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Labor market and natural rate of unemployment in US and Canadian

time series analysis

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Abstract

Canadian labor market data are being used in this paper. These series are quarterly data from

1980 Q1 to 2000 Q4. This series are stationary by test for cointegration I(0), meaning that

there exist equilibrium relationship between the time series labour productivity (prod),

employment (e), unemployment rate (U), real wages (rw). This notion was definitively confirmed with

VEC model. VEC model shows long run coefficient, and if the system is in disequilibrium,

alteration of the variables will only be -0.003 for real wages or -0.3%, -0.001 for

unemployment or -0.1%, -0.000 for productivity or -0%, and -0% for employment. This

means that Canadian labour market is in equilibrium working at natural rate of

unemployment and by equilibrium wages.

Key words: employment, real wages, labour productivity, VAR, VECM

1

Long-run Unemployment

Unemployment is one of harder and more severe macroeconomic problems for many reasons. First, the loss of a job causes reduction of income and living standard. Second, unemployment is not only macroeconomic problem, but it is social problem, that interested the society at whole. The unemployment is subject of interest especially for politicians, and the problem of unemployment is usually central topic of political debate. In that regard, economic researchers try to find out the causes of unemployment, and the policy makers try to create and implement policies that will reduce the number of unemployed.

The rate of unemployment is a stock variable that can be measured at a given point in time, and show how many people from the whole size of the population of working age (labour force) are unemployed. The labor force is the sum of the employed and the unemployed:

$$L = E + U \, \mathbf{1} \tag{1}$$

In this regard, the rate of unemployment is:

$$u = \frac{U}{L}^{2} \tag{2}$$

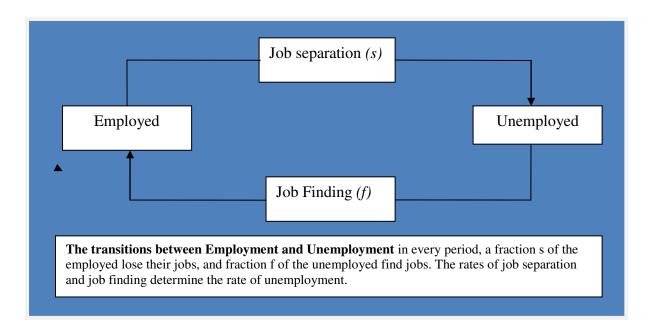
The steady-state rate of unemployment

In this section we will try to explain the factors which determine the natural rate of unemployment throughout creating the model of labour-force. Labour market is specific market in which some people find new job and other lost their jobs. Because our focus is determines of unemployment rate, we assume that the labour force is fixed, and our interest is

 $^{^1}$ $L = \pi P \Rightarrow L = \pi^w P^w + \pi^m P^m$, where P is the size of population of working age, π is participation rate, P^w is the size of women of working age, P^m is the size of man of working age, π^w is participation rate of women, and π^m is participation rate of man.

² Multiply with 100%, because all rates, including rate of unemployment is expressed in percentage.

the transition of people in the labour force between employed and unemployed. In the picture below we illustrate the previous statement. The rate of job separation s is the fraction of employed individuals who lose their job each month (or every quarter), the rate of job finding f is the fraction of unemployed individuals who find a job each month (or every quarter). Together, the rate of job separation s and the rate of job finding f determine the rate of unemployment.



If the unemployment rate is nearly stable, that means, if the labor market is in a steady state-than the number of people finding job s must equal the number of people losing jobs. The number of people finding jobs is fU, the number of people losing jobs is sE, so we can write the steady state as

$$fU = sE \Rightarrow 3 \tag{3}$$

$$fU = s(L - U) \tag{4}$$

To solving the mathematical equation for the rate of unemployment, we divide both sides of equation by L to obtain:

³ Form previous equation, $L = E + U \Rightarrow E = L - U$.

$$f\frac{U}{I} = s(1 - \frac{U}{I}) \tag{5}$$

Now we can solve for $\frac{U}{L}$ to find

$$\frac{U}{L} = \frac{s}{s+f} 4 \tag{6}$$

From this equation we can conclude that the steady-state rate of unemployment u=U/L depends on the rates of job separation and job finding. That means when the rate of job separation increase, the rate of unemployment also increases. On the other hand, when the rate of job finding increase, the rate of unemployment decrease.

In addition, we will present empirical estimation for natural rate of unemployment by job fining and job separation.

$$u = \frac{U}{L} = \frac{7,29}{7,29 + 8,20}$$
$$= 8,18$$

The rate of unemployment in American (first quarter of 1995) is 8.18 percent.

$$u = \frac{U}{L} = \frac{6,69}{6,69 + 7,11}$$
 5 = 7.63

The rate of unemployment in American (first quarter of 2005) is 7.63 percent.

Mathematical note: If in equation $f\frac{U}{L} = s(1 - \frac{U}{L})$ we substitute (E+U) for L, we find $f\frac{U}{L} = s(1 - \frac{U}{E+U}) \Rightarrow f\frac{U}{L} = s(\frac{E+U-U}{E+U})$ if we substitute $\frac{s}{f}E$ for U, in the right side of the equation, we obtain: $f\frac{U}{L} = s(\frac{E}{E+\frac{s}{f}E})$ we can rearrange the equation $f\frac{U}{L} = s(\frac{E}{E(\frac{f+s}{f})})$, for $\frac{U}{L}$ the final equation is: $\frac{U}{L} = \frac{s}{s+f}$.

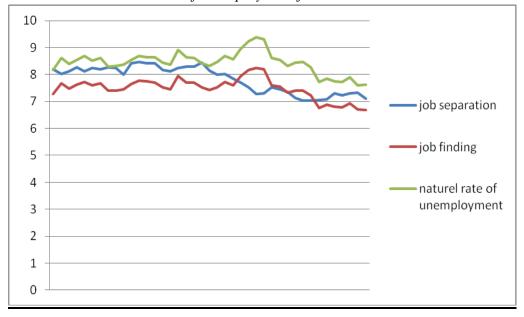
⁵ These estimations are based on data for American economy.

 $Tabel. I\ Natural\ rate\ of\ unemployment\ (steady-state\ unemployment\ rate)^{6}$

year/			rate of unemployment
quarter	job finding (f)	job separation (s)	(r)
1995/1	8,20	7,29	8,18
1995/2	8,01	7,67	8,62
1995/3	8,11	7,48	8,40
1995/4	8,26	7,62	8,54
1996/1	8,11	7,72	8,68
1996/2	8,24	7,59	8,51
1996/3	8,20	7,68	8,61
1996/4	8,28	7,40	8,30
1997/1	8,24	7,41	8,31
1997/2	8,00	7,44	8,37
1997/3	8,43	7,64	8,55
1997/4	8,47	7,77	8,69
1998/1	8,42	7,74	8,65
1998/2	8,43	7,71	8,63
1998/3	8,18	7,53	8,45
1998/4	8,11	7,44	8,36
1999/1	8,25	7,95	8,92
1999/2	8,29	7,70	8,63
1999/3	8,30	7,69	8,61
1996/4	8,44	7,52	8,41
2000/1	8,14	7,42	8,33
2000/2	8,00	7,53	8,47
2000/3	8,01	7,73	8,69
2000/4	7,85	7,60	8,57
2001/1	7,71	7,94	8,97
2001/2	7,52	8,16	9,24
2001/3	7,27	8,25	9,39
2001/4	7,31	8,20	9,32
2002/1	7,53	7,60	8,61
2002/2	7,45	7,54	8,55
2002/3	7,36	7,32	8,32
2002/4	7,13	7,40	8,44
2003/1	7,02	7,41	8,46
2003/2	7,04	7,24	8,27
2003/3	7,06	6,76	7,72
2003/4	7,08	6,88	7,86
2004/1	7,31	6,81	7,75
2004/2	7,22	6,79	7,73
2004/3	7,30	6,94	7,90
2004/4	7,34	6,70	7,61
2005/1	7,11	6,69	7,63

⁶ The estimation is based on data from The flow approach to Labor markets: Davis, Faberman and Haltiwanger (2006, Journal of Economic Perspectives)

Picture 1. The natural rate of unemployment flow



Data description

In this paper we use Canadian time series for, labour productivity (prod), employment (e), unemployment rate (U), real wages (rw).

Original time series are from OECD database, OECD Main Economic Indicators:

- ➤ 444113DSA Canadian unemployment rate in %
- ➤ 444321KSA Canadian manufacturing real wage index
- ➤ 445241K Canadian consumer price index
- ➤ OECD Quarterly National Accounts:
- > CAN1008S1 Canadian nominal GDP
- ➤ OECD Quarterly Labour Force Statistics:
- ➤ 445005DSA Canadian civilian employment in 1000 persons

The data included in this file are obtained by the following transformations:

```
prod = 100*(log(CAN1008S1/445241K)-log(445005DSA))
```

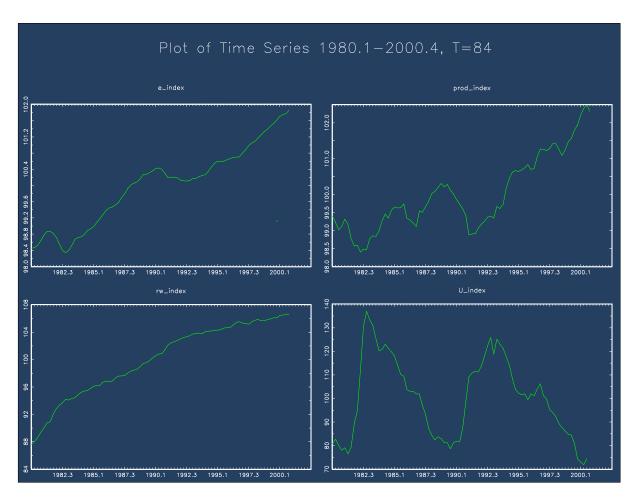
e = 100*log(445005DSA)

U = 444113DSA

rw = 100*log(100*444321KSA)

Plot of time series

On the next page it is presented plot of time series data. This is for purpose of visual inspection of the data and to see their movement across time. These series are quarterly data from 1980 Q1 to 2000 Q4



escriptive statistics

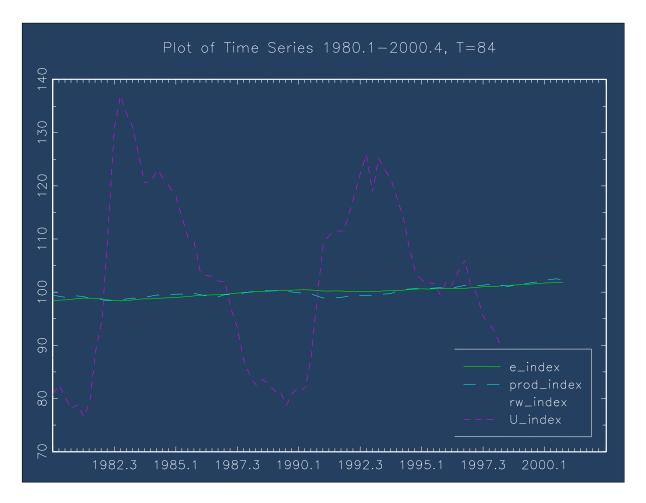
Descriptive statistics reports standard minimum, maximum and standard deviation.

sample range:	[1980 Q1, 20	00 Q4], T = 8	4	
DESCRIPTIVE STA	TISTICS:			
variable	mean	min	max	std. dev.
е	9.44257e+02	9.28563e+02	9.61766e+02	9.10304e+00
prod	4.07821e+02	4.01307e+02	4.18003e+02	4.19131e+00

```
rw 4.40751e+02 3.86136e+02 4.70012e+02 2.31316e+01
U 9.32083e+00 6.70000e+00 1.27700e+01 1.59761e+00
```

Plot of complete time series

On the next page is presented plot of complete time series data.



Test for normality and heteroscedasticity

Standard Jarque-Bera test for non-normality and test for heteroscedasticity ARCH-LM test will be applied.

sample range:	[1980 Q1,	2000 Q4], T = 84		
JARQUE-BERA TES	T			
variable	teststat	p-Value(Chi^2)	skewness	kurtosis
	3.1121	0.2110	-0.0773	2.0698
prod	6.5488	0.0378	0.6367	2.5006
rw	6.5146	0.0385	-0.5672	2.2422
U	4.5233	0.1042	0.1805	1.9220
sample range:	[1980 Q1,	2000 Q4], T = 84		
ARCH-LM TEST wi	th 1 lags			
variable	teststat	p-Value(Chi^2)	F stat	p-Value(F)
	80.7282	0.0000	2949.4304	0.0000
prod	77.0649	0.0000	1077.7141	0.0000
rw	82.1163	0.0000	7712.4830	0.0000
U	60.8812	0.0000	228.4549	0.0000

Normality and heteroscdasticity are not serious problem with time series data.

Nadaraya-Watson OLS regression

Next it is presented OLS regression of labour productivity on Real wages. The relationship between variables is positive and significant. This regression is presented graphically by crossplot (see Crossplot (rw)).

OLS ESTIMATION

```
sample range: [1980 Q1, 2000 Q4], T = 84
```

dependent: prod

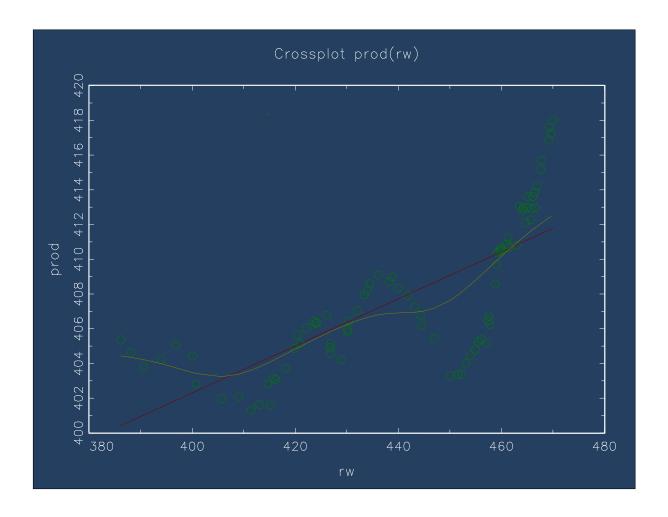
independent: rw

prod = 348.0978 + 0.1355 *rw

t-values = { 59.3718 10.2004 }

sigma = 2.8163

R-squared = 0.5593



OLS ESTIMATION PRODUCTIVITY VERSUS UNEMPLYMENT

OLS estimation is done on labour productivity versus unemployment and the result is negative and significant. This crossplot is given below OLS table.

```
ols ESTIMATION

sample range: [1980 Q1, 2000 Q4], T = 84

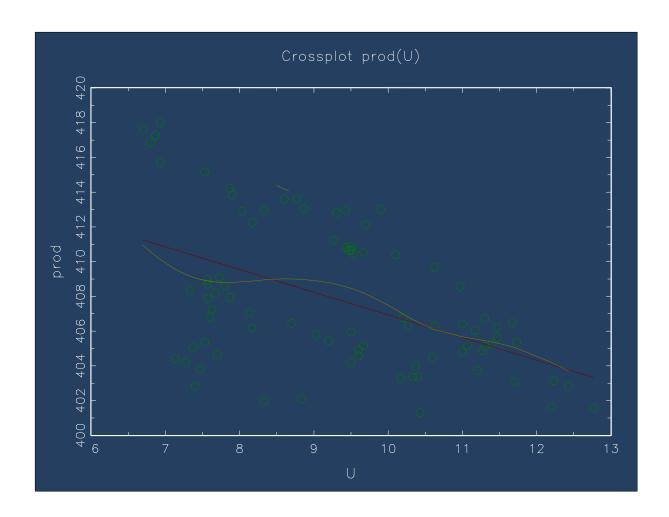
dependent: prod
independent: U

prod = 419.9796 + -1.3045 *U

t-values = { 176.6793 -5.1896 }

sigma = 3.6805

R-squared = 0.2472
```



OLS regression Employment vs real wages

Result is presented below and the result is positive and significant. Crossplot of the regression is presented below the OLS table.

```
OLS ESTIMATION

sample range: [1980 Q1, 2000 Q4], T = 84

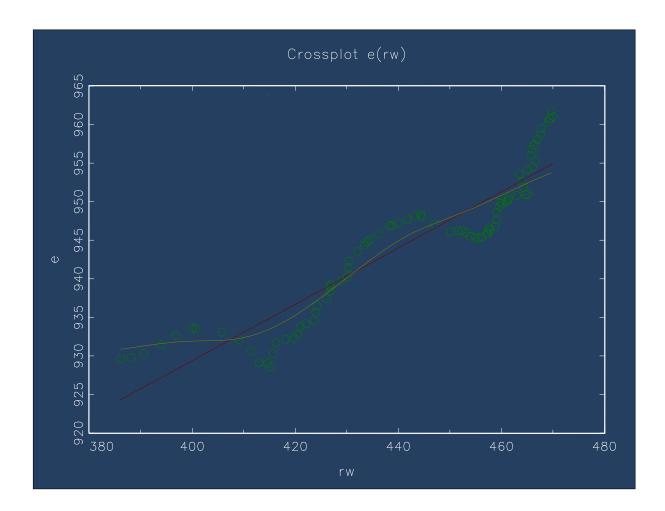
dependent: e
independent: rw

e = 783.4157 + 0.3649 *rw

t-values = { 109.1200 22.4341 }
```

```
sigma = 3.4486

R-squared = 0.8599
```



ADF TESTS FOR TIME SERIES

ADF test have been preformed to prove whether time series are stationary.

ADF unit root test for employment ADF Test for series: e sample range: [1980 Q4, 2000 Q4], T = 81

```
lagged differences: 2
intercept, time trend
asymptotic critical values
reference: Davidson, R. and MacKinnon, J. (1993),
"Estimation and Inference in Econometrics" p 708, table 20.1,
value of test statistic: -1.9087
regression results:
variable coefficient t-statistic
x(-1) -0.0371 -1.9087
dx(-1) 0.9281 8.6237
trend 0.0146 2.0316
            11.2584
```

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q4	, 2000 Q4], $T = 73$
optimal number of lags (searched up	p to 10 lags of 1. differences):
Akaike Info Criterion	9
Hannan-Quinn Criterion	1

Final Prediction Error	9
Schwarz Criterion	1

This variable is first difference stationary. Optimal number of lags by info criteria is (1,9).

Test for cointegration

Johansens trace test for cointegration is being delivered for employment variable.

This variable employment, is I(0) variable, meaning that is stationary at fist difference.

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q3	, 2000 Q4], $T = 74$
optimal number of lags (searched up	p to 10 lags of 1. differences):
Akaike Info Criterion	3
Hannan-Quinn Criterion	2
Final Prediction Error	2
Schwarz Criterion	2

Optimal number of lags according to info criteria is 2.

ADF test for labour productivity

In the next table it is presented unit root test for labour productivity.

ADF test for productivity ADF Test for series: prod sample range: [1980 Q4, 2000 Q4], T = 81 lagged differences: 2 intercept, time trend asymptotic critical values reference: Davidson, R. and MacKinnon, J. (1993), "Estimation and Inference in Econometrics" p 708, table 20.1, Oxford University Press, London 1% 5% 10%

This variable has unit root and is not stationary. Optimal number of lags is 1.

OPTIMAL ENDOGENOUS LAGS FROM INFOF	RMATION CRITERIA
sample range: [1982 Q4	1, 2000 Q4], T = 73
optimal number of lags (searched u	up to 10 lags of 1. differences):
Akaike Info Criterion	1
Hannan-Quinn Criterion	1
Final Prediction Error	1
Schwarz Criterion	1

Test for cointegration

Johansens trace test showed that up to 2 lags this variable is I(0), and optimal number of lags is 2.

Johansen Trace Test for: prod sample range: [1980 Q3, 2000 Q4], T = 82 included lags (levels): 2 dimension of the process: 1 trend and intercept included response surface computed: r0 LR pval 90% 95% 99% 0 5.45 0.5426 10.68 12.45 16.22

OPTIMAL ENDOGENOUS LAGS FROM INFORMATION CRITERIA

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q3	, 2000 Q4], $T = 74$
optimal number of lags (searched u	p to 10 lags of 1. differences):
Akaike Info Criterion	2
Hannan-Quinn Criterion	2
Final Prediction Error	2
Schwarz Criterion	2

ADF test for real wages

ADF test shows that this variable is not stationary and does have unit root.

ADF Test for :	series:	rw
sample range:		[1980 Q4, 2000 Q4], T = 81
lagged differe	ences:	2
intercept, tir	me trend	
asymptotic cr	itical values	
reference: Dav	vidson, R. an	nd MacKinnon, J. (1993),
"Estimation and	nd Inference	in Econometrics" p 708, table 20.1,
Oxford Univer:	sity Press, I	ondon
1% 59	10%	i de la companya de
-3.96 -3	.41 -3.1	.3
value of test	statistic: -	2.7911
regression re	sults:	
variable	coefficient	t-statistic
x(-1)	-0.0584	-2.7911
dx(-1)	0.1835	1.6601
dx (-2)	-0.0454	-0.4127
constant	26.6302	2.8733
trend	0.0339	1.7741
RSS	55.6165	

OPTIMAL ENDOGENOUS LAGS FROM INFORMATION CRITERIA

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q4	, 2000 Q4], T = 73
optimal number of lags (searched u	p to 10 lags of 1. differences):
Akaike Info Criterion	4
Hannan-Quinn Criterion	4
Final Prediction Error	4
Schwarz Criterion	0

Test for cointegration

Johansens trace test for variable real wages it has been conducted.

```
Johansen Trace Test for: rw

sample range: [1980 Q3, 2000 Q4], T = 82

included lags (levels): 2

dimension of the process: 1

intercept included

response surface computed:

r0 LR pval 90% 95% 99%

0 30.99 0.0000 7.60 9.14 12.53
```

OPTIMAL ENDOGENOUS LAGS FROM	INFORMATION CRITERIA
sample range: [1	982 Q4, 2000 Q4], T = 73
optimal number of lags (sear	ched up to 10 lags of 1. differences):
Akaike Info Criterion	5
Hannan-Quinn Criterion	5
Final Prediction Error	5
Schwarz Criterion	1

ADF test for unemployment

ADF test for unemployment it has been conducted and the results are presented below.

ADF Test for series: U
sample range: [1980 Q4, 2000 Q4], T = 81
lagged differences: 2
intercept, time trend
asymptotic critical values
reference: Davidson, R. and MacKinnon, J. (1993),
"Estimation and Inference in Econometrics" p 708, table 20.1,
Oxford University Press, London
1% 5% 10%
-3.96 -3.41 -3.13
value of test statistic: -2.8918
regression results:
variable coefficient t-statistic
x(-1) -0.0765 -2.8918
dx(-1) 0.5179 4.7868
dx(-2) 0.1157 1.0252

```
constant 0.7170 2.8492

trend -0.0029 -1.6544

RSS 9.2220
```

This variable is first difference stationary.

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q4	, 2000 Q4], T = 73
optimal number of lags (searched up	p to 10 lags of 1. differences):
Akaike Info Criterion	1
Hannan-Quinn Criterion	1
Final Prediction Error	1
Schwarz Criterion	1

Test for cointegration

Test for cointegration showed that this variables has cointegration vector r>0.

```
Johansen Trace Test for: rw

sample range: [1980 Q3, 2000 Q4], T = 82

included lags (levels): 2

dimension of the process: 1

intercept included

response surface computed:

r0 LR pval 90% 95% 99%

0 30.99 0.0000 7.60 9.14 12.53
```

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q3	, 2000 Q4], T = 74
optimal number of lags (searched u	p to 10 lags of 1. differences):
Akaike Info Criterion	5
Hannan-Quinn Criterion	5
Final Prediction Error	1
Schwarz Criterion	1

ADF test for unemployment

ADF test for unemployment showed that this variable has unit root at one lag but its first difference stationary.

```
ADF Test for series: U

sample range: [1980 Q4, 2000 Q4], T = 81

lagged differences: 2

intercept, time trend

asymptotic critical values

reference: Davidson, R. and MacKinnon, J. (1993),

"Estimation and Inference in Econometrics" p 708, table 20.1,

Oxford University Press, London

1% 5% 10%

-3.96 -3.41 -3.13

value of test statistic: -2.8918
```

regression	results:	
variable	coefficien	nt t-statistic
x(-1)	-0.0765	-2.8918
dx (-1)	0.5179	4.7868
dx (-2)	0.1157	1.0252
constant	0.7170	2.8492
trend	-0.0029	-1.6544
RSS	9.2220	

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q4	, 2000 Q4], $T = 73$
optimal number of lags (searched u	p to 10 lags of 1. differences):
Akaike Info Criterion	1
Hannan-Quinn Criterion	1
Final Prediction Error	1
Schwarz Criterion	1

Test of cointegration for unemployment variable

Johansens trace test has been conducted for unemployment and proved that this variable is I(0).

```
Johansen Trace Test for: U

sample range: [1980 Q3, 2000 Q4], T = 82

included lags (levels): 2

dimension of the process: 1

intercept included

response surface computed:

r0 LR pval 90% 95% 99%

0 4.99 0.2952 7.60 9.14 12.53
```

Optimal endogenous lags from info criteria is 2.

OPTIMAL ENDOGENOUS LAGS FROM INFOR	MATION CRITERIA
sample range: [1982 Q3	, 2000 Q4], T = 72
optimal number of lags (searched up	p to 10 lags of 1. differences):
Akaike Info Criterion	2
Hannan-Quinn Criterion	2
Final Prediction Error	2
Schwarz Criterion	2

VAR Model

To do a VAR model first we will seek for the optimal number of lags for the model.

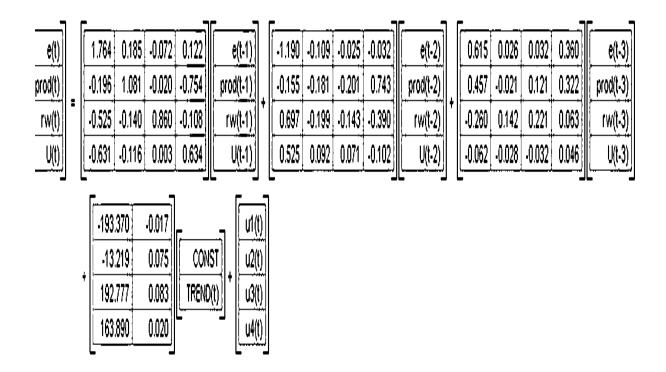
endogenous variables: e prod rw U deterministic variables: CONST TREND sample range: [1982 Q3, 2000 Q4], T = 74 optimal number of lags (searched up to 10 lags of levels): Akaike Info Criterion: 3 Final Prediction Error: 3 Hannan-Quinn Criterion: 2

VAR ESTIMATION RESULTS

VAR estimation results are presented in a matrix form while you can look up in the Appendix 1 to see their output format. ⁷

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⁷ See Appendix 1 VAR OUPUT FORMAT



The VAR model is up to three lags since info criteria demanded that this be modeled that way.

VAR matrix coefficients are presented on the previous page.

Granger causality test

From the below table for granger causality test we can see that there is granger causality between labour productivity, employment, real wages and unemployment, but labour productivity does not granger cause three other variables.

```
TEST FOR GRANGER-CAUSALITY:

H0: "prod" do not Granger-cause "e, rw, U"

Test statistic 1 = 2.8370
```

```
pval-F( 1; 9, 268) = 0.0033

TEST FOR INSTANTANEOUS CAUSALITY:

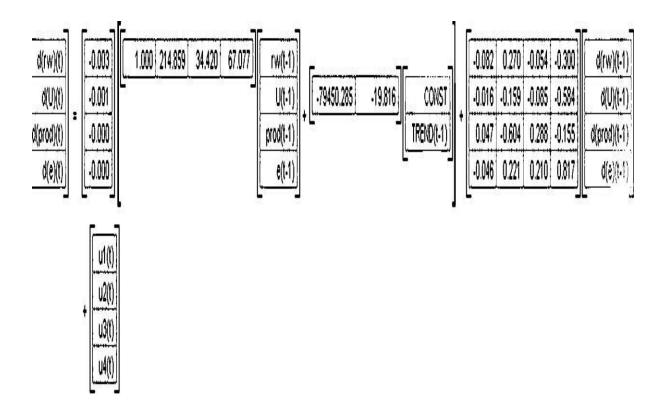
H0: No instantaneous causality between "prod" and "e, rw, U"

Test statistic: c = 1.5804

pval-Chi( c; 3) = 0.6638
```

VEC MODEL ⁸

VEC model for Canadian time series is presented as matrix below.



⁸ See Appendix 2 VEC model output in jmulti

VEC model shows long run coefficient, and if the system is in disequilibrium, alteration of the variables will only be -0.003 for real wages or -0.3%, -0.001 for unemployment or -0.1%, -0.000 for productivity or -0%, and -0% for employment. This means that Canadian labour market is in equilibrium working at natural rate of unemployment and by equilibrium wages.

Chow test for structural stability

Chow test below shows that VEC model is stable according to this test.

CHOW TEST FOR STRUCTURAL BREAK

On the reliability of Chow-type tests..., B. Candelon, H. Lütkepohl,

sample range: [1980 Q3, 2000 Q4], T = 82

tested break date: 1985 Q1 (18 observations before break)

break point Chow test: 67.7571

bootstrapped p-value: 0.3600

asymptotic chi^2 p-value: 0.0071

degrees of freedom: 42

sample split Chow test: 57.7302

bootstrapped p-value: 0.0400

asymptotic chi^2 p-value: 0.0035

degrees of freedom: 32

Chow forecast test: 0.1847

bootstrapped p-value: 0.9800

asymptotic F p-value: 1.0000

degrees of freedom: 256, 10

Appendix 1 VAR OUTPUT FORMAT

endogenous variables: e prod rw U exogenous variables: deterministic variables: CONST TREND endogenous lags: exogenous lags: 0 sample range: [1980 Q4, 2000 Q4], T = 81modulus of the eigenvalues of the reverse characteristic polynomial : |z| = (3.4351 1.7584 1.7584 1.64281.8444 1.8444 1.2214 1.2214 1.0442 1.0442 3.8469) Legend: ====== Equation 1 Equation 2 ... _____ Variable 1 | Coefficient ... | (Std. Dev.) | {p - Value} | [t - Value] Variable 2 | ...

Lagged endogenous term:

		е	prod	ĽW	U
е	(t-1)	1.764	-0.196	-0.525	-0.631
	1	(0.151)	(0.280)	(0.327)	(0.124)
	1	{0.000}	{0.483}	{0.109}	{0.000}
	1	[11.678]	[-0.702]	[-1.602]	[-5.075]
pro	d(t-1)	0.185	1.081	-0.140	-0.116
	1	(0.064)	(0.118)	(0.139)	(0.053)
	1	{0.004}	{0.000}	{0.314}	{0.028}
	1	[2.897]	[9.136]	[-1.007]	[-2.203]
rw	(t-1)	-0.072	-0.020	0.860	0.003
	1	(0.054)	(0.099)	(0.116)	(0.044)
	1	{0.177}	{0.841}	{0.000}	{0.950}
	1	[-1.352]	[-0.201]	[7.405]	[0.062]
U	(t-1)	0.122	-0.754	-0.108	0.634
	1	(0.198)	(0.367)	(0.430)	(0.163)
	1	{0.539}	{0.040}	{0.801}	{0.000}
	1	[0.615]	[-2.053]	[-0.252]	[3.883]
е	(t-2)	-1.190	-0.155	0.697	0.525
	I	(0.235)	(0.435)	(0.510)	(0.193)
	1	{0.000}	{0.722}	{0.171}	{0.007}

	1	[-5.064]	[-0.356]	[1.367]	[2.717]
pro	d(t-2)	-0.109	-0.181	-0.199	0.092
	1	(0.094)	(0.174)	(0.204)	(0.078)
	1	{0.246}	{0.300}	{0.330}	{0.234}
	1	[-1.161]	[-1.036]	[-0.975]	[1.189]
rw	(t-2)	-0.025	-0.201	-0.143	0.071
	1	(0.070)	(0.129)	(0.151)	(0.057)
	1	{0.720}	{0.118}	{0.342}	{0.218}
	1	[-0.358]	[-1.564]	[-0.951]	[1.233]
U	(t-2)	-0.032	0.743	-0.390	-0.102
	1	(0.246)	(0.455)	(0.533)	(0.202)
	1	{0.895}	{0.102}	{0.464}	{0.612}
	1	[-0.131]	[1.634]	[-0.732]	[-0.507]
е	(t-3)	0.615	0.457	-0.260	-0.062
	1	(0.166)	(0.308)	(0.360)	(0.137)
	1	{0.000}	{0.137}	{0.470}	{0.651}
	1	[3.699]	[1.487]	[-0.723]	[-0.453]
pro	d(t-3)	0.026	-0.021	0.142	-0.028
	1	(0.065)	(0.121)	(0.142)	(0.054)
	1	{0.695}	{0.865}	{0.318}	{0.597}
	1	[0.392]	[-0.169]	[0.999]	[-0.529]
rw	(t-3)	0.032	0.121	0.221	-0.032
	1	(0.054)	(0.100)	(0.117)	(0.044)
	1	{0.557}	{0.225}	{0.058}	{0.477}

	1	[0.588]	[1.214]	[1.893]	[-0.711]
U	(t-3)	0.360	0.322	0.063	0.046
	I	(0.206)	(0.381)	(0.446)	(0.169)
	I	{0.080}	{0.398}	{0.888}	{0.788}
	I	[1.748]	[0.845]	[0.140]	[0.269]

Deterministic term:

		е	prod	rw	Ŭ
CONST		-193.370	-13.219	192.777	163.890
		(73.005)	(135.180)	(158.276)	(60.057)
		{0.008}	{0.922}	{0.223}	{0.006}
		[-2.649]	[-0.098]	[1.218]	[2.729]
TREND(t)		-0.017	0.075	0.083	0.020
		(0.016)	(0.030)	(0.036)	(0.013)
		{0.288}	{0.014}	{0.019}	{0.134}
		[-1.062]	[2.455]	[2.347]	[1.498]

Appendix 2 VEC model

VEC REPRESENTATION

endogenous variables: rw U prod e

exogenous variables:

deterministic variables: CONST TREND

endogenous lags (diffs): 1

exogenous lags: 0

sample range: [1980 Q3, 2000 Q4], T = 82

estimation procedure: One stage. Johansen approach

Lagged endogenous term:

		d(rw)	d(U)	d(prod)	d(e)
d(rw)	(t-1)	-0.082	-0.016	0.047	-0.046
	I	(0.110)	(0.043)	(0.099)	(0.057)
	I	{0.457}	{0.714}	{0.636}	{0.416}
	I	[-0.744]	[-0.366]	[0.473]	[-0.814]
d(U)	(t-1)	0.270	-0.159	-0.604	0.221
	I	(0.368)	(0.143)	(0.334)	(0.190)
	1	{0.463}	{0.266}	{0.070}	{0.245}
	1	[0.733]	[-1.112]	[-1.810]	[1.164]
d(prod) (t-1)	-0.054	-0.085	0.288	0.210
	1	(0.118)	(0.046)	(0.107)	(0.061)
	1	{0.647}	{0.063}	{0.007}	{0.001}
	1	[-0.458]	[-1.863]	[2.685]	[3.460]
d(e)	(t-1)	-0.300	-0.584	-0.155	0.817
	1	(0.264)	(0.102)	(0.239)	(0.136)

Loading coefficients:

	d(rw)	d(U)	d(prod)	d(e)
ec1(t-1)	-0.003	-0.001	0.000	0.000
I	(0.000)	(0.000)	(0.000)	(0.000)
I	{0.000}	{0.000}	{0.768}	{0.416}
I	[-7.568]	[-3.886]	[-0.295]	[-0.813]

Estimated cointegration relation(s):

```
U (t-1) | 214.859
```

(44.981)

[(0.000)

[4.777]

prod(t-1) | 34.420

(19.716)

[0.081]

[1.746]

e (t-1) | 67.077

(22.682)

| {0.003}

[2.957]

CONST | -79450.285

(26488.658)

| {0.003}

[-2.999]

TREND(t-1)| -19.816

(9.336)

[-2.123]

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