left[ \epsilon A(1-\theta)K_g^{\theta} \right]^{\frac{\epsilon}{1+\epsilon}}, \]

and the level of production is given by

\[ F(K_g, n(K_g)) = \tilde{A} K_g^{\theta} \text{ where } \tilde{A} = A[\epsilon A(1-\theta)]^{\frac{\epsilon(1-\theta)}{1+\epsilon}} \text{ and } \bar{\theta} = \frac{\theta(1+\epsilon)}{1+\epsilon}. \]

Public capital evolves according to

\[ K_g' = s^* \tilde{A} K_g^{\theta}, \text{ with } \tilde{A} = \tilde{A} - \frac{\epsilon A(1-\theta)}{1+\epsilon}, \]

where \( \tilde{A} K_g^{\theta} \) equals the total amount of resources net of the disutility of labor, and we can think of it as 'labor-adjusted' production. A benevolent planner invests a constant proportion \( s^* = \beta \bar{\theta} \) of labor-adjusted resources, independently of the Pareto weights attached to each group (these weights only affect the composition of region-specific public goods but not the total amount of resources devoted to them). Since \( \bar{\theta} < 1 \), public capital converges deterministically to a steady state level \( K_g^* = [\beta \bar{\theta} \tilde{A}]^{\frac{1}{1-\theta}} \).
4.1 Dynamic inefficiencies in the MPE

In order to characterize the political equilibrium we will make more specific assumptions regarding the process that drives ideology shocks.

**Assumption 2:** Both parties have identical political power $\mu^A \phi^A = \mu^B \phi^B \equiv \mu \phi$ but party $B$ may have a popularity advantage $\eta \geq 0$.

Recall that $\psi$ represents the popularity of party $B$ relative to party $A$. When $\eta = 0$ both parties are completely symmetric. If on the other hand $\eta > 0$, party $B$ has an average popularity advantage over party $A$, creating an asymmetry in their likelihood of retaining power.

The competitive equilibrium given policy determines consumption and labor as functions of government spending and investment. The labor supply follows eq. (13), due to the fact that taxes are lump sum and there are no income effects under the GHH formulation. Consumption satisfies

$$c_i(K_g) = \bar{A}K_g - \bar{\theta} g_i(K_g) - G - h_i(K_g).$$

Under our functional assumptions, the probabilities of winning an election are independent of the stock of capital $K_g$. They are however functions of the marginal propensities to invest, as shown in Proposition 2, which fully characterizes government policy.

**Proposition 2:** Under Assumptions 1 and 2, there exists a differentiable Markov equilibrium where incumbent $i$ chooses:

$$g_i(K_g) = \frac{1}{2}(1 - s_i)\bar{A}K_g^\theta - G$$

and

$$h_i(K_g) = s_i\bar{A}K_g^\theta,$$

and the propensity $s_i$ satisfies

$$s_i = \frac{\bar{\theta} \beta}{2 - \theta \beta} \left[ \frac{1 + p_i}{1 - p_i} \right]. \quad (14)$$

The probabilities of reelection are $p_B = \frac{1}{2} + [\eta - \psi^*(K_g)]$ and $p_A = 1 - p_B$, where

$$\psi^*(K_g) = \frac{3}{2} \left[ \ln \left( \frac{1 - s_A}{1 - s_B} \right) + \frac{\bar{\theta} \beta}{1 - \theta \beta} \ln \frac{s_A}{s_B} \right]. \quad (15)$$

**Proof** See Appendix 7.2.

An incumbent of type $i$ invests a constant proportion of labor-adjusted resources, with the propensity to invest being a function of the probability of reelection. The next Corollary summarizes the effect of political uncertainty on government policy.

**Corollary 1:** The Markov-perfect equilibrium is Pareto efficient if and only if $p_i = 1$. When $p_i < 1$ there is under-investment in public capital $s_i < s^*$, so the MPE is inefficient.

The intuition behind this result can be understood by looking at the trade-offs faced by the group in power. An incumbent who believes that he will be replaced with high probability does not have strong incentives to abstain from consumption today in order to invest in public capital. Knowing that it is very likely that tomorrow’s policymaker would prefer a different composition of spending, the incumbent tries to manipulate next period’s policy through the choice of the state variable. He can ‘tie the hands’ of his successor by decreasing the amount of available resources (i.e. investing a small amount today), which shrinks the tax base in the future. It is then reasonable
to expect the propensity to invest under political uncertainty to be lower than that chosen by a planner.

**Corollary 2:** *Stable economies exhibit higher public investment as a fraction of GDP, and lower expenditures in region-specific public goods and transfers.*

The benefits from an extra unit of investment are not fully internalized, which causes the incumbent to behave *myopically* and over-spend today on unproductive public goods (and under-invest in public capital). The effect is stronger the lower the probability of remaining in power. We should observe that economies with high political turnover (frequent changes of power) present a bias towards spending and relatively low levels of investment in infrastructure, education, public health or other productive activities.

As we can see from Proposition 2, there is also feedback from policy decisions to political turnover since the probabilities of winning an election are in turn functions of the propensities to invest. If $s_B > s_A$, forward-looking voters realize that candidates from party $B$ spend relatively more resources in productive activities than the opposition. This increases $B$'s chances of re-election. On the other hand, higher investment in public capital implies more taxes and lower consumption than under party $A$. This force pushes down the likelihood of $B$ being re-elected. Overall it is not clear whether $p_A \leq p_B$ when $s_B > s_A$.

In equilibrium, probabilities of re-elections are jointly determined with propensities to invest. We have a system of four non-linear equations in four unknowns ($p_A, p_B, s_A$ and $s_B$). From Proposition 2 it is clear that if $\eta = 0$ then the equilibrium is symmetric with $s_A = s_B$ and $p_A = p_B = \frac{1}{2}$. Proposition 3 establishes that when $\eta > 0$ the equilibrium will be asymmetric.

**Proposition 3:** *Let $\eta > 0$. Then party $B$ has a popularity advantage, and as a result it invests more and it is re-elected more often than the opposition*

$$s_A < s_B < s^* \quad \text{and} \quad p_A < p = \frac{1}{2} < p_B.$$

**Proof:** see Appendix 7.3

When $\eta > 0$, party $B$ has an advantage over $A$ because positive realizations of the popularity shock are more likely. This tilts the utility of all voters in $B$'s favor, which in turn increases the probability of winning the next election. From the optimality condition eq. (12), this creates incentives to invest more. The opposite occurs with party $A$. Given his low chances of being in power next period, the incumbent is inclined towards unproductive expenditures. In this example, we see a *virtuous circle*: if individuals believe that one party has on average ‘better’ candidates (on aspects orthogonal to the management of economic policy), the strategic effects imply that they will indeed behave ‘better’ in choosing policy (overspend less on the unproductive region-specific goods). Despite the fact that $B$’s investment decision is closer than $A$’s decision to the one that would be undertaken by a planner, $B$’s saving propensity is lower than the first best, $s^*$. This is a result of the short-sightedness created by the political uncertainty and the disagreement over the composition of expenditures.

This result implies that some caution should be taken when inferring unobservable characteristics from observable actions in at least two respects. First, because the source of asymmetry is completely unrelated to how ‘competent’ candidates from different parties are. Suppose that we observe an economy where the average level of output and investment on infrastructure is higher.
under one of the parties, while spending on unproductive activities is lower. It would be incorrect to infer that candidates belonging to such party are more ‘capable’ or ‘efficient’ in dealing with economic issues. This observed outcome could be the result of equilibrium actions consistent with our model, where even though parties have identical investment technologies, political considerations make them choose different strategies. Second, because preferences over productive and unproductive spending are completely symmetric here. In the absence of political advantages both parties would invest equal proportions of available resources while spending the same amount on public goods. The difference in policy choices in the asymmetric case is a result of strategic considerations and does not rely on preference spending biases (i.e. differences in the weights each group assigns to public good provision).

**Corollary 3:** Increases in party B’s popularity advantage \( \eta \) result in higher probability of winning an election and propensity to invest for this party, while it reduces the opposition’s chances of gaining power and its incentives to invest in public goods. Formally,

\[
\frac{\partial p_B}{\partial \eta} > 0, \quad \frac{\partial s_B}{\partial \eta} > 0, \quad \frac{\partial p_A}{\partial \eta} < 0 \quad \text{and} \quad \frac{\partial s_A}{\partial \eta} < 0.
\]

An increase in B’s popularity advantage widens the asymmetry between the two parties. Foreseeing an even lower probability of regaining government control, party A chooses to spend a larger proportion of tax revenues whenever in power.

### 4.2 Ideology driven business cycles

An interesting feature of this model is that it delivers endogenous cycles in economic variables generated by parties’ alternation of power. Even though there are no exogenous productivity shocks, output, investment, consumption, labor, and taxes fluctuate in the long run.

From the government’s maximization problem, the evolution of public capital follows

\[
K_g^t = s_i \bar{A} K_g^\theta
\]

where \( s_i \in \{s_A, s_B\} \) depends on the identity of the incumbent. If party \( i \) were in power long enough, capital would approach \( K_{gs} = [s_i \bar{A}]^{1- \theta} \). When parties alternate in power, public investment fluctuates following the political cycle. Since public capital affects the productivity of the private sector, other macroeconomic variables (such as labor, output, and consumption) also fluctuate, with political shocks propagating into the real economy. The following corollary summarizes the evolution of capital.

**Corollary 4:** Consider an economy with \( K_{g0} < K_{A}^{ss} \). Then capital increases at a fast (but not constant) rate following the political cycle. Eventually, the economy converges to an ergodic set. Once there, capital fluctuates around a constant mean. Moreover, the economy is inefficient.

If the government were always to follow B’s optimal investment rule, \( K_g \) would evolve according to the upper line in Figure 2, converging eventually to \( K_{gB}^{ss} \) (where B’s policy function intersects the 45 degree line). If A’s rule was followed instead, not only would the steady state be lower (\( K_{gA}^{ss} < K_{gB}^{ss} \)) but convergence would take place at a slower pace. Under political uncertainty the evolution of capital is stochastic. A possible path is represented by the arrows in Figure 2.

Eventually, the economy reaches an ‘ergodic set’ in which public capital only takes values belonging to the interval \( (K_{gA}^{ss}, K_{gB}^{ss}) \). Once there, all macroeconomic variables evolve cyclically.
Figure 3 depicts a series of investment for a simulation of this economy (the parameters used are described in detail in the next section). It also shows the evolution of capital that would be followed by a benevolent planner. We can see that a planner reaches a significantly higher steady state.

Figure 4 depicts the evolution of investment and spending in region-specific goods for a period of time once the economy has reached its ergodic set.

We can see that the economy experiences booms when $B$ is in office and short periods of recession when $A$ happens to win an election. For example, consider what happens after $t=7$, when group $B$ takes office. There is an immediate jump in investment and a contraction of expenditures. This results in larger levels of public capital, and hence more production. Government investment grows over time (periods 7 to 13) and, as public capital becomes larger, the amount provided of the public good also increases. Group $A$ gets into power in period 14 and we can see that the expenditures in public goods has a boost accompanied by a contraction of investment. An empirical implication from this analysis is that we should observe a jump in unproductive expenditures when a party that doesn’t win often takes power, together with a sudden decrease in investment. Notice that the nature of the economic cycle is then intrinsically different from the one found in traditional partisan cycle models, where one of the parties is assumed to derive higher utility from public goods than the other. It would then be inaccurate to label parties as being ‘right’ or ‘left’ just because they are observed to choose opposite investment and spending decisions.

Quantitative implications

To shed some more light on the propagation effect of ideology driven cycles I simulate the economy for a specific parameterization. A time period represents a year, so the discount factor is $\beta = 0.95$. Following Greenwood, Hercowitz and Huffman (1988) I assume the elasticity of labor supply $\epsilon$ equal to 2. The level of productivity $A$ is normalized to one. There are three non-standard parameters in this model: the elasticity of public capital $\theta$, the fixed cost of providing public goods $G$, and the popularity advantage $\eta$. I choose the three parameters so that simulated moments at the political equilibrium match three target moments in the data. The first target is mean non-defense public investment as a proportion of GDP in the US for the period 1929-2006 ($GNDI/Y$). The second target is average non-defense public consumption as a proportion to output, for the same time period ($GNDC/Y$). All figures are obtained from the NIPA tables. The third target is computed so that the equilibrium advantage of party $B$, given by $p_B - p_A$ in the model, matches the average advantage obtained by the Democrats during all congressional elections to the House of Representatives between 1929 and 2006 ($AD$). The variable is computed as follows. Let $sh_t(i) = \frac{i}{D_t + R_t}$ denote the share of seats obtained by party $i \in \{R, D\}$ at the House of Representatives in Congress $t \in \{70^{th}, \ldots, 109^{th}\}$ (that is, covering the period 1929-2006). Following Diermeier, Keane and Merlo (2004) the advantage of party $D$ at each period of time is simply $Adv_t = sh_t(D) - sh_t(R)$. I then average out these values over the whole sample period.

I simulated the political equilibrium for 5000 periods and discarded the first 1000 to eliminate the effects of initial conditions. Table I summarizes the value of the parameters obtained from the calibration, together with the target variables.

The value of $\theta$ is in line with empirical estimates and close to the estimate used in Baxter and King (1993), who set the elasticity of public capital to 0.05. While they use the same target—public investment as a ratio of output—to calibrate the model, their measure of investment includes defense expenditures while mine excludes them. If I were to include defense expenditures as well, I would obtain a value closer to Baxter and King’s. The parameter $G$ captures expenditures that have not been modeled (such as defense spending). To the extent of my knowledge, this is the first
time an attempt to estimate the parameter $\eta$ is done in a calibrated political economy model, so there is no counterpart in the literature. As we will see in the next section, assuming a constant value for $\eta$ is clearly a simplification, since its value has fluctuated over the time interval (however, using a stochastic popularity advantage would complicate the solution presented in this paper, and it is left for an extension).  

The size of fluctuations

Table II summarizes the politically induced volatility (first row) and cyclicality (second row) generated by the model for a set of variables of interest, computed from the simulation. The objective of this exercise is to analyze the amplification effect of political shocks. To make this analysis stark, I am assuming away real business cycles shocks to productivity and only considering the effect of power changes (hence, a direct comparison of the values obtained with moments from the data is meaningless).

From the theoretical section of this paper, we know that switches of power cause policy changes (taxes, spending and investment), which in turn induce fluctuations in macroeconomic variables. Public investment is slightly more volatile than public spending in the political equilibrium, as evident by comparing columns 3 and 4 in Table II. The labor supply is affected directly by changes in public capital. Output on the other hand, is directly affected by public investment and indirectly by labor. As a result, output is more volatile than $n$ and $I_g$. We can also see that both public spending and public investment are procyclical, with spending being more correlated with output than investment is. This can be understood by looking back at Figure 4. Whenever the party enjoying popularity advantage gains power, investment increases. This rises the level of output next period and increases the amount of resources that can be devoted for public spending. Because this party stays on average longer in power, $y$, $g$, and $I_g$ tend to move in the same direction. Finally, consumption is highly correlated with output because agents do not have access to capital markets in this model (ie they cannot save). Analyzing the effect of political shocks on private investment would be an interesting extension to this paper.

The effect of $\eta$

Consider an increase in the value of $\eta$ in the neighborhood of zero. From Corollary 3 we know that, everything else constant, the probability of re-election of party $B$ rises. Therefore, if the incumbent belongs to that group, he is more likely to be succeeded by a candidate of his own type and has incentives to invest more resources in productive activities. If $A$ was in power instead, a higher value of $\eta$ would decrease this party’s probability of staying in power, so the short-sightedness would be strengthened, resulting in a propensity to invest even further away from the first best. Numerically, we can show that this result extends to all values of $\eta$ for which $B$’s probability of winning an election belongs to the interval $[0, 0.5, 1]$.

Figure (5) illustrates that the relationship between popularity bias and the volatility of the economic and political variables of interest is non-monotonic.

The reason is that there are two opposing forces driving these volatilities. One is given by the gap between the propensities to save of each party, which increases the volatility of policy and allocations. The other force is political stability, which reduces it. When $\eta = 0$, both parties are completely symmetric. Even though political turnover reaches its maximum value (with $p_A = p_B = 0.5$), the gap is zero (since $s_A = s_B$) so there are no fluctuations in policy or economic variables. As

\[\text{See Battaglini (2010) for an environment where a party’s advantage changes over time in a symmetric environment with commitment.}\]
\( \eta \) increases, the marginal propensity to invest of type \( A \) falls below the symmetric level, while that of type \( B \) lies above that value. Hence, the gap in the marginal propensities to invest is widened and volatility rises. For small deviations from symmetry, this effect dominates that of political stability. Eventually, \( \eta \) becomes large enough that even though the gap between \( s_A \) and \( s_B \) is large, political turnover is very infrequent. Since \( B \) is in power most of the time, policy remains stable and volatility goes down.

This result provides a testable implication of the model. Countries where parties are very symmetric (ie there is almost no popularity advantage for any of them) will exhibit frequent turnover, but little volatility in policy variables. We should also expect low variability in countries where turnover is infrequent. Fluctuations are biggest for those with intermediate values of the ideology bias.

5 Empirical support

A main point of this paper is that political turnover introduces fluctuations in macroeconomic variables via changes in policy when one party has a popularity advantage over the opposition.

One implication of the model is that a country should grow faster when the more popular party is in power. Alesina and Roubini (1997) provide some evidence of this by computing an average growth rate of output of 4.24% under a Democratic government and of 2.41% under a Republican one in the US (for the sample 1949-1994). In a standard regression, they found that a change of regime to a Republican (Democratic) administration, leads to a fall (increase) in output growth (even after controlling for differences in the exchange rate system, shocks from the rest of the world, etc.). The effects of a change in regime also hold for a sample of industrial (and bipartisan) countries.

Another prediction is that as popularity advantage \( \eta \) goes up, the share of total expenditures devoted to investment increases (while that of public consumption decreases). The bars in Figure 6 represent the variable \( Adv_t \) (described in detail in the previous section) whose changes proxy for movements in \( \eta \), the popularity advantage of the Democratic party over the Republican party during the period 1929-2006. We can see that Democrats experienced an average advantage since the series is positive for most of the sample. Because this advantage has not been constant over time, it is possible to test our prediction by analyzing how changes in popularity affect the share of public investment.

In order to estimate the investment share as close to the model as possible, I computed it as the ratio of public investment to government spending,

\[
\text{Investment Share} = \frac{GNDI}{GNDI + GNDC},
\]

where \( GNDI \) stands for real non-defense public investment and \( GNDC \) for real non-defense public consumption. Both series are obtained from the NIPA tables, and deflated by their respective deflator. Notice that I am not using government revenues or total expenditures since the model does not include debt. The investment share is HP-filtered with \( w=100 \) (due to its annual frequency), and represented by a line in Figure 6. We can see that the popularity advantage and the investment share are positively related. A correlation coefficient of 0.25 provides support for the theory. \(^{15}\)

\(^{15}\)I must note that the value of \( Adv_t \) represents the average number of seats at the end of the \( t^{th} \) Congress. If I were to correlate the investment share with the popularity advantage at mid-Congress the correlation would decrease to 0.18.
Concluding Remarks

I presented a model where disagreements about the composition of spending results in implementation of myopic policies by the government: investment in infrastructure is too low while spending on public goods is too high. Groups with conflicting interests try to gain power in order to implement their preferred fiscal plan. Since there is a chance of being replaced by the opposition, strategic manipulation of the level of investment is optimal. In particular, the incumbent invests so as to restrict spending in the future and to maximize his group’s probability of staying in power. In contrast to previous models, the degree of ‘impatience’ of the government is endogenous here and depends on preferences and technology. The forces that drive short-sightedness are disagreement of consecutive governments, political uncertainty, and the induced lack of commitment.

I considered a case where ideological biases towards candidates from one of the groups gives them an advantage in the political arena. As a result, the voting equilibrium is asymmetric and public investment is not only inefficiently low but it also fluctuates. The group with the advantage wins elections more often becoming less impatient, so it chooses a share of investment to GDP closer to the first best. Even though both groups have symmetric preferences over the size of spending and investment, in equilibrium the group with the disadvantage tends to spend more and invest less. The political cycle is propagated into the real economy, so as parties alternate in power, different policies are implemented. In equilibrium, macroeconomic variables fluctuate even in the absence of economic shocks. Moreover, consumption, employment and output are distorted despite the fact that the government has access to lump-sum taxation.

Increases in the ideological bias induce rises in the share of public investment to total expenditures by the group that has the advantage. I show that this is roughly consistent with evidence from the US for the period 1929-2006. In a calibrated economy I quantified the size of the politically induced business cycle and showed that volatility is non-monotonic in the degree of ideological biases. Economies with intermediate values of this variable are expected to exhibit the largest volatility in political and economic variables.
7 Appendix

7.1 Proof of Proposition 1

The FOC with respect to $K'_g$ is:

\begin{equation}
    u_1(c_B(K_g), n_B(K_g)) = \beta \{ p_B(K'_g)V_{B1}(K'_g) + p_A(K'_g)W_{B1}(K'_g) \}
    + p_{B1}(K'_g) \left[ V_B(K'_g) - W_B(K'_g) \right] + E_{B2}(\xi'_g; K'_g),
\end{equation}

where $p_{B1}(K'_g) = \frac{\delta p_B(K'_g)}{\delta K'_g}$. Denote the rule that solves this functional equation by $h_B(K_g) \equiv K_B$. Define $h_A(K_g) \equiv K_A$ analogously.

Focus on the problem of party $B$ (and abstract from the subindexes in its value function). Obtain $V_1(K_g)$ by differentiating equation 9 and simplifying:

\begin{equation}
    V_1(K_g) = u_1(c_B(K_g), n_B(K_g))\left[F_1(K_g, n_B(K_g)) + 1 - \delta \right].
\end{equation}

To find $W_1(K_g)$ differentiate equation (10):

\begin{align*}
    W_1(K_g) &= u_1(c_A(K_g), n_A(K_g))c_A(K_g) + \beta h_A(K_g) \left\{ p_{B1}(K_A)\left[ V(K_A) - W(K_A) \right] \\
    &+ p_{B}(K_A)V_1(K_A) + p_A(K_A)W_1(K_A) + E_{A2}(\xi'_A; K_A) \right\},
\end{align*}

\begin{equation}
    \text{where } c_A(K_g) = F_1(K_g, n_A(K_g)) + 1 - \delta - x_g(g_A(K_g))g_A1(K_g) - h_A(K_g).
\end{equation}

Notice that allocations are evaluated given party $A$’s policy, because we are considering the value function of a type $B$ agent when his group is out of power.

Use eq. (16) to solve for $W_1(h_B(K_g))$: \begin{equation}
    W_1(K_g) = \frac{1}{p_A(K_B)} \left\{ \frac{1}{\beta} u_1(c_B(K_g), n_B(K_g)) - p_B(K_B)V_1(K_B) \right\},
\end{equation}

In order to replace the equation above in eq. (18) we need the value function to be evaluated in the investment choice of government $A$, $W_1(K_A)$. Assuming that the functions $h_i$ are invertible, we can achieve this by evaluating eq. (19) at $K_g = h_B^{-1}(h_A(K_g))$, \begin{equation}
    W_1(K_A) = \frac{1}{p_A(K_A)} \left\{ \frac{1}{\beta} u_c(c_B(K_g), n_B(K_g)) - p_B(K_A)V_1(K_A) \right\}
    - p_{B1}(K_A) \left[ V(K_A) - W(K_A) \right] - E_{B2}(\xi'_B; K_B).
\end{equation}

Replace eq. (20) into eq. (18) and simplify:

\begin{equation}
    W_1(K_g) = u_1(c_A(K_g), n_A(K_g))\left[F_1(K_g, n_A(K_g)) + 1 - \delta - x_g(g_A(K_g))g_A1(K_g) \right]
    - h_A(K_g) [u_1(c_A(K_g), n_A(K_g)) - u_c(c_B(K_g), n_B(K_g))],
\end{equation}

Update eq.(21) by substituting $K_g$ with $K'_g = h_B(K_g)$ and replace in eq.(16). After some manipulations obtain

\begin{equation}
    u_1(c_B(K_g), n_B(K_g)) = \beta \sum_{i=A,B} \frac{p_i(K'_g)u_1(c_i(K'_g), n_i(K'_g))\left[F_1(K'_g, n_i(K'_g)) \right] + 1 - \delta}.
\end{equation}
\[-p_A(K_g')x_g(g_A(K_g'))g_{A1}(K_g')u_1(c_A(K_g'), n_A(K_g')) \]
\[-h_{A1}(K_g')p_A(K_g')[u_1(c_A(K_g'), n_A(K_g')) - u(c_B(\tilde{K}_g'), n_B(\tilde{K}_g'))] \]
\[+p_{B1}(K_g') [V(K_g') - W(K_g')] + E_{B2}(\xi_j; K_g'). \]

### 7.2 Proof of Proposition 2

Guess a constant probability \( p_i(K_g) = p_i \) and a constant investment share \( h_i(K_g) = s_i \tilde{A}K_g^{\bar{q}} \). Eq. (11) implies:

\[ g_B(K_g) = \hat{c}_B(K_g) = \frac{1}{2}(1 - s_B)\tilde{A}K_g^{\bar{q}}. \]

with \( \hat{c}_B(K_g) = c_B(K_g) - \frac{n_B(K_g)^{1+\epsilon}}{1+\epsilon} \). Equation (12) simplifies to reduces to:

\[
\frac{1}{\hat{c}_B(K_g)} = \beta \left\{ p_B \frac{f_K(K_g')}{\hat{c}_B(K_g')} + (1 - p_B) \frac{[f_K(K_g') - g_{BK}(K_g')]}{\hat{c}_A(K_g')} \right\} + (1 - p_B)h_{AK}(K_g') \left[ -\frac{1}{\hat{c}_A(K_g')} + \frac{1}{\hat{c}_B(K_g')} \right].
\]

where \( K_g' = h_B(K_g) = s_B \tilde{A}K_g^{\bar{q}} \) and \( \hat{c}_B(K_g') = \frac{1 - s_B}{2}s_A \tilde{A}K_g^{\bar{q}} \).

Replacing the guess into the equation above and simplifying,

\[ s_B = \frac{\beta \bar{q}(1 + \bar{p}_B)}{2 - \beta \bar{q}(1 + \bar{p}_B)}. \tag{23} \]

This verifies that if \( p_i \) constant \( \Rightarrow s_i \) constant.

To verify that \( p_i \) is constant, note that the value functions satisfy

\[ V_j(K_g) = \tilde{\nu}_j + \nu_j \ln(K_g). \tag{24} \]
\[ W_j(K_g) = \tilde{\omega}_j + \omega_j \ln(K_g), \tag{25} \]

where

\[ \nu_j = \frac{\bar{\theta}(2 - \bar{\theta} \beta p_i)}{1 - \bar{\theta} \beta} \quad \text{and} \quad \omega_j = \frac{\bar{\theta}(1 + \bar{\theta} \beta p_i)}{1 - \bar{\theta} \beta}, \]

\[ \tilde{\nu}_j = \frac{1}{1 - \beta} \left\{ \beta (1 - p_j) \left[ \ln \left( \frac{1}{2}(1 - s_j)\tilde{A} \right) + \beta [p_j \nu_j + (1 - p_j)\omega_j] \ln(s_j\tilde{A}) \right] + [1 - \beta (1 - p_j)] \left[ 2\ln \left( \frac{1}{2}(1 - s_j)\tilde{A} \right) + \beta [p_j \nu_j + (1 - p_j)\omega_j] \ln(s_j\tilde{A}) \right] \right\}, \]

\[ \tilde{\omega}_j = \frac{1}{1 - \beta (1 - p_j)} \left\{ \ln \left( \frac{1}{2}(1 - s_j)\tilde{A} \right) + \beta [p_j \tilde{\nu}_j + p_j \nu_j + (1 - p_j)\omega_j] \ln(s_j\tilde{A}) \right\}. \]

Replace eq.(24) and eq.(25) into eq.(4) to obtain the expression that determines \( \psi^*(K_g) \).

Finally, we verify that probabilities are constant and that governments choose to invest a proportion of output. Notice that these rules are increasing in capital, differentiable and invertible.
7.3 Proof of Proposition 3

The Proof will be done in two steps.

**Step 1:** Let $\eta = 0$. Then, there exists a symmetric solution.

Substitute eq. (14) into eq. (15), and evaluate at $p_A(K_g) = \frac{1}{2} - \eta + \psi^*(K_g')$ to obtain

$$p_A = \frac{1}{2} - \eta + \frac{3}{2} \left\{ \ln \left( \frac{2 - \theta \beta p_A}{2 - \theta \beta (1 - p_A)} \right) + \frac{\theta \beta}{1 - \beta \theta} \ln \left( \frac{1 + p_A}{2 - \theta \beta (1 - p_A)} \right) \right\}. \quad (26)$$

At $\eta = 0$, $p_A = \frac{1}{2}$ solves equation (26). Replace this into eq. (14) to obtain $s_A = s_B$.

**Step 2:** Let $\eta > 0$. Then, there exists an asymmetric solution.

The LHS of equation (26) is increasing in $p_A$. The RHS is also increasing in $p_A$ for any $p_A \in [0, 1]$ since

$$\frac{\partial \text{RHS}(p_A)}{\partial p_A} = \frac{3}{2} \theta \beta \left( \frac{p_A}{(2 - \theta \beta p_A)(2 - p_A)} + \frac{1 - p_A}{(2 - \theta \beta (1 - p_A))(1 + p_A)} \right) > 0.$$  

From Step 1, there exists a solution at $\eta = 0$. Now let $\eta > 0$. The LHS remains unchanged and the RHS shifts to the left. Hence $p_A < \frac{1}{2}$ and $p_B > \frac{1}{2}$. Replace these in eq. (14) for $i = \{A, B\}$ to see that $s_A < s_B$.

References


8 Tables and Figures

<table>
<thead>
<tr>
<th>Variable</th>
<th>Parameter</th>
<th>Target</th>
<th>Target Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elasticity of public investment</td>
<td>$\theta$</td>
<td>Public Investment/Output</td>
<td>$GNDI/Y = 2.88$</td>
</tr>
<tr>
<td>Fixed cost of public goods</td>
<td>$G$</td>
<td>Public Spending/Output</td>
<td>$GNDC/Y = 13.84$</td>
</tr>
<tr>
<td>Popularity advantage</td>
<td>$\eta$</td>
<td>Democrat advantage</td>
<td>$AD = 0.145$</td>
</tr>
</tbody>
</table>

Table I: Calibration targets.

<table>
<thead>
<tr>
<th>Moment</th>
<th>$Y$</th>
<th>$c$</th>
<th>$I_g$</th>
<th>$g$</th>
<th>$n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>St. Dev</td>
<td>1.15</td>
<td>0.94</td>
<td>0.30</td>
<td>0.24</td>
<td>0.89</td>
</tr>
<tr>
<td>Corr ($Y,x$)</td>
<td>1.00</td>
<td>0.98</td>
<td>0.13</td>
<td>0.78</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Table II: Political cycle moments

Figure 1: Utility as a function of $\varphi^{jA}$
Figure 2: Evolution of capital: asymmetric case

Figure 3: Evolution of capital: asymmetric case
Figure 4: Understanding the cycle

Figure 5: Volatility of output, public investment and spending as a function of $\eta$
Figure 6: Popularity advantage and investment share, 1929-2006