

Income Transfer as Model of Economic Growth

Costa Junior, Celso Jose and Sampaio, Armando Vaz and Gonçalves, Flávio de Oliveria

Universidade Positivo - UP, Universidade Federal do Paraná - UFPR

10 December 2012

Online at https://mpra.ub.uni-muenchen.de/45494/ MPRA Paper No. 45494, posted 25 Mar 2013 04:46 UTC

Income Transfer as Model of Economic Growth

Celso Jose Costa Junior^{*} Armando Vaz Sampaio[†] Flavio de Oliveira Goncalves[‡]

First Draft Version

Abstract

This work aims to study the main Brazilian economic growth influenced by an income transfer program. For this purpose, we used the DSGE approach. The estimation of the parameters was performed using the Bayesian methodology and analysis of results was done by impulse response functions. The basic characteristic of this paper is to use two types of consumers: ricardian individuals and non-ricardian individuals. The first agents maximize intertemporally its utility function, while the second type of agents is limited to consume the amount received through income transfer. The results show that implantation this program brings positive returns for the whole economy, except for individuals ricardian.

Keyword: DSGE Models; Bayesian Estimation; and Income Transfers. JEL: C63; E37; E62.

^{*}Professor of Business School - Universidade Positivo

[†]Professor of PPGDE - Universidade Federal do Parana

[‡]Professor of PPGDE - Universidade Federal do Parana

1 Introduction

This study aims to examine the proposal of economic growth adopted by the Brazilian government in recent years - consumption fostered by income transfer policy. Considering that in December 2009, the Bolsa Familia¹ represented 12,370,915 benefits, and since the consolidation of this program, it settled a broad debate about its potential to reduce poverty and promote fall in income inequality existing in Brazil (Castro and Modesto , 2010).

The per capita income in Brazil increased 1.4% and 1% per year in the periods 1981-1995 and 1995-2003, respectively. After 2003 the combination of renewed economic growth with the expansion of income transfer programs promoted, significantly, the improve of per capita income, 5% per year (Castro and Modesto, 2010). Note that the per capita income grew 3.5 times over the period of expansion of these programs when compared to the other two periods. The modeling tool DSGE (*Dynamic Stochastic General Equilibrium*) was chosen due its ability to analyze the movements of economic variables in relation to an exogenous shock (Income Transfer). Through this approach, it is expected to study the behavior of key macroeconomic variables after the implementation of the social program.

Over the past twenty years have seen tremendous advances in tools mathematical, statistical, probabilistic and computing available for applied macroeconomists. This huge set of tools has changed the way researchers approach test models, validate theories or simply seek regularities in the data. The rational expectations and the calibration revolutions also forced researchers to try to build a stronger bridge between theoretical and applied work, a bridge was absent in most applied exercises conducted in the 1970s and 1980s (Canova , 2007). The work of Kydland and Prescott (1982) "*Time to Build and Aggregate Fluctuations*" revolutionized modern macroeconomics, but the first steps of this methodology are given by Ramsey [(Ramsey , 1927) and (Ramsey , 1928)], Cass (1965), Koopmans (1965) and Brock and Mirnam (1972).

One key assumption of DSGE models is that individuals are optimizers and, therefore, they can determine an optimal basket of consumption since one can to be separate to his income, fulfilling the hypothesis of the life cycle permanent

¹The Bolsa Familia Program was created in 2003 with the goal of unifying the income transfer programs started at the municipal, state and federal levels since 1995. It is conceived as an expression of the development process of these programs in Brazil.

income. For this, individuals use the variable investment to carry income intertemporally. However, empirical evidence shows that there is a certain relationship between consumption and current income [(Campbell and Mankiw , 1989), (Deaton , 1992), (Wolff , 2003), and (Johnson et al , 2006)], demonstrating a breach of that basic assumption.

The economic literature shows different elements that cause deviations from the theory of the life cycle permanent income. The main explanation for this result is due to the capital market is not perfect and therefore the existence of liquidity constraint for some individuals. Assuming this explanation, this paper develops a model in which there are two types of agents: ricardian agents and agents which have liquidity constraint denominated as non-ricardian (rule-of-thumb). In practice, many agents are subject to liquidity constraint but would like to raise the present consumption by future income, but they do not have access to credit. This implies that these agents can not maximize their utility intertemporal and their consumption is restricted to current income.

The calibration approach for parameter values is not the most appropriate, because their values are always conditional on a particular model. So, it is not indicated to import values from another model. Due to this, the estimation of DSGE models using methodologies Bayesian became the estimation method most commonly used among macroeconomists. Thus, we were decided to estimate the structural model using this approach.

The results demonstrate that the introduction of the income transfer program brings positive returns for the whole economy, except for ricardian individuals because consumption and wage level of these agents remains below its steady state throughout the simulation².

Besides this introductory section, this paper is structured as follows: section two describes the DSGE model; the third section deals with the estimation of the model parameters; section four shows the results; and finally, conclusions are drawn.

²The data used in the estimations are given annual GDP growth and aggregate consumption in Brazil for the period 1999 to 2011. Data obtained from the site www.ipeadata.gov.br.

2 Model

This section shows the economic model this work. It is a simple model consisting of households and firms (endogenous agents), and the Government as an exogenous agent (represented in the payment of income transfers)³. Moreover, the model is closed and no financial market.

2.1 Households

The first agent of this model is the representative agent households (ricardian and non-ricardian). The ricardian agent maximizes his utility function (which represents his instant happiness) by choosing consumption and leisure, subject to his budget constraint. Already the non-ricardian merely consumes the transfers received from the Government.

The most common form to represent the consumption of non-ricardian agents is to possible that they may optimize his utility intratemporal using his disposable income $(C_j = W - taxes)$ [(Gali et al , 2007), (Itawa , 2009), (Coenen and Straub, 2004), (Furlanetto and Seneca , 2007), (Dallari , 2012), (Colciago et al , 2006) and (Mayer and Stahler , 2009)], there are other authors who assume that these agents receive wage with government transfers ($C_j = W + transfers$)[(Fornero , 2010), (Swarbrick , 2012), (Forni et al , 2009) and (Monastier , 2012)]. However, this work follows the form shown by Vereda and Cavalcanti (2010), in which the revenue non-ricardian agent is limited to a transfer of income from the Government. But unlike these authors, this article works with the stochastic shock occurring in public income transfer to the non-ricardian agents.

2.1.1 Ricardian Consumers

It is assumed that each ricardian agent maximizes his utility choosing intertemporal consumption, $\{C_{i,t}\}_{t=0}^{\infty}$, and leisure, $\{1 - L_{i,t}\}_{t=0}^{\infty}$. Ricardian agents' preferences are defined by the following utility function:

³The idea of letting the simple model is to keep the focus on key variables this work, C and Y. Consider other forms of rigidity (imperfect market competition, consumer habits etc) would not spend much time in the resolution, but the results would not be substantially different. So the choice was to keep the model as simple as possible.

$$U = E_t \sum_{t=0}^{\infty} \beta^t \left[\gamma \log C_{i,t} + (1-\gamma) \log(1-L_{i,t}) \right]$$

where E_t is the expectations operator, β is the intertemporal discount rate, $\gamma \in (0, 1)$ is the share of consumption in the utility of ricardian individuals.

The budget constraint says that consumption plus investment do not exceed the sum of the revenues coming from labor and capital:

$$(C_{i,t} + I_{i,t})P_t = W_t L_{i,t} + R_t K_{i,t}$$
(1)

where W_t is the wage, R_t is the rate of return on capital, $K_{i,t}$ is the stock of capital, $L_{i,t}$ is the amount of work and P_t and is the price level, which is normalized to one.

The process of capital accumulation is defined by:

$$K_{i,t+1} = (1 - \delta)K_{i,t} + I_{i,t}$$
(2)

where δ is the depreciation rate.

Using (2) in (1), we obtain the budget constraint of the agent ricardian:

$$C_{i,t} + K_{i,t+1} = W_t L_{i,t} + (R_t + 1 - \delta) K_{i,t}$$
(3)

The corresponding Lagrangian problem faced by ricardian consumers is as follows:

$$\max_{C_{i,t}, L_{i,t}, K_{i,t}} \mathscr{L} = E_t \sum_{t=0}^{\infty} \beta^t \left\{ \gamma \log C_{i,t} + (1 - \gamma) \log(1 - L_{i,t}) - \lambda_t \left[C_{i,t} + K_{i,t+1} - W_t L_{i,t} - (R_t + 1 - \delta) K_{i,t} \right] \right\}$$

Thus, we arrive at the first order conditions of the above problem:

$$\frac{\partial \mathscr{L}}{\partial C_{i,t}} = \frac{\gamma}{C_{i,t}} - \lambda_t = 0 \tag{4}$$

$$\frac{\partial \mathscr{L}}{\partial L_{i,t}} = -\frac{(1-\gamma)}{(1-L_{i,t})} + \lambda_t W_t = 0$$
(5)

$$\frac{\partial \mathscr{L}}{\partial K_{i,t}} = \beta E_t \lambda_t \left[R_t + 1 - \delta \right] - \lambda_{t-1} = 0$$
(6)

Combining equations (4) and (5), it is obtained the equation of the work supply ricardian consumers:

$$\frac{(1-\gamma)}{\gamma}\frac{C_{i,t}}{(1-L_{i,t})} = W_t \tag{7}$$

And using equations (4) and (6), we arrive at the Euler equation for consumption:

$$\frac{1}{C_{i,t-1}} = \beta E_t \frac{1}{C_{i,t}} (R_t + 1 - \delta)$$
(8)

2.1.2 Non-Ricardian Consumers

Non-ricardian consumers have a behavior simpler. The idea is that these individuals do not participate in the labor market getting their consumption limited to government transfers⁴. Under this hypothesis:

$$C_{j,t} = Tr_t \tag{9}$$

where Tr_t is the income transfer to non-ricardian consumer j.

Payment of income transfer follows a stochastic process AR (1):

⁴Proof of equation (9): If to be in the Bolsa Familia Program is necessary that the family has at most five children, and that the monthly income does not exceed R\$ 70.00 per capita - total R\$ 490.00 for the whole family (7x70 = R\$ 490.00). Being the value of the Brazilian minimum wage of 2012, R\$ 622.00. So if the maximum total monthly income of the family included in this Government's program (R\$ 490.00) does not achieve the minimum wage (R\$ 622.00), this family is not part of the formal labor force, and lives merely with Government's income transfer.

$$Tr_t = \rho T r_{t-1} + \varepsilon \tag{10}$$

where ε is the error term.

2.1.3 Aggregation

The aggregate consumption of this work follows the most common functional form ($C_t = \omega C_{i,t} + (1 - \omega)C_{j,t}$) found in the main works of this type of literature [(Bosca et al, 2010), (Gali et al, 2007), (Itawa, 2009), (Coenen and Straub, 2004), (Furlanetto and Seneca, 2007), (Dallari, 2012), (Mayer et al, 2010), (Stahler and Thomas, 2011), (Swarbrick, 2012), (Motta and Tirelli, 2010), (Diaz, 2012), (Colciago, 2011), (Mayer and Stahler, 2009) and (Forni et al, 2009)].

Thus, the aggregate consumption is performed as follows:

$$C_t = \omega C_{i,t} + (1 - \omega) C_{j,t} \tag{11}$$

where ω the population share of ricardian consumers.

2.2 Firms

The firms' problem is to choose optimal values for the use of production factors, capital and labor. It is assumed that both markets for goods and services as factor markets are perfectly competitive. Firms acquire capital and work of households in order to maximize its profit, taking as prices given. The production function is given by:

$$Y_t = A_t K_t^{\alpha} L_t^{1-\alpha} \tag{12}$$

where A_t is the total factor productivity, α is the capital participation in the product, K_t is the capital stock, L_t the amount of hours worked and Y_t is product.

The productivity⁵ follows a stochastic process AR (1) described below:

$$A_t = \rho A_{t-1} + \varepsilon_A \tag{13}$$

where ε_A is the error term.

The problem of the firm is to maximize its profit function:

$$\pi = A_t K_t^{\alpha} L_t^{1-\alpha} - W_t L_t - R_t K_t \tag{14}$$

The maximization problem above obtains the following first order conditions:

$$\frac{\partial \pi}{\partial K_t} = \alpha A_t K_t^{\alpha - 1} L_t^{1 - \alpha} - R_t = 0$$
(15)

$$\frac{\partial \pi}{\partial L_t} = (1 - \alpha) A_t K_t^{\alpha} L_t^{-\alpha} - W_t = 0$$
(16)

From equations (15) and (16) results in the equations of the prices of factors of production:

$$W_t = (1 - \alpha) \frac{Y_t}{L_t} \tag{17}$$

$$R_t = \alpha \frac{Y_t}{K_t} \tag{18}$$

2.3 Aggregate Demand

The model also requires an aggregate demand equation:

$$Y_t = C_t + I_t \tag{19}$$

⁵The result related shock to productivity will not be presented in this paper. Just to keep the focus on income transfers.

2.4 Equilibrium

Once described the behavior of each agent of the model. This section presents the interaction of all agents to determine the macroeconomic equilibrium. Therefore, the competitive equilibrium of model is achieved via a set of eleven equations: (2), (7), (8), (9), (10), (11), (12), (13), (17), (18) and (19), which one seeks to represent the behavior of eleven endogenous variables (Y_t , C_i , C_j , C, W, L, R, I, K, A and Tr) and two exogenous variables (ε , ε_A).

3 Estimation

This article employs a Bayesian methodology to estimate the structural model presented in the previous section. This methodology has been used extensively in the estimation of complex stochastic models involving a large number of parameters⁶. In such cases, it is typical to use Bayesian estimation through Monte Carlo Markov Chain (MCMC) method, rather than the simple maximum likelihood, this is because in most cases it is not possible to specify the joint distribution of shape parameters explicit. This study uses the Metropolis-Hastings algorithm for MCMC method, whose basic procedure can be described as:

- 1. Start with the value $\theta^{(0)}$ and index of stage j = 0;
- 2. Generating a transition point β of the core;
- 3. Refresh $\theta^{(j)}$ by $\beta = \theta^{(j+1)}$ with a probability given by $p = min\left(1 \left| \frac{p(\beta)q(\theta^{j},\beta)}{p(\theta^{(j)})q(\beta,\theta^{(j)})} \right. \right)$
- 4. Keeping $\theta^{(j)}$ with probability 1-p;
- 5. Repeat the above procedure until to get a stationary distribution.

⁶(Schorfheide , 2000); (Lubik and Schorfheide, 2003); (Smets and Wouters , 2003); (Ireland , 2004); (Fernandez-Villaverde and Rubio-Ramirez , 2004); (Lubik and Schorfheide , 2005); and (Rabanal and Rubio-Ramirez , 2005).

3.1 Prior Distribution

The prior distribution reflects the beliefs of the values of the parameters. A large standard deviation for this value means that there is little confidence in the a prior value used. Taking the worry of making a proper estimation: the distributions of the parameters; the mean values; and standard deviations, following values used in the literature.

Table 1 presents the a prior distribution of the parameters selected for the model of this work ($\Theta = (\beta, \gamma, \delta, \alpha, \rho, \rho_A, \text{ and } \omega)$).

Parameters	Distribution	Mean	Standard Deviation			
β	beta	0,99	0,002			
γ	gama	0.7	0.002			
δ	beta	0.05	0.003			
α	beta	0.35	0.003			
ρ	beta	0.95	0.05			
$ ho_A$	beta	0.96	0.05			
ω	beta	0.8	0.05			

Table 1: Prior distribution. Source: Prepared by the authors.

3.2 Posterior Distribution

Table 2 presents the posterior distributions of the model and Figure 1⁷ compares the prior and posterior distributions.

The estimation results of this study followed the values obtained by the main DSGE literature. The value of the discount rate (β) estimated in this study was 0.9893. Rotemberg and Woodford (1997), Smets and Wouters (2003) and Juillard et al (2006) fix 0.99, while Christiano et al (2005) work 0.9926, among the articles related to Brazil: Kanczuk (2002) and Araujo et al (2006) use 0.99; while Ellery Jr et al (2010) choose 0.89; already Kanczuk (2004) chooses 0.98; Silveira (2008) works com 0.91; finally, Duarte and Carneiro (2001) fix 0.93.

⁷In Figure 1, the gray and black lines represent the prior and posterior distributions, respectively. While the dashed line shows the estimated parameter value.

We found the depreciation rate (δ) 0.0507, while the international literature: Smets and Wouters (2003), Christiano et al (2005) and Juillard et al (2006) work with a depreciation rate of 0.025. While in Brazilian literature: Kanczuk (2002) uses 0.048; and Ellery Jr et al (2010) adopt 0.17.

The value found for the participation of private capital in the product (α) was 0.3314. While Kanczuk (2002) calibrates in 0.39, Ellery Jr et al (2010) think that this value is equal to 0.49 and Kanczuk (2004) uses 0.4, the same value that Duarte and Carneiro (2001).

The main parameter of this study is the population share of non-ricardian individuals $((1 - \omega))$. Who obtained value was 0.4071. Among the works related to Brazil: Reis, Issler, Blanco and de Carvalho (1998) found 0.8, already Cavalcanti and Vereda (2011) worked with a range of values between 0.67 and 0.8, while Vereda and Cavalcanti (2010) and Monastier (2012) used the value 0.6. In foreign literature: Bosca et al (2010) used 0.5 for the Spanish economy; Campbell and Mankiw (1989) estimated this parameter for the G7 using OLS getting 0.616, 0.53, 0.646, 0.4, 0.553, 0.221 and 0.478 for Canada, France, Germany, Italy, Japan, England and United States, respectively; Gali et al (2007) worked with 0.5; Itawa (2009) found 0.25 for the Japanese economy; Mayer et al (2010) used 0.25 for the U.S. economy; and Stahler and Thomas (2011) obtained 0.44 for the Spanish economy.

Parameter	Mean	Confidence Interval				
β	0.9893	0.9864 0.9925				
γ	0.6996	0.6962 0.7030				
δ	0.0507	0.0467 0.0551				
α	0.3314	0.3011 0.3524				
ρ	0.9940	0.9823 1.0000				
$ ho_A$	0.9763	0.9394 0.9994				
ω	0.5929	0.5476 0.6494				

Table 2: Posterior distribution

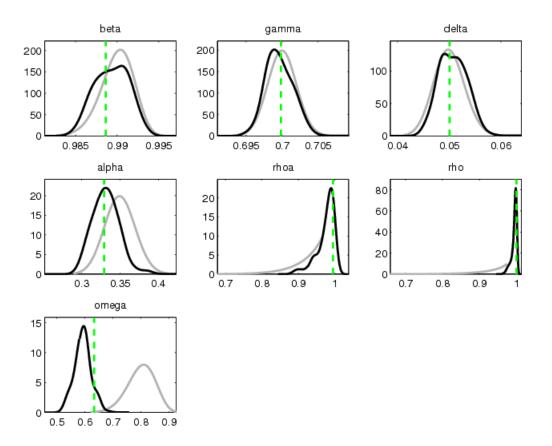


Figure 1: Prior and posterior distributions.

4 **Results**

In this section, we examine the dynamic properties of the models using impulseresponse functions. As far as the estimation of the simulation model were shot on the platform Dynare⁸⁹.

4.1 Impulse-Response Functions

Figure 2 and Table 3 present the results for the shock in the payment of income transfer to non-ricardian. Note that a positive effect on output (*Y*), non-ricardian household's consumption (*C_j*), aggregate consumption (*C*), labor supply (*L*), the return on capital (*R*), investment (*I*) and the stock of capital (*K*). And a negative result in the ricardian individuals' consumption (*C_i*), the level of wages (*W*) and productivity (*A*). Using Table 3, we can see two effects in opposite directions. The first relates to the negative effect of shock *Tr* in the ricardian agents' consumption, $(Corr(Tr,C_i) = -0.2598)$, and on the other hand, a positive effect on labor supply shock (Corr(Tr,L) = 0.1853). These two effects will reverberate in the product, and the negative result of the fall of the ricardian individuals' consumption in the output ($Corr(C_i, Y) = 0.9071$) is mitigated by the positive effect of labor supply in the output (Corr(L, Y) = 0.7764).

Other variables also exhibit high correlation with the product: 0.9643; 0.9874; 0.6789; 0.9641; 0.8665; and 0.9629. In relation to aggregate consumption, wage, return of capital, investment, capital stock and productivity, respectively. While the exogenous shock (*Tr*) has a low correlation with the product (0.0804).

Briefly, the shock in income transfer has a negative effect in the ricardian agents' consumption, these, to try to maintain the level of consumption, increase

⁸Dynare is a software platform for the treatment of a broad class of macro models, in particular models of dynamic stochastic general equilibrium (DSGE) and overlapping generations (OLG). The models solved by Dynare include the hypothesis of rational expectations, but the Dynare is also able to handle models where expectations are formed differently: on one extreme, models where agents perfectly anticipate the future, at the other extreme, models where the agents have limited rationality or imperfect knowledge and thus form their expectations through a learning process. In terms of types of agents, it is possible to incorporate in Dynare: consumers; firms, government, monetary authorities, investors and financial intermediaries. Some degree of heterogeneity can be accomplished by including several distinct classes of agents in each of the above categories of agents(Adjemian et al , 1996).

⁹The resolution models DSGE can be achieved using methods of disruption, which use a local approximation based on the Taylor expansion. After linearizing the model is solved using methods such as Blanchard and Kahn (1980). The Dynare follows this approach in solving stochastic DSGE models.

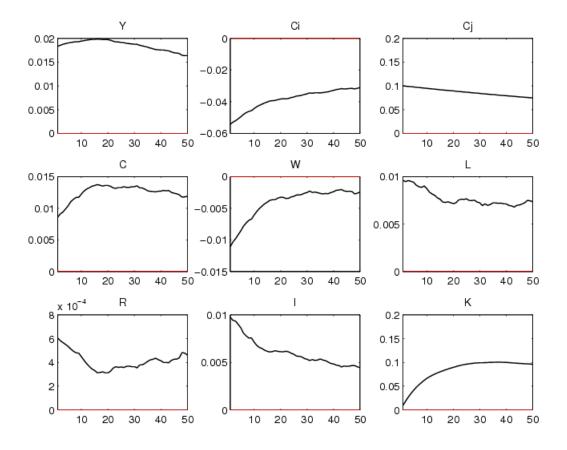


Figure 2: Impulse-response functions for the shock in the payment of income transfers. Source: Prepared by the authors.

their labor supply, even with a fall in the wage level (Income effect). The overall effect of shock is positive, it is being able to keep the product above its steady state throughout the study period (fifty periods). Also, notice that the behavior of all variables is to stay away from the steady state, they are not showing a trend of return within the simulated period.¹⁰.

¹⁰Here is not being said that the variables will not return to steady states, but that these return will not occur within the study period.

Variable	Y	C_i	C_j	С	W	L	R	Ι	K	Α	Tr
Y	1	0.9071	0.0804	0.9643	0.9874	0.7764	0.6789	0.9641	0.8665	0.9629	0.0804
C_i	0.9071	1	-0.2598	0.9416	0.9622	0.6963	0.6673	0.8075	0.8773	0.9298	-0.2598
C_{j}	0.0804	-0.2598	1	0.0806	-0.0456	0.1853	0.0174	0.0744	0.0296	-0.0377	1
Ċ	0.9643	0.9416	0.0806	1	0.9773	0.7833	0.6948	0.8594	0.9159	0.9466	0.0806
W	0.9874	0.9622	-0.0456	0.9773	1	0.7636	0.6897	0.9268	0.8899	0.972	-0.0456
L	0.7764	0.6963	0.1853	0.7833	0.7636	1	0.9696	0.7137	0.9347	0.8024	0.1853
R	0.6789	0.6673	0.0174	0.6948	0.6897	0.9696	1	0.6143	0.9143	0.7299	0.0174
Ι	0.9641	0.8075	0.0744	0.8594	0.9268	0.7137	0.6143	1	0.7549	0.9103	0.0744
Κ	0.8665	0.8773	0.0296	0.9159	0.8899	0.9347	0.9143	0.7549	1	0.8806	0.0296
A	0.9629	0.9298	-0.0377	0.9466	0.972	0.8024	0.7299	0.9103	0.8806	1	-0.0377
Tr	0.0804	-0.2598	1	0.0806	-0.0456	0.1853	0.0174	0.0744	0.0296	-0.0377	1

Table 3: Correlation of Simulated Variables. Source: Prepared by the authors.

15

Conclusions

This work aimed to study the main Brazilian economic growth through a income transfer program. For this, we used the DSGE approach. The estimation of the parameters was performed using the Bayesian methodology and analysis of results was done by impulse-response functions.

The results of the estimates followed, satisfactorily, the values found in the literature. The parameter that relates the population share of non-ricardian individuals was slightly below the value found in the work related to Brazil. However, one can attribute this difference to the functional form of the consumption of these agents. In this work, we assume a form more restricted, since it believes that the non-ricardian agent only has transfers as revenue. Still, in section 3, one can no-tice the large variation of this parameter in the international literature DSGE.

The impulse-response functions showed positive responses to the variables: Y, C_j, C, L, R, I , and K, and negative responses to the variables: C_i, W , and A. The main result is that the ricardian agents' consumption responds negatively to the shock, and these agents seek to compensate for this loss of utility increasing his labor supply. So even with this negative effect, the response of the economy to the shock is positive. Demonstrating that the introduction of the income transfer program brings positive returns for the whole economy, except for ricardian individuals because consumption and wage level of these agents remains below its steady state throughout the simulation.

References

- Adjemian, S., Bastani, H., Karamme, F., Juillard, M., Maih, J., Mihoubi, F., Perendia, G., Pfeifer, J., Ratto, M., and Villemot, S. (1996): *Dynare: Reference Manual*, Version 4.
- Araujo, M., Bugarin, M., Muinhos, M., and Silva, J. R. (2006): *The effect of adverse supply shocks on monetary policy and output*. Banco Central do Brasil, Texto para Discussao, 103.
- Blanchard, O. J., and Kahn, C. M. (1980): The solution of linear difference models under rational expectation. Econometrica, 48, 1305 - 1312.

- Bosca, J., Diaz, A., Domenech, R., Ferri, J., Perez, E., and Puch, L. (2010): A Rational Expectations Model for Simulation and Policy Evaluation of the Spanish Economy. SERIEs, 1(1).
- Brock, W., and Mirman, L. (1972): *Optimal economic growth and uncertainty: The discounted case*. Journal of Economic Theory, 4, 479 513.
- Campbell, J., and Mankiw N. G. (1989): *Consumption, income, and interest rates: Reinterpreting the time series evidence*. NBER Macroeconomics Annual, MIT Press, pages 185 - 246.
- Canova, F. (2007): *Methods for Applied Macroeconomic Research*. New Jersey: Princeton University Press.
- Cass, D. (1965): *Optimum growth in an aggregative model of capital accumulation.* Review of Economic Studies, 32, 233 - 240.
- Castro, J. A., and Modesto, L. (2010): *Bolsa Familia 2003-2010: Avancos e Desafios*. IPEA: Brasilia.
- Cavalcanti, M. A. F. H., and Vereda, L. (2011): Propriedades dinamicas de um modelo DSGE com parametrizacoes alternativas para o Brasil. Ipea, Texto para Discussao, n 1588.
- Christiano, L., Eichembaum, M., and Evans, C. (2005): *Nominal rigidities and the dynamic effects to a shock of monetary policy*. Journal of Political Economy, 113, 1 45.
- Coenen, G., and Straub, R.. (2004): Non-ricardian households and fiscal policy in an estimated DSGE modelo to the Euro Area. Mimeo.
- Colciago, A..(2011): Rule of thumb consumers meet sticky wages. Journal of Money, Credit and Banking, 43, 325 353.
- Colciago, A., Muscatelli, V. A., Ropele, T., and Tirelli, P. (2006): *The role of fiscal policy in a monetary union: Are national automatic stabilizers efective?* ECONSTOR, Working Paper, 1682.
- Dallari, P. (2012): *Testing rule-of-thumb using irfs matching*. Departamento de EconomÃa Aplicada Universidade de Vigo.
- Deaton, A. (1992): Undestanding Consumption. Clarenton Press: Oxford.

- Diaz, S. O.. (2012): A model of rule-of-thumb consumers with nominal price and wage rigidities. Bando de La Republica Colombia, Borradores de Economia, 707.
- Duarte, P., and Carneiro, D.. (2001): Inercia de juros e regras de taylor: Explorando as funcoes de resposta a impulso em um modelo de equilibrio geral com parametros estilizados para o Brasil. Td 450, Departamento de Economia-Puc-Rio.
- Ellery Junior, R., Gomes, V., and Sachsida, A. (2010): *Business cycle fluctuations in Brazil*. Revista Brasileira de Economia, 56, 269 308.
- Fernandez-Villaverde, J., and Rubio-Ramirez, J. F. (2004): *Comparing dynamic equilibrium models to data: a bayesian approach*. Journal Econometrics, 123(1), 153-187.
- Fornero, J.. (2010): *Ricardian equivalence proporsition in a NK DSGE model for two large economies: The EU and the US*. Central Bank of Chile, Working Paper, 563.
- Forni, L., Monteforte, L., and Sessa, L.. (2009): *The general equilibrium effects of fiscal policy: Estimates for the euro area.* Journal of Public Economics, 93, 559 585.
- Furlanetto, F., and Seneca, M. (2007) *Rule-of-thumb consumers, productivity and hours*. Norges Bank, Working Paper, 5.
- Gali, J., Lopez-Salido, J. D., and Valles, J. (2007) Understanding the effects of government spending on consumption. Journal of the European Economic Association, 5(1), 227 270.
- Ireland, P. N. (2004): *A method for taking models to the data*. Journal of Economic Dynamics and Control , 28(6), 1205-1226.
- Itawa, Y. (2009): Fiscal policy in an estimated DSGE model of the Japanese economy: Do non-ricardian households explain all? ESRI Discussion Paper Series, 216.
- Kanczuk, F. (2002): *Juros reais e ciclos reais brasileiros*. Revista Brasileira de Economia, 56, 249 267.

- Kanczuk, F. (2004): *Choques de oferta em modelos de metas inflacionarias*. Revista Brasileira de Economia, 58, 559 581.
- Koopmans, T. (1965): On the concept of optimal economic growth. The Econometric Approach to Development Planning, Amsterdam.
- Kydland, F., and Prescott, E.. (1982): *Time to build and aggregate fluctuations*. Econometrica, 50, 1350 1372.
- Johnson, D., Parker, J., and Souleles, J. (2006): *Household expenditure and the income tax rebates of 2001*. American Economic Review, 90(2), 1589 1610.
- Juillard, M., Karam, P., Laxton, D., and Pesenti, P. (2006): Welfare-based monetary policy rules in an estimated DSGE model of the us economy. ECB, Working Paper, 613.
- Lubik, T., and Schorfheide, F. (2003): *Do central banks respond to exchange rate movements? a structural investigation.* The Johns Hopkins University, Department of Economics, Economics Work ing Paper Archive, 505, 0-1.
- Lubik, T., and Schorfheide, F. (2005): A bayesian look at new open economy macroeconomics. The Johns Hopkins University, Department of Economics, Economics Work ing Paper Archive, 521, 0-1.
- Mayer, E., and Stahler, N. (2009): *Simple fiscal policy rules: Two cheers for a debt brake!* XVI Encuentro de Economia Publica.
- Mayer, E., Moyen, S., and Stahler, N.. (2010): *Fiscal expenditures and unemployment: A DSGE perspective.* ECONSTOR, Working Paper, E6 - V3.
- Monastier, R. A.. (2012): *O impacto de variaveis fiscais sobre o bem-estar na economia brasileira sob uma abordagem DSGE*. Dissertação, UFPR.
- Motta, G., and Tirelli, P. (2010): *Rule-of-thumb consumers, consumption habits and the taylor principle.* University of Milan Bicocca, Working Paper Series, 194.
- Rabanal, P., and Rubio-Ramirez, J. F. (2005): Comparing new keynesian models of the business cycle: A bayesian approach. Journal of Monetary Economics, 52(6), 1151-1166.

- Ramsey, F. (1927): A contribution to the theory of taxation. Economic Journal, 37(145), 47 61.
- Ramsey, F. (1928): *A mathematical theory of saving*. Economic Journal, 38(152), 543 559.
- Reis, E., Issler, J. V., Blanco, F., and de Carvalho, L. M. (1998): Renda permanente e poupanca precaucional: Evidencias empiricas para o Brasil no passado recente. Pesq. Plan. Econ., 28, 233 - 272.
- Rotemberg, J., and Woodford, M. (1997): An optimization-based econometric framework for the evaluation of monetary policy. NBER Macroeconomics Annual, 12, 297 - 346.
- Schorfheide, F. (2000): *Loss function-based evaluation of dsge models*. Journal of Applied Econometrics, 15(6), 645-670.
- Siveira, M. A.. (2008): Using a bayesian approach to estimate and compare new keynesian DSGE models for the Brazilian economy: the role for endogenous persistence. Revista Brasielira de Economia, 62, 333 357.
- Smets, F., and Wouters, R.. (2003) An estimated dynamic stochastic general equilibrium model of the euro area. Journal of the European Economic Association, 1(5):1123 - 1175.
- Stahler, N., and Thomas, C. (2011): *Fimod a DSGE model for fiscal policy simulations*. Banco de Espana, Documentos de Trabajo, 1110.
- Swarbrick, J. (2012): *Optimal fiscal policy in a dsge model with heterogeneous agents*. Master thesis, School of Economics, University of Surrey.
- Vereda, L., and Cavalcanti, M. A. F. H.. (2010): *Modelo dinamico estocastico de equilibrio geral (DSGE) para a economia brasileira*. Ipea, Texto para Discussao, 1479.
- Wolff, M. (2003): *Recent trends in the size distribution of household wealth.* Journal of Economic Perspective, 12:131 - 150.