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Financial Time Series Forecasting by Developing a Hybrid Intelligent System

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Abstract

The design of models for time series forecasting has found a solid foundation on statistics and mathematics. On this basis, in recent years, using intelligence-based techniques for forecasting has proved to be extremely successful and also is an appropriate choice as approximators to model and forecast time series, but designing a neural network model which provides a desirable forecasting is the main concern of researchers. For this purpose, the present study tries to examine the capabilities of two sets of models, i.e., those based on artificial intelligence and regressive models. In addition, fractal markets hypothesis investigates in daily data of the Tehran Stock Exchange (TSE) index. Finally, in order to introduce a complete design of a neural network for modeling and forecasting of stock return series, the long memory feature and dynamic neural network model were combined. Our results showed that fractal markets hypothesis was confirmed in TSE; therefore, it can be concluded that the fractal structure exists in the return of the TSE series. The results further indicate that although dynamic artificial neural network model have a stronger performance compared to ARFIMA model, taking into consideration the inherent features of a market and combining it with neural network models can yield much better results.

JEL Classification: C14, C22, C45, C53.

Keywords: Stock Return, Long Memory, NNAR, ARFIMA, Hybrid Models.

1. Introduction

The growing of the financial markets during the recent decades, had led these markets to acquire a lot of significance in the economy of different countries such that growth and prosperity of the stock exchange, as an example of these markets, is a criterion for confirming health and dynamicity of an economy. The reason for the importance of these markets in economy is their important role in attracting widespread capitals and optimal allocation of internal and external financial resources for

economic development and also increasing investors' profit (Abdullahi, 2013; Hondroyiannis and et al., 2005; Khan and Senhadji, 2003). On the other hand, along with the development of markets, an increase in the number of investors and complications involved in the analysis of the effect of different variables on the stock index due to the close relationship of the markets with macroeconomic variables during the last two decades, forecasting the pricing behavior of the financial properties in the dynamic field of economy and capital market has turned into one of the most important issues discussed in financial sciences leading to a growing increase in the significance and value of forecasting-related issues. The reason is that it guides policy-makers, planners, researchers and investors in exact and efficient evaluation, pricing the properties, and proper allocation of resources (Stekler, 2007). However, the unknown nature of the variables influencing the changes in the financial markets has led to politicians and investors' growing interest in forecasting the behavioral processes in the markets using univariate regressive models and advanced mathematical models since these models are capable of identifying and modeling the complicated behavior of financial markets and have produced encouraging results in providing accurate and reliable forecasts (Kao and et al., 2013; Chen and et al., 2010).

Predictability of the stock return has a close relationship with the Efficient Markets Hypothesis (EMH). Efficiency is a fundamental concept in financial markets proposed in 1965 in the field of finance and many studies have been conducted in this regard. According to this issue. After presenting these empirical evidences, EMH stated in its more full-fledged form that if return was predictable, many of the investors would gain huge benefits. Accordingly, we would be faced with a "money making machine" that could build unlimited wealth; this is, however, impossible in a stable economy (Granger & Timmermann, 2004).

EMH built based on Random Walk Models has been one of the basic challenges facing financial analysts since according to this hypothesis, the complex behavior of the financial markets cannot be modeled and predicted. By finding the roots of this issue, it can be found that the basic assumptions of the EMH cannot take into account all the elements involved in the financial markets. The most important assumption is that markets do not have memory in the sense that yesterday's happenings will not influence today's events and that investors are risk averse and always carefully consider all the information in the market (Burton, 1987). However, the results of many applied studies are indicative of the fact that majority of the investors are under the influence of the happenings in the market and form their expectations of the future stock prices in keeping with their experiences. This fact points to the conclusion that markets have memory (Granger and Joyeux, 1980). In addition, one cannot make a confident assertion that all the investors in the financial markets behave logically but that they may do trading and favor risking without paying attention to the market information because always some investors may make a profit and some may sustain losses. Therefore, although based on the assumptions of EMH, financial markets are apparently unpredictable, the fact is that this is not the case (Sowell, 1992). Thus, the assumptions of the EMH were faced with such criticisms and "Fractal Market Hypothesis" (FMH) was proposed which was able to provide a more comprehensive analysis of the markets. This hypothesis, in fact, implied the existence of a market composed of numerous investors pursuing their goals with different investment horizons. The types of information important to each one of these investors is different. On this basis, as long as the market sustains its fractal structure, it will stay stable without considering time scale of the investment horizons. On the other hand, when all the investors in the market have the same time horizon, the stability of the market will be undermined because people will do trading drawing on similar market information (Baillie, 1996). Although rejecting the EMH implies non-randomness and, as a consequence, predictability of different series, this result is achieved because EMH has been formed based on the Random Walk Model and consequently the existence of a linear structure in the behavior of the market (Lebaron, 1994). On the other hand, with regard to the financial markets which mainly have a complex and chaotic structure, FMH analyzes and assesses the issue of predictability from the perspective of nonlinear models (Vacha

and Vosvrda, 2005). Although accepting the dependence of the behavior of a financial market on the FMH is a confirmation of the use of different non-linear models in consonance with the feature of long memory (e.g., Auto Regressive fractionally Integrated Moving Average or ARFIMA model) and also different types of neural network models (e.g., Nonlinear Neural network Auto Regressive or NNAR model as a dynamic model), it should also be noted that the fact that the inherent features of the mentioned markets (e.g., long memory) can improve the results of modeling should not be overlooked. Therefore, the present study attempts not only to consider fractal markets hypothesis in the return of TSE index and use different models based on the long memory (ARFIMA) and Dynamic Artificial Neural Network Model (NNAR), but also to introduce a novel hybrid intelligent framework developed by applying a combination of the two models and to compare them in terms of their out-of-sample forecasting performance using MSE and RMSE forecasting error measures. For this purpose, daily time series data were used from 25/3/2009 to 22/10/2011 (616 observations) out of which 555 observations (about 90% of the observations) were used for modeling and 60 observations for out-of-sample forecasting.

2. Methodology

2.1. Long Memory

After many important studies were conducted on the existence of Unite Root and Cointegration in time series starting in 1980, econometrics experts examined other types and subtypes of non-stationary and approximate persistence which explain the processes existing in many of the financial and economic time series. Today, different studies have been and are being conducted on these processes including "Fractional Brownian Motion" and "Fractional Integrated Process" and the "processes with long memory" (Lento, 2009). Hurst (1951) for the first time found out about the existence of processes with long memory in the field of hydrology. After that, in early 1980s econometricians such as Granger and Joyex (1980) and Hosking (1981) developed econometric models dealing with long memory and specified the statistical properties of these models. During the last three decades, numerous theoretical and empirical studies have been done in this area. For example, (Mandelbrot, 1999; Lee and et al. 2006; Onali and Goddard 2009)'s studies can be mentioned as among the most influential in this regard.

The concept of long memory includes a strong dependency between outlier observations in time series which, in fact, means that if a shock hits the market, the effect of this shock remains in the memory of the market and influences market activists' decisions; however, its effect will disappear after several periods of time (in the long term). Thus, considering the nature and the structure of financial markets such as the stock market, which are easily and quickly influenced by different shocks (economic, financial and political), it is possible to analyze the effects of these shocks and in a way determine the time of their disappearance by observing the behavior of these markets (Los and Yalamova, 2004). Meanwhile, the long memory will be used as a means of showing the memory of the market. By examining the long memory, the ground will also be prepared for improvement of financial data modeling.

2.2. ARFIMA Model

One of the most popular and most flexible models dealing with the long memory is the ARFIMA model in which fractional cointegration degree (d) is representative of the long memory parameter because it is indicative of the features of the long memory in the time series of the related variable. After making sure about the existence of this feature in a time series using ACF¹ tests, classic R/S² analysis and also semi-parametric methods such as GPH³, MRS⁴, etc. (Xiu and Jin, 2007), the most

¹ Auto Correlation Function

² Rescaled Range Analysis

³ Geweke and Porter-Hudak

⁴ Modified Rescaled Range

important stage in the process of estimation of these models is the "fractional differencing" stage; economists, however, used first-time differencing in their empirical analyses due to its ease of use (in order to avoid the problems of spurious regression in non-stationary data and the difficulty of fractional differencing). Undoubtedly, this replacement (of first-time differencing with fractional differencing) leads to over- or under-differencing and consequently loss of some of the information in the time series (Huang, 2010). On the other hand, considering the fact that majority of the financial and economic time series are non-stationary and of the Differencing Stationary Process (DSP¹) kind, in order to eliminate the problems related to over differencing and to obtain stationary data and get rid of the problems related to spurious regression, we can use Fractional Integration. Another interesting point is that Fractional Integration can assume different values, but a specific value for this parameter (d) is indicative the long memory feature. Two conditions need to be met for assuming these values. Firstly, if $-0.5 < d < 0.5$, a series exhibits a stationary and invertible ARMA process with geometrically bounded autocorrelations. In other words, when $0 < d < 0.5$, the autocorrelation function decreases hyperbolically and the related process is a stationary long memory process meaning that the autocorrelations decay to zero and will not be summable. When $-0.5 < d < 0$, the long memory process will be invoked. The medium-term memory shows that the related variable has been over-differenced and under such conditions, the reverse autocorrelation function decreases hyperbolically. The second condition is that a non-stationary is exhibited by the series if $0.5 \leq d < 1$ (Hosking, 1981).

Finally, it is worth mentioning that spurious long memory should not be overlooked; in fact, spurious long memory happens as the result of structural change and inattention to nonlinear transformations (Kuswanto and Sibbertsen, 2008). Therefore, based on the concepts introduced, we can correctly model the behavior of a variable using this model. The general form of the model $ARFIMA(p,d,q)$ is as follows:

$$\phi(L)(1-L)^d(y_t - \mu_t) = \theta(L)\varepsilon_t \quad t=1,2,3,\dots,T \quad (1)$$

In which $\phi(L)$ is polynomial autocorrelation, $\theta(L)$ represents moving average polynomial, L is Lag Operator, μ_t is the mean of y_t . Besides, in this equation, $Z_t = y_t - \mu_t$ and is cointegrated with rank d . Features of Z are dependent on the d value. If $d < 0.5$, covariance of the model will be fixed and if $d > 0$, it will have long memory feature (Hosking, 1981). p and q are integers and d is a long memory parameter. $(1-L)^d$ represents a fractional differencing operator which is calculated using the following formula:

$$(1-L)^d = \sum_{j=0}^{\infty} \delta_j L^j = \sum_{j=0}^{\infty} \binom{d}{j} (-L)^j \quad (2)$$

In the above equation, it has been hypothesized that $\varepsilon_t \sim N(0, \sigma_{\varepsilon_t}^2)$ and also ARMA section of the model are reversible (Aye and et al., 2012).

2.3. Nonlinear Neural Network Auto Regressive Model (NNAR)

Forecasting the behavior of a time series using econometric nonlinear models is constrained by many limitations. New models, however, enjoy more flexible structures and can get a better fitting of linear and non-linear econometric models. These models are a parallel distribution process with a natural structure and their most important feature is their ability to model nonlinear and complicated relationships without a need for prior hypothesis about the nature of relationships among the data. Generally, neural networks include two groups of dynamic and static networks (Dase and Pawar, 2010). Static networks such as the artificial neural network (ANN) do not have feedback factor; their output is calculated directly via inputs that have feedforward connections. But in dynamic neural networks (such as the Nonlinear Neural Network Auto Regressive (NNAR) and Nonlinear Neural

¹ And some are also trend stationary processes

Network Auto Regressive with exogenous variables (NNARX)), the value of the output is dependent on current and past input values, the outputs, and also the structure of the network (Georgescu and Dinucă, 2011; Khashei and Bijari, 2010).

These models have numerous applications in different areas such as prediction of financial markets, communication systems, power systems, classification, error detection, recognizing voices, and even in genetics. One of the most frequently used models among dynamic neural network models is the NNAR model. This model is developed by adding an AR process to a neural network model. Dynamic neural network (NNAR) has a linear and a nonlinear section; its nonlinear section is estimated by a Feed Forward artificial neural network with hidden layers and its linear section includes an autoregressive model (AR). The main advantage of using this model is that it is able to make more accurate long term predictions under similar conditions in comparison with the ANN model (Taskaya and Casey 2005). The training approach in these models, which is consistent with Levenberg-Marquardt (LM) Training (Levenberg, 1944 and Marquardt, 1963) and the hyperbolic tangent activation function, is built on Error-Correction Learning Rule and starts the training process using random initial weights (Matkovskyy, 2012). After determining the output of the model for any of the models presented in the training set, the error resulting from the difference between the model output and the expected values is calculated and after moving back into the network in the reverse direction (from output to input), the error is corrected. The general form of the NNAR neural network models is:

$$\hat{Y}(t) = f[u(t), u(t-1), u(t-2), \dots, u(t-n_u), y(t-1), y(t-2), \dots, y(t-n_y)] \quad (3)$$

In this formula, f represents a mapping performed by the neural network. The input for the network includes two $u(t)$ exogenous variables (input signals) and target values (the lags of the output signals). The numbers for n_u and n_y include output signals and actual target values respectively which are determined by the neural network (Trapletti, and et al., 1998).

3. Empirical Results

In this present study, we are going to compare the performance of ARFIMA and NNAR and also their combination in the framework of the NNAR model (NNARX), in terms of their forecasting of the returns of TSE index. It should be mentioned that the abbreviation for the variables used in this study include *TEDPIX*, which is indicative of price index and dividend, *DLTED*, which shows Logarithmic differential of TEDPIX series.

3.1.Examining predictability of return of TSE

In this section, in order to explain the reasons for using non-linear models, two tests will be analyzed; first the non-randomness (and consequently predictability) of stock return series will be considered using the Variance Ratio Test and then its non-linearity will be examined using the BDS test.

3.1.1. Variance Ration test (VR Test)

This test (Lo and MacKinlay's,1988) is used to examine whether the behavior of the components of stock return series is Martingale. In this test, when the null hypothesis is rejected, it can be concluded that the tested series will not be *i.i.d.* Overall, rejection of the null hypothesis in the VR test is indicative of the existence of linear or nonlinear effects among the residuals or the time series variable under investigation (Bley, 2011).

Test	Probability	Value
Variance ratio test	0.000	6.38

Source: Findings of Study

The results of the above test show that there is no evidence that the mentioned series (and the lag series) is of the Martingale; thus, the process of the data is not random. Accordingly, predictability of this series is implied in this way. The interesting point is that one cannot find out whether the data process in the stock return series is linear or non-linear as suggested by the results of this test, but can conclude that it is non-Martingale and predictable.

3.1.2. BDS test

This test which was introduced in 1987 by Brock, Dechert and Scheinkman (BDS) acts based on the correlation integral which tests the randomness of the process of a time series against the existence of a general correlation in it. For this purpose, the BDS method first estimates the related time series using different methods. Then it uses correlation integral to test the null hypothesis on the existence of linear relationships between the series. Indeed, rejection of the null hypothesis indicates the existence of non-linear relationships between the related time series.

The statistics of this test (correlation integral) measures the probability that the distance between the two points from different directions in the fuzzy space is less than ε and like the fractal dimension in the fuzzy space when there is an increase in ε , this probability also changes in accordance with it (Olmedo, 2011). Accordingly, the general form of the test is

$$BDS_{m,T}(\varepsilon) = \frac{T^{\frac{1}{2}}[C_{m,T}(\varepsilon) - C_{1,T}(\varepsilon)^m]}{\sigma_{m,T}(\varepsilon)}$$

In this equation, $\sigma_{m,T}(\varepsilon)$ is an estimation of the distribution of

the asymptotic standard $C_{m,T}(\varepsilon) - C_{1,T}(\varepsilon)^m$. If a process is i.i.d, the BDS statistics will be normal distribution of the asymptotic standard. In this equation, if the BDS statistics is large enough, the null hypothesis will be rejected and the opposite hypothesis on the existence of a non-linear relationship in the process under investigation will be accepted (Moloney and Raghavendra, 2011). This test can be usefully applied for assessing the existence of a non-linear relationship in the observed time series. The results of this test have been provided in Table 2.

Table 2: The results of BDS test in the stock return series

Dimension	BDS-Statistic	standard division	Z-Statistic	Probability
2	0.03678	0.003112	11.788	0.000
3	0.05957	0.004954	12.025	0.000
4	0.07071	0.005893	11.999	0.000
5	0.07201	0.006136	11.738	0.000

Source: Findings of Study

As it can be seen in Table 2, the null hypothesis, that means non-randomness of the stock return series, is rejected. So, this indicates the existence of a nonlinear process in the stock return series (there can also be a chaotic process as well). It is worth mentioning that whenever randomness of a series is rejected in more than two dimensions in the results of BDS test, the probability of the nonlinearity of this series will be high (because the opposite hypothesis is not clear in this test). So, this test can be a corroborative evidence of nonlinearity of the stock return series. Ergo, by confirming predictability and also nonlinearity of the related time series during the research, nonlinear models, i.e., ARFIMA, NNAR and NNARX (hybrid models) can be used for forecasting.

3.2. Stationary Test

As the next step, stationary of the DLTED series (done to prevent creation of a spurious regression) will be assessed using different tests (see Table 3 for the results).

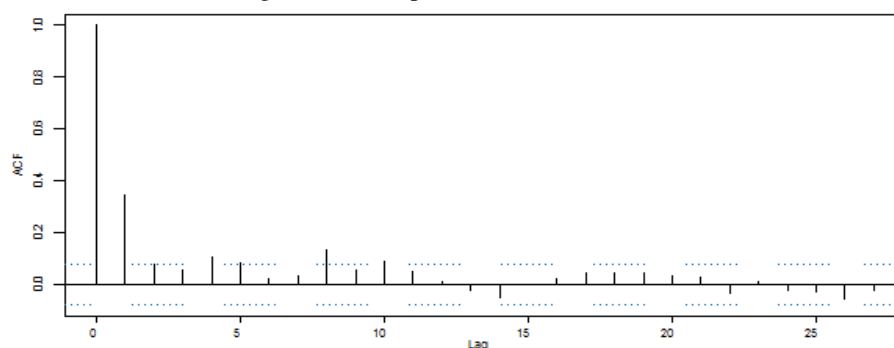
Table 3: The results related to stationary of the stock return series

Test	Critical Stat.	Accounting Value	Result
ADF ¹	-1.9413	-16.586	Stationary
ERS ²	3.2600	0.9403	Non-Stationary
PP ³	-1.9413	-17.543	Stationary
KPSS ⁴	0.4630	0.590	Non-Stationary

Source: Findings of Study

If the long memory feature does not exist, it is expected that the series becomes stationary by first differencing, but the results of first differencing show that stock return series is stationary in ADF and PP tests while in the KPSS and also ERS test the results are indicative of non-stationary of the series (see Table 3 for the results). Such conditions might have been caused by the long memory feature in this series. For this reason, the long memory feature in the stock return series (by fractional differencing series) was further analyzed by the researchers. Besides, interpreting the Autocorrelation plot can also help to find if there is long memory in the stock return series; as shown in Fig. 1 below, the autocorrelation between different lags in the time series has not disappeared even after about 30 periods and, in fact, these autocorrelations in the series are decreasing at a very slow rate. This is anomalous to the behavior of autocorrelation of the stationary series in which the autocorrelations between different lags in the series decrease exponentially.

Fig. 1. ACF Graph for Stock Return Series



Source: Findings of Study

3.3. Examining the fractal market Hypothesis

Generally, dependence of the behavior of a market on the Efficient Markets Hypothesis depends on the significance of long memory parameter in its time series. In general, models that are based on long memory are highly dependent on the value of long memory parameter and also attenuation of the autocorrelation functions. On this basis, in the following subsections, the values of long memory parameter are estimated using the GPH. On the whole, this test is conforms to the frequency domain analysis and uses the Log-Period gram technique; this technique is a means for differentiating short and the long memory processes. It should also mentioned that slope of the regression line resulting from applying the Log-Period gram technique gives us the long memory parameter and if significant, the significance of the related feature in the stock return series can be inferred and the fractal markets hypothesis is confirmed. The results of this test have been provided in Table 4 below.

¹ Augmented Dickey–Fuller

² Elliott, Rothenberg and Stock

³ Philips-Prone

⁴ Kwiatkowski–Phillips–Schmidt–Shin

Table 4: Estimation of d parameter using GPH test based on the NLS method

Series	d-Parameter	t-stat.	Probability
Stock return series	0.14695	12.3	0.000
Stock series	1.14088	3.13	0.001

Source: Findings of Study

As shown in Table 4 above, the value for long memory parameter is non-zero (and also lower than 0.5) which is a confirmation of the existence of long memory in the stock return series. Therefore, two conclusions can be drawn from the above test: first, the fractal markets hypothesis is supported. The second conclusion is that this series should be fraction differenced once again so that modeling can be done in conformity with it. In the following sections, stock return series models will be focused upon using the models that are based upon long memory.

3.4. Estimation of the ARFIMA Model

There are different methods for estimation of the ARFIMA model and d parameter including Approximate Maximum Likelihood (AML), Exact Maximum Likelihood (EML), Modified Profile Likelihood (MPL), and Non Linear Least Square (NLS) (Ooms and Doornik, 1998). In the present study, EML, MPL, NLS methods have been selected for estimating these types of models using Ox-Metrics software. Furthermore, based on the Akaike information criterion, a comparison was made between different models of ARFIMA and the model that is found to have the lowest score of the information criterion, will be the best model for explaining mean equation of the stock return series.

Table 5: The Results of Estimation of Different Models of ARFIMA

Models	Akaike Information Criterion		
	ML	NLS	EML
ARFIMA(1,0.14,1)	-7.2126	-7.3241	-7.3235
ARFIMA(1,0.14,2)	-7.2153	-7.3289	-7.3242
ARFIMA(2,0.14,1)	-7.2124	-7.3234	-7.3226
ARFIMA(2,0.14,2)	-7.2125	-7.3250	-7.3237

Source: Findings of Study

According to Table 5, it can be concluded that $ARFIMA(1,0.14,2)$ has the lowest Akaike information criteria score and has the best performance (see Table 6 for specifications).

Table 6: The results of estimation for ARFIMA(1,0.14,2)

Variables	Coefficient	t-Stat.	Probability
Constant	0.0316	2.21	0.002
d-ARFIMA	0.1408	3.13	0.001
AR(1)	0.8541	31.41	0.000
MA(1)	0.6163	18.67	0.000
MA(2)	0.2358	3.53	0.001
Dummy(1)	0.0796	7.28	0.000
Dummy(2)	0.0519	8.73	0.000

Source: Findings of Study

It is worth mentioning that, the dummy variables introduced in the above equation can be defined as the following: *Dummy(1)* are related to the financial crisis in 2007-2008 and *Dummy(2)* is related to transferring the shares of Telecommunication Company of Iran in the stock in line with the implementation of Article 44. Additionally, considering the fact that diagnostic tests conducted on residuals of the related model are indicative of the existence of conditional variance heteroscedasticity effects, Robust Regression was used for estimating this model.

3.5. Estimation of NNAR Model

Basically, the first step in modeling all non-linear models which is based on neural networks, determining the optimal combination of design elements of neural network with the same “Network Architecture”. Hence, before comparing different models of dynamic neural network, some points related to the network architecture will be mentioned. First, for finding the number of optimal Neurons, an attempt was made to test and evaluate different networks using different neurons via encoding in the MATLAB software. Therefore, about 2 to 20 neurons were tested with two or three-layered networks; in this way, each one was trained 30 times. For comparing their performance, errors of the test data, which included 30% of the whole data, were randomly set as criterion in different models. Finally, the number of optimal neurons was found to be 10 and there were also two optimal hidden layers. The summary of information related to the network architecture has been provided in Table 7 below.

Table 7: Network Architecture

Design factor	Value
Network type	NNAR & NNARX
Number of neurons in the first hidden layer	10
Number of neurons in the second hidden layer	1
Preprocessing function	Feed Forward Network
Layer conversion function	Levenberg-Marquardt

According to the network architecture explained in Table 7 above, different models of NNAR will be estimated and compared:

Table 8: The results of estimation for different NNAR models

Models	MSE	RMSE
NNAR (1)	5.65×10^{-5}	7.52×10^{-3}
NNAR (2)	5.58×10^{-5}	7.47×10^{-3}
NNAR (3)	5.40×10^{-5}	7.35×10^{-3}
NNAR (4)	5.35×10^{-5}	7.31×10^{-3}
NNAR (5)	5.28×10^{-5}	7.26×10^{-3}
NNAR (6)	5.37×10^{-5}	7.33×10^{-3}
NNAR (7)	5.46×10^{-5}	7.39×10^{-3}
NNAR (8)	5.55×10^{-5}	7.45×10^{-3}
NNAR (9)	5.63×10^{-5}	7.50×10^{-3}
NNAR (10)	5.78×10^{-5}	7.60×10^{-3}
NNAR (15)	5.97×10^{-5}	7.73×10^{-3}
NNAR (20)	6.42×10^{-5}	8.01×10^{-3}
NNAR (30)	7.04×10^{-5}	8.39×10^{-3}

Source: Findings of Study

According to Table 8, NNAR(5) model (using 5 lags in stock series) had the best performance in comparison with other models based on the MSE and RMSE criteria.

3.6. Estimation of Hybrid model (NNARX)

Considering the fact that, the main purpose of this study was to develop a new hybrid model that could yield more accurate forecasts of the return series, in this part of the study, there will be an attempt to combine the models mentioned above and present a model that could not only takes into consideration the theories related to the financial markets (such as the fractal markets hypothesis) but also benefits from the strength and flexibility of the models based on artificial intelligence. Thus, in order to achieve more accurate forecasts, the forecasting results from ARFIMA model, which had been obtained via Robust Regression, were used as the input for the dynamic neural network model and on this basis, the improvement in forecasting stock return series will be focused upon. The results produced by this model have been presented in the following table.

Table 9: The results of estimation for different NNARX models

Models	MSE	RMSE
NNARX (1)	4.63*10 [^] (-5)	6.80*10 [^] (-3)
NNARX (2)	4.42*10 [^] (-5)	6.64*10 [^] (-3)
NNARX (3)	4.17*10 [^] (-5)	6.45*10 [^] (-3)
NNARX (4)	3.91*10 [^] (-5)	6.25*10 [^] (-3)
NNARX (5)	4.08*10 [^] (-5)	6.39*10 [^] (-3)
NNARX (6)	4.29*10 [^] (-5)	6.55*10 [^] (-3)
NNARX (7)	4.51*10 [^] (-5)	6.72*10 [^] (-3)
NNARX (8)	4.73*10 [^] (-5)	6.88*10 [^] (-3)
NNARX (9)	4.96*10 [^] (-5)	7.04*10 [^] (-3)
NNARX (10)	5.18*10 [^] (-5)	7.20*10 [^] (-3)
NNARX (15)	5.37*10 [^] (-5)	7.33*10 [^] (-3)
NNARX (20)	6.01*10 [^] (-5)	7.75*10 [^] (-3)
NNARX (30)	7.94*10 [^] (-5)	8.91*10 [^] (-3)

Source: Findings of Study

The results shown in Table 9, are indicative of the fact that NNARX(4) has the best performance in comparison with other models based on the forecasting error criterion. The reason for the difference between NNAR and NNARX models in forecasting results might be the use of the results obtained from a model based on long memory in the NNAR model.

3.7. Comparing the performance of models in accuracy of forecasts

MSE and RMSE are the most frequently used criteria for comparing models in accuracy of predictions among other criteria for assessing accuracy of prediction (Swanson & et al, 2011). Therefore, on the basis of the specified criteria, a comparison will be made between different models in their accuracy of out-of-sample forecasting (60 out-of-sample observations) (see Table 10 for the results of comparison).

Table 10: The results of comparison of the models

Models	MSE	RMSE
ARFIMA(1,0.14,2)	6.57*10 [^] (-5)	8.11*10 [^] (-2)
NNAR(5)	5.28*10 [^] (-5)	7.26*10 [^] (-3)
NNARX(4)	3.91*10 [^] (-5)	6.25*10 [^] (-3)

Source: Findings of Study

As shown in Table 8, the performance of NNAR(5) model is better than ARFIMA(1,0.12,1) in forecasting stock return series during the period under investigation while the hybrid model or NNARX had a better forecasting performance compared to other two models.

4. Conclusions

In this study, Nonlinear Neural Network Auto Regressive Model (NNAR) and Autoregressive Fractionally Integrated Moving Average (ARFIMA) model were used to forecast TSE's Price and Dividend Index. The results of this study showed that NNAR model yields more accurate forecasts about stock return index in the time series under investigation in comparison with the ARFIMA model. Furthermore, considering the importance of making more accurate forecasts, an attempt was made to obtain more reliable results about stock return series using a novel hybrid intelligent framework based on dynamic neural network and also the results from ARFIMA model. The results of this study showed that NNAR model yields more accurate forecasts about stock return series under investigation in comparison with the ARFIMA model. This result was not unexpected because considering the high flexibility of neural network models and especially dynamic neural network models in contrast the inflexible and imposed structure of regressive models such as ARFIMA model causes a change (adaptation) in their coefficients when there is a change in the time series under investigation. Another

finding of the study was that the combination of ARFIMA and NNAR yielded more accurate forecasts. Thus, the hybrid model might be more effective in improving the accuracy of forecasting because it combines the results of regressive models based on theory with the results from nonlinear dynamic neural network models. This result has important implications for future studies as well. In fact, future studies might be directed at improving the forecasting accuracy by changing the type of NNAR in hybrid models presented here. Finally, dynamic neural networks can also be introduced to policy-makers and mass economy decision-makers and also investors as an appropriate method.

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