

# Population and economic growth theme: Longitudinal data for a sample of Balkan countries

Josheski, Dushko and Nikola, Dimitrov and Koteski, Cane

Goce Delcev University-Stip

25 February 2012

Online at https://mpra.ub.uni-muenchen.de/36946/ MPRA Paper No. 36946, posted 26 Feb 2012 17:18 UTC

# Population and economic growth theme: Longitudinal data for a sample of Balkan countries

Dushko Josheski (<u>dushkojosheski@gmail.com</u>) Nikola V.Dimitrov (<u>nikola.dimitrov@ugd.edu.mk</u>) Cane Koteski (<u>cane.koteski@ugd.edu.mk</u>) University Goce Delcev-Stip

#### Abstract

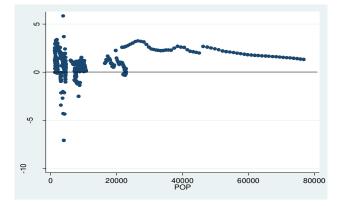
In this paper we use pooled cross-sectional (longitudinal data) in a sample of 10 Balkan countries. The period we cover is from 1950-2009 data are for population and economic growth. In the theoretical part we present optimal intergenerational model of population growth .The optimal population growth depends on capital in the future period and future consumption. Consumption should be greater than zero, and less than total capital of the current generation. In the econometric part OLS regression with dummies the coefficient on Macedonia, is highest significant coefficient meaning, if we control for Macedonia we will on average find more positive association between growth of GDP and population growth. Hausman test was in favor of fixed effects model, but fixed effects and Random effects model showed that there is positive coefficient between GDP growth and population growth. Coefficient in the FE model was statistically significant, which was not case in RE model. From the Fischer's panel unit root test we reject the null hypothesis that panels contain unit root and we accept the alternative that at least one panel is stationary, for the population growth and GDP growth.

Keywords: Population growth, economic growth, Fixed effects model, Random effects model, OLS with dummies model

#### Introduction

In the beginning of the theoretical section we will start with <u>(Kremer, (1993))</u><sup>1</sup> evidence that the relationship between population growth and population is almost linear but also statistically significant. In this section we will use our data on population and population growth (<u>See Section data and methodology for explanations</u>)<sup>2</sup>. This data cover 10 Balkan countries ,panel data that cover time period for every of the 10 Balkan countries from 1950 to 2009 The level and growth population are presented in the next scatter

Scatter level of population and population growth



This figure shows strongly positive and as we will see statistically significant relationship between population (in thousands) and growth of population.

A regression on a constant and population (in thousands) yields (See Appendix 1)<sup>3</sup>:

$$popgro = 0.58 + 0.0000196 pop$$
(1)  
(0.000) (0.000)  
R<sup>2</sup>=0.06

Here *popgro* is population growth and *pop* is population in thousands, score is positive and statistically significant at all levels of conventional significance. On the next 2 tables we present the data on GDP and Population growth for the 10 Balkan countries from 2001-2010.

<sup>&</sup>lt;sup>1</sup> Michael Kremer (1993), "Population Growth and Technological Change: One Million B.C. to 1990," *Quarter-ly Journal of Economics* 108:3 (August), pp. 681-716.

<sup>&</sup>lt;sup>2</sup> See Section data and methodology for explanations.

<sup>&</sup>lt;sup>3</sup> See Appendix 1 Regression on population growth and level of population

Country Name	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010
Albania	0.18	0.40	0.55	0.58	0.54	0.47	0.41	0.37	0.36	0.36
Bosnia and Herzegovina	1.47	0.73	0.18	-0.04	-0.01	0.02	-0.07	-0.13	-0.17	-0.20
Bulgaria	-1.88	-0.52	-0.59	-0.54	-0.53	-0.53	-0.51	-0.48	-0.50	-0.55
Croatia	0.32	0.00	0.00	-0.02	0.07	-0.05	-0.09	-0.05	-0.11	-0.11
Greece	0.30	0.34	0.33	0.35	0.38	0.40	0.40	0.40	0.41	0.32
Macedonia, FYR	0.35	0.31	0.27	0.26	0.25	0.24	0.24	0.22	0.21	0.18
Romania	-1.40	-1.50	-0.28	-0.26	-0.23	-0.22	-0.19	-0.15	-0.15	-0.18
Serbia	-0.17	-0.05	-0.26	-0.23	-0.30	-0.39	-0.41	-0.43	-0.40	-0.39
Slovenia	0.15	0.10	0.09	0.07	0.18	0.32	0.56	0.16	0.90	0.64
Turkey	1.43	1.39	1.36	1.34	1.34	1.34	1.34	1.32	1.29	1.25
a <b>1</b> 1	1 0 1									

Table 1 Population growth in 10 Balkan countries for the period 2001 -2010<sup>4</sup>

Source: World Bank

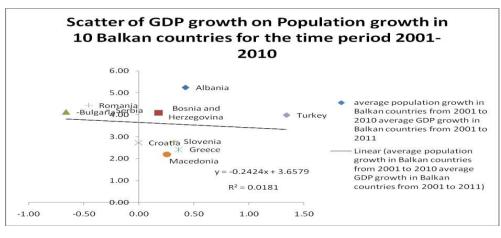
Table 2 GDP growth in 10 Balkan countries for the period 2001-2010

Country Name	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010
Albania	7.00	2.90	5.70	5.90	5.50	5.00	5.90	7.70	3.30	3.50
Bosnia and Herzegovina	4.40	5.30	4.00	6.10	5.00	6.20	6.84	5.42	-3.10	0.80
Bulgaria	4.15	4.65	5.51	6.75	6.36	6.51	6.45	6.22	-5.52	0.20
Croatia	3.66	4.88	5.37	4.13	4.28	4.94	5.06	2.17	-5.99	-1.19
Greece	4.20	3.44	5.94	4.37	2.28	5.17	4.28	1.02	-2.04	-4.47
Macedonia, FYR	-4.53	0.85	2.82	4.09	4.10	3.95	5.90	5.00	-0.90	0.70
Romania	5.70	5.10	5.20	8.40	4.17	7.90	6.00	9.43	-8.50	0.95
Serbia	5.60	3.90	2.40	8.30	5.60	5.23	6.90	5.52	-3.12	1.76
Slovenia	2.85	3.97	2.84	4.29	4.49	5.81	6.80	3.49	-7.80	1.18
Turkey	-5.70	6.16	5.27	9.36	8.40	6.89	4.67	0.66	-4.83	8.95

Source: World Bank

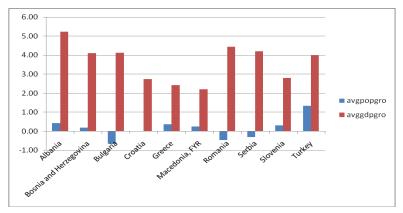
On the next scatter are presented average growth rates of population and GDP, we add a linear trend to the scatter and GDP growth is negatively correlated with the population growth by -0.24 and intercept is 3.65. This means that if population increases by 1 percentage point GDP growth on average will decline by 0.24 percentage points.

Scatter GDP growth on population growth



<sup>4</sup> These data are gathered from World Bank data base: <u>http://data.worldbank.org/country</u>.

Population growth rate is very slow in the Balkans.Especially in Bulgaria (-0.66), Romania (-0.46), Serbia(-0.30), have negative population growth rate (see chart below).Croatia (0.0) doesn't have population growth, Bosnia and Herzegovina (0.18), Macedonia (0.25), Greece(0.36), Slovenia (0.32), Albania (0.42) and Turkey(1.34).



The demographic structure will be very old in the next decades. This can bring social security problems similar to those of Germany and the other Western European countries. Albania has highest average GDP growth (5.24), followed by Romania(4.43), Serbia(4.21), Bulgaria(4.13), Bosnia and Herzegovina (4.10), Slovenia(2.79), Croatia(2.73), Greece (2.42), Macedonia (2.20). Macedonia has lowest GDP growth from 2001-2010.

#### **Population growth theories**

Malthus prediction, made in 1801 that population growth would run up against the fixity of earth's resources and condemn most of the population to poverty and high death rates proved wrong. Kuznets defined growth in 1966 as sustained increase in population attained without any lowering of per capita product, and viewed population growth as positive contributor to economic growth (Birdsall,N.,(1988)<sup>5</sup>.

Birth and death rates of natural increase, by region, 1950-1955 to 1980-85									
	Crude birth rate			Crude death rate			Natural increase		
	1950-55	1960-65	1980-85	1950-55	1960-65	1980-85	1950-55	1960-65	1980-85
Developed countries	22.7	20.3	15.5	10.1	9.0	9.6	1.3	1.1	0.6
Developing countries	44.4	41.9	31.0	24.2	18.3	10.8	2.0	2.4	2.0
Africa	48.3	48.2	45.9	27.1	23.2	16.6	2.1	2.5	2.9
Latin America	42.5	41.0	31.6	15.4	12.2	8.2	2.7	2.9	2.3
East Asia	43.4	39.0	22.5	25.0	17.3	7.7	1.8	2.2	1.5
Other Asia	41.8	40.1	32.8	22.7	18.2	12.3	1.9	2.2	2.1

Table 3 Natural increase in population in the World by economies and regions

Source: United Nations, Department of International Economic and Social Affairs, World population prospects as assessed in 1984(printout).

<sup>&</sup>lt;sup>5</sup> Birdsall, N., (1988), Handbook of development economics ,Volume 1, edited by T.N.Srinivasan

Since 1950's population growth in developing countries has been around 2.0. Most of the Balkan countries belong to this group except Greece that is advanced economy according to IMF and Slovenia (developing country before 2007). In the developed economies since 1950's we have population growth slowdown to 0.6 in the end of 1980's. In the regions Africa has achieved growth in population, Latin America had declined in population growth, and Other than East Asia the other parts of Asia had increased population growth to 2.1 in the end of 1980's. The population growth rate for the developing countries as well for the world, is predicted to decline towards zero rate bringing population stabilization in the twentieth second century<sup>6</sup>.Even with population growth rate decline size of population in the developing countries will continue to rise, and world population to reach 10 billion before 2050. For the next few decades the variance of prediction is small, so we cannot be sure about the precision of these demographic predictions. Industrial countries according to some projections will increase their population for 20% by 2050, and developing countries will double their population by 2050. Assaf Razin and Uri Ben-Zion(1993) have outlined intergenerational model of population .Population was included in social utility function and assumption was made that preferences are same for each generation:

$$V = \sum_{t=0}^{\infty} \beta^{t} U(c_{t}, \lambda_{t})$$
<sup>(2)</sup>

Here  $\beta$  is the subjective factor by which current generation discounts utility of the next generation. The inclusion of population growth in the social utility function has also an empirical implication for the measurement of welfare improvement. That is, growth of per capita income, by itself, is an inappropriate measure of welfare improvement, and as a measure it is biased against countries with a high rate of population growth. The decision problem for current generation can be written as :

$$V(k_0) = \max\left\{\sum_{t=0}^{\infty} \beta^t U(c_t, \lambda_t)\right\}$$

$$0 \le c_t \le k_t$$

$$0 \le \lambda \le \overline{\lambda}$$
(3)

<sup>&</sup>lt;sup>6</sup> Based on the population projections by World Bank

 $K_t$  is the capital for the current generation;  $\lambda_t$  is the current level of population growth  $\overline{\lambda}$  is the maximum feasible level of population growth. Marginal utilities are positive and diminishing.  $c_t$  is per capita life time consumption. Following decision is presented partially derived:

$$\frac{\partial U}{\partial \lambda}(c_{t},\lambda_{t}) = \frac{\beta}{\lambda_{t}} k_{t+1} \frac{\partial U}{\partial c}(c_{t+1},\lambda_{t+1})$$

$$\frac{\partial U}{\partial \lambda}(c_{t},\lambda_{t}) = \frac{\beta}{\lambda_{t}} \frac{\partial f}{\partial k}(k_{t}-c_{t}) \frac{\partial U}{\partial c}(c_{t+1},\lambda_{t+1})$$
(5)

Equation (4) may be interpreted as describing the optimum decision with respect to the level of population growth  $\lambda_t$  On the one hand an extra unit of  $\lambda_t$  will increase welfare by the marginal utility of population growth, the left-hand side of (4). In the second equation the level of capital is decreased by the consumption of the current generation. And this equation (5) describes the optimal level of consumption.

According to <u>Ramsey  $(1928)^7$ </u>, optimal rate of consumption is:

$$u(c) = \frac{dU(c)}{dc} \tag{6}$$

In the equilibrium there will be no saving and

$$\frac{dc}{dt} = \frac{dk}{dt} = 0 \tag{7}$$

Marginal productivity of capital is :

$$\frac{\partial f}{\partial k} = \rho \qquad ^8 \tag{8}$$

If we take into account intergenerational differences in tastes we get:

$$U(c_0, \lambda_0) = a \log c_0 + v(\lambda_0) \tag{9}$$

$$U(c_t, \lambda_t) = a \log c_t + v(\lambda_t, \theta), t \ge 1$$
(10)

Here  $\Theta$  is parameter in the function v which distinguishes the utility of future generations, derived from population increase, from that of the parents generation .If we include uncertainty in the population growth we get :

<sup>8</sup>  $\rho$  is the rate of discounting if  $\frac{\partial f}{\partial k} > \rho$  there will be saving ,or investment  $\frac{\partial f}{\partial k} < \rho$ 

<sup>&</sup>lt;sup>7</sup> Ramsey, F., P.(1928), A Mathematical theory of saving, The Economic journal Vol.38 No.152

$$V(k_0) = E\left\{\sum_{t=0}^{\infty} \beta^t U(c_t, \lambda_t)\right\}$$

$$0 \le c_t \le k_t$$

$$0 \le h_t \le \overline{h}$$
(11)

Here E is the expected value of the population growth, expectation operator. Consumption should be greater than zero, and less than total capital of the current generation, and  $h_t$  is the variable by which population change is controlled.

#### **Empirical part**

#### **Econometric Methodology**

Data in this paper are gathered from <u>Penn world Table</u><sup>9</sup>. Data cover period from 1950 to 2009 for 10 Balkan countries: **Albania, Bosnia and Herzegovina, Bulgaria, Croatia, Greece, Macedonia, Romania, Serbia, Slovenia, Turkey**. These are 10 panels 60 observations per panel. But the data set has gaps on average we have 59,6 observations per group, so in 10 panels we have around 596 observations. Mostly data are missing for the GDPPPP (GDP in PPP terms) for the period 1950 to 1969 this is due to lack of data collection by the statistical bureaus in this countries for this period.

These data are pooled cross-section time series or panel data. Pooled data are characterized by having repeated observations (most frequently years) on fixed units (most frequently states and nations). This means that pooled arrays of data are one that combines cross-sectional data on N spatial units and T time periods to produce a data set of  $N \times T$  observations (Podestà,2002). However, when the cross-section units are more numerous than temporal units (N>T), the pool is often conceptualized as a "cross-sectional dominant". conversely, when the temporal units are more numerous than spatial units (T>N), the pool is called "temporal dominant" (Stimson 1985). The generic pooled linear regression model estimable by Ordinary Least Squares (OLS) procedure is given by the following equation:

$$y_{it} = \beta_1 + \sum_{k=2}^{k} \beta_k x_{kit} + e_{it}$$
(12)

$$\Delta y_i = \delta_0 + \beta_1 \Delta x_i + \Delta u_i \tag{13}$$

where " $\Delta$ " denotes the change from t = 1 to t = 2. The unobserved effect,  $a_i$ , does not appear in (2): it has been "differenced away." Also, the intercept in (2) is actually

<sup>&</sup>lt;sup>9</sup> <u>http://pwt.econ.upenn.edu/php\_site/pwt70/pwt70\_form.php</u> Alan Heston, Robert Summers and Bettina Aten, Penn World Table Version 7.0, Center for International Comparisons of Production, Income and Prices at the University of Pennsylvania, May 2011.

the change in the intercept from t = 1 to t = 2.Equation (2) is simple first differenced pooled cross section regression where each variable is differenced over time. After we apply OLS estimation we will run fixed effects and random effects model

Static two way fixed effect model:

$$y_{it} = \alpha_i + \delta_i t + \rho y_{t-1} + \theta_t + e_{it}$$
(14)

$$i = 1,...N$$
  $t = 1,...T$  (15)

- 1.  $\alpha_i$  unit-specific characteristics
- 2.  $\gamma_i$  unit-specific deterministic trend parameters
- 3.  $\mu_t$  time-specific effects (common to all units)
- 4.  $\beta$  is common to all units

Next random effects model also is going to be applied. If you have reason to believe that differences across entities have some influence on your dependent variable then you should use random effects.

The random effects model is :

$$Y_{it} = \beta X_{it} + \alpha + u_{it} + \varepsilon_{it}$$
(16)

 $u_{it}$  is between entity error,  $\varepsilon_{it}$  is within entity error.

Unobserved model becomes random effects model when we assume that unobserved effect  $\alpha$  is uncorrelated with each explanatory variable:

$$\operatorname{cov}(x_{iti}, \alpha_i) = 0, t = 1, 2, \dots, T; j = 1, 2, \dots, K$$
 (17)

If we define composition error term  $v_{it} = \alpha_i + u_{it}$ :

$$y_{it} = \beta_0 + \beta_1 x_{it1} + \dots + \beta_k x_{itk} + v_{it}$$
(18)

Im, Pesaran and Shin (JE 2003) propose a test based on the average of a augmented Dickey-Fuller tests computed for each panel unit in the model

$$y_{it} = \alpha_i + \delta_i t + \rho y_{it-1} + \theta_t + e_{it}$$
<sup>(19)</sup>

where  $e_{it}$  can be.

- > Serially correlated
- ➤ and heteroscedastic
- > but cross-sectional independent apart from the presence of the common time effects  $\theta_t$ .

The estimating equation is :

$$\Delta y_{it} = \phi_i y_{it-1} + \sum_{k=1}^{K_i} \gamma k i \Delta y_{it-k} + \varepsilon_{it}$$
<sup>(20)</sup>

The null hypothesis of a unit root is tested using  $t_{bar} = \frac{1}{N} \sum_{i=1}^{N} t \phi i$ 

$$H_0: \phi = 0$$

against the heterogeneous alternative:

$$H_{1}:\begin{cases} \phi < 0 \text{ for } i = 1, \dots, N_{1} \\ \phi = 0 \text{ for } i = N_{1} + 1, \dots, N \end{cases}$$
(21)

In the panel unit root test in the general model, let us first look at the test  $H_0 = \rho = 1$ 

H<sub>0</sub>: unit root Different H<sub>1</sub> specifications have been proposed for the model:

$$y_{it} = \alpha_i + \delta_i t + \rho y_{it-1} + \delta_i \theta_t + \varepsilon_{it}$$

$$H_1: \begin{cases} \rho < 1 \quad for \quad all \quad i \\ \rho = 1 \quad for \quad i = N_1 + 1, \dots N \end{cases}$$
(22)

Data

To estimate the following model we define the following set of variables:

Variable	Definition			
lgdpgro	Logarithm of growth of GDP per capita PPP converted at 2005 constant prices			
lpopgro	Log of growth rate of population in thou- sands			

#### Table 1 Variable definitions

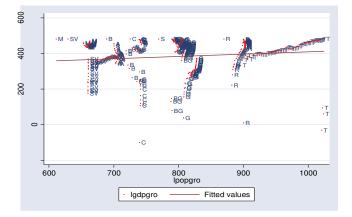
#### Descriptive statistics of the model

In the descriptive statistics we report the usual number of observations per variable, means, standard deviations, and minimums and maximums. The descriptive statistics of our model for ten countries is given below in a Table 2.

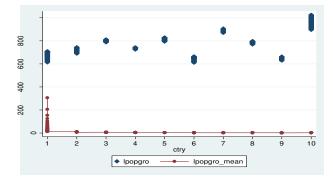
Table 2 Descriptive statistics of the model

Variable	Obs.	Mean	Std.deviation	Min	Max
lgdpgro	342	384.5786	98.82886	-100	481.413
lpopgro	596	770.1818	101.867	611.0394	1024.904

For the table of the descriptive statistics of the model we can see that the mean of log of population growth is 770.1818 (thousands), minimum is 611.0394(thousands) while the maximum of this variable is 1024.904(1 million and 24 thousands and 904). Visually from the next graph we can see that lgdpgro and lpopgro are positively correlated. On this plot we use acronyms for the 10 countries (Albania-A, Bosnia and Herzegovina-B, Bulgaria-BG, Croatia-C, Greece-G, Macedonia-M, Romania-R, Serbia-S, Slovenia-SV, Turkey-T).



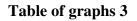
From the graph we can see that substantial part of the observations is below the trend in logarithm of the GDP per capita growth and Turkey has highest population growth from the sample countries while Macedonia some of the lowest, and Croatia and Turkey have experienced negative GDP growth rates. When we try to investigate heterogeneity across countries or entities we do so by creating scatter two way for population growth and country. The resulting scatter from our data I given on the next page. There countries are numbered: **1.Albania 2. Bosnia and Herzegovina, 3.Bulgaria,4. Croatia, 5.Greece,6. Macedonia,7. Romania,8.Serbia, 9.Slovenia, 10. Turkey.** 

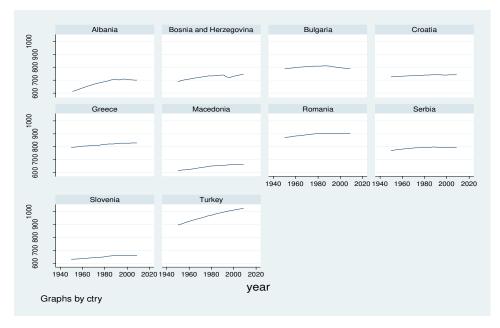


Scatter: Fixed effects: Heterogeneity across countries (or entities)

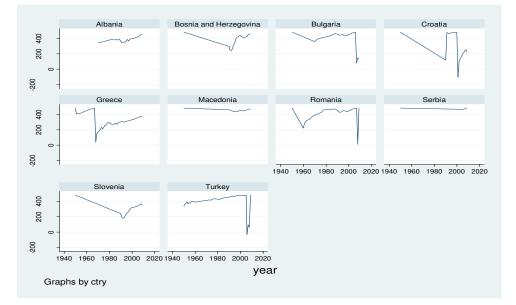
On the scatter is presented logarithm of population growth mean for the 10 countries. Turkey has highest population growth, while Macedonia lowest in the region, together with Slovenia

that has little higher growth of population. Log of population growth across Balkan countries si given in the following table of graphs 3





We can create a Table of graphs even for log of GDP per capita growth Table of graphs 4



From the scatter we can see that countries like Croatia, Bulgaria, Turkey, Romania have suffered from the economic and financial crisis circa 2007-2008, with a sharp decline in the log of growth of GDP variable.

#### Least squares dummy variable model (LSDV)

There are several strategies for estimating fixed effect models. The least squares dummy variable model (LSDV) uses dummy variables, whereas the within effect does not. These strategies produce the identical slopes of non-dummy independent variables. The between effect model also does not use dummies, but produces different parameter estimates. There are pros and cons of these strategies .These are presented in the following table

	LSDV1	Within effect	Between effect	
Functional form	$y_i = i\alpha_i + X_i\beta + \varepsilon_i$	$y_{it} - \overline{y}_{in} = x_{it} - \overline{x}_{in} + \mathcal{E}_{it} - \overline{\mathcal{E}}_{in}$	$\overline{y}_{in} = \alpha + \overline{x}_{in} + \mathcal{E}_i$	
Dummy	Yes	No	No	
Dummy coefficient	Presented	Need to be computed	N/A	
Transformation	No	Deviation from the group means	Group means	
Intercept	Yes	No	No	
$\mathbf{R}^2$	Correct	Incorrect		
SSE	Correct	Correct		
MSE	Correct	Smaller		
Standard error of $\beta$	Correct	Incorrect(smaller)		
DF <sub>error</sub>	nT-n-k	nT-n-k(Larger)	n-K	
Observations	nT	nT	n	

Table 5 Pros and cons of different ways of estimating fixed effects model <sup>10</sup>

#### **Testing for group effects**

The null hypothesis is that all dummy parameters except one are zero:

$$H_0: \mu_1 = \dots = \mu_{n-1} = 0 \tag{23}$$

This hypothesis is tested by the F test (Greene ,2008)<sup>11</sup>, which is based on loss of goodnessof-fit. The robust model in the following formula is LSDV and the efficient model is the pooled regression.

$$F(n-1,nT-n-K) = \frac{\left(R_{LSDV}^2 - R_{Pooled}^2\right)/(n-1)}{\left(1 - R_{LSDV}^2\right)/(nT-n-K)}$$
(24)

<sup>&</sup>lt;sup>10</sup> Source: Indiana University Stath/Math center

<sup>&</sup>lt;sup>11</sup> Greene,H.W.,(2008), Econometric Analysis, Prentice Hall

Here *T*=total number of temporal observations. *n*=the number of groups, and *k*=number of regressors in the model. If we find significant improvements in the  $R^2$ , then we have statistically significant group effects.

In Greene (2008) this model in matrix notation is presented as:

$$y = \begin{bmatrix} x & d_1 & d_2 \dots d_n \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} + \varepsilon$$
(25)

With assembling all nT rows gives:

$$y = X\beta + D\alpha + \varepsilon \tag{26}$$

#### Table 6 OLS regression and OLS with dummies (Appendix 2)<sup>12</sup>

Dependent varia- ble: lgdpgro	Logarithm of growth of GDP per capi- ta PPP	Ordinary least squares	Ordinary least squares with dummies
variables		OLS	OLS_dum
lpopgro	Log of growth rate of popula- tion	0.13*	0.06
_Icountry_2	Bosnia and Herzegovina		4.81
_Icountry_3	Bulgaria		23.99
_Icountry_4	Croatia		-61.16*
_Icountry_5	Greece		-55.76
_Icountry_6	Macedonia		71.53**
_Icountry_7	Romania		22.48
_Icountry_8	Serbia		86.1
_Icountry_9	Slovenia		-87.8**
_Icountry_10	Turkey		10.79
_cons	Constant	280.31***	341.85
Ν		339	339
F-statistics (1, 337)			8.40***

legend: \* p<0.05; \*\* p<0.01; \*\*\* p<0.001

This OLS model shows that on average in these 10 Balkan countries if the population increases by 1% GDP in these 10 countries will rise by 0.13 percent. This coefficient is signifi-

<sup>&</sup>lt;sup>12</sup> See Appendix 2

cant at 1% level of significance. Dummy variables take values from [0,1],zero if the country is not included in the regression and 1 if the country is in the regression. Dummies for Croatia, Macedonia, and Slovenia are significant at 1%, 5%, and 10% levels of significance. So for instance coefficient on Macedonia is highest significant coefficient meaning if we control for Macedonia we will on average find more positive association between growth of GDP and population growth. If we include Croatia and Slovenia in the regression growth of population would have been growth detrimental. If Serbia was in the regression we would have on average found more positive association between growth of GDP and population growth, but typically if we control for Serbia in the regression t-statistics will report 0.10 lower. Fstatistics is significant at all levels of conventional significance; this means that we can reject H<sub>0</sub>: jointly insignificant dummy variables in favor of the alternative jointly significant dummy variables. By adding the dummy for each country we are estimating the pure effect of lpopgro (by controlling for the unobserved heterogeneity)

#### Fixed effects model <sup>13</sup>

"... The fixed-effects model controls for all time-invariant differences between the individuals, so the estimated coefficients of the fixed-effects models cannot be biased because of omitted time-invariant characteristics...[like culture,religion, gender, race, etc] "

To see if time fixed effects are needed when running fixed effect model we will use a joint test to see if the dummies for all years are equal to zero.

The linear regression model with fixed effects is

$$y_{it} = \boldsymbol{\beta}' \mathbf{x}_{it} + \alpha_i + \delta_t + \varepsilon_{it}, t = 1,...,T(i), i = 1,...,N,$$
(27)  
$$E[\varepsilon_{it}|\mathbf{x}_{i1}, \mathbf{x}_{i2}, ..., \mathbf{x}_{iT(i)}] = 0,$$
$$Var[\varepsilon_{it}|\mathbf{x}_{i1}, \mathbf{x}_{i2}, ..., \mathbf{x}_{iT(i)}] = \sigma^2.$$

We have assumed the strictly exogenous regressors case in the conditional moments, [see Woolridge (1995)]. We have not assumed equal sized groups in the panel. The vector  $\beta$  is a

<sup>&</sup>lt;sup>13</sup>Greene, W.(2001), Estimating Econometric Models with Fixed Effects, Department of Economics, Stern School of Business, New York University,

set of parameters of primary interest,  $\alpha_i$  is the group specific heterogeneity. We have included time specific effects but, they are only tangential in what follows. Since the number of periods is usually fairly small, these can usually be accommodated simply by adding a set of time specific dummy variables to the model. Our interest here is in the case in which N is too large to do likewise for the group effects. For example in analyzing census based data sets, N might number in the tens of thousands. The analysis of two way models, both fixed and random effects, has been well worked out in the linear case [See, e.g., Baltagi (1995) and Baltagi, et al. (2005).]. A full extension to the nonlinear models considered in this paper remains for further research The parameters of the linear model with fixed individual effects can be estimated by the 'least squares dummy variable' (LSDV) or 'within groups' estimator, which we denote **b**<sub>LSDV</sub>. This is computed by least squares regression of  $y_{it}^* = (y_{it} - \overline{y}_{i.})$  on the same transformation of  $\mathbf{x}_{it}$  where the averages are group specific means. The individual specific dummy variable coefficients can be estimated using group specific averages of residuals. [See, e.g., Greene (2000, Chapter 14).] The slope parameters can also be estimated using simple first differences. Under the assumptions,  $\mathbf{b}_{LSDV}$  is a consistent estimator of  $\boldsymbol{\beta}$ . However, the individual effects,  $\alpha_i$ , are each estimated with the T(i) group specific observations. Since T(i) might be small, and is, moreover, fixed, the estimator,  $a_{i,LSDV}$ , is inconsistent. But, the inconsistency of  $a_{i,LSDV}$ , is not transmitted to  $\mathbf{b}_{LSDV}$  because  $\overline{y}_{i}$  is a sufficient statistic. The LSDV estimator  $\mathbf{b}_{LSDV}$  is not a function of  $a_{i,LSDV}$ . There are a few nonlinear models in which a like result appears.

We will define a nonlinear model by the density for an observed random variable,  $y_{it}$ ,

$$f(\mathbf{y}_{it} \mid \mathbf{x}_{i1}, \mathbf{x}_{i2}, \dots, \mathbf{x}_{iT(i)}) = g(\mathbf{y}_{it}, \boldsymbol{\beta}' \mathbf{x}_{it} + \alpha_i, \boldsymbol{\theta})$$
(28)

where  $\theta$  is a vector of ancillary parameters such as a scale parameter, an overdispersion parameter in the Poisson model or the threshold parameters in an ordered probit model. We have narrowed our focus to linear index function models. For the present, we also rule out dynamic effects;  $y_{i,t-1}$  does not appear on the right hand side of the equation. [See, e.g., Arellano and Bond (1991), Arellano and Bover (1995), Ahn and Schmidt (1995), Orme (1999), Heckman and MaCurdy (1980)]. However, it does appear that extension of the fixed effects model to dynamic models may well be practical. This, and multiple equation models, such as VAR's are left for later extensions. [See Holtz-Eakin (1988) and Holtz-Eakin, Newey and Rosen (1988, 1989).] Lastly, note that only the current data appear directly in the density for

the current  $y_{it}$ . We will also be limiting attention to parametric approaches to modeling. The density is assumed to be fully defined.

Many of the models we have studied involve an ancillary parameter vector,  $\theta$ . No generality is gained by treating  $\theta$  separately from  $\beta$ , so at this point, we will simply group them in the single parameter vector  $\gamma = [\beta', \theta']'$ . Denote the gradient of the log likelihood by

$$\mathbf{g}_{\gamma} = \frac{\partial \log L}{\partial \gamma} = \sum_{i=1}^{N} \sum_{t=1}^{T(i)} \frac{\partial \log g(y_{it}, \gamma, \mathbf{x}_{it}, \alpha_i)}{\partial \gamma} \text{ (a } \mathcal{K}_{\gamma} \times 1 \text{ vector)}$$
(29)  
$$g_{\alpha i} = \frac{\partial \log L}{\partial \alpha_i} = \sum_{t=1}^{T(i)} \frac{\partial \log g(y_{it}, \gamma, \mathbf{x}_{it}, \alpha_i)}{\partial \alpha_i} \text{ (a scalar)}$$
(30)

$$\mathbf{g}_{\alpha} = [g_{\alpha 1}, \dots, g_{\alpha N}]' \text{ (an } N \times 1 \text{ vector)}$$
(31)

$$\mathbf{g} = [\mathbf{g}_{\gamma}', \mathbf{g}_{\alpha}']' (a (K_{\gamma} + N) \times 1 \text{ vector}).$$
(32)

The full  $(K_{\gamma}+N) \times (K_{\gamma}+N)$  Hessian is

$$\mathbf{H} = \begin{bmatrix} \mathbf{H}_{\gamma\gamma} & \mathbf{h}_{\gamma1} & \mathbf{h}_{\gamma2} & \cdots & \mathbf{h}_{\gammaN} \\ \mathbf{h}_{\gamma1}' & h_{11} & 0 & \cdots & 0 \\ \mathbf{h}_{\gamma2}' & 0 & h_{22} & \cdots & 0 \\ \vdots & \vdots & \ddots & 0 \\ \mathbf{h}_{\gamma N}' & 0 & 0 & 0 & h_{NN} \end{bmatrix}$$

#### **Estimating the Fixed Effects Model**

We could just include dummy variables for all but one of the units. This "sweeps out the unit effects" because when you mean deviate variables, you no longer need to include an intercept term. So the model regresses  $y_{i,t} - mean(y_i)$  on  $x_{i,t} - mean(x_i)$ . This is often called this "with-in" estimator because it looks at how changes in the explanatory variables cause y to vary around a mean within the unit.

#### **Random Effects models**

Instead of thinking of each unit as having its own systematic baseline, we think of each intercept as the result of a random deviation from some mean intercept. If we have a large N (panel data), we will be able to do this, and random effects will be more efficient than fixed effects. It has N more degrees of freedom, and it also uses information from the "between" estimator (which averages observations over a unit and regresses average y on average x to look at differences across units). If we have a big T (TS-CS data), then the difference between fixed effects and random effects, goes away.

$$y_{i,t} = \mu + \alpha_i + x_{i,t}\beta + e_{i,t}$$
(33)

Table 7 Distinguishing between random effects and fixed effects model<sup>14</sup>

Random vs. Fixed	Definition
Variables	<b>Random variable</b> : (1) is assumed to be measured with measurement error. The scores are a function of a true score and random error; (2) the values come from and are intended to generalize to a much larger population of possible values with a certain probability distribution (e.g., normal distribution); (3) the number of values in the study is small relative to the values of the variable as it appears in the population it is drawn from. <i>Fixed variable</i> : (1) assumed to be measured without measurement error; (2) desired generalization to population or other studies is to the same values; (3) the variable used in the study contains all or most of the variable's values in the population. It is important to distinguish between a variable that is <i>varying</i> and a variable that is <i>random</i> . A fixed variable can have different values, it is not necessarily invariant (equal) across groups.
Effects	<b>Random effect:</b> (1) different statistical model of regression or ANOVA model which assumes that an independent variable is random; (2) generally used if the levels of the independent variable are thought to be a small subset of the possible values which one wishes to generalize to; (3) will probably produce larger standard errors (less powerful). <i>Fixed effect</i> : (1) statistical model typically used in regression and ANOVA assuming independent variable is fixed; (2) generalization of the results apply to similar values of independent variable in the population or in other studies; (3) will probably produce smaller standard errors (more powerful).
Coefficients	<ul> <li><i>Random coefficient:</i> term applies only to MLR analyses in which intercepts, slopes, and variances can be assumed to be random. MLR analyses most typically assume random coefficients. One can conceptualize the coefficients obtained from the level-1 regressions as a type of random variable which comes from and generalizes to a distribution of possible values. Groups are conceived of as a subset of the possible groups.</li> <li><i>Fixed coefficient:</i> a coefficient can be fixed to be non-varying (invariant) across groups by setting its between group variance to zero.</li> <li>Random coefficients must be variable across groups. Conceptually, fixed coefficients may be invariant <i>or</i> varying across groups.</li> </ul>

#### Estimations of random and fixed effects model

In the next Table we will present the results from the fixed and random effect regressions. We will perform a Hausman test. Here we mention that when we do this panel models and

<sup>&</sup>lt;sup>14</sup> Newsom USP 656 Multilevel Regression Winter 2006

regressions on our data independent variables are collinear with the panel variable ctry, so we use second panel variable year because we cannot run the regressions otherwise. Table 8 Fixed effects model and random effects model (See Appendix 3)<sup>15</sup>

Dependent variable: lgdpgro	Logarithm of growth of GDP per capita PPP	Fixed Effects model	Random Effects model
variables		FE	RE
lpopgro	Log of growth rate of popula- tion	0.76	0.28
_Iyear_1951	Dummy 1951	-40.99	-56.28
_Iyear_1952	Dummy 1952	-37.999	-52.399
 Iyear_1953	Dummy 1953	-29.76	-43.268
_Iyear_1954	Dummy 1954	-41.07	-53.69
_Iyear_1955	Dummy 1955	-33.03	-44.74
_Iyear_1956	Dummy 1956	-34.37	-45.16
_Iyear_1957	Dummy 1957	-22.94	-32.79
_Iyear_1958	Dummy 1958	-19.70	-28.55
_Iyear_1959	Dummy 1959	-20.83	-28.67
_Iyear_1960	Dummy 1960	-109.62	-112.96
_Iyear_1961	Dummy 1961	-87.74	-90.35
_Iyear_1962	Dummy 1962	-77.88	-79.88
_Iyear_1963	Dummy 1963	-68.69	-70.14
_Iyear_2007	Dummy 2007	-149.48174***	-130.11**
_Iyear_2008	Dummy 2008	-188.25289***	-168.84***
	Dummy 2009	-106.23162*	-86.79*
_cons	Constant	-132.74	256.91
Ν		339	339

legend: \* p<0.05; \*\* p<0.01; \*\*\* p<0.001

In the time fixed effects model lpopgro is statistically significant t=1,75 at 10% level of significance, the coefficient is positive 0.76, meaning that 1% increase in growth of population will induce GDP growth of 0.76%. This variable in RE model has not got significant coefficient. We set years as number of dummies here. We set null hypothesis here that all dummies are equal to zero and we test with F statistics. Probability exceeding F statistics is  $0,8507^{16}$ 

<sup>&</sup>lt;sup>15</sup> See Appendix 3 Panel estimation techniques

<sup>&</sup>lt;sup>16</sup> See Appendix 3 testparm

this means that we cannot reject the null that all years coefficients are zero, therefore no time fixed effects are needed. Hausman test is in favor of Fixed effects model i.e. difference in coefficients is not systematic. Probability >chi2=1.000<sup>17</sup>. Coefficients for the years 2007.2008 and 2009 are highly significant but more negative than other years this is due to financial crisis if we controlled only for these three years on average we will get less positive association between GDP growth and population growth.

#### Panel unit root tests (See Appendix 4)

"xtunitroot performs a variety of tests for unit roots (or stationarity) in panel datasets. The Levin-Lin-Chu (2002), Harris-Tzavalis (1999), Breitung (2000; Breitung and Das 2005), Im-Pesaran-Shin (2003), and Fisher-type (Choi 2001) tests have as the null hypothesis that all the panels contain a unit root. The Hadri (2000) Lagrange multiplier (LM) test has as the null hypothesis that all the panels are (trend) stationary. The top of the output for each test makes explicit the null and alternative hypotheses. Options allow you to include panelspecific means (fixed effects) and time trends in the model of the data-generating process"<sup>18</sup>

xtfisher combines the p-values from N independent unit root tests, as developed by Maddala and Wu (1999). Based on the p-values of individual unit root tests, Fisher's test assumes that all series are non-stationary under the null hypothesis against the alternative that at least one series in the panel is stationary. Unlike the Im-Pesaran-Shin (1997) test (ipshin or xtunitroot ips), Fisher's test does not require a balanced panel. This test is based on augmented Dickey-Fuller tests.

Table 9 Panel Unit root tests Variable gdpgro (Growth of GDP)Ho: All panels contain unit rootsHa: At least one panel is stationary

Type of statistic	statistic	p-value	Decision
Inverse chi-squared(20) P	49.1548	0.0003	Sufficient evidence to accept H <sub>A</sub>
Inverse normal Z	-3.8714	0.0001	Sufficient evidence to accept H <sub>A</sub>
Inverse logit t(49) L*	-4.0690	0.0001	Sufficient evidence to accept H <sub>A</sub>
Modified inv. chi-squared Pm	4.6098	0.0000	Sufficient evidence to accept $H_A$

<sup>&</sup>lt;sup>17</sup> See Appendix 3 Hausman test

<sup>&</sup>lt;sup>18</sup> Source Stata manual

So we reject the null hypothesis that panels contain unit root and we accept the alternative that at least one panel is stationary.

#### Table 10 Panel Unit root tests Variable popgro (population growth) Ho: All panels contain unit roots Ha: At least one panel is stationary

Type of statistic	statistic	p-value	Decision
Inverse chi-squared(20) P	61.3497	0.0000	Sufficient evidence to accept $H_A$
Inverse normal Z	-4.5153	0.0000	Sufficient evidence to accept $H_A$
Inverse logit t(54) L*	-5.0274	0.0000	Sufficient evidence to accept $H_A$
Modified inv. chi-squared Pm	6.5380	0.0000	Sufficient evidence to accept $H_A$

So here also we reject the null hypothesis that panels contain unit root and we accept the alternative that at least one panel is stationary. In conclusion population growth and GDP growth are stationary.

#### Conclusion

This paper confirmed that for the Balkan countries also applies the rule of linear relationship between population growth and population, but also that demographic structure in the Balkan countries will be very old in the next decades. Optimal population growth depends on capital in the future period and future consumption. Turkey has highest population growth, while Macedonia lowest in the region, together with Slovenia that has little higher growth of population. In the OLS regression with dummies the coefficient on Macedonia, is highest significant coefficient meaning, if we control for Macedonia we will on average find more positive association between growth of GDP and population growth. Hausman test was in favor of FE model, but FE and RE model showed that there is positive coefficient between GDP growth and population growth. Coefficient in the FE model was statistically significant, which was not case in RE model. From the Fischer's panel unit root test we reject the null hypothesis that panels contain unit root and we accept the alternative that at least one panel is stationary, for the population growth and GDP growth.

. regress popgr	to pop					
Source	SS	df	MS		Number of obs F( 1, 588)	
Model	46.4512362 684.078853	1 46. 588 1.1	4512362 6339941		Prob > F R-squared Adj R-squared Root MSE	= 0.0000 = 0.0636 = 0.0620
popgro		Std. Err.	t	P> t	[95% Conf.	Interval]
pop   _cons		3.11e-06 .0554657		0.000	.0000135 .466433	.0000257

## Appendix 1 Regression on population growth and level of population

### Appendix 2 OLS and OLS\_dummies regression

Variable	ols	ols_dum
_Icountry_2   _Icountry_3   _Icountry_4   _Icountry_5   _Icountry_6   _Icountry_7   _Icountry_8   _Icountry_9   _Icountry_10	.12929031* 280.31333***	.05814148 4.8024968 23.983916 -61.154368* -55.759953 71.522809** 22.472556 86.099647 -87.803317** 10.780687 341.84296
N	339	339
legend: '	p<0.05; ** p<	0.01; *** p<0.001

## . xi: regress lgdpgro lpopgro i.country

\_Icountry\_1-10 (\_Icountry\_1 for coun~y==Albania omitted)

Source	SS	df	MS		Number of obs	=	339
+-					F(10, 328)	=	8.40
Model	650078.81	10 6	5007.881		Prob > F	=	0.0000
Residual	2537279.52	328 7	735.6083		R-squared	=	0.2040
+-					Adj R-squared	=	0.1797
Total	3187358.33	338 94	30.05423		Root MSE	=	87.952
lgdpgro	Coef.	Std. Err	. t	P> t	[95% Conf.	In	terval]
+-							
lpopgro	.0581415	.2607112	0.22	0.824	4547355	•	5710185

_Icountry_2	4.802497	25.39018	0.19	0.850	-45.14565	54.75064
_Icountry_3	23.98392	33.98436	0.71	0.481	-42.87089	90.83872
_Icountry_4	-61.15437	26.33497	-2.32	0.021	-112.9611	-9.347613
_Icountry_5	-55.75995	35.73427	-1.56	0.120	-126.0572	14.53731
_Icountry_6	71.52281	25.75835	2.78	0.006	20.85039	122.1952
_Icountry_7	22.47256	55.59951	0.40	0.686	-86.90407	131.8492
_Icountry_8	86.09965	45.34624	1.90	0.058	-3.10652	175.3058
_Icountry_9	-87.80332	26.78825	-3.28	0.001	-140.5018	-35.10485
_Icountry_10	10.78069	73.11564	0.15	0.883	-133.0541	154.6154
_cons	341.843	181.9686	1.88	0.061	-16.12976	699.8157

Source	SS	df	MS		Number of obs	
Model   Residual	61128.9658 3126229.37	1 6112 337 92	28.9658 276.645		F( 1, 337) Prob > F R-squared Adj R-squared	= 0.0107 = 0.0192
Total	3187358.33		.05423		Root MSE	= 96.315
lgdpgro	Coef.	Std. Err.	t	P> t		Interval]
lpopgro   _cons	.1292903 280.3133	.0503661 41.14543	2.57 6.81	0.011	.0302189 199.3791	.2283618 361.2475

Variable	ols	ols_dum
+		
lpopgro	.12929031*	.05814148
_Icountry_2		4.8024968
_Icountry_3		23.983916
_Icountry_4		-61.154368*
_Icountry_5		-55.759953
_Icountry_6		71.522809**
_Icountry_7		22.472556
_Icountry_8		86.099647
_Icountry_9		-87.803317**
_Icountry_10		10.780687
_cons	280.31333***	341.84296
+		
N	339	339
legend:	* p<0.05; ** p<0	0.01; *** p<0.001

# Appendix 3 Panel estimation techniques

. xi: xtreg l i.year		-		y coded;	_Iyear_1950 (	omitted)
Fixed-effects Group variable	-	ression		Number ( Number (	of obs = of groups =	339 10
	$= 0.1490 \\ = 0.0464 \\ = 0.0597$			Obs per	group: min = avg = max =	6 33.9 60
corr(u_i, Xb)	= -0.7906			F(60,26) Prob > 1		
lgdpgro	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
lpopgro   _Iyear_1951   _Iyear_1952	-40.98947 -37.99571	.4349449 71.56379 71.45078	1.75 -0.57 -0.53	0.081 0.567 0.595	0957353 -181.8858 -178.6696	1.616923 99.90689 102.6782
_Iyear_1953   _Iyear_1954   _Iyear_1955   _Iyear_1956	-41.06829 -33.02969 -34.36171	71.34648 71.25146 71.1641 71.08532	-0.42 -0.58 -0.46 -0.48	0.677 0.565 0.643 0.629	-170.2264 -181.3497 -173.1391 -174.3161	110.7107 99.21316 107.0798 105.5926
_Iyear_1957   _Iyear_1958   _Iyear_1959   Iyear 1960	-19.70167 -20.82628	71.01376 70.94973 70.89659 60.4036	-0.32 -0.28 -0.29 -1.81	0.747 0.781 0.769 0.071	-162.7577 -159.3891 -160.409 -228.5477	116.8692 119.9857 118.7565 9.300167
	-77.87545 -68.6982	60.40654 60.41447 60.42612 60.44104	-1.45 -1.29 -1.14 -1.10	0.148 0.198 0.257 0.273	-206.6724 -196.8208 -187.6665 -185.4488	31.18708 41.06989 50.27006 52.54655
 Iyear_1965   Iyear_1966   Iyear_1967	-62.68548 -60.85861 -54.70754	60.4597 60.48429 60.51841	-1.04 -1.01 -0.90	0.301 0.315 0.367	-181.7199 -179.9414 -173.8575	56.34889 58.2242 64.44242
_Iyear_1968   _Iyear_1969   _Iyear_1970   _Iyear_1971	-156.2577 -145.0668 -138.3513	60.56466 60.61089 51.06815 51.1494	-3.27 -2.58 -2.84 -2.70	0.001 0.010 0.005 0.007	-317.581 -275.5898 -245.6109 -239.0554	-79.09895 -36.92568 -44.5227 -37.64727
_Iyear_1972   _Iyear_1973   _Iyear_1974   _Iyear_1975	-122.658 -125.865	51.24072 51.32261 51.42468 51.5398	-2.53 -2.39 -2.45 -2.31	0.012 0.018 0.015 0.022	-230.3177 -223.7031 -227.111 -220.4939	-28.54999 -21.61294 -24.61893 -17.54848
_Iyear_1976   _Iyear_1977   _Iyear_1978   Iyear 1979	-104.646 -96.13875	51.6613 51.7932 51.91444 52.03819	-2.15 -2.02 -1.85 -1.80	0.033 0.044 0.065 0.073	-212.5373 -206.6176 -198.349 -196.1563	-9.113524 -2.674423 6.071541 8.751567
 Iyear_1980   Iyear_1981   Iyear_1982	-93.30143 -97.08487 -97.20503	52.16077 52.29739 52.42912	-1.79 -1.86 -1.85	0.075 0.064 0.065	-195.9967 -200.0491 -200.4286	9.393845 5.879381 6.018566
_Iyear_1983   _Iyear_1984   _Iyear_1985   _Iyear_1986	-95.16551 -92.94244 -88.78871	52.55625 52.68298 52.81052 52.93538	-1.86 -1.81 -1.76 -1.68	0.064 0.072 0.080 0.095	-201.1021 -198.8889 -196.9169 -193.0091	5.845729 8.557902 11.03207 15.43164
_Iyear_1987   _Iyear_1988   _Iyear_1989   Iyear 1990	-86.13444 -84.9631	53.06046 53.18221 53.31231 45.76825	-1.70 -1.62 -1.59 -2.91	0.090 0.106 0.112 0.004	-194.7273 -190.8407 -189.9255 -223.2762	14.20585 18.57186 19.99934 -43.05715
Iyear_1991   Iyear_1992   Iyear_1993   Iyear_1994	-109.3995 -115.1622 -111.2897	45.79388 45.67449 45.56029	-2.39 -2.52 -2.44 -2.22	0.018 0.012 0.015	-199.5595 -205.0871 -200.9898	-19.23946 -25.23725 -21.58964
_1year_1994   _1year_1995		45.55359 45.56847	-2.22	0.027 0.045	-190.9822 -181.6085	-11.60843 -2.176119

- 1000	00 000	45 56070	1	0 070	170 0001	0 01 0 0 0 0
_Iyear_1996	-80.682	45.56079	-1.77	0.078	-170.3831	9.019093
_Iyear_1997	-79.65478	45.58771	-1.75	0.082	-169.4089	10.09931
_Iyear_1998	-73.52062	45.68832	-1.61	0.109	-163.4728	16.43155
_Iyear_1999	-68.16816	45.75291	-1.49	0.137	-158.2475	21.91118
_Iyear_2000	-63.60586	45.79475	-1.39	0.166	-153.7676	26.55584
_Iyear_2001	-134.7835	47.13355	-2.86	0.005	-227.581	-41.98589
_Iyear_2002	-107.8351	47.17669	-2.29	0.023	-200.7176	-14.9526
_Iyear_2003	-97.18599	45.92017	-2.12	0.035	-187.5946	-6.777339
_Iyear_2004	-90.45919	45.96222	-1.97	0.050	-180.9506	.0322352
_Iyear_2005	-90.43073	45.8519	-1.97	0.050	-180.705	1565113
_Iyear_2006	-131.8986	44.79873	-2.94	0.004	-220.0993	-43.69785
_Iyear_2007	-149.4817	44.81625	-3.34	0.001	-237.717	-61.24651
_Iyear_2008	-188.2529	44.82956	-4.20	0.000	-276.5143	-99.99146
_Iyear_2009	-106.2316	44.839	-2.37	0.019	-194.5116	-17.95161
_cons	-132.7358	341.1825	-0.39	0.698	-804.4635	538.9918
+-						
sigma_u	87.310538					
sigma e	89.598029					
rho	.4870718	(fraction	of variar	nce due t	oui)	
F test that all	u i=0:	F(9, 269) =	8.73	3	Prob >	F = 0.0000
		(-,,				

#### testparm

. testparm \_Iyear\*

(1)	_Iyear_1951 = 0	
(2)	_Iyear_1952 = 0	
(3)	_Iyear_1953 = 0	
(4)	_Iyear_1954 = 0	
(5)	_Iyear_1955 = 0	
(6)	_Iyear_1956 = 0	
(7)	_Iyear_1957 = 0	
(8)	_Iyear_1958 = 0	
(9)	_Iyear_1959 = 0	
(10)	_Iyear_1960 = 0	
(11)	_Iyear_1961 = 0	
(12)	_Iyear_1962 = 0	
(13)	_Iyear_1963 = 0	
(14)	_Iyear_1964 = 0	
(15)	_Iyear_1965 = 0	
(16)	_Iyear_1966 = 0	
(17)	_Iyear_1967 = 0	
(18)	_Iyear_1968 = 0	
(19)	_Iyear_1969 = 0	
(20)	_Iyear_1970 = 0	
(21)	_Iyear_1971 = 0	
(22)	$_{_{_{_{_{_{}}}}}}$ Iyear_1972 = 0	
(23)	_Iyear_1973 = 0	
(24)	_Iyear_1974 = 0	
(25)	_Iyear_1975 = 0	
(26)	_Iyear_1976 = 0	
(27)	_Iyear_1977 = 0	
(28)	$_{_{_{_{_{_{}}}}}}$ Iyear_1978 = 0	
(29)	_Iyear_1979 = 0	
(30)	_Iyear_1980 = 0	
(31)	_Iyear_1981 = 0	
(32)	_Iyear_1982 = 0	
(33)	_Iyear_1983 = 0	
(34)	_Iyear_1984 = 0	
(35)	Iyear 1985 = 0	
(36)		
(37)		
(38)		
(39)		
(40)		
(41)		

(42)	_Iyear_1992 = 0	
(43)	_Iyear_1993 = 0	
(44)	_Iyear_1994 = 0	
(45)	_Iyear_1995 = 0	
(46)	_Iyear_1996 = 0	
(47)	_Iyear_1997 = 0	
(48)	_Iyear_1998 = 0	
(49)	_Iyear_1999 = 0	
(50)	_Iyear_2000 = 0	
(51)	_Iyear_2001 = 0	
	$_{Iyear_{2002} = 0}$	
(53)	_Iyear_2003 = 0	
(54)	$_{iyear_{2004} = 0}$	
(55)	_Iyear_2005 = 0	
(56)	_Iyear_2006 = 0	
(57)	_Iyear_2007 = 0	
(58)	_Iyear_2008 = 0	
(59)	_Iyear_2009 = 0	
	F(59, 269) =	0.80
	Prob > F =	0.8507

. We failed to reject the null that all years coefficients are jointly equal to zero therefore no time fixed effects are needed.

. estimates store fixed . xi: xtreg lgdpgro lpopgro i.year, re \_Iyear\_1950-2009 (naturally coded; \_Iyear\_1950 omitted) i.vear Random-effects GLS regression Number of obs = 339 Number of groups = Group variable: ctry 10 R-sq: within = 0.1451Obs per group: min = 6 between = 0.0292avg = 33.9 overall = 0.1063max = 60 Random effects u\_i ~ Gaussian Wald chi2(60) = 45.80 0.9120 corr(u i, X) = 0 (assumed) Prob > chi2 = \_\_\_\_\_ lgdpgro | Coef. Std. Err. z P>|z| [95% Conf. Interval] \_\_\_\_\_ lpopgro | .2798707 .2033972 1.38 0.169 -.1187805 .6785219 \_Iyear\_1951 | -56.28473 70.55534 -0.80 0.425 -194.5707 82.00118 \_Iyear\_1952 | -52.39935 70.53754 -0.74 0.458 -190.6504 85.85168 \_Iyear\_1953 | -43.2677 70.52172 -0.61 0.540 -181.4877 94.95233 \_Iyear\_1955 | -44.74231 \_Iyear\_1956 | -45.15891 -183.3091 70.48611 Iyear 1957 | -32.79237 70.47806 -0.47 0.642 -170.9268 105.3421 \_\_\_\_\_ Iyear 1958 | -28.55334 70.47207 -0.41 0.685 -166.6761 109.5694 \_Iyear\_1959 | -28.67037 70.46858 -0.41 0.684 -166.7862 109.4455 \_Iyear\_1960 | -112.9651 60.12139 -1.88 0.060 -230.8009 4.870631 -1.50 0.133 -208.2025 \_Iyear\_1961 | -90.35182 60.12901 27.49888 60.13654 60.14439 -1.33 0.184 -1.17 0.244 \_Iyear\_1962 | -79.87784 -197.7433 37.98761 \_Iyear\_1963 | -70.14497 -188.0258 47.73587 60.1527 -1.12 0.263 -185.2674 50.52689 \_Iyear\_1964 | -67.37024 \_Iyear\_1965 | -63.078 60.16182 -1.05 0.294 -180.993 54.837 \_Iyear\_1966 | -60.67713 60.17269 -1.01 0.313 -178.6134 57.25918 \_Iyear\_1967 | -53.86012 60.18654 -0.89 0.371 -171.8236 64.10332 \_Iyear\_1968 | -196.7322 60.20395 -314.7298 -78.73463 -3.27 0.001 Iyear\_1969-153.992960.22038Iyear\_1970-139.969950.51022Iyear\_1971-132.609450.53302 -2.56 0.011 -2.77 0.006 -2.62 0.009 -272.0227 -35.96313 -238.9681 -40.9717 -231.6523 -33.56648

_Iyear_1972	-123.0217	50.55826	-2.43	0.015	-222.114	-23.92932
_Iyear_1973	-115.6844	50.58061	-2.29	0.022	-214.8206	-16.54824
_Iyear_1974	-118.2342	50.60818	-2.34	0.019	-217.4244	-19.04395
_Iyear_1975	-110.6957	50.63897	-2.19	0.029	-209.9463	-11.44513
_Iyear_1976	-101.8109	50.67118	-2.01	0.045	-201.1246	-2.497197
_Iyear_1977	-94.92584	50.70588	-1.87	0.061	-194.3075	4.455856
_Iyear_1978	-85.80285	50.73757	-1.69	0.091	-185.2467	13.64096
_Iyear_1979	-82.76576	50.76976	-1.63	0.103	-182.2727	16.74113
_Iyear_1980	-81.79398	50.8015	-1.61	0.107	-181.3631	17.77514
_Iyear_1981	-84.96605	50.83676	-1.67	0.095	-184.6043	14.67216
_Iyear_1982	-84.51868	50.87063	-1.66	0.097	-184.2233	15.18593
_Iyear_1983	-84.41229	50.90325	-1.66	0.097	-184.1808	15.35623
_Iyear_1984	-81.43782	50.93568	-1.60	0.110	-181.2699	18.39429
_Iyear_1985	-78.71435	50.96827	-1.54	0.122	-178.6103	21.18163
	-74.08371	51.00012	-1.45	0.146	-174.0421	25.87469
	-75.0899	51.03199	-1.47	0.141	-175.1108	24.93096
	-70.52065	51.06297	-1.38	0.167	-170.6022	29.56093
	-68.88661	51.09605	-1.35	0.178	-169.033	31.25982
	-116.5801	43.00243	-2.71	0.007	-200.8633	-32.29684
	-92.7368	43.00835	-2.16	0.031	-177.0316	-8.441991
	-98.85596	42.98083	-2.30	0.021	-183.0968	-14.61508
	-95.33006	42.95457	-2.22	0.026	-179.5195	-11.14065
	-85.35618	42.95303	-1.99	0.047	-169.5426	-1.169792
	-75.90763	42.95645	-1.77	0.077	-160.1007	8.285464
	-64.72078	42.95468	-1.51	0.132	-148.9104	19.46886
	-63.61137	42.96087	-1.48	0.139	-147.8131	20.59039
	-57.17279	42.98402	-1.33	0.183	-141.4199	27.07433
	-51.62716	42.9989	-1.20	0.230	-135.9034	32.64913
	-46.94064	43.00855	-1.09	0.275	-131.2358	37.35456
	-117.3597	44.41108	-2.64	0.008	-204.4038	-30.31559
	-90.2815	44.42131	-2.03	0.042	-177.3457	-3.217338
	-80.1525	43.03751	-1.86	0.063	-164.5045	4.199475
	-73.3036	43.04724	-1.70	0.089	-157.6746	11.06743
	-70.34215	43.00249	-1.64	0.102	-154.6255	13.94118
	-112.5712	41.85031	-2.69	0.007	-194.5963	-30.54614
Iyear 2007	-130.1051	41.8544	-3.11	0.002	-212.1383	-48.07203
Iyear 2008	-168.8389	41.85751	-4.03	0.000	-250.8782	-86.79974
Iyear 2009	-86.79124	41.85971	-2.07	0.038	-168.8348	-4.747705
cons	256.9051	155.7634	1.65	0.099	-48.38564	562.1958
+						
sigma u	71.607679					
sigma e	89.598029					
rho	.38977407	(fraction	of variar	nce due t	coui)	
					—	

\_\_\_\_\_

•

. estimates table fixed random, star stats(N r2 r2\_a)

Variable		fixed	random
lpopgro		.7605937	.27987068
_Iyear_1951		-40.989471	-56.284735
_Iyear_1952		-37.995715	-52.39935
_Iyear_1953		-29.757835	-43.267699
_Iyear_1954		-41.068291	-53.68698
_Iyear_1955		-33.029687	-44.742312
_Iyear_1956		-34.361712	-45.158912
_Iyear_1957		-22.944289	-32.792366
_Iyear_1958		-19.701667	-28.553338
_Iyear_1959		-20.82628	-28.670366
_Iyear_1960		-109.62376	-112.96512
_Iyear_1961		-87.742636	-90.351818
_Iyear_1962		-77.875454	-79.877844
_Iyear_1963		-68.698204	-70.144973

_Iyear_1964	-66.451109	-67.370239
Iyear 1965	-62.685482	-63.078
	-60.858608	-60.677127
	-54.707543	-53.860119
	-198.33999**	-196.7322**
	-156.25773*	-153.9929*
	-145.0668**	-139.96991**
_Iyear_1971	-138.35133**	-132.60937**
_Iyear_1972	-129.43385*	-123.02167*
Iyear 1973	-122.65802*	-115.68442*
 Iyear 1974	-125.86497*	-118.23417*
	-119.02118*	-110.69569*
	-110.82543*	-101.81088*
	-104.64602*	-94.925836
	-96.138746	-85.802845
_Iyear_1979	-93.702372	-82.765761
_Iyear_1980	-93.301426	-81.79398
Iyear 1981	-97.084873	-84.966048
	-97.205033	-84.518683
	-97.628174	-84.412295
	-95.165505	-81.437819
	-92.942442	-78.714345
	-88.788709	-74.083709
	-90.260748	-75.089896
	-86.134437	-70.520653
_Iyear_1989	-84.963103	-68.886611
_Iyear_1990	-133.16668**	-116.58006**
_Iyear_1991	-109.39946*	-92.736801*
Iyear 1992	-115.16219*	-98.855958*
	-111.28974*	-95.33006*
	-101.29533*	-85.356181*
	-91.892333*	-75.907629
	-80.682	-64.720779
		-63.611366
	-73.520622	-57.172791
	-68.168159	-51.62716
_Iyear_2000	-63.605863	-46.940641
_Iyear_2001	-134.78347**	-117.35971**
_Iyear_2002	-107.8351*	-90.281499*
_Iyear_2003	-97.185988*	-80.152504
_Iyear_2004	-90.459194	-73.303605
	-90.430732*	-70.342153
 Ivear 2006	-131.89859**	-112.57124**
	-149.48174***	-130.10514**
	-188.25289***	-168.83895***
	-106.23162*	-86.791237*
_cons	-132.73585	256.9051
	 >>0	 220
N		339
	.14902846	
r2_a	06925048	
1 '	+	) 01. +++ - <0 001
⊥egend:	^ p<0.05; ** p<0	).01; *** p<0.001

#### Hausman test

. hausman fixed random

.

	(b)	(B)	(b-B)	sqrt(diag(V_b-V_B))
1	fixed	random	Difference	S.E.
+-				
lpopgro	.7605937	.2798707	.480723	.3844562
_Iyear_1951	-40.98947	-56.28473	15.29526	11.97167
_Iyear_1952	-37.99571	-52.39935	14.40363	11.38728

Tuon 1053	-29.75784	-43.2677	13.50986	10.81699
_Iyear_1953 Iyear 1954		-53.68698	12.61869	10.26638
_iyear_1954 Iyear 1955		-44.74231	11.71262	9.728177
_iyear_1955 Iyear 1956		-45.15891	10.7972	9.210406
		-32.79237	9.848077	8.706126
_iyear_1957 Iyear 1958	-22.94429   -19.70167	-28.55334	8.851671	8.21897
		-28.55334		
_Iyear_1959			7.844086	7.778513
_Iyear_1960		-112.9651	3.341357	5.832114
_Iyear_1961		-90.35182 -79.87784	2.609181	5.783722
_Iyear_1962			2.00239	5.788372
_Iyear_1963		-70.14497	1.446769 .9191297	5.828173 5.896799
_Iyear_1964 Iyear 1965		-67.37024 -63.078		5.994197
		-60.67713	.3925173 1814807	
_Iyear_1966		-53.86012	8474237	6.131626
_Iyear_1967 Iyear 1968		-196.7322	-1.607786	6.329167
_iyear_1968 Iyear 1969		-198.7322	-2.264839	6.600189 6.869222
		-139.9699	-2.284839	7.528222
_Iyear_1970 Iyear 1971		-132.6094	-5.741962	7.916782
_iyear_1971 Iyear 1972		-123.0217	-6.412175	8.335137
_iyear_1972 Iyear 1973		-115.6844	-6.973604	8.69553
	-125.865	-118.2342	-7.630801	9.127388
_Iyear_1974 Iyear 1975		-110.6957	-8.325484	9.12/388
_iyear_1975 Iyear 1976		-101.8109	-9.014546	10.06587
_iyear_1970 Iyear 1977		-94.92584	-9.720186	10.55699
_iyear_1977 Iyear 1978	-96.13875	-85.80285	-10.3359	10.99127
_iyear_1978 Iyear 1979		-82.76576	-10.93661	11.41952
_iyear_1980 Iyear 1980		-81.79398	-11.50745	11.83018
_iyear_1980 Iyear 1981		-84.96605	-12.11882	12.27361
_iyear_1981 Iyear 1982		-84.51868	-12.68635	12.68822
_iyear_1983 Iyear 1983		-84.41229	-13.21588	13.07743
		-81.43782	-13.72769	13.45557
		-78.71435	-14.2281	13.82702
		-74.08371	-14.705	14.18247
		-75.0899	-15.17085	14.53095
		-70.52065	-15.61378	14.86337
		-68.88661	-16.07649	15.21169
 Iyear 1990		-116.5801	-16.58663	15.66919
 Iyear 1991		-92.7368	-16.66266	15.72775
		-98.85596	-16.30623	15.45338
 Iyear 1993		-95.33006	-15.95968	15.187
		-85.35618	-15.93915	15.17124
 Iyear_1995		-75.90763	-15.9847	15.20623
		-64.72078	-15.96122	15.18819
 Iyear 1997	-79.65478	-63.61137	-16.04342	15.25134
Iyear 1998		-57.17279	-16.34783	15.48539
 Iyear 1999		-51.62716	-16.541	15.63405
	-63.60586	-46.94064	-16.66522	15.72972
	-134.7835	-117.3597	-17.42376	15.78695
	-107.8351	-90.2815	-17.5536	15.88671
	-97.18599	-80.1525	-17.03348	16.01358
	-90.45919	-73.3036	-17.15559	16.10779
	-90.43073	-70.34215	-20.08858	15.9117
		-112.5712	-19.32735	15.98369
		-130.1051	-19.3766	16.02204
	-188.2529	-168.8389	-19.41394	16.05112
	-106.2316	-86.79124	-19.44038	16.07172

b = consistent under Ho and Ha; obtained from xtreg B = inconsistent under Ha, efficient under Ho; obtained from xtreg

Test: Ho: difference in coefficients not systematic

chi2(60) = (b-B)'[(V\_b-V\_B)^(-1)](b-B) = 2.92 Prob>chi2 = 1.0000

#### **Appendix 4 Unit root tests**

. xtunitroot fisher gdpgro, dfuller trend lags(4) (1 missing value generated) Fisher-type unit-root test for gdpgro Based on augmented Dickey-Fuller tests \_\_\_\_\_ = Ho: All panels contain unit roots Number of panels 10 Avg. number of periods = 59.90 Ha: At least one panel is stationary AR parameter: Panel-specific Asymptotics: T -> Infinity Panel means: Included Time trend: Included Drift term: Not included ADF regressions: 4 lags \_\_\_\_\_ \_\_\_\_\_ Statistic p-value \_\_\_\_\_ Inverse chi-squared(20) P 49.1548 0.0003 Inverse normal Z Inverse logit t(49) L\* 0.0001 -3.8714 Inverse logit t(49) L\* -4.0690 Modified inv. chi-squared Pm 4.6098 0.0001 0.0000 \_\_\_\_\_ \_\_\_\_\_ \_\_\_\_\_ P statistic requires number of panels to be finite. Other statistics are suitable for finite or infinite number of panels. xtunitroot fisher popgro, dfuller trend lags(4) (1 missing value generated) Fisher-type unit-root test for popgro Based on augmented Dickey-Fuller tests \_\_\_\_\_ Number of panels Ho: All panels contain unit roots = 10 Avg. number of periods = 59.90 Ha: At least one panel is stationary AR parameter: Panel-specific Asymptotics: T -> Infinity Panel means: Included Time trend: Included Drift term: Not included ADF regressions: 4 lags \_\_\_\_\_ Statistic p-value \_\_\_\_\_ Inverse chi-squared(20) P 61.3497 Inverse normal Z -4.5153 0.0000 Inverse normalZ-4.5153Inverse logit t(54)L\*-5.0274Modified inv. chi-squared Pm6.5380 0.0000 0.0000 0.0000 P statistic requires number of panels to be finite. Other statistics are suitable for finite or infinite number of panels.

#### References

- [1] Alan Heston, Robert Summers and Bettina Aten, Penn World Table Version 7.0, Center for International Comparisons of Production, Income and Prices at the University of Pennsylvania, May 2011.
- [2] Assaf Razin and Uri Ben-Zion,(1973), *An intergenerational model of population growth*, Discussion Paper No. 73-34,University of Minnesota
- [3] Badi H. Baltagi, (2008), Econometric Analysis of Panel Data, Wiley
- [4] Birdsall, N., (1988), Handbook of development economics ,Volume 1, edited by T.N.Srinivasan
- [5] Greene ,William H.,(2008), *Econometric analysis*, Upper Saddle River, N.J. : Prentice Hall, 2008
- [6] Greene, W.(2001), Estimating Econometric Models with Fixed Effects, *Department* of Economics, Stern School of Business, New York University
- [7] Michael Kremer (1993), "Population Growth and Technological Change: One Million B.C. to 1990," *Quarterly Journal of Economics* 108:3 (August), pp. 681-716.
- [8] Ramsey, F., P.(1928), A Mathematical theory of saving, The Economic journal Vol.38 No.152
- [9] Paul R. Ehrlich and John P. Holdren, (1971), Impact of Population Growth, Science, New Series, Vol. 171, No. 3977 (Mar. 26, 1971), pp. 1212-1217
- [10] Podestà,F.(2002),Recent developments in quantitative comparative methodology: The case of pooled time series cross-section analysis, DSS PAPERS SOC 3-02
- [11] Wooldridge, J.M., 1995, Selection corrections for panel data models under conditional mean independence assumptions, Journal of Econometrics 68, 115-132.