Foundations of the economic and social history of the United States: Empirical

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Volume One

Empirical Foundations of the Economic and Social History of the United States

by Scott A. Albers

At present the consequences of this hypothesis (of a fifth dimension unifying general relativity and Maxwell's equations for electro-magnetism) cannot be estimated; furthermore there are other possibilities to be investigated. In any case, every Anzatz which claims universal validity is threatened by the sphinx of modern physics, quantum theory.

Theodor Kaluza
On the Problem of Unity in Physics, 1921

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[1]   The pagination of this volume is designed to permit a two-page pdf view of the material. At several points in these essays it is convenient to contrast the material on the left hand side of the screen with the right hand side.

PREFACE: PREDICTIONS

At the dawn of the last century Albert Einstein proposed that three dimensions of space and one dimension of time must be considered to understand the world around us. In 1919 Theodor Kaluza proposed an undiscovered "fifth dimension" which might be used to unify General Relativity with Maxwell's equations for electro-magnetism. He writes: "Even with full regard for the physical and epistemological difficulties outlined which tower before the above developed view, it appears hard to believe that those relations, hardly to be surpassed in their formal correspondence, are nothing more than an alluring play of whimsical chance." (Kaluza, 1921)

As these ideas relate to the social sciences we must admit that the prevailing view of time, at least as it presents itself to the historian, the economist or the social scientist, is hardly better than "one damn thing after another." However the growing body of historic, social and particularly economic data which has been collected over the past three centuries permits us to challenge this view.

On December 8, 2003 an early draft of this essay entitled "The Coming Panic of 2005" was sent to Mr. Jim Foley, head of the Montana office of Senator Max Baucus, chairman of the Senate Finance Committee. The abstract of the article states:

> A 56-year spiral of American economic growth demonstrates the Fibonacci Series, thereby illustrating the mathematic and biologic relationship between the American economy and the natural phenomena underlying it. This spiral provides the basis for a prediction that *the year 2005 will mark a tremendous diplomatic and financial panic throughout the world.* The chief advantage of this approach is that it provides exact dates as to when change will occur, and hints as to what sort of change will occur. This approach anticipates that the years 1781, 1837, 1949 and 2005 will be analogous to one another, each year presenting a sudden, dramatic challenge to the United States. (emphasis supplied)

Ten months later, on September 17, 2004, the FBI also warned that a financial crisis was imminent. http://www2.fbi.gov/congress/congress04/swecker100704.htm

> The potential impact of mortgage fraud on financial institutions and the stock market is clear. If fraudulent practices become systemic within the mortgage industry and mortgage fraud is allowed to become unrestrained, it will ultimately place financial institutions at risk and have adverse effects on the stock market. Investors may lose faith and require higher returns from mortgage backed securities. This may result in higher interest rates and fees paid by borrowers and limit the amount of investment funds available for mortgage loans.

> Often times, mortgage loans are sold in secondary markets or are used by financial institutions as collateral for other investments. Repurchase agreements have been utilized by investors for protection against mortgage fraud. When loans sold in the secondary market default and have fraudulent or material misrepresentation, loans are repurchased by the lending financial institution based

on a "repurchase agreement." As a result, these loans become a non performing asset. In extreme fraud cases, the mortgage backed security is worthless. Mortgage fraud losses adversely affect loan loss reserves, profits, liquidity levels and capitalization ratios, ultimately affecting the soundness of the financial institution.

The first prediction above precedes by ten months the warning given by the FBI to Congress in September, 2004. Both warnings highlight the historic precedents and imminent nature of the crisis, i.e. 2005. Yet nothing was done to anticipate or to mitigate the forewarned and even expected "tremendous diplomatic and financial panic throughout the world."

On November 4, 2008 Senator Barrack Obama was elected 44th President of the United States and its first African-American President in the midst of a devastating Global Financial Crisis, wars in Afghanistan and Iraq, and with the largest popular vote in American history. To put in perspective the significance of these predictions in light of subsequent experience, see Roberts, 2011.

How did the official leaders of capitalist economic strategy act before, during and after the Great Recession?

Before 2007, no official strategist of economic policy forecast any crisis. US Fed Chairman Greenspan in 2004 told us that *"a national severe price distortion is most unlikely in real estate."* In 2006, he told us that *"the worst may be over for housing,"* just the housing bubble burst. US treasury secretary Hank Paulson said the crisis in the overall economy "appears to be contained," March 2007.

During the crisis, in October 2008, the great financial maestro Greenspan told the US Congress, *"I am in a state of shocked disbelief."* He was questioned: *"In other words, you found that your view of the world, your ideology was not right, it was not working?"* (House Oversight Committee Chair, Henry Waxman). *"Absolutely, precisely, you know that's precisely the reason I was shocked, because I have been going for 40 years or more with very considerable evidence that it was working exceptionally well."*[2]

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[2]   As taken from "The causes of the Great Recession: mainstream and heterodox interpretations and the cherry pickers," emphasis in the original. http://www.karlmarx.net/marx-crisis-theory/thecausesofthegreatrecessionmainstreamandheterodoxinterpretationsandthecherrypickers

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1.1 The basis for predictions of crises

If the amendments to the federal constitution of the United States are tracked according to their placement in a unit circle, moving clock-wise in a 56-year cycle, we have the following. The portion in blue represents a 22-year "upswing" in American history, a period of increasing radicalization. The portion in pink represents a 22-year "downswing" in American history, a period of increasing conservatism. The two portions in purple represent two 6-year "transition periods" lodged between the two opposing and longer periods of time. (Albers & Albers, 2011)

DIAGRAM 5-4.
UPSWING, TRANSITION AND DOWNSWING IN THE KONDRATIEV WAVE
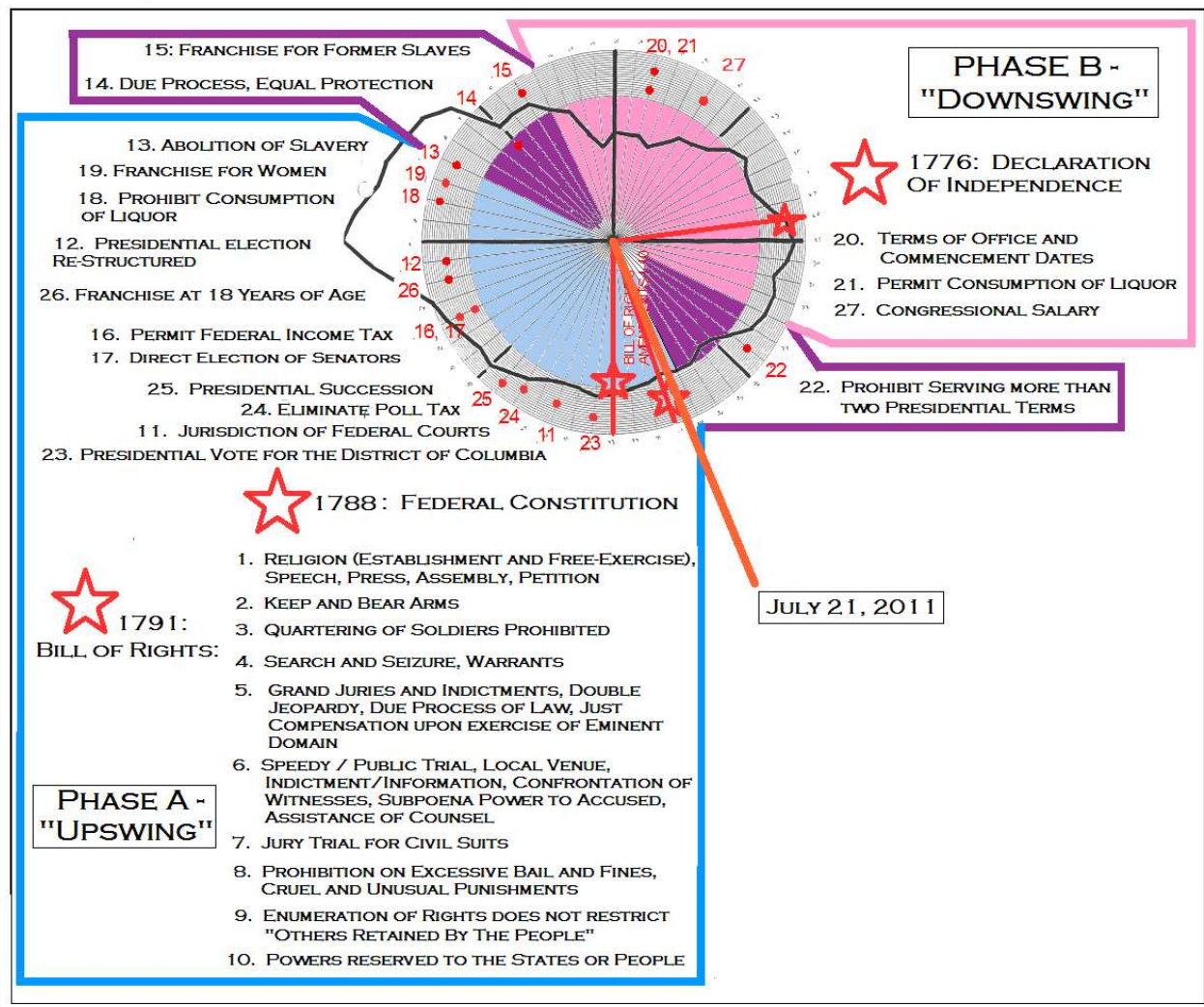
If these same amendments are placed in a sine wave based upon the same unit circle we have the following. One can plainly see that the most significant amendments, and the vast majority of amendments, are associated with the upswing of the sine curve.

DIAGRAM 5-5.
56-YEAR KONDRATIEV SINE WAVE WITH AMENDMENTS IN UPSWING AND DOWNSWING PERIODS
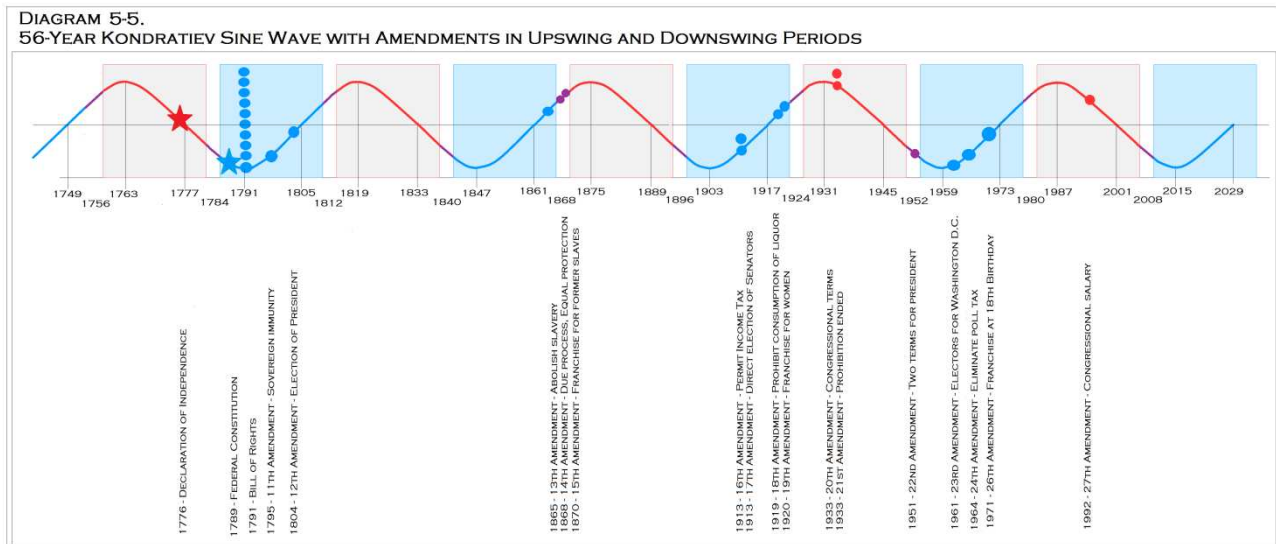
This chart may be better viewed placed on end, as set forth on the following page. Note that the up-swing amendments change the character of the American history, whereas the down-swing amendments generally enshrine a previously established set of values.

On the basis of these regularities I argue that a form of consciousness may be found in American economic history, one which is both mathematically demonstrable and important. In this book I present a model of economic and political growth based upon systematic addition.

We begin with a philosophic model of trade (pp. 34-46);

aggregate this model over the course of year to state the real Gross National Product of the United States and its relationship to the rate of employment (pp. 47-62);
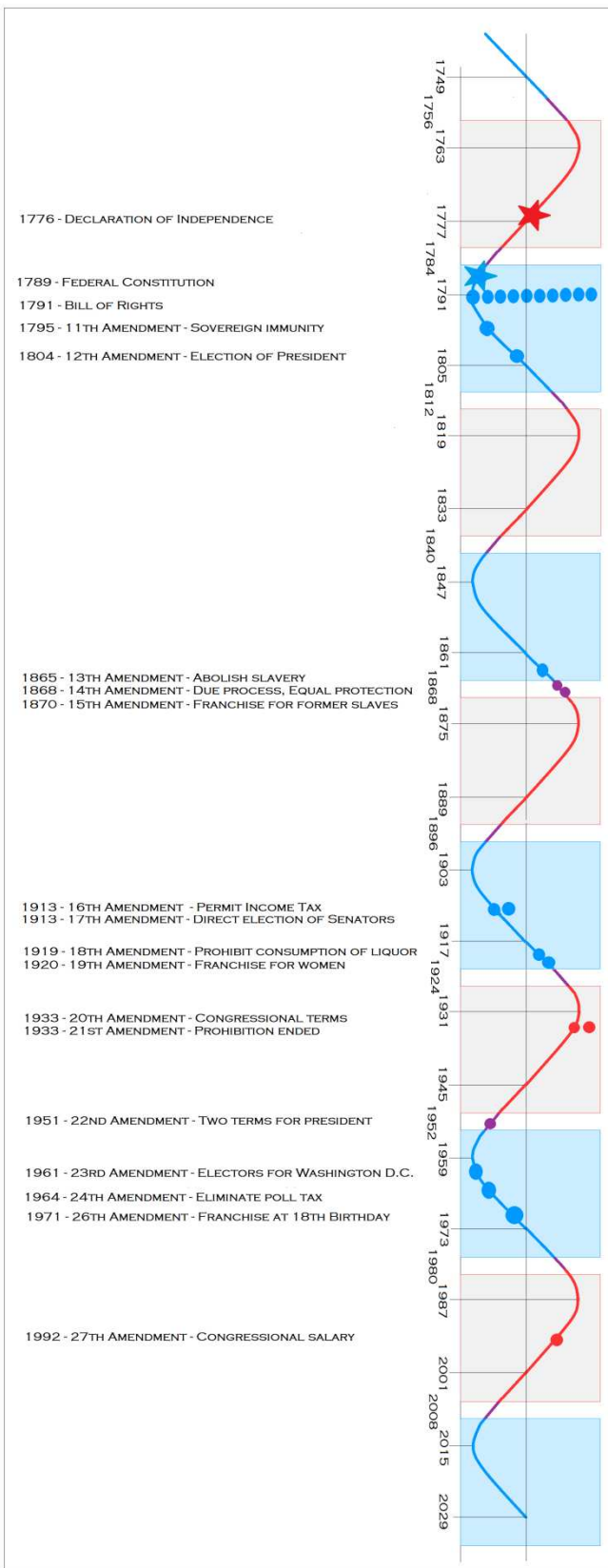
aggregate this model over the course of many years to find the growth of the United States stated as a natural "14-year octave" within real GNP data (pp. 63-91);

multiply this octave times two to find the 28-year natural rate of price fluctuation (pp. 92-112); and

multiply this octave times four to find the 56-year natural rate of political change (p. 92-112).

The final model (pp. 113-136) is the larger "fractal" of the model of trade which begins these essays, in essence demonstrating that the United States "trades" values over a period of time in much the same way the individual citizen trades goods and services for money on a personal basis.

Diagram 5-5.
56-Year Kondratiev Sine Wave with Amendments in Upswing and Downswing Periods

1776 - Declaration of Independence

1789 - Federal Constitution
1791 - Bill of Rights
1795 - 11th Amendment - Sovereign immunity
1804 - 12th Amendment - Election of President

1865 - 13th Amendment - Abolish slavery
1868 - 14th Amendment - Due process, Equal protection
1870 - 15th Amendment - Franchise for former slaves

1913 - 16th Amendment - Permit Income Tax
1913 - 17th Amendment - Direct election of Senators

1919 - 18th Amendment - Prohibit consumption of liquor
1920 - 19th Amendment - Franchise for women

1933 - 20th Amendment - Congressional terms
1933 - 21st Amendment - Prohibition ended

1951 - 22nd Amendment - Two terms for president

1961 - 23rd Amendment - Electors for Washington D.C.

1964 - 24th Amendment - Eliminate poll tax
1971 - 26th Amendment - Franchise at 18th Birthday

1992 - 27th Amendment - Congressional salary

1749
1756
1763
1777
1784
1791
1805
1812
1819
1833
1840
1847
1861
1868
1875
1889
1896
1903
1917
1924
1931
1945
1952
1959
1973
1980
1987
2001
2008
2015
2029

1.2 The Objective Determination of a "Crisis"

The first four essays of this work lay the intellectual foundation for an extended discussion in Essay Five of the "Political Economy Wave," pictured below. The x-axis values represent 20,454 days within a 56-year cycle, beginning with April 9, 1805, 1861, 1917, 1973 and, prospectively, 2029. Positive y-axis values are associated with thoughts in favor of political stability and negative y-axis values are associated with thoughts in favor of political change. After a careful review of all possible intersections of the waves which make up this model, the following points have been found to represent predictable dates of "crises," or fundamental change, in the understandings and behavior of citizens within the United States. These points are:

(A)   the beginning point,
(B)   the first peak, wherein positive y-values reach their greatest level,
(E)   the first trough,
(H)   the second peak,
(M)   the point wherein the wave passes from positive y-values to
               negative values,
(P)   the second trough, wherein negative y-values reach their lowest
               point and
(X)   the point wherein the wave passes from negative y-values to
               positive without the introduction of a new cosine wave.
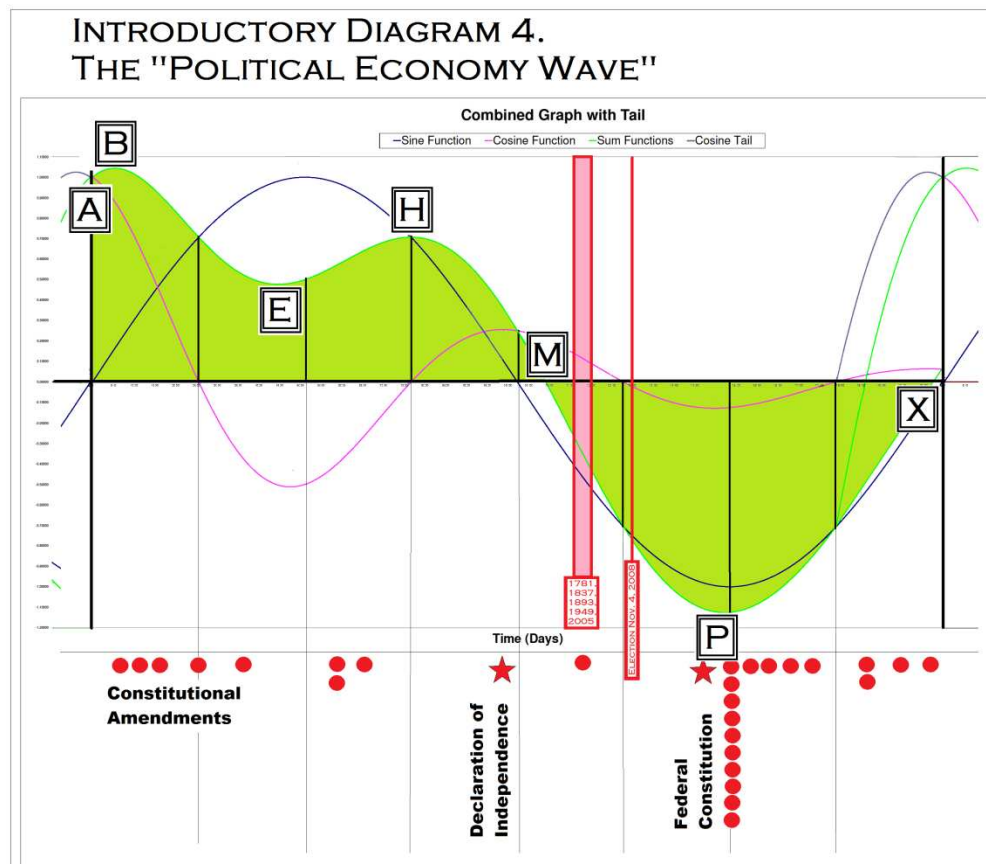
The pink rectangle above represents the year 2005, a date associated with previous financial political-economic crises coming in 56-year increments in 1781, 1837, 1893, 1949 and – prospectively – 2005. The vertical red line represents the election of November, 2008 at which point Senator Barack Obama was elected President of the United States in the midst of a global financial crisis.
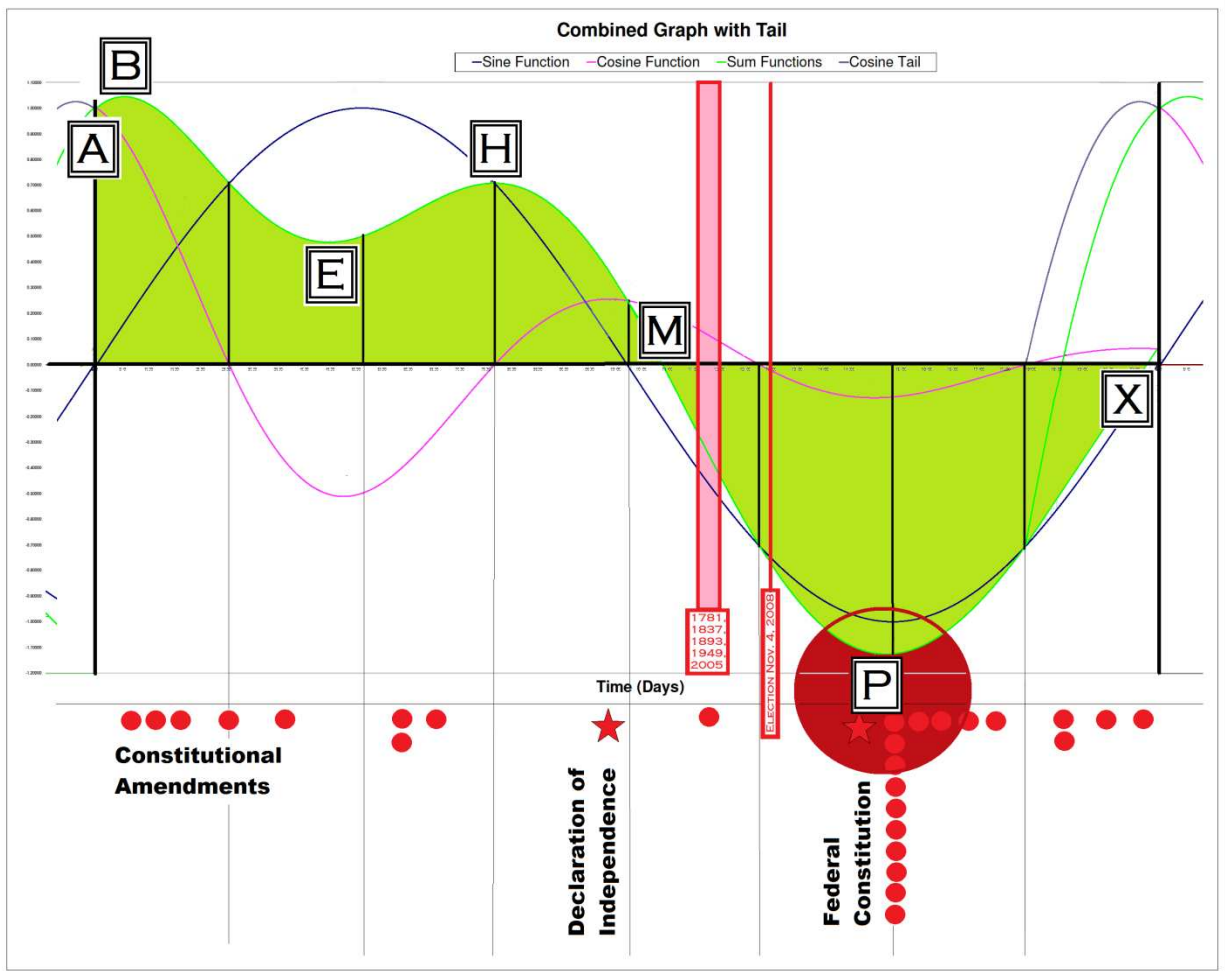
In this essay I present seven predictions which may be associated with the seven points given above – A, B, E, H, M, P, and X – vis-à-vis their association with the cover of TIME Magazine. These magazine covers represent a public statement of pressing events which is completely independent of this approach.

The magazine's interpretation of the event is not in question. Of interest to these essays are the dates associated with the event in question and the bold, unequivocal and "for profit" manner in which the event is stated, i.e. "on the cover." These covers are linked to this essay for ready reference.

Also provided are proposed correlations for much earlier dates at the same point of in the Political Economy Wave. Links are provided to internet articles pertinent to the crisis described. Predictions are listed in order of proximity to the date of the publication of these essays.

One of the most striking things about this approach is the interesting association of TIME Magazine covers – each of which conveys a serious, pressing and dramatic turn of events – with the dates provided. A review of the magazine covers linked to these essays, as well as those covers immediately preceding and subsequent to the dates given, may be sufficient to confirm the interest and potential usefulness of this approach.

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INTRODUCTORY DIAGRAM 4.
THE "POLITICAL ECONOMY WAVE"

Combined Graph with Tail
—Sine Function —Cosine Function —Sum Functions —Cosine Tail

Time (Days)

Constitutional Amendments

Declaration of Independence

Federal Constitution

1781, 1837, 1893, 1949, 2005

ELECTION Nov. 4, 2008

Point P.   The second trough.

This point will next be reached between **December 8 to 12, 2014.**

The most recent dates associated with this point are December 8 to 12, 1958.
    TIME National Affairs Articles:
    Rising racial tension in the South and the threat of nuclear war.
    http://www.time.com/time/covers/0,16641,19581208,00.html

Interpretation of the Political Economy Wave: Point P introduces Americans to
    their future, ultimately leading to the wholesale change to which it is
    directly related at Point A.

Important dates near December 8-12, 2014 at 56-year intervals are:

December 14, 1790: Alexander Hamilton proposes a National Bank, a perennial issue
since that time, made vastly more complicated by the Louisiana Purchase of 1803.
http://www.civil-liberties.com/cases/bank.html

December 6-7, 1846: The Battle of San Pasqual. American troops reach California per
annexation agreement ending Mexican-American War, leading to the California Gold Rush and
the strengthening of Yankee non-slave commerce throughout the North.
http://en.wikipedia.org/wiki/Battle_of_San_Pasqual

December 7, 1902: British and German ultimatum ignites the Venezuelan Crisis,
eventually leading President Roosevelt to the Roosevelt Corollary to the Monroe Doctrine.
American imperialism in Latin America is thus codified and leads to an ever more expansive
international involvement by the United States and ultimately entry into World War I.
http://en.wikipedia.org/wiki/Venezuela_Crisis_of_1902%E2%80%931903

Introductory Diagram 4.
The "Political Economy Wave"

Combined Graph with Tail

— Sine Function — Cosine Function — Sum Functions — Cosine Tail

B

A

H

E

M

1781,
1837,
1893,
1949,
2005

ELECTION Nov. 4, 2008

X

P

Time (Days)

Constitutional
Amendments

Declaration of
Independence

Federal
Constitution
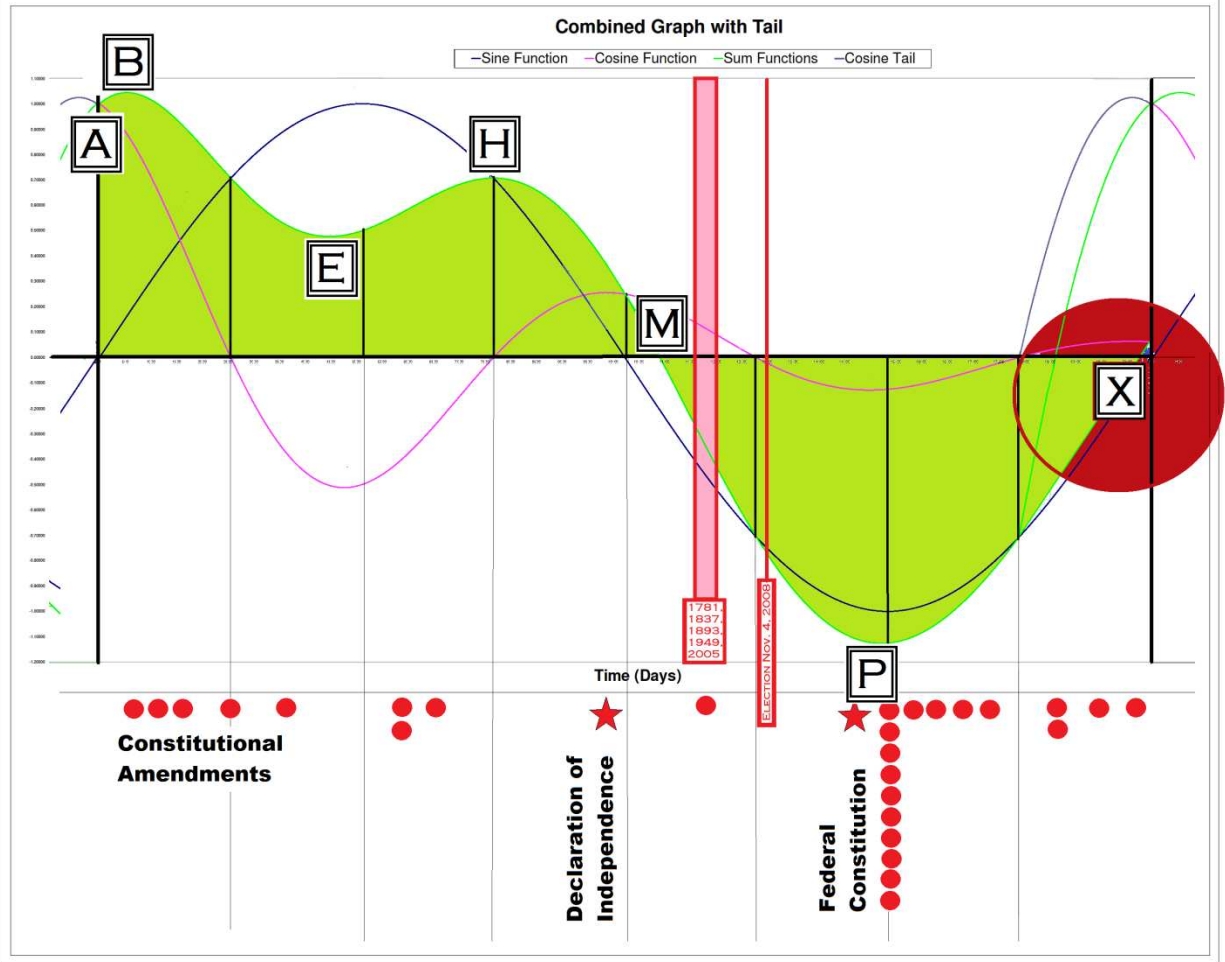
Point X. The point wherein the wave passes from negative y-values to positive without the introduction of a new cosine wave.

This point will next be reached on **September 13, 2028.**

The most recent date associated with this point is September 13, 1972.
TIME Cover: Massacre of Israeli athletes in Munich.
http://www.time.com/time/covers/0,16641,19720918,00.html

Interpretation of the Political Economy Wave: Point X anticipates the tremendous change which arrives at Point A.

Important dates near September 13, 2028 at 56-year intervals are:

September 13, 1804: Lewis and Clark in Brule County, South Dakota, travelling west, yet not reaching the terminus of the available settlements;
http://www.lewisandclarktrail.com/section2/sdcities/Chamberlain/history1.htm

September 13, 1860: Senator John Crittenden of Kentucky, a border state, declares that he would stand for the union even if Lincoln won. His Crittenden Compromise of December 18, 1860 was unsuccessful in averting civil war. He returned home and worked to keep Kentucky in the union. Two of his sons would become generals on opposing sides of the war.
 http://www.civilwar-online.com/2010/09/september-13-1860-senator-john-j.html
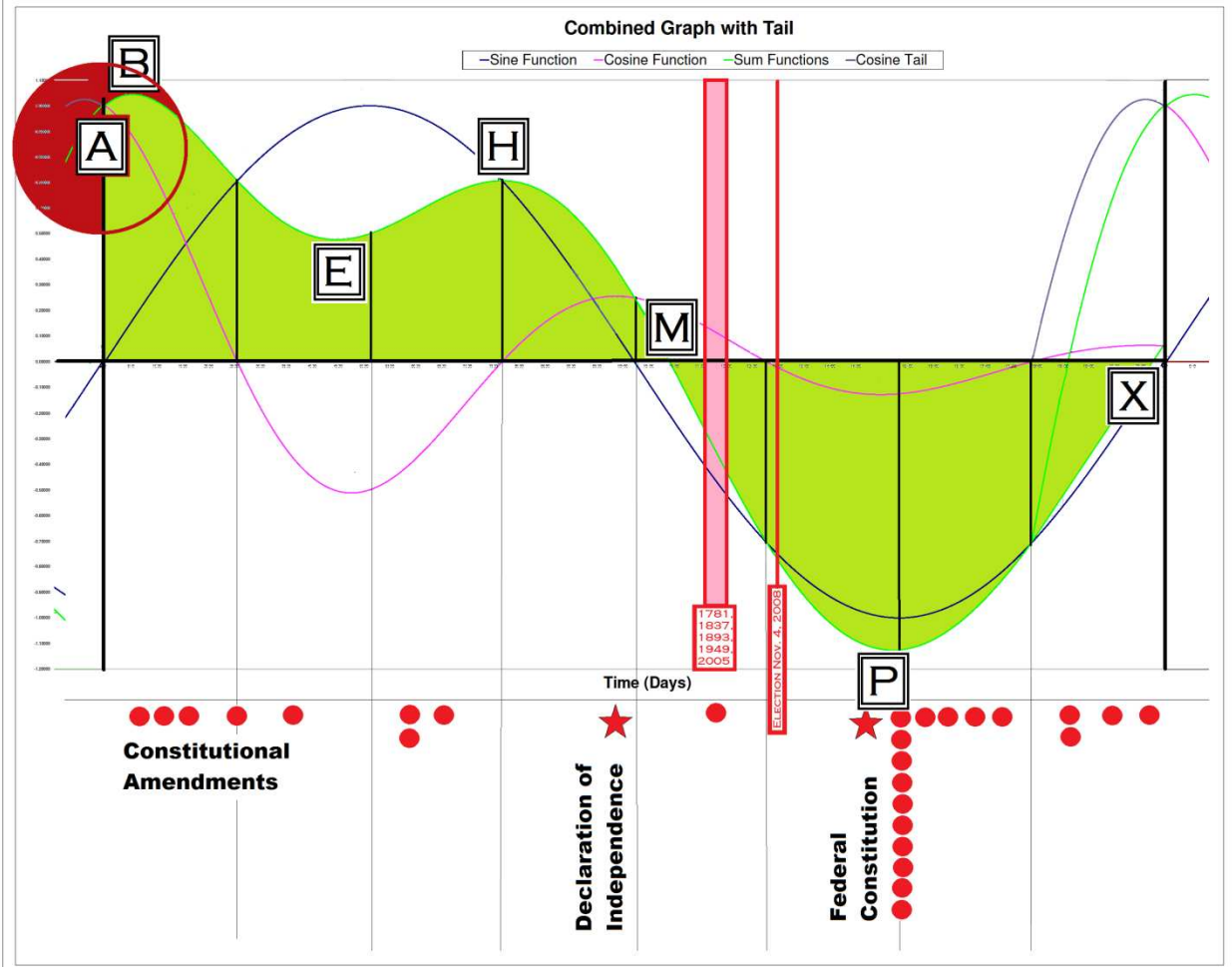http://sunsite.utk.edu/civil-war/critten.html

September 15, 1916: First tank used in World War I, a new military technology which American troops would face upon their entry into France and the European Theatre.
http://www.eyewitnesstohistory.com/tank.htm

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INTRODUCTORY DIAGRAM 4.
THE "POLITICAL ECONOMY WAVE"

Combined Graph with Tail

—Sine Function —Cosine Function —Sum Functions —Cosine Tail

A B H E M X P

1781, 1837, 1893, 1949, 2005

ELECTION NOV. 4, 2008

Time (Days)

Constitutional Amendments

Declaration of Independence

Federal Constitution

Point A.   The beginning point.

                    This point will next be reached on **April 9, 2029.**

                    The most recent date associated with this point is **April 9, 1973.**
                           TIME Cover: High inflation rates sweep the nation.
                           http://www.time.com/time/covers/0,16641,19730409,00.html

                    Interpretation of the Political Economy Wave: Point A ends all previous
                           associations with previous historic development and begins something
                           entirely new, hitherto untried and unknown.

          Important dates near April 9, 2029 at 56-year intervals are:

          April 6, 1805: Lewis and Clark depart Fort Mandan, North Dakota: "We were now about to penetrate a country at least 2000 miles in width upon which the foot of civilized man had never trodden." http://www.infoplease.com/t/hist/lewis-clark-journal/day329.html

          April 12-14, 1861: South Carolina fires on Fort Sumter, beginning the American Civil War. http://en.wikipedia.org/wiki/Battle_of_Fort_Sumter

          April 6, 1917: Entry of the United States into World War I. http://en.wikipedia.org/wiki/American_entry_into_World_War_I

        Of the 71 Time Magazine covers between points A (April 9, 1973) and Point B (September 16, 1974) 37 covers – slightly over half – specifically refer to events involving the Watergate scandal. Included in this sequence of events were the resignation of Vice President Agnew on October 10, 1973, the appointment of Gerald Ford as Vice President on December 6, 1973, the resignation of President Nixon and the beginning of the presidency of Gerald Ford on August 9, 1974.

INTRODUCTORY DIAGRAM 4.
THE "POLITICAL ECONOMY WAVE"

Combined Graph with Tail

—Sine Function   —Cosine Function   —Sum Functions   —Cosine Tail

1781, 1837, 1893, 1949, 2005

ELECTION Nov 4, 2008

Time (Days)

Constitutional Amendments

Declaration of Independence

Federal Constitution
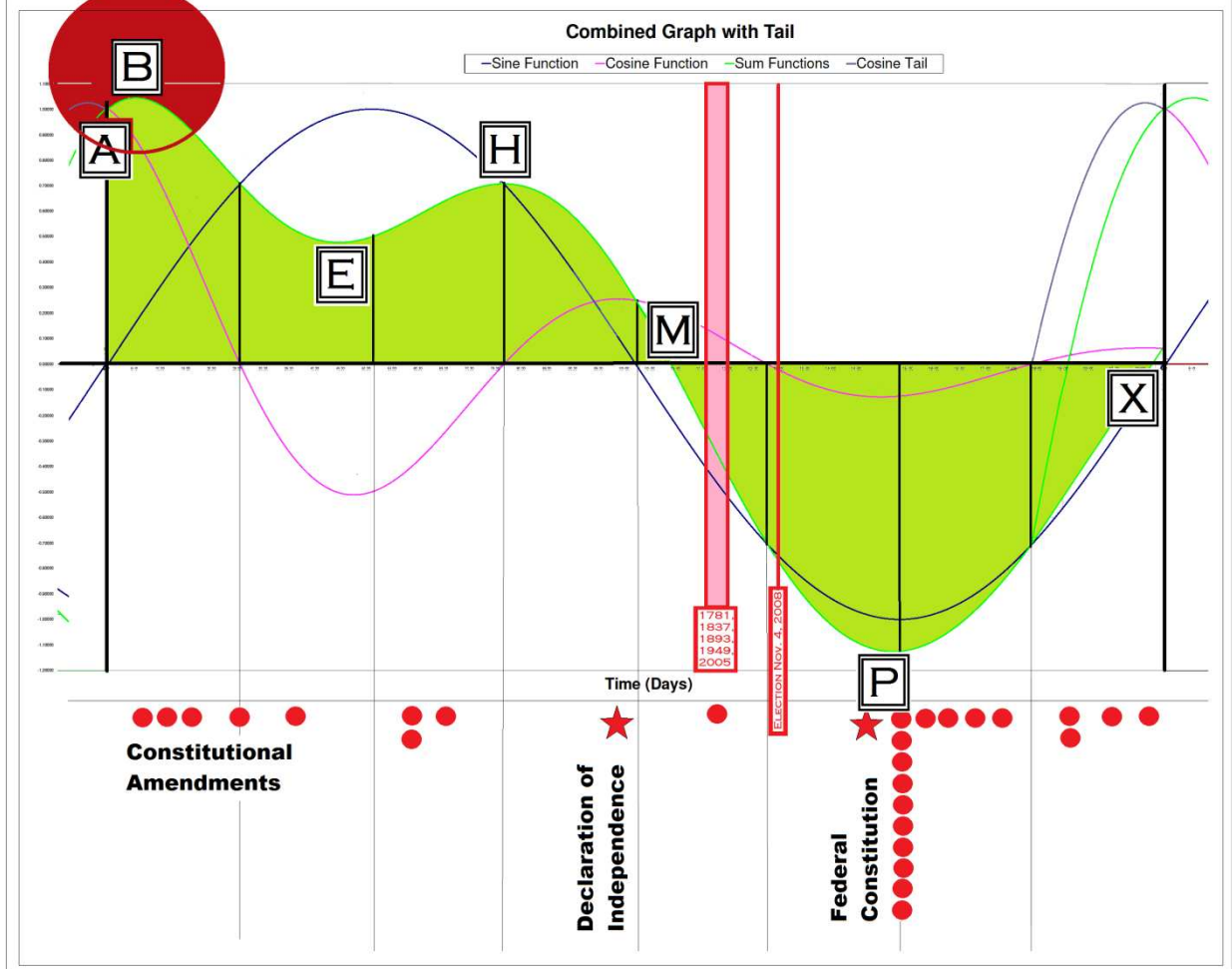
Point B. The first peak, wherein the y-values reach their greatest level.

This point will next be reached between **September 16-October 1, 2030.**

The most recent dates associated with this point are **Sept. 16 – Oct. 1, 1974.**
TIME Cover: President Ford pardons ex-President Nixon for his role in the Watergate scandal.
http://www.time.com/time/covers/0,16641,19740916,00.html
http://www.time.com/time/covers/0,16641,19740923,00.html
http://www.time.com/time/covers/0,16641,19740930,00.html
http://www.time.com/time/covers/0,16641,19741007,00.html

Interpretation of the Political Economy Wave: Point B resolves the intense conflict / difficulty running between Points A and B.

Important dates near September 16-October 1, 2030 at 56-year intervals are:

September 23, 1806: Lewis and Clark complete their journey, arriving in St. Louis.
http://www.lewisandclarktrail.com/section1/mocities/St.Charles/1806history1.htm

September 17, 1862: Battle of Antietam, Union victory in "the bloodiest single day in American military history" giving Lincoln the military success he desired to prelude the Emancipation Proclamation and forestall British and French recognition of the Confederacy.
http://en.wikipedia.org/wiki/Battle_of_Antietam

August 18-September 16, 1918: The last stage of the Second Battle of the Marne, the Oise-Aisne Offensive, first use of independent American forces in Europe at St. Mihiel September 12-16, 1918, with the Americans freeing the St. Mihiel salient on September 16, 1918 and "the beginning of the end of the Great War" with an armistice declared 100 days later.
http://en.wikipedia.org/wiki/United_States_campaigns_in_World_War_I

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INTRODUCTORY DIAGRAM 4.
THE "POLITICAL ECONOMY WAVE"

Combined Graph with Tail

Sine Function — Cosine Function — Sum Functions — Cosine Tail

Time (Days)

Constitutional Amendments

Declaration of Independence

Federal Constitution

1781, 1837, 1893, 1949, 2005

Election Nov. 4, 2008
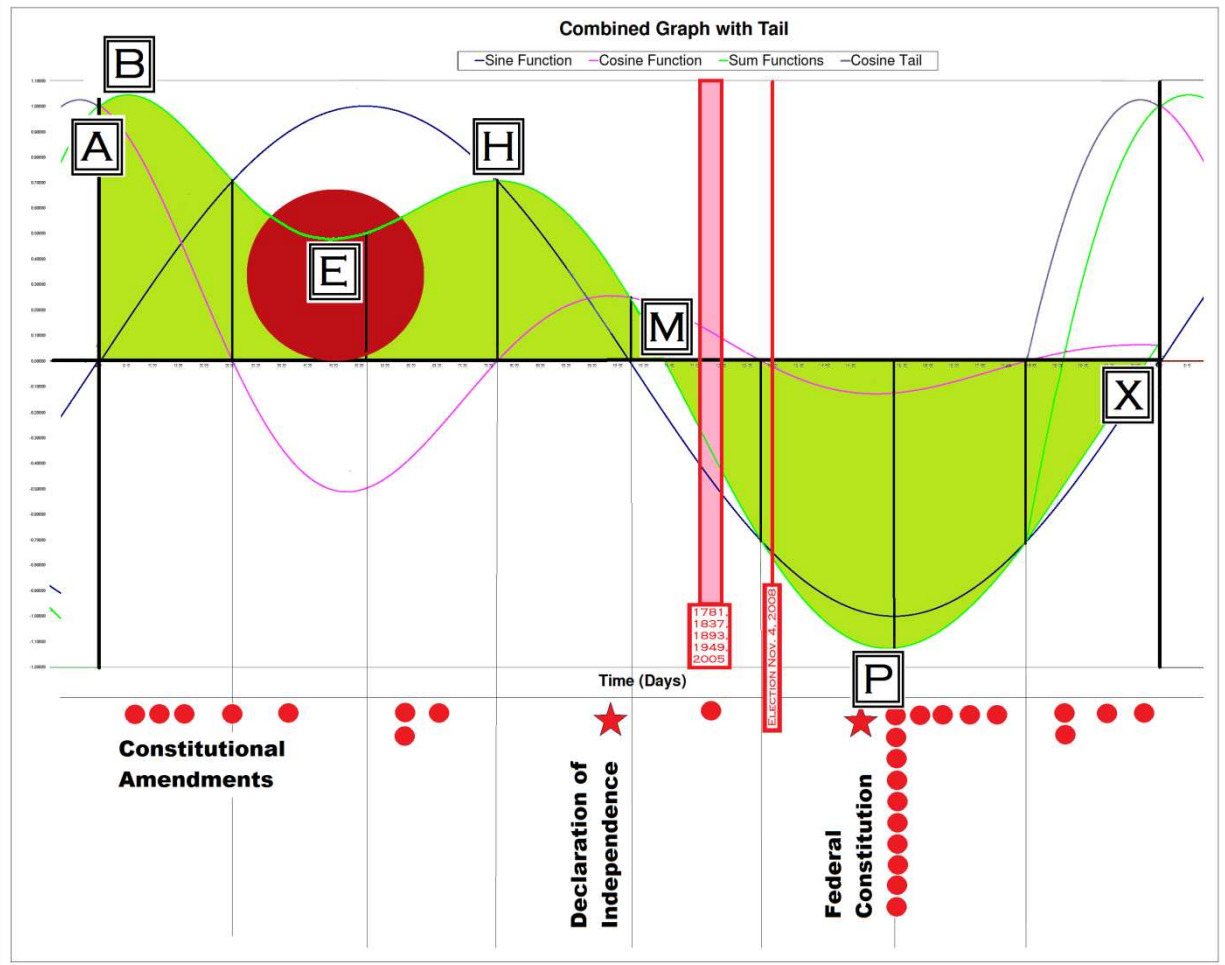
Point E.　　　The first trough.
　　　　　　　This point will next be reached between **June 28 – July 20, 2041.**
　　　　　　　The most recent dates associated with this point are June 28 – July 20, 1985.

　　　　　　　TIME Cover: Hijacking / Terrorism of TWA Flight 847 and the return of 151 of
　　　　　　　　　152 hostages.
　　　　　　http://www.time.com/time/covers/0,16641,19850624,00.html
　　　　　　http://www.time.com/time/covers/0,16641,19850701,00.html
　　　　　　http://www.time.com/time/covers/0,16641,19850708,00.html
　　　　　　http://www.time.com/time/covers/0,16641,19850715,00.html

　　　　　　　Interpretation of the Political Economy Wave: Point E resolves long-standing
　　　　　　　　　prior difficulties with success.

　　　Important dates near June 28 – July 20, 2041 at 56-year intervals are:

　　　July 4, 1817: construction on the Erie canal begins, resolves difficulty of transportation across long distances, sets off a "canal mania" and extensive investment in canals in the United State. http://en.wikipedia.org/wiki/Erie_Canal

　　　July 8, 1873: the Modoc War, last of the Indian Wars in California and Oregon, resolves for California ongoing Indian conflicts ending with convictions and the death sentences of the Indians involved on July 8, 1873. http://en.wikipedia.org/wiki/Modoc_War

　　　July 24, 1929: the Kellogg-Briand Pact comes into effect, whereby signatory states promised not to use war to　　resolve "disputes or conflicts of whatever nature or of whatever origin they may be, which may arise among them." Parties failing to abide by this promise "should be denied the benefits furnished by this treaty." This treaty resolves the legality of war for territorial aggrandizement, a law still binding law in the United States. http://en.wikipedia.org/wiki/Kellogg%E2%80%93Briand_Pact

Introductory Diagram 4.
The "Political Economy Wave"

Combined Graph with Tail

—Sine Function   —Cosine Function   —Sum Functions   —Cosine Tail

A B H E M X P

1781, 1837, 1893, 1949, 2005

ELECTION Nov. 4, 2008

Time (Days)

Constitutional Amendments

Declaration of Independence

Federal Constitution
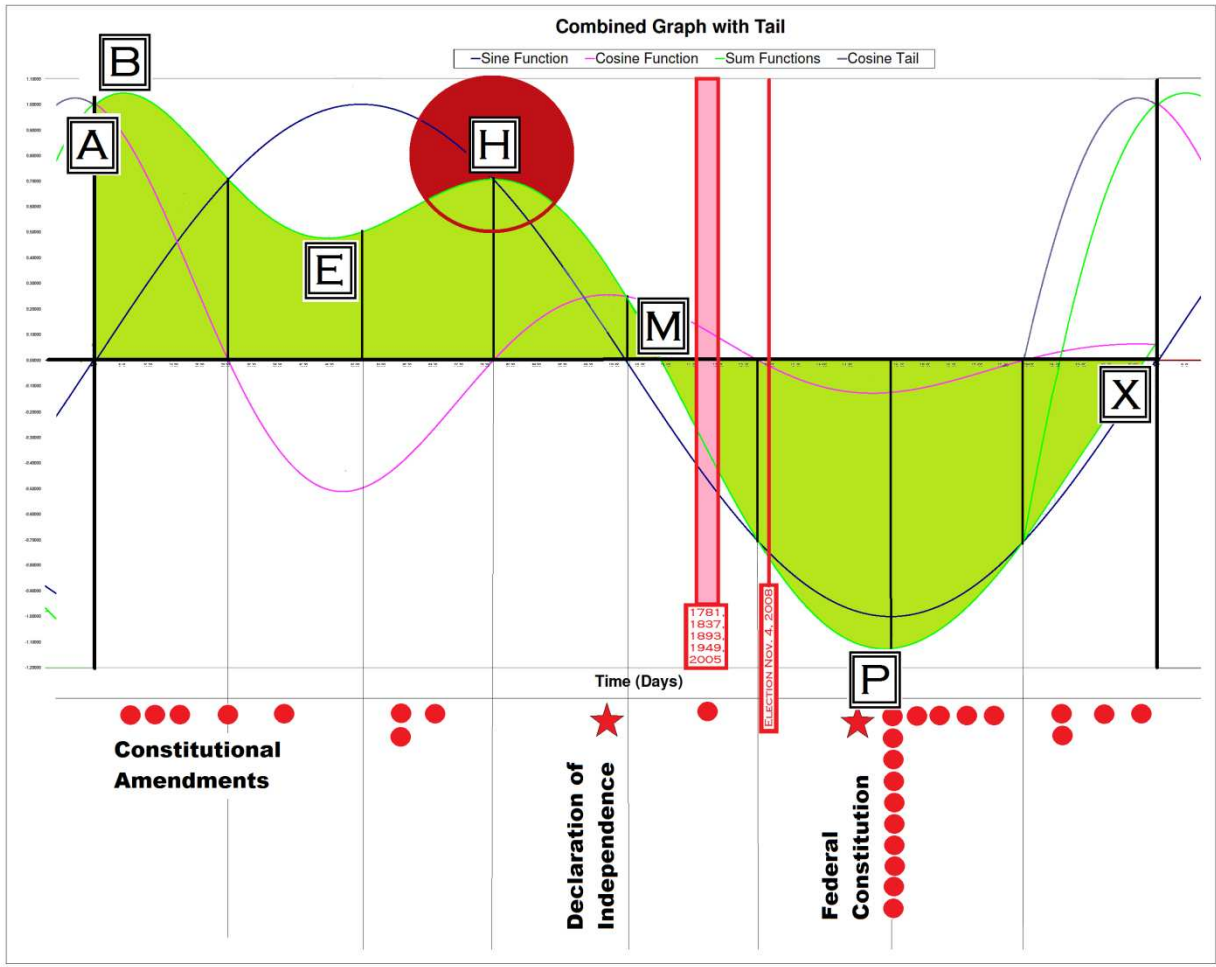
Point H.   The second peak.
                This point will next be reached between **April 4 – April 14, 2050.**
                The most recent dates associated with this point are April 4 – April 14, 1994.

                TIME Cover: The Whitewater Scandal, Stock Market Meltdown and the Rise of
                        Derivatives.
                http://www.time.com/time/covers/0,16641,19940404,00.html
                http://www.time.com/time/covers/0,16641,19940411,00.html

                Interpretation of the Political Economy Wave: Point H raises difficult
                        international issues left unresolved, presaging troubles in the near future.

        Important dates near April 4 – April 14 2050 at 56-year intervals are:

        April 12, 1770: in light of the Boston Massacre of the previous month (March 5),
Parliament repeals all duties imposed by the earlier Townshend Act except that on tea (April 12),
thereby permitting further colonial dissent from English policies;
http://en.wikipedia.org/wiki/Townshend_Acts

        April 1, 1826:   Samuel Morey, an American inventor, patents the first internal
combustion engine, a central part of the modern economy.
http://kinnexions.com/smlsource/samuel.htm

        April 13, 1882: Anti-Semitic League formed in Prussia, a society dedicated to the
expulsion of all Jews in Europe, raises the question of its possible success and under what terms;
http://quod.lib.umich.edu/m/moajrnl/bac8387.0033.193/135:17?rgn=full+text;view=image

        April 10, 1938: Plebiscite in Austria approves Anschluss by Germany by 99%, leading to
the expansion of Nazi Germany on a wave of public enthusiasm.
http://www.otr.com/Linz.html

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INTRODUCTORY DIAGRAM 4.
THE "POLITICAL ECONOMY WAVE"

Combined Graph with Tail

—Sine Function   —Cosine Function   —Sum Functions   —Cosine Tail

Time (Days)

1781, 1837, 1893, 1949, 2005

ELECTION Nov. 4, 2008

Constitutional Amendments

Declaration of Independence

Federal Constitution
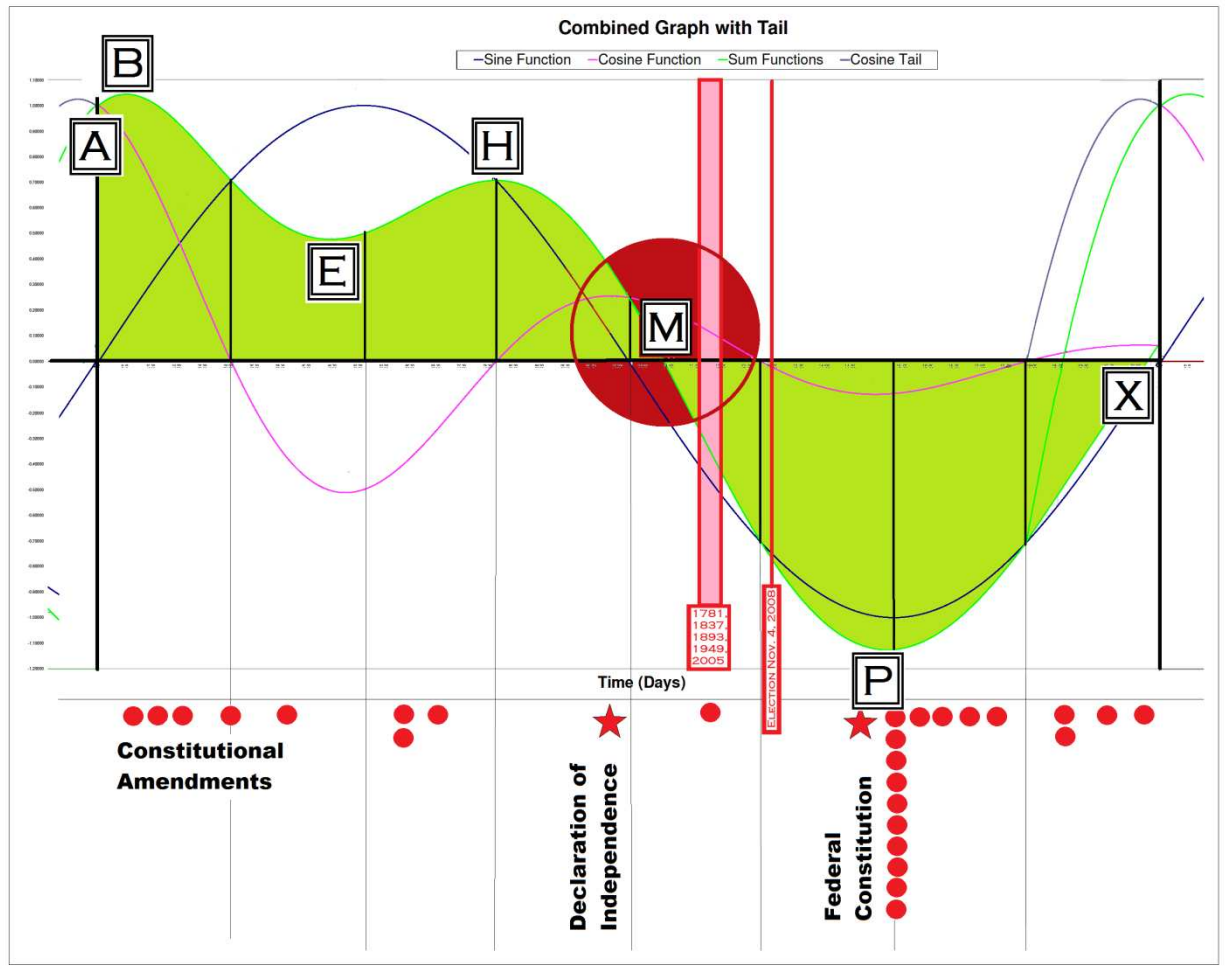
Point M.   The point wherein the wave passes from positive y-values to negative values. This point will next be reached on **February 21, 2059.** The most recent date associated with this point is February 21, 2003.

TIME Cover: President G. W. Bush's effort to invade Iraq.
http://www.time.com/time/covers/0,16641,20030224,00.html

Interpretation of the Political Economy Wave: Point M enormously and controversially expands the idea of American democracy and its applicability to new groups of people.

Important dates near February 22, 2059 at 56-year intervals are:

February 25, 1779:   Gen. G. W. Clark captures the British fort at Vincennes, Indiana, thereby doubling the colonial geographic area of the United States.
http://en.wikipedia.org/wiki/Illinois_campaign;

February, 1835: "Democracy in American" Volume I by Alexis de Tocqueville is published, a work still used to analyze American character and civic identity in the United States.
http://en.wikipedia.org/wiki/Democracy_in_America;
http://www.loc.gov/loc/lcib/9712/kammen.html

February 22-25, 1891:   First meeting of National Council of Women of the United States held in Washington, D. C. leading to the 19th (prohibition) and 20th (suffrage) Amendments.
.http://books.google.com/books/about/Transactions_of_the_National_Council_of.html?id=bpU0xGnVETsC

February 17, 1947:   The Voice of America begins broadcasts into Eastern Europe and the USSR.
http://www.history.com/this-day-in-history/voice-of-america-begins-broadcasts-to-russia

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Conclusion

This model is derived entirely from an analysis of published data. It is intended as an empirical statement of the manner in which the political economy of the United States evolves over time.

The methodology presented in these essays has not been used previously in studies of economics. The economy of the United States is the sole topic herein inasmuch as:

(1)   the United States has not suffered from the invasions and border reductions which have typified virtually all other countries available for consideration, thereby permitting an equivalence between the data generated and the subject studied,

(2)   the economic data pertaining to the United States is long-standing, precise, self-consistent, authoritative and easily available and

(3)   the combination of a single political sovereignty with the right to tax, a national legal jurisdiction of arbitrary finality and a monetary / fiscal policy orchestrated by a single government have been central characteristics of the economic history of the United States from at least 1868.

In sum, this model singles out certain dates as carrying the weight of historic change. Not unlike a vibrating string wherein the tension of the string itself actually defines its own points of maximum stress, so do these conjoined waves appear to create moments of vital change in the body politic of the United States.
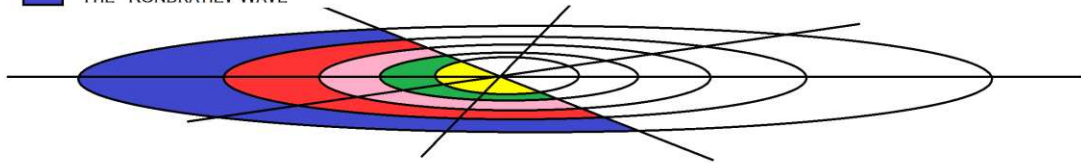
The purpose of this model is to demonstrate the periodicity of American economic and social history, and to provide a basis for its understanding in scientific terms.

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INTRODUCTION: WHAT IS A "CRISIS"?

As used in these essays, the term "crisis" refers to a mathematically determined and yet fundamental date of change which forever alters all subsequent understanding of events. I propose to predict crucial dates of social and economic change using a mathematic model of nested waves repeated at five separate levels of society and as derived entirely from data on annual real GNP, prices and employment of the United States.

INTRODUCTION. DIAGRAM 3.
BASIC PLAN.

1. [yellow] MICRO-ECONOMIC CHOICE
X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. [green] MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
OKUN'S LAW STATES A π : 1 RATIO AS TO
HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. [pink] REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. [red] DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. [blue] SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
THE "KONDRATIEV WAVE"

The model presented here is of five concentric unit circles which collectively provide patterns of economic and social development in the United States generated by trigonometric functions.[3] In this model each "larger" radius states an aggregate of the preceding and smaller unit circles.[4] Using this model I propose that it is possible to predict exactly when and what sort of crises are likely to occur within the economic and social structure of the United States for specific dates far distant in the future.[5]

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[3]   Trigonometric ratios are derived from the "unit circle," a mathematic device whereby the center point of a circle is placed at the origin (the "x y intercept") of a Cartesian coordinate graph; an arbitrary value of "1" is given to the radius of a circle commensurate with the value "1" on the graph; and the measurement of the circumference of the circle of 2π is then charted on the graph. An infinite number of right triangles are circumscribed within this circle, taking the radius of the circle as a hypotenuse of a right triangle; and the placement of the right angle along the x-axis always moving in accord with a y-axis variable as located by the circumference of the circle. The Pythagorean Theorem states that the square of one side of a right triangle (the x value) plus the square of the second side (the y value) shall equal the square of the hypotenuse (the radius). Calculations from this arrangement are made systematic by the fact that the "radius / hypotenuse" of all triangles created is "1" and that the square of "1" is "1." The study of these angles and the proportions of these sides is known as "trigonometry."

[4]   Although the radius of the "unit circle" of trigonometry never varies from the ratio of $1 : \pi$ at any point, the word "larger" here is meant simply as a demonstrative aid. From a strictly pedagogical point of view, this model proposes that the "larger" logical relationships within society are an aggregate of congruent "smaller" dimensions within the same society.

[5]   The "clock-wise" direction of movement around the unit circle and the "9:00 o'clock" place of beginning the analysis as used in these essays are opposite that taken in most trigonometry textbooks.

1.1 A brief description of these essays

1.   The first essay introduces the "chooser – available choice" model. The "chooser – available choice" model is the initial "fractal" at the core of the entire system. The first unit circle (Introductory Diagram 3, in yellow) uses dichotomies of economic "actions" ("trading" vs. "keeping," along the x-axis) and economic "thoughts" (y-axis) to state the essential elements underlying the simplest economic transaction. The radius of the unit circle represents the *choice* of the consumer as faced with ½ the circumference of the circle, the *choices available*. This "chooser – available choice" model is the underlying basis for the remaining "unit circles."

DIAGRAM 1-18
NEW CIRCLE ON TRADE.
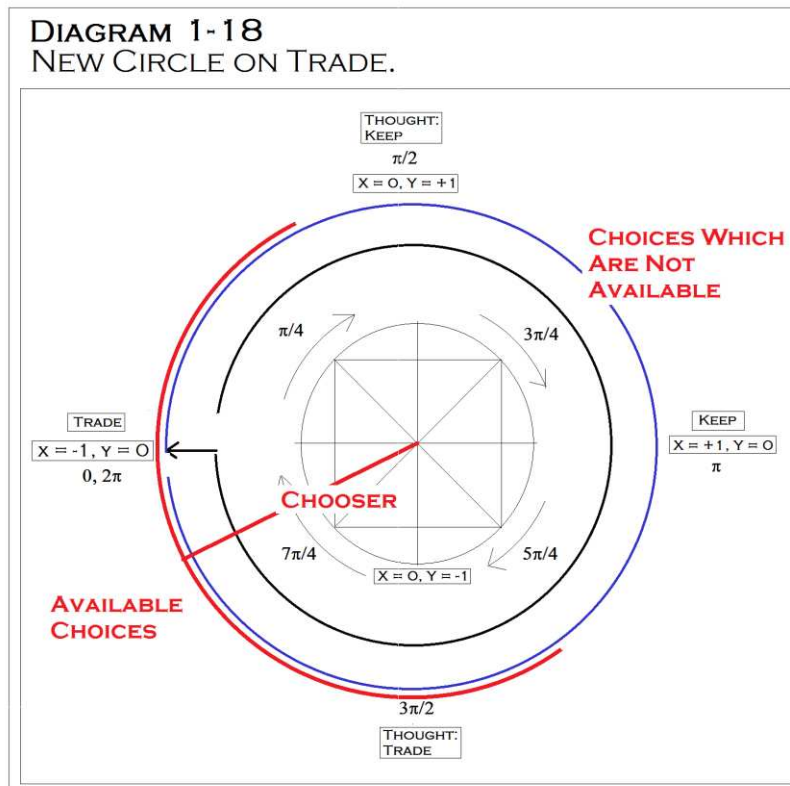
This approach does not alter the trigonometric identities considered in the slightest and provides an approach to the measurement of time which is consistent with the sense of the hands of a clock.
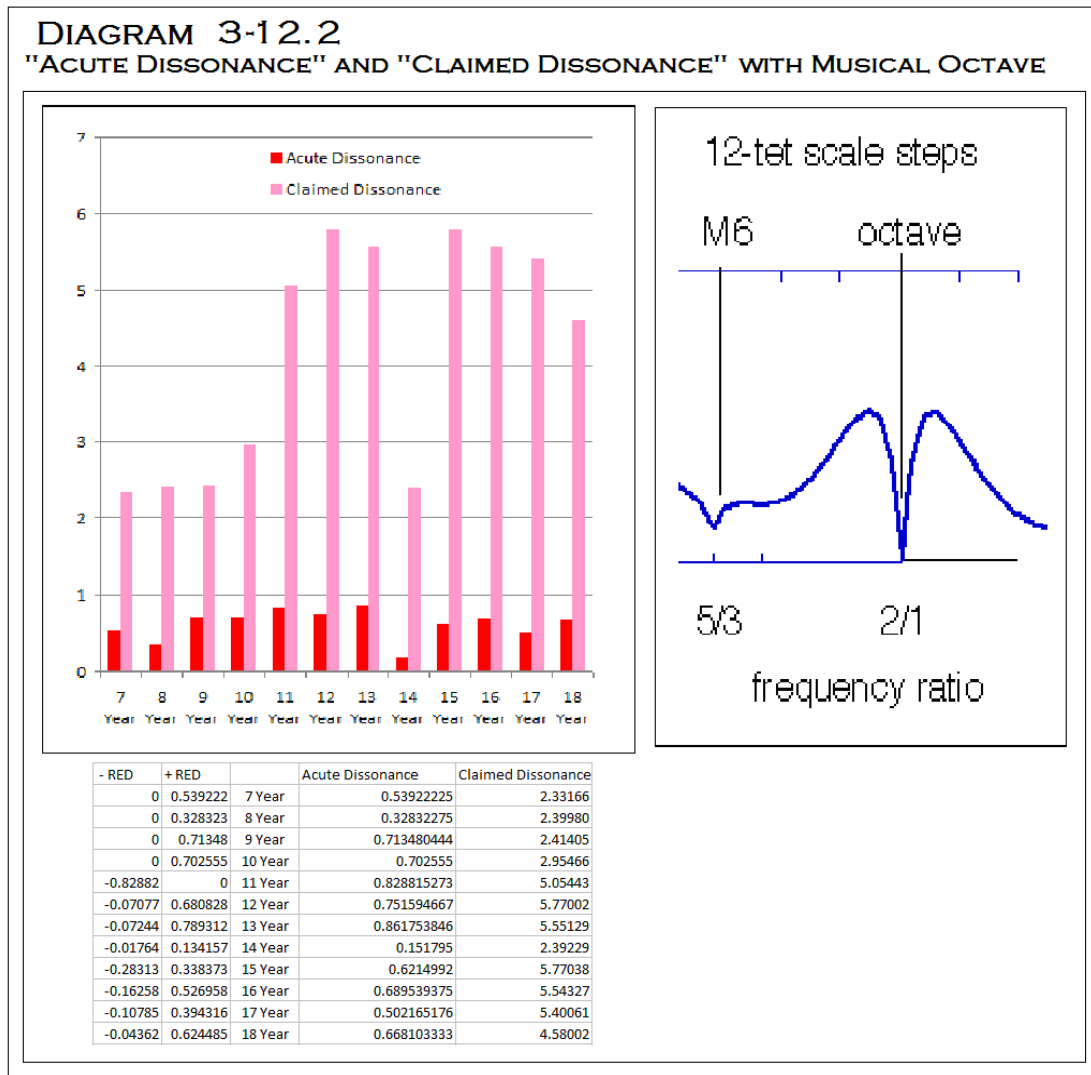
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2.   The aggregate of all economic choices over the course of a single year is stated by the annual Gross National Product of the United States. The second essay aggregates the "chooser – available choice" model over the course of a year to derive Okun's Law, a fundamental proportion of economics. (Introductory Diagram 3, in green)

      The second essay presents Okun's Law as the function of a ring torus, a three dimensional figure resembling an inner tube wherein a smaller circle (with radius "r" for "Minor Radius" representing the choices made by consumers) is swept around the axis of a larger circle (with radius "R" for "Major Radius" representing the annual rate of employment). A $1 : \pi$ relationship between the change in employment and change in annual GNP results, a figure strikingly consistent with the data available as to the economy of the United States.

DIAGRAM 2-8.
UNITED STATES ANNUAL REAL GNP

FARMER BROWN
FARMER FREDERICKS
FARMER SMITH
FARMER ARMSTRONG

1973

MONETARY PRICE PAID FOR GOOD OR SERVICE PURCHASED

GOOD OR SERVICE INCLUDED IN ANNUAL REAL GNP
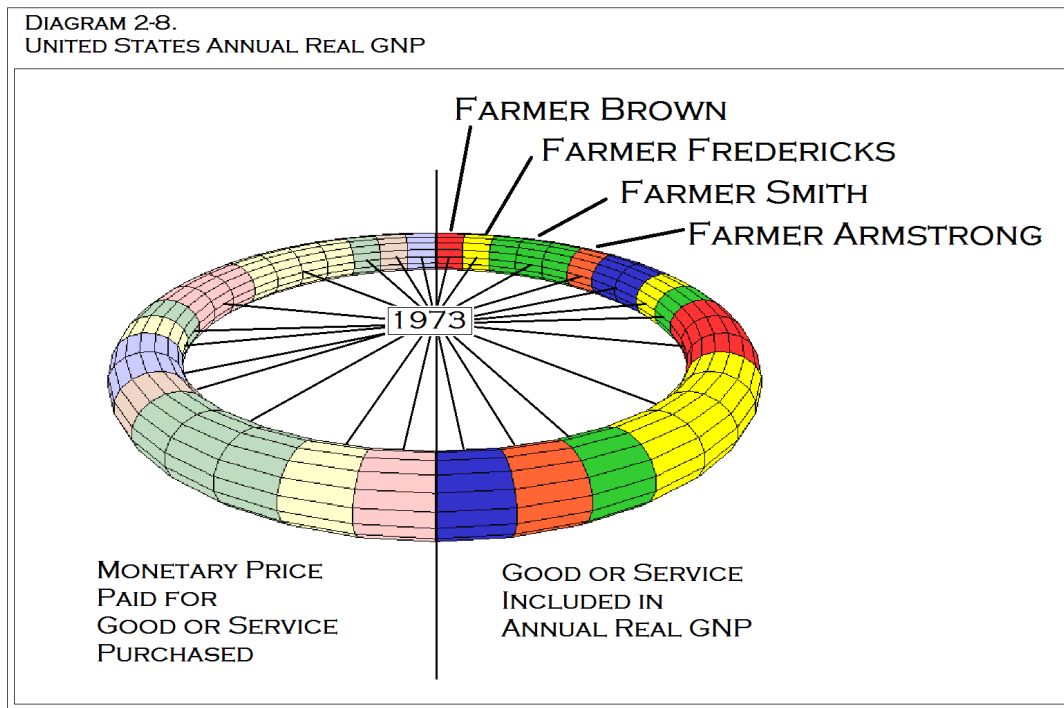
3.	The third essay aggregates these annual figures for real GNP through the use of the "GNP ratio," i.e. the quotient of one year's real GNP as divided by the real GNP of an earlier year. Using two different but compatible techniques we discover two interesting patterns presented by these ratios at different "spreads" of years, i.e. the time interval separating the numerator and denominator of the ratio itself.

The first of these is the "14-year octave." (Introductory Diagram 3, in pink) This technique provides an unmistakable sense that a form of musical harmony governs the rate of production in the United States.

DIAGRAM 3-12.2
"ACUTE DISSONANCE" AND "CLAIMED DISSONANCE" WITH MUSICAL OCTAVE

- RED	+ RED		Acute Dissonance	Claimed Dissonance
0	0.539222	7 Year	0.53922225	2.33166
0	0.328323	8 Year	0.32832275	2.39980
0	0.71348	9 Year	0.713480444	2.41405
0	0.702555	10 Year	0.702555	2.95466
-0.82882	0	11 Year	0.828815273	5.05443
-0.07077	0.680828	12 Year	0.751594667	5.77002
-0.07244	0.789312	13 Year	0.861753846	5.55129
-0.01764	0.134157	14 Year	0.151795	2.39229
-0.28313	0.338373	15 Year	0.6214992	5.77038
-0.16258	0.526958	16 Year	0.689539375	5.54327
-0.10785	0.394316	17 Year	0.502165176	5.40061
-0.04362	0.624485	18 Year	0.668103333	4.58002

The second pattern of obvious interest is a pentagonal figure associated with the 11-year spread and an unusual pattern of dissonance. These two discoveries are described in more detail in the essay itself.

4.   The fourth essay aggregates the 14-year octave in two larger octaves building upon it, i.e. the 28-year and 56-year octaves. These are presented as the largest of the unit circles (Introductory Diagram 3, in red and blue).

The fourth unit circle (in red) describes a damping cosine wave of prices over periods of 28-years, twice that of the 14-year octave.

The fifth unit circle (in blue) describes a 56-year sine wave of socio-political change, the "Kondratiev Wave," at twice the length of the price wave.

The fourth essay proposes that these octaves work together to create a relationship between the economy of the United States and the Golden Mean, an ancient and important mathematic ratio of 1 : 1.6180… (given as the symbol φ, Albers & Albers, 2011) A 14-year period of economic development commensurate with the Golden Mean requires a steady-state rate of growth of exactly 3.4969 percent per year, a rate which matches quite well the available data.   In this way the economic past is connected to the economic present as well as the economic future.

DIAGRAM 4-7.   THE "GNP SPIRAL"

Left table:

	Date	Date	Date	Date	Date	Date
14	1762	1818	1874	1930	1986	
13	1761	1817	1873	1929	1985	
12	1760	1816	1872	1928	1984	
11	1769	1815	1871	1927	1983	
10	1768	1814	1870	1926	1982	
9	1767	1813	1869	1925	1981	
8	1766	1812	1868	1924	1980	2036
7	1765	1811	1867	1923	1979	2035
6	1764	1810	1866	1922	1978	2034
5	1763	1809	1865	1921	1977	2033
4	1762	1808	1864	1920	1976	2032
3	1761	1807	1863	1919	1975	2031
2	1760	1806	1862	1918	1974	2030
1	1759	1805	1861	1917	1973	2029
56		1804	1860	1916	1972	2028
55		1803	1859	1915	1971	2027
54		1802	1858	1914	1970	2026
53		1801	1857	1913	1969	2025
52		1800	1856	1912	1968	2024
51		1799	1855	1911	1967	2023
50		1798	1854	1910	1966	2022
49		1797	1853	1909	1965	2021
48		1796	1852	1908	1964	2020
47		1795	1851	1907	1963	2019
46		1794	1850	1906	1962	2018
45		1793	1849	1905	1961	2017
44		1792	1848	1904	1960	2016
43		1791	1847	1903	1959	2015

Right table:

	Date	Date	Date	Date	Date
15	1763	1819	1875	1931	1987
16	1764	1820	1876	1932	1988
17	1765	1821	1877	1933	1989
18	1766	1822	1878	1934	1990
19	1767	1823	1879	1935	1991
20	1768	1824	1880	1936	1992
21	1769	1825	1881	1937	1993
22	1770	1826	1882	1938	1994
23	1771	1827	1883	1939	1995
24	1772	1828	1884	1940	1996
25	1773	1829	1885	1941	1997
26	1774	1830	1886	1942	1998
27	1775	1831	1887	1943	1999
28	1776	1832	1888	1944	2000
29	1777	1833	1889	1945	2001
30	1778	1834	1890	1946	2002
31	1779	1835	1891	1947	2003
32	1780	1836	1892	1948	2004
33	1781	1837	1893	1949	2005
34	1782	1838	1894	1950	2006
35	1783	1839	1895	1951	2007
36	1784	1840	1896	1952	2008
37	1785	1841	1897	1953	2009
38	1786	1842	1898	1954	2010
39	1787	1843	1899	1955	2011
40	1788	1844	1900	1956	2012
41	1789	1845	1901	1957	2013
42	1790	1846	1902	1958	2014

An appreciation of the role played by both π (essay two) and φ (essay four) within the economic statistics of the United States is essential to an understanding of economics and social dynamics.

5.   The fifth essay proposes that the "Chooser – Available Choice" model, given for the decisions of a single person, is copied in the economy of the United States as a larger fractal of historic development.
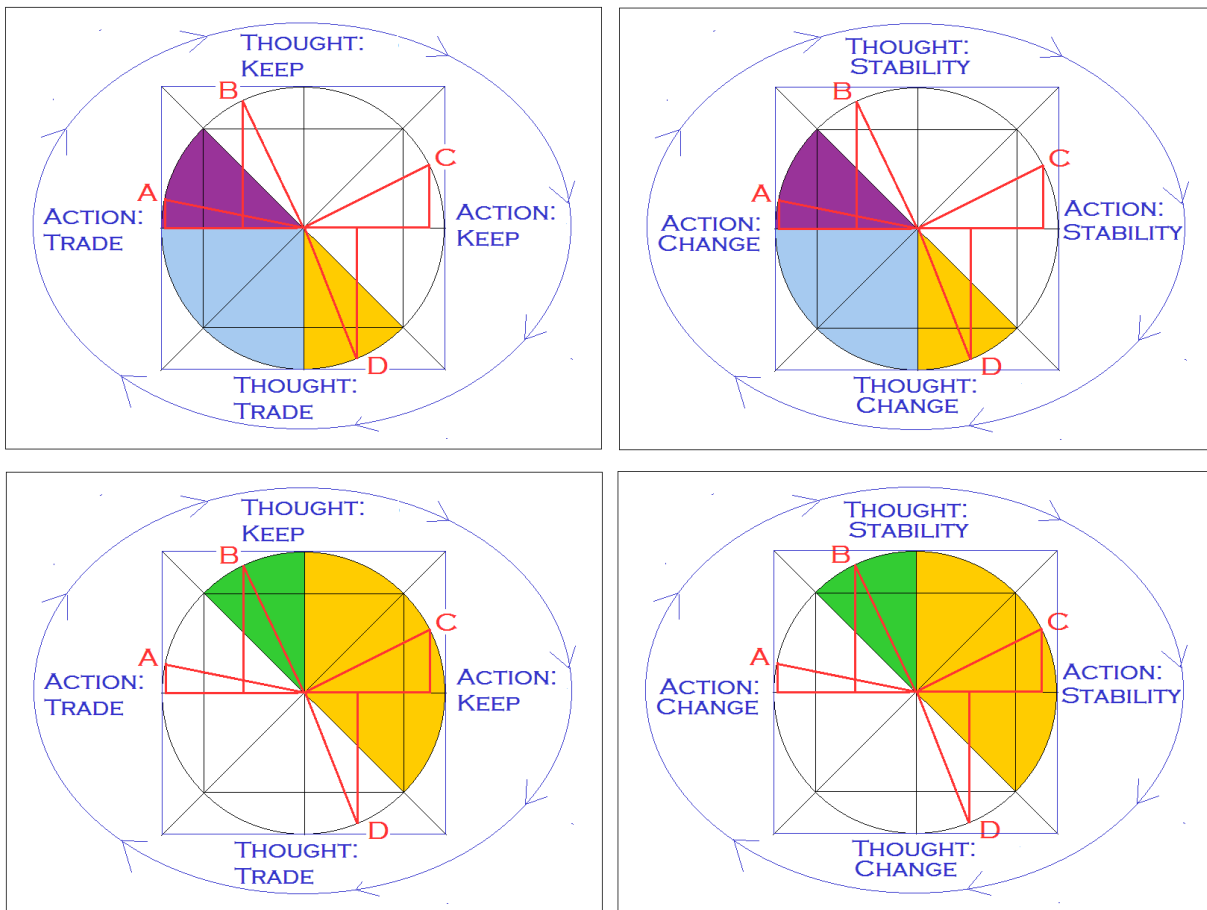
To demonstrate this, the fifth essay adds together the 28-year "economy wave" (damping cosine curve) and a 56-year "political wave" or "Kondratiev Wave" into the 56-year Political Economy Wave by charting a 56-year (20,454 day) period of changes beginning on April 9, 1805, 1861, 1917 and 1973. The equation for this combined wave is the following:

$$g(y) = 2^{\frac{1}{2} - \frac{2\left(y + \frac{1}{4}\pi\right)}{\pi}} \sin\left(2y + \frac{1}{2}\pi\right) + \sin(y)$$

DAMPING COSINE CURVE   SINE CURVE

Using the same color scheme given for the previous models we will examine in these essays the creation of the following mathematic wave running through American economic and social history.

Through an understanding of this wave and its operation we may propose historic analogies and predict crises in accord with these analogies. These predictions may then be tested against events as they unfold.

At the conclusion of the third volume of these essays the proportions of this model are combined into the following geometric form.
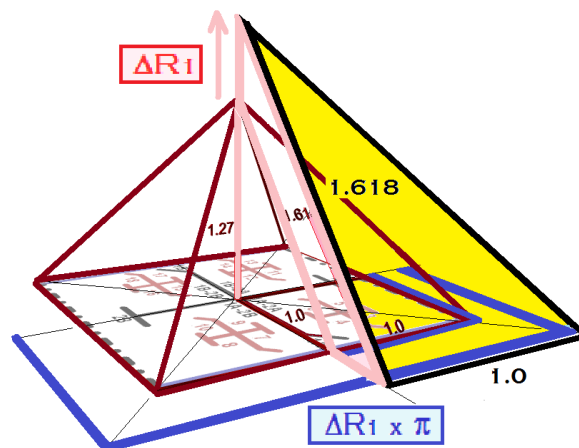
The combination of the economic ratios "1 : φ" and "1 : π" into a single structure suggests that the Great Pyramid of Giza, the dimensions of which incorporates ratios virtually identical to those described herein, is a model of five dimensions of reality, three of space, one of time and one of consciousness.

Empirical Foundations of the
Economic and Social History of the United States

Essay 1:
The "Chooser – Available Choice" Model

1. Hypothesis

I propose that social law is the larger fractal of the human mind and that society is the set of fractals created by this fact. We begin with a discussion of the central core of this model, the "Chooser- Available Choice" model.

DIAGRAM 1-1.
BASIC PLAN.

1. [yellow] MICRO-ECONOMIC CHOICE
   X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
   Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. [green] MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
   OKUN'S LAW STATES A $\pi : 1$ RATIO AS TO
   HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. [pink] REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
   THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
   AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. [red] DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. [blue] SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
   THE "KONDRATIEV WAVE"

2. Methods

I introduce the Cartesian coordinate system to establish a plane between that which is experienced by human beings (the x-axis) and that which is known to human beings (the y-axis). Taking the knowledge of something as the exact equal of the experience of it, we propose an infinite set of squares representing the merger of these two parts of human existence in a simple geometric shape.

The jury trial is proposed as the human mind writ large. From this social fact a "unit circle" may be developed based upon a geometric graphing of "actions" (the x-axis) and "thoughts" (the y-axis) regarding trading vs. keeping a piece of property in the simplest possible exchange of goods.

3. Data

I present here a strictly philosophic argument underlying the rest of the essays.

4. Procedure

4.1 The Pythagorean Theorem in relation to Actions and Thoughts

Every jury trial in the United States begins with the proposition that all which is necessary for the jury to know for its decision will be presented to it as a part of the evidence in the trial, and that which is irrelevant will be kept away. In this fashion the jury's personal *experience* of the evidence as presented in trial is contrasted with the *decisions* they make collectively as a result of their deliberations on that evidence.

We may build upon this social fact in the following manner.

For the purposes of these essays we will take as an axiomatic truth that all human life is based upon the presumed equivalence between that which we experience through the senses and that which we know to be real.[6] If "that which we experience" is given the variable "X" and "that which we know to be real" is given the variable "Y", we may state this equivalence as:

$$X = Y.$$

If we place this equation in a Cartesian coordinate system, we have the following 45 degree angle line, beginning at x = 0, y = 0 and extending on toward and infinite number of associations.

DIAGRAM 1-2.
TRIGONOMETRY OF EXPERIENCE AND KNOWLEDGE

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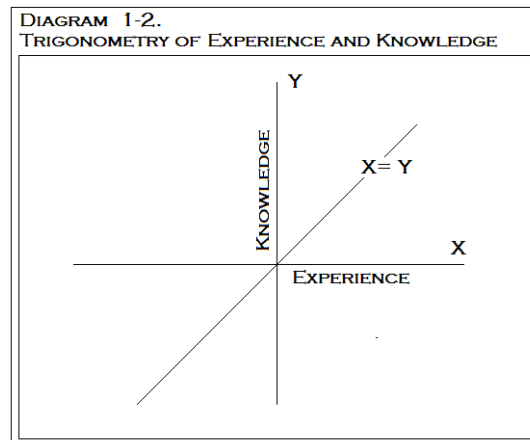
[6] See Boswell, J. (1820). "After we came out of the church, we stood talking for some time together of Bishop Berkeley's ingenious sophistry to prove the nonexistence of matter, and that every thing in the universe is merely ideal. I observed, that though we are satisfied his doctrine is not true, it is impossible to refute it. I never shall forget the alacrity with which (Samuel) Johnson answered, striking his foot with mighty force against a large stone, till he rebounded from it -- "I refute it *thus*."

One might assert that the experience of reading a book and enjoying the imaginary world conveyed is not the same as "experiencing" or "knowing" anything about the world imagined.

Our point here is far more modest and direct. The "experience" referred in this essay is simply that of "reading the book" and the knowledge considered is simply that the person reading knows that he or she is reading a book. The equivalence understood between the *experience* of reading the book, and the *knowledge* that one *is* reading a book, is the equivalence with which we begin this analysis.

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This picture represents the outcome of an infinite number of squares, wherein each corner point has a specific meaning. "X" represents our experience of something, "Y" represents our knowledge of the thing experienced, the point "(X, Y)" represents the interaction between our experience of the thing itself and our knowledge of the thing itself, and the origin of the graph "(0, 0)" represents the beginning association we make between experience and knowledge as fundamental assumptions of all inquiry.[7]

DIAGRAM 1-3.
TRIGONOMETRY OF EXPERIENCE AND KNOWLEDGE
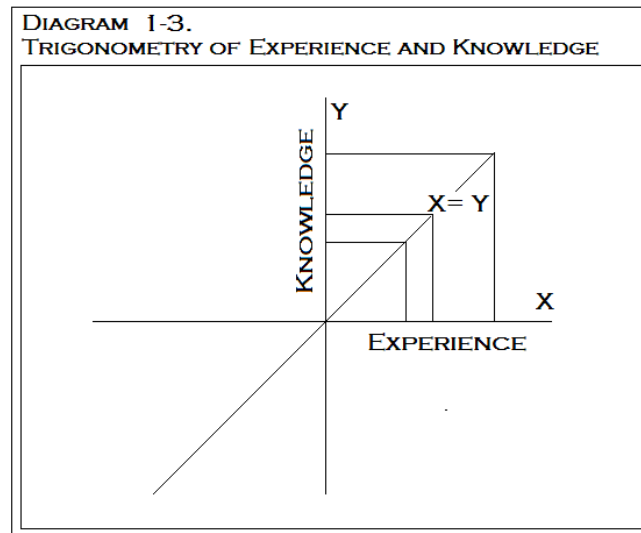
4.2 Extension to the Jury Trial of a Criminal Case

In the United States the jury trial of a case is premised on this same equation "X = Y," "experience" and "knowledge," taken to the next higher social level of the jury. The jury's reception and consideration of the evidence presented indicates that this small group is the expansion of the smaller individual and included minds. In the jury's deliberation the jury demonstrates itself as being the larger, expanded, copied and congruent larger "fractal" of the individual mind.

This expansion has significant mathematic consequences.

As indicated at the outset, every jury trial in the United States begins with the proposition that all which is necessary for the jury to know for its decision will be presented to it as a part of the trial, and that which is irrelevant will be kept away. In this fashion the jury's personal *experience* of the evidence as presented in trial represents the "X" of a trial proceeding.

The jury's evaluation of this evidence as understood through the prism of their own life experiences is the "Y" of the trial proceeding, their collective *knowledge* of the facts presented.

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[7]   See Ornstein, at 63: "In 1268, Roger Bacon, one of the founders of modern science, wrote (in his *Opus Maius....*), 'There are two modes of knowing, through argument and experience. Argument brings conclusion and compels us to concede them, but does not cause certainty nor remove doubts in order that the mind may remain at rest in truth, unless this is provided by experience.' These two modes are complementary (both are "right"), and together form the basis for the complete human consciousness."

The final verdict given by the jury states its evaluation of the association between the "X" of the trial (the evidence presented) with the "Y" of the trial (the jury's evaluation of this evidence).
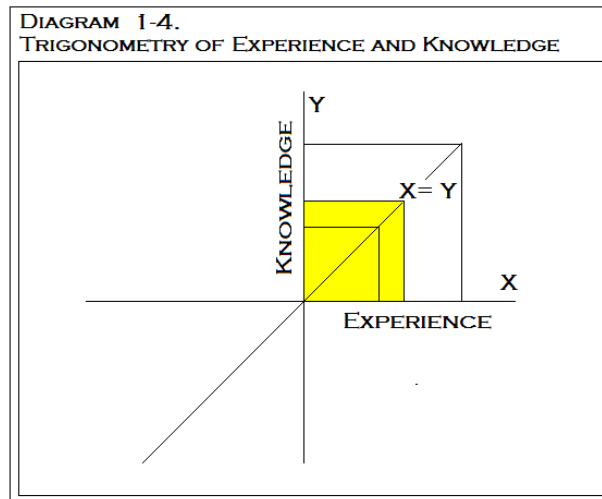
This simple model may be expanded upon.

The criminal law of the United States is based upon a dichotomy between the criminal act alleged to have been committed – the *actus reus* of the offense – and the mental intent –the *mens rea* of the offense – associated with the crime. For example, the act of killing someone is a homicide if done with the intent to kill the individual. If the killing was the result of recklessly driving in a crowded street, the crime is less because the evil of the intent to harm was less. Differences in the consequence to the Defendant can be quite significant, depending upon the nature of the criminal act and mental intent found by the jury.

If we let the "actus reus" of any given offense equal a particular number – for example, 5 – then the jury's experience with the evidence presented as to the criminal act (X = 5) and the jury's understanding of that evidence (Y = 5) may be given as a square, in blue below.

Similarly, if we let the "mens rea" of the same offense equal a different number – for example, 3 – then the jury's experience with the evidence presented as to mental intent (X = 3) and the jury's understanding of that evidence (Y = 3) may be given as a red square, in red below.

DIAGRAM 1-5.
TRIGONOMETRY OF EXPERIENCE AND KNOWLEDGE

EXPERIENCE / KNOWLEDGE OF "ACTUS REUS"   EXPERIENCE / KNOWLEDGE OF "MENTAL INTENT"
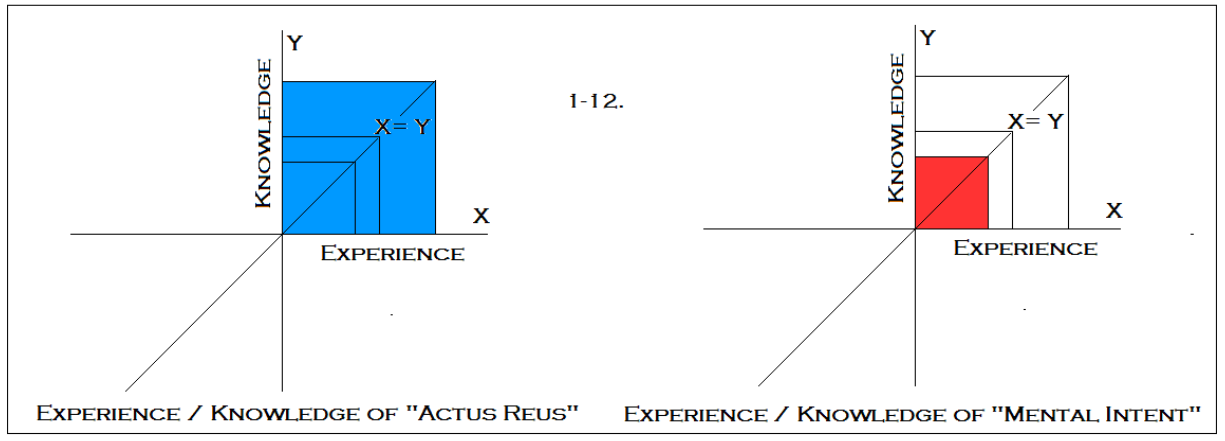
The culpability, if any, of the Defendant for a crime is given in accordance with the sum of these two elements of proof. The full experience and knowledge summarized by the case will equal the sum of these two squares. Stating the jury's experience with the evidence of a criminal act as a positive distance "A" and the jury's experience with the evidence of mental intent as a positive distance "B", then the experience / knowledge represented by Culpability (C) associated with the verdict should equal the sum of these two things, or :

$$A^2 + B^2 = C^2$$

Geometrically, this equation may be portrayed with the proportions of the Pythagorean Theorem as follows.

DIAGRAM 1-6.
PYTHAGOREAN THEOREM OF SOCIAL CONDUCT

CULPABIILITY
(CONSEQUENCE)

KNOWLEDGE

EXPERIENCE

MENTAL INTENT
("MENS REA")

KNOWLEDGE

EXPERIENCE

CRIMINAL ACT
("RES GESTAE")

KNOWLEDGE

EXPERIENCE
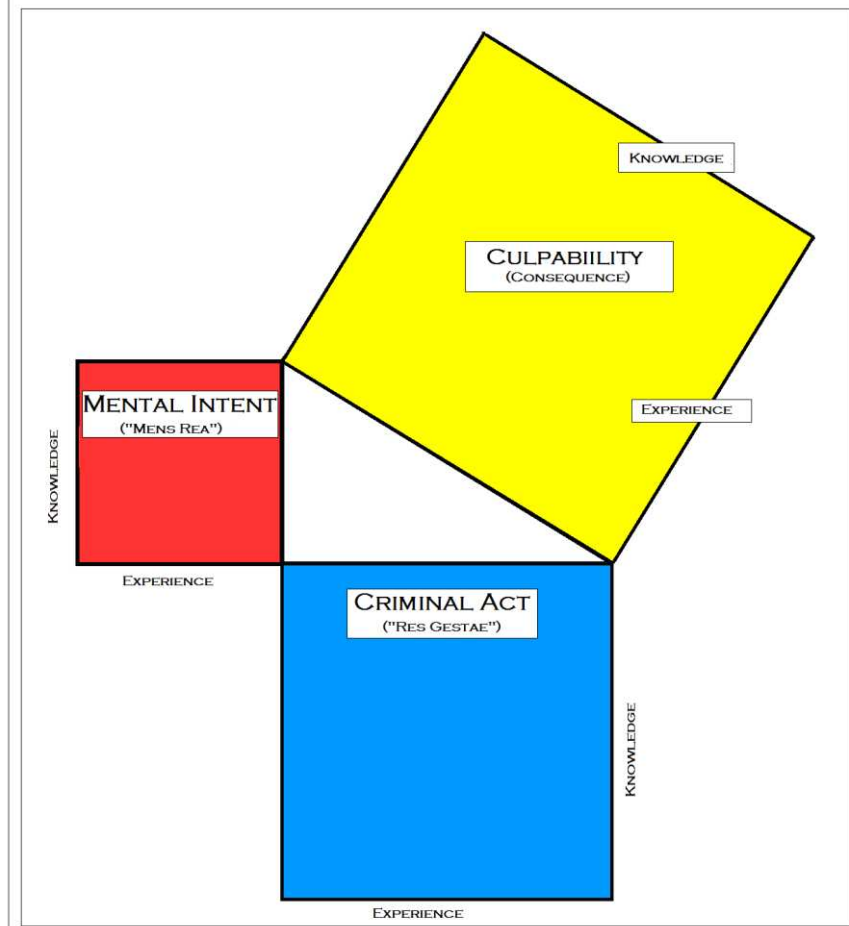
The use of Euclidean Geometry as a basis for understanding social relationships leads to a form of trigonometry which describes the wave characteristics explored in later essays. In this essay we present that trigonometry, a trigonometry of time.

4.3 Neo-Classical Economics and its Relationship to Our Approach

We may explore the impact of this approach through the indifference curve of neo-classical economics. (Shapiro, 2012) These curves attempt to demonstrate the microeconomic relationship between consumer preferences as balanced between two different goods. The curve drawn represents the "indifference" for any consumer as to which combination of good is offered. (left, Diag. 1-14)

The "indifference curves" generated from this pair of dichotomies represents the willingness to trade one set of goods for different goods. As increasing levels of affluence at provided, a map of multiple curves becomes possible. (center Diag. 1-14) The indifference curves of two competing trading partners may be explored by inverting the curve of one of the partners. (right, Diag. 1-14) "Pareto optimality" refers to the qualitative evaluation of these relationships. Given an initial allocation of goods among a set of individuals, a change to a different allocation that makes at least one individual better off without making any other individual worse off is called a Pareto improvement. An allocation is defined as "Pareto efficient" or "Pareto optimal" when no further Pareto improvements can be made.
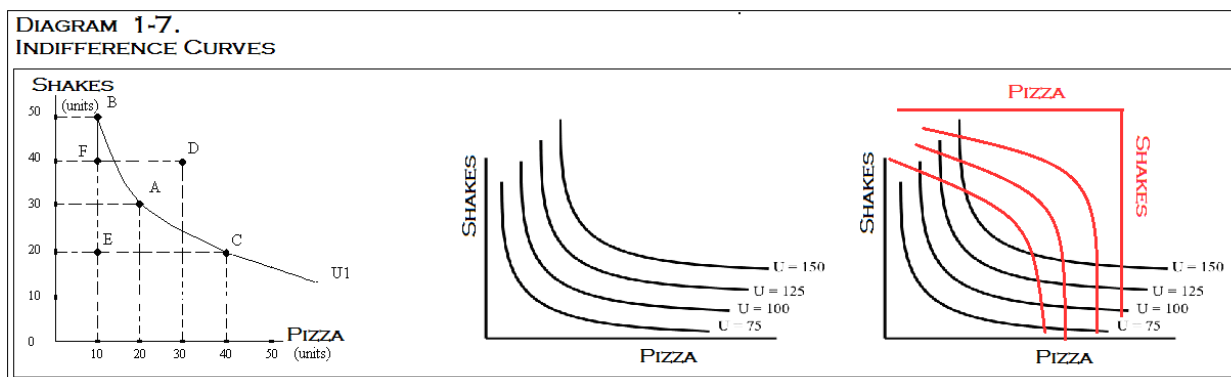
The thought process which pertains to a jury trial may be joined to our modern views of economics to create a foundation for our approach. We begin with the fact that American Society is governed by laws which state the rights of persons and parties within the jurisdiction of the United States and its member states. The right to a jury is guaranteed to every party before the courts, thereby permitting the party to have judgment declared by persons not directly connected with the political process. Empirically testable hypotheses may be structured upon these relationships as lawfully required.

From the economic point of view, there is no difference between stating that "John purchased x" and "John is guilty of purchasing x." The relationship between the act and the thought which motivates the act, speaking economically, is the same as that of the court considering such an act criminally.

DIAGRAM 1-8.
PYTHAGOREAN THEOREM - SOCIAL AND ECONOMIC ACTIVITY
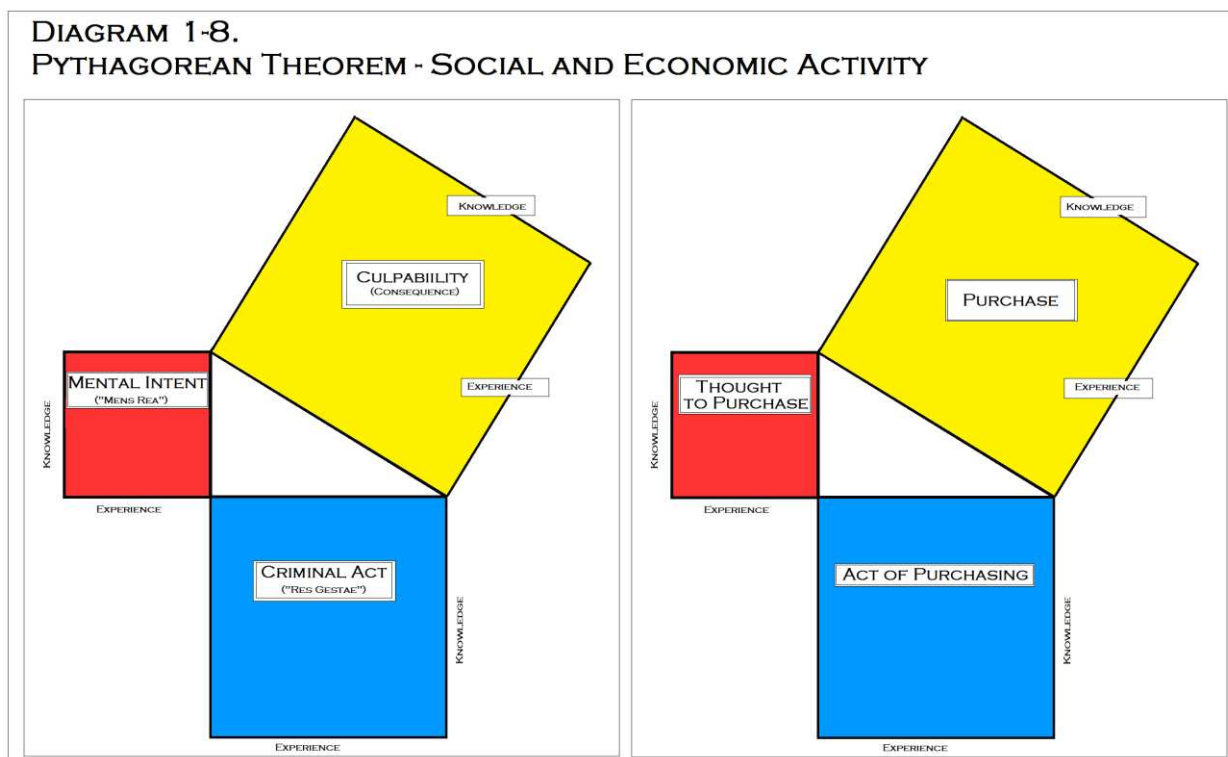
4.4 Extension to Micro-economics - The "Chooser – Available Choice" Model

Each of the points within the plane of an indifference curve – both those on the curves and those outside the curve – represents a given decision to trade or to keep various properties. If we contrast the actions of *trading* a good versus *keeping* that same good, a set of dichotomies may be constructed which maybe used to structure our understanding of economic development.

The first dichotomy – action, as comparable to the "actus reus" of criminal law – represents a tension between "Keeping" a particular good vs. "Trading" the good for something else. This is indicated in the circle below by the opposition of "Keep" at 3 o'clock and "Trade" at 9 o'clock. All economic life stems from the core principle that one may *act* freely in choosing either to keep a given property or to trade it for some other piece of property and that these transactions clearly affect the status of the property so owned or traded.

This is contrasted with a secondary dichotomy – thoughts, as comparable to the "mens rea" of criminal law – which represents a tension between one's mental "thoughts in favor of keeping" and "thoughts in favor of trading" a particular property, located at 12 o'clock and 6 o'clock respectively in the circle below. These are the mental pre-dispositions of every owner towards keeping or trading a given piece of property for something else.

DIAGRAM 1-9.
TRIGONOMETRY OF ACTION AND THOUGHTS
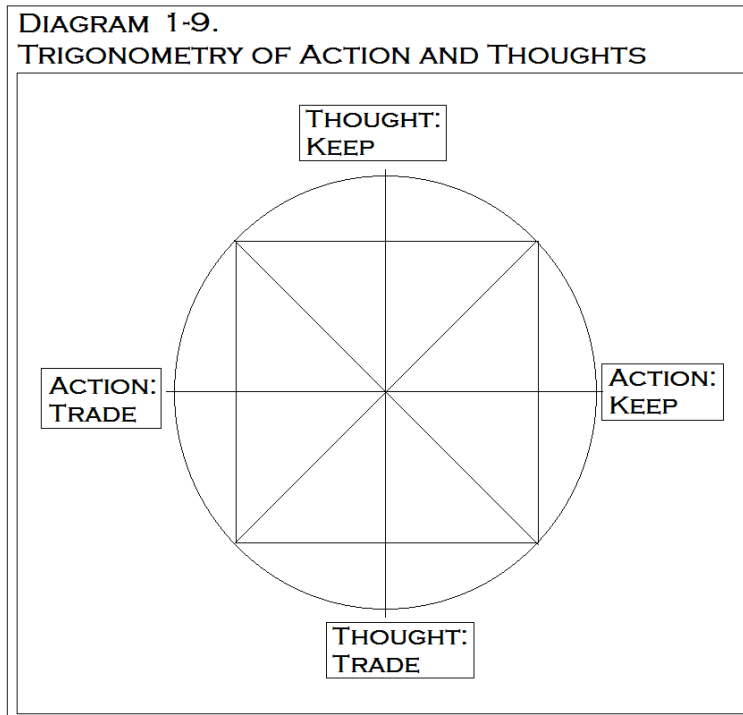
Using the Pythagorean Theorem to structure the sum total of possible permutations between the "Action" aspect of a purchase, and the "Thought" aspect of a decision to Purchase, we may structure every possible balancing of these two with the "Purchase" itself.

DIAGRAM 1-10.
TRIGONOMETRY OF TRADING VS. KEEPING PROPERTY
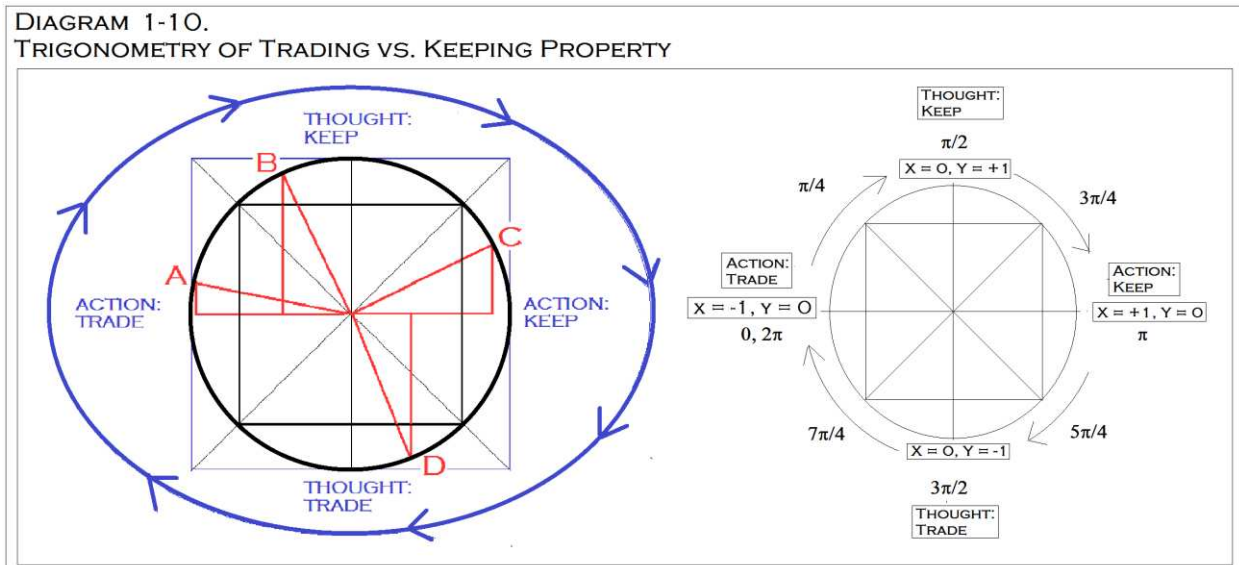
The Pythagorean relationships inherent in the association of Action and Thought as expressed previously create around the unit circle create an infinite set of mathematic relationships wherein the actual possibility of a Purchase is set as the sum of some combination of Action and Thought.

DIAGRAM 1-11.
TRIGONOMETRIC RATIOS.
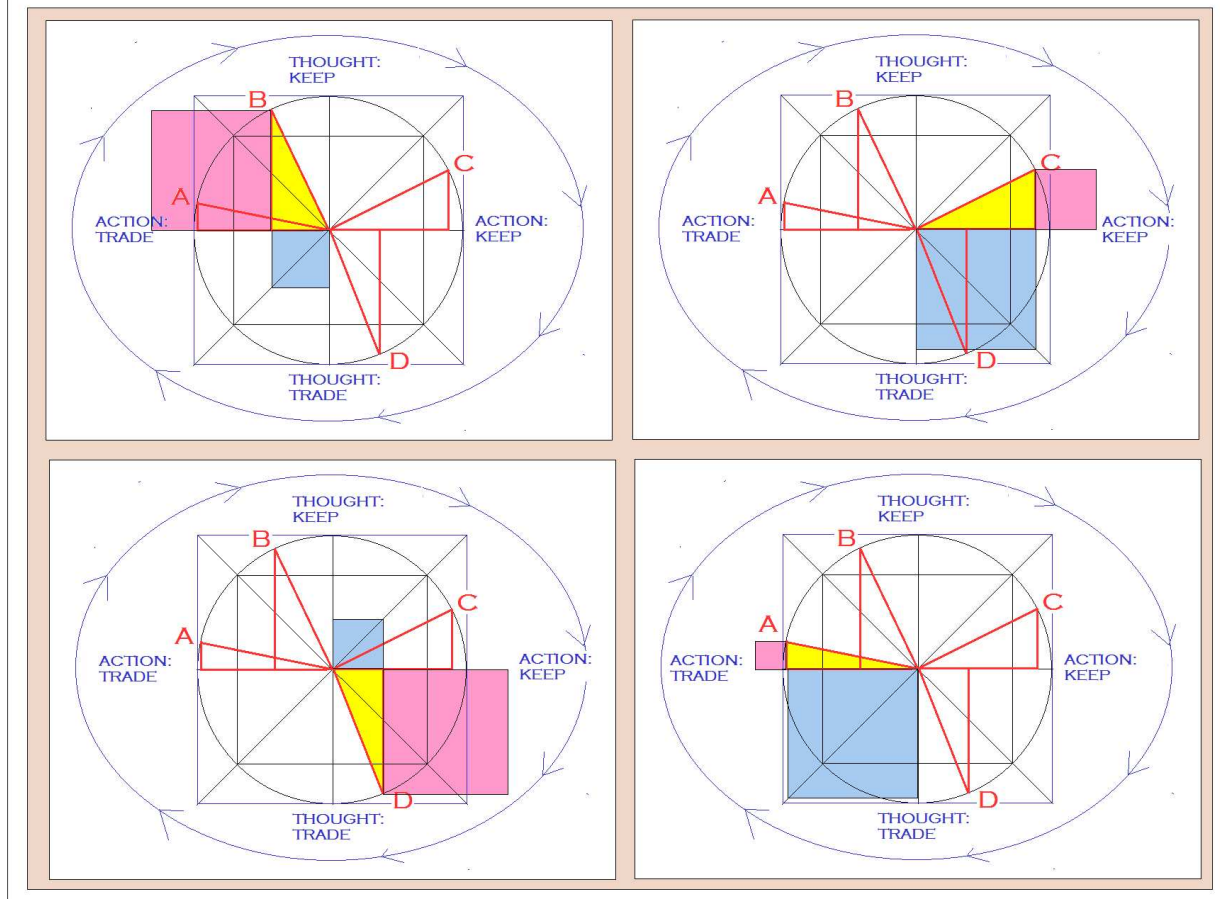
The unity of the underlying ego which selects these various points may be associated with the radius of this circle. If we give this radius the number "1" it represents the "unity" of the ego as a balancing radius between these two dichotomies of Action ("Trading" vs. Keeping") and Thoughts ("Thoughts related to Trading the property," "Thoughts related to Keeping the property"). An internal angle is thus constructed at the origin of the coordinate system.

4.5 Waves Arising From The "Chooser – Available Choice" Model

If we consider the side opposite the internal angle as divided by the hypotenuse of "1" we set up a set of fractions which may be charted against an x-axis wherein the circumference of the circle is superimposed upon the x-axis in divisions associated with 2π. Beginning at 9 o'clock and moving clockwise, we have the following mathematic associations between various points along the unit circle, to wit, the sine curve.

DIAGRAM 1-12.
56-YEAR "KONDRATIEV WAVE" SINE CURVE.
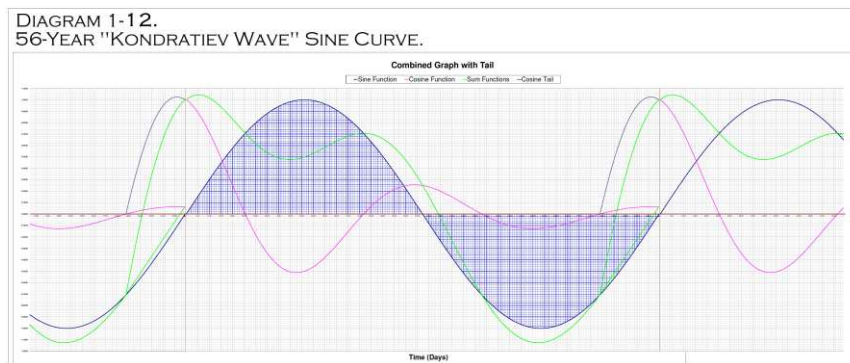
The equation for this wave is:

$$g(y) = \operatorname{SIN}(y)$$

There is only one point along the Unit Circle where Action is wholly aligned with Trading, i.e. the point at 9:00. All other points along the unit circle are similar to one another in that there is some "Y" component connected to some mental aspect of trading and/ or keeping the object in question. This mental aspect must include some possibility of cancelling the action contemplated.   Consequently only at 9:00 o'clock is the possibility of a "Trade" wholly equivalent with Action, and at this point "Thought" is Zero and the Action Trading occurs.

Conversely at 3:00 o'clock the action undertaken is to "Keep" the property in question and the status quo is actively continued.

DIAGRAM 1-13.
TRIGONOMETRY OF TRADE.
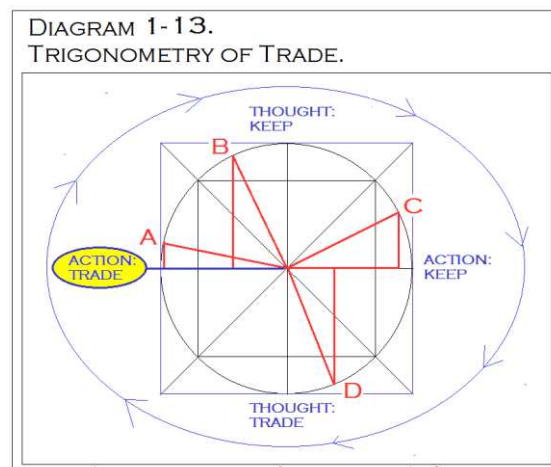
The unique aspect of this point at 9:00 o'clock creates an unavoidable change in the overall unit circle. The break which is presented at (x = -1, y = 0) creates a new and unknown element in the unit circle itself. Once the trade is made, the situation is no longer the way it was. Something new has taken place. [8]

In contrast, when the x-axis is directed toward "Keeping" a particular good, the point at which Thought = 0 will be that point most dedicated in favor of the status quo.

DIAGRAM 1-14.
NEW CIRCLE ON TRADE.

THOUGHT: KEEP
π/2
X = O, Y = +1

π/4   3π/4

TRADE
X = -1, Y = O
0, 2π

KEEP
X = +1, Y = O
π

7π/4   5π/4
X = O, Y = -1

3π/2
THOUGHT: TRADE

---
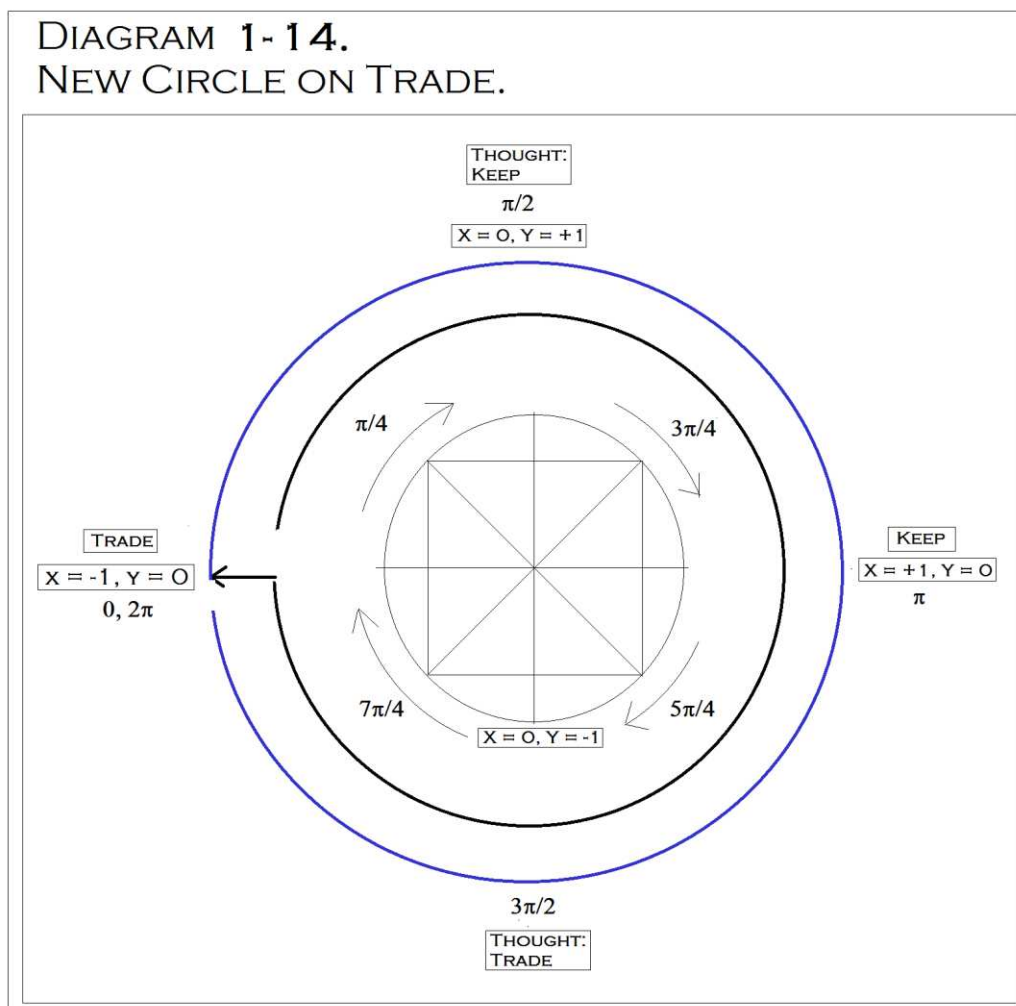
[8]   There is an analogy here to quantum mechanics in the "Schrodinger's Cat Thought Experiment." The second half of the third postulate of quantum mechanics states, roughly speaking, that observation changes the physical system. http://vergil.chemistry.gatech.edu/notes/quantrev/node20.html   A physical system exists in as many state as possible until it is observed. Once the observation has been made, it changes into another state, one which can be unique or not.

Until one opens the box, the cat is both dead and alive. Opening the box (observing the state of the cat), indicates which state it is, and so changes the state of the physical system. In this essay, trading equates with the observation. By analogy, stating that with trade "something new has happened" one would indicate that the wave function describing the state of the cat has changed.

The model will be referred to as the "chooser – available choice" model, as a way of presenting the unit circle and its radius of "1" – representing the "chooser" – and the number π – representing the "choices available" – in a simple and direct fashion. Our premise is that a radius originating at the center of the unit circle and moving toward any spot on the circle of possible choices divides the circle at a 1 : π ratio. Half of the circle constitutes "available choices" which will be associated with the point at which the radius and the circle intersect. This relationship will exclude an equivalent set of opposite choices on the opposing side of the circle.

In other words, one can not simultaneous trade a good and keep the same good, or vice versa. The possible choices which *are* available toward any particular goal are those which are not directly undermining of whatever goal is chosen. The choices which are *not* available are those which are in some negative value, or opposite position, from this chosen goal. This same dynamic applies to any point of psychological consideration along the unit circle.
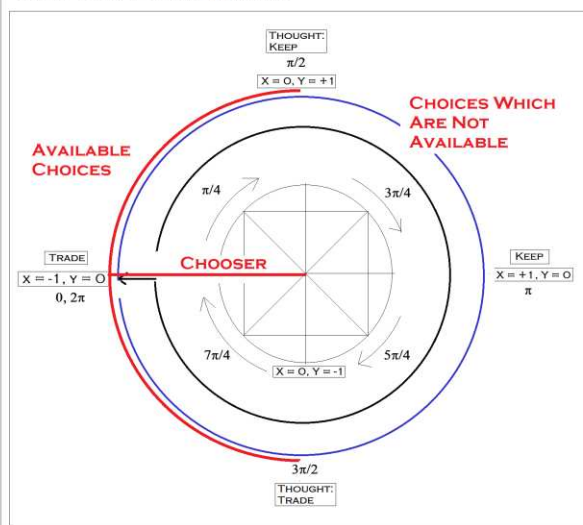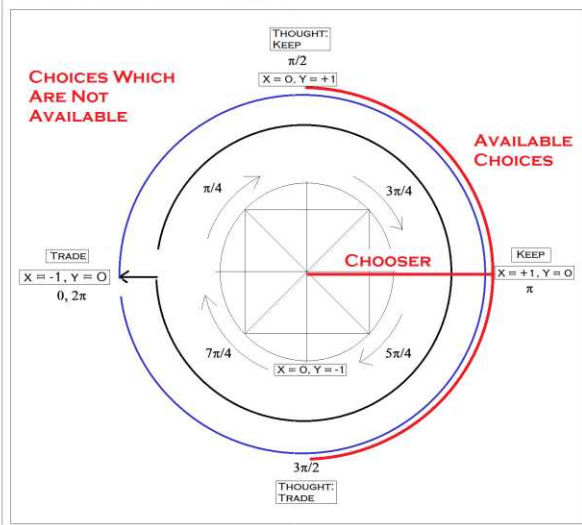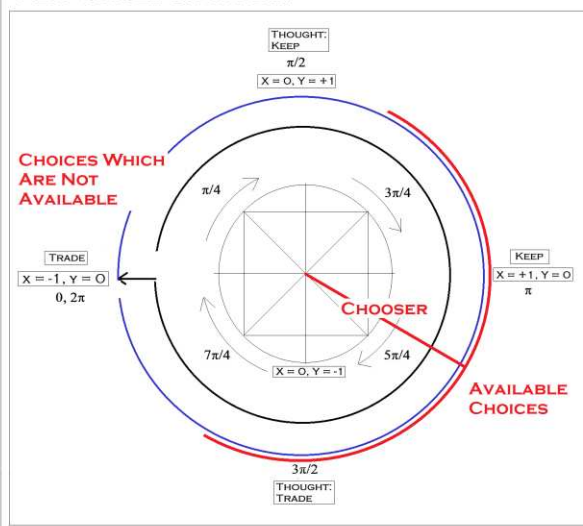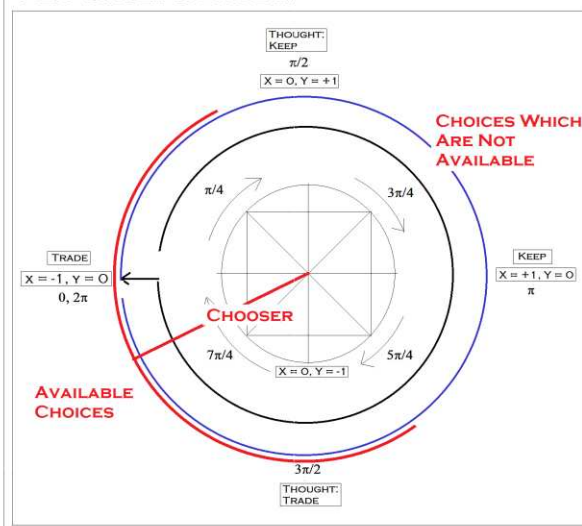
CONCLUSION

We conclude that it is possible to construct a simple and mathematically straight-forward model of micro-economic choices which is completely in accord with the available evidence of social behavior as evidenced by universal and legally required social understandings.

By drafting the experience and knowledge of a jury as the larger "fractal" of the individual mind, we have the ability to state a pattern of "mind" itself which is both useful and concrete in its form.

Empirical Foundations of the
Economic and Social History of the United States

Essay 2:
Does Okun's Law State A "π : 1" Relationship?

INTRODUCTION: WHAT IS "OKUN'S LAW"?

In the previous essay we discussed the first, central "unit circle" relating to the "chooser – available choice" model. We come now to the aggregate of this model, that "unit circle" wherein microeconomic decisions to trade or keep a given thing aggregate to form a year's worth of such decisions. This aggregate is known as "annual real Gross National Product." (Diagram below, in orange)

The Gross National Product of any country, in association its rate of employment, are two of the most important variables in economics.

DIAGRAM 2-1.
BASIC PLAN.

1. MICRO-ECONOMIC CHOICE
X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
OKUN'S LAW STATES A π : 1 RATIO AS TO
HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
THE "KONDRATIEV WAVE"

The empirical relationship between production and employment in the United States is known to mainstream economics as "Okun's Law." "Okun's Law" states that for every three percentage points of increase in real GNP the rate of employment will increase by one percentage point, and that decreases of both will take place in the same proportion. This 3 : 1 proportion is generally referred to using a double negative, i.e. an increase of three percent in real GNP will lead to a one percent *decrease* in the rate of *un*employment. First stated by Arthur Okun, at the time senior economist of President Kennedy's Council of Economic Advisors, the rule is "one of the most reliable empirical regularities in macroeconomics." (Tobin, 1983)

The article "How Useful Is Okun's Law?" by Dr. Edward Knotek, a senior researcher for the Kansas City Branch of the Federal Reserve, was published in the bank's research journal Economic Review in the Fourth Quarter 2007. The data sets used in this essay cover a 60 year period of American economic history, i.e. the second quarter of 1947 through the third quarter of 2007.
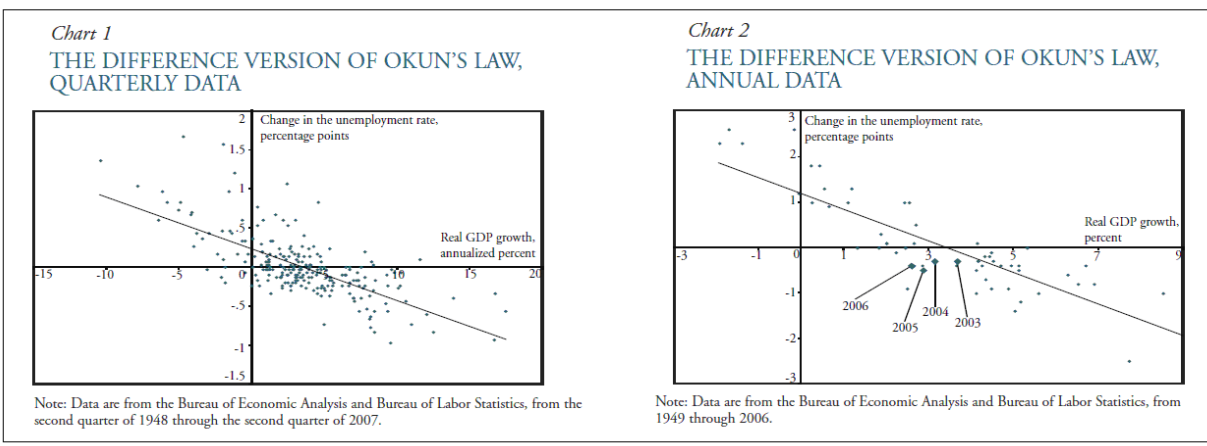
In this article Dr. Knotek provides an overview of the ideas underlying Okun's Law as well as the economic measurements which support it. According to this article at the present time Okun's Law is an unexplained statistical regularity which must be considered more a "rule of thumb" rather than a formal law.

Our purpose in this essay is (1) to lay a theoretic foundation for an understanding of the regularity of Okun's Law, as well as (2) to present our proof that the actual mathematic relationship between changes in the rate of unemployment and the rate of GNP growth is not a 3 : 1 relationship but a π: 1 relationship.

This essay will concentrate on three charts from Knotek 2007. Charts One and Two graph the quarterly and annual data sets supporting the regularity of the relationship between changes in the size of real GNP (x-axis) and the corresponding effect this has on the rate of employment (y-axis).

DIAGRAM 2-2.
CHARTS ONE AND TWO OF "HOW USEFUL IS OKUN'S LAW?"

Chart 1
THE DIFFERENCE VERSION OF OKUN'S LAW, QUARTERLY DATA

Note: Data are from the Bureau of Economic Analysis and Bureau of Labor Statistics, from the second quarter of 1948 through the second quarter of 2007.

Chart 2
THE DIFFERENCE VERSION OF OKUN'S LAW, ANNUAL DATA

Note: Data are from the Bureau of Economic Analysis and Bureau of Labor Statistics, from 1949 through 2006.

Dr. Knotek argues that the stability of the trend lines shown above masks the underlying dynamics of these relationships. Consequently Chart 3 also will be discussed (in Essay 5). He states:

> One problem with a long time series – such as from 1948 to 2007 – is that history can hide changes in relationships. This is the case for Okun's law. The previous section (Charts 1 and 2) found considerable similarities between Okun's original estimate and an updated regression using a longer time series. This section shows that, when estimated over shorter time horizons, the relationship between changes in the unemployment rate and real output growth has varied considerably.
>
> To capture this variation, this article uses a technique called rolling regressions. A rolling regression estimates a particular relation over many

different sample periods. Each regression produces a set of estimated coefficients. If the relationship is stable over time, then the estimated coefficients should be relatively similar from one regression to the next. Variations in the relation will appear as sizeable movements in the estimated coefficients.

DIAGRAM 2-3.
CHART THREE OF "HOW USEFUL IS OKUN'S LAW?"

Chart 3
ROLLING REGRESSION ESTIMATES

Notes: Dates along the horizontal axis denote the last quarter in the sample period for each rolling regression. Each sample period is 13 years long.
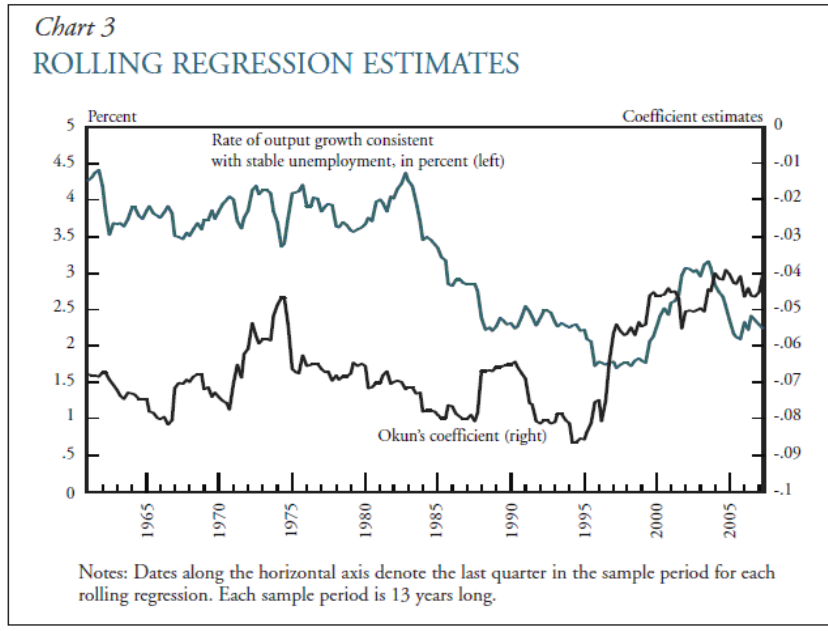
We seek here to augment this opinion with information from these essays.

ECONOMIC METHODOLOGY

1. Hypothesis

United States annual real GNP may be represented geometrically as a torus the radius of which represents the rate of employment; one half the circumference of which represents the chronologic creation of real GNP over the course of a calendar year; the opposing half circumference of which represents the money price of each transaction making up that real GNP; and the cylindrical radius of which is set equal to the GNP per capita of the United States for the year in question. Using this model the relationship between an increase in the rate of employment and the size of real GNP is not 1: 3 but rather $1 : \pi$.

2. Method

We provide a description of the econometric measurements which may be expected to develop from the previous essays surrounding the relationship between economic choice, employment and real GNP. We then review the data sets used in Knotek 2007.

We conclude that there is strong support for the proposition that the 3:1 ratio presented by Okun's Law is in reality a $\pi : 1$ ratio. We further suggest that the regularity of Okun's Law and its central place in macroeconomics is due to the trigonometric relationship which this $\pi : 1$ ratio has on the entire spectrum of economic study.

3. Data

This essay is an extended comment on the measurements provided by Dr. Edward Knotek in his article "How Useful Is Okun's Law?" published by the Federal Reserve of Kansas City in their publication Economic Review. The employment and GNP data used are those of the article has kindly been supplied by Dr. Knotek, and this has been cross-referenced with the original data kept by the United States Government.

4. Procedure.

4.1 U. S. Real Gross National Product:
The "Chooser - Available Choice" model in aggregate

The "chooser – available choice" model is the central point of departure for this model. If we invert this model such that the willingness to "trade" of one person meets the willingness to "trade" of a trading partner, we have a connection between two people indicating a mutual willingness to exchange goods or services with one another. (See discussion of Pareto efficiency in Essay One, lines 503-509) The willingness and ability of persons to trade goods and their services with one another is the foundation for the entire economy.

Let us begin with a proposed willingness of Farmer Jones to part with two cows in return for three horses. This willingness is met by Farmer Smith who is willing to trade three specific horses which he owns in return for two specific cows belonging to Farmer Jones.

The fact that these two farmers have met with a match which in their minds is favorable to both is indicated by the fact that both have extended the 9:00 axis "Action : Trade" towards one another. As a result of this trade, Farmer Jones' two cows will be handed over to Farmer Smith, and Farmer Smith's three horses will be handed over to Farmer Jones.

DIAGRAM 2-4.
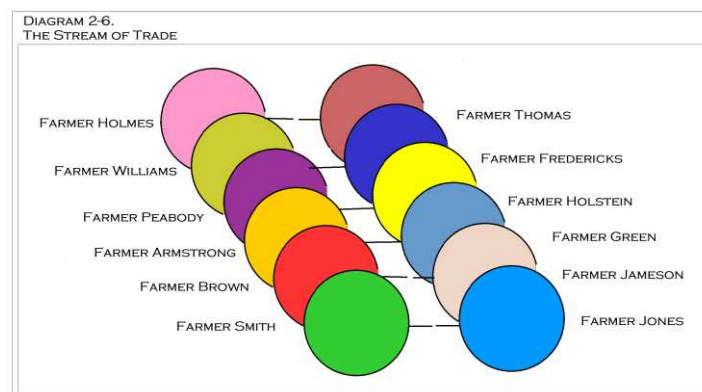"TRADE" UNDER THE "CHOOSER - AVAILABLE CHOICE" MODEL
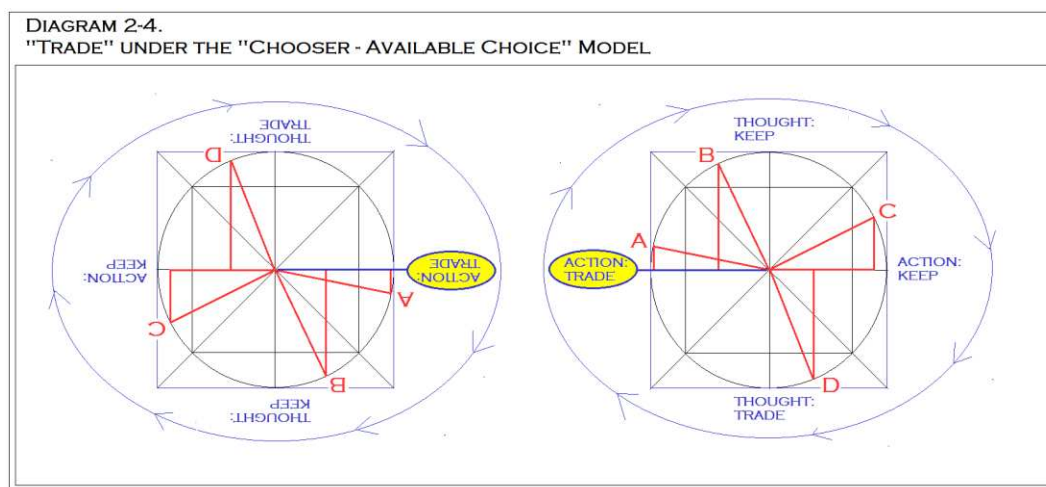
The following two circles simplify the basic ideas going into the above trade. Note that the early barter of horses for cows suggested by the circles below depicts trading at its most elementary level. Note that the trade itself must in some fashion state an improvement in the lives of the trading partners. Consequently the act of trading makes more efficient and useful the sum total of property within society because those who own the property are seeking ever more agreeable collections of that property by trading what they have for things which they desire but do not possess.

DIAGRAM 2-5.
A SINGLE TRADE

FARMER SMITH   FARMER JONES
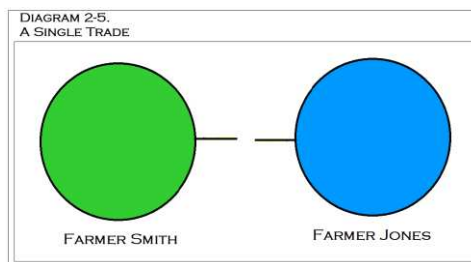
These trades represent a re-arrangement of property amongst those owning property. There is no "expansion" of the economy based upon this trade. However the usefulness of the property exchanged, in combination with the improved efficiency brought about by the trade, suggests that the natural rate of increase in any biologic organism – a farm, a household, a local market – will result from the full set of trades engaged in by all persons.

In short, the same property and the same traders exist after as well as before the trade. However the straight forward exchange of one set of property for another is conveyed by the model above.

There is no limit to the number of such trades which can be done over the course of any particular period of time. We may imagine two pipes running parallel, each suggesting the desire of one of two trading partners to enter into trade. Each trade may be listed in chronologic order and depicted as below.

DIAGRAM 2-6.
THE STREAM OF TRADE

FARMER HOLMES
FARMER WILLIAMS
FARMER PEABODY
FARMER ARMSTRONG
FARMER BROWN
FARMER SMITH

FARMER THOMAS
FARMER FREDERICKS
FARMER HOLSTEIN
FARMER GREEN
FARMER JAMESON
FARMER JONES

As reliable currency enters into circulation persons engaged in trading have the further ability to makes trades of much greater complexity that a straight-forward barter. By saving the money obtained from prior trades people are able to amass a trading ability to trade which far exceeds the more clumsy and complicated trade of physical objects, herds of cattle or flocks of geese, etc.

The ability to trade goods and services for currency permits the evaluation of the worth of the trade itself in relative terms visa vi all other trades, however subjective. A trade of $50 might represent an acre of land, a pair of mules, a suit of fine clothes or a suite of furniture. By "mirroring" the value of these various goods (or services), currency permits a much broader extent of trading and trading partners.

The pastel coloration below of the thing traded – money – is available to give a relative value to all the trades of an economy. These "trades" now become "sales," i.e. the surrender of something in return for currency.

The chronology of the trade is given be the difference in color, the red trade being first, the yellow being second, the green third, the orange fourth, etc. The pastel coloration indicates that in this case Farmer Jones did not trade goods for goods but rather money for goods (or services).

The size of the trade in question, its monetary value, is indicated by the number of circles used. For example Farmer Smith's trade of goods or services for money (three green circles) is three times as valuable in monetary terms as Farmer Brown's trade of goods and serves for money (one red circle), Farmer Frederick's trade of goods or services for money (one yellow circle) and Farmer Armstrong's trade of goods or services for money (one orange circle).

DIAGRAM 2-7.
CHRONOLOGIC SALES OF GOODS AND SERVICES

FARMER BROWN

FARMER FREDERICKS

FARMER SMITH

FARMER ARMSTRONG
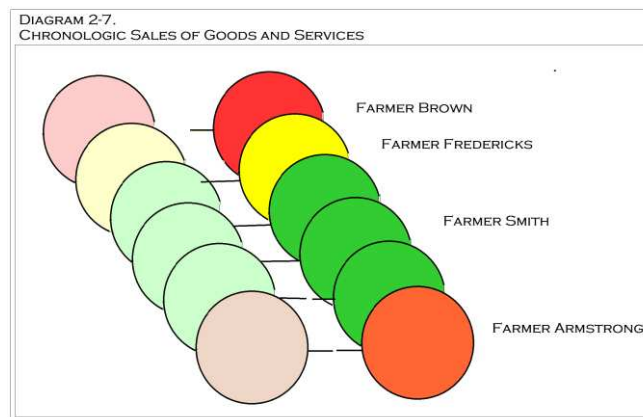
If we set an arbitrary division of the stream of trade at a single 365-day year, we can place the monetary and the "real" aspects of these sales of goods and services as oppositions from one another. The result is a circle of such sales. The length of half the circle indicates the monetary value of each of the sales of goods or services included in the year. If the size of these transactions is copied into the length of the circuit itself, we have the following. Because the connection of any particular sale of a good or service to the year "1973" is no greater than any other trade, we draw here a circle, i.e. that geometric construct in which all points in a plane lie equidistant from a single point.

DIAGRAM 2-8.
UNITED STATES ANNUAL REAL GNP

FARMER BROWN
FARMER FREDERICKS
FARMER SMITH
FARMER ARMSTRONG

1973

MONETARY PRICE
PAID FOR
GOOD OR SERVICE
PURCHASED

GOOD OR SERVICE
INCLUDED IN
ANNUAL REAL GNP
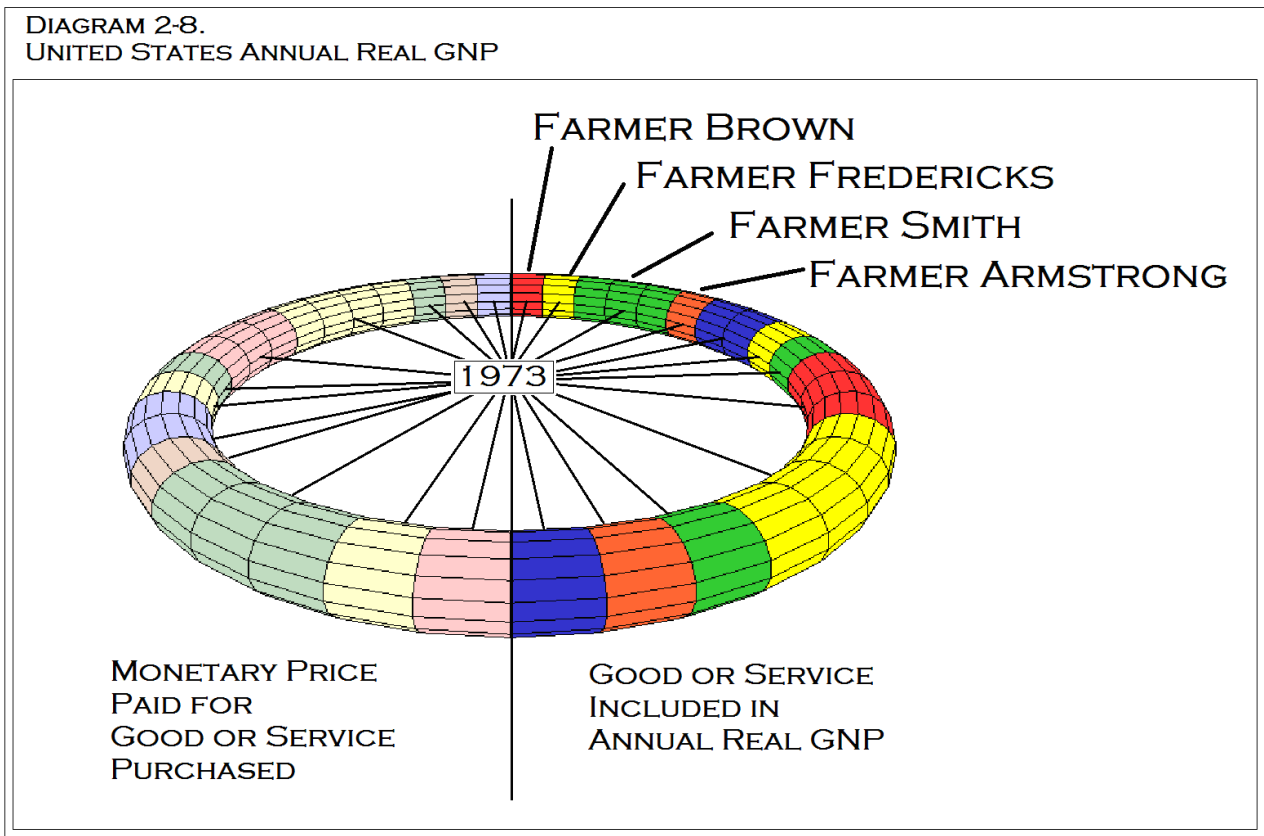
The development of currency and its association with trade given above suggests that the "employment" necessary for Farmer Smith or Farmer Jones to possess trade-able items has now become the "employment" of Farmer Smith and Farmer Jones as engaged in these occupations. In this fashion the use of currency which has turned "trades" into "sales" is in a direct relationship to the rate of employment, i.e. that employment necessary to sustain the full scope of sales given above.

In the above diagram 2-8 we have used the GNP per capita of the United States as a radius "r" of the generating circle and the rate of unemployment as the radius "R" of the generating torus which swings the smaller circle in an arc around the center point "1973." [9]

If this relationship is stated geometrically, it would appear necessary that an increase in the rate of employment from one year to the next (R = the radius of the circle = 1) will correlate geometrically to a necessary increase in the size of GNP (Y = half circumference = π) at the necessary ratio of 1 : π, as follows.

DIAGRAM 2-9.
MODEL OF PRODUCTION VS. EMPLOYMENT

$$\frac{\pi}{GNP}$$

$$\frac{R_1}{Y}$$

$$\frac{\Delta R_1}{Y}$$

$$\frac{\Delta R_1 \times \pi}{GNP}$$

4.2. Data Survey – Expected Findings

Let us examine how these relationships must be found in the available data.

1.   The selection of a chain of economic transactions as a subset of an entire chain of such transactions is an action arbitrary in nature.

DIAGRAM 2-10.
CHRONOLOGIC CHAIN OF TRANSACTIONS
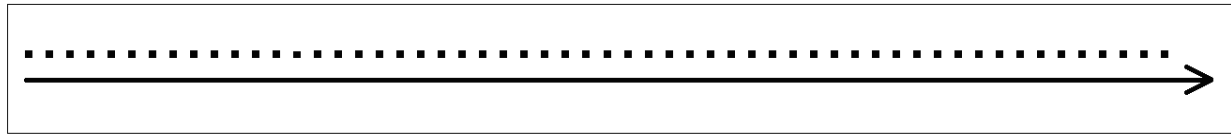
2.   The above points simply indicate an ongoing flow of transactions over time. If we denominate a certain subset of these transactions as occurring in "1973", we draw an arbitrary distinction between them. This is the arbitrary and imposed similarity of a temporal association between these transactions as occurring within the time span of "1973."

DIAGRAM 2-11.
SELECTION OF TRANSACTIONS WITHIN "1973"

1972   1973   1974
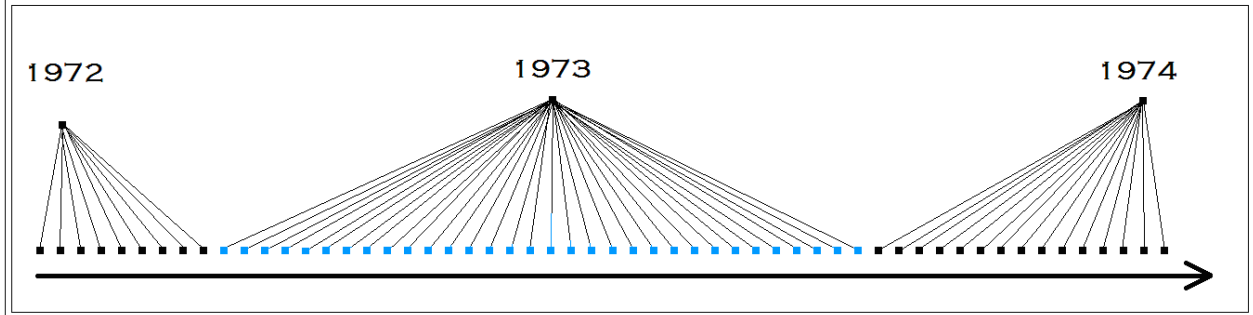
3.   As we associate these transactions with a period of time, none are more or less connected to 1973 than any of the others. Consequently there is an equivalence between all points listed as equidistant from a single point. This is conveyed by a diagram of the radius of ½ a circle (in blue), the other ½ being the monetary value of the particular transaction (in red). The relative value of these transactions vis-a-vis all other transactions is given by the length of the circumference taken up. A larger transaction occupies a larger portion of the circumference, smaller transactions occupy a lesser portion of the circumference.

DIAGRAM 2-12.
CHRONOLOGIC SET OF TRANSACTIONS

1973
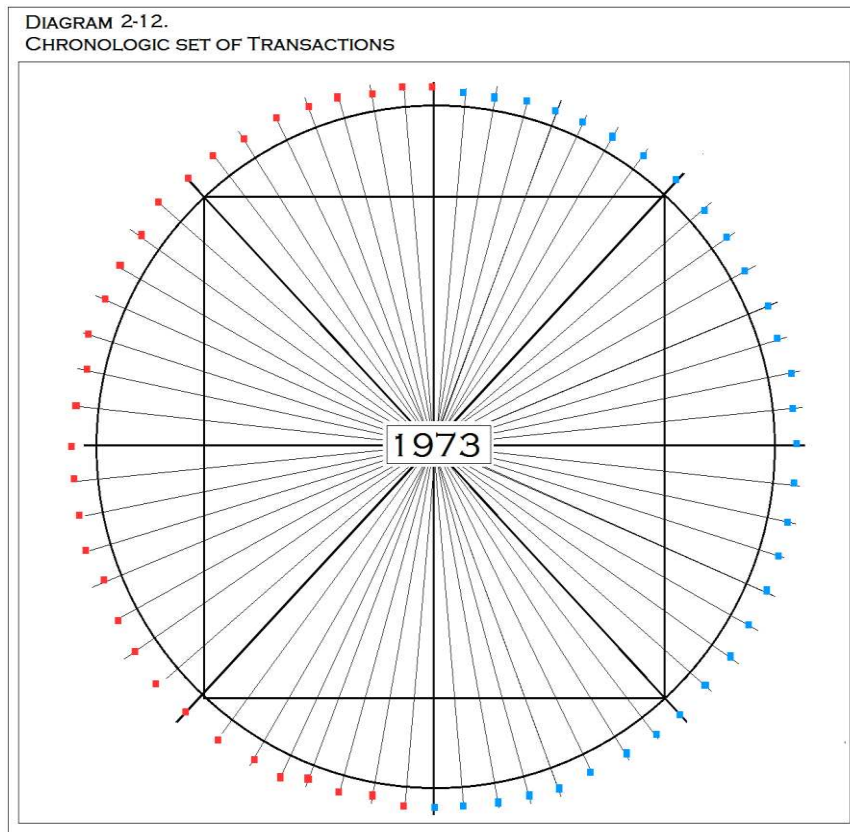
4.3 Necessary Linear Relationships

4.   The relationship which we are anticipating is that a 1: π relationship will exist between a change in the rate of unemployment and the percent change in growth of GNP. As the rate of growth increases on the x-axis, the rate of unemployment will go down on the y-axis. Setting this relationship as a straight-forward linear relationship, we have the following.


DIAGRAM 2-13.
PI : 1 RELATIONSHIP BETWEEN GNP GROWTH AND CHANGE IN THE RATE OF EMPLOYMENT
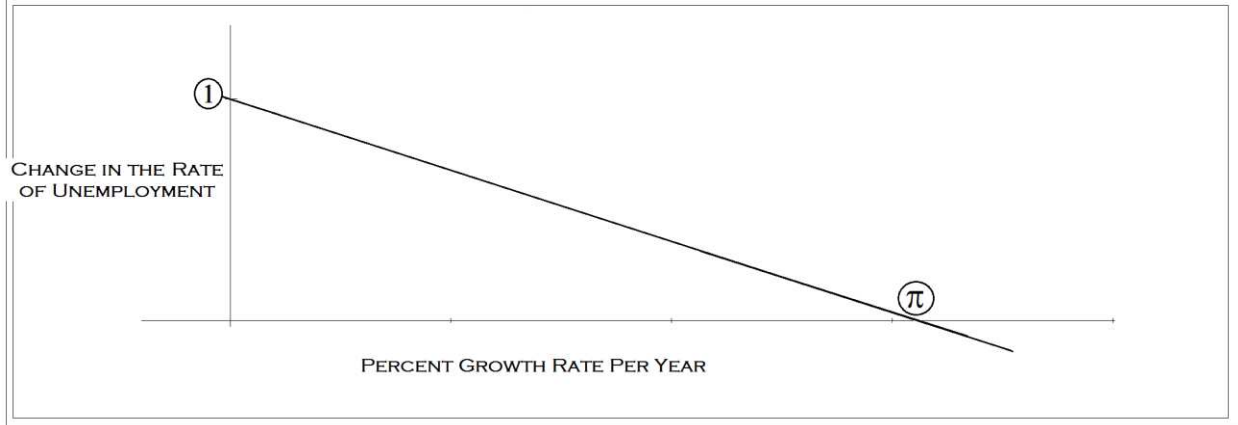
5.   In order to establish a Golden Mean proportion in the economy the United States must possess a steady state rate of growth of approximately 3.4969% per year (see Essay Three and Four). As these associations are made with a new steady state rate of growth of 3.4969% per year, the new y-axis intercept is not "1" but 3.4969 / π = 1.1131227.


DIAGRAM 2-14.
PI : 1 RELATIONSHIP BETWEEN GNP GROWTH AND CHANGE IN THE RATE OF EMPLOYMENT USING GOLDEN MEAN RATE OF GROWTH OF 14-YEAR OCTAVES = 3.4969
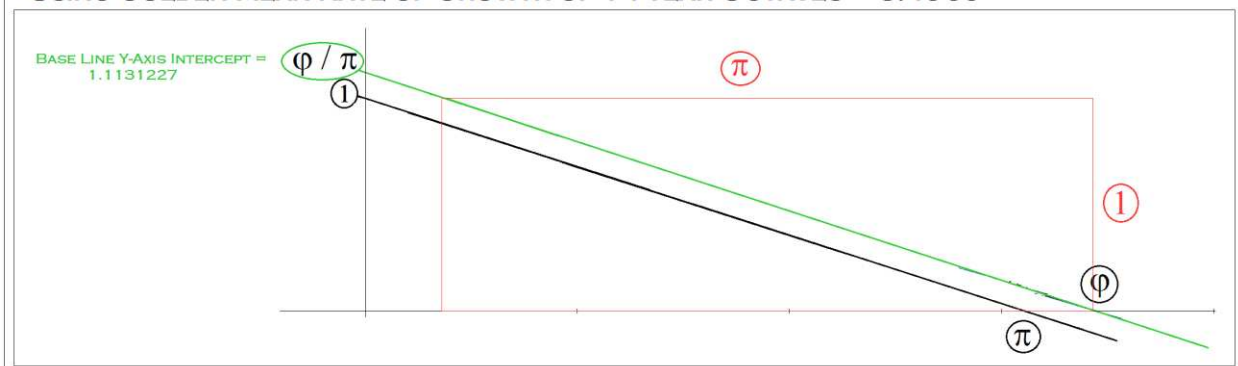
## 4.4 Knotek's Presentation

6.   We now review the econometrics presented in Knotek 2007.

Chart One (Knotek 2007) uses quarterly growth data which has been annualized. However quarterly employment data is not annualized.

DIAGRAM 2-2.
CHARTS ONE AND TWO OF "HOW USEFUL IS OKUN'S LAW?"
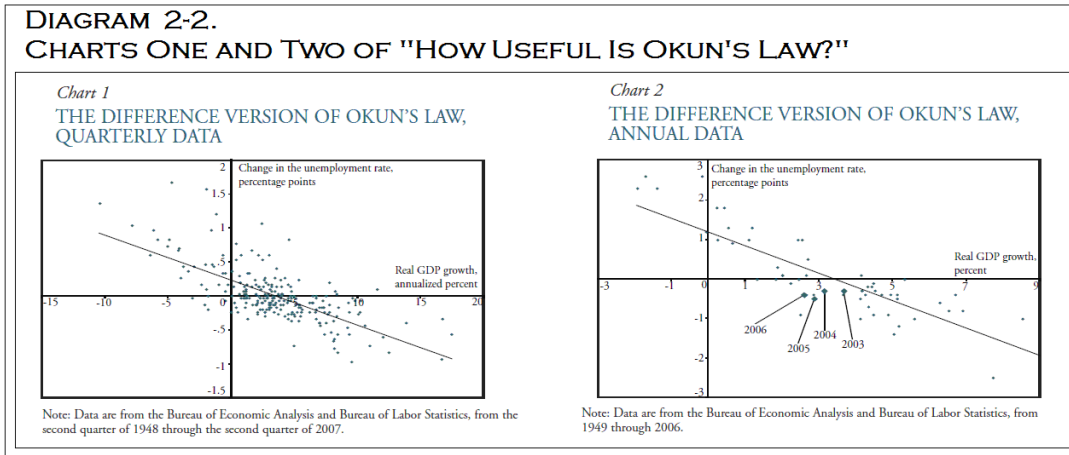
7.   We adjust the trend line for annualized quarterly data by multiplying quarterly employment data by four, thereby "annualizing" quarterly employment data. We thereby match annualized quarterly data on growth with "annualized" quarterly data on employment.

Throughout this essay the phrase "observed fully annualized quarterly trend line" will represent the trend line in Chart One wherein the data for quarterly employment data has been multiplied by four.


DIAGRAM 2-15.
MULTIPLYING QUARTERLY UNEMPLOYMENT RATE X 4
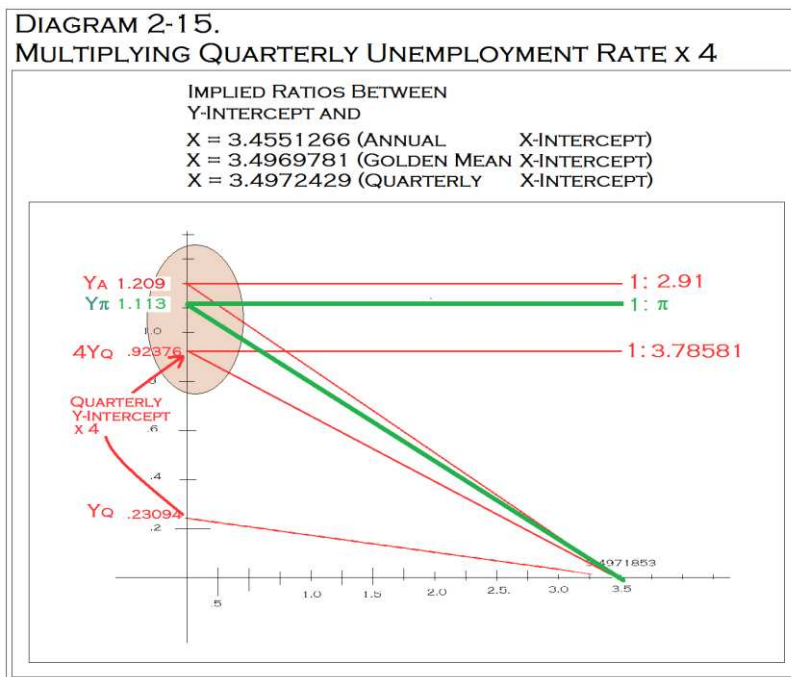
4.5   Relationship between Knotek 2007 and the "Chooser – Available Choice" Model

8.   Charts One and Two of Knotek's paper, below, provide the statistical trend lines of both quarterly and annual measurements of Okun's Law, as follows.

DIAGRAM 2-16.
CHARTS ONE AND TWO OF "HOW USEFUL IS OKUN'S LAW?"
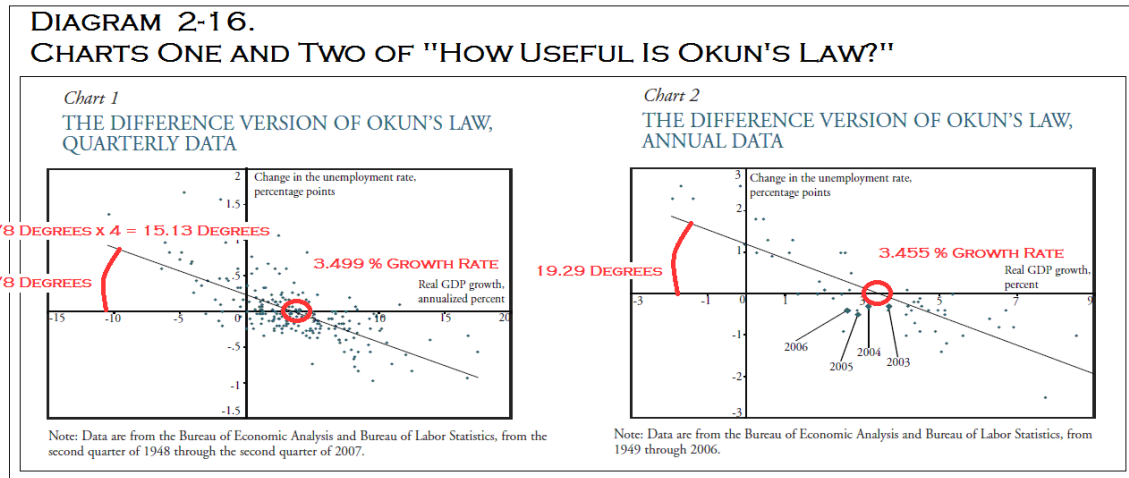
9.   Note that the slopes of the "observed annual" and "observed fully annualized quarterly" trend lines are 19.29 degrees and 15.136 degrees respectively.
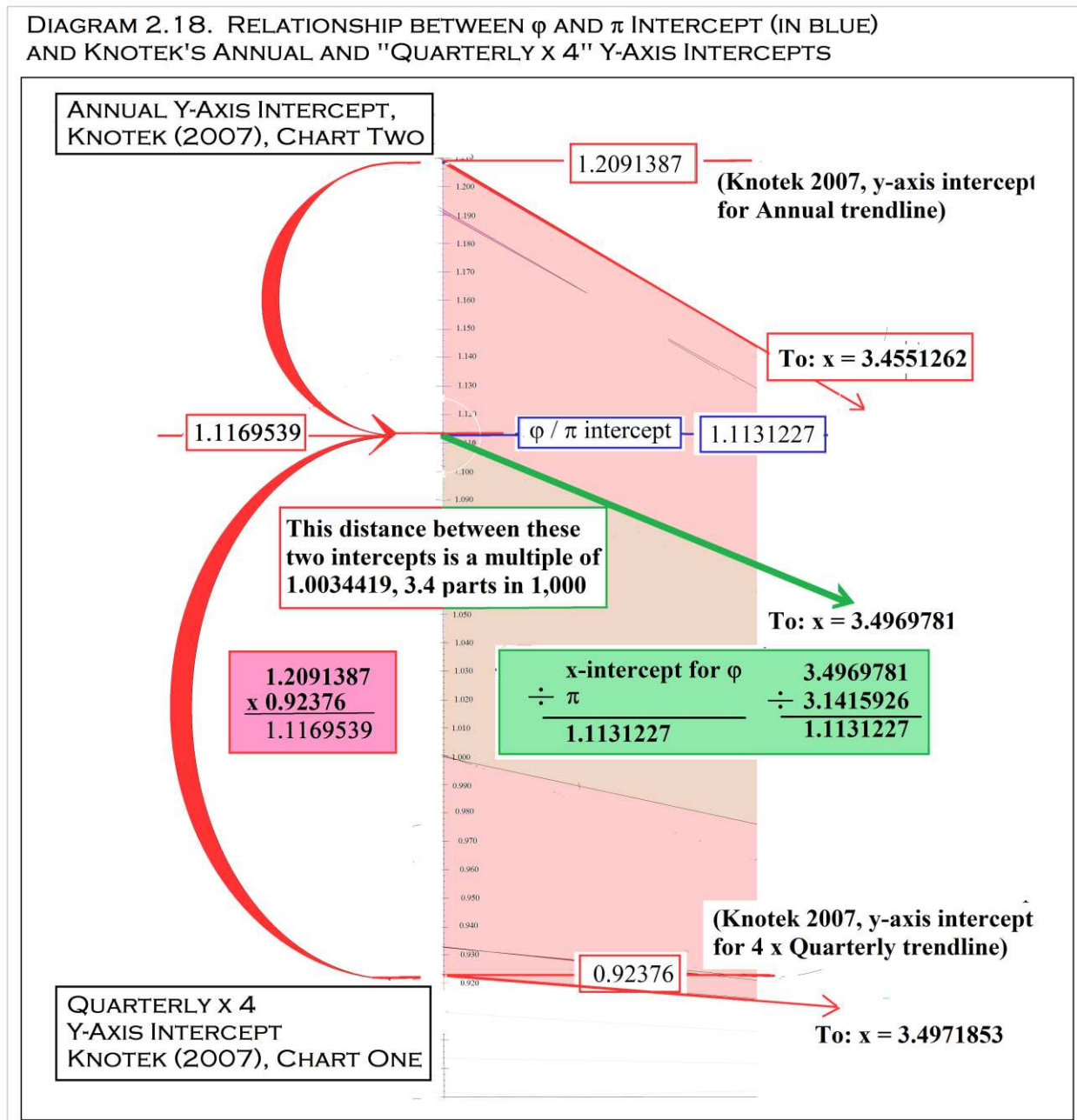
The "chooser- available choice" model makes clear that the relationship between the radius and 1/2 the circumference of a circle is an important trigonometric identity to consider in relation to economic growth. The area of rectangle, π x 1, figured through such an association is as follows, with a bisecting angle of 17.66 degrees.

DIAGRAM 2-17.
RELATIONSHIP OF π TO 1
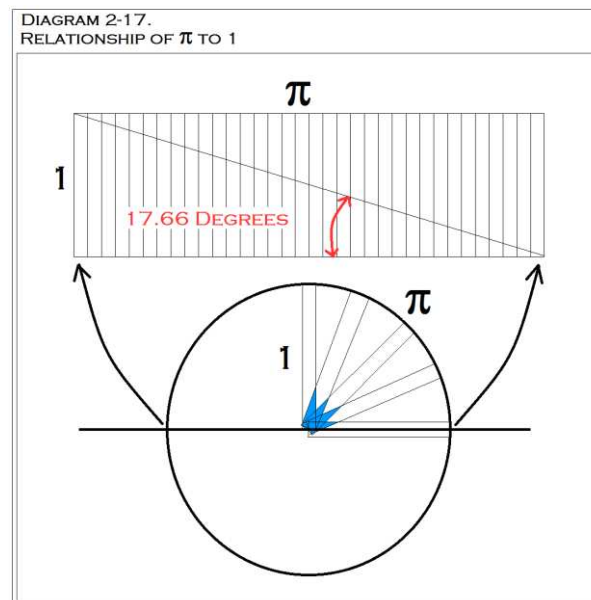
The slope of the angle bisecting the angles given in Charts One and Two is 17.213 degrees, less than half a degree from the slope of 17.66 degrees of the "chooser – available choice" model.

10.   The "Annual" y-intercept given in Knotek 2007 as 1.2091387.   The "4 x Quarterly" intercept is 0.92376. The multiple of these two intercepts is 1.1169539.

If the steady state rate given for the Golden Mean proportion (Essay Four, median average growth rate of 3.4969) is divided by π, the y-axis intercept is 1.1131227.   The extraordinary proximity of these two intercepts to one another – the "Annual" and "4 X Quarterly" intercept on the left in red and the φ/π intercept on the right in blue – is demonstrated in the chart below.

DIAGRAM 2.18. RELATIONSHIP BETWEEN φ AND π INTERCEPT (IN BLUE)
AND KNOTEK'S ANNUAL AND "QUARTERLY X 4" Y-AXIS INTERCEPTS

ANNUAL Y-AXIS INTERCEPT,
KNOTEK (2007), CHART TWO

1.2091387

(Knotek 2007, y-axis intercept
for Annual trendline)

To: x = 3.4551262

1.1169539 φ/π intercept   1.1131227

This distance between these
two intercepts is a multiple of
1.0034419, 3.4 parts in 1,000

To: x = 3.4969781

1.2091387		x-intercept for φ	3.4969781
x 0.92376		$\div\ \pi$	$\div$ 3.1415926
1.1169539		1.1131227	1.1131227

(Knotek 2007, y-axis intercept
for 4 x Quarterly trendline)

0.92376

QUARTERLY X 4
Y-AXIS INTERCEPT
KNOTEK (2007), CHART ONE

To: x = 3.4971853

In short at that place on Charts One and Two where change in the growth rate is zero (the y-axis), the "Annual" and "4 x Quarterly" y-axis intercepts are multiplicative inverses of one another as set about the line designated in green in Diagram 2-14.

11. Let us now turn to the x-intercept for annual data. The annual x intercept is 3.4551266. The x-intercept for the Golden Mean is 3.4969781.

As to this discrepancy, it must be pointed out that the data used in Knotek 2007 goes back only through 1947. This data misses all GNP values which are available for the period 1869 through 1946, a period of 78 years. During the early part of this period very large values were stated in GNP ratios. (See Essay Three) Thus the annual data used by Knotek must be slightly less than that generated by our analysis herein because it does not include the same set of figures for GNP, but only a subset..

Interestingly the x-axis intercept given for Annualized Quarterly Data is virtually the same as that anticipated by the Golden Mean analysis herein. This may be because the number of observations for quarterly values is four times that of observations for annual values. These values are 3.4969 (Golden Mean) vs. 3.4971 ("Rounded" Annualized Quarterly) and 3.4999 (Updated, Unrounded Annualized Quarterly) [10]


DIAGRAM 2-19.
X-AXIS INTERCEPTS

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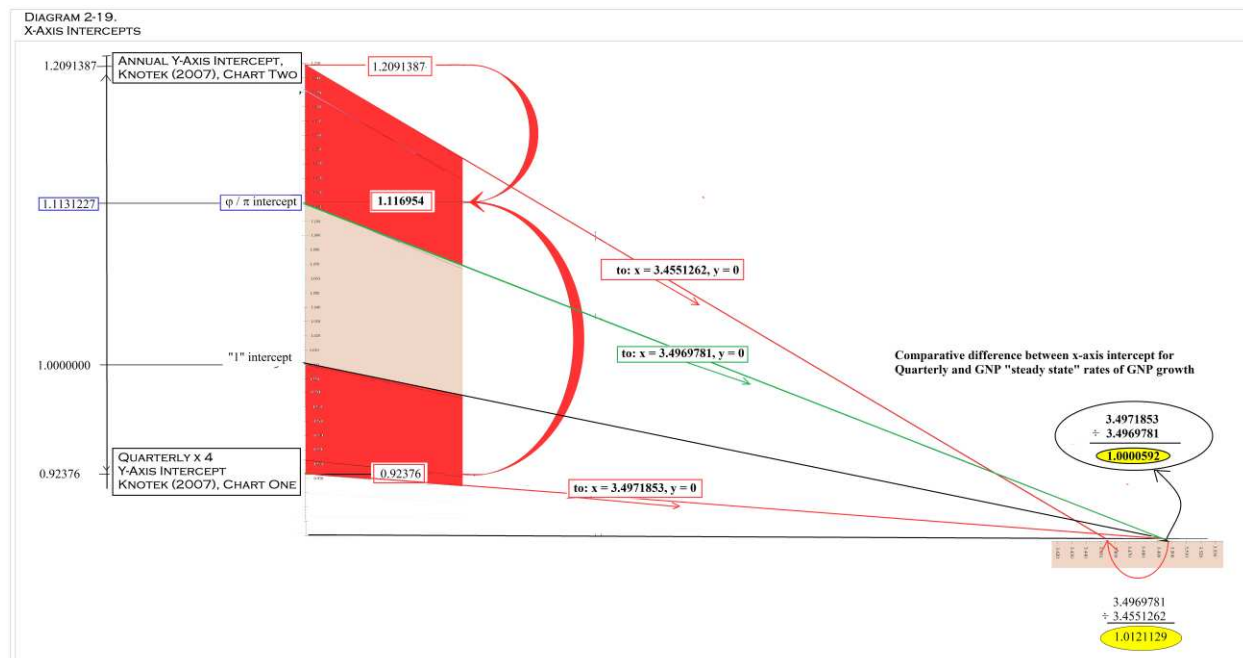
[10] See also Essay Four. This last value of 3.4999 is quite close to the Median Average figured for the 14-year spread of 3.4995226.

CONCLUSION

The mathematic regularity of Okun's Law over time, and the correlations noted, are possible only if the relationship between change in the rate of employment and the growth of GNP are connected by the geometry of a half-circle via the steady ratio of 1 : π as described herein.

DIAGRAM 2-20.
PI : 1 RELATIONSHIP BETWEEN GNP GROWTH AND CHANGE IN THE RATE OF EMPLOYMENT
USING GOLDEN MEAN RATE OF GROWTH OF 14-YEAR OCTAVES = 3.4969
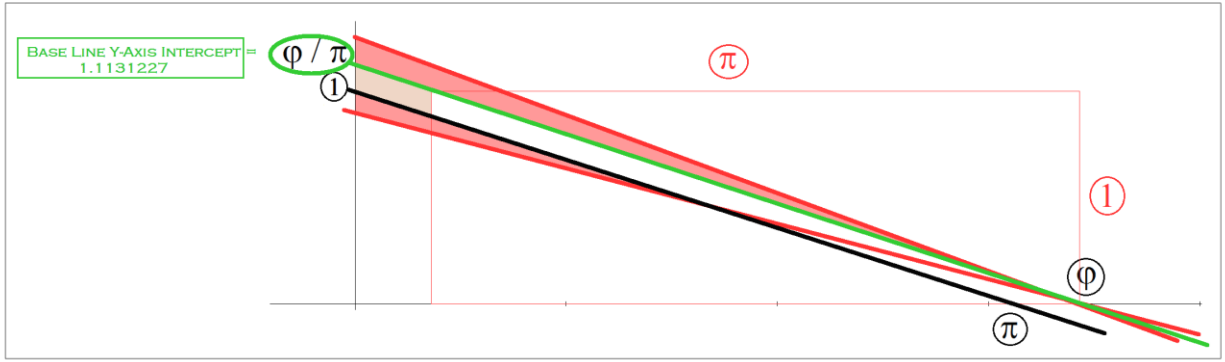
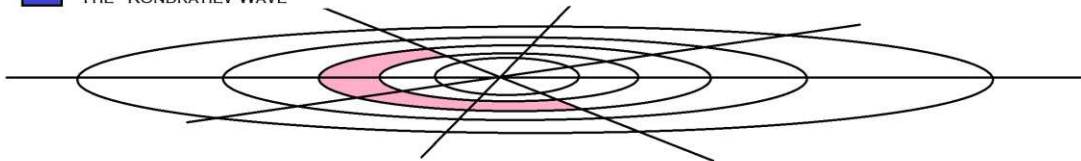# Empirical Foundations of the Economic and Social History of the United States

Essay 3:
Toward an "Economic Octave"

INTRODUCTION: THE GNP RATIO,
THE "AGGREGATE" OF ANNUAL REAL GNP

In this essay we will discuss the third of the rings of this model, a demonstration of the economic "octave" of U.S. real GNP as manifested at 14-year intervals.

DIAGRAM 3-1.
BASIC PLAN.

1. MICRO-ECONOMIC CHOICE
X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
OKUN'S LAW STATES A π : 1 RATIO AS TO
HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
THE "KONDRATIEV WAVE"

We suggest in this essay that, just as the "Chooser-Available Choice" model is a mathematic "wave" which is in sync with the human mind, and just as Okun's Law represents that mind in aggregate over the course of a single year, so may the growth of U.S. real GNP be considered a wave which is in sync with the annual growth of human development.

Introduction 1.1: Intervals in Music as an Analogy in Economics

It is well known that Pythagoras first developed the modal system of Western harmony upon noticing that a vibrating string, divided exactly in half, produced a pleasant, melodious sound, whereas even a slight alteration from the division of the string into perfect halves produced dissonant, unpleasant discording sounds. From this a spectrum emerged – the eight tones of the ancient modal scale made famous by Pythagoras, and the thirteen halftones of the modern chromatic scale made famous by J. S. Bach, each based upon the mathematic division of a vibrating string. Upon this modal system the entire spectrum of Western musical harmony has emerged.

DIAGRAM 3-2.
INTERVALS OF THE CHROMATIC MUSICAL SCALE
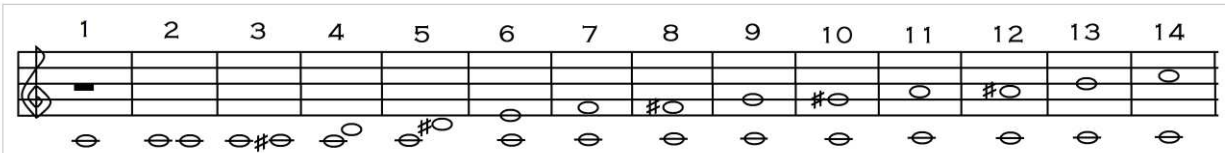
Of importance for this paper, between solitary note Middle C and its octave there exist 14 separate "chords" or "intervals" which may be sounded.[11]

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[11]   Notice that I do not state that there exist 14 notes in the chromatic scale (there are 13, including both Middle C and its higher octave). Nor do I state that there are 14 half-tones (there are twelve). Rather I state that two instruments, playing each possibility of harmony between them and including both the solo note of one instrument played while its partner remains at rest, as well as the unison of both instruments on the same note, combine to create fourteen "intervals."

Introduction 1.2: Intervals in Human Development

A similar span of fourteen distinct years of human growth may be explored as human development passes through childhood and reaches adolescence.

To connect this musical scale to the development of the human being, let us propose that a child is born at 1:00 a.m., January 1, 2000. On this day the child experiences his first New Year's Day. From this point we may chart the chronologic sequence of his second, third, fourth, etc. New Year's Day, as follows.

DIAGRAM 3-3.
PHYSICAL CHRONOLOGY OF EVENTS.
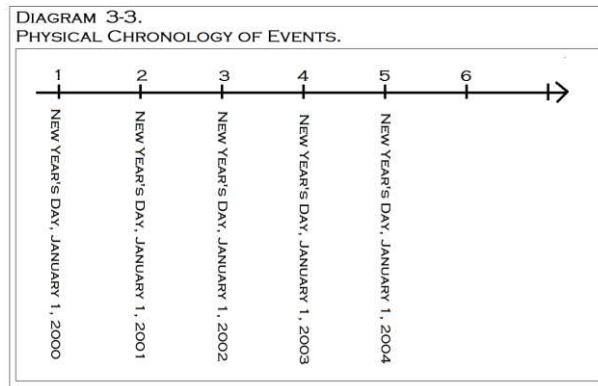
This counting of dates is to be distinguished from the counting of the child's birthdays. To experience one's first birthday party, or second, or third, etc. is a celebration of developmental growth. Each year claimed by a new birthday arrives with the celebration of a new biologic level of accomplishment. This concept of biologic development may be placed along the y-axis as follows.

DIAGRAM 3-4.
PHYSICAL CHRONOLOGY (X-AXIS)
VS.
BIOLOGIC DEVELOPMENTS (Y-AXIS)
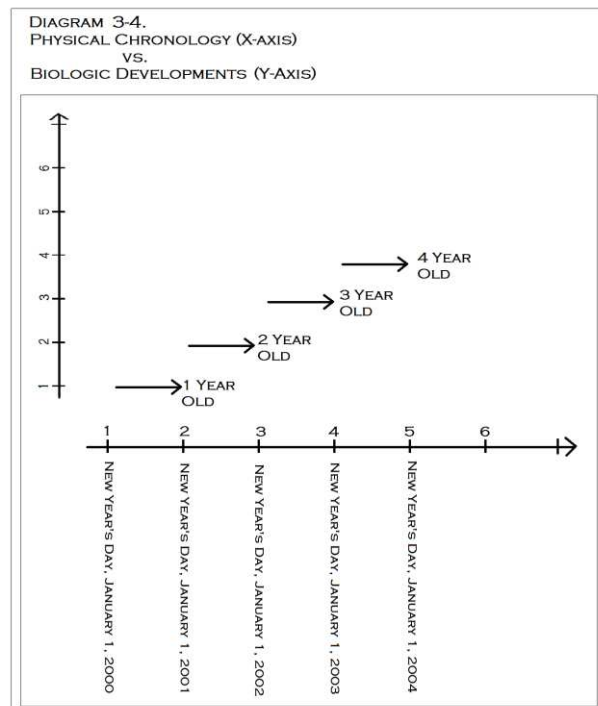
As demonstrated below, of the 15.6 million "regular secondary school students" in the United States in 2007-2008, 12.5 million (79.7%) were enrolled in school systems which ended primary school at eighth grade and began enrollment in secondary school at ninth grade. This break occurs generally at the age of 14. (total student population of these schools, including 9, 10, 11, 12 grade students in red lettering below).

		Student Population	School System[12]
1.	Total, all secondary schools (post-primary)	16,184,724	24,426
2.	Total, all regular secondary schools	15,680,507	19,264
3.	Grades 7 to 8 and 7 to 9	1,578,163	3,047
4.	Grades 7 to 12	927,888	3,278
5.	Grades 8 to 12	451,656	777
6.	Grades 9 to 12	12,500,341	15,179
7.	Grades 10 to 12	418,850	748
8.	Other spans ending with Grade 12	41,545	378
9.	Other grade spans	266,281	1,409

The en masse separation of primary and secondary education into two completely different school systems tracks the tremendous difference between the end of childhood (in aggregate at the age of 14) and the beginning of adolescence and onset of procreative capabilities (in aggregate at the age of 14). [13] Certainly the popularity of alternative systems to the 9-12 scheme, as measured by student enrollment, leaves little doubt that the preferred transfer date for students from primary to secondary education is at the age of 14. Other ages for transfer to secondary enrollment are less popular by ratios of 13:1, 27:1, 29:1, 46:1 and 300:1.

		Student enrollment	Comparative size to enrollment in 9-12 system	
4.	Grades 7 to 12	927,888	1:	13.47
5.	Grades 8 to 12	451,656	1:	27.67
6.	Grades 9 to 12	12,500,341	1:	1.00
7.	Grades 10 to 12	418,850	1:	29.84
8.	Other spans ending with Grade 12	41,545	1:	300.88
9.	Other grade spans	266,281	1:	46.94

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[12] Taken from the Digest of Education Statistics, Table 99, Public secondary schools, by grade span, average school size and state or jurisdiction: 2007-2008, National Center for Education Statistics; and Enrollment of public secondary schools, by state, 2007-2008, collected at the request of the authors from the NCES on Friday, June 10, 2011. Data Set Four and Five are at the conclusion of this paper.

[13] This approach may parallel studies emphasizing the role of learning in the structure of globalization. See e.g. Marchetti, C. (1980) and Devezas, T., et al. (2008:32) "The framework proposed by Devezas and Modelski opens the door to conceptualizing the emergence of world organization and, more recently of globalization, as a process of systemic learning, which leads in turn to the concept of a learning civilization."

Viewed in aggregate, the 14th year of life may be a fundamental biologic rhythm, one which lays through biologic fertility the economic basis for a 14-year spread in the higher social level of the Kondratiev Wave.

It is possible to find in these constantly recurring 14-year cycles a pattern of human development over time. In other words, there are "harmonies" within human productivity which – like the musical intervals above – may be calculated, studied and used.

ECONOMIC METHODOLOGY

1. Hypothesis

My hypothesis is that the 50-60 year Kondratiev Wave is in reality a wave form composed of a number of smaller well-defined parts. Possible wavelengths can be evaluated and distinguished from one another by examining the underlying ratios of real GNP in the United States over various "intervals of years" or "spreads of years" which make up the cycle itself.

2. Methods

The musical scale results in the comparison of notes to one another, giving birth to the idea of the musical concept of dissonance and harmony as found between the various musical intervals. Musical harmony and comparative dissonance may be modeled mathematically.

With the idea of a musical "interval" in mind, I place a consistent set of real GNP figures (1868 to present) in "GNP ratios," i.e. the quotient of one year's real GNP as divided by that of a former year. This method results in the discovery of an "octave" in the data when the numerator and denominator are separated by a period of 14 years. In other words, the notable lack of economic "dissonance" when an interval of 14 years is given as the "spread" of the ratio is surrounded by much greater levels of economic dissonance for ratios using 11, 12, 13, and 15, 16, and 17 years of separation in the ratio.

The shape of the economic "octave" is virtually identical to the musical "octave" as graphed mathematically

3. Data

These essays use figures for U.S. real GNP data published by the United States Government, as described and located in the Appendices.

4. Procedure: Examine Ratios of un-averaged U.S. real GNP

4.1.   The Musical Intervals of the Diatonic Scale

We begin with the observation that one way in which to understand the interaction of waves and their mathematic construction is through the generation of waves of sound in music. Using a musical analogy we may better understand the mathematic relationships between waves and their interaction.

When a musical scale is sounded it can be thought of (or realized) as a wave moving through the atmosphere in the form of a sound wave. The velocity of this pulse moving through the atmosphere is the same for all notes.[14] However the wavelength of that pulse is inversely proportional to the frequency of its peaks and troughs. The longer the wavelength, the less frequent the peaks and troughs of the wave; the shorter the wavelength, the more frequently occur its peaks and troughs. A higher frequency corresponds to a higher sounding note, or a higher pitch. A lower frequency corresponds to a lower sounding note and a lower pitch.

The relationship between (pairs of) notes are intervals. Collections of intervals can be thought of as a musical scale. As presented below the frequency of a particular note is given as "x". The frequencies of the other notes in the diatonic scale as based upon this note "x" are given as multiples of this first basic "root" note.

DIAGRAM 3-5.
MATHEMATIC RATIOS OF THE DIATONIC SCALE

The chief interval is the octave, an even division of a vibrating string into two parts, thereby doubling the frequency of the new higher pitched note as compared with the first note of lower pitch. The further division of the string into other mathematic subdivisions results in a number of differently pitched musical scales. The diatonic scale pictured above is among the most common.

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[14]   The speed of sound is the distance travelled during a unit of time by a <u>sound wave</u> propagating through an <u>elastic</u> medium. In dry <u>air</u> at 20 °C (68 °F), the speed of sound is 340 metres per second (1,115 ft/s). This is 1,236 kilometres per hour (768 mph), or about one kilometer in three seconds or approximately one mile in five seconds.

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4.2.   Ratios of GNP as Intervals of Economic Growth

As used in this paper, a "ratio of GNP" is a numeric fraction which takes as its numerator the real GNP of one year and takes as its denominator the real GNP of an earlier year. The comparison of a GNP ratio as created by "an interval of years" or "a spread" between economic figures represents the economic equivalent of a musical "interval" in the harmonic relationship between one note and a note distant from it in the musical scale. Music is the art of juxtaposition of these relationships; the intervals are not "all the same."

From the point of view of existing economic theories, no useful information should emerge from the interplay of different intervals of time as rates of U.S. real GNP are compared to one another. Neoclassical economics – and all other forms of economics – considers the physical passage of time as an irrelevant or at least an un-described / unknown mechanism and the relationships between economic quantities in time have no meaning beyond the numeric result obtained.

From the biologic standpoint however mathematic ratios of real GNP taken at different years represent the production of between 2.6 million to 311 million people over 235+ years (1777-present) as they live their lives in patterns associated with family, pride, livelihood, health, rigid social forms, moral expectations, criminal laws, civil relationships and a host of other necessary and indeed vital social interactions and expectations. These relationships are the generating substrate of all economic measurement.

For example let us consider two ratios of GNP, 1933/1928 and 1943/1938, each composed of an interval of but five years between numerator and denominator. In billions of dollars these are:

Years compared	GNP figures	#1 GNP ratio	Years compared	GNP figures	#2 GNP ratio
1933 1928	169.5 190.9	**0.887**	1943 1938	337.1 192.9	**1.747**

The first ratio, 0.887, a ratio less than one representing a decline in value over time, states in a single number the decline between the peak of the Roaring Twenties and the nadir of the Great Depression. The second ratio, 1.747, roughly double the preceding ratio, represents in a single number the explosion of production associated with the end of the Great Depression and the middle year of World War II. The entire sequence of numbers occupies but 15 years, 1928 through 1943.

Considered biologically, the measurement of the difference between "myself now" and "myself next year" is a significantly different biologic measurement than the measurement of "myself now" as against "myself 20 years hence." Considered biologically, the relationship of one year's GNP to the next year's GNP is actually a measurement of life at one point as measured against life at a point separated by some specified number of years.

As figures for real GNP are put into ratios against one another, we have the beginning of a biologic approach to economics, something upon which a larger theory of economic bio-complexity might be proposed.

4.3.   An Evaluation of Multiple Spreadsheets of all GNP Ratios

We examined "ratios of U.S. real GNP" in order to determine whether such sub-cycles may be demonstrated empirically. As mentioned previously, a ratio of GNP is a numeric fraction which takes as its numerator the real GNP of one year and takes as its denominator the real GNP of an earlier year. The term "ratio" suggests a proportion between these two numbers which, no matter how large, over time governs the general existence of the numbers themselves.

A typical Excel spread sheet with this data is as follows[15]

The number of years between numerator and denominator – the "interval" between them – represents the passage of time. It is referred to herein as a "spread of years" or simply a "spread." In order to establish the possible period of the sub-cycle we took ratios of GNP at different spreads of years and placed these ratios in Excel spreadsheets based upon the number of years in the spread.

For every year of the spread we constructed a single row within a spreadsheet. Because the data set is finite, a tighter spread between years results in a larger number of columns, and a broader spread between years results in a reduced number of columns.

DIAGRAM 3.6.
SAMPLE SPREAD SHEET

12 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

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15   See Appendix for all spreadsheets used in this evaluation.

By way of example let us consider Column Four Row One of the 12 year spread. (See Diagram 1, Sample Spread Sheet.) This GNP ratio is 1916 / 1904, representing a spread of 12 years between the numerator and the denominator of the ratio. The US real GNP values for this fraction are 134.4 / 89.7 with a result of 1.49833. This ratio is placed in Column Four Row One in the 12-year spread spreadsheet.

The next ratio in the series, 1917 / 1905, or 135.2 / 96.3, gives the result of 1.40395. This is placed in Column Four Row Two of the 12-year spread spreadsheet.

This continues on for a period of 12 years, i.e. from 1916 through 1927. The final fraction in Column Four Row Twelve is 1927/1915, or 189.9 / 124.5, for a result of 1.5253. This result is placed in Column Four Row Twelve and the series continues on to the next column.

The next column, Column Five, begins in Row One with the ratio 1928 / 1916, for a ratio of 190.9 / 134.4 and a result of 1.42039. This is placed in Column Five Row One and the process continues. Notice that the numerator of the cell in Column Four Row One ("1916 = 134.4") becomes the denominator of the cell immediately to the right, Column Five Row One.

An Excel spread sheet may be generated for any given spread of years using "Data Base 2 – U.S. Real GNP" as its foundation.[16], [17]

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[16]   The data provided by the Federal Government commences with a series of GNP values for the nine year period of 1869-1877 of a single figure, i.e. 23.1. This is followed by an 11-year period of 1878-1888 of a single value, i.e. 42.4. We have extended this series back one year by giving the year 1868 the figure 23.1, thereby permitting the larger spreads to include data series dating back to 1868.

This has been helpful in that it allows the 14-year, 15-year, 16-year, 17-year and 18-year spreads to include both the most antique, as well as the most current data – through 2010 – in their spreadsheets. Given the significance of the 14-year spread as described in this paper, it has been important to use this 1868 value of 23.1 as the beginning point for each spreadsheet in an effort to provide uniformity in this approach.

[17]   The use of this spreadsheet is the direct progeny of the first spreadsheet used in the discovery of the Golden Mean as an operating mathematic structure in the economy of the United States. (see Albers and Albers, 2012.) The only columns considered in the evaluation of spreadsheets (plural) are those columns which are complete. Under this rule the final column of the 12-year spread spreadsheet presented here, 2002/1990 through 2010/1998, would not be counted in any evaluation of spreadsheets. In this way a consistency between "spreadsheets" qua spreadsheets is obtained which would be impossible under any other measurement.

On the other hand this rule has the effect of eliminating from consideration between the spreadsheets themselves a number of years of data, depending upon the common year with which one begins the creation of each of the spreadsheets, the number of years in the data set, the spreads used to create the various spreadsheets to be compared and the final date of the data set which is used.

An alternative method to these difficulties is presented at the end of this essay which permits all data in the set to be considered, and which permits the evaluation of very broad and very narrow "spreads" between data. A "fingerprint" is not generated by this method however (see 4.2.6). Both methods appear to be legitimate in that they both discover the "octave" of the economy of the United States at 14 years, although the specific method used varies slightly.

For every Row and for every Column in every spread sheet there exists a High Ratio and a Low Ratio. For example, in the Columns and Rows mentioned previously regarding the 12-year spread, we have the following:

12-year Spread,	High		
Row One	1880/1868	= 42.4/23.1	= 1.8354978
Row Two	1881/1869	= 42.4/23.1	= 1.8354978
Row Twelve	1951/1939	= 383.4/209.4	= 1.8309455
Column Four	1927/1915	= 189.9/124.5	= 1.5253012
Column Five	1928/1916	= 190.9/134.3	= 1.4203869

12-year Spread,	Low		
Row One	1940/1928	= 227.2/190.9	= 1.1901519
Row Two	1941/1929	= 263.7/203.6	= 1.2951866
Row Twelve	1939/1927	= 209.4/189.9	= 1.1026856
Column Four	1921/1909	= 127.8/116.8	= 1.0941781
Column Five	1938/1926	= 192.9/190.0	= 1.0152632

We noticed that High Averages represent ratios which contrast a very dynamic year of growth in the numerator with a previous year of very slow or depressed growth in the denominator. Conversely Low Averages contrast a year of slow or depressed growth in the numerator with a previous year of growth in the denominator.

The full range of these contrasts is as follows as to the 12-year spread.

DIAGRAM 3.7.
ROW AND COLUMN DYNAMICS FOR 12-YEAR SPREAD
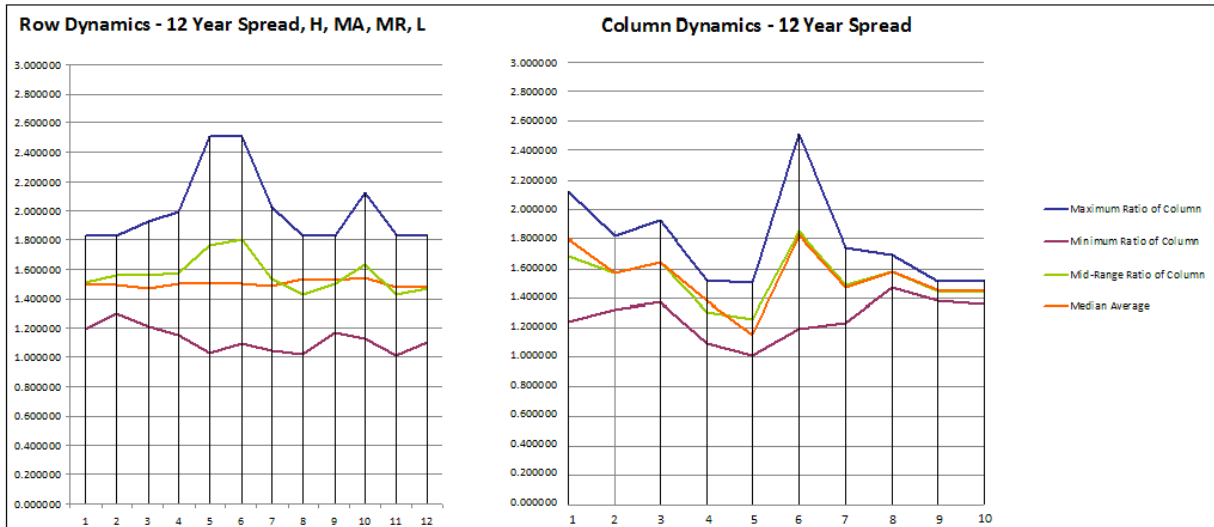
4.4.   Examination of Row Dynamics

From the above charts it becomes clear that these spread sheets are characterized by "Row Dynamics" and "Column Dynamics."   From these dynamics we have calculated four additional points within both the Rows and the Columns of all spreadsheets. These are:

The "Mid-Range." The mid-range is the mid-point lying between the high and low ratios in the sample, i.e. the average of the highest and lowest numbers in the set: "(H + L) / 2".

The "Average" or "Arithmetic Mean." The sample mean is the sum of all the observations divided by the number of observations.

The "Median." The median is that number for which half the data is larger than it, and half the data is smaller. It is also called the 50th percentile. If the data has an odd number of members, the median will be the number in the center of these members; if an even number of members, the median will be the mid-point between the two numbers closest to the center.

The "Median Average." The Median Average is the mid-point between the Median and the Average (Arithmetic Mean). It is figured as: "(Median + Average) / 2" and is the approximation used throughout this paper – in conjunction with the Midrange – as the best estimate of the dynamics within Rows and Columns.

The High, Midrange, Median Average and Low of Row Dynamics for each Excel spread sheet may now be compared. The following points are made as to this approach.

1)   In every Row there exists a Highest Average of the possible averages in the Row. This Highest Average represents the greatest margin of growth over decline for the time period of that spread for that Row. Conversely the Lowest Average represents the greatest depth of decline over growth for the time period of the spread for that Row.

2)   The Midrange between the Highest Average and the Lowest Average is simply the arithmetic division of the distance between these two. It lies half-way between them in any given row. The Midrange represents the arbitrary balance between these two extremes for that Row in any given spread of years. The Midrange is completely independent of, and unconnected to, the Median Average of the Row, other than the fact that they both include the Highest Average and the Lowest Average in their calculus.

3)   The Median Average states the accumulated "weight" of all the ratios in the row. It is unconnected to the Highest Average and the Lowest Average other than it includes both of them as a part of its calculation. It is completely independent of, and unconnected to, the Midrange value and does not take it directly into account in its calculus.

4)   When a particular spread of years generates Rows which contain Midrange values and the Median Average values which are quite close to one another, the spread has established a relationship between the most basic ratios of the economy which is balanced and uniform. In the context of our search herein, we use the term "harmonic" to indicate this balance.

5)   When a particular spread of years generates Rows which contain Midrange values and Median Average values which are at relatively great distances from one another, the spread has failed to establish a relationship between these basic ratios of the economy. By comparison to the other spreads, the particular spread in question is relatively unbalanced and not uniform. In the context of our search herein, we use the term "dissonant" to indicate this discord, turbulence or lack of harmony.[18]

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[18]   A physical analogy may be helpful to follow the logic at this point. Imagine that a mother and three children are at a playground and that a see-saw is available. A "harmonious" or "balanced" see-saw might be characterized by a simple fulcrum with a board balanced upon it. This would be analogous to the "midrange" (the center of the board) and the "median average" (the weight as distributed on the board) of the spread being very proximate to one another and thereby balanced without further effort or conflict.

The manufacturers of see-saws know, however, that the balance of children and their parents are frequently not evenly distributed. For this reason they place beneath the board a metal set of arches which may be used to adjust the length of the see-saw vis-à-vis the fulcrum in aid of the balance itself. An imbalanced see-saw is characterized by more weight at one end of the see saw than the other. In the analogy under these circumstances the center of the board (midrange of the spread) and the weight imposed upon the board (the median average of the spread) are far apart and a form of imbalance or "dissonance" must result.
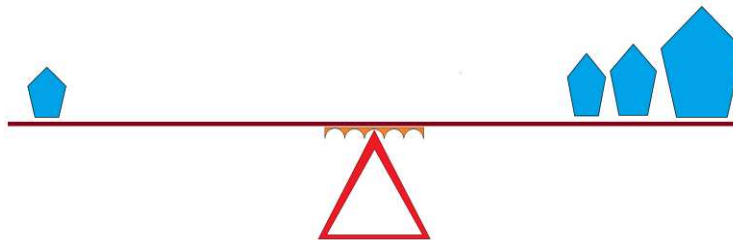
A balance may be restored by the addition of weight on one end of the see-saw to bring the balanced weight back, or by the shifting of the board itself from the center point within the metal arches to a point "off-center." This displacement of the fulcrum beneath the board is equal to the imbalance of weight above the board. In this essay we seek to measure the extent of this displacement as applied systematically to economics.

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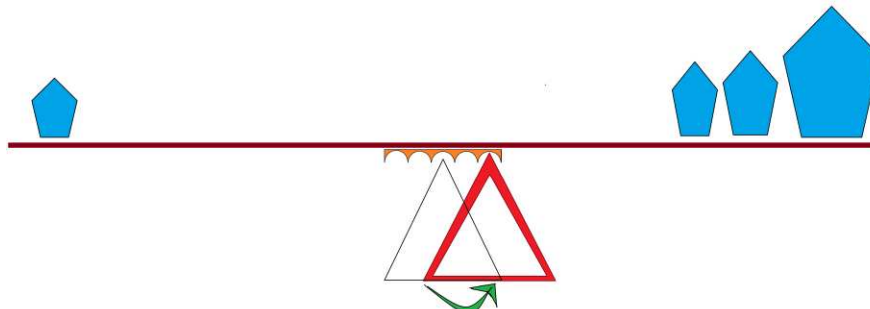
6)   The implication is that when a given spread of years generates Midrange and Median Average values which are proximate to one another and therefore "harmonious" or "balanced," some underlying pattern or overriding logic may be at work to create this harmony as opposed to a random and disconnected set of processes and their resulting discordant and dissonant variables.

4.5.   "Midrange Minus Median Average": ### An Evaluation of Differing Levels of Dissonance

In order to examine these relationships more carefully and across all spreadsheets, the following program was constructed.

Diagram 1-12, left side, presents the Row Dynamics for the 12-year spread shown in Diagram 1-11. The x-axis indicates the row of the spreadsheet under consideration. The y-axis represents the figure presented by that row as its High, Low, Midrange or Median Average ratio.
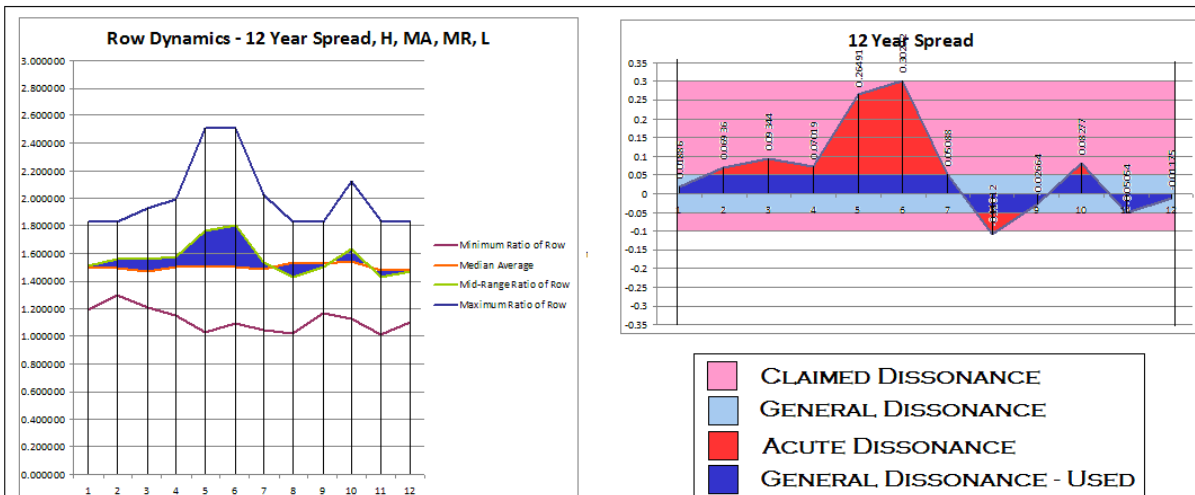
Diagram 1-12, right side, presents the graph of the

x-axis =   Row of the Spread
y-axis =   Midrange minus Median Average

When the Median Average is greater than the Midrange, the score is negative; when the Median Average is less than the Midrange, the score is positive. The number along the x-axis again indicates the row of the spread sheet under consideration. The number along the y-axis represents an amount of difference between Midrange and Median Average as found in that row.

The effort to compare systematically the common characteristics of different spreads led us to invent four new terms. Referring to Diagram 1-12 above these are:

"General Dissonance." The pale blue area running as a ribbon from left to right represents the notion of a "General Dissonance," i.e. an arbitrary, acceptable distance between Median-Average and Midpoint. When a row possesses a Midrange and a Median Average which are in close proximity to one another, the distance between them will be found within the space designated by pale blue, "General Dissonance." After reviewing all spreads of years, this number has been set at +/- 0.05 in as much as it appears applicable to all spreads of years as general field of activity.

"Used General Dissonance." The amount of dark blue is termed "Used General Dissonance," i.e. that portion of "General Dissonance" which is actually used by the given row in stating the distance between the Midrange and the Median Average, either as a positive or negative amount surrounding y = 0.

"Acute Dissonance." The portion in red represents an "Acute Dissonance." When the distance between Midrange and Median Average falls outside the arbitrarily stated "General Dissonance" the excess is given in red shading. If the distance between the Midrange and the Median Average of a row is great, the "Acute Dissonance" so stated will be signified by large areas of red shading. Lesser amounts of "Acute Dissonance" generate less red shading.

"Claimed Dissonance." The pink portion running as a ribbon from left to right is "Claimed Dissonance," i.e. that volume of spread between the high point of "Acute Dissonance" and the low point of "Acute Dissonance." This is the range of values necessary to accommodate the entire spectrum of variation between these two extreme points.

We then compared all spreads of years, from the 7-year spread to the 18-year spread using the "Midrange Minus Median Average" formula. The data used in this formula is as follows.

4.6. The "Fingerprint" of Growth Rates

An important difficulty arises in this regard as each spreadsheet is composed of varying numbers of columns and rows. Consequently the frequency of repetition varies. The 18-year spread is 2.571 longer in duration than is the 7-year spread. This means that – taken to infinity – the 7-year spread may be anticipated to have 2.571 as many columns as the 18-year spread. Conversely, because the number of rows is always finite, the 18-year spread has approximately 2.5 as many rows as the 7-year spread.

In the chart below the number of years in the spread is equalized by stretching the horizontal frame so that all spreads between a 7-year and an 18-year spread take up the same total horizontal space. This balances large spreads (large number of rows, relatively few columns) with the smaller spreads (small number of rows, large number of columns).

DIAGRAM 3.9. "MIDRANGE MINUS MEDIAN AVERAGE" 7-YEAR SPREAD THROUGH 18-YEAR SPREAD
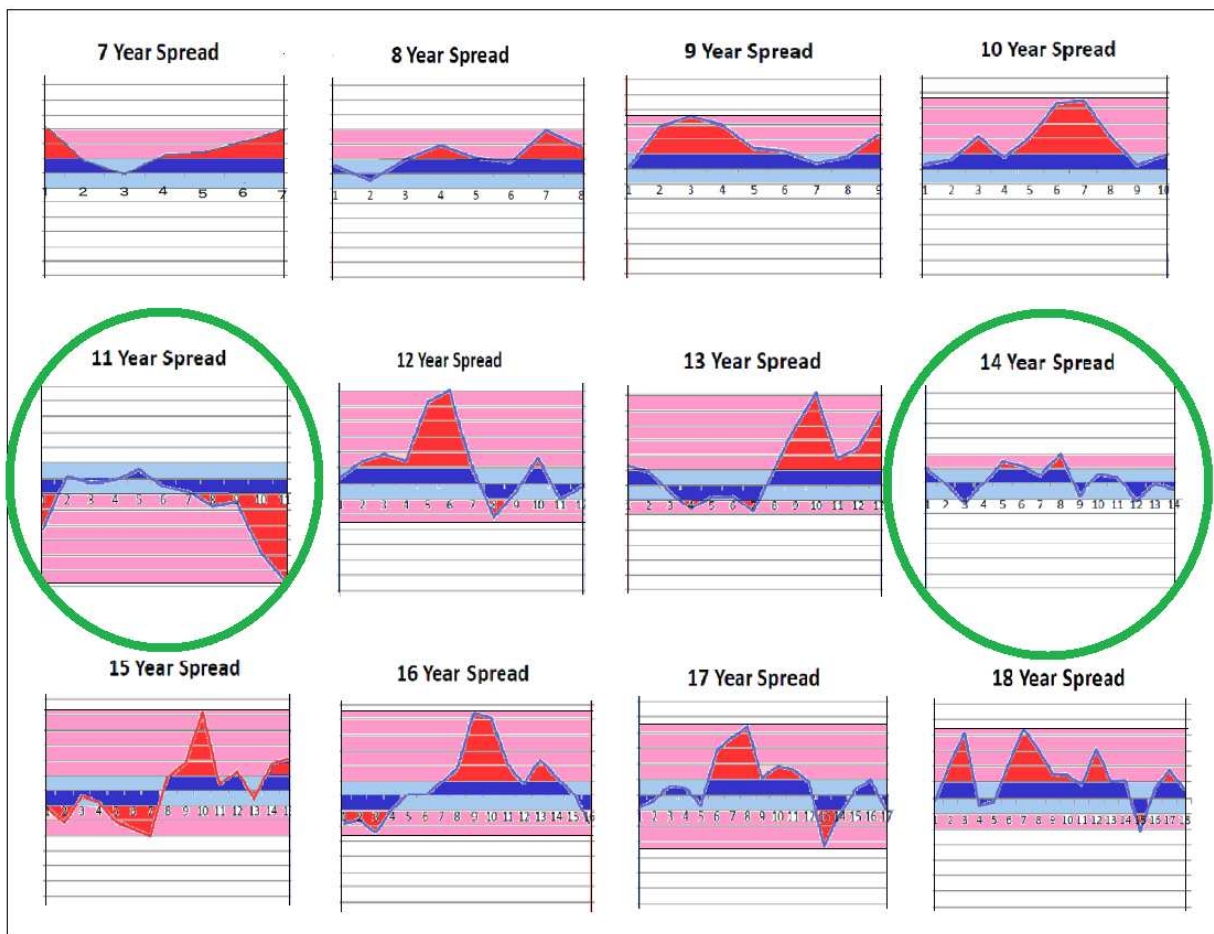
One may notice above that some spreads have distinctly lower profiles as to claimed dissonance than the other spreads. In addition the pattern of peaks and troughs created by this method provides a distinct "fingerprint" for each growth rate, irrespective of the growth rate

itself, as generated by this method for separate spreads of years. Note, in particular, the low profile of claimed and acute dissonance in the 14-year spread. Note also the sudden change to an entirely negative set of values with large levels of claimed dissonance found in the 11-year spread.[19]

4.7.   Systematic Description of Claimed, Acute and Used General Dissonance

We examined this finding in more detail by comparing the numbers generated by these different spreads and associating them with one another in a more systematic way.

Each value given as the sum or difference for equation "Midrange Minus Median Average" may be divided into two parts, i.e. positive and negative values. These parts are further sub-divided by those values for this number which fall close to the $y = 0$ axis and inside the range of +/- 0.05. This range is referred to as "General Dissonance." Values which fall outside this range are referred to as "Acute Dissonance."

"Claimed Dissonance" locates the High and the Low extremes of the "Midrange Minus Median Average" for a given Row. Once we locate the point at which the Midrange most exceeds the Median Average (High), and the point at which the Midrange is most exceeded by the Median Average (Low), we may draw the y-axis distance between these two extremes (column 13). This is then taken as the boundary of a pink ribbon denoting "Claimed Dissonance" against the y-axis for the entire spread.

"Claimed Dissonance" is a measurement of the extent to which any given spread of years generates turbulence and discord between the Midrange and the Median Average. Like harmonies with discord between them, a high value for Claimed Dissonance indicates that the GNP ratio in question would not function well as a fundamental building block for an economic system, whereas low values for Claimed Dissonance provide the underlying balance necessary.

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[19]   These two spreads of years have been found to have a remarkable connection to the Golden Mean in two different ways. The 56-year cycle which is developed from the 14-year spread (Essays 4 and 5) clearly generates ratios within the GNP of the United States which indicate that the Golden Mean is a constant operating force upon the development of the United States. On the other hand, the 11 year spread, as seen here, is characterized by a very negative relationship within its fingerprint, a feature which is completely unknown to the other spreads.

If one considers the 11–year spread in the context of a 56-year cycle (see Essay Five) one notices that at 55 years the 11-year spread has gone through five repetitions, while the 14 year spread has gone through almost four. The result is a pentagon shape in the economic data (See Essay 5) which is dramatically connected to the Golden Mean by way of the geometry of a pentagon.
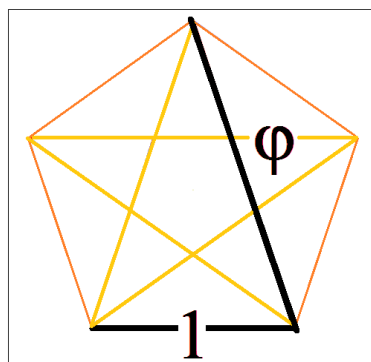
"The Expansion – Contraction Fraction"

All of these figures fit into the broader scheme of our effort to compare spreadsheets. Toward this end we have developed "the expansion – contraction fraction," i.e. that fraction which serves as a stretching or shrinking device to accomplish numerically for spreadsheets what stretching and shrinking the horizontal frame of graphs accomplished in Diagram 3.

By way of example, in order to make the distance for "Claimed Dissonance" for the seven year spread equal that of the "Claimed Dissonance" for the 18-year spread, it must expand 2.571 times. If we used the fraction 18/7 we would create this "expansion – contraction fraction" and thereby "stretch" the data for the seven year spread accordingly.

Such a fraction may be used to equalize all figures for all spreadsheets. For example, an "Acute Dissonance" at the 7-year spread sheet exists within a pattern of time which repeats itself 10 times in a 70 year span. An "Acute Dissonance" of an equivalent amount in an 18-year spreadsheet repeats under four times in the same 70 year span. The following fractions were used to multiply the spreadsheet data into numeric representations which would be equivalent.

7-year spread x	12/7	1.7142
8	12/8	1.5000
9	12/9	1.3333
10	12/10	1.2000
11	12/11	1.0909
12	12/12	1.0000
13	12/13	0.9230
14	12/14	0.8571
15	12/15	0.8000
16	12/16	0.7500
17	12/17	0.7058
18	12/18.	0.6666

4.8.   The Economic Octave

As demonstrated below, a remarkable and unexpected result occurs when a ratio of real GNP possesses a numerator and the denominator separated by 14 years. At this span of time, the level of Acute Dissonance is the least of all ratios (0.151795) and the level of Claimed Dissonance is second-to-least (2.39229).

In addition, the spreads of three years before (11, 12, 13) and after (15, 16, 17) the 14-year spread generate the greatest amount of Claimed Dissonance, more than double that of the 14-year spread. One may demonstrate this conclusively by:

(1) setting out each spread in direct proportion to the others,

(2) repeating the spread as necessary to demonstrate the continual repetition of the spread itself over a given period of time, and

(3) measuring the area of "Claimed Dissonance" taken up by each spread for the same period of years.

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In Diagram 3-10 each spread is set into the repetition necessary to complete a 36-year period of time. One can see the pattern of Claimed Dissonance building to the 13-year spread, then suddenly dropping at the 14-year spread, and then immediately returning to a very high level of Claimed Dissonance at the 15-year Spread.

DIAGRAM 3.10.
CLAIMED DISSONANCE OVER A 36-YEAR PERIOD, SPREADS COMPARED
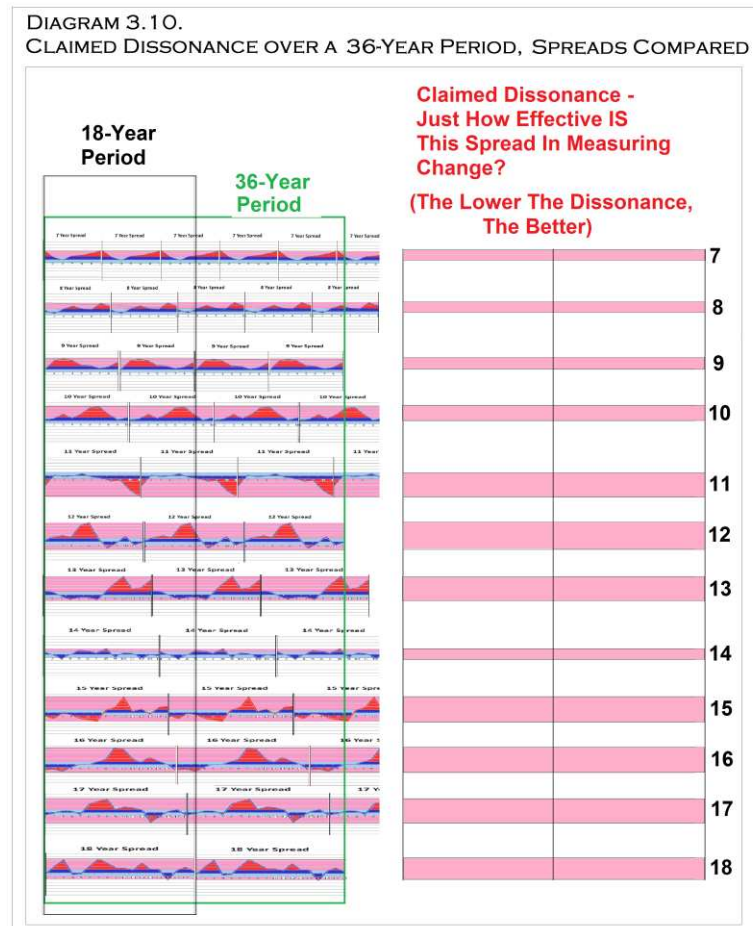
This "piling on" of Claimed Dissonance immediately before and after the 14-year spread is the origin of our selection of the term "dissonant," i.e. the sense that at the 14-year spread an almost acoustic "octave" is sounded against an underlying reality.

This is surrounded by discording, conflicting "harmonies" immediately preceding and following this spread which are out-of-harmony with this reality. [20]

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[20]   See e.g. William Sethares, Relating Tuning and Timbre, *Experimental Musical Instruments*: "To explain perceptions of musical intervals, Plomp and Levelt note that most traditional musical tones have a spectrum consisting of a root or fundamental frequency, and a series of sine wave partials that occur at integer multiples of the fundamental. Figure 2 depicts one such timbre. If this timbre is sounded at various intervals, the dissonance of the intervals can be calculated by adding up all of the dissonances between all pairs of partials. Carrying out this calculation for a range of intervals leads to the dissonance curve. For example, the dissonance curve formed by the timbre of figure 2 is shown below in figure 3.

In Diagram 3-11 the same effect is created with the numeric values of these ranges, as calculated with the "Expansion – Contraction Fraction" given above. The result is a rather vivid suggestion of the significance of an "octave" at the 14-year spread within a single set of data, i.e. the Real GNP of the United States, 1868 to present.

DIAGRAM 3.11.
"ACUTE DISSONANCE" AND "CLAIMED DISSONANCE" WITH MUSICAL OCTAVE

- RED	+ RED		Acute Dissonance	Claimed Dissonance
0	0.539222	7 Year	0.53922225	2.33166
0	0.328323	8 Year	0.32832275	2.39980
0	0.71348	9 Year	0.713480444	2.41405
0	0.702555	10 Year	0.702555	2.95466
-0.82882	0	11 Year	0.828815273	5.05443
-0.07077	0.680828	12 Year	0.751594667	5.77002
-0.07244	0.789312	13 Year	0.861753846	5.55129
-0.01764	0.134157	14 Year	0.151795	2.39229
-0.28313	0.338373	15 Year	0.6214992	5.77038
-0.16258	0.526958	16 Year	0.689539375	5.54327
-0.10785	0.394316	17 Year	0.502165176	5.40061
-0.04362	0.624485	18 Year	0.668103333	4.58002

DIAGRAM 3.12.
MUSICAL DISSONANCE AND HARMONY
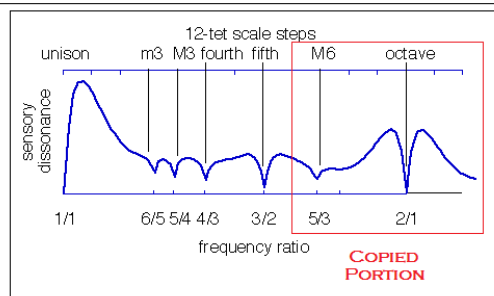
Observe that this curve contains major dips at many of the intervals of the 12 tone equal tempered scale. The most consonant interval is the unison, followed closely by the octave. Next is the fifth, followed by the fourth, the major third, the major sixth, and the minor third. These agree with standard musical usage and experience. Looking at the data more closely shows that the minima do not occur at exactly the scale steps of the 12 tone equal tempered scale. Rather, they occur at the "nearby" simple ratios 1:1, 2:1, 3:2, 4:3, 5:4, and 5:3 respectively, which are exactly the locations of notes in the "justly intoned" scales (see Wilkinson). Thus an argument based on tonal consonance is consistent with the use of just intonation (scales based on intervals with simple integer ratios), at least for harmonic timbres."

The suggestion is that, just as an octave is created by the equal division of a vibrating string into two harmonic parts, and just as a slight variation from this even division between the perfect center of the vibrating string results in intolerable out-of-tune sense of dis-harmony, so does the use of a 14-year interval between years when measuring GNP values result in great sympathy and proximity between Midrange and Median Average values for the entire economy, unlike every other spread of years. And also like the vibrating string, the most out-of-tune dissonance occurs immediately surrounding the perfect division of the string, while tapering off as one takes distances further from the center.

4.9.   A Measurement of Economic "Harmony"

If we consider the positive and the negative "General Dissonances" as a combined positive distance (absolute value), we can see that each spread of years comes to approximately the same amount of "General Dissonance" (dark blue columns below). However the 11 and 14 year spreads are quite different from the rest in that the first is almost entirely in the negative region, and the second is, by comparison to the others, relatively small.

DIAGRAM 3-13.
DIFFERENCES BETWEEN MIDPOINT AND MEDIAN AVERAGE
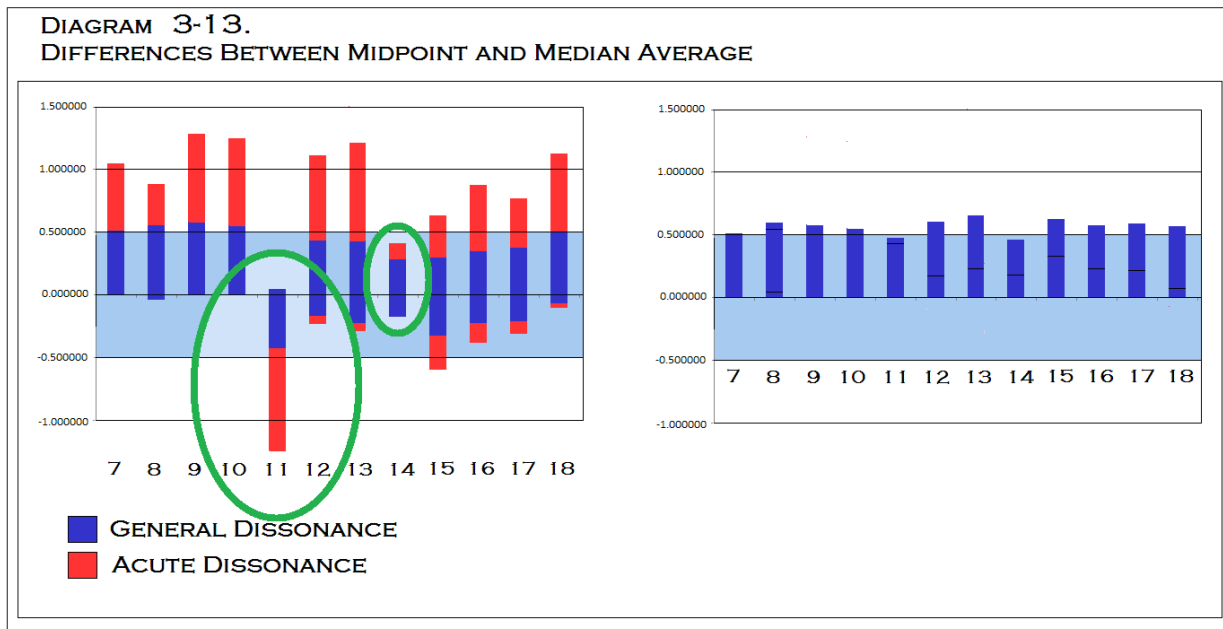
If we look to the amount of "Acute Dissonance" which goes above and beyond the general dissonance of these two points we have the following. The diagram on the left represents the amount of dissonance created by the spread (absolute value), and the diagram on the right represents the amount of harmony of the spread, i.e. the difference between the greatest level of dissonance (13 year spread) and the year in question.

DIAGRAM 3-14.
DIFFERENCES BETWEEN MIDPOINT AND MEDIAN AVERAGE

GENERAL DISSONANCE
ACUTE DISSONANCE
COMPARATIVE HARMONY
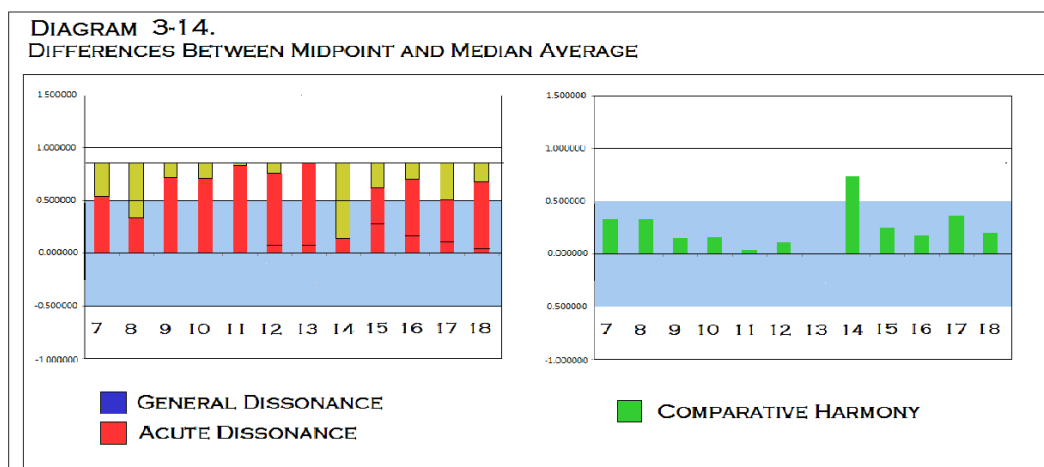
In both charts, the relative lack of dissonance in the 14 year spread, or conversely the striking harmony of the 14 year spread, is quite clear.

If we look at the combined total of these dissonances, we have an even stronger representation of that portion wherein harmony resides, as opposed to measurements of other spreads.

DIAGRAM 3-15.
DIFFERENCES BETWEEN MIDPOINT AND MEDIAN AVERAGE

GENERAL DISSONANCE
ACUTE DISSONANCE
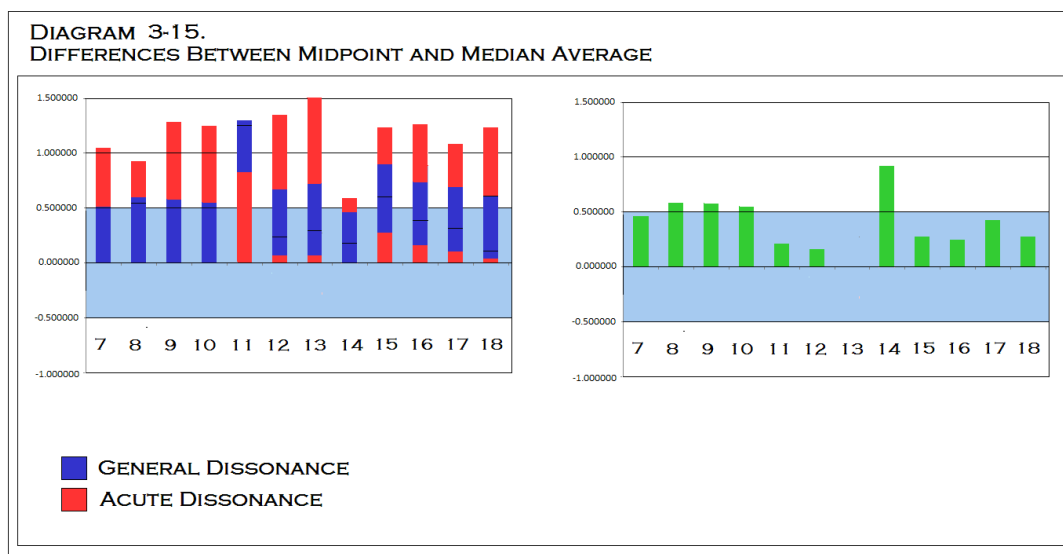
The charts above track the level of harmony/dissonance for twelve different spreads between years. It is quite clear that again the 14-year spread provides the most harmony and the least dissonance. Like a place on a ball bat where the "acoustics" of the bat provide a "sweet spot" where it is best to hit a baseball, the span of 14 years seems to bring with it a natural "sweet spot" in the harmonics of the economy.

DIAGRAM 3-16.
ABSOLUTE VALUE COMPARISONS
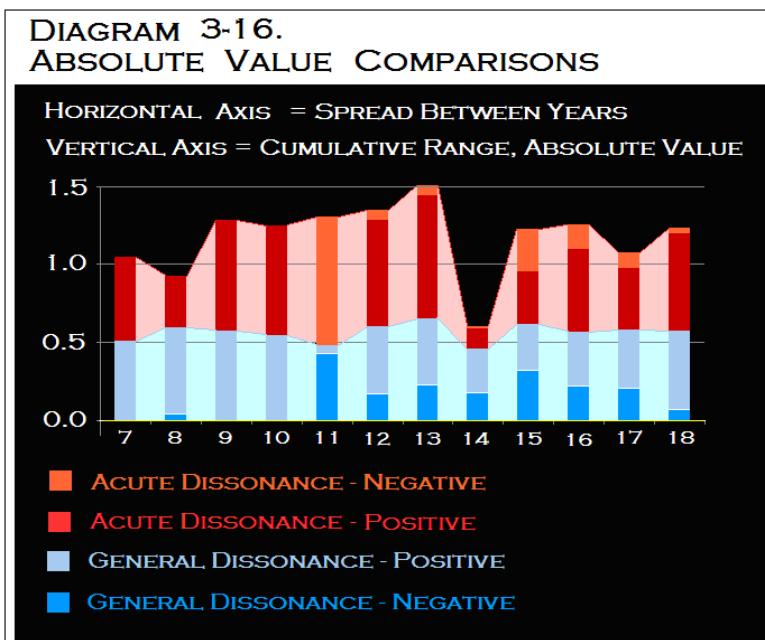
By simply flipping the comparison, we can see the preferred harmony brought on by a 14 year spread between years with very little acute dissonance.

DIAGRAM 3-17.
ABSOLUTE VALUE COMPARISONS
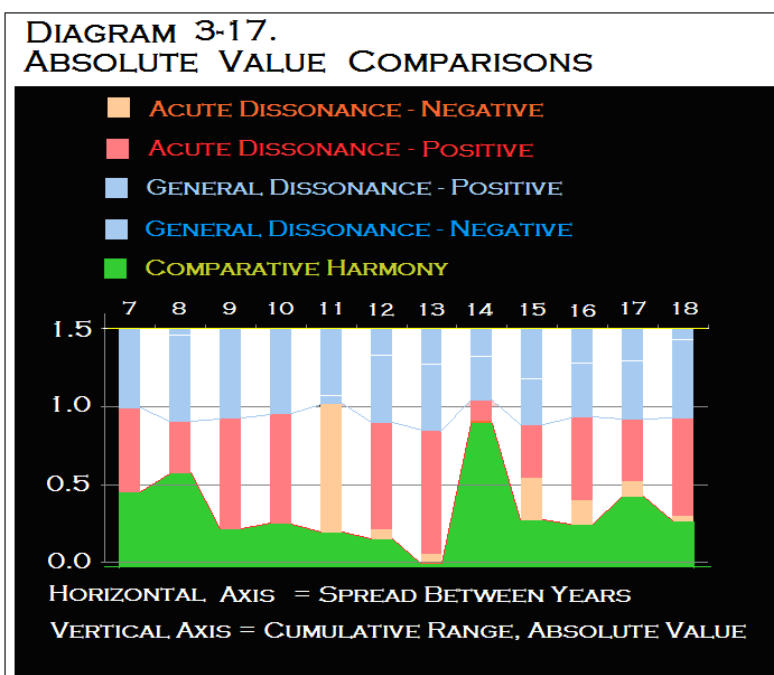
4.10. An Alternative Approach

As mentioned previously, the use of spreadsheets is problematic in several ways. First, the choice of a common date with which to begin all spreadsheets is an inherently arbitrary choice. Second in order to maintain the integrity of the "spreadsheet" approach, only columns which are complete within the spreadsheet have been used. The "fingerprint" thereby generated may be compared to other spreadsheets in a fashion which is consistent as to the method employed, i.e. "only completed columns will be considered." However the exclusion of uncompleted columns for analysis means that each spreadsheet excludes data which others may or may not use. Consequently the data being considered is not consistent and the results may be suspect.

If this analysis is run through a computer program whereby the spreads themselves are considered independently of the spread sheets which are generated, we have the following. This method does not permit a comparison of "fingerprints" per spread. Note that the use of the "expansion contraction fraction" in this example does not result in the same graph as previously as to "claimed dissonance." However an examination of the ranges without this alteration is quite similar in its finding of an octave without the expansion contraction fraction.

DIAGRAM 3-18.
COMPUTER GENERATED RATIO COMPARISONS

MUSICAL HARMONY AND DISSONANCE

RATIO COMPARISONS WITHOUT "EXPANSION CONTRACTION FRACTION"

RATIO COMPARISONS WITH "EXPANSION CONTRACTION FRACTION"

MUSICAL INTERVALS
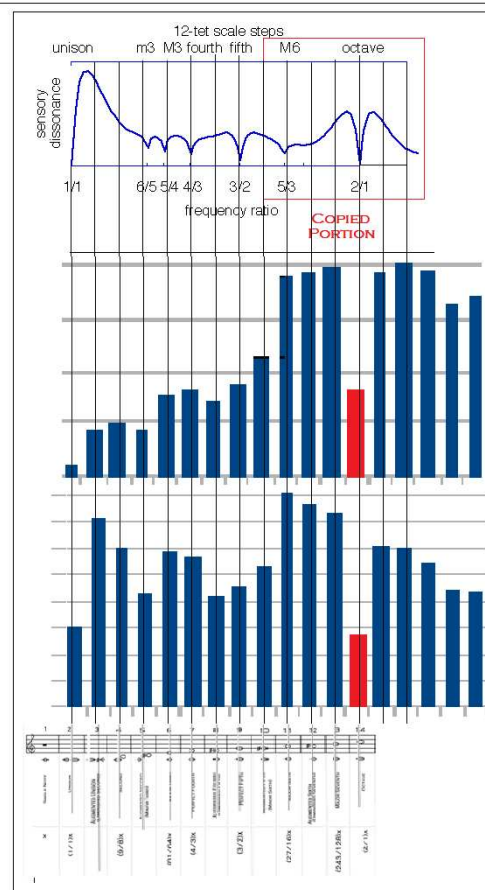
Using the computer program we are able to generate spreads of years with all available data in a consistent fashion. Although there are no "fingerprints" of different spreads to compare using this method, we are nevertheless enabled to see the same "octave" in the analysis generated.

This dissonance graphs are virtually identical.

And the extension of this method into multiple years demonstrates that the 14-year period appears to be of significance for at least two additional periods of 14 years.

Moreover we have in this method the ability to consider other spreads as well, for example, the fingerprint of the 11year spread was entirely negative. If multiples of 11 years are considered we have the following. In the case of the 11, 22 and 33 years spreads a significant jump in dissonance is brought on, one which is perhaps consistent with the one-off aspect of the multiple 55 years spread.

DIAGRAM 3-21.
11-YEAR SPREAD IN COMPUTER - GENERATED DISSONANCE GRAPHS
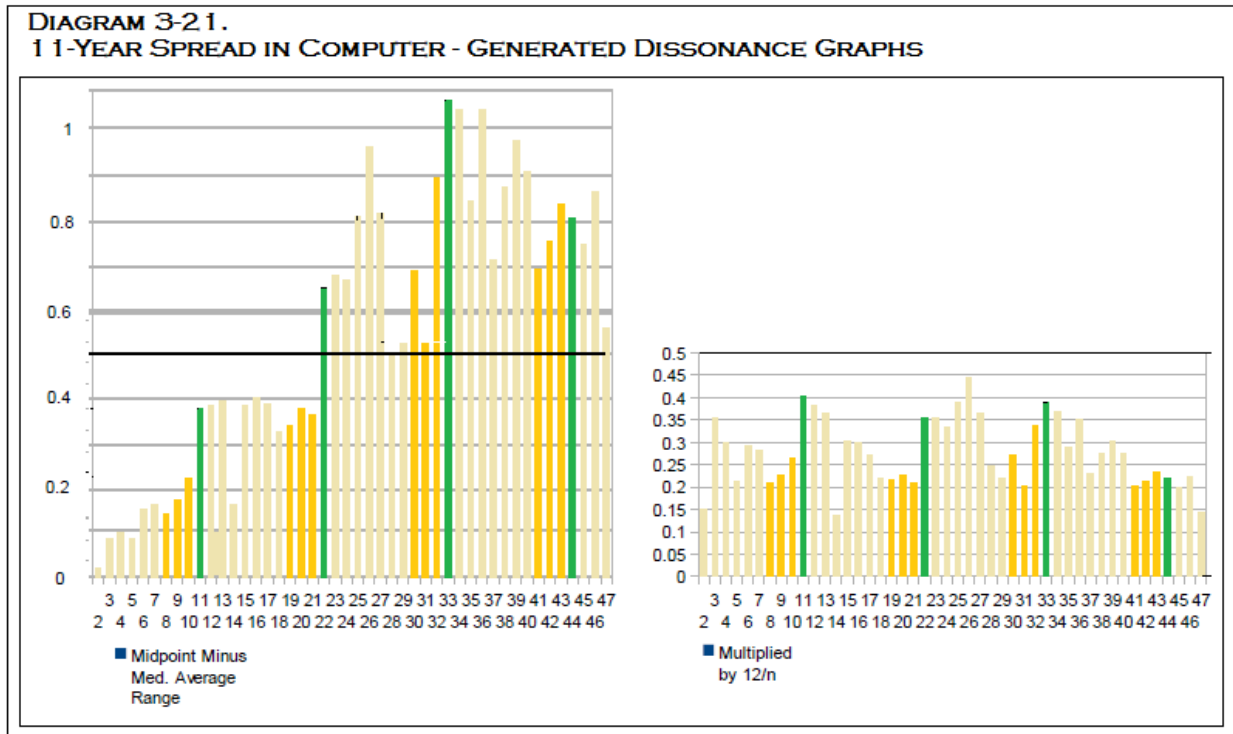
4.11. What accounts for the relatively small dissonance of the 14-year spread?

If we place all of the row and column dynamic charts next to each other, we have the following. This chart clearly shows that a rhythm exists in the economy such that at the 14-year spread the highest maximum ratio and the deepest minimum ratio balance each other with such perfection that the resulting midranges and median averages cancel each other out leaving very little dissonance. In addition, the least maximum ratio and the least minimum ratio again balance each other out.

In each of the other spreads the peaks and troughs do not align against one another or cancel out.

For example, the 12 year spread aligns the least minimum ratio with the greatest maximum ratio, resulting in significant dissonance.

Conversely, the 15 year, 16 year and 17 year spreads present a highest maximum ratio which is clearly "out of sync" or "out of phase" with the deepest minimum ratio.

Consequently it is the discovery of a rhythm or a phase within the economy of the United States which accounts for this octave, an empirical discovery of importance to these essays.

DIAGRAM 22.A.
ROW AND COLUMN DYNAMICS COMPARED
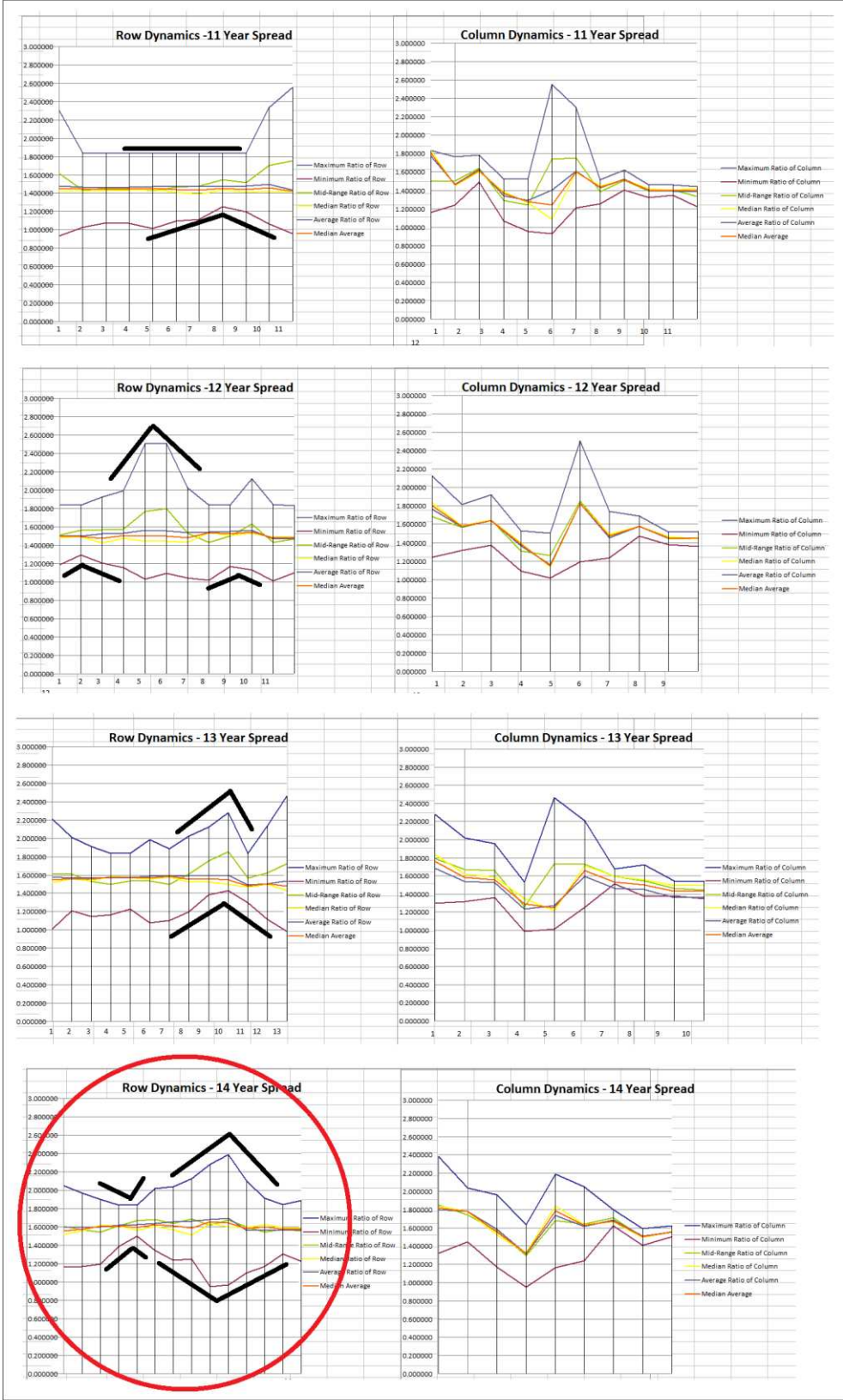
DIAGRAM 22.B.
ROW AND COLUMN DYNAMICS COMPARED

CONCLUSION

In this paper I have suggested that significant evidence supports the proposition that the economy of the United States may be organized according to "octaves" of economic growth in connection with a 14-year spread between years. One possible basis underlying the 14-year period may be that this is the period of time necessary for human development to turn the individual citizen from an infant to a reproducing adult, a period which is indicated by the break which occurs in four fifths of American lives, i.e. the end of grade school and the beginning of secondary education.

It may be helpful to state specifically several points which may be taken from this essay.

1.   Just as bees are alive and contribute to the life of the larger hive, so must the hive have distinct similarities in time span and structure as imposed upon it by the biology of the bees themselves.

2.   Just as human beings are subject to the requirements of their own biologic growth, so too is the economy of the United States the outgrowth of these human beings and their collective biologic forces, needs, limitations, etc.

3.   If the human beings which make up the economy are alive, then the economy itself is a living thing, something with its own rhythm and pace. In this essay we have proposed to seek out that rhythm and that pace.

4.   As the product of living human beings who mature and grow, give birth and die, at fixed stages of biologic development, the collective economic product created by these people, year after year, will demonstrate a "tree-ring" type of development over time.

5.   Human biology regulates the productive growth of the United States and draws it into accord with its own rhythm and pace. When the economic growth of the United States is excessive it is balanced by naturally occurring economic depression at a span of 14-years hence.

6.   An "octave" is sounded in economic data when measurements of GNP ratios are in accord with the underlying scheme of human development, i.e. when a congruent "pace" is located between biology of the small (individual human) and the biology of the large (American economic history); it "makes sense." Dissonance, chaos, wrong-answers and misunderstanding are sounded when measurements of economic data conflict with this scheme or when the scheme is ignored entirely.

7.   We find in these essays that harmony is noted in the data which is congruent with the biologic pace of human beings, when they are viewed in a fashion which is synchronous. We further note that disharmony is noted in the data when these two "paces" are not synchronous.

DIAGRAM 3-23.
ROW AND COLUMN DYNAMICS: 14-YEAR SPREAD
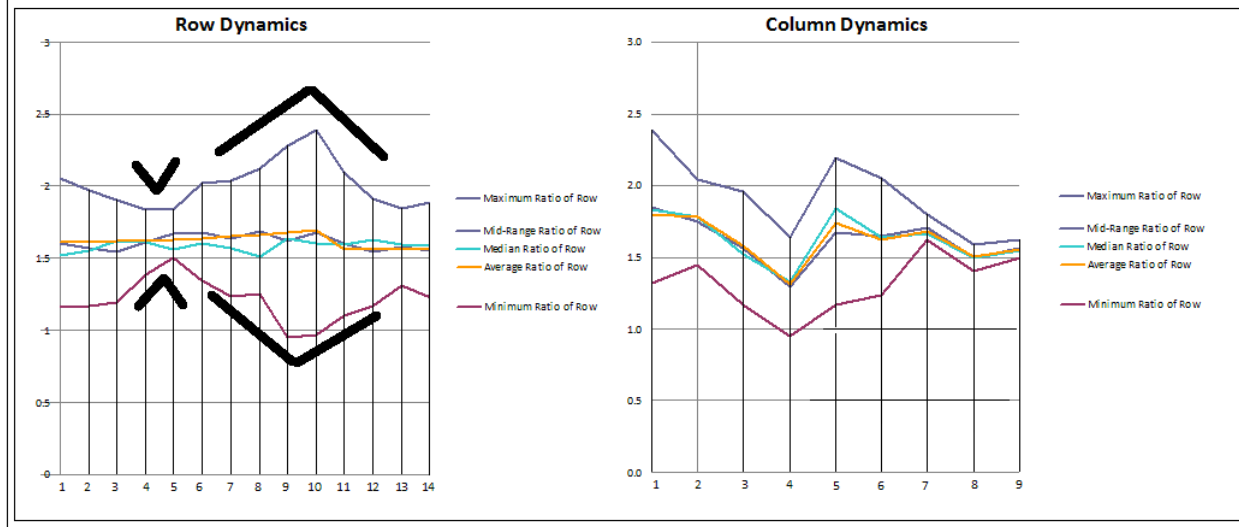
8.   When the measurement of the economy takes into account the underlying biology of the economy, a picture of American economy history may be developed which is in accord with both the biology of the individual member as well as the larger and encompassing biology of the economy. When the measurement of the economy ignores the underlying biology of the economy, nothing but dissonance and chaos results.

This completes the central, third unit circle described at the beginning of these essay.

To the further elaboration of this "octave" approach as displayed in the fourth and fifth circles we now turn. [21]

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[21]   The significance of a 14-year spread between years as a defining characteristic of the American economy finds at least tentative support in spectral analysis.   See e.g. Korotayev and Tsirel, 2007:10. Note that in both charts provided, the 14-year span is the most significant point of balance between the two charts, no matter how adjusted. (as taken from)

Empirical Foundations of the
Economic and Social History of the United States

Essay 4:
Toward a Harmonic Interpretation of
the Kondratiev Wave

INTRODUCTION: 28-YEAR AND 56-YEAR HARMONIC OCTAVES
BASED UPON THE 14-YEAR OCTAVE

We turn now to the fourth and fifth "octaves" presented at the beginning of these essays, i.e. the presence of a 28-year damping price wave as encompassed by a 56-year sine wave of political change, the "Kondratiev Wave."

DIAGRAM 4-1.
BASIC PLAN.

1. MICRO-ECONOMIC CHOICE
X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
OKUN'S LAW STATES A $\pi : 1$ RATIO AS TO
HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
THE "KONDRATIEV WAVE"

In his 1925 work *The Major Economic Cycles* Nikolai Kondratiev postulated a long-term wave running throughout the economic histories of various western countries of approximately 50 to 60 years. (Kondratiev, 1925) Kondratiev's plan analyzed European and even global patterns of economic development with the thesis that democratic capitalism may possess the tools necessary to save itself from the inevitable self-destruction predicted by Marx[22] and many

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[22] Kondratiev's work originated in the dangerous political context of prior socialist discoveries (Van Gelderen (1913), DeWolff (1924) and Kautsky (1917)) and communist theories (e.g. Marx, Lenin, Trotsky, Stalin) as to the evils of capitalism and the nature of its inevitable demise. (Goldstein, 1988:30-31) Kondratiev's suggestion that democratic capitalism might avoid such demise brought to him the censure of Stalin and death in a prison camp.

of his disciples.[23] Kondratiev's original plan (Korotayev & Tsirel, 2010) provided dates for "upswings," "transition periods" and "downswings"[24] which Joseph Schumpeter's 1939 work *Business Cycles* acknowledged as significant to economics. (Schumpeter, 1939)

The academic search for evidence of "long waves" running through the economic history of various nation-states is long standing (Goldstein, 1988) and a central topic of heterodox economics. Indeed a 52-53 year cycle has been described in very extensive detail underlying the global meltdown (Korotayev and Tsirel, 2010) and incorporated into the study of the current revolutionary movements in the Middle East. (Tausch, 2011) As one modern researcher of Kondratiev Waves has remarked, "Altogether I think the idea of 55 year cycles in the behavior of our society is one of the most penetrating and useful in organizing social and economic facts." (Marchetti, 1988:7) However the dating and even existence of these periods are controversial.[25]

Orthodox economics, on the other hand, maintains an enormous breadth of opinion as to whether considerations of political policy must, or must not, be a part of doctrinal discipline. This paper concludes that there is much in Kondratiev's work which is directly applicable to the economic history of the United States, but does so without reference to Marx, et al.

[23]   See Goldstein, 1988:30: "The Kondratieff-Trotsky long-wave debate … revolved around the question of the stability of capitalism. Do 'universal crises' threaten the survival of capitalism (as Trotsky thought), or are they only a phase of a more stable capitalist dynamic (as Kondratieff argued)? Kondratieff, like Kautsky, presented a picture of capitalism as more stable over the long term than either Trotsky or Lenin saw it. This parallel between Kondratieff's approach and that of the hated Kautsky may help to explain the very negative reception given to Kondratieff by his fellow Soviet Marxists."

[24]   See Goldstein 1988:7. "Long waves (or Kondratieff cycles) are defined by alternating economic phases – an expansion phase (for which I will often use the more convenient term *upswing*) and a stagnation phase (which I will often call the *downswing*). These economic phase periods are not uniform in length or quality. The transition point from an expansion phase to a stagnation phase is called a peak, and that from stagnation to expansion is a trough. The long wave, which repeats roughly every fifty years, is synchronous across national borders, indicating that the alternative phases are a systemic-level phenomenon."

These terms are used in Korotayev and Tsirel, 2010:1-2, et seq. but may hide a diversity of views in light of contrasting research. See e.g. Korotayev and Tsirel, 2010:1-6, Goldstein 1988. See also Coccia, M. 2010:730-738. "(T)here are different long-wave chronologies and certain timings of long waves are often better for some countries but not for the world as a whole... These different cycles "do not have a synchronized rhythm across countries..."

[25]   Orthodox economics rejects Kondratiev as a fallacy. See e.g. Rothbard, 1984. See also, e.g. Solomou, 1990:61. "(T)he evidence rejects the Kondratieff wave phasing of post-1850 economic growth. This conclusion is valid for all the national case studies examined here. Whether one takes the 1856-1913 or 1856-1973 a Kondratieff wave phasing can not be supported. … (O)bserved variations do not follow a Kondratieff wave pattern."

Mainstream analysis has focused rather on econometric measurements of other variables, i.e. the stochastic vs. deterministic effects governing the creation of real GNP itself. (See e.g. Nelson and Plosser, 1982) The distinction has been important for mainstream economics. (See e.g. Cochrane, 1988: "The distinction between a random walk … and a trend-stationary series … is extreme. Long-range forecasts of a random walk move one for one with shocks at each date, while long-range forecasts of a trend-stationary series do not change at all. There are two related ways to think about a series that lies between these two extremes.")

The significance of this inquiry however may be questionable. (Sowell, 1992: "The fact that postwar GNP series cannot distinguish between a time trend and a unit root model has important implications for theoretical models of the economy. Attention should be given to models where both the policy and theoretical implications of interest are not sensitive to the model of the trend. Ideally we would like a model which implies the same results if the trend is modeled as either a time trend or a unit

Studies in globalization have attempted to merge evolutionary theories[26] with fractal geometry, "emergence," the study of complexity and a host of other mechanisms in explication of Kondratiev Waves.[27] Calls for clarification have followed as to the methods, dates and theories surrounding "long waves."[28]

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root. Until such models are developed, further attention should be given to new statistical techniques which focus on discovering the long-run behavior of time series.")

[26] See e.g. Modelski, G. (2008:5) "(There are) two important implications of this evolutionary approach: first, there is reason to believe that an analysis drawing on evolutionary theory lends itself to modeling, simulation, and forecasting. Secondly, such an approach allows us to view globalization as an enterprise of the human species as a whole. … The emphasis is not on broad based accounts of the course of world affairs but, selectively, on processes that reshape the social (including economic, political, and cultural) organization of the human species; processes such as urbanization, economic growth, political reform and world organization, and the making of world opinion; and the innovations that animate these developments.

[27] As to requirements for a theory of causation for long waves, see Louca, F. (1999). "According to Kuznets, two conditions had to be met in order to establish the credibility of the Long Wave program: (for the "weak version of the recurrence requirement") one must prove (i) that the oscillations are general, and (ii) that there are either external factors or internal peculiarities within the economic system that create the recurrence (Kuznets, 1940:267). … A stronger version… means that the recurrence must conform to further definitions: a time variation in certain very precise limits and under well defined and stable causal relations – i.e. that the previous phase causes the next phase in the cycle or that sequence not only exists but also that causality can be exhaustively accounted for. This may be called the *strong version of the recurrence requirement*. … Rosenberg and Frischtak prolonged (the debate) by requiring the research programme on Long Waves to indicate a specific form of *causality, timing, recurrence* – precisely what was implied by Kuznets and Lange – and *economy-wide repercussions* of such fluctuations in order to be valid."

[28] See e.g. Devezas, T., Corredine, J. (2001) "… Complexity theory and nonlinearity are currently hot topics of interdisciplinary interest among the natural and social sciences, but still fall short of explaining the cyclic and evolutionary dynamics of society. … Although much has been published on K-waves, we must consider:

1 - a comprehensive and embracing theory of Kondratiev economic cycles still needs to be elaborated, while at least four major issues remain to be clarified:

i - why is there disregard among many contemporary economists and social scientists, some of them even stubbornly rejecting the existence of these waves?

ii - what is to be understood about the causality of the phenomenon - not just the mechanisms, but also the underlying causes?

iii- why the half-century beat? and since when? (only after, or even before the Industrial Revolution?, and more: where did the clock come from?).

iv- will there be more Kondratievs? Free-will or determinism? …

3 - The use of new tools of science mentioned above may lead us to a better understanding of the causality of the phenomenon. … But the question remains: is it something endogenous, inherent to social behavior of the human being? Or is there some kind of exogenous causality (external to human beings, even cosmic causes?). The understanding of all the above-mentioned aspects (not only in their economic character, but as a whole physical or social phenomenon), could contribute significantly to futures research, helping us trace the best trajectory through the coming millennium. ..."

ECONOMIC METHODOLOGY

1. Hypothesis

Our hypothesis is that the 50-60 year Kondratiev Wave is in reality a wave form composed of a number of smaller well-defined parts. 28-year and 56-year wavelengths are found in the price data collected for the United States as larger "octaves" of the 14-year octave demonstrated in Essay Three.

2. Methods

We graph prices in the United States, 1800 – 1993, and find therein evidence of a damping cosine wave with a period of 28 years. This wave is repeated twice as nested within a sine wave of longer-term relationships over 56-years, a period of time associated with the Kondratiev or "long" wave.

We review inflation figures and suggest that both "endogenous" and "exogenous" arguments for causality of the Kondratiev Wave are valid and that both endogenous and exogenous factors are at work in the timing of the wave. The wave itself is endogenous to the United States but the context in which this wave appears as a historic trend is closely related to the exogenous actions of other nation states.

Finally we evaluate the operation of these two longer waves in a single circuit, finding therein an increase in U.S. real GNP every 14 years of 1.618590, a figure 0.034% greater than "the Golden Mean," a famous mathematic constant of 1.618033…. This reference to the Golden Mean connects economics to Euclidean geometry and trigonometry. Using this constant as one governing the creation of the data itself we are able to calculate an expectation that the United States is controlled by a steady-state growth rate of between 3.4969% and 3.4995% per year on average.

3. Data

The price and production data collected in Data Sets 1 and 2 from Essay One are utilized in this Essay Two.

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4. Procedure

4.1. Price Patterns

Having established that a 14-year sub-period may be important in the evaluation of the economic history of the United States, we now examine the price indexes for the United States between 1800 and 1994. The figures from "Data Set 1 – Prices" (as taken from Essay Three) are stated below (1) in 7-year running averages (red line, top graph, semi-logarithmic scale), and (2) the change between a given year's seven-year average as divided by the average itself (blue line, bottom graph). The lower graph permits us to see the increasingly large inflationary price index values of later years (post-1966) as placed in a more consistent relationship with the preceding values of the series.
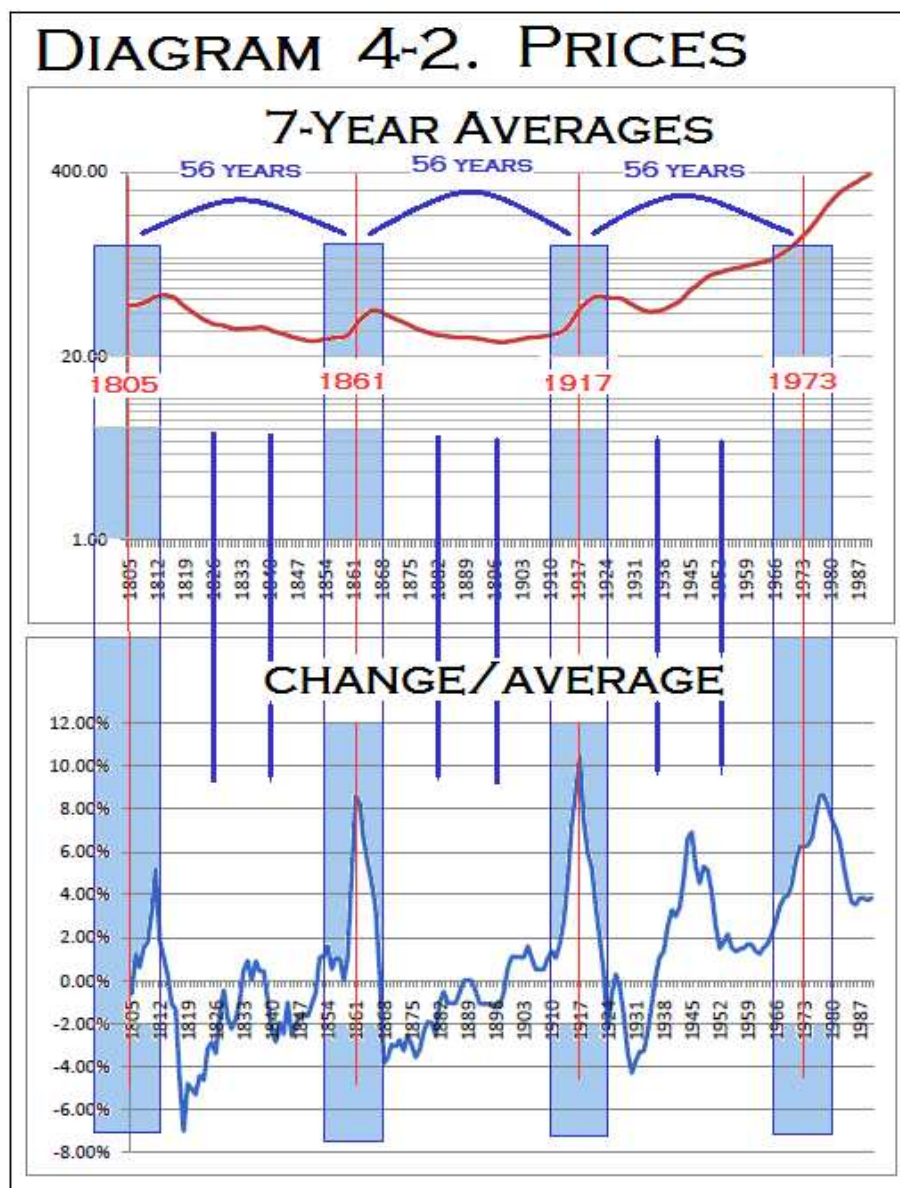
Note that the 56 year period (14 x 4 = 56) between peaks at 1861 through 1917 suggests the possibility that similar periods of time might connect other peak points of inflation. If a 14-year span (blue rectangles above) is drawn around the years 1805, 1861, 1917 and 1973 (each of which is separated by periods of 56 years), virtually all inflationary peaks are contained in a single model.

A damping wave, beginning with a peak in the blue-shaded areas, has been noticed three times in the course of American economic history in consideration of prices.

DIAGRAM 4-3.
PERIODS OF INFLATION
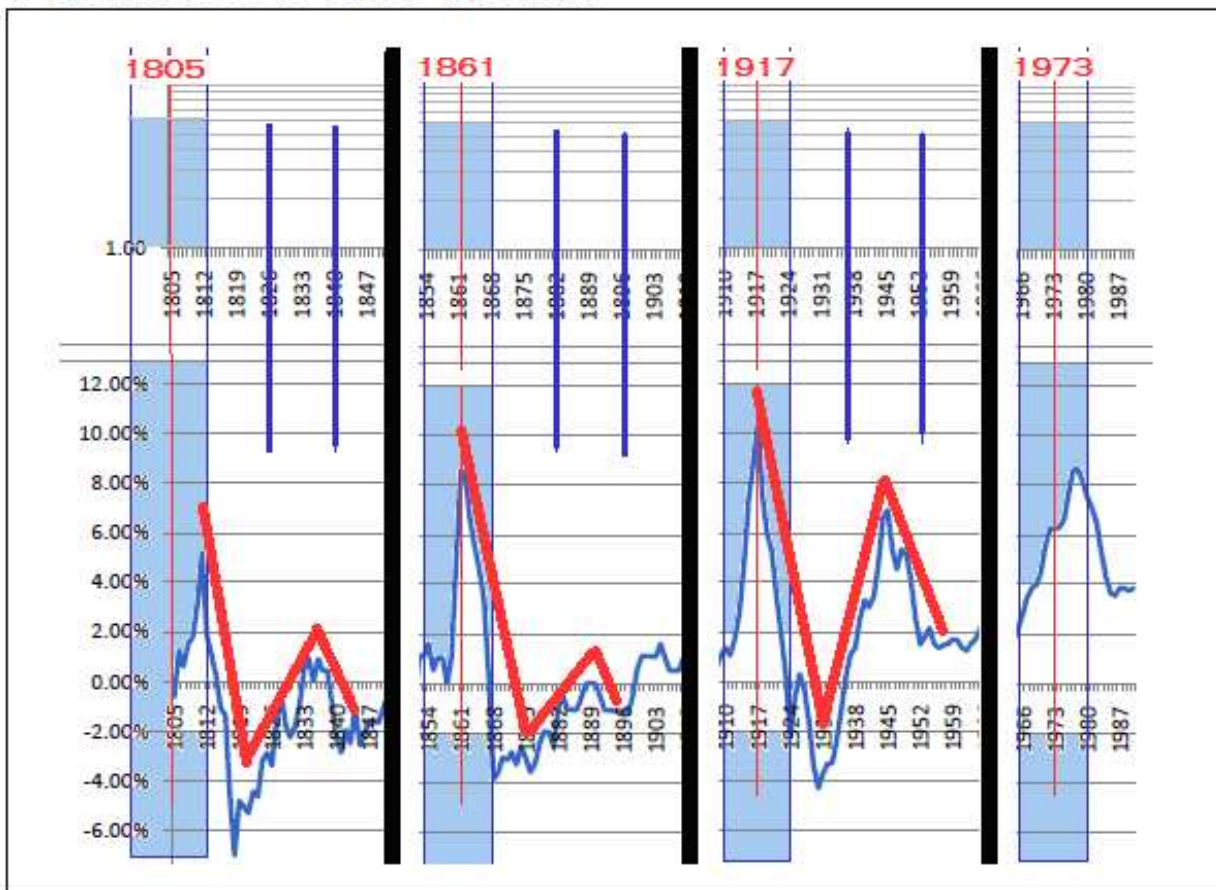
4.2. Models of Price Fluctuation

Regarding the diagram above, we may relate the foregoing chart of price fluctuations to US real GNP. If we divide a circle into 56-year rays, all things being equal, as the arrows of production move outward to meet the expectation of GNP per year (arrows of radii moving out from the center of the circle) this production should be met by uniform resistances (arrows moving toward the center of the circle) which balance the natural increase of production exactly. As will be discussed at greater length in Essay Three, a trigonometric sine wave may be used to represent the application of a steady, uniform growth rate over time to all angles of the circumference of the circle as indicated by 56 equal divisions.
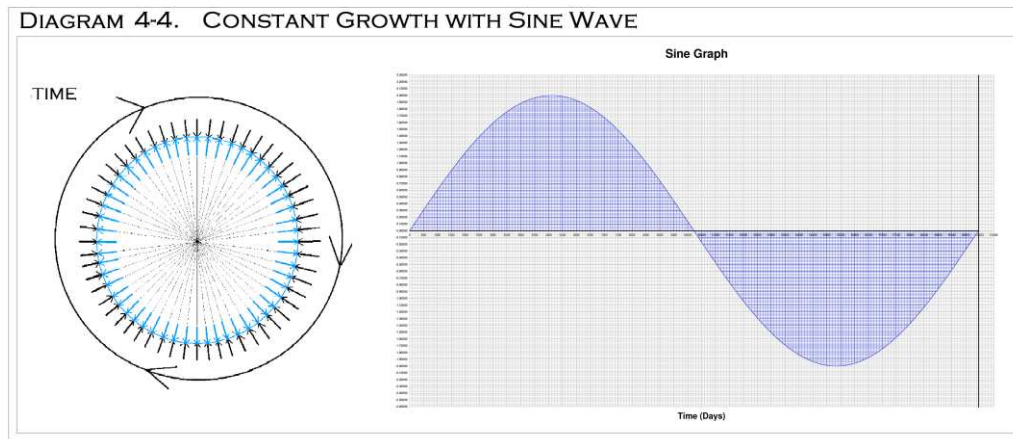
DIAGRAM 4-4. CONSTANT GROWTH WITH SINE WAVE

Regarding the diagram above we might consider as well extreme yet periodic events which cause these spikes in inflation noticed in Diagram 4-3. If a particular period of time fails to offer uniform resistance to production, or if the strength of production for some reason is particularly strong, the inherent productivity of the citizenry will create a bulge in productivity which must then be balanced out by a depression at some other time in the course of the circuit. Only in this fashion can a constant of growth be maintained in the face of unequal strengths of production and resistance to production. A wave must then develop over time during which this bulge will even out as time goes on until the next (generally unexpected) opportunity for unusual productivity occurs. If this damping price wave is placed along an x-axis, we have the following.

DIAGRAM 4-5. IRREGULAR GROWTH WITH DAMPING COSINE WAVE

4.3. Exogenous vs. Endogenous Causation

We deal here exclusively with the United States and the discovery of strong evidence that a 56-year Kondratiev Wave appears to have significant impact upon the US economy. A long-standing issue regarding the Kondratiev Wave is the causation of the wave itself. This debate centers largely upon the "exogenous" vs. "endogenous" nature of the cycle.

From the "exogenous" point of view, it is difficult to understand how events which occur with an apparently chaotic randomness outside the United States can affect the American economy with dependable regularity.

From the "endogenous" point of view, although a form of biologic regularity might be granted to the American economy, it remains difficult to explain how such internal developments might affect with the same regularity international events over which the United States has no control whatsoever.

There can be no question that political events in Europe and throughout the world have had much to do with the inauguration of these cycles. Nor can there be serious question that the relationship between the economic development of the United States and that of Europe must be explored. The problem appears to be that two distinct yet interacting levels of economic life must be considered, one national (American) and one European. These concerns are dealt with in our separate paper entitled "*On Revolution and the Cultural Development of Europe: Toward a European "System of Movement.*" (unpublished at this time)

As to the United States considered endogenously and independently, we present as persuasive a 14 x 4 = 56 year cycle as found between the inauguration of the American Civil War and the entry of the United States into the First World War. As these relate to the "exogenous" / "endogenous" debate, the following points may be made.

1. The American Civil War began on April 12-13, 1861.

2. The First World War began in Europe on July 28, 1914.

3. 56 years after the inauguration of the American Civil War, almost to the day, the United States entered the First World War "by joint resolution of Congress on April 6, 1917" (as taken from the Peace Treaty of August 25, 1921, section 1, between the United States and Germany)

One can explore the "endogenous" vs. "exogenous" nature of the 56-year period by considering the price patterns within the United States leading up to the First World War. As taken from Data Set One, these are:

Year	Price Index	Change from previous year	
1910	28.00		
1911	28.00	+0.0	
1912	29.00	+1.0	
1913	29.70	+0.7	
1914	**30.10**	**+0.4**	**World War I Between European States**
1915	**30.40**	**+0.3**	
1916	**32.70**	**+2.3**	
1917	**38.40**	**+5.7**	**United States Enters World War I**
1918	**45.10**	**+6.7**	
1919	**51.80**	**+6.7**	
1920	**60.00**	**+8.2**	
1921	53.60	- 6.4	
1922	50.20	- 3.4	
1923	51.10	+0.9	

One can see from the above that the inauguration of World War I in Europe in 1914 did not impact dramatically upon the price structure of the United States. Examining the United States' price structure for the years of European conflict 1914, 1915 and 1916 (in blue) changes of 0.4 + 0.3 + 2.3 = 3.0 may be noted.

The American entry into World War I in 1917 is associated with a spike in prices for the years 1917, 1918 and 1919 (in red) for a total of 5.7 + 6.7+ 6.7 = 19.1, over six times the cumulative changes of the previous three years. This would indicate that the domestic decision to enter World War I had far more to do with the resulting inflation than did the existence of the war in Europe itself. Indeed this inflationary trend carried on beyond the 1919 Armistice, entering into a downward trend only in the year of the Peace Treaty with German in 1921.

The "exogenous" aspects of the analysis simply admit that at a European level, a vast war was occurring into which the United States ultimately was drawn. The "endogenous" aspects of the analysis insist that the United States was governed by its own internal development as to whether and when to join the conflict.

A similar point may be made with regard to the Vietnam War. Below are contrasted the steadily rising casualty counts for American soldiers 1956-1980 (as taken from the National Archives at http://www.archives.gov/research/military/vietnam-war/casualty-statistics.html) with the price index from Data Set 1. When changes to the price index exceed the fraction 1.06 they are highlighted in red.

We see below that the Vietnam War was not a strong inflationary factor throughout the years of its most ferocious conflict when the annual casualty count exceeded 1,000, i.e. between 1965-1971 (also highlighted in red). At no time during this period did the price index exceed a multiple of 1.06 over the previous year.

On the other hand as of 1973, a year when the annual casualty count had diminished to less than 200, the inflation rate suddenly increased by no less than a multiple of 1.06 for nine of the next ten years.

In a fashion similar to 1917, inflation during this period is associated with the United States passing through a particular phase of its development and is not directly connected with the previous existence of the War in Vietnam.

	Casualty count	Current year / Previous year	Price Index	Current year / Previous year
1956-1960	9		88.70	
1961	16	+ 1.77	89.60	1.0101
1962	52	+ 3.25	90.60	1.0111
1963	118	+ 2.26	91.70	1.0121
1964	206	+ 1.74	92.90	1.0130
1965	**1,863**	**+ 9.04**	94.50	1.0172
1966	**6,143**	**+ 3.29**	97.20	1.0285
1967	**11,153**	**+ 1.81**	100.00	1.0288
1968	**16,592**	**+ 1.48**	104.20	1.0420
1969	**11,616**	**+ 0.70**	109.80	1.0537
1970	**6,081**	**+ 0.52**	116.30	1.0591
1971	**2,357**	**+ 0.38**	121.50	1.0447
1972	641	+ 0.27	125.40	1.0320
1973	168	+ 0.26	**133.20**	**1.0622**
1974	178	+ 1.05	**147.90**	**1.1103**
1975	161	+ 0.90	**161.40**	**1.0912**
1976	77	+ 0.47	170.70	1.0576
1977	96	+ 1.24	**181.80**	**1.0650**
1978	447	+ 4.65	**195.60**	**1.0759**
1979	148	+ 0.33	**217.80**	**1.1134**
1980	26	+ 0.17	**247.20**	**1.1349**
1981			**272.70**	**1.1031**
1982			**289.50**	**1.0616**
1983			298.80	1.0310
1984				

Placing in red inflation rates exceeding a multiple of 1.06 or greater from the previous year, we have:

Year	Price Index	Change from previous year	Year	Price Index	Change from previous year	Year	Price Index	Change from previous year
						1961	89.60	+1.01
						1962	90.60	+1.01
						1963	91.70	+1.01
						1964	92.90	+1.01
						1965	94.50	+1.01
1854	27		1910	28.00		1966	97.20	+1.02
1855	28	1.03	1911	28.00	+1.00	1967	100.00	+1.02
1856	27	0.96	1912	29.00	+1.03	1968	104.20	+1.04
1857	28	1.03	1913	29.70	+1.02	1969	109.80	+1.05
1858	26	0.92	1914	30.10	+1.01	1970	116.30	+1.05
1859	27	1.03	1915	30.40	+1.00	1971	121.50	+1.04
1860	27	1.00	**1916**	**32.70**	**+1.07**	1972	125.40	+1.03
1861	27	1.00	**1917**	**38.40**	**+1.17**	**1973**	**133.20**	**+1.06**
1862	**30**	**1.11**	**1918**	**45.10**	**+1.17**	**1974**	**147.90**	**+1.11**
1863	**37**	**1.23**	**1919**	**51.80**	**+1.14**	**1975**	**161.40**	**+1.09**
1864	**47**	**1.27**	**1920**	**60.00**	**+1.15**	1976	170.70	+1.05
1865	46	0.97	1921	53.60	+0.89	**1977**	**181.80**	**+1.06**
1866	44	0.95	1922	50.20	+0.93	**1978**	**195.60**	**+1.07**
1867	42	0.95	1923	51.10	+1.01	**1979**	**217.80**	**+1.11**
						1980	**247.20**	**+1.13**
						1981	**272.70**	**+1.10**
						1982	**289.50**	**+1.06**
						1983	298.80	+1.03

56 years separates dates along a horizontal line. Given the striking inflationary trends noticed below the above horizontal line, we conclude that a 56-year Kondratiev Wave has much to offer in the analysis of decisions "endogenously" considered by the United States, while acknowledging the importance of the world wide "exogenous" factors which compel these decisions to be made.

4.4. Cumulative Change/Average Inflation Over A 56-Year Cycle

We then placed all change/average inflation (lower graph above) along a 56-year circuit shown below. In the following diagram 9 o'clock represents the midpoint of the cumulative average of all inflation along a 56 year cycle as contained within the blue rectangles above. (This is marked as "Year One" in Data Set 6.) 3 o'clock represents the midpoint of the cumulative average of all inflation rates 28 years later. (Line 29 in Data Set 6)

The circumference of each circle represents a positive increase in the cumulative change/average figure of 1/2 percent (for example, a change/average cumulative amount of 1805 + 1861 + 1917 + 1973 lying directly at 9 o'clock). Points found within the interior of the smallest circumference represent negative figures by a comparable amount.

The blue square below represents the four 14-year segments of time set forth in Diagrams 4-2 and 4-3. The blue-shaded rectangles previously given in Diagrams 4-2 and 4-3 are represented by the vertical left line segment (below). Taken together 4 x 14 periods of time create the 56 year circuit of time of this model. Note that the Great Depression of 1929-1940 is part of the deep indentation between axis 12 and 22, i.e. at the top horizontal of the blue square and interior to the smallest radii.

DIAGRAM 4-6.
CUMULATIVE "CHANGE/AVERAGE" INFLATION

1805, 1861, 1917, 1973, 2029
1777, 1833, 1889, 1945, 2001

LINES IN BLUE REPRESENT 14 YEAR PERIODS OF TIME
NUMBERS IN BLACK REPRESENT SEPARATE AND DISTINCT RAYS ALONG THE 56-YEAR CIRCUIT
YEARS IN RED INDICATE DATES LYING ALONG THE SAME AXIS
EACH RADIUS OF CIRCUMFERENCE REPRESENTS A POSITIVE INCREASE OF 1/2 PERCENT IN THE CUMULATIVE INFLATION RATE FOR THAT AXIS

TIME

4.5. The GNP Spiral and the Median Average for Growth

We then placed the U.S. real GNP figures given in "Data Set 2 – U.S. Real GNP" in a 56 year circuit, with the four 14-year quarter cycles indicated in blue, to create "the GNP Spiral" below. The center of the spiral, beginning at axis 9 = 1869, represents the real Gross National Product for that year of 23.10 billion dollars in 1958 prices. The Gross National Product for subsequent years in real terms are given along each axis respectively, with each circle of circumference representing ten billion dollars of real GNP in 1958 prices. Each row of the 14-year spreadsheet is represented by a "cross" within the spiral. Row One of the spread sheet is given below as the diagonal "cross" of the square, Row 8 of the spreadsheet is at the horizontal and vertical axes or "cross" of the square.

DIAGRAM 4-7. THE "GNP SPIRAL"
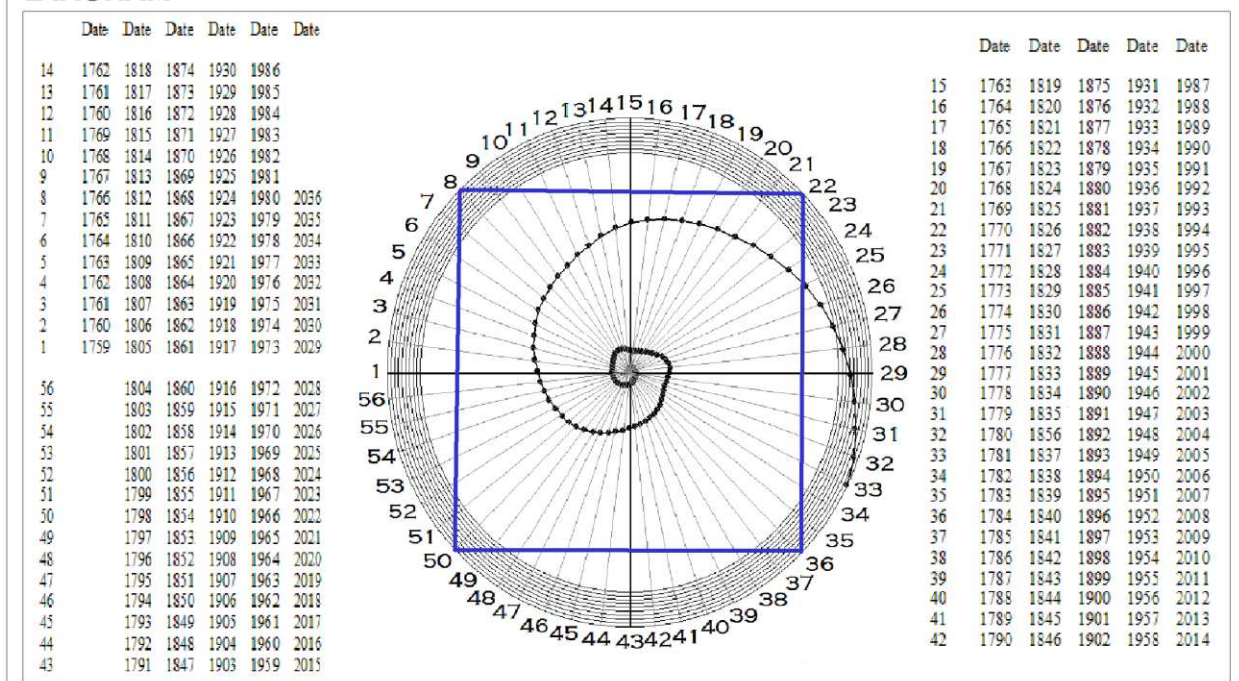
As can be seen from the 14-year spreadsheet (placed in the Appendix, we then:

(1)   figured the average for each row of the spreadsheet for a total of 14 averages (Column F),

(2)   figured the Median (1.617735) and Average (1.619446) of Column F, and

(3)   *figured a final Median Average for the entire spreadsheet of 1.618590.*

In all spreadsheets this set of calculations is termed a "circle analysis." This nomenclature refers to the arrangement of Row Averages as points along the circumference of a circle, each one counted equally and but once toward a final Median Average of the spreadsheet.

4.6. The Golden Mean and the Structure of American Economic History

This number 1.618590, the final Median Average of rows[29], is 0.034% greater than the constant phi, 1.6180339…   This constant, sometimes referred to as "the Golden Mean," "the Golden Ratio" or "the Golden Section," was defined circa 300 b.c. by Euclid of Alexandria, as follows:
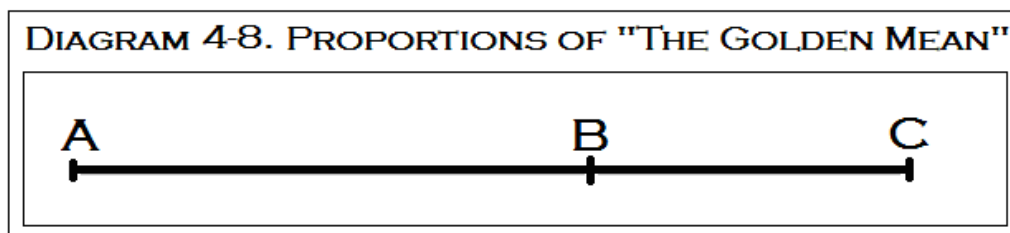
DIAGRAM 4-8. PROPORTIONS OF "THE GOLDEN MEAN"

> A straight line is said to have been cut in extreme and mean ratio when, as the whole line is to the greater segment, so is the greater to the lesser.[30], [31]

If line segment AB is set to 1, and if the line segment AC is in a Golden Mean relationship to AB, then line segment AC will equal 1.6180339… often referred to by the Greek letter phi, φ, small case.

This finding can be checked by creating the following graph wherein we:

     a)   indicate the spread between years which generates the ratio (presented below in the "# of years" first column),

     b)   set forth the Median Average for all ratios generated for any given spread of years (second column below),

     c)   figure the "absolute difference" and the "percentage difference" of these different Median Averages from phi (3rd and 4th columns below), and finally

     d)   state these differences as absolute values (5th and 6th columns below).

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[29]   As mentioned in the text, a "circle analysis" counts each average of rows (column F) a single time toward a final Median Average for the entire spreadsheet. A "square analysis" counts the first row twice, and arrives at a slightly different number, one which is 0.0053% in proximity to the Golden Mean.

[30]   Euclid of Alexandria, Elements, Book VI, Definition 3, circa 300 b.c. A broad array of texts may be suggested describing the well-known associations between the Golden Mean and patterns discovered in Nature. See e.g. Livio, 2002; Skinner, 2006; Hemenway, 2005.

[31]   See the discussion of the Golden Mean in Essay One, lines 290-306.

This data is summarized in the bar graph below this data. This graph demonstrates that Median Average generated by a 14-year spread between years are closest to 1.6180339…, = □, or the Golden Mean.

DIAGRAM 4-9.
COMPARATIVE DIFFERENCES:
MEDIAN AVERAGES VS. 1.61803399

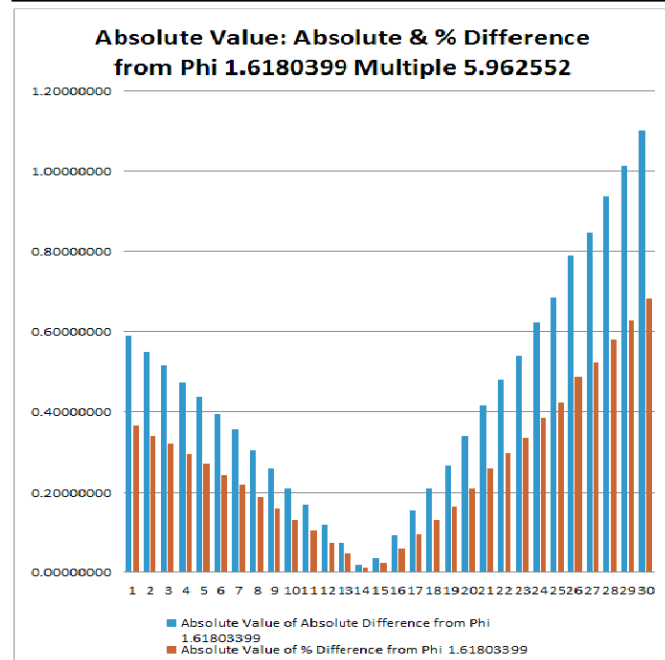| # of Years	Median Aveage	Absolute Difference from Phi 1.61803399	% Difference from Phi 1.61803399	Absolute Value of Absolute Difference from Phi 1.61803399	Absolute Value of % Difference from Phi 1.61803399
1	1.03086043	0.58717356	36.2893216%	0.58717356	36.2893216%
2	1.06996068	0.54807331	33.8727936%	0.54807331	33.8727936%
3	1.10353672	0.51449727	31.7976802%	0.51449727	31.7976802%
4	1.14504076	0.47299323	29.2325895%	0.47299323	29.2325895%
5	1.18247232	0.43556167	26.9191915%	0.43556167	26.9191915%
6	1.22633118	0.39170281	24.2085649%	0.39170281	24.2085649%
7	1.26388505	0.35414894	21.8876084%	0.35414894	21.8876084%
8	1.31520833	0.30282566	18.7156551%	0.30282566	18.7156551%
9	1.36070905	0.25732494	15.9035558%	0.25732494	15.9035558%
10	1.40916235	0.20887164	12.9089775%	0.20887164	12.9089775%
11	1.44965664	0.16837735	10.4062924%	0.16837735	10.4062924%
12	1.50019982	0.11783417	7.2825524%	0.11783417	7.2825524%
13	1.54501537	0.07301862	4.5127988%	0.07301862	4.5127988%
14	1.60189961	0.01613438	0.9971593%	0.01613438	0.9971593%
15	1.65125029	-0.03321630	-2.0528801%	0.03321630	2.0528801%
16	1.70936280	-0.09132881	-5.6444307%	0.09132881	5.6444307%
17	1.77052591	-0.15249192	-9.4245191%	0.15249192	9.4245191%
18	1.82742627	-0.20939228	-12.9411549%	0.20939228	12.9411549%
19	1.88097935	-0.26294536	-16.2509171%	0.26294536	16.2509171%
20	1.95675154	-0.33871755	-20.9338960%	0.33871755	20.9338960%
21	2.03196341	-0.41392942	-25.5822452%	0.41392942	25.5822452%
22	2.09620235	-0.47816836	-29.5524302%	0.47816836	29.5524302%
23	2.15690921	-0.53887522	-33.3043204%	0.53887522	33.3043204%
24	2.23755840	-0.61952441	-38.2887142%	0.61952441	38.2887142%
25	2.30123214	-0.68319815	-42.2239677%	0.68319815	42.2239677%
26	2.40625778	-0.78822379	-48.7149093%	0.78822379	48.7149093%
27	2.46439399	-0.84636000	-52.3079247%	0.84636000	52.3079247%
28	2.55145856	-0.93342457	-57.6888107%	0.93342457	57.6888107%
29	2.62813943	-1.01010544	-62.4279492%	1.01010544	62.4279492%
30	2.71795717	-1.09992318	-67.9789908%	1.09992318	67.9789908%

Absolute Value: Absolute & % Difference from Phi 1.6180399 Multiple 5.962552

■ Absolute Value of Absolute Difference from Phi 1.61803399
■ Absolute Value of % Difference from Phi 1.61803399

As noted in Essay One, the final Median Average for the 14-year spread of 1.618590 was generated as a result of the following Row Dynamics, a pattern which had the least "Used General Dissonance," the least "Acute Dissonance" and the second-to-least "Claimed Dissonance" of all spreads considered. As can be seen below quite clearly, and unlike the other spreads considered, when a high average of the row is reached it is immediately balanced by a low as determined from the approximate midpoint of the Golden Mean. In addition, as time has passed the American economy has steadily narrowed its focus to precisely this same single point.[32]

DIAGRAM 4-10.
ROW AND COLUMN DYNAMICS: 14-YEAR SPREAD

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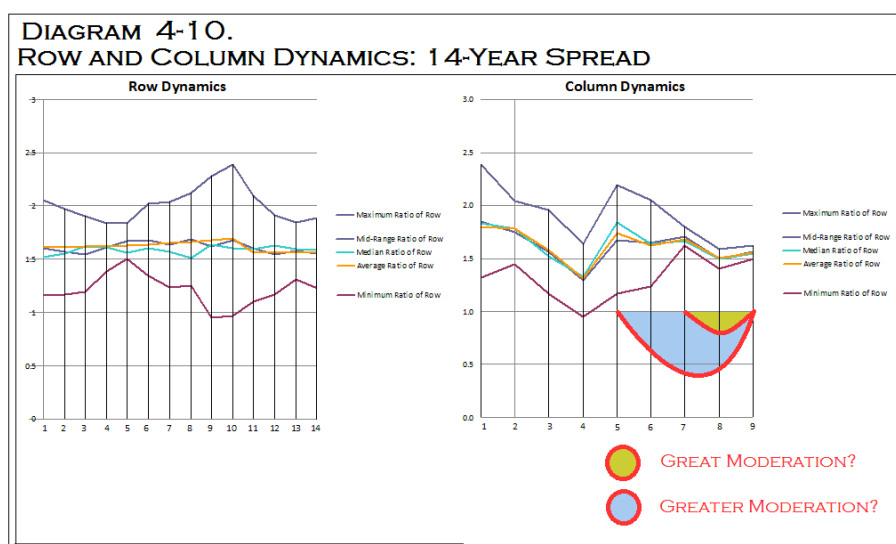
[32]   The last two columns of the Column Dynamic graphic represent a time period stretching from the end of Column 7 (1979) through the end of Column 9 (2007). During this period of time the economic volatility of previous years markedly narrowed. This finding is reflected in the graph below charting the volatility of the U. S. Gross Domestic Product and its abrupt lessening in 1984. (Summers, 2005)

DIAGRAM 4-10A.
"THE GREAT MODERATION"
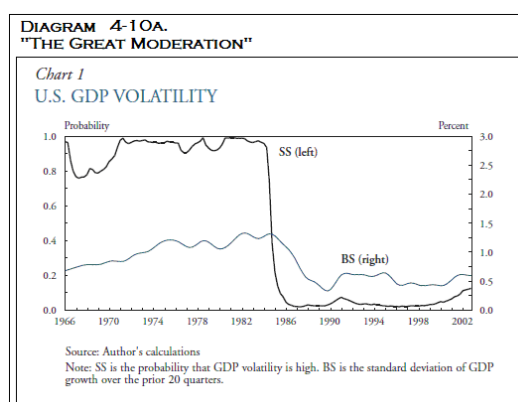
Although hailed at the time as "The Great Moderation" and a possible sign of progress in economic understanding (e.g. Bernanke, 2004) post-Global Financial Crisis this view has come under attack. (e.g. Chomsky, 2011) Chart 2-10 demonstrates that a marked narrowing of volatility began two columns prior to 1979, i.e. beginning with the end of Column 5 (1951), named here "The Greater Moderation" by way of comparison. See Essay Five for further comments on this matter.

To figure the annual increase implied by the GNP Spiral, we may use the formula for simple interest compounded annually…

$$FV = PV\,(1+r)^{t}$$

… ; state a present value (PV) of $1,000,000; a time period (t) of 14 years; and the future value (FV) as given below in proportion to the varying numbers derived in the GNP Spiral. These assumptions give us the following interest rates (r).

	Future Value		Interest rate
x= Circle Analysis:	$1,618,590	interest rate is:	3.4995226
x= Golden Mean:	$1,618,033	interest rate is:	3.4969781

These "interest rates" are the annual "rates of growth" necessary to obtain the various proportions of the GNP Spiral over time,[33],[34]

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[33]   At least one reference – albeit atavistic – may be cited in support of a similarity between the large number of designs found in Nature which incorporate the Golden Mean (the galactic spiral, the Chambered Nautilus, seed pods of various plants, aspects of DNA, etc.) and the almost biologic dynamism of the GNP Spiral presented herein. (See e.g. Kahn, 1961:425) "(I)t … seems likely that Stalin's caution (regarding antagonism toward the United States) did not stem from fear of the atomic bomb as a decisive weapon. What alarmed him about the United States was Detroit – not (the Strategic Air Command)! He appears to have felt very strongly that no sensible government tangles with a nation with a GNP of $300 billion a year. Luckily we had both assets – the bomb and the GNP – so that any difference between U.S. and Soviet calculations was not crucial."

[34]   A surprisingly eclectic reading list may be constructed on possible parallels to the 56-year cycle suggested herein. These include: (1) the circular arrangement of 56 "Aubrey holes" at Stonehenge, (Cleal, et al. 1995); (2) price fluctuations predicted in 1875 by an Ohio farmer (Benner 1875); (3) business cycles of 56-years (Funk 1933); (4) astrologic cycles generally connected to the orbit of Saturn (Williams 1947, 1959, 1982); (5) an "energy use cycle" of 56-years (Stewart 1989); (6) the "Joseph Cycle" (Sim 2008) and (7) a compendium of geologic, weather, financial and other information (McMinn 2006, 2007, 2011). The Jewish festival *Birkat Hakhammah* "Blessing of the Sun" takes place every 28 years, most recently April 8, 2009. See also Tompkins (1976:282) "Hunab Ku, sole source of movement and measure, symbolized the universe for the Maya in the form of a circle with an inscribed square. The circle was the symbol of the infinite, the spiritual; the square of the material. Hunab Ku was thus a universal dynamism or that which motivates and stimulates life in its total manifestation as spirit and matter, the all in one."

CONCLUSION

Referring once again to the definition of the Golden Mean, we have:

A straight line is said to have been cut in extreme and mean ratio when, as the whole line is to the greater segment, so is the greater to the lesser.

DIAGRAM 4-8. PROPORTIONS OF "THE GOLDEN MEAN"

A   B   C
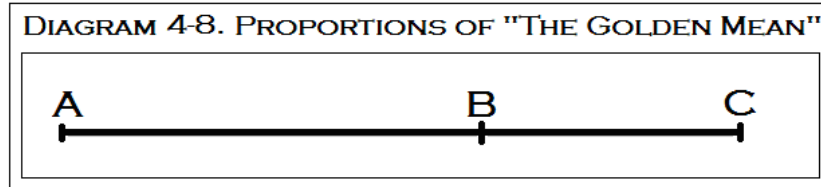
As described in this article, and in connection with the economic progress of the United States, *the Golden Mean appears to tie the past (line segment BC) to the present (line segment AB) to the future (line segment AC) in a self-consistent and harmonic fashion*. It is a mathematic statement of the historic identity of the United States itself, as moving from date to date in a coherent, repeating manner as connected to a 14-year spread between years and as nested as a quarter-cycle within a 56-year circuit of social time.

The 14-year interval of time which lays the foundation for the 14-year spread between numerator and denominator in ratios of GNP, like the musical interval of an octave, provides a framework within which this evolution of GNP may take place. Like the octave, it lays the essential mathematic relationship of the entire spectrum of harmonies of growth. This coincides with the 50-60 year period given by Kondratiev as the basis for his model.

There is at least a poetic similarity between the division of a line segment into past-present-future and the familial context underlying society itself wherein one's parents (past) give birth to one's self (present) as continued through one's children (future). Inasmuch as each stage of this familial expansion of self begins with the onset of reproductive capacities at age 14, the GNP Spiral / classic Kondratiev Wave may form as a parallel to an underlying biologic pattern.

DIAGRAM 4-11.
TIME BY GENERATIONS.
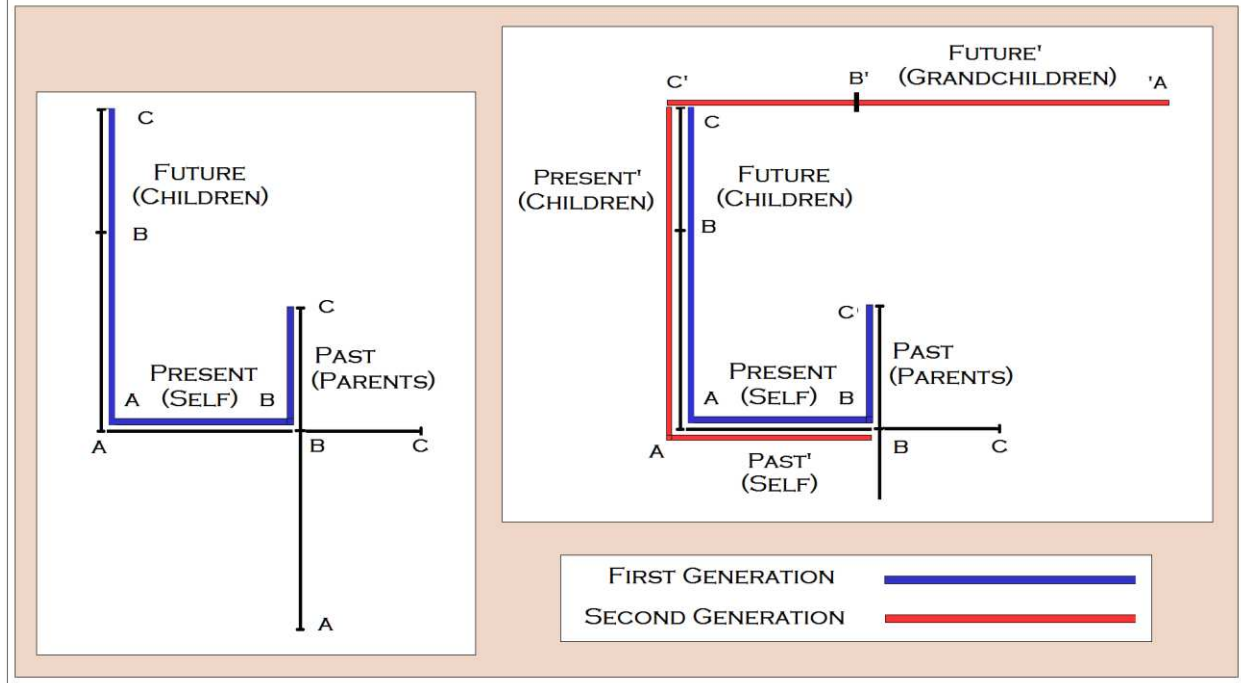
It appears to be very likely that this underlying geometry of "generational time" lays the foundation for the strict cyclical element of the Kondratiev Wave, one which is biologically driven but upon which an enormous host of other economic, social and political relationships float inter-connectedly.

One might bear in mind the sheer force of life which continually bears on this dynamic. If we imagine that this "life force" of the economy may be viewed physically at the graduation of a high-school class, we can see that the force of these repetitive 14-year periods is not limited to a single family unit but rather constitutes a continuing host of waves, each breaking into the future as a new, highly charged and hopeful high school graduation class.

Returning to the hypothetical child born on January 1, 2000, we can watch the cumulative force of this development. Below we see a straight-line development over time as represented by each high school class graduation date, beginning with the graduation date of said child at 2018 (in highlighted yellow below). Every graduation class possesses a 14-year wavelength sustaining it. And each class is like the others in that the persons graduating begin the ascent through the careers which they choose.

As a single life goes through the sequential 14-year periods of Primary School, Secondary School, Early Career, Mid-Career, Late Career and Retirement which are themselves complemented by similar high school class graduations, we have the following.

DIAGRAM 4-12.
HIGH SCHOOL GRADUATION CLASSES
WITH 14-YEAR CYCLES
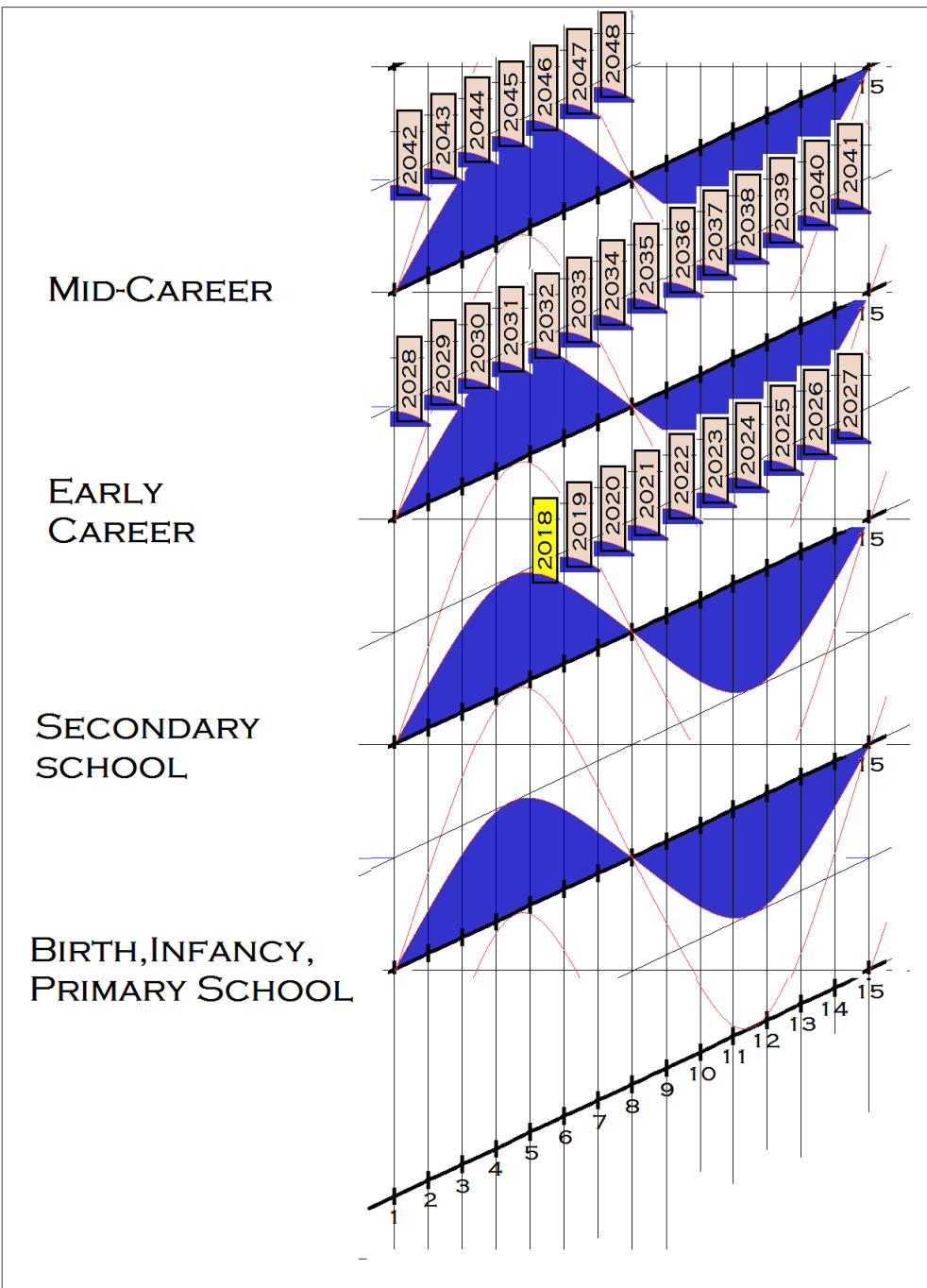
In conclusion it appears that the fundamental "octave" of life is the motion leading from birth to reproductive capacity (Diagram 3-12, pink "claimed dissonance" graph). This is encompassed by the dampening price wave (Diagram 4-3, 4-5), and the largest 56-year octave of the entire Kondratiev cycle (Diagram 4-4).

We note that the intermediate "octave" represented below by the damping wave of price change appears to connect the biologic human octave of 14 years to the larger 56-year octave of the Kondratiev Wave.

If we associate the "political" life of the United States with a 56-year Kondratiev Wave (the sine wave below in dark green), and the "economic" life of the United States with the damping price wave (the cosine wave below in red), we may construct a "political economy wave" (below in light green) by the simple addition of these two separate but inter-connected waves.

April 9 is used as the beginning date of this approach, i.e. the date mid-way between the April 12-13 date in 1861 beginning the American Civil War, and the April 6, 1917 date beginning the United States' involvement in World War I. Figuring 20,453 days between these April 9, 1961 and April 9, 1917, this figure can be added to April 9, 1917 to obtain the date April 8, 1973. It can also be subtracted from April 1861 to obtain the date April 10, 1805.

It has been proved helpful to figure the length of the cycle as exactly 20,454 days, beginning with the dates of April 9 in the years 1805, 1861, 1917 and 1973, using a common "April 9" starting date. Despite this numeric inconsistency of one day, the cycles suggested by this approach are useful in that they track trigonometrically essential aspects of American economic history, as follows.
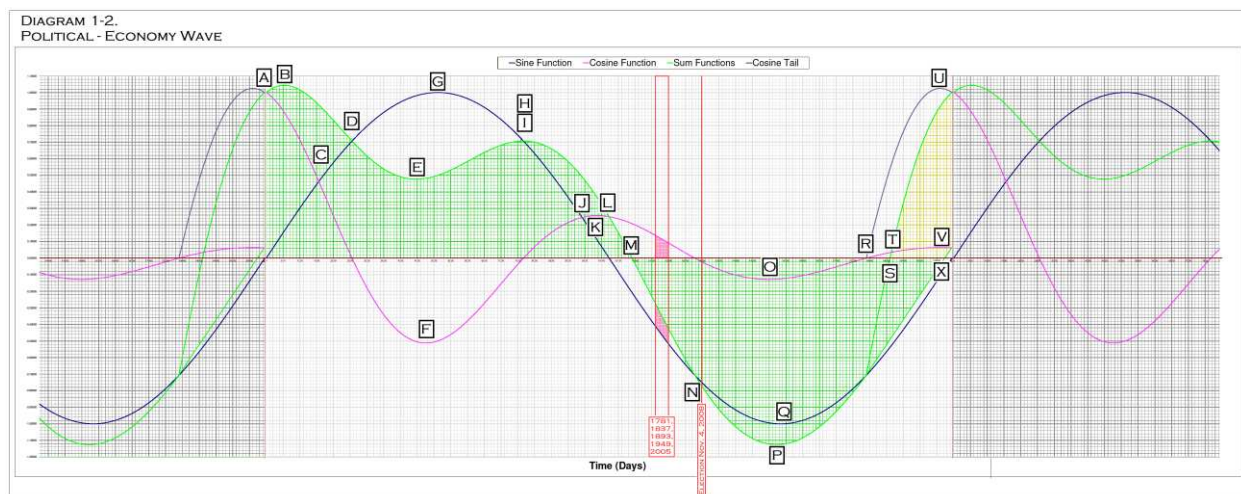
In Essay Five we turn to the systematic study of these relationships.

Essay 5:
Time and Consciousness

INTRODUCTION

As mentioned in the Preface to these essays, based upon the analysis presented one can predict that a financial panic should be expected to take place in 2005, as based upon similar financial economic / political panics which occurred previously in the years 1781, 1837, 1893 and 1949, each date separated by 56 years.

DIAGRAM 5-1.
BASIC PLAN.

1. MICRO-ECONOMIC CHOICE
   X-AXIS = ECONOMIC ACTIONS (TRADING VS. KEEPING)
   Y-AXIS = ECONOMIC THOUGHTS (TRADING VS. KEEPING)

2. MICRO-ECONOMIC CHOICES AGGREGATED OVER A YEAR:
   OKUN'S LAW STATES A $\pi : 1$ RATIO AS TO
   HOW OUTPUT GROWTH VARIES WITH CHANGES IN THE UNEMPLOYMENT RATE

3. REAL GNP AGGREGATED OVER 14-YEARS, AN "ECONOMIC OCTAVE,"
   THE PERIOD OF TIME DURING WHICH HUMAN DEVELOPMENT PROCEEDS FROM BIRTH TO PROCREATIVE CAPACITY
   AND CREATES A GOLDEN MEAN RATIO WITHIN U.S. REAL GNP

4. DAMPING COSINE WAVE OF PRICE FLUCTUATIONS OVER A 28-YEAR PERIOD

5. SINE WAVE OF 56-YEARS ENCOMPASSING SOCIO-POLITICAL CHANGE IN A SINGLE CIRCUIT,
   THE "KONDRATIEV WAVE"

The spreads noted in Essay Three may be graphed in association with their placement in the 56-year cycle. The red lines of association between dates of a spread are drawn by taking the first row of each spreadsheet and indicating the date associated with the denominator (in each case, 1868) and then drawing lines to the point associated with each subsequent denominator in the row.

DIAGRAM 5-2.
AN ECONOMIC CLOCK OF BIO-COMPLEXITY
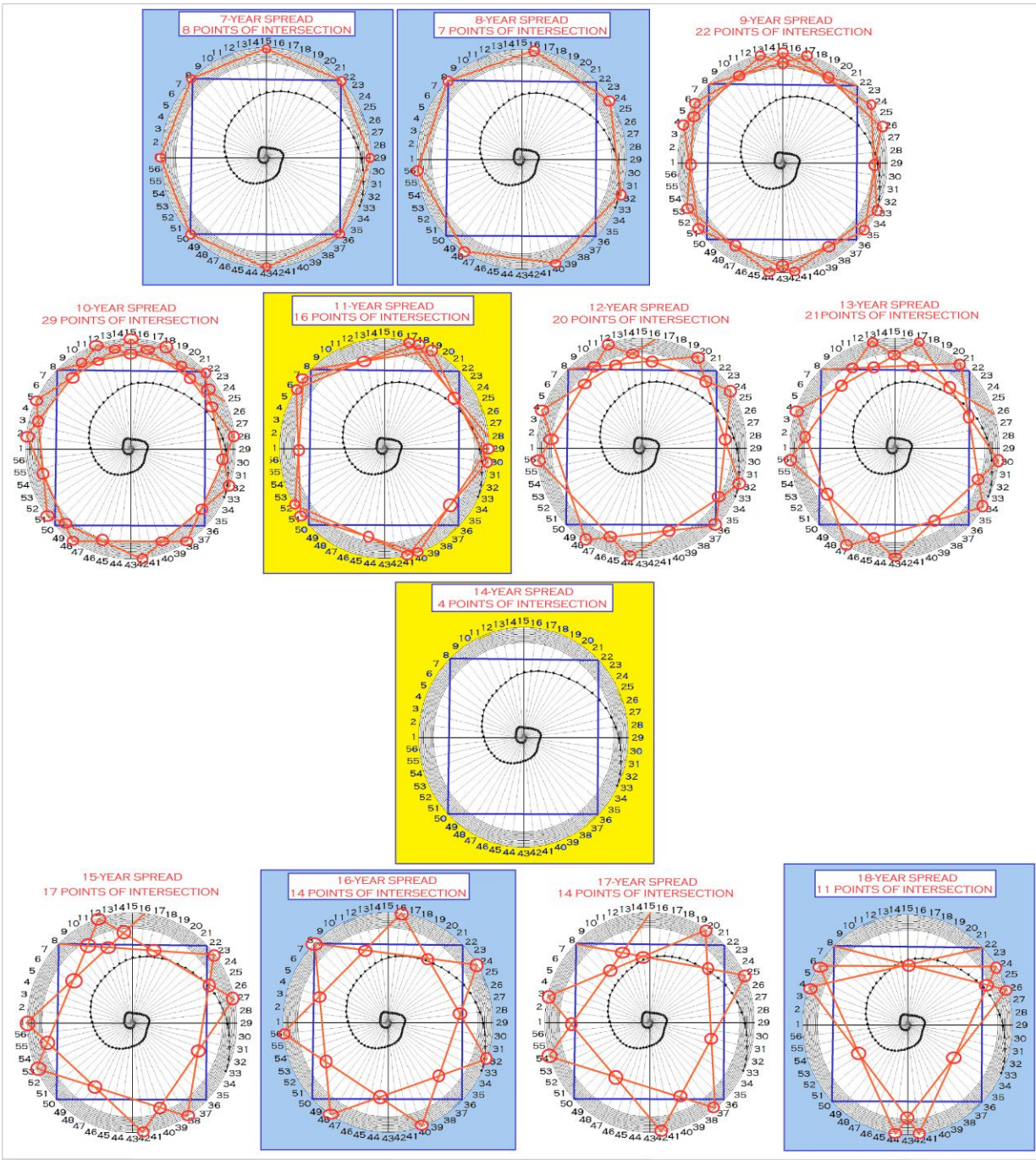
This has the effect of creating a "clock of bio-complexity" in that, as one moves down the rows of the spreadsheets, the graph of the associated red lines of Diagram 5-2 move over one space moving clockwise.

Highlighted in yellow are the two spreads which appear most dramatically from the previous essays to evidence a relationship to the Golden Mean, these being the 14-year spread (Essays 3 and 4) and the pentagon pattern of the 11 year spread which is closely connected to the geometry of the Golden Mean as well and whose "fingerprint" was so strikingly different. [35]

Highlighted in blue are the remaining symmetries of the spreadsheets

These essays propose that the waves described herein have a central place in the steady development of the United States over time, and that maintenance of fundamental proportions of this development require a continuing and predictable series of crises during which the electorate is forced to change existing attitudes and beliefs to accommodate new, developing standards

As researchers we must be interested in the timing, meaning and prediction of these crises because they form a key element in the understanding of the economy itself. Had these warnings been heeded the crisis may have been better anticipated perhaps would have occurred at the time predicted and resolved along historic precedents. The global financial crisis of 2008, imploding just months before the election of United States Senator Barack Obama, meets the description of the panic predicted but as postponed – and thereby expanded – by a delay of three years [36]

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[35]   The 56-year cycle may be used as a basis for comparison between spreadsheets creating, in effect, a biologic clock of time as operating on the history of the United States. The Golden Mean is displayed in the following pentagon, which matches the effect of the 11-year spread as transposed onto a 56-year cycle.
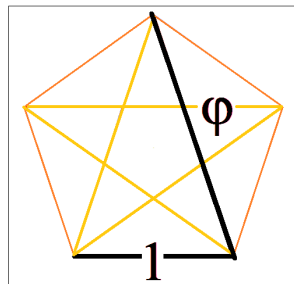
[36]   On March 7, 2012 Professor William Black, Associate Professor of Economics and Law at University of Missouri - Kansas City, criticized neo-classical economics in testimony before Congress on hearings related to the Global Financial Crisis. (Black, 2012)   He states: *Neo-Classical Economic Policies are Criminogenic: They Cause Control Fraud Epidemics.*

> Neo-classical economics (has) failed … to develop a coherent theory of fraud, bubbles, or financial crises (Black 2005). It (has) continued to rely on a single methodological approach (econometrics) that inherently produces the worst possible policy advice during the expansion phase of a bubble. …

ECONOMIC METHODOLOGY

1. Hypothesis

Our hypothesis is that the 50-60 year Kondratiev Wave may be analyzed as a precise fluctuation in the consciousness of the American People over time. This is demonstrated by the fact that the Kondratiev Wave as described in these essays is the larger fractal of the "Chooser-Available Choice" model presented in the first essay. (See Diagrams 5-7 and 5-8.)

2. Methods

We review the previous four essays and develop a mathematics which accommodates the concepts involved.

3. Data

We recapitulate the materials of the previous essays, placing them in an effective working arrangement.

In the wake of the Global Financial Crisis, a large body of criticism of neoclassical macroeconomics and its various models may be cited in support of this view.

See e.g. Krugman, 2009:
http://www.nytimes.com/2009/09/06/magazine/06Economic-t.html?pagewanted=all&_r=0

See also Solow, 2010.
http://www2.econ.iastate.edu/classes/econ502/tesfatsion/Solow.StateOfMacro.CongressionalTestimony.July2010.pdf

See also Stiglitz, 2011. http://ces.univ-paris1.fr/membre/schubert/j.1542-4774.2011.01030.x.pdf

A candid appraisal of graduate education in economics is found at Smith, 2011.
http://noahpinionblog.blogspot.com/2011/04/what-i-learned-in-econ-grad-school.html

For neo-classical analysis of unemployment see Knotek (2007, Footnote 9): "(I)ntegrated models featuring monetary policy and unemployment are only now beginning to appear; see, for instance, Blanchard and Gali (2006). For the most part, New Keynesian dynamic stochastic general equilibrium models – including medium-scale models of the type developed by Smets and Wouters (2003) – have avoided unemployment per se. Moreover, see Shimer (2005) for evidence on the severe shortcoming of the models that do include unemployment."

4. Procedure

4.1. The Kondratiev Wave as the Larger Fractal
of the Chooser – Available Choice Model

We began the search for the fundamental root of this "clock of bio-complexity" underlying American Economic History with the "Chooser - Available Choice" Model.

The micro-economic approach to "trading" vs. "keeping" a particular good may be expanded "fractal-like" in the consideration of the Kondratiev Wave as a method whereby society "trades" or "keeps" various social values over time. If the process whereby the Kondratiev Wave is constructed is congruent to – a "larger fractal" of – the micro-economic dynamics described previously, the similarities and interaction between the two models should assist in the understanding of both.

The coloration of the square-shaped timeline below surrounding the GNP Spiral provides the dates actually given by Kondratiev for periods of Phase A "upswing" (blue), Phase B "downswing" (pink), "transition" (purple). (Korotayev and Tsirel, 2010). The same coloration is used to figure a similar set of economic periods albeit based upon the GNP Spiral itself.

INTRODUCTORY DIAGRAM 5-3.
KONDRATIEV WAVE AS COMBINED WITH THE GNP SPIRAL
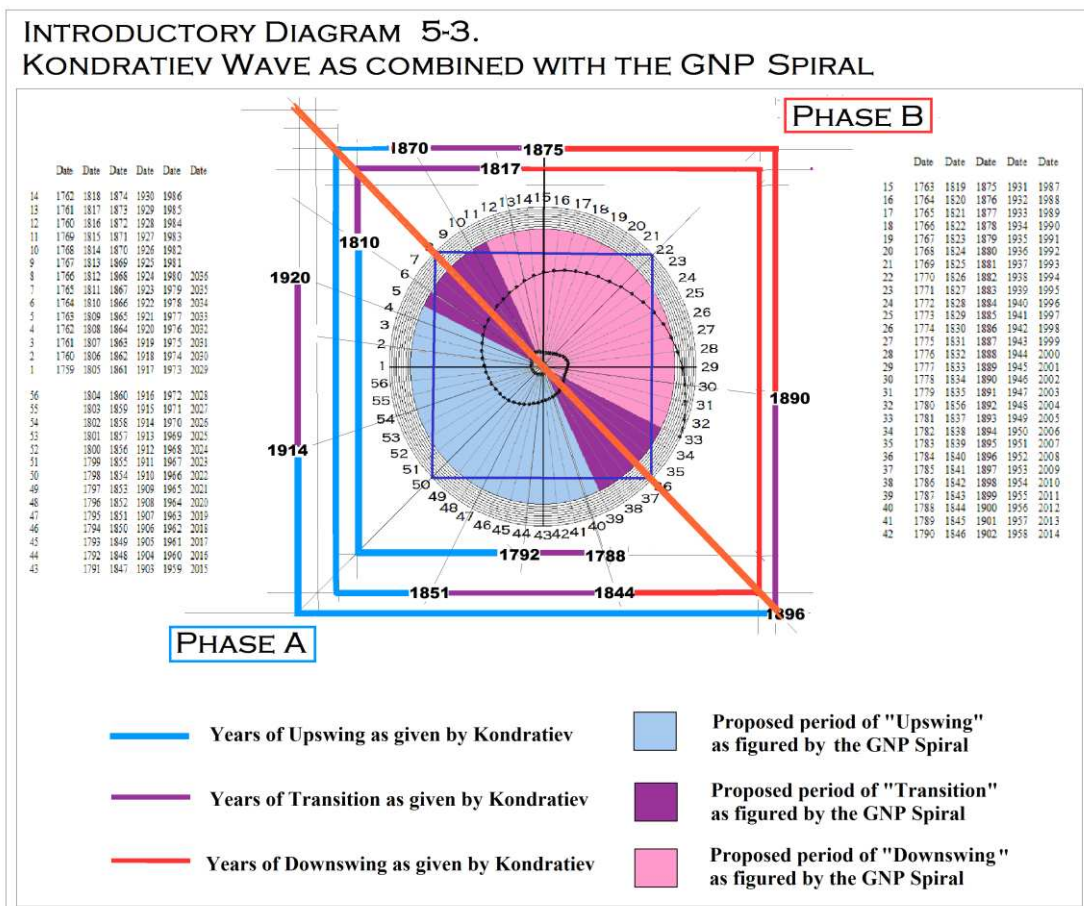
In short, the square timeline represents the Kondratiev wave as it relates to the GNP Spiral and the circular shading represents the GNP Spiral as it relates to Kondratiev wave.

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We may chart the political development of the United States by observing that the amendment of the Federal Constitution appears to be closely related to the phases of the GNP Spiral – Classic Kondratiev scheme.[37] Considering the pale blue "Phase A" region given above, we find a striking willingness to alter existing rules in favor of new methods and legal expectations. These include:

1)   the Federal Constitution itself, ratified in 1788,
2)   the Bill of Rights, the first ten Amendments, ratified in 1791, and
3)   11 additional Constitutional Amendments,

… for a total of 21 Amendments. Conversely only 3 Amendments are found in the downswing phase "Phase B" region, below in pink. The ratio of amendments between the phases is 7:1.

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[37]   Additional plans of other scholars are considered briefly in Albers & Albers (2011).

Amendments falling in the blue shaded area are far more fundamental to American constitutional law than those in the pink shaded area. Moreover the transition periods form an interesting unit. Amendment 22, prohibiting a single individual from serving more than two presidential terms, was aimed (by Republicans) at the four elections won by (Democrat) President Roosevelt. The 13th, 14th and 15th Civil War Amendments were clearly intended to consolidate Abolitionist, Western and Northern gains against the Southern slave holding class.

DIAGRAM 5-4.
UPSWING, TRANSITION AND DOWNSWING IN THE KONDRATIEV WAVE

15: FRANCHISE FOR FORMER SLAVES
14. DUE PROCESS, EQUAL PROTECTION

13. ABOLITION OF SLAVERY
19. FRANCHISE FOR WOMEN
18. PROHIBIT CONSUMPTION OF LIQUOR
12. PRESIDENTIAL ELECTION RE-STRUCTURED
26. FRANCHISE AT 18 YEARS OF AGE
16. PERMIT FEDERAL INCOME TAX
17. DIRECT ELECTION OF SENATORS
25. PRESIDENTIAL SUCCESSION
24. ELIMINATE POLL TAX
11. JURISDICTION OF FEDERAL COURTS
23. PRESIDENTIAL VOTE FOR THE DISTRICT OF COLUMBIA

PHASE B - "DOWNSWING"

1776: DECLARATION OF INDEPENDENCE

20. TERMS OF OFFICE AND COMMENCEMENT DATES
21. PERMIT CONSUMPTION OF LIQUOR
27. CONGRESSIONAL SALARY

22. PROHIBIT SERVING MORE THAN TWO PRESIDENTIAL TERMS

JULY 21, 2011

1788: FEDERAL CONSTITUTION

1. RELIGION (ESTABLISHMENT AND FREE-EXERCISE), SPEECH, PRESS, ASSEMBLY, PETITION
2. KEEP AND BEAR ARMS
3. QUARTERING OF SOLDIERS PROHIBITED
4. SEARCH AND SEIZURE, WARRANTS
5. GRAND JURIES AND INDICTMENTS, DOUBLE JEOPARDY, DUE PROCESS OF LAW, JUST COMPENSATION UPON EXERCISE OF EMINENT DOMAIN
6. SPEEDY / PUBLIC TRIAL, LOCAL VENUE, INDICTMENT/INFORMATION, CONFRONTATION OF WITNESSES, SUBPOENA POWER TO ACCUSED, ASSISTANCE OF COUNSEL
7. JURY TRIAL FOR CIVIL SUITS
8. PROHIBITION ON EXCESSIVE BAIL AND FINES, CRUEL AND UNUSUAL PUNISHMENTS
9. ENUMERATION OF RIGHTS DOES NOT RESTRICT "OTHERS RETAINED BY THE PEOPLE"
10. POWERS RESERVED TO THE STATES OR PEOPLE

1791: BILL OF RIGHTS:

PHASE A - "UPSWING"

If the historic course of amendments is tracked according to their placement on a sine wave and color-coded in directly relationship with the foregoing cycle, we have the following.

DIAGRAM 5-5.
56-YEAR KONDRATIEV SINE WAVE WITH AMENDMENTS IN UPSWING AND DOWNSWING PERIODS
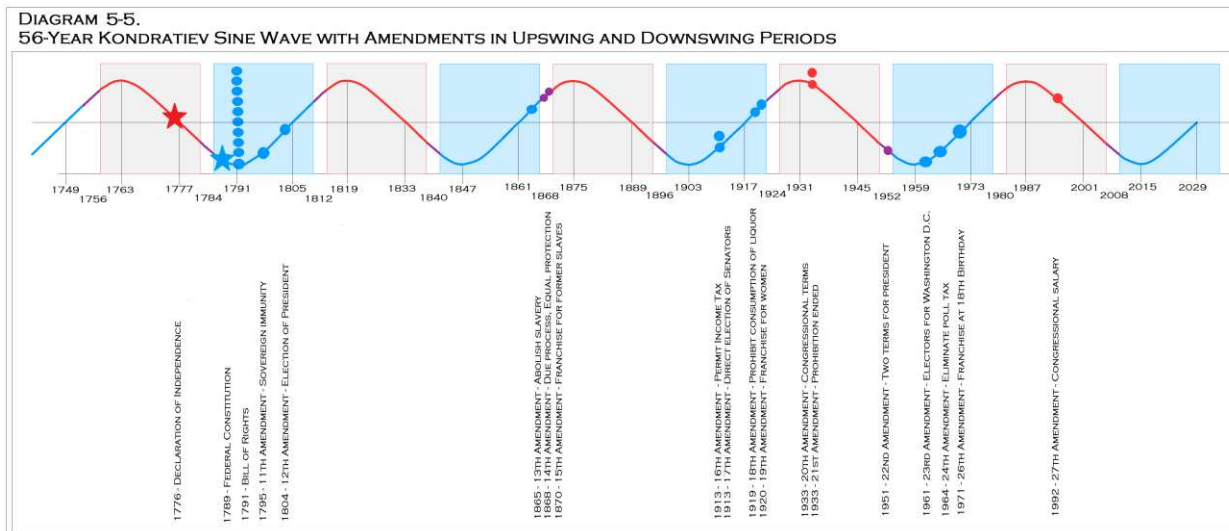
The amendments which most dramatically affect the lives and legal history of the United States are clearly associated with the up-sweep of this sine curve. A la Kondratiev, "Phase A" Amendments were often the victories of hard-fought battles wherein the people of the United States did, indeed, save themselves from demise.

We may begin to connect the foregoing macro-economic statement of change with the neo-classical micro-economic dichotomies of "trading" vs. "keeping" a particular good if we color code the GNP Spiral and the Political Economy Wave as follows. As noted below, four distinct historic periods – expansion, hyper-inflation, collapse and consequence – may be considered.

DIAGRAM 5-6.
CUMULATIVE "CHANGE/AVERAGE" INFLATION

EXPANSION
HYPER-INFLATION
COLLAPSE
CONSEQUENCES

1805, 1861, 1917, 1973, 2029
1777, 1833, 1889, 1945, 2001

LINES IN BLUE REPRESENT 14 YEAR PERIODS OF TIME
NUMBERS IN BLACK REPRESENT SEPARATE AND
DISTINCT RAYS ALONG THE 56-YEAR CIRCUIT
YEARS IN RED INDICATE DATES LYING ALONG THE SAME AXIS
EACH RADIUS OF CIRCUMFERENCE REPRESENTS A POSITIVE INCREASE OF
1/2 PERCENT IN THE CUMULATIVE INFLATION RATE FOR THAT AXIS

The nature of the upswing vs. downswing noticed by Kondratiev is directly related to the "chooser- available choices" model provided earlier in this essay. Let us first consider those portions of the trigonometric unit circle wherein the actions and thoughts in favor of trade (change) exceed those of keeping the property (stability). These are the amendments associated with this period of time.

DIAGRAM 5-7.
CHANGE VS. STABILITY - SOUTHWEST CORNER
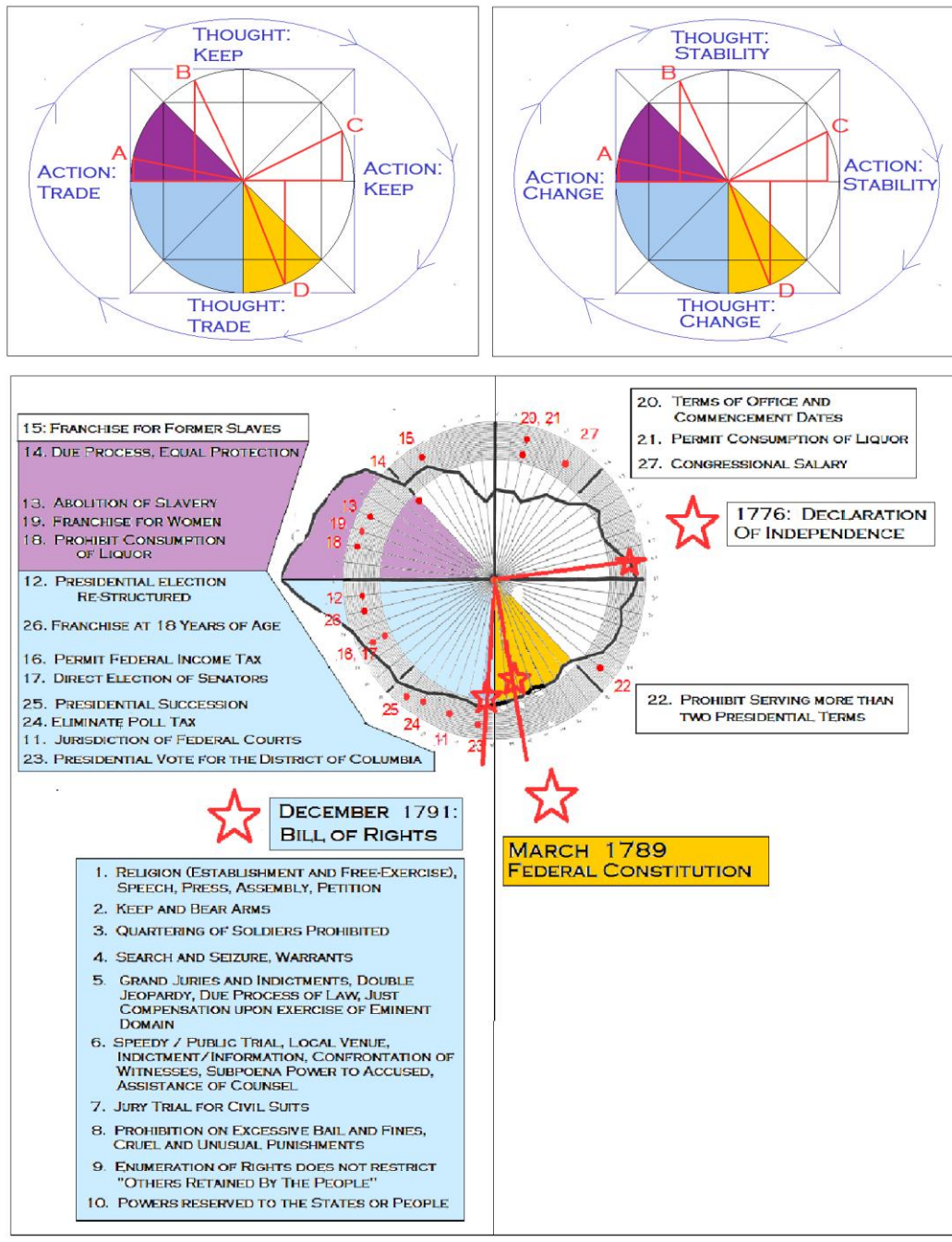
The northeast half of this model is quite different.

DIAGRAM 5-8.
CHANGE VS. STABILITY - NORTHEAST CORNER
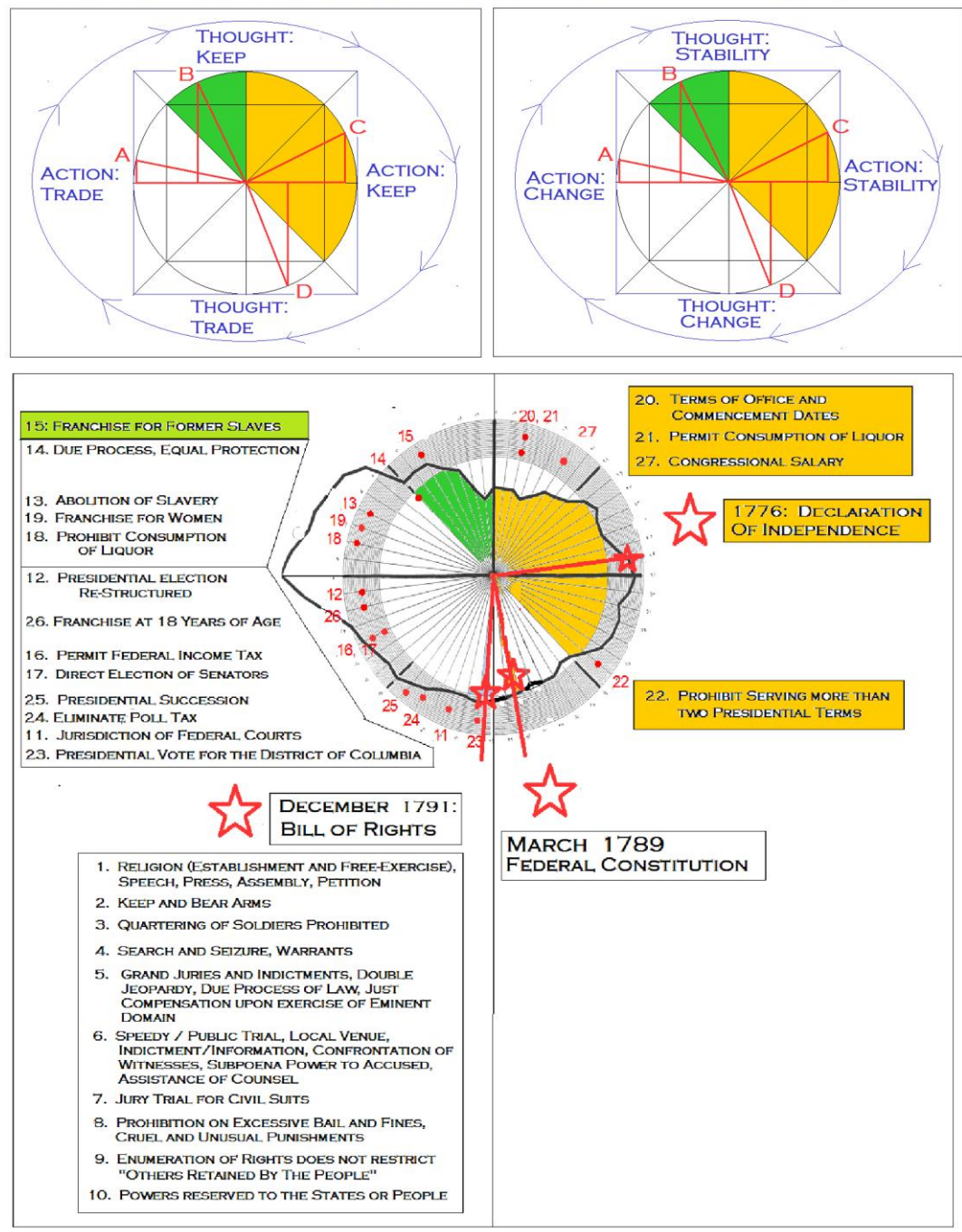
Only two constitutional amendments fall within a ten year span of "Year 29," i.e. 3 o'clock. Amendment 22 restricts a president from serving more than 2 terms in office (axis 31=1951) and enshrines in law a tradition begun by George Washington 154 years earlier when in 1797 he refused to run for a third term in office. Amendment 27 prohibits laws affecting Congressional salary from taking effect until the beginning of the next session of Congress. This amendment was proposed September 25, 1789 and enacted 203 years later in May 1992.

We might also consider the two remaining Amendments on the right hand side of the cycle. Both enacted in 1933, Amendment 20 determined the dates of term commencements for Congress and the President and Amendment 21 repealed the federal prohibition on consumption of alcohol. Amendment 20 was a purely administrative and Amendment 21 returned the country to a well-established social norm

It is of course possible to take any data set and superimpose upon it a spiral of any sort. The list of Amendments to the Federal Constitution is useful in this analysis because:

(1) each Amendment carries with it a specific date of adoption, thereby making placement in the cycle non-controversial,

(2) each Amendment engages the entire United States by virtue of the centrality of the Federal Constitution and the difficulties posed in their adoption,

(3) each Amendment declares in the clearest possible terms what is intended, albeit this interpretation remains subject to further interpretation by the courts, and

(4) each Amendment remains an influence upon continued American development. In many cases these Amendments are intended to direct the process of the economic future of the American people away from evils previously experienced (slavery, disenfranchisement of African-Americans, women and persons of draft age, resistance to federal taxation of income, addiction to alcohol, unjust use of governmental powers, etc.)

The numerous amendments on the left-hand side of the circuit above should be contrasted with one of the most fundamental documents of American economic history occurring on the right-hand side of the circuit, the Declaration of Independence of 1776. This document makes clear that the colonists did not perceive themselves as setting forth upon some new and novel declaration of rights. Rather they viewed themselves as collectively determined to continue to enjoy rights which they already possessed.

Regarding George III the colonists declared in their first five grievances:

He has refused his assent to laws, the most wholesome and necessary for the public good.

He has forbidden his governors to pass laws of immediate and pressing importance, unless suspended in their operation till his assent should be obtained; and when so suspended, he has utterly neglected to attend to them.

He has refused to pass other laws for the accommodation of large districts of people, unless those people would relinquish the right of representation in the legislature, a right inestimable to them and formidable to tyrants only.

He has called together legislative bodies at places unusual, uncomfortable, and distant from the depository of their public records, for the sole purpose of fatiguing them into compliance with his measures.

He has dissolved representative houses repeatedly, for opposing with manly firmness his invasions on the rights of the people.

The remainder of the Declaration of Independence describes in ever expanding detail the list of wrongs done by the king to his colonists. Each of these royal acts or omissions justified – at least in the minds of the signatory colonists – an immediate separation of the colonies from the crown in protection of long-held rights, customs and privileges.

4.3. Employment and Okun's Law under this Model

One must ask the mechanism by which these various waves are kept in check. According to Knotek 2007 the statistical pattern viewed is a regularity of the data, with no explanation being given for the recurrence of these proportions over time.

On the contrary, we may examine the "random-ness" of the variables published in Knotek 2007 and find a strict congruence with the 56-year cycle described herein.

As we examine the coefficients of Okun's Law under the analysis give so far and using the same color scheme for "Expansion" (blue), "Hyper-Inflation" (purple), "Collapse" (green) and "Consequences" (yellow) we have the following. Note below that the green portion "Collapse" has proven to be a formal historic period which is entirely predictable in nature. It would appear that the each of these sections of time have had a bearing on the manner in which Okun's Law has functioned via a connection to the underlying geometries implied.

DIAGRAM 5-9.
ROLLING REGRESSIONS WITH HISTORIC CONTEXT
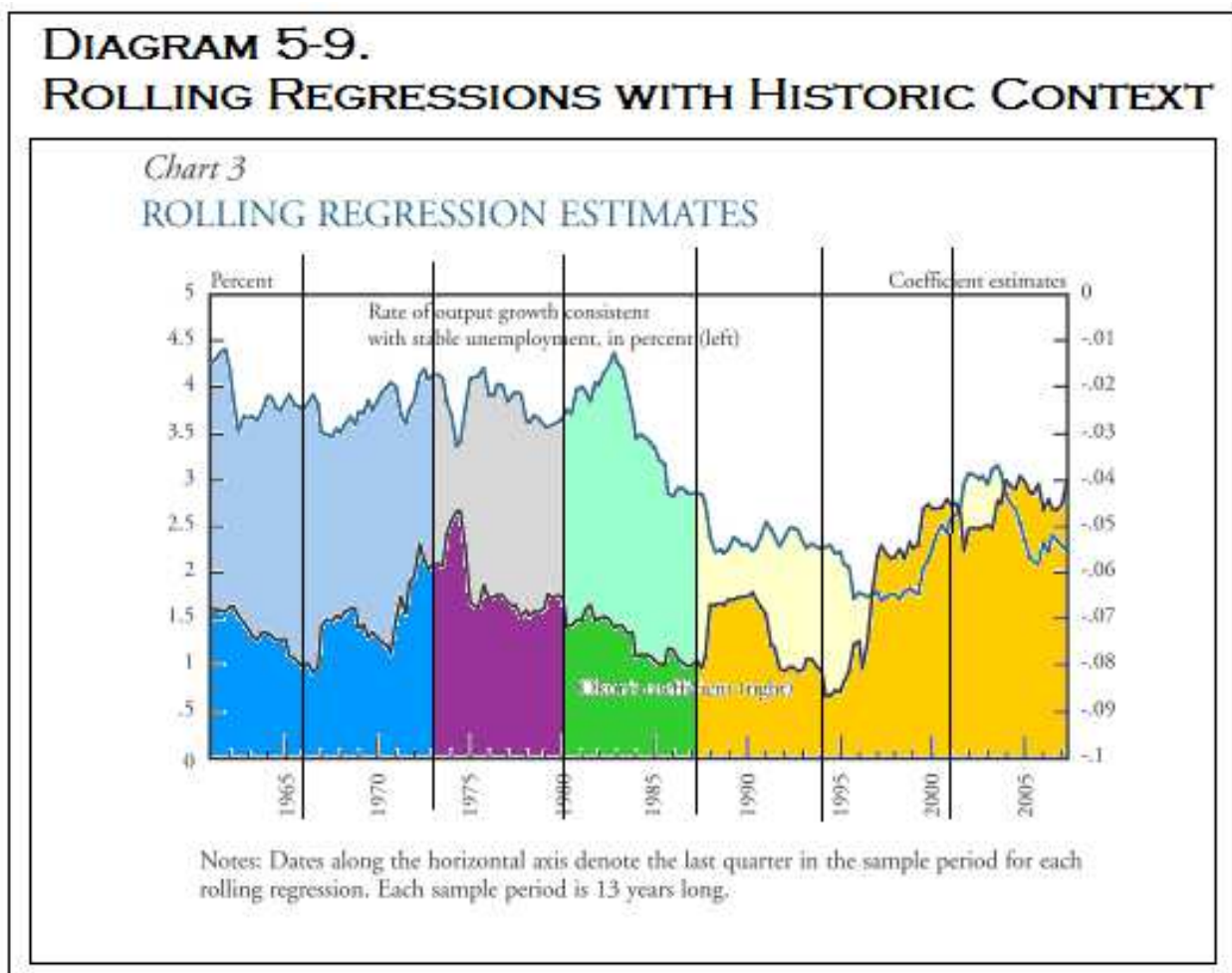
4.4. Speculation as to the nature of the cycle

We may now speculate as to the nature of the right-left division underlying the GNP Spiral.

For the purposes of this paper regarding American economic history, let us define a "*Belief-system*" as the constellation of ideas surrounding any principle of governance: a monarchy, the bourgeoisie, slavery, the relationship of labor to capital, etc. Second, let us define the term "*Revolution*" as a period of time when significant portions of a time-honored belief-systems are destroyed and when new and largely untried belief systems are inaugurated. Third, let us define in contradistinction to "Revolution" the term "*Consolidation*" as an opposing historical period in which honor or reverence are given to relatively recent belief-systems in a manner calculated to preserve and prolong them. It would appear that the left half of the circuit is "revolutionary" in character, while the right half is "consolidating" in character in the context of historic American belief systems.

In light of the numerous constitutional amendments adopted on the left-hand side of the circuit, and the virtual lack thereof on the right-hand side, let us label each of the segments of American History as follows:

DIAGRAM 5-10. "EVOLVING CONSOLIDATION" AND "CONSOLIDATION"
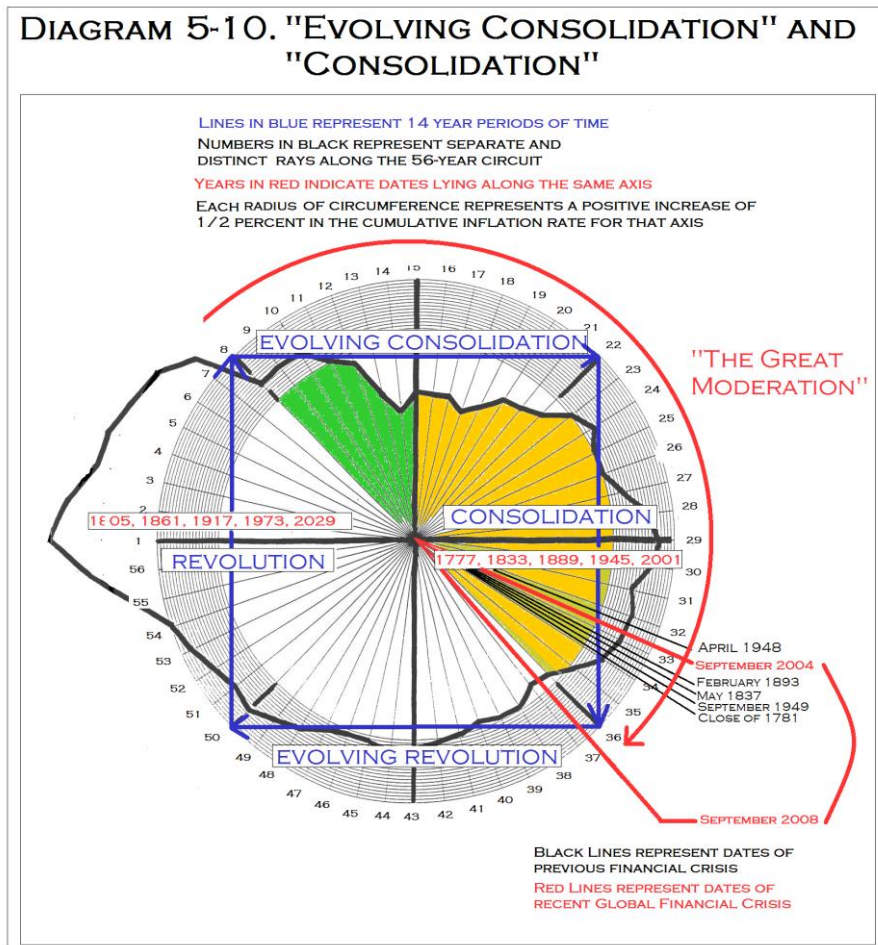
Note in the above that as each period of consolidation has come to its close, the United States has very predictably experienced a complete meltdown of the economy. This occurred most recently in September through December of 2008, the last months of the terms of George W. Bush. Prior events of similar magnitude are:

1.   The collapse of the colonial economy, circa 1781,
2.   The Panic of 1837,
3.   The Panic of 1893 and
4.   The Marshall Plan of 1948 and the events of 1949.

Two unusual characteristics of the recent global meltdown should be pointed out. These are (1) the difficulty of "dating" the recent crisis, and (2) the delay of the expected time of crisis. Let us consider these important points briefly.

DIAGRAM 5-11.
RECENT GLOBAL FINANCIAL CRISIS

1777, 1833, 1889, 1945, 2001

APRIL 1948
SEPTEMBER 2004
FEBRUARY 1893
MAY 1837
SEPTEMBER 1949
CLOSE OF 1781

EVOLUTION

SEPTEMBER 2008

BLACK LINES REPRESENT DATES OF PREVIOUS FINANCIAL CRISIS

RED LINES REPRESENT DATES OF RECENT GLOBAL FINANCIAL CRISIS
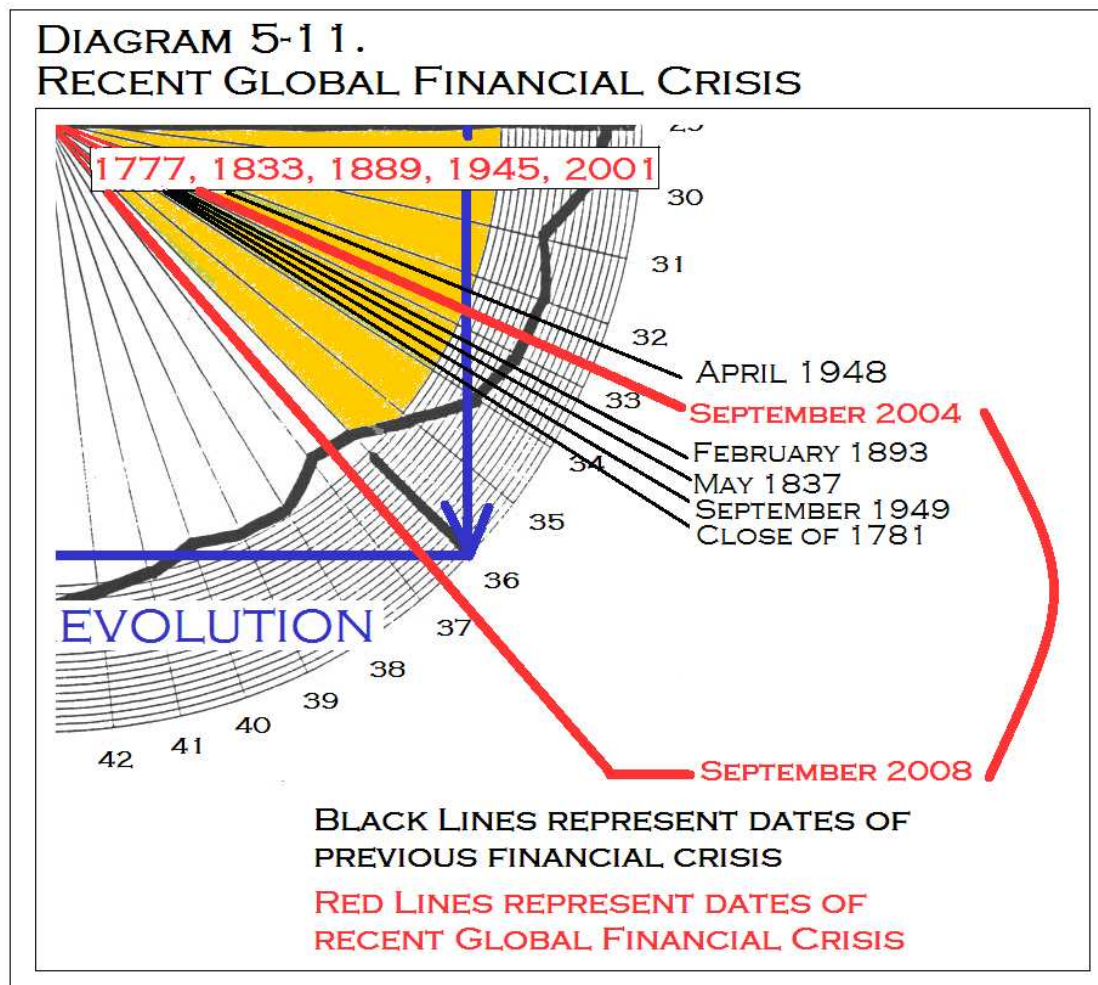
Each of the previous dates of "meltdown" clearly corresponded with events between axes 33 and 34. A description of these crises may be given simply by citing textbooks of American History.

Colonial meltdown of 1781
"In 1764 Parliament had outlawed paper money in the colonies altogether. Independence ended this restriction, and both the Continental Congress and the states printed large amounts of money during the Revolution, with inflationary results. To cite some examples, the Continental dollar became utterly worthless by 1781, and Virginia eventually called in its paper money at 1,000 to 1."[38]

Panic of 1837
"In 1836 the second United States Bank automatically came to the end of its checkered career and the country under the inspiration of the new democracy entered an epoch of "wild cat" finance. The very next year (May, 1837), a terrible business depression fell like a blight upon the land, bringing as usual more suffering to farmers and mechanics than to the "rich and wellborn"; but this calamity was likewise attributed by the masses to the machinations of the money power rather than to the conduct of their hero, President Jackson. Nothing would induce them to retrace their steps. For three decades a union of the South and West prevented a restoration of the centralized banking system. Not until the planting statesmen withdrew from Congress and the storm of the Civil War swept minor gusts before it were the ravages wrought by Jackson repaired by the directors of affairs in Washington."[39]

Panic of 1893
"The (Cleveland) Administration was not three months old when a series of bank failure and industrial collapses inaugurated the panic of (February) 1893. The treasury's gold reserve was depleted by an excess of imports and by liquidation of American securities in London after a panic there. Gold was subject to a steady drain by the monthly purchase of useless silver required by the Silver Purchase Act of 1890, and by the redemption of greenbacks which by law were promptly reissued and formed an "endless chain for conveying gold to Europe."[40]

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[38]   John A Garraty, *The American Nation, A History of the United States*, Harper-American Heritage Textbook, p. 144.
[39]   Charles A. Beard, Mary R. Beard, *The Rise of American Civilization*, New Edition, Macmillan Company, New York., p. 570-571.
[40]   Garraty, p. 795.

Reviewing the same axes for the years 1948-1949, we have, in addition to the creation of the Marshall Plan to rebuild post-war Europe (April 1948), the following:

1949
In 1949 a business recession occurred and prices declined slightly. (p. 819) … Further alarmed by the news, released in September 1949, that the Russians had produced an atomic bomb, Congress appropriated $1.5 billion to arm NATO and in 1951 General Eisenhower was recalled to active duty and placed in command of all NATO forces. (p. 785) … This (civil war in China) resulted in the total defeat of the nationalists; by the end of 1949 Mao ruled all China and Chiang's shattered armies had fled to sanctuary on the island of Formosa, now called Taiwan. This loss of over half a billion souls to communism caused an outburst of indignation in the United States and deeply divided the American people. Critics claimed that Truman had not backed the nationalists strongly enough and that he had stupidly underestimated both Mao's power and his dedication to the cause of world revolution. (p. 786)[41]

The recent Global Financial Crisis began when, in September 2004, the FBI reported that it had uncovered widespread fraud in the home mortgage market (axis 32). The date of this FBI report precedes the axes of the above mentioned crises, i.e. 1781, 1837, 1893 and 1948-1949, by a matter of months. However, and unlike previous crises, action to correct these frauds was not undertaken and the final implosion was delayed for four years, i.e. to September 2008, two months before the election of Barack Obama. Public reaction, not unlike previous moments along axis 33, has been extremely suspicious about the timing and origin of this world-wide panic. [42]

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[41] Garraty, p. 786.

[42] See e.g. House Bill 3995, presented by Representative Kaptur, November 3, 2009:

"(4) Fraud also played a decisive role in the Savings and Loan crisis (of the late 1980s and early 1990s). The FBI and Justice Department made prosecuting those elite frauds among its highest priorities. This took a massive commitment of FBI resources, but it produced the most successful prosecution of an epidemic of elite fraud in history--over 1,000 `priority' felony convictions of senior insiders, according to Professor William K. Black in his book `The Best Way to Rob a Bank is to Own One'.

(5) However, the FBI, because of its crippling personnel limitations, has been unable to assign sufficient FBI agents to investigate the current global financial crisis. The FBI identified the mortgage fraud `epidemic' in congressional testimony in September 2004. It had so few white-collar crime specialists available, however, that it was able to assign only 120 special agents to mortgage fraud cases-- less than one-eighth the agents it found essential to respond adequately to the huge, but far smaller, Savings and Loan crisis.

(6) Given the magnitude of the financial crisis of 2008 and the resulting losses and billions of taxpayer dollars spent to keep the financial system from collapsing, the FBI should have no less than 1,000 agents to address corporate, securities, and mortgage fraud located across the country, and, in addition, more forensic experts and Federal prosecutors to uncover the crimes committed and bring the perpetrators to justice."

To conclude our speculation as to the nature of this circuit brings us to a discussion of the current events of today. We are, today, at the dividing line within the yellow section marked below.

DIAGRAM 5-12.
"EVOLVING REVOLUTION" AND "REVOLUTION"

LINES IN BLUE REPRESENT 14 YEAR PERIODS OF TIME
NUMBERS IN BLACK REPRESENT SEPARATE AND DISTINCT RAYS ALONG THE 56-YEAR CIRCUIT
YEARS IN RED INDICATE DATES LYING ALONG THE SAME AXIS
EACH RADIUS OF CIRCUMFERENCE REPRESENTS A POSITIVE INCREASE OF 1/2 PERCENT IN THE CUMULATIVE INFLATION RATE FOR THAT AXIS

EVOLVING CONSOLIDATION
CONSOLIDATION
1805, 1861, 1917, 1973, 2029
1777, 1833, 1889, 1945, 2001
REVOLUTION
EVOLVING REVOLUTION
AUGUST 2012

The yellow portion of the above represents the beginning of an evolving revolutionary trend starting in 2008. This correlates to an impressive extent with the current difficulties faced by the United States in the Middle East. Note that as of the date of the publication of this article, the United States has attempted to deal with a number of revolutionary changes throughout the Arab world.

These have included but are not limited to: Tunisia, Egypt, Libya, Bahrain, Yemen, Syria, Morocco and Algeria. These events have become known popularly as "The Arab Spring." Chronologically, these were preceded by the 2009 Revolution in Iran. They have been joined since that time by protests, revolts and crackdowns in Tibet, China, England and Greece as well as a painful sovereign debt crisis in Europe with additional austerity measures generally anticipated. The fact that these events are taking place at the very beginning of the "Evolving Revolution" segment of American economic history may presage much greater events to come.

A strong correlation between the onset of inflation and the axes of this period has been described by this model. The graph above demonstrates the historic inflationary rise which typically accompanies this period of American economic history.

The amount of blue and purple given in the above development towards revolution represents inflation, the strength of which emerges most dramatically along the left-pointing axis at nine o'clock. These years represent very difficult times in the history of the United States – the coming of the war with Britain in 1812 during which the White House, the Capitol, the Library of Congress and the Treasury were burned to the ground (1814); the American Civil War beginning in 1861 ending in the assassination of President Lincoln in 1865; the First World War beginning for the United States in 1917; and the OPEC Embargo of 1973. This axis brings revolutionary times of great uncertainty, a forced re-reading of America's place in world history.

4.5. Predictions which may be made from this model

We have mentioned that there is only one point along the Unit Circle where Action is wholly aligned with Trading, i.e. the point at 9:00. All other points along the unit circle are similar to one another in that there is some "Y" component connected to some mental aspect of trading and/ or keeping the object in question. This mental aspect must include some possibility of cancelling the action contemplated. Consequently only at 9:00 o'clock is the possibility of a "Trade" wholly equivalent with Action, and at this point "Thought" is Zero and the Action Trading occurs.
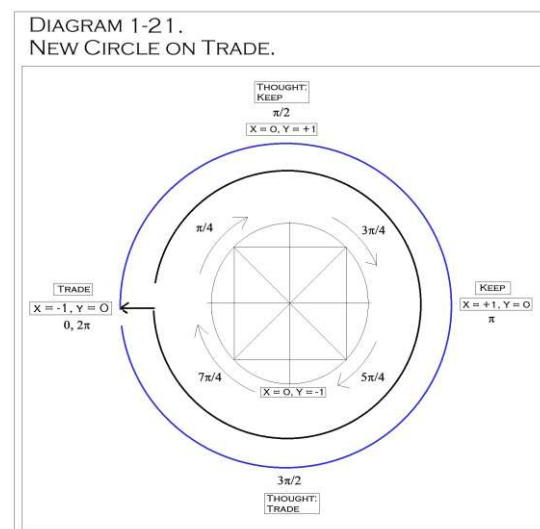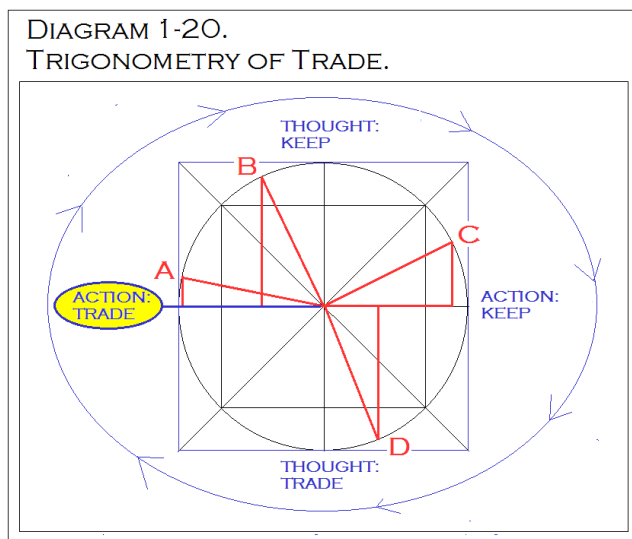
The unique aspect of this point along the circle creates an unavoidable change in the overall unit circle. The break which is presented at (x = = -1, y = 0) creates a new and unknown element in the unit circle itself. Once the trade is made, the situation is no longer the way it was. Something new has taken place.

In Essay Four we mentioned that

Regarding the diagram above we might consider as well extreme yet periodic events which cause these spikes in inflation noticed in Diagram 2-3. If a particular period of time fails to offer uniform resistance to production, or if the strength of production for some reason is particularly strong, the inherent productivity of the citizenry will create a bulge in productivity which must then be balanced out by a depression at some other time in the course of the circuit. Only in this fashion can a constant of growth be maintained in the face of unequal strengths of production and resistance to production. A wave must then develop over time during which this bulge will even out as time goes on until the next (generally unexpected) opportunity for unusual productivity occurs. If this damping price wave is placed along an x-axis, we have the following.

This same moment of trading, a crisis at the social level, was pointed out in Essay Part Fourne, as follows.

DIAGRAM 4-3.
PERIODS OF INFLATION
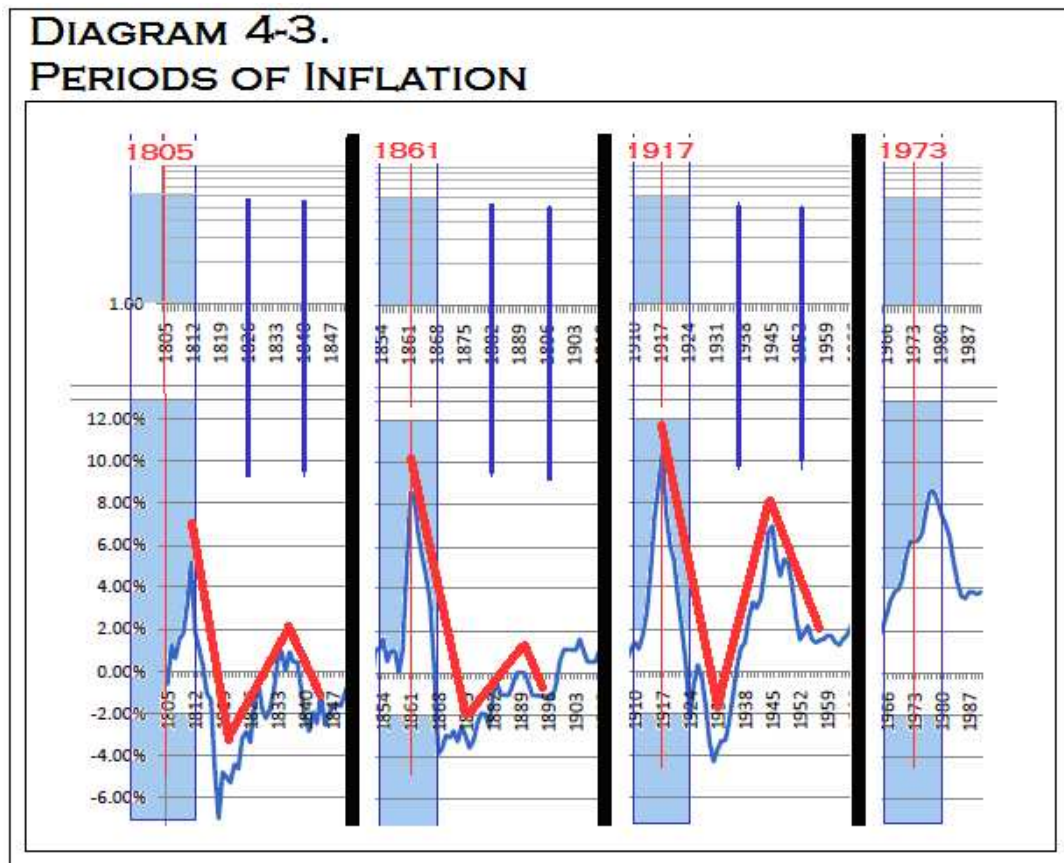
The development of a damping cosine curve is inherent in such a change, because through this new curve an adjustment is made to the underlying sine curve of established values.

DIAGRAM 5-13.
DAMPING COSINE CURVE
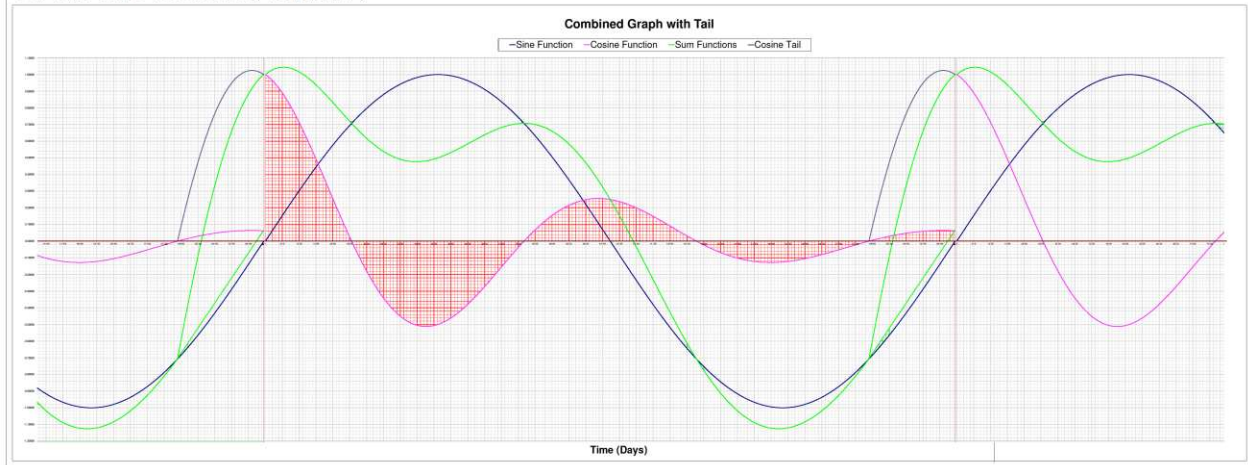
One door into the study of these relationships is to consider more carefully the 56-year "Political Economy Wave" and its intersections. Keeping the peak of the damping cosine wave at the same level as that of the original sine wave ("1") we may graph the damping to occur by halves. The equation which adds the previous sine curve together with this damping cosine curve is as follows:

$$g(y) = \underbrace{2^{\frac{1}{2} - \frac{2\left(y + \frac{1}{4}\pi\right)}{\pi}} \sin\left(2y + \frac{1}{2}\pi\right)}_{\text{DAMPING COSINE CURVE}} + \underbrace{\sin(y)}_{\text{SINE CURVE}}$$

If we associate this graph with a period of 20,454 days, beginning April 9, 1973, we may chart the

addition of these two waves together are as follows, with the peaks, troughs and intersections between the lines noted.[43] These are:

     (A)   the beginning point,
     (B)   the first peak, wherein positive y-values is at its greatest point,
     (E)   the first trough,
     (H)   the second peak,
     (M)   the point wherein the wave passes from positive y-values to negative values,
     (P)   the second trough (P), wherein negative y-values is at its greatest point and
     (X)   the point wherein the wave passes from negative y-values to positive without the introduction of a new cosine wave.
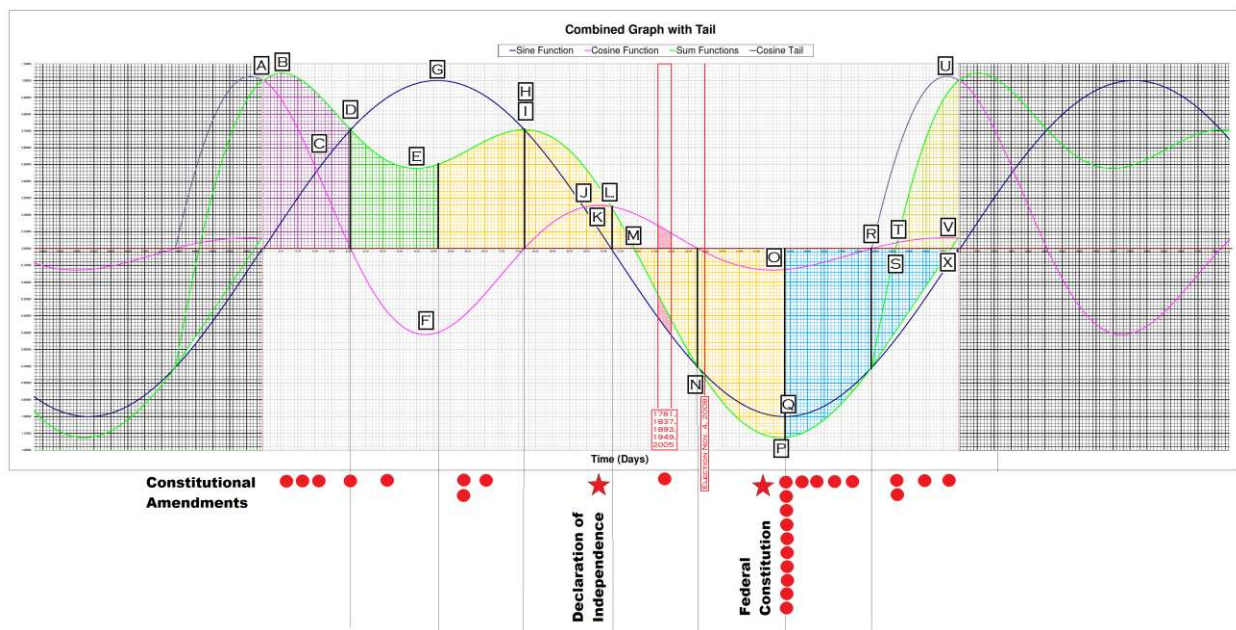
The red rectangle above represents the year 2005, a date associated with previous financial political-economic crises coming in 56-year increments in 1781, 1837, 1893 and 1949. The vertical red line represents the election of November, 2008 at which point Senator Barack Obama was elected President of the United States in the midst of a global financial crisis.

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[43]   The addition (in pale green below) of a pre-cursive half-cosine wave has been added to further the study of this wave as it relates to the possibility of the expression of this wave over time.

CONCLUSION

The reader may now return to the Preface where a brief synopsis was given as to the points of crisis calculated by this model. Although a large number of potential points have been considered and investigated, only seven – A, B, E, H, M, P and X – appear to be recurring points of key historic interest.

The techniques used in these essays give researchers a clear set of empirical measurements to use in their studies. These measurements may be tested by considering the accuracy of the predictions made. If this model tracks accurately the development of the United States, then it may be of assistance in the understanding of the role played by consciousness in the physical sciences as well.

Scott A. Albers
Great Falls, Montana
February 15, 2013

Appendices

Charts One and Two of Knotek 2007 were based upon data which was constructed by manipulating data originally taken from the St. Louis Fed's FRED database. The change in unemployment (du) is the December level of the unemployment rate in a given year minus the December level of the previous year, and the GDP growth rate (dy) is the percent change in GDP from the fourth quarter of a given year over the fourth quarter of the previous year.

As to unemployment data, the Bureau of Economic Analysis now uses 2005 chain weights. For annual data, the change in the unemployment rate is the current December minus the previous December, and GDP growth is 100*((GDP in the fourth quarter of this year)/(GDP in the fourth quarter of last year)-1). For quarterly data, the change in the unemployment rate is the difference between subsequent quarterly averages, while the BEA gives a formula for computing seasonally adjusted annualized growth rates.

Knotek's Annual Data, Email of July 28, 2011

	dy	du
1949	-1.69481	2.6
1950	13.43641	-2.3
1951	5.165233	-1.2
1952	5.112117	-0.4
1953	0.425678	1.8
1954	2.694275	0.5
1955	6.523389	-0.8
1956	1.834944	0
1957	0.26241	1
1958	2.420938	1
1959	4.88075	-0.9
1960	0.552262	1.3
1961	6.283822	-0.6
1962	4.111255	-0.5
1963	5.321168	0
1964	5.12163	-0.5
1965	8.51134	-1
1966	4.310711	-0.2
1967	2.460902	0
1968	4.940026	-0.4
1969	2.012459	0.1
1970	-0.17258	2.6
1971	4.470982	-0.1
1972	6.894269	-0.8
1973	4.15843	-0.3
1974	-1.92989	2.3
1975	2.539113	1
1976	4.247578	-0.4
1977	5.032064	-1.4
1978	6.689095	-0.4
1979	1.310001	0
1980	-0.04995	1.2
1981	1.17837	1.3
1982	-1.39834	2.3
1983	7.720914	-2.5
1984	5.579107	-1
1985	4.171185	-0.3
1986	2.842924	-0.4
1987	4.481766	-0.9
1988	3.659866	-0.4
1989	2.661858	0.1
1990	0.654255	0.9
1991	1.090873	1
1992	4.145874	0.1
1993	2.505805	-0.9
1994	4.113965	-1
1995	2.017204	0.1
1996	4.420611	-0.2
1997	4.342077	-0.7
1998	4.510997	-0.3
1999	4.698444	-0.4
2000	2.239662	-0.1
2001	0.225533	1.8
2002	1.874874	0.3
2003	3.676776	-0.3
2004	3.40021	-0.3
2005	3.149803	-0.5
2006	3.127967	-0.4

Knotek's Quarterly Data, Email of November 30, 2011

Quarterly Figure

	dy	du_avg
1948.2	7.242819	-0.06667
1948.3	2.33069	0.1
1948.4	0.946452	0.066667
1949.1	-5.8502	0.833333
1949.2	-1.17043	1.2
1949.3	4.571555	0.833333
1949.4	-4.01886	0.266667
1950.1	17.45697	-0.56667
1950.2	12.44685	-0.83333
1950.3	16.62782	-0.93333
1950.4	7.493361	-0.4
1951.1	4.934907	-0.73333
1951.2	6.972653	-0.4
1951.3	8.229388	0.066667
1951.4	0.681763	0.2
1952.1	4.241951	-0.3
1952.2	0.264934	-0.1
1952.3	2.629817	0.266667
1952.4	13.80097	-0.4
1953.1	7.75058	-0.13333
1953.2	3.069825	-0.13333
1953.3	-2.39934	0.166667
1953.4	-6.16277	0.966667
1954.1	-1.95385	1.566667
1954.2	0.372631	0.533333
1954.3	4.495923	0.166667
1954.4	8.153291	-0.63333
1955.1	12.02633	-0.6
1955.2	6.710869	-0.33333
1955.3	5.443469	-0.3
1955.4	2.148374	0.133333
1956.1	-1.85749	-0.2
1956.2	3.205905	0.166667
1956.3	-0.47861	-0.06667
1956.4	6.686428	-1E-15
1957.1	2.436114	-0.2
1957.2	-0.9875	0.166667
1957.3	3.962372	0.133333
1957.4	-4.16299	0.7
1958.1	-10.4351	1.366667
1958.2	2.388603	1.066667
1958.3	9.560821	-0.33333
1958.4	9.524235	-0.96667
1959.1	7.871279	-0.53333
1959.2	10.93633	-0.73333
1959.3	-0.30911	0.166667
1959.4	1.42571	0.333333
1960.1	9.202709	-0.46667
1960.2	-1.98708	0.1
1960.3	0.62426	0.3
1960.4	-5.08214	0.733333
1961.1	2.445174	0.533333
1961.2	7.728866	0.2
1961.3	6.636591	-0.23333
1961.4	8.42734	-0.56667
1962.1	7.385135	-0.56667
1962.2	4.446892	-0.1
1962.3	3.728473	0.033333
1962.4	0.984111	-0.03333

	dy	du_avg
1963.1	5.344779	0.233333
1963.2	5.094721	-0.03333
1963.3	7.743873	-0.23333
1963.4	3.151647	0.066667
1964.1	9.274181	-0.1
1964.2	4.731776	-0.26667
1964.3	5.56688	-0.2
1964.4	1.075206	-0.03333
1965.1	10.20532	-0.06667
1965.2	5.515603	-0.23333
1965.3	8.364001	-0.3
1965.4	10.02623	-0.26667
1966.1	10.14659	-0.23333
1966.2	1.395016	-0.03333
1966.3	2.662104	-0.06667
1966.4	3.256599	-0.06667
1967.1	3.588677	0.133333
1967.2	0.023096	0
1967.3	3.213253	-0.03333
1967.4	3.058699	0.1
1968.1	8.501162	-0.16667
1968.2	6.958747	-0.16667
1968.3	2.755597	-0.03333
1968.4	1.697081	-0.13333
1969.1	6.456197	0
1969.2	1.146166	0.033333
1969.3	2.501255	0.133333
1969.4	-1.8787	0
1970.1	-0.66741	0.6
1970.2	0.757461	0.6
1970.3	3.59394	0.4
1970.4	-4.21533	0.666667
1971.1	11.56607	0.1
1971.2	2.275839	-0.03333
1971.3	3.20833	0.133333
1971.4	1.148736	-0.1
1972.1	7.299849	-0.16667
1972.2	9.78529	-0.06667
1972.3	3.86707	-0.13333
1972.4	6.707894	-0.2
1973.1	10.54887	-0.43333
1973.2	4.707755	0
1973.3	-2.11387	-0.13333
1973.4	3.877955	-0.03333
1974.1	-3.42169	0.366667
1974.2	1.158294	0.066667
1974.3	-3.81724	0.433333
1974.4	-1.56076	0.966667
1975.1	-4.69929	1.666667
1975.2	2.958451	0.6
1975.3	6.949137	-0.4
1975.4	5.347146	-0.16667
1976.1	9.313145	-0.56667
1976.2	3.013362	-0.16667
1976.3	1.929798	0.166667
1976.4	2.895596	0.033333
1977.1	4.921894	-0.26667
1977.2	8.087778	-0.36667
1977.3	7.355737	-0.23333
1977.4	-0.04152	-0.23333

	dy	du_avg
1978.1	1.293793	-0.33333
1978.2	16.7223	-0.33333
1978.3	4.001975	0.033333
1978.4	5.366331	-0.13333
1979.1	0.78088	-0.03333
1979.2	0.381319	-0.16667
1979.3	2.911526	0.166667
1979.4	1.184553	0.1
1980.1	1.281886	0.333333
1980.2	-7.83339	1.033333
1980.3	-0.66294	0.333333
1980.4	7.625528	-0.26667
1981.1	8.354069	0.033333
1981.2	-3.0838	-0.03333
1981.3	4.926997	2E-15
1981.4	-4.89095	0.833333
1982.1	-6.39895	0.6
1982.2	2.165284	0.6
1982.3	-1.50538	0.466667
1982.4	0.355329	0.766667
1983.1	5.02475	-0.3
1983.2	9.331896	-0.23333
1983.3	8.136903	-0.76667
1983.4	8.439536	-0.83333
1984.1	8.052759	-0.66667
1984.2	7.064234	-0.43333
1984.3	3.94821	0
1984.4	3.327199	-0.13333
1985.1	3.744883	-0.06667
1985.2	3.461942	0.066667
1985.3	6.399978	-0.1
1985.4	3.110183	-0.16667
1986.1	3.880484	0
1986.2	1.594653	0.133333
1986.3	3.887249	-0.2
1986.4	2.030636	-0.13333
1987.1	2.657578	-0.23333
1987.2	4.47216	-0.33333
1987.3	3.679865	-0.26667
1987.4	7.170687	-0.16667
1988.1	1.969949	-0.13333
1988.2	5.182817	-0.23333
1988.3	2.152959	0
1988.4	5.383985	-0.13333
1989.1	4.121433	-0.13333
1989.2	2.650951	0.033333
1989.3	2.879728	0
1989.4	1.019115	0.133333
1990.1	4.700254	-0.06667
1990.2	1.027544	0.033333
1990.3	0.028052	0.366667
1990.4	-2.9894	0.433333
1991.1	-2.02488	0.466667
1991.2	2.621683	0.233333
1991.3	1.944451	0.033333
1991.4	1.889462	0.233333
1992.1	4.207894	0.266667
1992.2	3.913265	0.233333
1992.3	3.982549	0.033333
1992.4	4.480734	-0.26667

	dy	du_avg
1993.1	0.484052	-0.23333
1993.2	2.042349	-0.06667
1993.3	2.069893	-0.26667
1993.4	5.491772	-0.16667
1994.1	4.131972	-0.06667
1994.2	5.31865	-0.36667
1994.3	2.260556	-0.2
1994.4	4.770358	-0.36667
1995.1	1.116369	-0.16667
1995.2	0.71929	0.2
1995.3	3.299958	0
1995.4	2.957835	-0.1
1996.1	2.850486	-0.03333
1996.2	6.719298	-0.03333
1996.3	3.39536	-0.23333
1996.4	4.759779	0.066667
1997.1	3.129113	-0.1
1997.2	6.217645	-0.23333
1997.3	5.074293	-0.13333
1997.4	2.982514	-0.2
1998.1	4.500149	-0.03333
1998.2	2.671779	-0.23333
1998.3	4.68705	0.133333
1998.4	6.215284	-0.1
1999.1	3.438473	-0.13333
1999.2	3.351939	-0.03333
1999.3	4.749838	-0.03333
1999.4	7.301756	-0.16667
2000.1	1.017186	-0.03333
2000.2	6.432867	-0.1
2000.3	-0.45819	0.066667
2000.4	2.094202	-0.1
2001.1	-0.4886	0.333333
2001.2	1.232927	0.166667
2001.3	-1.39784	0.433333
2001.4	1.585661	0.666667
2002.1	2.744245	0.2
2002.2	2.194778	0.133333
2002.3	2.37746	-0.1
2002.4	0.20232	0.133333
2003.1	1.201917	0
2003.2	3.469084	0.266667
2003.3	7.486494	0
2003.4	2.653249	-0.3
2004.1	2.959586	-0.13333
2004.2	3.481713	-0.1
2004.3	3.602232	-0.16667
2004.4	2.548063	-0.03333
2005.1	3.072837	-0.13333
2005.2	2.812687	-0.2
2005.3	4.461999	-0.06667
2005.4	1.193643	-0.03333
2006.1	4.820432	-0.23333
2006.2	2.442263	-0.1
2006.3	1.065549	0.066667
2006.4	2.090875	-0.23333
2007.1	0.601589	0.033333
2007.2	3.382239	0

2.963692

Change in Annual Unemployment vs. Change in Annual GDP

Quarterly GDP, Bureau of Economic Analysis
Table 1.1.6. Real Gross Domestic Product, Chained Dollars
[Billions of chained (2000) dollars]; Seasonally adjusted at annual rates
Quarterly data from 1947 To 2007
Bureau of Economic Analysis
Data published September 27, 2007
File created 9/26/2007 9:47:04 AM

						Albers' GDP Calculations from Table 1.1.6, September 27, 2007				Knotek's Annual Data as provided through correspondence	
		Gross domestic product				Quarter 4 divided by Quarter 4 Minus 1		Multiply 100			
							n=m-1	n=mx100		dy	du
1947	4	1,590.9									
1948	4	1,658.0		1948	4	1.042177	n=m-1	n=mx100			
1949	4	1,629.9		1949	4	0.983052	-0.01695	-1.694813	1949	-1.69481	2.6
1950	4	1,848.9		1950	4	1.134364	0.134364	13.436407	1950	13.43641	-2.3
1951	4	1,944.4		1951	4	1.051652	0.051652	5.1652334	1951	5.165233	-1.2
1952	4	2,043.8		1952	4	1.051121	0.051121	5.1121168	1952	5.112117	-0.4
1953	4	2,052.5		1953	4	1.004257	0.004257	0.4256777	1953	0.425678	1.8
1954	4	2,107.8		1954	4	1.026943	0.026943	2.6942753	1954	2.694275	0.5
1955	4	2,245.3		1955	4	1.065234	0.065234	6.5233893	1955	6.523389	-0.8
1956	4	2,286.5		1956	4	1.018349	0.018349	1.8349441	1956	1.834944	0
1957	4	2,292.5		1957	4	1.002624	0.002624	0.2624098	1957	0.26241	1
1958	4	2,348.0		1958	4	1.024209	0.024209	2.420938	1958	2.420938	1
1959	4	2,462.6		1959	4	1.048807	0.048807	4.8807496	1959	4.88075	-0.9
1960	4	2,476.2		1960	4	1.005523	0.005523	0.5522618	1960	0.552262	1.3
1961	4	2,631.8		1961	4	1.062838	0.062838	6.283822	1961	6.283822	-0.6
1962	4	2,740.0		1962	4	1.041113	0.041113	4.1112547	1962	4.111255	-0.5
1963	4	2,885.8		1963	4	1.053212	0.053212	5.3211679	1963	5.321168	0
1964	4	3,033.6		1964	4	1.051216	0.051216	5.1216301	1964	5.12163	-0.5
1965	4	3,291.8		1965	4	1.085113	0.085113	8.5113397	1965	8.51134	-1
1966	4	3,433.7		1966	4	1.043107	0.043107	4.3107115	1966	4.310711	-0.2
1967	4	3,518.2		1967	4	1.024609	0.024609	2.4609022	1967	2.460902	0
1968	4	3,692.0		1968	4	1.0494	0.0494	4.9400261	1968	4.940026	-0.4
1969	4	3,766.3		1969	4	1.020125	0.020125	2.0124594	1969	2.012459	0.1
1970	4	3,759.8		1970	4	0.998274	-0.00173	-0.1725832	1970	-0.17258	2.6
1971	4	3,927.9		1971	4	1.04471	0.04471	4.4709825	1971	4.470982	-0.1
1972	4	4,198.7		1972	4	1.068943	0.068943	6.8942692	1972	6.894269	-0.8
1973	4	4,373.3		1973	4	1.041584	0.041584	4.15843	1973	4.15843	-0.3
1974	4	4,288.9		1974	4	0.980701	-0.0193	-1.9298928	1974	-1.92989	2.3
1975	4	4,397.8		1975	4	1.025391	0.025391	2.5391126	1975	2.539113	1
1976	4	4,584.6		1976	4	1.042476	0.042476	4.2475783	1976	4.247578	-0.4
1977	4	4,815.3		1977	4	1.050321	0.050321	5.0320639	1977	5.032064	-1.4
1978	4	5,137.4		1978	4	1.066891	0.066891	6.6890952	1978	6.689095	-0.4
1979	4	5,204.7		1979	4	1.0131	0.0131	1.310012	1979	1.310001	0
1980	4	5,202.1		1980	4	0.9995	-0.0005	-0.0499548	1980	-0.04995	1.2
1981	4	5,263.4		1981	4	1.011784	0.011784	1.1783703	1981	1.17837	1.3
1982	4	5,189.8		1982	4	0.986017	-0.01398	-1.3983357	1982	-1.39834	2.3
1983	4	5,590.5		1983	4	1.077209	0.077209	7.7209141	1983	7.720914	-2.5
1984	4	5,902.4		1984	4	1.055791	0.055791	5.5791074	1984	5.579107	-1
1985	4	6,148.6		1985	4	1.041712	0.041712	4.1711846	1985	4.171185	-0.3
1986	4	6,323.4		1986	4	1.028429	0.028429	2.8429236	1986	2.842924	-0.4
1987	4	6,606.8		1987	4	1.044818	0.044818	4.4817661	1987	4.481766	-0.9
1988	4	6,848.6		1988	4	1.036599	0.036599	3.6598656	1988	3.659866	-0.4
1989	4	7,030.9		1989	4	1.026619	0.026619	2.6618579	1989	2.661858	0.1
1990	4	7,076.9		1990	4	1.006543	0.006543	0.6542548	1990	0.654255	0.9
1991	4	7,154.1		1991	4	1.010909	0.010909	1.0908731	1991	1.090873	1
1992	4	7,450.7		1992	4	1.041459	0.041459	4.1458744	1992	4.145874	0.1
1993	4	7,637.4		1993	4	1.025058	0.025058	2.5058048	1993	2.505805	-0.9
1994	4	7,951.6		1994	4	1.04114	0.04114	4.1139655	1994	4.113965	-1
1995	4	8,112.0		1995	4	1.020172	0.020172	2.0172041	1995	2.017204	0.1
1996	4	8,470.6		1996	4	1.044206	0.044206	4.4206114	1996	4.420611	-0.2
1997	4	8,838.4		1997	4	1.043421	0.043421	4.3420773	1997	4.342077	-0.7
1998	4	9,237.1		1998	4	1.04511	0.04511	4.5109975	1998	4.510997	-0.3
1999	4	9,671.1		1999	4	1.046984	0.046984	4.6984443	1999	4.698444	-0.4
2000	4	9,887.7		2000	4	1.022397	0.022397	2.2396625	2000	2.239662	-0.1
2001	4	9,910.0		2001	4	1.002255	0.002255	0.2255327	2001	0.225533	1.8
2002	4	10,095.8		2002	4	1.018749	0.018749	1.8748739	2002	1.874874	0.3
2003	4	10,467.0		2003	4	1.036768	0.036768	3.6767765	2003	3.676776	-0.3
2004	4	10,796.4		2004	4	1.03147	0.03147	3.1470335	2004	3.40021	-0.3
2005	4	11,107.2		2005	4	1.028787	0.028787	2.8787374	2005	3.149803	-0.5
2006	4	11,395.5		2006	4	1.025956	0.025956	2.5956137	2006	3.127967	-0.4

$y = -0.3499550x + 1.2091387$

Table 1.1.6. Real Gross Domestic Product, Chained Dollars

[Billions of chained (2000) dollars]; Seasonally adjusted at annual rates
Quarterly data from 1947 To 2007
Bureau of Economic Analysis
Data published September 27, 2007
File created 9/26/2007 9:47:04 AM

Year	Qtr	Gross domestic product	Current Quarter Divided by Previous Quarter	Seasonally Adjusted Annualized Growth Rate ([Current Quarter divided by Previous Quarter]^4 minus 1)	Copy of Previous Column (Values Only)	Make Column F a Percent (Multiply by 100)
1947	1	1,570.5				
1947	2	1,568.7	0.999	-0.00458	-0.00458	-0.45767
1947	3	1,568.0	1.000	-0.00178	-0.00178	-0.17837
1947	4	1,590.9	1.015	0.05971	0.05971	5.97106
1948	1	1,616.1	1.016	0.06488	0.06488	6.48818
1948	2	1,644.6	1.018	0.07243	0.07243	7.24282
1948	3	1,654.5	1.006	0.02331	0.02331	2.33069
1948	4	1,658.0	1.002	0.00946	0.00946	0.94645
1949	1	1,633.2	0.985	-0.05850	-0.05850	-5.85020
1949	2	1,628.4	0.997	-0.01170	-0.01170	-1.17043
1949	3	1,646.7	1.011	0.04572	0.04572	4.57156
1949	4	1,629.9	0.990	-0.04019	-0.04019	-4.01806
1950	1	1,696.8	1.041	0.17457	0.17457	17.45697
1950	2	1,747.3	1.030	0.12447	0.12447	12.44685
1950	3	1,815.8	1.039	0.16628	0.16628	16.62782
1950	4	1,848.9	1.018	0.07493	0.07493	7.49336
1951	1	1,871.3	1.012	0.04935	0.04935	4.93491
1951	2	1,903.1	1.017	0.06973	0.06973	6.97265
1951	3	1,941.1	1.020	0.08229	0.08229	8.22939
1951	4	1,944.4	1.002	0.00682	0.00682	0.68176
1952	1	1,964.7	1.010	0.04242	0.04242	4.24195
1952	2	1,966.0	1.001	0.00265	0.00265	0.26493
1952	3	1,978.8	1.007	0.02630	0.02630	2.62982
1952	4	2,043.8	1.033	0.13801	0.13801	13.80097
1953	1	2,082.3	1.019	0.07751	0.07751	7.75058
1953	2	2,098.1	1.008	0.03070	0.03070	3.06982
1953	3	2,085.4	0.994	-0.02399	-0.02399	-2.39934
1953	4	2,052.5	0.984	-0.06163	-0.06163	-6.16277
1954	1	2,042.4	0.995	-0.01954	-0.01954	-1.95385
1954	2	2,044.3	1.001	0.00373	0.00373	0.37263
1954	3	2,066.9	1.011	0.04496	0.04496	4.49592
1954	4	2,107.8	1.020	0.08153	0.08153	8.15329
1955	1	2,168.5	1.029	0.12026	0.12026	12.02633
1955	2	2,204.0	1.016	0.06711	0.06711	6.71087
1955	3	2,233.4	1.013	0.05443	0.05443	5.44347
1955	4	2,245.3	1.005	0.02148	0.02148	2.14837
1956	1	2,234.8	0.995	-0.01857	-0.01857	-1.85749
1956	2	2,252.5	1.008	0.03206	0.03206	3.20591
1956	3	2,249.8	0.999	-0.00479	-0.00479	-0.47861
1956	4	2,286.5	1.016	0.06686	0.06686	6.68643
1957	1	2,300.3	1.006	0.02436	0.02436	2.43611
1957	2	2,294.6	0.998	-0.00987	-0.00987	-0.98750
1957	3	2,317.0	1.010	0.03962	0.03962	3.96237
1957	4	2,292.5	0.989	-0.04163	-0.04163	-4.16299
1958	1	2,230.2	0.973	-0.10435	-0.10435	-10.43550
1958	2	2,243.4	1.006	0.02389	0.02389	2.38860
1958	3	2,295.2	1.023	0.09561	0.09561	9.56082
1958	4	2,348.0	1.023	0.09524	0.09524	9.52424
1959	1	2,392.3	1.019	0.07871	0.07871	7.87128
1959	2	2,455.8	1.026	0.10936	0.10936	10.93633
1959	3	2,453.9	0.999	-0.00309	-0.00309	-0.30911
1959	4	2,462.6	1.004	0.01426	0.01426	1.42571
1960	1	2,517.4	1.022	0.09203	0.09203	9.20271
1960	2	2,504.8	0.995	-0.01987	-0.01987	-1.98708
1960	3	2,508.7	1.002	0.00624	0.00624	0.62426
1960	4	2,476.2	0.987	-0.05082	-0.05082	-5.08214
1961	1	2,491.2	1.006	0.02445	0.02445	2.44517
1961	2	2,538.0	1.019	0.07729	0.07729	7.72887
1961	3	2,579.1	1.016	0.06637	0.06637	6.63659
1961	4	2,631.8	1.020	0.08427	0.08427	8.42734
1962	1	2,679.1	1.018	0.07385	0.07385	7.38513
1962	2	2,708.4	1.011	0.04447	0.04447	4.44609
1962	3	2,733.3	1.009	0.03728	0.03728	3.72847
1962	4	2,740.0	1.002	0.00984	0.00984	0.98411
1963	1	2,775.9	1.013	0.05345	0.05345	5.34478
1963	2	2,810.6	1.013	0.05095	0.05095	5.09472
1963	3	2,863.5	1.019	0.07744	0.07744	7.74387
1963	4	2,885.8	1.008	0.03152	0.03152	3.15165
1964	1	2,950.5	1.022	0.09274	0.09274	9.27498
1964	2	2,984.8	1.012	0.04732	0.04732	4.73178
1964	3	3,025.5	1.014	0.05567	0.05567	5.56688
1964	4	3,033.6	1.003	0.01075	0.01075	1.07521
1965	1	3,108.2	1.025	0.10205	0.10205	10.20532
1965	2	3,150.2	1.014	0.05516	0.05516	5.51560
1965	3	3,214.1	1.020	0.08364	0.08364	8.36400
1965	4	3,291.8	1.024	0.10026	0.10026	10.02623
1966	1	3,372.3	1.024	0.10147	0.10147	10.14659
1966	2	3,384.0	1.003	0.01395	0.01395	1.39502
1966	3	3,406.3	1.007	0.02662	0.02662	2.66210
1966	4	3,433.7	1.008	0.03257	0.03257	3.25660
1967	1	3,464.1	1.009	0.03589	0.03589	3.58868
1967	2	3,464.3	1.000	0.00023	0.00023	0.02310
1967	3	3,491.8	1.008	0.03213	0.03213	3.21325
1967	4	3,598.2	1.008	0.03059	0.03059	3.05870
1968	1	3,590.7	1.021	0.08501	0.08501	8.50116
1968	2	3,651.6	1.017	0.06959	0.06959	6.95875
1968	3	3,676.5	1.007	0.02756	0.02756	2.75560
1968	4	3,692.0	1.004	0.01697	0.01697	1.69708
1969	1	3,750.2	1.016	0.06456	0.06456	6.45620
1969	2	3,760.9	1.003	0.01146	0.01146	1.14617
1969	3	3,784.2	1.006	0.02501	0.02501	2.50125
1969	4	3,766.3	0.995	-0.01879	-0.01879	-1.87870
1970	1	3,760.0	0.998	-0.00667	-0.00667	-0.66741
1970	2	3,767.1	1.002	0.00757	0.00757	0.75746
1970	3	3,800.5	1.009	0.03594	0.03594	3.59394
1970	4	3,759.8	0.989	-0.04215	-0.04215	-4.21533
1971	1	3,864.1	1.028	0.11567	0.11567	11.56667
1971	2	3,885.9	1.006	0.02276	0.02276	2.27584
1971	3	3,916.7	1.008	0.03208	0.03208	3.20833
1971	4	3,927.9	1.003	0.01149	0.01149	1.14874
1972	1	3,997.7	1.018	0.07300	0.07300	7.29985
1972	2	4,092.1	1.024	0.09785	0.09785	9.78529
1972	3	4,131.1	1.010	0.03867	0.03867	3.86707
1972	4	4,198.7	1.016	0.06708	0.06708	6.70789
1973	1	4,305.3	1.025	0.10549	0.10549	10.54887
1973	2	4,355.1	1.012	0.04708	0.04708	4.70776
1973	3	4,331.9	0.995	-0.02114	-0.02114	-2.11387
1973	4	4,373.3	1.010	0.03878	0.03878	3.87795
1974	1	4,335.4	0.991	-0.03422	-0.03422	-3.42169
1974	2	4,347.9	1.003	0.01158	0.01158	1.15829
1974	3	4,305.8	0.990	-0.03817	-0.03817	-3.81724
1974	4	4,288.9	0.996	-0.01561	-0.01561	-1.56076
1975	1	4,237.6	0.988	-0.04699	-0.04699	-4.69929
1975	2	4,268.6	1.007	0.02958	0.02958	2.95845
1975	3	4,340.9	1.017	0.06949	0.06949	6.94914
1975	4	4,397.8	1.013	0.05347	0.05347	5.34715
1976	1	4,496.8	1.023	0.09313	0.09313	9.31315
1976	2	4,530.3	1.007	0.03013	0.03013	3.01336
1976	3	4,552.0	1.005	0.01930	0.01930	1.92980
1976	4	4,584.6	1.007	0.02896	0.02896	2.89560
1977	1	4,640.0	1.012	0.04922	0.04922	4.92189
1977	2	4,731.1	1.020	0.08088	0.08088	8.08778
1977	3	4,815.8	1.018	0.07356	0.07356	7.35574
1977	4	4,815.3	1.000	-0.00042	-0.00042	-0.04152
1978	1	4,830.8	1.003	0.01294	0.01294	1.29379
1978	2	5,021.2	1.039	0.16722	0.16722	16.72230
1978	3	5,070.7	1.010	0.04002	0.04002	4.00198
1978	4	5,137.4	1.013	0.05366	0.05366	5.36633
1979	1	5,147.4	1.002	0.00781	0.00781	0.78088
1979	2	5,152.3	1.001	0.00381	0.00381	0.38132
1979	3	5,189.4	1.007	0.02912	0.02912	2.91153
1979	4	5,204.7	1.003	0.01185	0.01185	1.18455
1980	1	5,221.3	1.003	0.01282	0.01282	1.28189
1980	2	5,115.9	0.980	-0.07833	-0.07833	-7.83339
1980	3	5,107.4	0.998	-0.00663	-0.00663	-0.66294
1980	4	5,202.1	1.019	0.07626	0.07626	7.62553
1981	1	5,307.5	1.020	0.08354	0.08354	8.35407
1981	2	5,266.1	0.992	-0.03084	-0.03084	-3.08380
1981	3	5,329.8	1.012	0.04927	0.04927	4.92700
1981	4	5,263.4	0.988	-0.04891	-0.04891	-4.89095
1982	1	5,177.1	0.984	-0.06399	-0.06399	-6.39895
1982	2	5,204.9	1.005	0.02165	0.02165	2.16528
1982	3	5,185.2	0.996	-0.01505	-0.01505	-1.50538
1982	4	5,189.8	1.001	0.00355	0.00355	0.35533
1983	1	5,253.8	1.012	0.05025	0.05025	5.02475
1983	2	5,372.3	1.023	0.09332	0.09332	9.33190
1983	3	5,478.4	1.020	0.08137	0.08137	8.13690
1983	4	5,590.5	1.020	0.08440	0.08440	8.43954
1984	1	5,699.8	1.020	0.08053	0.08053	8.05276
1984	2	5,797.9	1.017	0.07064	0.07064	7.06423
1984	3	5,854.3	1.010	0.03948	0.03948	3.94829
1984	4	5,902.4	1.008	0.03327	0.03327	3.32720
1985	1	5,956.9	1.009	0.03745	0.03745	3.74488
1985	2	6,007.8	1.009	0.03462	0.03462	3.46194
1985	3	6,101.7	1.016	0.06400	0.06400	6.39998
1985	4	6,148.6	1.008	0.03110	0.03110	3.11018
1986	1	6,207.4	1.010	0.03880	0.03880	3.88048
1986	2	6,232.0	1.004	0.01595	0.01595	1.59465
1986	3	6,291.7	1.010	0.03887	0.03887	3.88725
1986	4	6,323.4	1.005	0.02031	0.02031	2.03064
1987	1	6,365.0	1.007	0.02658	0.02658	2.65758
1987	2	6,435.0	1.011	0.04472	0.04472	4.47216
1987	3	6,493.4	1.009	0.03680	0.03680	3.67986
1987	4	6,606.8	1.017	0.07171	0.07171	7.17069
1988	1	6,639.1	1.005	0.01970	0.01970	1.96995
1988	2	6,723.5	1.013	0.05183	0.05183	5.18282
1988	3	6,759.4	1.005	0.02153	0.02153	2.15296
1988	4	6,848.6	1.013	0.05384	0.05384	5.38398
1989	1	6,918.1	1.010	0.04121	0.04121	4.12163
1989	2	6,963.5	1.007	0.02651	0.02651	2.65095
1989	3	7,013.1	1.007	0.02880	0.02880	2.87973
1989	4	7,030.9	1.003	0.01019	0.01019	1.01911
1990	1	7,112.1	1.012	0.04700	0.04700	4.70025
1990	2	7,130.3	1.003	0.01028	0.01028	1.02754
1990	3	7,130.8	1.000	0.00028	0.00028	0.02805
1990	4	7,076.9	0.992	-0.02989	-0.02989	-2.98940
1991	1	7,040.8	0.995	-0.02025	-0.02025	-2.02488
1991	2	7,086.5	1.006	0.02622	0.02622	2.62168
1991	3	7,120.7	1.005	0.01944	0.01944	1.94445
1991	4	7,154.1	1.005	0.01889	0.01889	1.88946
1992	1	7,228.2	1.010	0.04208	0.04208	4.20789
1992	2	7,297.9	1.010	0.03913	0.03913	3.91326
1992	3	7,369.5	1.010	0.03983	0.03983	3.98255
1992	4	7,450.7	1.011	0.04481	0.04481	4.48073
1994	1	7,715.1	1.010	0.04132	0.04132	4.13197
1994	2	7,815.7	1.013	0.05319	0.05319	5.31865
1994	3	7,859.5	1.006	0.02261	0.02261	2.26056
1994	4	7,951.6	1.012	0.04770	0.04770	4.77036
1995	1	7,973.7	1.003	0.01116	0.01116	1.11637
1995	2	7,988.0	1.002	0.00719	0.00719	0.71929
1995	3	8,053.1	1.008	0.03300	0.03300	3.29996
1995	4	8,112.0	1.007	0.02958	0.02958	2.95783
1996	1	8,169.2	1.007	0.02850	0.02850	2.85049
1996	2	8,303.1	1.016	0.06719	0.06719	6.71930
1996	3	8,372.7	1.008	0.03395	0.03395	3.39536
1996	4	8,470.6	1.012	0.04760	0.04760	4.75978
1997	1	8,536.1	1.008	0.03129	0.03129	3.12911
1997	2	8,665.8	1.015	0.06210	0.06210	6.21765
1997	3	8,773.7	1.012	0.05074	0.05074	5.07429
1997	4	8,838.4	1.007	0.02983	0.02983	2.98251
1998	1	8,936.2	1.011	0.04490	0.04490	4.50015
1998	2	8,995.3	1.007	0.02672	0.02672	2.67178
1998	3	9,098.9	1.012	0.04687	0.04687	4.68705
1998	4	9,237.1	1.015	0.06215	0.06215	6.21528
1999	1	9,315.5	1.008	0.03438	0.03438	3.43847
1999	2	9,392.6	1.008	0.03352	0.03352	3.35194
1999	3	9,502.2	1.012	0.04750	0.04750	4.74984
1999	4	9,671.1	1.018	0.07302	0.07302	7.30176
2000	1	9,695.6	1.003	0.01017	0.01017	1.01719
2000	2	9,847.9	1.016	0.06433	0.06433	6.43287
2000	3	9,836.6	0.999	-0.00458	-0.00458	-0.45819
2000	4	9,887.7	1.005	0.02094	0.02094	2.09420
2001	1	9,875.6	0.999	-0.00489	-0.00489	-0.48860
2001	2	9,905.9	1.003	0.01233	0.01233	1.23293
2001	3	9,871.1	0.996	-0.01398	-0.01398	-1.39784
2001	4	9,910.0	1.004	0.01586	0.01586	1.58566
2002	1	9,977.3	1.007	0.02744	0.02744	2.74425
2002	2	10,031.6	1.005	0.02195	0.02195	2.19478
2002	3	10,090.7	1.006	0.02337	0.02337	2.37746
2002	4	10,095.8	1.001	0.00202	0.00202	0.20232
2003	1	10,126.0	1.003	0.01202	0.01202	1.20192
2003	2	10,212.7	1.009	0.03469	0.03469	3.46908
2003	3	10,398.7	1.018	0.07486	0.07486	7.48649
2003	4	10,467.0	1.007	0.02653	0.02653	2.65325
2004	1	10,543.6	1.007	0.02960	0.02960	2.95959
2004	2	10,634.2	1.009	0.03482	0.03482	3.48171
2004	3	10,728.7	1.009	0.03602	0.03602	3.60223
2004	4	10,796.4	1.006	0.02548	0.02548	2.54806
2005	1	10,878.4	1.008	0.03073	0.03073	3.07284
2005	2	10,954.1	1.007	0.02813	0.02813	2.81269
2005	3	11,074.3	1.011	0.04462	0.04462	4.46200
2005	4	11,107.2	1.003	0.01194	0.01194	1.19364
2006	1	11,238.7	1.012	0.04820	0.04820	4.82043
2006	2	11,306.7	1.006	0.02442	0.02442	2.44226
2006	3	11,336.7	1.003	0.01066	0.01066	1.06555
2006	4	11,395.5	1.005	0.02091	0.02091	2.09687
2007	1	11,412.6	1.002	0.00602	0.00602	0.60159
2007	2	11,520.1	1.009	0.03821	0.03821	3.82134

Monthly Unemployment, Bureau of Labor Statistics
Labor Force Statistics from the Current Population Survey

Series Id: LNS14000000
Seasonally Adjusted
Series title: (Seas) Unemployment Rate
Labor force status: Unemployment rate
Type of data: Percent or rate
Age: 16 years and over

Download:
.xls

Year	Jan	Feb	Mar	1st Quarter Average (example: "1948.1")	Apr	May	Jun	2nd Quarter Average (example: "1948.2")	Jul	Aug	Sep	3rd Quarter Average (example: "1948.3")	Oct	Nov	Dec	4th Quarter Average (example: "1948.4")	Annual
1948	3.4	3.8	4	3.733333333	3.9	3.5	3.6	3.666666667	3.6	3.9	3.8	3.766666667	3.7	3.8	4	3.833333333	
1949	4.3	4.7	5	4.666666667	5.3	6.1	6.2	5.866666667	6.7	6.8	6.6	6.7	7.9	6.4	6.6	6.966666667	
1950	6.5	6.4	6.3	6.4	5.8	5.5	5.4	5.566666667	5	4.5	4.4	4.633333333	4.2	4.2	4.3	4.233333333	
1951	3.7	3.4	3.4	3.5	3.1	3	3.2	3.1	3.1	3.1	3.3	3.166666667	3.5	3.5	3.1	3.366666667	
1952	3.2	3.1	2.9	3.066666667	2.9	3	3	2.966666667	3.2	3.4	3.1	3.233333333	3	2.8	2.7	2.833333333	
1953	2.9	2.6	2.6	2.7	2.7	2.5	2.5	2.566666667	2.6	2.7	2.9	2.733333333	3.1	3.5	4.5	3.7	
1954	4.9	5.2	5.7	5.266666667	5.9	5.9	5.6	5.8	5.8	6	6.1	5.966666667	5.7	5.3	5	5.333333333	
1955	4.9	4.7	4.6	4.733333333	4.7	4.3	4.2	4.4	4	4.2	4.1	4.1	4.3	4.2	4.2	4.233333333	
1956	4	3.9	4.2	4.033333333	4	4.3	4.3	4.2	4.4	4.1	3.9	4.133333333	3.9	4.3	4.2	4.133333333	
1957	4.2	3.9	3.7	3.933333333	3.9	4.1	4.3	4.1	4.2	4.1	4.4	4.233333333	4.5	5.1	5.2	4.933333333	
1958	5.8	6.4	6.7	6.3	7.4	7.4	7.3	7.366666667	7.5	7.4	7.1	7.333333333	6.7	6.2	6.2	6.366666667	
1959	6	5.9	5.6	5.833333333	5.2	5.1	5	5.1	5.1	5.2	5.5	5.266666667	5.7	5.8	5.3	5.6	
1960	5.2	4.8	5.4	5.133333333	5.2	5.1	5.4	5.233333333	5.5	5.6	5.5	5.533333333	6.1	6.1	6.6	6.266666667	
1961	6.6	6.9	6.9	6.8	7	7.1	6.9	7	7	6.6	6.7	6.766666667	6.5	6.1	6	6.2	
1962	5.8	5.5	5.6	5.633333333	5.6	5.5	5.5	5.533333333	5.4	5.7	5.6	5.566666667	5.4	5.7	5.5	5.533333333	
1963	5.7	5.9	5.7	5.766666667	5.7	5.9	5.6	5.733333333	5.6	5.4	5.5	5.5	5.5	5.7	5.5	5.566666667	
1964	5.6	5.4	5.4	5.466666667	5.3	5.1	5.2	5.2	4.9	5	5.1	5	5.1	4.8	5	4.966666667	
1965	4.9	5.1	4.7	4.9	4.8	4.6	4.6	4.666666667	4.4	4.4	4.3	4.366666667	4.2	4.1	4	4.1	
1966	4	3.8	3.8	3.866666667	3.8	3.9	3.8	3.833333333	3.8	3.8	3.7	3.766666667	3.7	3.6	3.8	3.7	
1967	3.9	3.8	3.8	3.833333333	3.8	3.8	3.9	3.833333333	3.8	3.8	3.8	3.8	4	3.9	3.8	3.9	
1968	3.7	3.8	3.7	3.733333333	3.5	3.5	3.7	3.566666667	3.7	3.5	3.4	3.533333333	3.4	3.4	3.4	3.4	
1969	3.4	3.4	3.4	3.4	3.4	3.4	3.5	3.433333333	3.5	3.5	3.7	3.566666667	3.7	3.5	3.5	3.566666667	
1970	3.9	4.2	4.4	4.166666667	4.6	4.8	4.9	4.766666667	5	5.1	5.4	5.166666667	5.5	5.9	6.1	5.833333333	
1971	5.9	5.9	6	5.933333333	5.9	5.9	5.9	5.9	6	6.1	6	6.033333333	5.8	6	6	5.933333333	
1972	5.8	5.7	5.8	5.766666667	5.7	5.7	5.7	5.7	5.6	5.6	5.5	5.566666667	5.6	5.3	5.2	5.366666667	
1973	4.9	5	4.9	4.933333333	5	4.9	4.9	4.933333333	4.8	4.8	4.8	4.8	4.6	4.8	4.9	4.766666667	
1974	5.1	5.2	5.1	5.133333333	5.1	5.1	5.4	5.2	5.5	5.5	5.9	5.633333333	6	6.6	7.2	6.6	
1975	8.1	8.1	8.6	8.266666667	8.8	9	8.8	8.866666667	8.6	8.4	8.4	8.466666667	8.4	8.3	8.2	8.3	
1976	7.9	7.7	7.6	7.733333333	7.7	7.4	7.6	7.566666667	7.8	7.8	7.6	7.733333333	7.7	7.8	7.8	7.766666667	
1977	7.5	7.6	7.4	7.5	7.2	7	7.2	7.133333333	6.9	7	6.8	6.9	6.8	6.8	6.4	6.666666667	
1978	6.4	6.3	6.3	6.333333333	6.1	6	5.9	6	6.2	5.9	6	6.033333333	5.8	5.9	6	5.9	
1979	5.9	5.9	5.8	5.866666667	5.8	5.6	5.7	5.7	5.7	6	5.9	5.866666667	6	5.9	6	5.966666667	
1980	6.3	6.3	6.3	6.3	6.9	7.5	7.6	7.333333333	7.8	7.7	7.5	7.666666667	7.5	7.5	7.2	7.4	
1981	7.5	7.4	7.4	7.433333333	7.2	7.5	7.5	7.4	7.2	7.4	7.6	7.4	7.9	8.3	8.5	8.233333333	
1982	8.6	8.9	9	8.833333333	9.3	9.4	9.6	9.433333333	9.8	9.8	10.1	9.9	10.4	10.8	10.8	10.66666667	
1983	10.4	10.4	10.3	10.36666667	10.2	10.1	10.1	10.13333333	9.4	9.5	9.2	9.366666667	8.8	8.5	8.3	8.533333333	
1984	8	7.8	7.8	7.866666667	7.7	7.4	7.2	7.433333333	7.5	7.5	7.3	7.433333333	7.4	7.2	7.3	7.3	
1985	7.3	7.2	7.2	7.233333333	7.3	7.2	7.4	7.3	7.4	7.1	7.1	7.2	7.1	7	7	7.033333333	
1986	6.7	7.2	7.2	7.033333333	7.1	7.2	7.2	7.166666667	7	6.9	7	6.966666667	7	6.9	6.6	6.833333333	
1987	6.6	6.6	6.6	6.6	6.3	6.3	6.2	6.266666667	6.1	6	5.9	6	6	5.8	5.7	5.833333333	
1988	5.7	5.7	5.7	5.7	5.4	5.6	5.4	5.466666667	5.4	5.6	5.4	5.466666667	5.4	5.3	5.3	5.333333333	
1989	5.4	5.2	5	5.2	5.2	5.2	5.3	5.233333333	5.2	5.2	5.3	5.233333333	5.3	5.4	5.4	5.366666667	
1990	5.4	5.3	5.2	5.3	5.4	5.4	5.2	5.333333333	5.5	5.7	5.9	5.7	5.9	6.2	6.3	6.133333333	
1991	6.4	6.6	6.8	6.6	6.7	6.9	6.9	6.833333333	6.8	6.9	6.9	6.866666667	7	7	7.3	7.1	
1992	7.3	7.4	7.4	7.366666667	7.4	7.6	7.8	7.6	7.7	7.6	7.6	7.633333333	7.3	7.4	7.4	7.366666667	
1993	7.3	7.1	7	7.133333333	7.1	7.1	7	7.066666667	6.9	6.8	6.7	6.8	6.8	6.6	6.5	6.633333333	
1994	6.6	6.6	6.5	6.566666667	6.4	6.1	6.1	6.2	6.1	6	5.9	6	5.8	5.6	5.5	5.633333333	
1995	5.6	5.4	5.4	5.466666667	5.8	5.6	5.6	5.666666667	5.7	5.7	5.6	5.666666667	5.5	5.6	5.6	5.566666667	
1996	5.6	5.5	5.5	5.533333333	5.6	5.6	5.3	5.5	5.5	5.1	5.2	5.266666667	5.2	5.4	5.4	5.333333333	
1997	5.3	5.2	5.2	5.233333333	5.1	4.9	5	5	4.9	4.8	4.9	4.866666667	4.7	4.6	4.7	4.666666667	
1998	4.6	4.6	4.7	4.633333333	4.3	4.4	4.5	4.4	4.5	4.5	4.6	4.533333333	4.5	4.4	4.4	4.433333333	
1999	4.3	4.4	4.2	4.3	4.3	4.2	4.3	4.266666667	4.3	4.2	4.2	4.233333333	4.1	4.1	4	4.066666667	
2000	4	4.1	4	4.033333333	3.8	4	4	3.933333333	4	4.1	3.9	4	3.9	3.9	3.9	3.9	
2001	4.2	4.2	4.3	4.233333333	4.4	4.3	4.5	4.4	4.6	4.9	5	4.833333333	5.3	5.5	5.7	5.5	
2002	5.7	5.7	5.7	5.7	5.9	5.8	5.8	5.833333333	5.8	5.7	5.7	5.733333333	5.7	5.9	6	5.866666667	
2003	5.8	5.9	5.9	5.866666667	6	6.1	6.3	6.133333333	6.2	6.1	6.1	6.133333333	6	5.8	5.7	5.833333333	
2004	5.7	5.6	5.8	5.7	5.6	5.6	5.6	5.6	5.5	5.4	5.4	5.433333333	5.5	5.4	5.4	5.433333333	
2005	5.3	5.4	5.2	5.3	5.2	5.1	5	5.1	5	4.9	5	4.966666667	5	5	4.9	4.966666667	
2006	4.7	4.8	4.7	4.733333333	4.7	4.6	4.6	4.633333333	4.7	4.7	4.5	4.633333333	4.4	4.5	4.4	4.433333333	
2007	4.6	4.5	4.4	4.5	4.5	4.4	4.6	4.5	4.7	4.6	4.7	4.666666667	4.7	4.7	5	4.8	
2008	5	4.8	5.1	4.966666667	4.9	5.4	5.6	5.3	5.8	6.1	6.2	6.033333333	6.6	6.8	7.3	6.9	
2009	7.8	8.2	8.6	8.2	8.9	9.4	9.5	9.266666667	9.5	9.7	9.8	9.666666667	10.1	9.9	9.9	9.966666667	
2010	9.7	9.7	9.7	9.7	9.8	9.6	9.5	9.633333333	9.5	9.6	9.6	9.566666667	9.7	9.8	9.4	9.633333333	
2011	9	8.9	8.8	8.9	9	9.1	9.2	9.1	9.1	9.1	9.1	9.1					

Change in Quarterly Unemployment vs. Change in Quarterly GDP

Knotek's Email of November 30, 2011

Original Data

$$y = -0.0660730x + 0.2311940$$

- Series1
- Linear (Series1)

Knotek's Data

$$y = -0.0660355x + 0.2309423$$

- Series1
- Linear (Series1)

1.   Prices.

For price data, 1800 through 1993, we used two sources.

1.   Series E 135-166, "Consumer Price Indexes (BLS - all items, 1800-1970, and by groups, 1913-1970), pp 210-211, of the book *Historical Statistics of the United States: Colonial Times to 1970, Part 1*, published by the United States Department of Commerce.

2.   The Consumer Price Index of 1997, also published by the United States Department of Commerce, continues this series by dividing the historic series by 3, or a multiple of 1/3.

In the following table, we begin with the Consumer Price Index listed in Series E 135-166 of the *Historical Statistics of the United States: Colonial Times to 1970, Part 1* (column 3) and compare this with the Consumer Price Index of 1960–1997. (column 1) The years of overlap clearly reduce the number for the historic series to a precise one-third of its value as the value given for the modern series. (column 2)

We then spliced these two series into a single data set for prices based upon the values given in the historic series. We continued this data set past 1970 by multiplying the modern number by 3 and including this value in the final data set. (column 4)

We then figured centered moving averages for seven-year periods for the entire series. In this format a price index is averaged for seven sequential years and the average is placed at the middle term, e.g. the price indices for 1870, 1871, 1872, 1873, 1874, 1875, 1876 are averaged and placed as the figure for 1873. The process then continues to the next seven-year series by dropping the first and adding the next year in the chronology and beginning the averaging again. The technical term for this alteration of the data is "smoothing." (column 5)

We then found the annual change between 7-year running averages for each year, and placed these next to the centered moving average itself. (column 6)

We then divided the annual change in 7-year running averages for a given year by the 7-year running average for that year, to be denominated "Change / Average Inflation." In this way the larger numbers for the Consumer Price Index found in later years were brought into conformity with the price patterns of prior years. (column 7)

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Data Set 1 – Prices.

Left block (Years 1801–1860)

Year	Column 1 Consumer Price Index, Statistical Abstract 1997	Column 2 Multiple	Column 3 Consumer Price Index-Historical Statistics of U.S.	Column 4 Extended Series 1800-1993	Column 5 7-Yr Average	Column 6 Change	Column 7 Change/Average
1801			50.00	50.00			
1802			43.00	43.00			
1803			45.00	45.00			
1804			45.00	45.00			
1805			45.00	45.00	43.57		
1806			47.00	47.00	45.29	-0.29	-0.006
1807			44.00	44.00	45.86	0.57	0.012
1808			48.00	48.00	46.14	0.29	0.006
1809			47.00	47.00	46.86	0.71	0.015
1810			47.00	47.00	47.71	0.86	0.018
1811			50.00	50.00	49.29	1.57	0.032
1812			51.00	51.00	52.00	2.71	0.052
1813			58.00	58.00	53.00	1.00	0.019
1814			63.00	63.00	53.57	0.57	0.011
1815			55.00	55.00	53.14	-0.43	-0.008
1816			51.00	51.00	52.43	-0.71	-0.014
1817			48.00	48.00	50.14	-2.29	-0.046
1818			46.00	46.00	46.86	-3.29	-0.070
1819			46.00	46.00	44.71	-2.14	-0.048
1820			42.00	42.00	42.57	-2.14	-0.050
1821			40.00	40.00	40.43	-2.14	-0.053
1822			40.00	40.00	38.71	-1.71	-0.044
1823			36.00	36.00	37.00	-1.71	-0.046
1824			33.00	33.00	35.86	-1.14	-0.032
1825			34.00	34.00	34.86	-1.00	-0.029
1826			34.00	34.00	33.71	-1.14	-0.034
1827			34.00	34.00	33.14	-0.57	-0.017
1828			33.00	33.00	33.00	-0.14	-0.004
1829			32.00	32.00	32.43	-0.57	-0.018
1830			32.00	32.00	31.71	-0.71	-0.023
1831			32.00	32.00	30.86	-0.29	-0.009
1832			30.00	30.00	30.86	0.14	0.004
1833			29.00	29.00	30.00	-0.86	-0.029
1834			30.00	30.00	30.00		
1835			30.00	30.00	31.29		
1836			33.00	33.00	31.57	0.29	0.009
1837			32.00	32.00	31.71	0.14	0.005
1838			34.00	34.00	30.86	-0.71	-0.023
1839			30.00	30.00	30.86	-0.29	
1840			30.00	30.00	31.29	-0.71	
1841			31.00	31.00	31.29	0.29	
1842			33.00	33.00	30.43	-0.86	
1843			29.00	29.00	29.43	-0.57	-0.019
1844			28.00	28.00	28.43	-0.71	-0.025
1845			28.00	28.00	27.71	-0.71	-0.025
1846			27.00	27.00	27.14	-0.57	-0.021
1847			28.00	28.00	26.71	-0.43	
1848			28.00	28.00	26.29	-0.43	
1849			26.00	26.00	25.86	-0.57	
1850			25.00	25.00	25.43	-0.45	-0.017
1851			25.00	25.00	25.43	0.00	
1852			25.00	25.00	25.71	0.29	0.011
1853			25.00	25.00	26.00	0.29	0.011
1854			27.00	27.00	26.43	0.43	
1855			28.00	28.00	26.57	0.14	
1856			27.00	27.00	26.86	0.29	0.011
1857			28.00	28.00	27.14	0.29	0.011
1858			26.00	26.00	27.14	0.00	0.000
1859			27.00	27.00	27.43	0.25	
1860			27.00	27.00	28.86	1.43	0.050

Middle block (Years 1861–1916)

Year	Column 1 Consumer Price Index, Statistical Abstract 1997	Column 2 Multiple	Column 3 Consumer Price Index-Historical Statistics of U.S.	Column 4 Extended Series 1800-1993	Column 5 7-Yr Average	Column 6 Change	Column 7 Change/Average
1861			27.00	27.00	31.57	2.71	0.086
1862			30.00	30.00	34.43	2.86	0.083
1863			37.00	37.00	36.86	2.43	0.066
1864			47.00	47.00	39.00	2.14	0.055
1865			46.00	46.00	40.86	1.86	0.045
1866			44.00	44.00	42.29	1.43	0.034
1867			42.00	42.00	42.43	0.14	0.003
1868			40.00	40.00	40.86	-1.57	-0.038
1869			40.00	40.00	39.43	-1.43	-0.036
1870			38.00	38.00	38.29	-1.14	-0.030
1871			36.00	36.00	37.14	-1.14	-0.031
1872			36.00	36.00	36.14	-1.00	-0.028
1873			35.00	35.00	35.00	-1.14	-0.033
1874			34.00	34.00	34.14	-0.86	-0.025
1875			33.00	33.00	33.14	-1.00	-0.030
1876			32.00	32.00	32.00	-1.14	-0.036
1877			32.00	32.00	31.00	-1.00	-0.032
1878			29.00	29.00	30.29	-0.71	-0.024
1879			28.00	28.00	29.71	-0.57	-0.019
1880			29.00	29.00	29.14	-1.14	-0.039
1881			29.00	29.00	28.43	-0.86	-0.030
1882			29.00	29.00	28.34	-0.71	-0.025
1883			28.00	28.00	28.00	-0.43	-0.015
1884			27.00	27.00	27.71	-0.29	-0.010
1885			27.00	27.00	27.43	-0.29	-0.010
1886			27.00	27.00	27.14	-0.29	-0.011
1887			27.00	27.00	27.00	0.00	0.000
1888			27.00	27.00	27.00	0.00	0.000
1889			27.00	27.00	27.00	0.00	0.000
1890			27.00	27.00	26.89	-0.14	-0.005
1891			27.00	27.00	26.71	-0.29	-0.011
1892			27.00	27.00	26.57	-0.29	-0.011
1893			27.00	27.00	26.29	-0.29	-0.011
1894			26.00	26.00	25.71	-0.29	-0.011
1895			25.00	25.00	25.43	-0.29	-0.011
1896			25.00	25.00	25.14	-0.29	-0.011
1897			25.00	25.00	25.14	0.14	0.006
1898			25.00	25.00	25.00	-0.14	-0.006
1899			25.00	25.00	25.14	0.14	0.006
1900			25.00	25.00	25.43	0.29	0.011
1901			25.00	25.00	25.71	0.29	0.011
1902			26.00	26.00	26.00	0.29	0.011
1903			27.00	27.00	26.71	0.43	0.017
1904			27.00	27.00	27.14	0.29	0.011
1905			27.00	27.00	27.00	0.14	0.005
1906			27.00	27.00	27.14	0.14	0.005
1907			28.00	28.00	27.29	0.14	0.005
1908			27.00	27.00	27.43	0.14	0.005
1909			27.00	27.00	27.71	0.29	0.010
1910			28.00	28.00	28.10	0.39	0.014
1911			28.00	28.00	28.40	0.30	0.011
1912			29.00	29.00	28.89	0.49	0.017
1913			29.70	29.70	29.70	0.81	0.027
1914			30.10	30.10	31.19	1.49	0.048
1915			30.40	30.40	33.63	2.44	0.073
1916			32.70	32.70	36.85	3.29	0.089

Middle-right block (Years 1917–1972)

Year	Column 1 Consumer Price Index, Statistical Abstract 1997	Column 2 Multiple	Column 3 Consumer Price Index-Historical Statistics of U.S.	Column 4 Extended Series 1800-1993	Column 5 7-Yr Average	Column 6 Change	Column 7 Change/Average
1917			38.40	38.40	45.21	4.33	0.105
1918			45.10	45.10	44.57	3.36	0.075
1919			51.80	51.80	47.40	2.83	0.060
1920			60.00	60.00	50.03	2.63	0.053
1921			53.60	53.60	51.86	1.83	0.035
1922			50.20	50.20	52.91	1.06	0.020
1923			51.10	51.10	53.09	0.17	0.003
1924			51.20	51.20	51.94	-1.14	-0.022
1925			52.50	52.50	51.61	-0.33	-0.006
1926			53.00	53.00	51.77	0.16	0.003
1927			52.00	52.00	51.61	-0.16	-0.003
1928			51.30	51.30	50.03	-0.88	-0.016
1929			51.30	51.30	49.16	-1.66	-0.034
1930			50.00	50.00	47.13	-2.03	-0.043
1931			45.60	45.60	45.43	-1.70	-0.037
1932			40.90	40.90	43.97	-1.46	-0.033
1933			38.80	38.80	42.57	-1.40	-0.033
1934			40.10	40.10	41.57	-1.00	-0.024
1935			41.10	41.10	41.11	-0.46	-0.011
1936			41.50	41.50	41.21	0.10	0.002
1937			43.00	43.00	41.67	0.46	0.011
1938			42.40	42.40	42.24	0.57	0.014
1939			41.60	41.60	43.34	1.10	0.025
1940			42.00	42.00	44.81	1.47	0.033
1941			44.10	44.10	46.20	1.39	0.030
1942			48.80	48.80	47.84	1.64	0.034
1943			51.80	51.80	50.26	2.41	0.048
1944			52.70	52.70	53.81	3.56	0.066
1945			53.90	53.90	57.81	4.00	0.069
1946			58.50	58.50	61.04	3.23	0.053
1947			66.90	66.90	64.34	3.29	0.051
1948			72.10	72.10	67.33	3.00	0.045
1949			71.40	71.40	71.19	3.85	0.054
1950			72.10	72.10	74.27	3.09	0.042
1951			77.80	77.80	76.21	1.94	0.025
1952			79.50	79.50	77.37	1.16	0.015
1953			80.10	80.10	78.80	1.43	0.018
1954			80.50	80.50	80.54	1.74	0.022
1955			80.20	80.20	81.88	1.26	0.015
1956			81.40	81.40	82.91	1.11	0.013
1957		2.99	84.30	84.14	84.14	1.23	0.015
1958		3.00	86.60	86.60	85.44	1.30	0.015
1959	29.60	2.99	87.30	87.30	86.53	1.09	0.013
1960	29.50	2.99	88.70	88.70	88.40	1.47	0.017
1961	30.20	1.00	89.60	89.60	89.63	1.23	0.014
1962	30.60	2.99	90.60	90.60	90.76	1.13	0.012
1963	31.00	2.99	91.70	91.70	92.17	1.41	0.015
1964	31.50	3.00	92.90	92.90	93.79	1.61	0.017
1965	32.40	1.00	94.50	94.50	95.87	2.09	0.022
1966	33.40	2.99	97.20	97.20	98.61	2.74	0.028
1967	34.80	2.99	100.00	100.00	102.13	3.51	0.034
1968	36.70	2.99	104.20	104.20	106.21	4.09	0.038
1969	38.80	2.99	109.80	109.80	110.63	4.41	0.040
1970	40.50	3.00	116.30	116.30	115.77	5.14	0.044
1971	41.80	3.00		121.50	122.61	6.84	0.056
1972		3.00		125.40	130.79	8.17	0.062

Right block (Years 1973–1993)

Year	Column 1 Consumer Price Index, Statistical Abstract 1997	Column 2 Multiple	Column 3 Consumer Price Index-Historical Statistics of U.S.	Column 4 Extended Series 1800-1993	Column 5 7-Yr Average	Column 6 Change	Column 7 Change/Average
1973	44.40	3.00		133.20	139.49	8.70	0.062
1974	49.30	3.00		147.90	148.84	9.38	0.063
1975	53.80	3.00		161.40	159.43	10.59	0.066
1976	56.90	3.00		170.70	172.63	11.20	0.065
1977	60.60	3.00		181.80	188.91	16.29	0.086
1978	65.20	3.00		195.60	206.74	17.83	0.086
1979	72.60	3.00		217.80	225.04	18.30	0.081
1980	82.40	3.00		247.20	243.34	18.30	0.075
1981	90.90	3.00		272.70	261.90	18.56	0.071
1982	96.50	3.00		289.50	280.07	18.17	0.065
1983	99.50	3.00		298.80	295.93	15.86	0.054
1984	103.90	3.00		311.70	309.30	13.37	0.043
1985	107.60	3.00		322.80	321.04	11.34	0.037
1986	109.60	3.00		328.80	332.83	11.79	0.035
1987	113.60	3.00		340.80	346.16	13.33	0.039
1988	118.30	3.00		354.90	360.00	13.84	0.038
1989	124.00	3.00		372.00	374.01	14.01	0.037
1990	130.70	3.00		392.10	388.97	14.96	0.038
1991	136.20	3.00		408.60			
1992	140.30	3.00		420.90			
1993	144.50	3.00		433.50			

Data Set 6 - Inflation: Cumulative Averages.

	Col. 1		Col. 2		Col. 3		Col. 4		Col. 5	Col 6.
Axis	Year		Year		Year		Year		Average %	Cumulative %
1	1805	-0.63%	1861	8.60%	1917	10.50%	1973	6.24%	6.1765%	24.71%
2	1806	1.25%	1862	8.30%	1918	7.53%	1974	6.29%	5.8409%	23.36%
3	1807	0.62%	1863	6.59%	1919	5.97%	1975	6.64%	4.9539%	19.82%
4	1808	1.52%	1864	5.49%	1920	5.25%	1976	7.65%	4.9799%	19.92%
5	1809	1.80%	1865	4.55%	1921	3.53%	1977	8.62%	4.6222%	18.49%
6	1810	3.19%	1866	3.38%	1922	2.00%	1978	8.62%	4.2970%	17.19%
7	1811	5.22%	1867	0.34%	1923	0.32%	1979	8.13%	3.5028%	14.01%
8	1812	1.89%	1868	-3.85%	1924	-2.20%	1980	7.52%	0.8402%	3.36%
9	1813	1.07%	1869	-3.62%	1925	-0.64%	1981	7.09%	0.9731%	3.89%
10	1814	0.27%	1870	-2.99%	1926	0.30%	1982	6.49%	1.0181%	4.07%
11	1815	-1.08%	1871	-3.08%	1927	-0.30%	1983	5.36%	0.2254%	0.90%
12	1816	-1.36%	1872	-2.77%	1928	-1.57%	1984	4.32%	-0.3451%	-1.38%
13	1817	-4.56%	1873	-3.27%	1929	-3.37%	1985	3.66%	-1.8843%	-7.54%
14	1818	-7.01%	1874	-2.51%	1930	-4.30%	1986	3.54%	-2.5715%	-10.29%
15	1819	-4.79%	1875	-3.02%	1931	-3.74%	1987	3.85%	-1.9253%	-7.70%
16	1820	-5.03%	1876	-3.57%	1932	-3.31%	1988	3.85%	-2.0184%	-8.07%
17	1821	-5.30%	1877	-3.23%	1933	-3.29%	1989	3.75%	-2.0169%	-8.07%
18	1822	-4.43%	1878	-2.36%	1934	-2.41%	1990		-3.0640%	-9.19%
19	1823	-4.63%	1879	-1.92%	1935	-1.11%	1991		-2.5561%	-7.67%
20	1824	-3.19%	1880	-1.96%	1936	0.24%	1992		-1.6351%	-4.91%
21	1825	-2.87%	1881	-2.51%	1937	1.10%	1993		-1.4281%	-4.28%
22	1826	-3.39%	1882	-1.02%	1938	1.35%	1994		-1.0174%	-3.05%
23	1827	-1.72%	1883	-0.51%	1939	2.54%	1995		0.1012%	0.30%
24	1828	-0.43%	1884	-1.03%	1940	3.28%	1996		0.6065%	1.82%
25	1829	-1.76%	1885	-1.04%	1941	3.00%	1997		0.0652%	0.20%
26	1830	-2.25%	1886	-1.05%	1942	3.43%	1998		0.0430%	0.13%
27	1831	-1.83%	1887	-0.53%	1943	4.80%	1999		0.8133%	2.44%
28	1832	-0.93%	1888	0.00%	1944	6.61%	2000		1.8947%	5.68%
29	1833	0.46%	1889	0.00%	1945	6.92%	2001		2.4598%	7.38%
30	1834	0.91%	1890	0.00%	1946	5.29%	2002		2.0674%	6.20%
31	1835	0.00%	1891	-0.53%	1947	4.54%	2003		1.3345%	4.00%
32	1836	0.90%	1892	-1.08%	1948	5.31%	2004		1.7132%	5.14%
33	1837	0.45%	1893	-1.09%	1949	5.14%	2005		1.5003%	4.50%
34	1838	0.45%	1894	-1.10%	1950	4.15%	2006		1.1681%	3.50%
35	1839	-0.90%	1895	-1.11%	1951	2.55%	2007		0.1777%	0.53%
36	1840	-2.31%	1896	-1.12%	1952	1.50%	2008		-0.6476%	-1.94%
37	1841	-2.86%	1897	-1.14%	1953	1.81%	2009		-0.7269%	-2.18%
38	1842	-1.94%	1898	-0.57%	1954	2.16%	2010		-0.1164%	-0.35%
39	1843	-2.49%	1899	0.57%	1955	1.54%	2011		-0.1275%	-0.38%
40	1844	-1.01%	1900	1.12%	1956	1.34%	2012		0.4875%	1.46%
41	1845	-2.58%	1901	1.11%	1957	1.46%	2013		-0.0020%	-0.01%
42	1846	-2.11%	1902	1.10%	1958	1.52%	2014		0.1717%	0.52%
43	1847	-1.60%	1903	1.09%	1959	1.71%	2015		0.3973%	1.19%
44	1848	-1.63%	1904	1.60%	1960	1.66%	2016		0.5461%	1.64%
45	1849	-1.66%	1905	1.06%	1961	1.37%	2017		0.2572%	0.77%
46	1850	-1.12%	1906	0.53%	1962	1.24%	2018		0.2175%	0.65%
47	1851	-0.56%	1907	0.52%	1963	1.53%	2019		0.4987%	1.50%
48	1852	1.11%	1908	0.52%	1964	1.72%	2020		1.1177%	3.35%
49	1853	1.10%	1909	1.03%	1965	2.18%	2021		1.4351%	4.31%
50	1854	1.62%	1910	1.37%	1966	2.78%	2022		1.9252%	5.78%
51	1855	0.54%	1911	1.06%	1967	3.44%	2023		1.6783%	5.04%
52	1856	1.06%	1912	1.68%	1968	3.85%	2024		2.1973%	6.59%
53	1857	1.05%	1913	2.74%	1969	3.99%	2025		2.5948%	7.78%
54	1858	0.00%	1914	4.76%	1970	4.44%	2026		3.0688%	9.21%
55	1859	1.04%	1915	7.26%	1971	5.58%	2027		4.6289%	13.89%
56	1860	4.95%	1916	8.83%	1972	6.25%	2028		6.6763%	20.03%

2. United States Real Gross National Product.

We located two sources for real US GNP.

1.   Figures for U. S. Real GNP 1869-1970 may be found in the book *Historical Statistics of the United States: Colonial Times to 1970, Part 1*, published by the United States Department of Commerce. Series F 1-5 presents "Gross National Product" for the United States between the years 1869-1970 according to 1958 prices. The years 1869-1878, and 1879-1888 are given with decade averages of 23.1 billion and 42.4 billion dollars respectively.

2.   Figures for U. S. Real GNP 1947-present are collected by the St. Louis Federal Reserve.[44]

In Data Set 2 we begin with figures from the United States Department of Commerce which has published one set of numbers based upon 1958 prices running from 1869 through 1970. (column 2) The St. Louis Federal Reserve has published a different sequence of numbers based upon 2005 prices extending between 1947 through to the present day. (column 7)

Splicing multiples are quite necessary when considering two different series each of which proposes to calculate U.S. Real GNP over different periods of time. To "splice" or to "graft" these two sets together is necessary if an extended series running from 1869 to the present day is to be obtained. There does not exist at the present time such a series published by the United States Government. Consequently our first step in the analysis is to construct such a series as the foundation of this approach.[45]

We considered two possible multiples with which to splice these two series of U.S. Real GNP figures together. The first possible splicing multiple is 5.881696, the average of all 23 multiples between 1947-1970. These are the years during which these two separate series overlap. (column 6) This number is problematic in that there is a clear drift from 1947 through 1970 toward higher multiples. Figures from 1947-1960 range from 5.646318 (1953) to 5.977644 (1958) and average at 5.8239423. Figures from 1961-1970 range a bit higher, i.e. from 5.907649 (1962) to 6.071220 (1965).

A second possible splicing multiple is 5.962552, the average of the final ten years of overlap, i.e. between 1961-1970. This multiple is the one used to splice these series in this paper as it is nearer in time to the eventual cutoff between the series and includes only multiples found in the later and more recent multiples. (column four)

For the purposes of the demonstration herein, more elaborate splicing techniques have not been deemed necessary. Data Set 2 figures an extended series for U.S. Real GNP in constant terms from 1868 to 2009. For the purposes of this paper only the second splicing multiple, 5.962552, will be used for calculations. (column 9)

Each spreadsheet is a mathematic arrangement of the figures in "Data Set 2 – U.S. Real GNP."

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[44]   These figures are available at: http://research.stlouisfed.org/fred2/series/GNPC96
[45]   See e.g. Cochrane, 1988:902. "The presence of a splice in 1947 also does not drive the result. Every long series of GNP data contains at least one splice. The wide surveys used to construct later data are simply not available for earlier periods, so some projection using a restricted set of industries is unavoidable."

Data Set 2 – U.S. Real GNP.

Column 1	Column 2	Column 4	Column 6	Column 7	Column 9
Year	Historical Abstract	Historical Abstract as estimated in 1958 dollars for 1971-2009 using St. Louis Federal Reserve Figures divided by 5.962552	Multiples calculated between St. Louis Federal Reserve and Historical Abstract 1947-1970	St. Louis Federal Reserve Estimate for US Real GNP, 2005 Dollars	Hist. Abstract with extension to 2009 using multiple 5.962552
1868	23.10				23.1000
1869	23.10				23.1000
1870	23.10				23.1000
1871	23.10				23.1000
1872	23.10				23.1000
1873	23.10				23.1000
1874	23.10				23.1000
1875	23.10				23.1000
1876	23.10				23.1000
1877	23.10				23.1000
1878	42.40				42.4000
1879	42.40				42.4000
1880	42.40				42.4000
1881	42.40				42.4000
1882	42.40				42.4000
1883	42.40				42.4000
1884	42.40				42.4000
1885	42.40				42.4000
1886	42.40				42.4000
1887	42.40				42.4000
1888	42.40				42.4000
1889	49.10				49.1000
1890	52.70				52.7000
1891	55.10				55.1000
1892	60.40				60.4000
1893	57.50				57.5000
1894	55.90				55.9000
1895	62.60				62.6000
1896	61.30				61.3000
1897	67.10				67.1000
1898	68.60				68.6000
1899	74.80				74.8000
1900	76.90				76.9000
1901	85.70				85.7000
1902	86.50				86.5000
1903	90.80				90.8000
1904	89.70				89.7000
1905	96.30				96.3000
1906	107.50				107.5000
1907	109.20				109.2000
1908	100.20				100.2000
1909	116.80				116.8000
1910	120.10				120.1000
1911	123.20				123.2000
1912	130.20				130.2000
1913	131.40				131.4000
1914	125.60				125.6000
1915	124.50				124.5000
1916	134.40				134.4000

Column 1	Column 2	Column 4	Column 6	Column 7	Column 9
Year	Historical Abstract	Historical Abstract as estimated in 1958 dollars for 1971-2009 using St. Louis Federal Reserve Figures divided by 5.962552	Multiples calculated between St. Louis Federal Reserve and Historical Abstract 1947-1970	St. Louis Federal Reserve Estimate for US Real GNP, 2005 Dollars	Hist. Abstract with extension to 2009 using multiple 5.962552
1917	135.20				135.2000
1918	151.80				151.8000
1919	146.40				146.4000
1920	140.00				140.0000
1921	127.80				127.8000
1922	148.00				148.0000
1923	165.90				165.9000
1924	165.50				165.5000
1925	179.40				179.4000
1926	190.00				190.0000
1927	189.90				189.9000
1928	190.90				190.9000
1929	203.60				203.6000
1930	183.50				183.5000
1931	169.30				169.3000
1932	144.20				144.2000
1933	141.50				141.5000
1934	154.30				154.3000
1935	169.50				169.5000
1936	193.00				193.0000
1937	203.20				203.2000
1938	192.90				192.9000
1939	209.40				209.4000
1940	227.20				227.2000
1941	263.70				263.7000
1942	297.80				297.8000
1943	337.10				337.1000
1944	361.30				361.3000
1945	355.20				355.2000
1946	312.60				312.6000
1947	309.90		5.826073	1805.5	309.9000
1948	323.70		5.814334	1882.1	323.7000
1949	324.10		5.709349	1850.4	324.1000
1950	355.30		5.909372	2099.6	355.3000
1951	383.40		5.765780	2210.6	383.4000
1952	395.10		5.878006	2322.4	395.1000
1953	412.80		5.646318	2330.8	412.8000
1954	407.00		5.892875	2398.4	407.0000
1955	438.00		5.834703	2555.6	438.0000
1956	446.10		5.832997	2602.1	446.1000
1957	452.50		5.764862	2608.6	452.5000
1958	447.30		5.977644	2673.8	447.3000
1959	475.90		5.893255	2804.6	475.9000
1960	487.70		5.789625	2823.6	487.7000
1961	497.20		6.033387	2999.8	497.2000
1962	529.50		5.907649	3128.1	529.5000
1963	551.00		5.974047	3291.7	551.0000
1964	581.10		5.952160	3458.8	581.1000
1965	617.80		6.071220	3750.8	617.8000
1966	658.10		5.945601	3912.8	658.1000
1967	675.20		5.939129	4010.1	675.2000
1968	706.60		5.957260	4209.4	706.6000
1969	725.60		5.915243	4292.1	725.6000
1970	722.50		5.929827	4284.3	722.5000
1971		751.205189		4479.1	751.2051
1972		803.481462		4790.8	803.4814

Column 1	Column 2	Column 4	Column 6	Column 7	Column 9
Year	Historical Abstract	Historical Abstract as estimated in 1958 dollars for 1971-2009 using St. Louis Federal Reserve Figures divided by 5.962552	Multiples calculated between St. Louis Federal Reserve and Historical Abstract 1947-1970	St. Louis Federal Reserve Estimate for US Real GNP, 2005 Dollars	Hist. Abstract with extension to 2009 using multiple 5.962552
1973		839.418200		5005.1	839.4182
1974		821.740134		4899.7	821.7401
1975		843.077800		5026.9	843.0778
1976		879.313837		5243.0	879.3138
1977		922.669096		5501.5	922.6690
1978		985.882183		5878.4	985.8821
1979		1001.730450		5972.9	1001.7304
1980		996.830985		5943.7	996.8309
1981		1010.839453		6027.2	1010.8394
1982		995.141170		5933.6	995.1411
1983		1072.572702		6395.3	1072.5727
1984		1129.446482		6734.4	1129.4464
1985		1174.071602		7000.5	1174.0716
1986		1203.268409		7174.6	1203.2684
1987		1256.182622		7490.1	1256.1826
1988		1303.177483		7770.3	1303.1774
1989		1340.043451		7990.1	1340.0434
1990		1351.362214		8057.6	1351.3622
1991		1360.351230		8111.2	1360.3512
1992		1418.014924		8455.0	1418.0149
1993		1454.140974		8670.4	1454.1409
1994		1514.394384		9029.7	1514.3943
1995		1546.730848		9222.5	1546.7308
1996		1615.003381		9629.5	1615.0033
1997		1681.876068		10028.3	1681.8760
1998		1764.537028		10521.1	1764.5370
1999		1854.067237		11055.0	1854.0672
2000		1911.320976		11396.4	1911.3209
2001		1925.179460		11479.0	1925.1794
2002		1957.195959		11669.9	1957.1959
2003		2036.067333		12140.2	2036.0677
2004		2093.681033		12483.7	2093.6810
2005		2151.024762		12825.6	2151.0247
2006		2201.989188		13129.5	2201.9891
2007		2272.261503		13548.5	2272.2615
2008		2198.629555		13109.4	2198.6295
2009		2208.798443		13170.1	2208.7984

7-Year Spread

7 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

7 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics - 7 Year Spread

- Maximum Ratio of Row
- Minimum Ratio of Row
- Mid-Range Ratio of Row
- Median Ratio of Row
- Average Ratio of Row
- Median Average

Column Dynamics - 7 Year Spread

- Maximum Ratio of Column
- Minimum Ratio of Column
- Mid-Range Ratio of Column
- Median Ratio of Column
- Average Ratio of Column
- Median Average

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8-YEAR SPREAD

8 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

8 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics - 8 Year Spread

Column Dynamics - 8 Year Spread

9-YEAR SPREAD

9 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics - 9 Year Spread

Column Dynamics - 9 Year Spread

10-YEAR SPREAD

10 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics - 10 Year Spread

Column Dynamics - 10 Year Spread

11-YEAR SPREAD

11 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Column headers (A–G):
A — Maximum Ratio of Row
B — Minimum Ratio of Row
C — Spread
D — Mid-Range Ratio of Row
E — Median Ratio of Row
F — Average Ratio of Row
G — Median Average

Row labels (A–G):
A — Maximum Ratio of Column
B — Minimum Ratio of Column
C — Spread Range Ratio of Column
D — Range Ratio of Column
E — Median Ratio of Column
F — Average Ratio of Column
G — Median Average

Row Dynamics – 11 Year Spread

Legend:
- Maximum Ratio of Row
- Minimum Ratio of Row
- Mid-Range Ratio of Row
- Median Ratio of Row
- Average Ratio of Row
- Median Average

Column Dynamics – 11 Year Spread

Legend:
- Maximum Ratio of Column
- Minimum Ratio of Column
- Mid-Range Ratio of Column
- Median Ratio of Column
- Average Ratio of Column
- Median Average

12-YEAR SPREAD

12 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics -12 Year Spread

Column Dynamics - 12 Year Spread

13-YEAR SPREAD

13 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

		1		2		3		4		5		6		7		8		9		10			A	B	C	D	E	F	G
		YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP		Maximum Ratio of Row	Minimum Ratio of Row	Spread	Mid-Range Ratio of Row	Median Ratio of Row	Average Ratio of Row	Median Average
1	Year	1881	42.4000	1894	55.9000	1907	109.2000	1920	140.0000	1933	141.5000	1946	312.6000	1959	475.9000	1972	803.4814	1985	1174.0716	1998	1764.5370								
	14	1868	23.1000	1881	42.4000	1894	55.9000	1907	109.2000	1920	140.0000	1933	141.5000	1946	312.6000	1959	475.9000	1972	803.4814	1985	1174.0716								
	Ratio		1.8354978		1.3183962		1.9534884		1.282051282		1.01071429		2.20918728		1.5223928		1.6883408		1.46123059		1.50292112		2.209187	1.010714	1.198473	1.609951	1.512657	1.578422	1.545540

(remainder of the dense data grid omitted for legibility)

Row Dynamics – 13 Year Spread

(line chart, x-axis 1–13, y-axis 0.000000–3.000000; series: Maximum Ratio of Row, Minimum Ratio of Row, Mid-Range Ratio of Row, Median Ratio of Row, Average Ratio of Row, Median Average)

Column Dynamics – 13 Year Spread

(line chart, x-axis 1–10, y-axis 0.000000–3.000000; series: Maximum Ratio of Column, Minimum Ratio of Column, Mid-Range Ratio of Column, Median Ratio of Column, Average Ratio of Column, Median Average)

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14-YEAR SPREAD

14 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

		1		2		3		4		5		6		7		8		9		10		A	B	C	D	E	F	G
		YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	Maximum Ratio of Row	Minimum Ratio of Row	Spread	Mid-Range Ratio of Row	Median Ratio of Row	Average Ratio of Row	Median Average
1	Year	1882	42.4000	1896	61.3000	1910	120.1000	1924	165.5000	1938	192.9000	1952	395.1000	1966	658.1000	1980	996.8309	1994	1514.3943	2008	2198.6295							
	14	Est. *	23.1000	1882	42.4000	1896	61.3000	1910	120.1000	1924	165.5000	1938	192.9000	1952	395.1000	1966	658.1000	1980	996.8309	1994	1514.3943							
	Ratio		1.8354978		1.4457547		1.959217		1.3780183		1.1655589		2.04821151		1.66565426		1.51471037		1.51920882		1.45182103	2.048212	1.165559	0.882653	1.606885	1.516960	1.598365	1.557662
2	Year	1883	42.4000	1897	67.1000	1911	123.2000	1925	179.4000	1939	209.4000	1953	412.8000	1967	675.2000	1981	1010.8394	1995	1546.7308	2009	2208.7984							
	14	1869	23.1000	1883	42.4000	1897	67.1000	1911	123.2000	1925	179.4000	1939	209.4000	1953	412.8000	1967	675.2000	1981	1010.8394	1995	1546.7308							
	Ratio		1.8354978		1.5825472		1.8360656		1.4561688		1.1672241		1.9713467		1.63565891		1.497096268		1.53014495		1.4280432	1.971347	1.167224	0.804123	1.569285	1.556346	1.593979	1.575163
3	Year	1884	42.4000	1898	68.6000	1912	130.2000	1926	190.0000	1940	227.2000	1954	407.0000	1968	706.6000	1982	995.1411	1996	1615.0033	2010	2270.9907							
	14	1870	23.1000	1884	42.4000	1898	68.6000	1912	130.2000	1926	190.0000	1940	227.2000	1954	407.0000	1968	706.6000	1982	995.1411	1996	1615.0033							
	Ratio		1.8354978		1.6179245		1.8979592		1.4592934		1.1957895		1.79137324		1.73611794		1.408351401		1.62288875		1.4061833	1.897959	1.195789	0.702170	1.546874	1.620407	1.597138	1.608772
4	Year	1885	42.4000	1899	74.8000	1913	131.4000	1927	189.9000	1941	263.7000	1955	438.0000	1969	725.6000	1983	1072.5727	1997	1681.8760								
	14	1871	23.1000	1885	42.4000	1899	74.8000	1913	131.4000	1927	189.9000	1941	263.7000	1955	438.0000	1969	725.6000	1983	1072.5727								
	Ratio		1.8354978		1.7641509		1.7566845		1.4452055		1.3886256		1.66097838		1.656621		1.478187293		1.56807646			1.835498	1.388626	0.446872	1.612062	1.612349	1.617114	1.614731
5	Year	1886	42.4000	1900	76.9000	1914	125.6000	1928	190.9000	1942	297.8000	1956	446.1000	1970	722.5000	1984	1129.4464	1998	1764.5370								
	14	1872	23.1000	1886	42.4000	1900	76.9000	1914	125.6000	1928	190.9000	1942	297.8000	1956	446.1000	1970	722.5000	1984	1129.4464								
	Ratio		1.8354978		1.8136792		1.63329		1.5199045		1.55979		1.49798522		1.61959202		1.563247612		1.56230256			1.835498	1.497985	0.337513	1.666742	1.562775	1.622831	1.592803
6	Year	1887	42.4000	1901	85.7000	1915	124.5000	1929	203.6000	1943	337.1000	1957	452.5000	1971	751.2051	1985	1174.0716	1999	1854.0672								
	14	1873	23.1000	1887	42.4000	1901	85.7000	1915	124.5000	1929	203.6000	1943	337.1000	1957	452.5000	1971	751.2051	1985	1174.0716								
	Ratio		1.8354978		2.0212264		1.4527421		1.6353414		1.6556974		1.34233165		1.66012177		1.562917504		1.57917728			2.021226	1.342332	0.678895	1.681779	1.607259	1.638339	1.622799
7	Year	1888	42.4000	1902	86.5000	1916	134.4000	1930	183.5000	1944	361.3000	1958	447.3000	1972	803.4814	1986	1203.2684	2000	1911.3209								
	14	1874	23.1000	1888	42.4000	1902	86.5000	1916	134.4000	1930	183.5000	1944	361.3000	1958	447.3000	1972	803.4814	1986	1203.2684								
	Ratio		1.8354978		2.0400943		1.5537570		1.3653274		1.9689373		1.23802934		1.79629197		1.497568456		1.58844103			2.040094	1.238029	0.802065	1.639062	1.571099	1.653772	1.612435
8	Year	1889	49.1000	1903	90.8000	1917	135.2000	1931	169.3000	1945	355.2000	1959	475.9000	1973	839.4182	1987	1256.1826	2001	1925.1794								
	14	1875	23.1000	1889	49.1000	1903	90.8000	1917	135.2000	1931	169.3000	1945	355.2000	1959	475.9000	1973	839.4182	1987	1256.1826								
	Ratio		2.1255411		1.8492872		1.4889868		1.2522189		2.0980508		1.33980856		1.76385417		1.496491975		1.53256334			2.125541	1.252219	0.873322	1.688880	1.514528	1.660756	1.587642
9	Year	1890	52.7000	1904	89.7000	1918	151.8000	1932	144.2000	1946	312.6000	1960	487.7000	1974	821.7401	1988	1303.1774	2002	1957.1959								
	14	1876	23.1000	1890	52.7000	1904	89.7000	1918	151.8000	1932	144.2000	1946	312.6000	1960	487.7000	1974	821.7401	1988	1303.1774								
	Ratio		2.2813853		1.7020873		1.6923077		0.9499341		2.1678225		1.56014075		1.68492946		1.585875388		1.50186452			2.281385	0.949934	1.331451	1.615660	1.635402	1.680705	1.658054
10	Year	1891	55.1000	1905	96.3000	1919	146.4000	1933	141.5000	1947	309.9000	1961	497.2000	1975	843.0778	1989	1340.0434	2003	2036.0677								
	14	1877	23.1000	1891	55.1000	1905	96.3000	1919	146.4000	1933	141.5000	1947	309.9000	1961	497.2000	1975	843.0778	1989	1340.0434								
	Ratio		2.3852814		1.7477314		1.5202492		0.9665301		2.190106		1.60438851		1.69565125		1.589465883		1.5194043			2.385281	0.966530	1.418751	1.675906	1.596927	1.690979	1.643953
11	Year	1892	60.4000	1906	107.5000	1920	140.0000	1934	154.3000	1948	323.7000	1962	529.5000	1976	879.3138	1990	1351.3622	2004	2093.6810								
	14	1878	42.4000	1892	60.4000	1906	107.5000	1920	140.0000	1934	154.3000	1948	323.7000	1962	529.5000	1976	879.3138	1990	1351.3622								
	Ratio		1.4245283		1.7798013		1.3023256		1.1021429		2.0978613		1.63577386		1.66064929		1.536837247		1.5493115			2.097881	1.102143	0.995718	1.600002	1.592543	1.565470	1.579006
12	Year	1893	57.5000	1907	109.2000	1921	127.8000	1935	169.5000	1949	324.1000	1963	551.0000	1977	922.6690	1991	1360.3512	2005	2151.0247								
	14	1879	42.4000	1893	57.5000	1907	109.2000	1921	127.8000	1935	169.5000	1949	324.1000	1963	551.0000	1977	922.6690	1991	1360.3512								
	Ratio		1.3561321		1.8991304		1.1703297		1.3262911		1.9120944		1.70009256		1.67453539		1.474365347		1.58122748			1.912094	1.170330	0.741765	1.541212	1.627881	1.566022	1.596952
13	Year	1894	55.9000	1908	100.2000	1922	148.0000	1936	193.0000	1950	355.3000	1964	581.1000	1978	985.8821	1992	1418.0149	2006	2201.9891								
	14	1880	42.4000	1894	55.9000	1908	100.2000	1922	148.0000	1936	193.0000	1950	355.3000	1964	581.1000	1978	985.8821	1992	1418.0149								
	Ratio		1.3183962		1.7924866		1.4770459		1.3040541		1.8409326		1.63551928		1.69657907		1.438320972		1.55286739			1.840933	1.304054	0.536879	1.572493	1.594193	1.561800	1.577997
14	Year	1895	62.6000	1909	116.8000	1923	165.9000	1937	203.2000	1951	383.4000	1965	617.8000	1979	1001.7304	1993	1454.1409	2007	2272.2615								
	14	1881	42.4000	1895	62.6000	1909	116.8000	1923	165.9000	1937	203.2000	1951	383.4000	1965	617.8000	1979	1001.7304	1993	1454.1409								
	Ratio		1.4764151		1.8658147		1.4203767		1.2248342		1.886811		1.61137194		1.62144772		1.451629001		1.56261439			1.886811	1.224834	0.661977	1.555823	1.586993	1.569035	1.578014
A	Maximum Ratio of Column		2.385281		2.040094		1.959217		1.635341		2.190106		2.048212		1.796292		1.589466		1.622889									
B	Minimum Ratio of Column		1.318396		1.445755		1.170330		0.949934		1.165559		1.238029		1.619592		1.408351		1.501865			Max. of F - Rows	Min. of F - Rows	Mid-Range of F - Rows	Median of F - Rows	Avg. of F - Rows	Mid-Range + Average/ 2	Median + Average/2
C	Spread		1.066885		0.594340		0.788887		0.685407		1.024547		0.810182		0.176700		0.181114		0.121024			1.690979	1.561800	1.626389	1.607740	1.615450	1.620920	1.611595
D	Mid-Range Ratio of Column		1.851839		1.742925		1.564773		1.292638		1.677832		1.643120		1.707942		1.498909		1.562377									
E	Median Ratio of Column		1.835498		1.779801		1.520249		1.326291		1.840933		1.635519		1.665654		1.497096		1.552867			Max. of F - Columns	Min. of F - Columns	Mid-Range of F - Columns	Median of F - Columns	Avg. of F - Columns	Mid-Range + Average/ 2	Median + Average/2
F	Average Ratio of Column		1.801155		1.780123		1.582953		1.313233		1.735392		1.616954		1.683407		1.506790		1.555007			1.801155	1.313233	1.557194	1.616954	1.619446	1.588320	1.618200
G	Median Average		1.818326		1.779962		1.551601		1.319762		1.788162		1.626236		1.674531		1.501943		1.553937									

Row Dynamics - 14 Year Spread

Maximum Ratio of Row / Minimum Ratio of Row / Mid-Range Ratio of Row / Median Ratio of Row / Average Ratio of Row / Median Average

Column Dynamics - 14 Year Spread

Maximum Ratio of Column / Minimum Ratio of Column / Mid-Range Ratio of Column / Median Ratio of Column / Average Ratio of Column / Median Average

15-YEAR SPREAD

15 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

Row Dynamics - 15 Year Spread

Legend: Maximum Ratio of Row, Minimum Ratio of Row, Mid-Range Ratio of Row, Median Ratio of Row, Average Ratio of Row, Median Average

Column Dynamics - 15 Year Spread

Legend: Maximum Ratio of Column, Minimum Ratio of Column, Mid-Range Ratio of Column, Median Ratio of Column, Average Ratio of Column, Median Average

16-YEAR SPREAD

16 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

		1		2		3		4		5		6		7		8			A	B	C	D	E	F	G
		YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP		Maximum Ratio of Row	Minimum Ratio of Row	Spread	Mid-Range Ratio of Row	Median Ratio of Row	Average Ratio of Row	Median Average
1	Year	1884	42.4000	1900	76.9000	1916	134.4000	1932	144.2000	1948	323.7000	1964	581.1000	1980	996.8309	1996	1615.0033								
	14	1868	23.1000	1884	42.4000	1900	76.9000	1916	134.4000	1932	144.2000	1948	323.7000	1964	581.1000	1980	996.8309								
	Ratio		1.8354978		1.8136792		1.7477243		1.072916667		2.24479889		1.79518072		1.71542058		1.62013768		2.244799	1.072917	1.171882	1.658858	1.771453	1.730669	1.751061
2	Year	1885	42.4000	1901	85.7000	1917	135.2000	1933	141.5000	1949	324.1000	1965	617.8000	1981	1010.8394	1997	1681.8760								
	14	1869	23.1000	1885	42.4000	1901	85.7000	1917	135.2000	1933	141.5000	1949	324.1000	1965	617.8000	1981	1010.8394								
	Ratio		1.8354978		2.0212264		1.5775963		1.046597633		2.29045936		1.90620179		1.63619197		1.66384096		2.290459	1.046598	1.243862	1.668528	1.749669	1.747202	1.748435
3	Year	1886	42.4000	1902	86.5000	1918	151.8000	1934	154.3000	1950	355.3000	1966	658.1000	1982	995.1411	1998	1764.5370								
	14	1870	23.1000	1886	42.4000	1902	86.5000	1918	151.8000	1934	154.3000	1950	355.3000	1966	658.1000	1982	995.1411								
	Ratio		1.8354978		2.0400943		1.7549133		1.016469038		2.30265716		1.85223755		1.51214268		1.77315257		2.302657	1.016469	1.286188	1.659563	1.804325	1.760896	1.782610
4	Year	1887	42.4000	1903	90.8000	1919	146.4000	1935	169.5000	1951	383.4000	1967	675.2000	1983	1072.5727	1999	1854.0672								
	14	1871	23.1000	1887	42.4000	1903	90.8000	1919	146.4000	1935	169.5000	1951	383.4000	1967	675.2000	1983	1072.5727								
	Ratio		1.8354978		2.1415094		1.6123348		1.157786885		2.2619469		1.76108503		1.58852592		1.72861681		2.261947	1.157787	1.104160	1.709867	1.744851	1.760913	1.752882
5	Year	1888	42.4000	1904	89.7000	1920	140.0000	1936	193.0000	1952	395.1000	1968	706.6000	1984	1129.4464	2000	1911.3209								
	14	1872	23.1000	1888	42.4000	1904	89.7000	1920	140.0000	1936	193.0000	1952	395.1000	1968	706.6000	1984	1129.4464								
	Ratio		1.8354978		2.115566		1.5607581		1.378571429		2.04715026		1.788408		1.598424		1.69226348		2.115566	1.378571	0.736995	1.747069	1.740336	1.752080	1.746208
6	Year	1889	49.1000	1905	96.3000	1921	127.8000	1937	203.2000	1953	412.8000	1969	725.6000	1985	1174.0716	2001	1925.1794								
	14	1873	23.1000	1889	49.1000	1905	96.3000	1921	127.8000	1937	203.2000	1953	412.8000	1969	725.6000	1985	1174.0716								
	Ratio		2.1255411		1.9613035		1.3271028		1.589984351		2.03149606		1.75775194		1.61807001		1.63974616		2.125541	1.327103	0.798438	1.726322	1.698749	1.756374	1.727562
7	Year	1890	52.7000	1906	107.5000	1922	148.0000	1938	192.9000	1954	407.0000	1970	722.5000	1986	1203.2684	2002	1957.1959								
	14	1874	23.1000	1890	52.7000	1906	107.5000	1922	148.0000	1938	192.9000	1954	407.0000	1970	722.5000	1986	1203.2684								
	Ratio		2.281385		2.0398482		1.3767442		1.303378379		2.1099015		1.77518428		1.66542319		1.62656631		2.281385	1.303378	0.978007	1.792382	1.720304	1.772304	1.746304
8	Year	1891	55.1000	1907	109.2000	1923	165.9000	1939	209.4000	1955	438.0000	1971	751.2051	1987	1256.1826	2003	2036.0677								
	14	1875	23.1000	1891	55.1000	1907	109.2000	1923	165.9000	1939	209.4000	1955	438.0000	1971	751.2051	1987	1256.1826								
	Ratio		2.3852814		1.9818512		1.5192308		1.262206148		2.09169054		1.71508014		1.67222321		1.62083737		2.385281	1.262206	1.123075	1.823744	1.693652	1.781050	1.737351
9	Year	1892	60.4000	1908	100.2000	1924	165.5000	1940	227.2000	1956	446.1000	1972	803.4814	1988	1303.1774	2004	2093.6810								
	14	1876	23.1000	1892	60.4000	1908	100.2000	1924	165.5000	1940	227.2000	1956	446.1000	1972	803.4814	1988	1303.1774								
	Ratio		2.6147186		1.6589404		1.6516966		1.372809668		1.96346831		1.80112396		1.62191359		1.60659708		2.614719	1.372810	1.241909	1.993764	1.655319	1.786409	1.720864
10	Year	1893	57.5000	1909	116.8000	1925	179.4000	1941	263.7000	1957	452.5000	1973	839.4182	1989	1340.0434	2005	2151.0247								
	14	1877	23.1000	1893	57.5000	1909	116.8000	1925	179.4000	1941	263.7000	1957	452.5000	1973	839.4182	1989	1340.0434								
	Ratio		2.4891775		2.0313043		1.5359589		1.469899666		1.71596511		1.85506785		1.59639546		1.60519032		2.489177	1.469900	1.019278	1.979539	1.660578	1.787370	1.723974
11	Year	1894	55.9000	1910	120.1000	1926	190.0000	1942	297.8000	1958	447.3000	1974	821.7401	1990	1351.3622	2006	2201.9891								
	14	1878	42.4000	1894	55.9000	1910	120.1000	1926	190.0000	1942	297.8000	1958	447.3000	1974	821.7401	1990	1351.3622								
	Ratio		1.3183962		2.1484794		1.582015		1.567368421		1.50201478		1.83711178		1.64451291		1.62945885		2.148479	1.318396	0.830083	1.733438	1.605737	1.653670	1.629703
12	Year	1895	62.6000	1911	123.2000	1927	189.9000	1943	337.1000	1959	475.9000	1975	843.0778	1991	1360.3512	2007	2272.2615								
	14	1879	42.4000	1895	62.6000	1911	123.2000	1927	189.9000	1943	337.1000	1959	475.9000	1975	843.0778	1991	1360.3512								
	Ratio		1.4764151		1.9680511		1.5413961		1.775144813		1.41174726		1.77154402		1.61355358		1.67034917		1.968051	1.411747	0.556304	1.689899	1.641951	1.653525	1.647738
13	Year	1896	61.3000	1912	130.2000	1928	190.9000	1944	361.3000	1960	487.7000	1976	879.3138	1992	1418.0149	2008	2198.6295								
	14	1880	42.4000	1896	61.3000	1912	130.2000	1928	190.9000	1944	361.3000	1960	487.7000	1976	879.3138	1992	1418.0149								
	Ratio		1.4457547		2.1239804		1.4662058		1.892613934		1.34984777		1.80298093		1.61263806		1.55049816		2.123980	1.349848	0.774133	1.736914	1.581568	1.655565	1.618567
14	Year	1897	67.1000	1913	131.4000	1929	203.6000	1945	355.2000	1961	497.2000	1977	922.6690	1993	1454.1409	2009	2208.7984								
	14	1881	42.4000	1897	67.1000	1913	131.4000	1929	203.6000	1945	355.2000	1961	497.2000	1977	922.6690	1993	1454.1409								
	Ratio		1.5825472		1.9582712		1.5494673		1.744597925		1.39977477		1.85573009		1.57601578		1.51897137		1.958271	1.399775	0.558496	1.679023	1.579281	1.648172	1.613727
15	Year	1898	68.6000	1914	125.6000	1930	183.5000	1946	312.6000	1962	529.5000	1978	985.8821	1994	1514.3943	2010	2270.9907								
	14	1882	42.4000	1898	68.6000	1914	125.6000	1930	183.5000	1946	312.6000	1962	529.5000	1978	985.8821	1994	1514.3943								
	Ratio		1.6179245		1.8309038		1.4609873		1.703542234		1.69385797		1.86191143		1.53608053		1.49960329		1.861911	1.460987	0.400924	1.661449	1.655891	1.650601	1.653246
16	Year	1899	74.8000	1915	124.5000	1931	169.3000	1947	309.9000	1963	551.0000	1979	1001.7304	1995	1546.7308	2010	2270.9907								
	14	1883	42.4000	1899	74.8000	1915	124.5000	1931	169.3000	1947	309.9000	1963	551.0000	1979	1001.7304	1994	1514.3943								
	Ratio		1.7641509		1.6644385		1.3598394		1.830478441		1.7779929		1.8180225		1.54405896		1.49960329		1.830478	1.359839	0.470639	1.595159	1.714295	1.657323	1.685809
A	Maximum Ratio of Column		2.614719		2.141509		1.754913		1.892614		2.302657		1.906202		1.715421		1.773153								
B	Minimum Ratio of Column		1.318396		1.658940		1.327103		1.016469		1.349848		1.715080		1.512143		1.499603								
C	Spread		1.296322		0.482569		0.427810		0.876145		0.952809		0.191122		0.203278		0.273549								
D	Mid-Range Ratio of Column		1.966557		1.900225		1.541008		1.454541		1.826252		1.810641		1.613782		1.636378								
E	Median Ratio of Column		1.835498		1.981851		1.549467		1.469900		1.963468		1.802981		1.612638		1.620837								
F	Average Ratio of Column		1.810024		1.834436		1.440122		1.351062		1.793297		1.694844		1.506692		1.519748								
G	Median Average		1.822761		1.908143		1.494795		1.410481		1.878383		1.748913		1.559665		1.570293								

Additional summary cells (right/bottom):

	Max. of F - Rows	Min. of F - Rows	Mid-Range of F - Rows	Median of F - Rows	Avg. of F - Rows	Range + Average/2	Median + Average/2
C / Spread	2.614719	1.016469	1.815594	1.749641	1.722133	1.768863	1.735887

	Max. of F - Columns	Min. of F - Columns	Mid-Range of F - Columns	Median of F - Columns	Avg. of F - Columns	Range + Average/2	Median + Average/2
F	2.614719	1.016469	1.404881	1.607296	1.618778	1.511831	1.613037

Row Dynamics - 16 Year Spread

Legend: Maximum Ratio of Row; Minimum Ratio of Row; Mid-Range Ratio of Row; Median Ratio of Row; Average Ratio of Row; Median Average

Column Dynamics - 16 Year Spread

Legend: Maximum Ratio of Column; Minimum Ratio of Column; Mid-Range Ratio of Column; Median Ratio of Column; Average Ratio of Column; Median Average

17-YEAR SPREAD

17 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

[Large data table of 17-year GNP ratios with columns 1–7, rows 1–17, and summary rows A–G: Maximum Ratio of Column, Minimum Ratio of Column, Spread, Mid-Range Ratio of Column, Median Ratio of Column, Average Ratio of Column, Median Average; and summary columns A–G: Maximum Ratio of Rows, Minimum Ratio of Rows, Spread, Mid-Range Ratio of Rows, Median Ratio of Rows, Average Ratio of Rows, Median Average.]

Row Dynamics – 17 Year Spread

Legend:
- Maximum Ratio of Row
- Minimum Ratio of Row
- Mid-Range Ratio of Row
- Median Ratio of Row
- Average Ratio of Row
- Median Average

Column Dynamics – 17 Year Spread

Legend:
- Maximum Ratio of Column
- Minimum Ratio of Column
- Mid-Range Ratio of Column
- Median Ratio of Column
- Average Ratio of Column
- Median Average

18-YEAR SPREAD

18 YEAR RATIOS BASED ON ANNUAL REAL GNP; MULTIPLE 5.962552

		1		2		3		4		5		6		7		A Maximum Ratio of Row	B Minimum Ratio of Row	C Spread	D Mid-Range Ratio of Row	E Median Ratio of Row	F Average Ratio of Row	G Median Average
		YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP	YEAR	GNP							
1	Year	1886	42.4000	1904	89.7000	1922	148.0000	1940	227.2000	1958	447.3000	1976	879.3138	1994	1514.3943							
	14	1868	23.1000	1886	42.4000	1904	89.7000	1922	148.0000	1940	227.2000	1958	447.3000	1976	879.3138							
	Ratio		1.8354978		2.115566		1.6499443		1.535135135		1.96875		1.96582562		1.72224557	2.115566	1.535135	0.580431	1.825351	1.835498	1.827566	1.831532
2	Year	1887	42.4000	1905	96.3000	1923	165.9000	1941	263.7000	1959	475.9000	1977	922.6690	1995	1546.7308							
	14	1869	23.1000	1887	42.4000	1905	96.3000	1923	165.9000	1941	263.7000	1959	475.9000	1977	922.6690							
	Ratio		1.8354978		2.2712264		1.7227414		1.589511754		1.80470231		1.93878756		1.67636585	2.271226	1.589512	0.681715	1.930369	1.804702	1.834119	1.819411
3	Year	1888	42.4000	1906	107.5000	1924	165.5000	1942	297.8000	1960	487.7000	1978	985.8821	1996	1615.0033							
	14	1870	23.1000	1888	42.4000	1906	107.5000	1924	165.5000	1942	297.8000	1960	487.7000	1978	985.8821							
	Ratio		1.8354978		2.5353774		1.5395349		1.79939577		1.63767629		2.02149293		1.63813026	2.535377	1.539535	0.995842	2.037456	1.799396	1.858158	1.828777
4	Year	1889	49.1000	1907	109.2000	1925	179.4000	1943	337.1000	1961	497.2000	1979	1001.7304	1997	1681.8760							
	14	1871	23.1000	1889	49.1000	1907	109.2000	1925	179.4000	1943	337.1000	1961	497.2000	1979	1001.7304							
	Ratio		2.1255411		2.2240326		1.6428571		1.879041249		1.47493325		2.01474336		1.67897071	2.224033	1.474933	0.749099	1.849483	1.879041	1.862874	1.870958
5	Year	1890	52.7000	1908	100.2000	1926	190.0000	1944	361.3000	1962	529.5000	1980	996.8309	1998	1764.5370							
	14	1872	23.1000	1890	52.7000	1908	100.2000	1926	190.0000	1944	361.3000	1962	529.5000	1980	996.8309							
	Ratio		2.2813853		1.9013283		1.8962076		1.901578947		1.4655411		1.88258905		1.77014677	2.281385	1.465541	0.815844	1.873463	1.896208	1.871254	1.883731
6	Year	1891	55.1000	1909	116.8000	1927	189.9000	1945	355.2000	1963	551.0000	1981	1010.8394	1999	1854.0672							
	14	1873	23.1000	1891	55.1000	1909	116.8000	1927	189.9000	1945	355.2000	1963	551.0000	1981	1010.8394							
	Ratio		2.3852814		2.1197822		1.6258562		1.870458136		1.55123874		1.83455426		1.83418573	2.385281	1.551239	0.834043	1.968260	1.834554	1.888765	1.861660
7	Year	1892	60.4000	1910	120.1000	1928	190.9000	1946	312.6000	1964	581.1000	1982	995.1411	2000	1911.3209							
	14	1874	23.1000	1892	60.4000	1910	120.1000	1928	190.9000	1946	312.6000	1964	581.1000	1982	995.1411							
	Ratio		2.6147186		1.9884106		1.5895087		1.637506548		1.85892514		1.71251265		1.92065316	2.614719	1.589509	1.025210	2.102114	1.858925	1.903176	1.881051
8	Year	1893	57.5000	1911	123.2000	1929	203.6000	1947	309.9000	1965	617.8000	1983	1072.5727	2001	1925.1794							
	14	1875	23.1000	1893	57.5000	1911	123.2000	1929	203.6000	1947	309.9000	1965	617.8000	1983	1072.5727							
	Ratio		2.4891775		2.1426087		1.6525974		1.522102161		1.99354631		1.73611638		1.7949174	2.489177	1.522102	0.967075	2.005640	1.794917	1.904438	1.849678
9	Year	1894	55.9000	1912	130.2000	1930	183.5000	1948	323.7000	1966	658.1000	1984	1129.4464	2002	1957.1959							
	14	1876	23.1000	1894	55.9000	1912	130.2000	1930	183.5000	1948	323.7000	1966	658.1000	1984	1129.4464							
	Ratio		2.4199134		2.3291592		1.4093702		1.764032698		2.0330553		1.71622307		1.73288073	2.419913	1.409370	1.010543	1.914642	1.764033	1.914948	1.839490
10	Year	1895	62.6000	1913	131.4000	1931	169.3000	1949	324.1000	1967	675.2000	1985	1174.0716	2003	2036.0677							
	14	1877	23.1000	1895	62.6000	1913	131.4000	1931	169.3000	1949	324.1000	1967	675.2000	1985	1174.0716							
	Ratio		2.7099567		2.0990415		1.2884323		1.914335219		2.08330762		1.73885012		1.73419381	2.709957	1.288432	1.421524	1.999194	1.914353	1.938305	1.926329
11	Year	1896	61.3000	1914	125.6000	1932	144.2000	1950	355.3000	1968	706.6000	1986	1203.2684	2004	2093.6810							
	14	1878	42.4000	1896	61.3000	1914	125.6000	1932	144.2000	1950	355.3000	1968	706.6000	1986	1203.2684							
	Ratio		1.4457547		2.0489396		1.1480892		2.463938974		1.98874191		1.70289895		1.739995	2.463939	1.148089	1.315850	1.806014	1.739995	1.791194	1.765595
12	Year	1897	67.1000	1915	124.5000	1933	141.5000	1951	383.4000	1969	725.6000	1987	1256.1826	2005	2151.0247							
	14	1879	42.4000	1897	67.1000	1915	124.5000	1933	141.5000	1951	383.4000	1969	725.6000	1987	1256.1826							
	Ratio		1.5825472		1.8554396		1.1365462		2.709540636		1.89254043		1.73123291		1.71235034	2.709541	1.136546	1.572994	1.923043	1.731233	1.802885	1.767059
13	Year	1898	68.6000	1916	134.4000	1934	154.3000	1952	395.1000	1970	722.5000	1988	1303.1774	2006	2201.9891							
	14	1880	42.4000	1898	68.6000	1916	134.4000	1934	154.3000	1952	395.1000	1970	722.5000	1988	1303.1774							
	Ratio		1.6179245		1.9591837		1.1480655		2.560596241		1.82865097		1.80170574		1.68970786	2.560596	1.148065	1.412531	1.854331	1.803706	1.801119	1.802412
14	Year	1899	74.8000	1917	135.2000	1935	169.5000	1953	412.8000	1971	751.2051	1989	1340.0434	2007	2272.2615							
	14	1881	42.4000	1899	74.8000	1917	135.2000	1935	169.5000	1953	412.8000	1971	751.2051	1989	1340.0434							
	Ratio		1.7641509		1.8074866		1.2536982		2.43539823		1.8197798		1.78385823		1.69566262	2.435398	1.253698	1.181700	1.844548	1.783858	1.794291	1.789074
15	Year	1900	76.9000	1918	151.8000	1936	193.0000	1954	407.0000	1972	803.4814	1990	1351.3622	2008	2198.6295							
	14	1882	42.4000	1900	76.9000	1918	151.8000	1936	193.0000	1954	407.0000	1972	803.4814	1990	1351.3622							
	Ratio		1.8136792		1.9739922		1.2714097		2.10880829		1.97415577		1.68188361		1.62697277	2.108808	1.271410	0.837399	1.690109	1.813679	1.778700	1.796190
16	Year	1901	85.7000	1919	146.4000	1937	203.2000	1955	438.0000	1973	839.4182	1991	1360.3512	2009	2208.7984							
	14	1883	42.4000	1901	85.7000	1919	146.4000	1937	203.2000	1955	438.0000	1973	839.4182	1991	1360.3512							
	Ratio		2.0212264		1.7082847		1.3879781		2.15551811		1.91647991		1.62058816		1.62369717	2.155512	1.387978	0.767534	1.771745	1.708285	1.776252	1.742269
17	Year	1902	86.5000	1920	140.0000	1938	192.9000	1956	446.1000	1974	821.7401	1992	1418.0149	2010	2270.9907							
	14	1884	42.4000	1902	86.5000	1920	140.0000	1938	192.9000	1956	446.1000	1974	821.7401	1992	1418.0149							
	Ratio		2.0400943		1.6184971		1.3778571		2.312597201		1.84205358		1.72562456		1.60152808	2.312597	1.377857	0.934740	1.845227	1.725625	1.788322	1.756973
18	Year	1903	90.8000	1921	127.8000	1939	209.4000	1957	452.5000	1975	843.0778	1993	1454.1409	2010	2270.9907							
	14	1885	42.4000	1903	90.8000	1921	127.8000	1939	209.4000	1957	452.5000	1975	843.0778	1992	1418.0149							
	Ratio		2.1415094		1.407489		1.6384977		2.160936008		1.86315536		1.72480037		1.60152808	2.160936	1.407489	0.753447	1.784212	1.724800	1.791131	1.757966

		1	2	3	4	5	6	7							
A	Maximum Ratio of Column	2.709957	2.535377	1.896208	2.709541	2.083308	2.021493	1.920653							
B	Minimum Ratio of Column	1.445755	1.407489	1.136546	1.522102	1.465541	1.620588	1.601528	Max. of F-Rows 2.709957	Min. of F-Rows 1.136546	Mid-Range of F-Rows 1.923251	Median of F-Rows 1.846138	Avg. of F-Rows 1.846753	Mid-Range+Average/2 1.885002	Median+Average/2 1.846446
C	Spread	1.264202	1.127888	0.759661	1.187438	0.617767	0.400905	0.319125							
D	Mid-Range Ratio of Column	2.077856	1.971433	1.516377	2.115821	1.774424	1.821041	1.761091							
E	Median Ratio of Column	2.021226	2.048940	1.409370	1.914353	1.863155	1.738850	1.695663	Max. of F-Columns 2.709957	Min. of F-Columns 1.136546	Mid-Range of F-Columns 1.429620	Median of F-Columns 1.722694	Avg. of F-Columns 1.740906	Mid-Range+Average/2 1.585263	Median+Average/2 1.731800
F	Average Ratio of Column	1.972978	1.892050	1.401728	1.880917	1.722694	1.701855	1.614119							
G	Median Average	1.997102	1.970495	1.405549	1.897635	1.792925	1.720353	1.654891							

Row Dynamics - 18 Year Spread — Maximum Ratio of Row, Minimum Ratio of Row, Mid-Range Ratio of Row, Median Ratio of Row, Average Ratio of Row, Median Average

Column Dynamics - 18 Year Spread — Maximum Ratio of Column, Minimum Ratio of Column, Mid-Range Ratio of Column, Median Ratio of Column, Average Ratio of Column, Median Average

DATA SET 3 -
VALUES FOR "MIDRANGE MINUS MEDIAN AVERAGE"

Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average
1.420684	1.257599	0.163085	1.353398	1.325104	0.028295	1.352348	1.347649	0.004699	1.417749	1.402263	0.015486	1.616044	1.452544	0.163500	1.512825	1.493969	0.018856
1.319644	1.279068	0.040576	1.326172	1.350297	-0.024125	1.479789	1.337755	0.142034	1.431993	1.401026	0.030967	1.434208	1.443657	-0.009449	1.565342	1.495986	0.069356
1.290117	1.293580	-0.003462	1.371056	1.322612	0.048444	1.522397	1.345267	0.177131	1.500597	1.395069	0.105528	1.455653	1.443306	0.012347	1.565952	1.472512	0.093440
1.324015	1.260418	0.063598	1.440683	1.344659	0.096024	1.511834	1.364345	0.147489	1.436418	1.398507	0.037911	1.452486	1.449358	0.003128	1.573780	1.503586	0.070195
1.361699	1.287513	0.074185	1.436010	1.382905	0.053106	1.428369	1.360640	0.067729	1.519756	1.416638	0.103118	1.425648	1.455403	-0.029755	1.767774	1.502866	0.264908
1.391717	1.285707	0.106011	1.404050	1.364457	0.039593	1.449965	1.391147	0.058818	1.617628	1.402286	0.215342	1.466204	1.442454	0.023750	1.802213	1.500188	0.302025
1.417749	1.266501	0.151248	1.443362	1.296073	0.147289	1.391472	1.371842	0.019630	1.636934	1.412955	0.223979	1.475706	1.432655	0.043051	1.534246	1.483369	0.050876
			1.427996	1.336802	0.091194	1.408532	1.366651	0.041881	1.520196	1.416338	0.103858	1.544457	1.454296	0.090161	1.428599	1.538718	-0.110119
						1.480915	1.365450	0.115465	1.425644	1.412712	0.012932	1.517064	1.441348	0.075716	1.500830	1.527473	-0.026643
									1.452767	1.410216	0.042551	1.700919	1.460360	0.240559	1.629103	1.546336	0.082767
												1.754719	1.423443	0.331276	1.428575	1.479113	-0.050538
															1.466816	1.478568	-0.011752

Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average	Mid-Range Ratio of Row	Median Average	Mid-Range Ratio - Median Average
1.609951	1.545540	0.064411	1.606885	1.557662	0.049223	1.621179	1.679915	-0.058736	1.658858	1.751061	-0.092203	1.728583	1.768989	-0.040406	1.825351	1.831532	-0.006182
1.607890	1.562299	0.045592	1.569285	1.575163	-0.005877	1.576343	1.685776	-0.109433	1.668528	1.748435	-0.079907	1.796469	1.814444	-0.017975	1.930369	1.819411	0.110958
1.527502	1.553554	-0.026052	1.546874	1.608772	-0.061898	1.654362	1.673314	-0.018952	1.659563	1.782610	-0.123047	1.847678	1.821362	0.026316	2.037456	1.828777	0.208679
1.499425	1.577735	-0.078310	1.612062	1.614731	-0.002670	1.640450	1.679591	-0.039142	1.709867	1.752882	-0.043015	1.843046	1.823491	0.019555	1.849483	1.870958	-0.021475
1.531646	1.571672	-0.040025	1.666742	1.592803	0.073939	1.607833	1.715428	-0.107595	1.747069	1.746208	0.000861	1.779455	1.814485	-0.035031	1.873463	1.883731	-0.010268
1.531405	1.568648	-0.037243	1.681779	1.622799	0.058980	1.609890	1.737551	-0.127661	1.726322	1.727562	-0.001240	1.898477	1.757082	0.141395	1.968260	1.861660	0.106600
1.494462	1.583419	-0.088957	1.639062	1.612435	0.026626	1.589751	1.739676	-0.149924	1.792382	1.746304	0.046078	1.991667	1.806185	0.185482	2.102114	1.881051	0.221063
1.608823	1.554593	0.054230	1.688880	1.587642	0.101238	1.746050	1.698917	0.047133	1.823744	1.737351	0.086393	2.030735	1.810631	0.220104	2.005640	1.849678	0.155962
1.753446	1.556557	0.196889	1.615660	1.658054	-0.042394	1.787059	1.695541	0.091518	1.932660	1.659759	0.272901	1.932660	1.879113	0.053546	1.914642	1.839490	0.075152
1.855977	1.548413	0.307564	1.675906	1.643953	0.031953	1.985015	1.722769	0.262246	1.979539	1.723974	0.255565	1.955311	1.860958	0.094354	1.999194	1.926329	0.072865
1.568293	1.478486	0.089807	1.600002	1.579006	0.020996	1.651359	1.633455	0.017904	1.733438	1.629703	0.103735	1.778144	1.694639	0.083504	1.806014	1.765595	0.040420
1.624682	1.500146	0.124536	1.541212	1.596952	-0.055740	1.677351	1.612950	0.064401	1.689899	1.647738	0.042161	1.770028	1.729400	0.040628	1.923043	1.767059	0.155984
1.724109	1.478613	0.245496	1.572493	1.577997	-0.005503	1.597130	1.624830	-0.027700	1.736914	1.618567	0.118348	1.795614	1.961268	-0.165654	1.854331	1.802412	0.051918
			1.555823	1.578014	-0.022191	1.698841	1.610624	0.088217	1.679023	1.613727	0.065296	1.702903	1.768209	-0.065306	1.844548	1.789074	0.055474
						1.699456	1.593296	0.106161	1.661449	1.653246	0.008203	1.781891	1.767960	0.013931	1.690109	1.796190	-0.106081
									1.595159	1.685809	-0.090650	1.813021	1.762594	0.050427	1.771745	1.742269	0.029476
												1.723787	1.773292	-0.049504	1.845227	1.756973	0.088254
															1.784212	1.757966	0.026247

Mid-Range Ratio Minus Median Average

7 Year Spread	8 Year Spread	9 Year Spread	10 Year Spread	11 Year Spread	12 Year Spread	13 Year Spread	14 Year Spread	15 Year Spread	16 Year Spread	17 Year Spread	18 Year Spread
0.163085	0.028295	0.004699	0.015486	-0.1635	0.018856	0.064411	0.049223	-0.058736	-0.092203	-0.040406	-0.006182
0.040576	-0.02412	0.142034	0.030967	0.009449	0.069356	0.045592	-0.005877	-0.109433	-0.079907	-0.017975	0.110958
-0.003462	0.048444	0.177131	0.105528	-0.01235	0.093440	-0.026052	-0.061898	-0.018952	-0.123047	0.026316	0.208679
0.063598	0.096024	0.147489	0.037911	-0.00313	0.070195	-0.078310	-0.002670	-0.039142	-0.043015	0.019555	-0.021475
0.074185	0.053106	0.067729	0.103118	0.029755	0.264908	-0.040025	0.073939	-0.107595	0.000861	-0.035031	-0.010268
0.106011	0.039593	0.058818	0.215342	-0.02375	0.302025	-0.037243	0.058980	-0.127661	-0.001240	0.141395	0.106600
0.151248	0.147289	0.019630	0.223979	-0.04305	0.050876	-0.088957	0.026626	-0.149924	0.046078	0.185482	0.221063
	0.091194	0.041881	0.103858	-0.09016	-0.110119	0.054230	0.101238	0.047133	0.086393	0.220104	0.155962
		0.115465	0.012932	-0.07572	-0.026643	0.196889	-0.042394	0.091518	0.272901	0.053546	0.075152
			0.042551	-0.24056	0.082767	0.307564	0.031953	0.262246	0.255565	0.094354	0.072865
				-0.33128	-0.050538	0.089807	0.020996	0.017904	0.103735	0.083504	0.040420
					-0.011752	0.124536	-0.055740	0.064401	0.042161	0.040628	0.155984
						0.245496	-0.0055	-0.027700	0.118348	-0.165654	0.051918
							-0.02219	0.088217	0.065296	-0.065306	0.055474
								0.106161	0.008203	0.013931	-0.106081
									-0.09065	0.050427	0.029476
										-0.0495	0.088254
											0.026247

DATA SET FOUR.
SCHOOL ENROLLMENT - STUDENT POPULATION

Enrollment of public secondary schools, by state, 2007-08

State	Total	Regular	Junior high	7 to 12	8 to 12	Grades 9-12	10 to 12	11,12-12	Other sec.
Total	16,184,724	15,680,507	1,578,163	927,888	451,656	12,500,341	418,850	41,545	266,281
Alabama	224,711	223,040	20,696	31,465	4,638	153,011	11,021	181	3,699
Alaska	41,004	39,078	7,907	3,433	672	28,726	266	0	0
Arizona	350,928	344,460	47,571	9,488	3,536	279,380	10,038	291	624
Arkansas	177,098	175,870	29,801	35,288	2,801	64,323	29,260	1,305	14,320
California	2,155,154	2,045,990	286,060	67,486	1,280	1,790,115	0	46	10,167
Colorado	253,235	244,201	27,213	8,358	205	207,613	5,787	99	3,960
Connecticut	197,194	183,550	20,092	3,330	5,877	166,038	424	9	1,424
Delaware	40,916	34,271	4,395	116	30,589	5,381	0	0	435
Dist. of Columbia	20,962	18,465	1,218	471	0	19,137	39	0	97
Florida	780,816	763,609	14,554	19,705	27,172	715,591	929	1,709	1,156
Georgia	472,846	467,357	7,694	1,616	3,032	447,166	3,880	89	9,369
Hawaii	63,118	62,939	8,996	5,531	0	48,591	0	0	0
Idaho	94,705	89,494	19,170	5,036	11	54,213	14,112	0	2,163
Illinois	695,769	681,319	64,033	19,151	4,440	589,359	9,091	1,517	8,178
Indiana..........	365,073	363,830	43,486	43,844	673	271,861	3,217	296	1,696
Iowa	171,477	167,360	15,323	18,821	0	126,224	7,571	21	3,517
Kansas	165,490	165,368	24,758	17,523	1,237	115,495	6,462	0	15
Kentucky	207,811	203,021	14,123	9,891	3,962	175,945	2,589	171	1,130
Louisiana	189,919	185,751	19,412	25,680	48,368	89,446	4,921	0	2,092
Maine	65,668	65,618	6,000	2,237	435	56,709	101	0	186
Maryland	280,768	264,881	13,151	1,028	3,431	259,507	272	486	2,893
Massachusetts	319,336	282,426	19,064	21,082	5,328	273,541	0	93	228
Michigan	591,680	557,118	51,998	28,354	21,176	446,232	29,987	2,477	11,456
Minnesota	314,250	299,280	29,259	62,591	9,874	179,606	25,598	2,674	4,648
Mississippi	148,111	148,021	13,128	21,902	3,634	97,600	7,313	362	4,172
Missouri..........	326,470	323,794	38,486	34,044	145	231,179	11,790	622	10,204
Montana	60,355	60,254	13,853	0	0	46,502	0	0	0
Nebraska	112,050	112,034	12,148	28,492	1,749	68,898	165	31	567
Nevada	131,671	126,175	10,970	481	3,660	114,025	1,640	812	83
New Hampshire	70,844	70,844	4,431	0	0	65,765	0	0	648
New Jersey	465,666	438,730	39,712	21,929	2,386	383,611	8,770	1,462	7,796
New Mexico	114,391	111,108	14,395	2,570	950	80,999	9,582	0	5,895
New York	913,079	860,711	50,934	78,176	5,997	729,745	23,676	337	24,214
North Carolina ...	415,325	412,194	13,676	1,409	621	390,498	1,705	355	7,061
North Dakota	38,626	38,617	4,218	11,846	157	16,207	3,770	947	1,481
Ohio	637,089	633,721	62,066	61,315	55,112	441,585	6,376	681	9,954
Oklahoma	199,392	198,585	24,753	0	0	137,023	22,176	4,140	11,300
Oregon	193,303	190,205	18,368	8,481	760	165,054	619	21	0
Pennsylvania	649,436	632,017	64,052	87,655	12,163	425,120	37,389	7,065	15,992
Rhode Island	50,061	47,096	4,033	993	0	44,434	30	0	571
South Carolina ...	221,608	221,526	15,855	4,841	755	188,676	8,388	90	3,003
South Dakota	41,607	41,026	3,921	29	0	37,657	0	0	0
Tennessee	288,904	286,784	12,577	9,050	15,846	246,916	2,268	484	1,763
Texas	1,429,301	1,392,149	181,487	37,720	97,344	1,041,501	10,433	10,566	50,250
Utah	215,405	207,270	71,658	10,861	11,688	46,890	59,578	783	13,947
Vermont	33,156	33,140	2,225	8,677	0	22,254	0	0	0
Virginia	410,561	409,423	26,999	13,741	15,399	348,628	2,971	0	2,823
Washington	357,904	341,744	45,437	19,713	43,622	219,623	21,300	146	8,063
West Virginia	83,502	82,971	4,491	5,684	136	70,499	2,643	12	37
Wisconsin	305,036	301,274	20,879	15,321	533	258,193	5,941	1,165	3,004
Wyoming	31,943	30,798	7,437	1,433	262	18,049	4,762	0	0

SOURCE: U.S. Department of Education, National Center for Education Statistics, Common Core of Data, 2007-08.

DATA SET FIVE.
SCHOOL ENROLLMENT - SCHOOL TYPE

Table 99. Public secondary schools, by grade span, average school size, and state or jurisdiction: 2007-08

State or jurisdiction	Total, all secondary schools	Total, all regular secondary schools\1\	Grades 7 to 8 and 7 to 9	Grades 7 to 12	Grades 8 to 12	Grades 9 to 12	Grades 10 to 12	Other spans ending with grade 12	Other grade spans	Vocational schools\2\	All secondary schools	Regular secondary schools\1\
1	2	3	4	5	6	7	8	9	10	11	12	13
United States	24,426	19,264	3,047	3,278	777	15,179	748	378	1,019	1,409	706	816
Alabama	414	314	34	96	19	226	28	3	8	73	681	709
Alaska	84	65	16	20	3	43	2	0	0	3	494	601
Arizona	667	470	76	36	7	527	10	3	8	166	696	729
Arkansas	393	360	59	134	8	127	42	1	22	24	484	494
California	2,449	1,495	342	321	42	1,679	25	13	27	76	901	1,355
Colorado	410	344	61	60	1	274	7	1	6	5	619	710
Connecticut	261	195	35	12	11	184	11	2	6	17	756	941
Delaware	46	34	7	1	27	10	0	0	1	6	952	1,008
District of Columbia .	38	30	6	3	1	26	1	0	1	5	549	606
Florida	668	475	20	67	30	488	9	19	35	51	1,276	1,667
Georgia	435	392	11	14	8	350	7	2	43	3	1,137	1,201
Hawaii	53	52	11	9	0	33	0	0	0	0	1,191	1,210
Idaho	231	154	40	47	1	115	24	0	4	11	440	593
Illinois	1,007	802	150	67	19	634	11	57	69	55	745	847
Indiana	439	420	75	89	1	265	1	1	7	29	853	866
Iowa	449	381	48	80	1	302	9	4	5	0	392	450
Kansas	392	387	58	81	4	239	8	0	2	1	430	432
Kentucky	465	240	30	43	24	295	12	9	52	126	586	803
Louisiana	310	263	41	49	68	125	18	0	9	6	637	709
Maine	153	124	15	10	2	115	9	0	2	27	525	533
Maryland	277	208	20	6	8	213	2	6	22	24	1,065	1,270
Massachusetts	370	315	33	36	6	293	0	1	1	39	860	894
Michigan	1,082	745	102	96	37	664	64	39	80	55	569	749
Minnesota	894	482	63	298	40	391	57	32	13	11	405	625
Mississippi	321	226	29	60	8	188	26	2	8	89	652	658
Missouri	684	587	80	204	1	350	21	11	17	63	548	557
Montana	352	348	180	1	0	171	0	0	0	0	172	173
Nebraska	329	325	28	181	1	116	1	1	1	0	360	361
Nevada	134	111	23	7	8	87	2	5	2	1	998	1,158
New Hampshire	106	106	18	0	0	85	0	0	3	0	681	681
New Jersey	503	401	60	40	8	352	18	7	18	55	930	1,094
New Mexico	230	200	39	30	7	137	9	0	8	2	527	572
New York	1,059	980	89	132	10	722	24	3	79	29	862	878
North Carolina	516	486	26	10	7	439	6	5	23	10	830	867
North Dakota	186	179	11	105	2	56	3	1	8	6	215	216
Ohio	1,015	928	131	142	80	605	9	17	31	75	664	684
Oklahoma	564	560	84	0	0	417	45	3	15	0	354	355
Oregon	302	270	30	41	12	211	7	1	0	0	620	679
Pennsylvania	815	720	101	162	13	449	59	9	22	87	863	875
Rhode Island	75	52	9	4	0	59	2	0	1	12	795	906
South Carolina	275	222	24	14	5	210	14	3	5	40	974	983
South Dakota	270	257	80	1	1	188	0	0	0	0	164	166
Tennessee	345	308	24	27	18	248	13	10	5	22	868	924
Texas	2,158	1,482	316	215	109	1,185	37	47	249	1	702	948
Utah	305	219	85	45	23	68	48	12	24	8	715	934
Vermont	72	56	8	19	0	30	0	0	15	15	582	592
Virginia	385	343	33	6	36	272	3	0	35	31	1,183	1,197
Washington	574	388	83	67	53	327	24	9	11	11	652	885
West Virginia	130	116	10	19	1	93	2	3	2	31	657	715
Wisconsin	631	561	69	60	4	434	14	36	14	8	495	543
Wyoming	103	86	24	11	2	62	4	0	0	0	310	358
Bureau of Indian Education	21	21	2	5	0	14	0	0	0	0	---	---
DoD, domestic	7	7	2	0	0	5	0	0	0	0	476	476
DoD, overseas	32	32	2	13	0	17	0	0	0	0	453	453
Other jurisdictions												
American Samoa	6	5	0	0	0	5	1	0	0	1	---	---
Guam	0	0	0	0	0	0	0	0	0	0	---	---
Northern Marianas ..	6	6	1	1	0	4	0	0	0	0	727	727
Puerto Rico	398	368	191	28	1	3	158	0	17	27	529	518
U.S. Virgin Islands .	10	8	5	0	0	5	0	0	0	1	803	896

---Not available.
\1\Excludes vocational, special education, and alternative schools.
\2\Vocational schools are also included under appropriate grade span.
\3\Average for schools reporting enrollment data. Enrollment data were available for 22,800 out of 24,426 public secondary schools in 2007-08.
NOTE: Includes schools with no grade lower than 7. Excludes schools not reported by grade level, such as some special education schools for the disabled. DoD = Department of Defense.
SOURCE: U.S. Department of Education, National Center for Education Statistics, Common Core of Data (CCD), "Public Elementary/Secondary School Universe Survey," 2007-08. (This table was prepared September 2009.)

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Additional information regarding the Golden Mean association with quasi-crystals may be found at:

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