The Escape-Infringement Effect of Blocking Patents on Innovation and Economic Growth

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December 2010

Online at https://mpra.ub.uni-muenchen.de/27233/
Abstract

This study develops a Schumpeterian growth model to analyze the effects of different patent instruments on innovation. We first analyze patent breadth that captures the traditional positive effect of patent rights on innovation. Then, we consider a profit-division rule between entrants and incumbents. Given the division of profit, increasing the share of profit assigned to incumbents reduces entrants’ incentives for innovation. This aspect of blocking patents captures the recently proposed negative effect of patent rights on innovation. Finally, blocking patents generate a non-monotonic effect on innovation when the step size of innovation is endogenous due to a novel escape-infringement effect. Calibrating the model to aggregate data, we find that a marginal increase in the blocking effect of patent protection is likely to raise economic growth.

JEL classification: O31, O34, O40
Keywords: economic growth, innovation, intellectual property rights
1 Introduction

The traditional understanding is that secure patent rights enhance the private return to R&D investment. According to this argument, stronger patent rights should increase innovation and economic growth. However, many economists, such as Bessen and Meurer (2008), Boldrin and Levin (2008) and Jaffe and Lerner (2004), have recently raised doubt against this traditional viewpoint on patent protection. According to this recent argument, stronger patent rights reduce innovation by increasing the power of existing patent holders, who use their enhanced power to extract surplus from subsequent innovators rather than providing more innovation. In this note, we develop a Schumpeterian growth model to analyze the effects of different patent instruments on innovation and economic growth. The first patent instrument that we analyze is patent breadth that captures the traditional positive effect of patent rights on innovation. Then, we consider a profit-division rule between entrants and incumbents. Given the division of profit, increasing the share of profit assigned to incumbents reduces entrants’ incentives for innovation, and this aspect of blocking patents captures the recently proposed negative effect of patent rights on innovation. Finally, we show that blocking patents generate a non-monotonic effect on innovation when the step size of innovation is endogenous due to an escape-infringement effect that is often neglected in the patent literature.

Intuitively, in the presence of blocking patents, entrants would develop more substantial innovations in order to avoid infringing the patents of incumbents. Therefore, although blocking patents generate a negative effect by reducing the arrival rate of innovation, they also generate a positive effect by increasing the step size of innovation. Combining these positive and negative effects of blocking patents gives rise to an inverted-U relationship between patent rights and innovation that has been documented in recent empirical studies, such as Lerner (2009) and Qian (2007). We also calibrate the model to aggregate data in order to quantify the effect of blocking patents, and we find that a marginal increase in the blocking effect of patent protection is likely to raise economic growth.

This study relates to the microeconomic literature on optimal patent design. In this literature, the seminal study is Nordhaus (1969), who shows that the optimal patent length should balance between the social benefit of innovation and the social cost of monopolistic distortion. Scotchmer (2004) provides a comprehensive review on the subsequent developments in this
patent-design literature. In this literature, an interesting and important policy lever is forward patent protection that gives rise to the division of profit between sequential innovators; see Green and Scotchmer (1995) for an early study. Our study differs from studies in this literature by analyzing the effects of patent instruments on innovation and economic growth in a quantitative dynamic general-equilibrium (DGE) framework.

As for the macroeconomic literature on patent policy, Judd (1985) provides the seminal DGE analysis on patent length, and he finds that an infinite patent length maximizes innovation. Subsequent studies find that strengthening patent rights via different patent instruments does not necessarily increase innovation and may even stifle it. Examples of these studies include Horowitz and Lai (1996) and Chen and Iyigun (2010) on patent length,\(^1\) O’Donoghue and Zweimuller (2004) on forward patent protection and patentability requirement, Akiyama and Furukawa (2009), Furukawa (2007, 2010) and Horii and Iwaisako (2007) on patent protection against imitation, and Chu (2009) on blocking patents. Our study complements these growth-theoretic studies by analyzing a novel channel through the escape-infringement effect that gives rise to a non-monotonic effect of patent rights on innovation and economic growth. Furthermore, we contrast the effects of blocking patents under an exogenous step size versus an endogenous step size of innovation and show that the same patent instrument can have drastically different effects on innovation in different environments.

The rest of this note is organized as follows. Section 2 presents the model. Section 3 defines the equilibrium and characterizes the equilibrium allocation. Section 4 analyzes the effects of patent instruments on innovation and economic growth. The final section concludes.

\(^1\)Horowitz and Lai (1996) show that longer patent length increases the size of innovation but delays the introduction of subsequent innovations. Although our model generates a similar asymmetric effect of patent rights on the size and frequency of innovation, the underlying mechanism (i.e., overlapping patent rights and the escape-infringement effect) in our model is very different from Horowitz and Lai (1996).
2 The model

In this section, we consider a quality-ladder growth model as in Grossman and Helpman (1991).\footnote{See also Aghion and Howitt (1992) and Segerstrom et al. (1990) for other pioneering studies on the quality-ladder growth model.} To consider the division of profit between sequential innovators along the quality ladder, we assume that each entrant (i.e., the most recent innovator) infringes the patent of the incumbent (i.e., the previous innovator). As a result of this patent infringement, the entrant has to transfer a share \( s \in [0, 1] \) of her profit to the incumbent. However, with sequential innovation, every innovator’s patent would eventually be infringed by the next innovation, and she can then extract a share \( s \) of profit from the next entrant. This formulation of profit division between sequential innovators originates from O’Donoghue and Zweimüller (2004), but our model differs from O’Donoghue and Zweimüller (2004) by endogenizing \( s \) as a function of the step size of innovation in order to analyze the escape-infringement effect. To make the quality-ladder model more suitable for calibration, we introduce capital accumulation into the model. Given that the Grossman-Helpman model has been well-studied, we will describe the familiar features briefly to conserve space and discuss the new features in details.

2.1 Households

There is a unit continuum of identical households. Their lifetime utility is

\[
U = \int_0^\infty e^{-\rho t} \ln C_t dt, \tag{1}
\]

where \( \rho > 0 \) is the discount rate, and \( C_t \) is the consumption of final goods at time \( t \). Households maximize (1) subject to

\[
\dot{A}_t = r_t A_t + W_t - C_t, \tag{2}
\]

\( A_t \) is the value of assets (including capital and patents) owned by households, and \( r_t \) is the real rate of return on assets. Households inelastically supply one unit of labor to earn the wage rate \( W_t \). The price of final goods is normalized to unity. From standard dynamic optimization, the Euler equation is

\[
\dot{C}_t / C_t = r_t - \rho. \tag{3}
\]
2.2 Final goods

This sector is perfectly competitive. Final goods $Y_t$ are produced via a standard Cobb-Douglas aggregator given by

$$Y_t = \exp \left( \int_0^1 \ln X_t(i) \, di \right),$$

(4)

where $X_t(i)$ is intermediate goods $i \in [0, 1]$. Competitive firms producing final goods take as given the output price and input prices $P_t(i)$ for $i \in [0, 1]$. From profit maximization, the conditional demand function for $X_t(i)$ is

$$X_t(i) = Y_t / P_t(i).$$

(5)

2.3 Intermediate goods

In this sector, there is a continuum of differentiated intermediate goods $i \in [0, 1]$. Given the technology of the most recent innovator, the production function of intermediate goods $i$ is

$$X_t(i) = Q_t(i)[L_{x,t}(i)]^{1-\alpha}[K_t(i)]^{\alpha}.$$  

(6)

$Q_t(i)$ is the highest level of technology in industry $i$ at time $t$, and it is given by $Q_t(i) = \prod_{j=1}^{n_t(i)} z_j(i)$. The integer $n_t(i)$ is the number of innovations that have occurred in industry $i$ as of time $t$, and $z_j(i) > 1$ is the step size of the $j$-th innovation in industry $i$. If $z_j(i) = z$ for all $j \in \{1, ..., n_t(i)\}$ and for all $i \in [0, 1]$, then $Q_t(i)$ simplifies to $z^{n_t(i)}$ as in the canonical quality-ladder model. Given that the equilibrium features a symmetric step size $z$ for all $j \in \{1, ..., n_t(i)\}$ and for all $i \in [0, 1]$, we use $z$ to denote $z_j(i)$ for notational simplicity.

$L_{x,t}(i)$ and $K_t(i)$ are respectively the number of production workers and the amount of capital employed in industry $i$ at time $t$. From cost minimization, the marginal cost of production for the industry leader (i.e., the most recent innovator) in industry $i$ is

$$MC_t(i) = \frac{1}{Q_t(i)} \left( \frac{W_t}{1 - \alpha} \right)^{1-\alpha} \left( \frac{R_t}{\alpha} \right)^{\alpha},$$

(7)
where $R_t$ is the rental price of capital. The standard no-arbitrage condition is $R_t = r_t + \delta$, where $\delta$ is the depreciation rate of capital. Given $MC_t(i)$, the industry leader charges a markup over the marginal cost to maximize profit. In the canonical quality-ladder model, this markup is given by the step size $z$ due to Bertrand competition. Here we consider patent breadth similar to Li (2001) and Goh and Olivier (2002) by assuming that the markup $\mu > 1$ is a policy instrument chosen by the patent authority. Therefore, the monopolistic price is given by

$$P_t(i) = \mu MC_t(i).$$

(8)

As a result, the amount of profit generated in industry $i$ is

$$\pi_t(i) = \left(\frac{\mu - 1}{\mu}\right) P_t(i) X_t(i) = \left(\frac{\mu - 1}{\mu}\right) Y_t,$$

(9)

where the second equality of (9) follows from (5). Furthermore, labor income in industry $i$ is

$$W_t L_{x,t}(i) = \left(\frac{1 - \alpha}{\mu}\right) P_t(i) X_t(i) = \left(\frac{1 - \alpha}{\mu}\right) Y_t.$$

(10)

In each industry $i$, the most recent innovator (i.e., the entrant) infringes the patent of the previous innovator (i.e., the incumbent). As a result of this patent infringement, the most recent innovator pays a licensing fee by transferring a share $s \in [0, 1]$ of her profit to the previous innovator. Here we differ from O’Donoghue and Zweimuller (2004) by considering an endogenous profit-division rule given by $s = \beta / z$, where the patent instrument $\beta \in [0, z]$ captures the negative effect of blocking patents. For a given $z$, a larger $\beta$ forces the entrant to pay a higher licensing fee to the incumbent and hence reduces the entrant’s incentives for innovation. However, the entrant can reduce the amount of this licensing fee by developing a more substantial innovation through a larger step size $z$. This setup is reasonable because in reality, the more different an innovation is from previous innovations, the less likely that it would be considered as an infringement. Given a lower chance of patent infringement, the entrant would have more power to bargain for a lower licensing fee. Due to profit division, the entrant obtains $(1 - s) \pi_t$ while the incumbent obtains $s \pi_t$. The most recent innovation and the second-most recent innovation are owned by different firms due to the well-known Arrow replacement effect.³

³See Cozzi (2007) for an interesting discussion on the Arrow effect.
2.4 R&D and innovation

Denote $V_{2,t}(i)$ as the value of the patent on the second-most recent innovation in industry $i$. Because $\pi_t(i) = \pi_t$ for $i \in [0, 1]$ from (9), $V_{2,t}(i) = V_{2,t}$ in a symmetric equilibrium that features an equal arrival rate of innovation across industries. The familiar no-arbitrage condition for $V_{2,t}$ is

$$r_t V_{2,t} = s \pi_t + \dot{V}_{2,t} - \lambda_t V_{2,t}. \tag{11}$$

Equation (11) equates the interest rate $r_t$ to the asset return per unit of asset. The asset return is given by the sum of (a) the profit $s \pi_t$ received by the patent holder, (b) the capital gain $\dot{V}_{2,t}$, and (c) the expected capital loss $\lambda_t V_{2,t}$ due to creative destruction for which $\lambda_t$ is the Poisson arrival rate of innovation. As for the value of the patent on the most recent innovation, the no-arbitrage condition for $V_{1,t}$ is

$$r_t V_{1,t} = (1 - s) \pi_t + \dot{V}_{1,t} - \lambda_t (V_{1,t} - V_{2,t}). \tag{12}$$

The intuition behind (12) is the same as (11) except for the last term. When the next innovation occurs, the current industry leader becomes the second-most recent innovator and hence her net capital loss is $V_{1,t} - V_{2,t}$.

There is a unit continuum of R&D entrepreneurs indexed by $k \in [0, 1]$, and each entrepreneur hires R&D labor $L_{r,t}(k)$ for innovation. The expected return from R&D is

$$\pi_{r,t}(k) = \lambda_t(k) V_{1,t} - W_t L_{r,t}(k). \tag{13}$$

The arrival rate of innovation for entrepreneur $k$ is

$$\lambda_t(k) = \frac{\varphi L_{r,t}(k)}{z}, \tag{14}$$

where $\varphi > 0$ is a productivity parameter for R&D, and $\varphi/z$ captures the effect that a larger step size of innovation has a lower chance of success. The zero-expected-profit condition for R&D is

$$\frac{\varphi V_{1,t}}{z} = W_t. \tag{15}$$

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4We follow the standard approach in the literature to focus on the symmetric equilibrium. See Cozzi et al. (2007) for a theoretical justification for the symmetric equilibrium as the unique rational-expectation equilibrium in the quality-ladder model.
For the rest of this study, we focus on the balanced growth path. In this case, (11) becomes
\[ V_2 = \frac{s\pi}{r - g_\pi + \lambda} = \frac{s\pi}{\rho + \lambda}, \] (16)
where \( g_\pi \) is the steady-state growth rate of profit, and the second equality of (16) follows from (3).\(^5\) Similarly, (12) becomes
\[ V_1 = \frac{(1-s)\pi}{\rho + \lambda} + \frac{\lambda V_2}{\rho + \lambda}. \] (17)
An entrepreneur takes \( \lambda \) and \( V_2 \) as given. Given that the step size \( z \) is endogenous, she chooses \( z \) to maximize
\[ \varphi \frac{V_1}{z} = \frac{\varphi}{z} \left( \frac{(1-s)\pi}{\rho + \lambda} + \frac{\lambda V_2}{\rho + \lambda} \right), \] (18)
where \( s = \beta/z.\)\(^6\) This optimization yields the equilibrium step size given by
\[ z^* = \beta \left( \frac{2\rho + \lambda}{\rho + \lambda} \right). \] (19)
It is useful to note that the equilibrium arrival rate \( \lambda^* \) is also a function of \( \beta.\) To ensure that \( z^* > 1 \) in equilibrium, we impose the following condition.

\textbf{Condition B (blocking patents):} \( \beta \left( \frac{2\rho + \lambda^*(\beta)}{\rho + \lambda^*(\beta)} \right) > 1. \)

In Section 4, we will show that \( z^* \) is strictly increasing in \( \beta \) even after taking into account the general-equilibrium effect on \( \lambda^*, \) so that there exists a lower-bound value of \( \beta \) above which Condition B holds. Equation (19) yields an important insight that increasing the blocking effect \( \beta \) of patent protection causes the innovators to develop more substantial innovations in order to escape patent infringement. In equilibrium, the profit-division rule under an endogenous step size of innovation becomes
\[ s^* = \frac{\beta}{z^*} = \frac{\rho + \lambda}{2\rho + \lambda}. \] (20)

\(^5\)It is useful to note that consumption, output and profit all grow at the same rate on the balanced growth path.

\(^6\)It is useful to note that the \( s \) in \( V_2 \) is not chosen by the entrepreneur (but by the next innovator instead).
3 Decentralized equilibrium

The equilibrium is a time path of allocations \( \{ C_t, Y_t, X_t(i), K_t, L_{x,t}, L_{r,t} \}_{t=0}^{\infty} \) and a time path of prices \( \{ P_t(i), W_t, R_t, r_t, V_{1,t}, V_{2,t} \}_{t=0}^{\infty} \). Also, at each instant of time,

- households maximize utility taking \( \{ W_t, r_t \} \) as given;
- competitive final-goods firms produce \( Y_t \) and maximize profit taking \( P_t(i) \) as given;
- monopolistic intermediate-goods firms employ \( \{ L_{x,t}, K_t \} \) to produce \( X_t(i) \) and choose \( P_t(i) \) to maximize profit taking \( \{ W_t, R_t \} \) as given;
- R&D entrepreneurs employ \( L_{r,t} \) to maximize expected profit taking \( \{ W_t, V_{1,t} \} \) as given;
- the labor market clears such that \( L_{x,t} + L_{r,t} = 1 \);
- the final-goods market clears such that \( Y_t = C_t + I_t \), where \( I_t \) is capital investment;
- the capital stock accumulates according to \( \dot{K}_t = I_t - \delta K_t \).

3.1 Equilibrium allocation

To derive the equilibrium allocation, we combine (10) and (15) to obtain

\[
\frac{\varphi V_1}{z^*} = W = \left( \frac{1 - \alpha}{\mu} \right) \frac{Y_t}{L_x}. \tag{21}
\]

Then, we substitute (9), (16) and (17) into (21) and rearrange terms to obtain

\[
\frac{\varphi}{z^*} \left[ (1 - s^*) + \left( \frac{\lambda}{\rho + \lambda} \right) s^* \right] \frac{\mu - 1}{\rho + \lambda} = \frac{1 - \alpha}{L_x}, \tag{22}
\]

where \( z^* \) and \( s^* \) are given by (19) and (20). Using \( L_x = 1 - L_r \) and \( \lambda = \varphi L_r / z \) from (14), we can re-express (22) as

\[
\varphi (\rho + \lambda) = \beta \left( (1 - \alpha) \frac{(2\rho + \lambda)^2}{\mu - 1} + \lambda (2\rho + \lambda) \right). \tag{23}
\]
Equation (23) determines the steady-state equilibrium arrival rate $\lambda^*$ of innovation. Both the left-hand side ($LHS$) and the right-hand side ($RHS$) of (23) are increasing in $\lambda$. To ensure that the equilibrium $\lambda^*$ is strictly positive, we impose a lower bound on the R&D-productivity parameter $\varphi$ given by

**Condition R (R&D productivity):** $\varphi > 4\beta(1 - \alpha)/\mu$. Given Condition R, $LHS|_{\lambda=0} = \varphi \rho > 4\beta(1 - \alpha)/\mu = RHS|_{\lambda=0}$. Furthermore, $LHS$ is a linear and increasing function in $\lambda$ while $RHS$ is a convex and increasing function in $\lambda$. Therefore, $RHS$ crosses $LHS$ exactly once from below giving rise to a unique equilibrium $\lambda^*$; see Figure 1 for an illustration. Solving the quadratic equation in (23) yields a closed-form solution for $\lambda^*$ given by

$$
\lambda^* = \Phi + \sqrt{\Phi^2 + \frac{\rho}{\mu - \alpha} \left[ \frac{\varphi(\mu - 1)}{\beta} - 4(1 - \alpha)\rho \right]},
$$

(24)

where $\Phi \equiv [\varphi(\mu - 1)/(2\beta) - (\mu + 1 - 2\alpha)\rho]/(\mu - \alpha)$ is a composite parameter.

### 4 Effects of patents on innovation and growth

In this section, we analyze the effects of the two patent instruments $\{\beta, \mu\}$ on innovation and economic growth. We begin by deriving the steady-state equilibrium growth rates of output and technology. Substituting (6) into (4) yields

$$
Y_t = Z_t (L_x)^{1-\alpha} (K_t)^\alpha,
$$

(25)

where the aggregate level of technology is defined as

$$
Z_t \equiv \exp \left( \int_0^1 \ln Q_t(i) di \right) = \exp \left( \int_0^1 n_t(i) di \ln z^* \right).
$$

(26)

The second equality of (26) applies $z_j(i) = z^*$ so that $Q_t(i) = (z^*)^{n_t(i)}$. Applying the law of large numbers, the log of $Z_t$ becomes

$$
\ln Z_t = \int_0^t \lambda^*_\tau d\tau \ln z^*.
$$

(27)
Therefore, the steady-state equilibrium growth rate of technology is
\[ g^* \equiv \frac{Z_t}{Z_t} = \lambda^* \ln z^*. \] (28)

On the balanced growth path, \( Y_t \) and \( K_t \) grow at \( g^*/(1 - \alpha) \).

The first patent instrument that we analyze is patent breadth \( \mu \). An increase in \( \mu \) shifts down RHS of (23) causing \( \lambda^* \) to increase. Intuitively, a larger patent breadth enables the industry leader to charge a higher markup, and this larger monopolistic power increases the amount of profits as well as providing more incentives for R&D and innovation. This is the traditional positive effect of patent protection emphasized by proponents of intellectual property rights. The higher arrival rate of innovation also increases the equilibrium growth rate \( g^* \) if \( \beta \) is sufficiently large. To see this result,
\[
\frac{\partial g^*}{\partial \lambda^*} = \ln z^* + \lambda^* \frac{\partial \ln z^*}{\partial \lambda^*} < 0
\]
\[= \ln \left( \frac{2\rho + \lambda^*}{\rho + \lambda^*} \right) - \frac{\rho \lambda^*}{(2\rho + \lambda^*)(\rho + \lambda^*)}. \] (29)

Then, using log approximation \( \ln(1 + x) \approx x \), we can show that
\[
\ln \left( \frac{2\rho + \lambda^*}{\rho + \lambda^*} \right) \approx \frac{\rho}{\rho + \lambda^*} > \frac{\rho \lambda^*}{(2\rho + \lambda^*)(\rho + \lambda^*)}. \] (30)

Therefore, if \( \beta > 1 \) (i.e., \( \ln \beta > 0 \)), then \( \frac{\partial g^*}{\partial \lambda^*} > 0 \).

**Proposition 1** The arrival rate of innovation is increasing in patent breadth \( \mu \). If \( \beta > 1 \), then economic growth is also increasing in patent breadth \( \mu \).

The second patent instrument that we analyze is the effect of blocking patents captured by \( \beta \). However, we first analyze its effect under an *exogenous* step size of innovation. In this case, \( z^* = z > 1 \) and \( s = \beta/z \), where \( z \) is a constant. Furthermore, (22) can be re-expressed as
\[
(\mu - 1) \left[ \left( 1 - \frac{\beta}{z} \right) \rho + \lambda \right] = \frac{(1 - \alpha)(\rho + \lambda)^2}{\varphi/z - \lambda}. \] (31)

It can be shown that Figure 1 also applies to (31). A larger \( \beta \) shifts down LHS of (31). As a result, \( \lambda^* \) decreases, and this lower arrival arrival rate of
innovation also decreases the equilibrium growth rate $g^*$ because $z$ is assumed to be exogenous in this case. Intuitively, a larger effect of blocking patents forces entrants to transfer a larger share of profit to incumbents reducing the entrants’ incentives for R&D and innovation. This is the recently emphasized negative effect of patent protection emphasized by opponents of intellectual property rights.

**Proposition 2** Under an exogenous step size $z$, the arrival rate of innovation and economic growth are decreasing in the blocking effect $\beta$ of patents.

Finally, we analyze blocking patents under an endogenous step size of innovation. In this case, $z^*$ and $s^*$ are given by (19) and (20). A larger $\beta$ induces innovators to choose a larger step size $z^*$ for a given $\lambda$, but this larger step size also reduces the equilibrium arrival rate of innovation due to lower R&D productivity $\varphi/z^*$. In (23), an increase in $\beta$ shifts up RHS, so that $\beta$ has a negative effect on $\lambda^*$ as in the case of exogenous step size. However, with endogenous step size, the larger $z^*$ chosen by innovators also contributes to economic growth. In other words, an increase in $\beta$ has a negative effect on $g^*$ through $\lambda^*$ (i.e., the frequency of innovation) as well as a positive effect through $z^*$ (i.e., the size of innovation). To our knowledge, this additional escape-infringement effect of blocking patents has never been analyzed in the patent literature. It is this novel mechanism that gives rise to a non-monotonic effect of blocking patents on innovation.

Differentiating $g^* = \lambda^* \ln z^*$ with respect to $\beta$ yields

$$\frac{\partial g^*}{\partial \beta} = \ln z^* \frac{\partial \lambda^*}{\partial \beta} + \lambda^* \frac{\partial \ln z^*}{\partial \beta},$$

where

$$\frac{\partial \ln z^*}{\partial \beta} = \frac{1}{\beta} - \frac{\rho}{(\rho + \lambda^*)(2\rho + \lambda^*)} \frac{\partial \lambda^*}{\partial \beta} > 0.$$  

Therefore, the equilibrium step size $z^*$ is strictly increasing in $\beta$ even after taking into account the general-equilibrium effect on $\lambda^*$. Equations (32) and (33) show that there are both positive and negative effects of blocking patents on economic growth. On the one hand, if $\beta$ is sufficiently large, the negative effect dominates the positive effect such that $\partial g^*/\partial \beta < 0$. As $\beta$ approaches
its upper bound $\varphi(\mu - 1)/[4(1 - \alpha)\rho]$. Condition R becomes an equality, and hence, $\lambda^*$ approaches zero; in this case, the negative effect dominates the positive effect. On the other hand, if $\beta$ is sufficiently small, the positive effect dominates the negative effect such that $\partial g^*/\partial \beta > 0$. As $\beta$ approaches its lower bound given by Condition B, $z^*$ approaches one, and hence, the positive effect dominates the negative effect in this case. The opposite signs of $\partial g^*/\partial \beta$ at the upper and lower bounds of $\beta$ imply that $g^*$ must be a non-monotonic function in $\beta$. For the special case of $\rho \to 0$, (23) yields

$$\lim_{\rho \to 0} \lambda^* = \left( \frac{\mu - 1}{\mu - \alpha} \right) \frac{\varphi}{\beta}. \quad (34)$$

Therefore, the equilibrium growth rate becomes

$$\lim_{\rho \to 0} g^* = \left( \frac{\mu - 1}{\mu - \alpha} \right) \frac{\varphi \ln \beta}{\beta}. \quad (35)$$

In this case, $g^*$ is explicitly an inverted-U function in $\beta$ and reaches a maximum at $\beta = \tilde{\beta} \equiv \exp(1)$. Finally, we have conducted a large number of numerical simulations for the general case of $\rho > 0$ and found that $g^*$ is always an inverted-U function in $\beta$.

**Proposition 3** Under the endogenous step size $z^*$, the arrival rate of innovation is decreasing in $\beta$, but the step size of innovation is increasing in $\beta$. Therefore, blocking patents generate a non-monotonic effect on economic growth.

### 4.1 Quantitative analysis

In this section, we calibrate the model to quantify the blocking effect $\beta$ of patent protection on innovation and economic growth. There are five structural parameters $\{\rho, \alpha, \mu, \varphi, \beta\}$ that are relevant for this numerical exercise. First, we set the discount rate $\rho$ and the capital-share parameter $\alpha$ to their standard values of 0.04 and 0.3 respectively. Then, we use three empirical moments to calibrate the remaining three parameters. Using (10) and (22), we can express R&D expenditure as a share of GDP as

$$S_r \equiv \frac{WL_r}{Y} = \left( \frac{\mu - 1}{\mu} \right) \left[ (1 - s^*) + \left( \frac{\lambda^*}{\rho + \lambda^*} \right) s^* \right] \frac{\lambda^*}{\rho + \lambda^*}, \quad (36)$$
where $s^*$ is given by (20). In the US, $S_r$ is about 0.025. Then, we use (24) to set the arrival rate $\lambda^*$ of innovation to 0.33 so that the expected duration between arrivals of innovation is 3 years as in Acemoglu and Akcigit (2009). Finally, we use (28) to set the growth rate $g^*$ of total factor productivity (TFP) to a standard value of 0.015 for the US economy. These three empirical moments pin down the values of $\{\mu, \varphi, \beta\} = \{1.03, 9.71, 0.94\}$.

Given these calibrated parameter values, we perform a counterfactual exercise by increasing $\beta$ to examine whether strengthening the blocking effect of patent protection would increase or decrease economic growth. The result is reported in Figure 2. In Figure 2, we see that $\beta = 0.94$ is on the upward-sloping side of the curve, and this finding is robust to varying the parameter values within a reasonable range. In our sensitivity analysis, we find that $\beta$ is on the downward-sloping side of the curve only when we consider an extremely low arrival rate $\lambda^*$ of less than 0.05, which implies an expected duration between innovation arrivals of more than 20 years. The intuition is as follows. From (28), $\lambda^* = g^*/\ln z^*$; therefore, for a given TFP growth rate $g^*$, a lower arrival rate $\lambda^*$ of innovation must be accompanied by a larger step size $z^*$, which in turn implies a larger $\beta$. Although the literature does not provide a precise estimate for $\lambda^*$, the expected duration between innovation arrivals should be less than 20 years. Therefore, we conclude that a marginal increase in the blocking effect of patent protection is likely to raise economic growth when we account for the escape-infringement effect.

### 5 Conclusion

In this note, we have analyzed the effects of different patent instruments on innovation and economic growth. We find that whether stronger patent rights stimulate or stifle innovation depends on the underlying patent instrument. While patent breadth has a positive effect on innovation, blocking patents generate a negative effect on innovation under an exogenous step size of innovation. However, the effect of blocking patents on innovation and economic growth becomes non-monotonic once we allow for an endogenous step size of innovation, and this non-monotonic effect of patent rights on innovation is consistent with the finding of recent empirical studies. Finally, calibrating the model to aggregate data, we find that a marginal increase in the blocking effect of patent protection is likely to stimulate economic growth.
References


Figure 1: Equilibrium arrival rate of innovation

Figure 2: Effects of blocking patents on growth