
Gianluigi Coppola

Dipartimento di Scienze Economiche e Statistiche. Università di Salerno. Italy, CELPE Centro di Economia del Lavoro e di Politica Economica

5. September 2012

Online at http://mpra.ub.uni-muenchen.de/49667/
Macro Models
An App for Macroeconomic Models.
User Manual 2.0

Gianluigi Coppola
DISES-Dipartimento di Scienze Economiche e Statistiche
CELPE -Centro di Economia del Lavoro e di Politica Economica
University of Salerno

July 4, 2013 – Version 2.0
Preliminary Version

1Email: glcoppola@unisa.it - http://www.unisa.it/docenti/gianluigicoppola/index
Abstract

Macro Models are a series of free Apps available in App Store and they work with the Ipad. Each App simulates a specific macroeconomic model and it shows both the static and the dynamic results. The first four Apps developed and published are: the Income-Expenditure model in two versions (I and II), the IS-LM model and the Taylor’s rule (IS-MP model). In this paper we describe the economic model of each single App and we also show several examples on how it works.

Keywords: Macroeconomics, Income-Expenditure model, IS-LM, Taylor's rule, APP.
Jel Codes: A20; E20

Acknowledgment

The Apps of Macro Models series have been developed by Gianluigi Coppola and Natalia Marsilia (nmarsilia@yahoo.it). Particularly she is the engineer who made the software. I would like to give a special thanks to her because it wasn't possible to realize the APPs and also this paper without her precious help. Thank you very much, Natalia!
## Contents

1 **Introduction** ............................................. 4

2 **The Income Expenditure model** ............................................. 6
   1. Introduction .................................................. 6
   2. The Model I: Income-Expenditure Model ......................... 7
      2.1. The Comparative Static .................................. 10
      2.2. Balanced Budget Multiplier ............................... 12
      2.3. The reduction of Government Budget Deficit (keeping Income constant) .................................. 13
      2.4. The Fiscal Policy Options ................................ 14
      2.5. Some Examples (I): A reduction of the Investment *(with a Government budget still positive)* .................................. 15
      2.6. Some Examples (I): A reduction of the Investment *(with a Government budget that becomes negative)* .................................. 24
      2.7. Legenda of the Income-Expenditure Model I ............... 29
   3. The Model II: the Samuelson’s Multiplier Accelerator Model .... 31
      3.1. Legenda of the Income-Expenditure Model II ............. 33

3 **The IS-LM model** ............................................. 35
   1. The Real Sector (IS Curve) .................................. 35
   2. The Monetary Market (LM Curve) ............................... 36
   3. The IS-LM Equilibrium ........................................ 38
   4. The impact of Fiscal Policy and of the Monetary Policy ........ 39
MACRO MODELS
AN APP FOR MACROECONOMIC MODELS.
USER MANUAL 2.0

4.1. The Classic Hypothesis .................................. 39
4.2. The Keynesian Hypothesis .............................. 40
4.3. Legenda of the IS-LM Model ......................... 46

4 The IS-MP model .............................................. 49
1. The IS Curve .................................................. 49
2. The Monetary Market: the Taylor’s rule ............... 50
   2.1. Legenda of the IS-MP Model ....................... 55
Chapter 1

Introduction

This paper is a user manual of an APP that simulates the widely used Macroeconomic Models. The first two apps developed concern the Income-Expenditure Model and the IS-LM Model. Other Apps will be realized in the next months. The first question we have to answer is: why an App? There are two reasons. Firstly, we think that tablets give another opportunity to learn. With the tablets you can play, write e-mail, and connect to Internet, everywhere. But you can also read articles and books and listen mp3. For these reasons an App is an opportunity to understand how the main macroeconomics models work. Secondly in the textbooks here are only few examples for each single model, and they concerns mainly the static aspects. With the app it is possible to simulate both the static and the dynamic results of the model. In fact with each app it is possible to input the parameters of the model in order to obtain both the static and the dynamic results.

But there is also another important issue. With this app and with this paper we would like to give another interpretation of the macroeconomic models. They are schemes useful to study the implication the instruments applied by the government in order to guarantee the social stability.

The logo of the app is a sphere over a picture of a water course. The sphere is un-
real while the photo is real. The sphere is stable and it represents the "perfect" equilibrium: each of the infinite points of the sphere is an equilibrium and it is identical to all the others. The water is dynamic and it represents the unstable conditions of the reality. The sphere may represent the being, the metaphysic, while the water is the becoming, the nature. For Talete water was also the origin of all things. Parmenides says that two things, being and becoming, sphere and water, are conflicting. But the government has to rule the dynamic, thinking to the sphere.

The Apps can be downloaded by the Appl Store. They are free. Each App may contains one or more models. The screen of the single app is divided into two parts that it can be scrolled. The first table of the upper side of the screen is the panel of inputs. It contains three columns, each of them represents a period. For example, the first one is the initial period, while in the second one there is a shock (i.e a decrease of the investment) and in the third period the Government reacts to that negative shock cutting the income tax rate. The first panel of the lower part of the screen shows the results of the model in the equilibrium. You can obtain them by pressing the RESET button, while with SAVE you save them. In the lower part of the screen the are also some graphs. Some of them shows the model’s static results while some others show the dynamics of the variables. It is possible to choice what variable to plot switching the cursors that are in "Graphic". The Legend, that is in the upper side of the screen, explains the meanings of the symbols, the results, and the graphs.
Chapter 2

The Income Expenditure model

1. Introduction

The Income Expenditure model is the first one that students find in the textbook of Macroeconomics. It is based on two assumptions. The first one is that prices are fixed. This implies that in the model the prices mechanism doesn't work. In order to reach the equilibrium it must change the quantity of goods and services offered. If the demand is greater than the supply, the production will fall, while it is the contrary, as to say the supply is greater than the demand, the production and the supply will rise.

The second assumption is that there are infinite equilibria but not all of them can ensure the social stability, because the economic system may reach an equilibrium were there isn't full employment. According the Keynesian theory, only with the Government's intervention, it will be possible to reach a full employment situation or a condition of social stability, even in the short run. In other words, the economic system is unstable. It is mainly due to the Investments that are the unstable component of the aggregate demand. The Government can stabilize the business cycle through the fiscal policy. In order to make the production growth, the government can increase the economic expenditure, or reduce the taxes. In the first case it substitute the private sector, while in the
second case, it stimulates the private sector through the disposable income and the consumption.

Anyway, in the recent years with the crises of the Eurozone, many European country, as Greece, Spain and Italy, were obliged to reduce their debt. In these cases the social stability was linked to the reduction of the public debts instead of the reduction of unemployment. For this reason in the software developed we give particular attention to the dynamic of the debt.

2. The Model I: Income-Expenditure Model

Be $Y$ the income, $t$ the Income tax rate, and $TR$ the net Government Transfers. $TR$ is positive if the amount of subsidies is greater than the lump-sum taxes, and it is negative otherwise. The after-tax income, or disposable income, $YD$, is equal to

$$YD = Y + TR - tY$$  \hspace{1cm} (2.1)$$

The Aggregate Demand $AD$ is equal to the sum of Consumption $C$, Investment $I$, Net Export $NX$, and the Government’s expenditure $G$.

$$AD = C + I + G + NX + G$$  \hspace{1cm} (2.2)$$

The Keynesian Consumption function is:

$$C = \overline{C} + cYD$$  \hspace{1cm} (2.3)$$

where $\overline{C}$ is the autonomous consumption, and $c$ is the marginal propensity to consume. $\overline{C} > 0$ and $0 < c < 1$. Substituting $Yd$ into the equation (2.3), it obtains:

$$C = \overline{C} + cTR + c(1 - t)Y$$  \hspace{1cm} (2.4)$$
\( c(1-t) \) is the Net Marginal Propensity (NMP) to consume. The Investment function is:

\[
I = T + \theta Y \tag{2.5}
\]

\( T \) is the autonomous investment and \( \theta \) the marginal propensity to invest. \( \theta \geq 0 \).

The Net Exports \( NX \) are exogenous.

The Government can modify the expenditure \( G \), the Net Transfer \( TR \), and the income taxes rate \( t \). They are the government’s instruments.

The Income Expenditure Model is:

\[
C = \bar{C} + cTR + c(1-t)Y
\]

\[
I = T + \theta Y
\]

\[
G = \bar{G}
\]

\[
TR = \bar{TR}
\]

\[
NX = \bar{NX}
\]

\[
Y = AD \tag{2.6}
\]

The equation (2.6) is the equilibrium where the supply \( Y \) is equal to the demand \( AD \). It also possible to rewrite (2.6) as:

\[
Y = \bar{C} + c\bar{TR} + \bar{T} + \bar{NX} + \bar{G} + C(1-t)Y + \theta Y \tag{2.7}
\]
Solving for $Y$, we obtain the equilibrium income:

$$Y_e = \frac{1}{(1 - c(1 - t) - \theta)}[\bar{C} + c\bar{TR} + \bar{NX} + I + G]$$  \hspace{1cm} (2.8)$$

$\frac{1}{(1 - c(1 - t) - \theta)}$ is the Keynesian Multiplier. It is possible to demonstrate that with $\theta = 0$ the Keynesian Multiplier is always greater than one. With $\theta > 0$ we assume that $0 < 1 - c(1 - t) - \theta < 1$. For this reason also in this case the Keynesian Multiplier is always positive and greater than 1.

Once obtained the equilibrium income, it is possible to calculate the equilibrium consumption and the equilibrium investment. They are respectively:

$$C_e = \bar{C} + c\bar{TR} + c(1 - t)Y_e$$  \hspace{1cm} (2.9)$$

$$I_e = \bar{I} + \theta Y_e$$  \hspace{1cm} (2.10)$$

The Balance Surplus $BS$ of the government is equal to the difference between receipts and expenditure. The receipts are the amount of taxes $tY$ and the expenditure are represented by the sum of the government’s expenditure $G$ and the Net Transfer $TR^1$. In formula:

$$BS = tY - (G + TR)$$  \hspace{1cm} (2.11)$$

The Balance Surplus in equilibrium is equal to:

$$BS_e = tY_e - (G + TR)$$  \hspace{1cm} (2.12)$$

or

$$BS_e = t\frac{1}{(1 - c(1 - t) - \theta)}[\bar{C} + c\bar{TR} + \bar{NX} + \bar{I} + \bar{G}] - (G + TR)$$  \hspace{1cm} (2.13)$$

There is a deficit for $BS < 0$. The government’s debt $B$ at the time $t$ is equal

---

$^1$If $TR < 0$ the net transfer are receipts.
to the algebraic sum of the previous surplus and deficits:\(^2\):

\[ B = \sum_{t=0}^{T} BS_t \quad (2.14) \]

### 2.1. The Comparative Static

\( C, I \) and \( NX \) are the exogenous variables of the model. A shock of one of these variables causes a variation of income equals to the Keynesian multiplier

\[
\frac{dY}{dI} = \frac{dY}{dC} = \frac{dY}{dNX} = \frac{1}{(1 - c(1 - t) - \theta)} \quad (2.15)
\]

The government can change the government expenditure \( G \), the Net Transfers \( TR \) and the income tax rate \( t \). The multiplier are respectively:

\[
\frac{dY}{dG} = \frac{1}{(1 - c(1 - t) - \theta)} \quad (2.16)
\]

\[
\frac{dY}{dTR} = \frac{c}{(1 - c(1 - t) - \theta)} \quad (2.17)
\]

\[
\frac{dY}{dt} = \frac{-c}{(1 - c(1 - t) - \theta)^2} \left[ C + cTR + NX + I + G \right] \quad (2.18)
\]

The impact on government budget is:

\[
\frac{dB}{dI} = \frac{dB}{dC} = \frac{dB}{dNX} = \frac{t}{(1 - c(1 - t) - \theta)} \quad (2.19)
\]

\[
\frac{dB}{dG} = \frac{t}{(1 - c(1 - t) - \theta)} - 1 \quad (2.20)
\]

\[
\frac{dB}{dTR} = \frac{ct}{(1 - c(1 - t) - \theta)} - 1 \quad (2.21)
\]

\(^2\)We are optimistic. We consider that the interest rate on the debt is equal to zero.
\[
\frac{dBS}{dt} = \frac{(1 - c - d)}{(1 - c(1 - t) - \theta)^2} [\bar{C} + c \bar{T}R + \bar{N}X + I + \bar{G}] \tag{2.22}
\]

The surplus is:

\[BS = tY - (\bar{G} + \bar{T}R)\tag{2.23}\]

The variation of surplus is equal to:

\[dBS = tdY - d\bar{G} - d\bar{T}R\tag{2.24}\]

For the sake of simplicity we suppose that \(\theta = 0\). The variation of Equilibrium income is equal to:

\[dY_e = \left(\frac{1}{1 - c(1 - t)}\right) [cd\bar{T}R + d\bar{G}]\tag{2.25}\]

and the change in the government Budget Surplus \(BS\) is:

\[dBS = t \left(\frac{1}{1 - c(1 - t)}\right) [cd\bar{T}R + d\bar{G}] - [d\bar{G} + d\bar{T}R]\tag{2.26}\]

\[dBS = \left(\frac{1}{1 - c(1 - t)} - 1\right) [d\bar{G}] + \left(\frac{c}{1 - c(1 - t)} - 1\right) [d\bar{T}R]\tag{2.27}\]

\[dBS = \left(\frac{(1 - c)(t - 1)}{1 - c(1 - t)}\right) [d\bar{G}] + \left(\frac{(c - 1)}{(1 - c(1 - t))} - 1\right) [d\bar{T}R]\tag{2.28}\]

\[dBS = \left(\frac{1}{(1 - c(1 - t))} - 1\right) [d\bar{G}]\tag{2.29}\]

The change in Government expenditure \(d\bar{G}\) has an impact on Budget Surplus less than its amount, being

\[0 \leq \left(\frac{1}{1 - c(1 - t)}\right) \leq 1\tag{2.30}\]
In other words an increase (or a decrease) in \( G \) causes also an increase (or decrease) in the Tax revenue \( tY \) equal to \( t \frac{1}{(1-c(1-t))} \). The algebraic sum is less than \( dG \).

### 2.2. Balanced Budget Multiplier

A government can increase spending and taxes keeping the budget in balance. In this case the Government expenditure multiplier has a different value, in another words, it is different the impact of a change in Government expenditure \( dG \) on income \( Y \).

The variation of Budget Surplus \( BS \) is equal to:

\[
dBS = tdY - dG - dTR
\]

or

\[
dBS = \left( \frac{(1-c)(t-1)}{(1-c(1-t))} \right) [dG] + \left( \frac{(c-1)}{(1-c(1-t))} - 1 \right) dTR \]

For \( dBS = 0 \)

\[
\left( \frac{(1-c)(t-1)}{(1-c(1-t))} \right) [dG] + \left( \frac{(c-1)}{(1-c(1-t))} - 1 \right) dTR = 0
\]

\[
dTR = (t - 1)dG
\]

Let’s now consider the change in income

\[
dY_e = \frac{1}{(1-c(1-t))}[cdTR + dG]
\]

and substituting \( TR \) with \( (t - 1)dG \), we obtain

\[
dY_e = \frac{1}{(1-c(1-t))}[c(t - 1)dG + dG]
\]
\[ dY_e = \frac{1}{(1 - c(1 - t))} [1 - c(1 - t)] d\overline{G} = 1 \] \hspace{1cm} (2.37)

This result is known as Haavelmo Theorem (Haavelmo, 1945). When the Government increases spending and taxes keeping the budget in balance, the multiplier is equal to 1.

### 2.3. The reduction of Government Budget Deficit (keeping Income constant)

In this subsection we consider the case in which the Government reduces its budget deficit, keeping the income constant. We know that the change in income is equal to:

\[ dY = \frac{1}{(1 - c(1 - t) - \theta)} [d\overline{G} + cdTR] \] \hspace{1cm} (2.38)

and the change in the Budget Surplus is:

\[ dBS = tdY - (d\overline{G} + dTR) \] \hspace{1cm} (2.39)

For \( dY=0 \), we obtain:

\[ d\overline{G} = -cdTR \] \hspace{1cm} (2.40)

or

\[ dTR = -\frac{1}{c}d\overline{G} \] \hspace{1cm} (2.41)

Substituting this result in the budget surplus equation, it becomes:

\[ dBS = (d\overline{G} - \frac{1}{c}d\overline{G}) \] \hspace{1cm} (2.42)
\[ dB\bar{S} = \frac{s}{c}d\bar{G} \]  

where \( s = 1 - c \). This is the impact of a change in Government expenditure on the budget surplus when income is kept constant.

### 2.4. The Fiscal Policy Options

In the next scheme, it is shown a list of feasible fiscal policy measures as consequence of a negative Investment shock. As it is well know, a decrease in investment \((I_{\downarrow})\) causes a reduction of income \((Y_{\downarrow})\) and of the Government Budget Surplus \((BS_{\downarrow})\).

It is useful to distinguish two scenarios. In the first one, the budget surplus remains positive, while, in the second scenario, it becomes negative.

In the first case the government can decide to increase income \((Y_{\uparrow})\) or to do nothing \((0)\)\(^3\). In the second case the Government can pursue three aims (one more compared with the first one): 1) to increase income \((Y_{\uparrow})\), to do nothing \((0)\), and to reduce Deficit \((BS_{\uparrow})\).

The first group includes the Keynesian fiscal Policies [1. ], the second group is a "non-intervention“ fiscal policy [2. ], while the third one is direct to control the Government’s Balance [3.].

The scheme 1 shows this possible list of fiscal policy,

Scheme 2. List of Fiscal Policies

---

\(^3\)to do nothing is always a political option.
2.5. Some Examples (I): A reduction of the Investment (with a Government budget still positive)

In this section we show some examples. Each case is represented by a figure that includes 4 graphs: 1) Income - Expenditure Equilibrium, 2) The Government’s Budget \((BS = f(Y))\), 3) The variables’ dynamic, 4) the Government’s budget’s dynamic. There is a short comment for Each case. The Figure are taken from the Macro Models’ APP. The history begins from the Equilibrium: a negative shock of the investment causes a reduction of Income and of government budget. In this first example
Table 2.1: Fiscal Policies

<table>
<thead>
<tr>
<th>Symbol</th>
<th>$t_0$</th>
<th>$t_1$</th>
<th>$t_2$ (I)</th>
<th>$t_2$ (II)</th>
<th>$t_2$ (III)</th>
<th>$t_2$ (IV)</th>
<th>$t_2$ (V)</th>
<th>$t_2$ (V)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_0$</td>
<td>900</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
</tr>
<tr>
<td>$C$</td>
<td>300</td>
<td>300</td>
<td>300</td>
<td>300</td>
<td>300</td>
<td>300</td>
<td>300</td>
<td>300</td>
</tr>
<tr>
<td>$I_0$</td>
<td>900</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
</tr>
<tr>
<td>$NX$</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
<td>-80</td>
</tr>
<tr>
<td>$c$</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
<td>0.75</td>
</tr>
<tr>
<td>$d$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$G$</td>
<td>700</td>
<td>700</td>
<td>900</td>
<td>811.43</td>
<td>700</td>
<td>700</td>
<td>1157.15</td>
<td></td>
</tr>
<tr>
<td>$TR$</td>
<td>200</td>
<td>200</td>
<td>200</td>
<td>200</td>
<td>466.6</td>
<td>200</td>
<td>-142.15</td>
<td></td>
</tr>
<tr>
<td>$t$</td>
<td>0.25</td>
<td>0.25</td>
<td>0.25</td>
<td>0.25</td>
<td>0.25</td>
<td>0.25</td>
<td>0.146</td>
<td></td>
</tr>
<tr>
<td>NMP</td>
<td>0.56</td>
<td>0.56</td>
<td>0.56</td>
<td>0.56</td>
<td>0.56</td>
<td>0.64</td>
<td></td>
<td></td>
</tr>
<tr>
<td>K. M</td>
<td>2.29</td>
<td>2.29</td>
<td>2.29</td>
<td>2.29</td>
<td>2.29</td>
<td>2.78</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$Y_e$</td>
<td>4502.86</td>
<td>4045.71</td>
<td>4502.86</td>
<td>4299.4</td>
<td>4502.86</td>
<td>4502.91</td>
<td>4502.91</td>
<td></td>
</tr>
<tr>
<td>$C_e$</td>
<td>2982.86</td>
<td>2725.71</td>
<td>2982.86</td>
<td>2868.43</td>
<td>3182.6</td>
<td>3182.91</td>
<td>2726.84</td>
<td></td>
</tr>
<tr>
<td>$I_e$</td>
<td>900</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td>700</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$BS_e$</td>
<td>225.71</td>
<td>111.43</td>
<td>25.71</td>
<td>63.86</td>
<td>-40.95</td>
<td>-40.97</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta Y$</td>
<td>-457.14</td>
<td>457.14</td>
<td>253.71</td>
<td>457.15</td>
<td>457.15</td>
<td>457.15</td>
<td>457.15</td>
<td></td>
</tr>
</tbody>
</table>
Figure 2.1: At the Beginning of the History
Figure 2.2: Case 1.1. A negative shock: $I_{\downarrow}$ and $BS > 0$
Figure 2.3: Case 1.II. the Keynesian scenarios: I↓ and G↑

$BS$ becomes negative for "a while". $Y$ returns at the initial level.
Figure 2.4: Case 1.III. I↓ and G↑
$BS$ is always positive but $Y$ does not return at the initial level.
Figure 2.5: Case 1.IV \( I \downarrow \) and \( TR \uparrow \)
\( C \uparrow \uparrow \), \( BS \) is negative and higher.
Figure 2.6: Case 1.V. I - Haavelmo Theorem. ↓ - \( G \uparrow \), \( TR \downarrow \)

\( BS \) is constant.
Figure 2.7: Case 1.VI \( \downarrow \) and \( TR \uparrow \)
\( C \uparrow \uparrow \), \( BS \) is negative and higher (as Case 1.IV.)
2.6. Some Examples (I): A reduction of the Investment (*with a Government budget that becomes negative*)
Figure 2.8: Case 2: A negative shock: $I \downarrow$ and $BS < 0$
Figure 2.9: Case 2.1: A negative shock: $I \downarrow$ and $BS < 0$. In order to reduce $BS \to 0$, $G \downarrow$, and also $C \downarrow$ and $Y \downarrow$. 
Figure 2.10: Case 2.2: A negative shock: $I_\downarrow$ and $BS < 0$.
In order to reduce $BS \to 0$, $G \uparrow$, $TR \downarrow$, $C \downarrow$ but $Y$ remains constant.
Figure 2.11: Case 2.2: A negative shock: $I \downarrow$ and $BS < 0$. In order to reduce $BS \rightarrow$ "initial value"=225.71, $G \uparrow$, $TR \downarrow$, $C \downarrow$ but $Y$ remains constant.
2.7. **Legenda of the Income-Expenditure Model I**

Legenda

**Table 2.2: Input**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\bar{C}$</td>
<td>Autonomous (exogenous) Consumption</td>
</tr>
<tr>
<td>$I_0$</td>
<td>Net Investment</td>
</tr>
<tr>
<td>$NX$</td>
<td>Net Export</td>
</tr>
<tr>
<td>$c$</td>
<td>Marginal Propensity To Consume</td>
</tr>
<tr>
<td>$d$</td>
<td>Marginal Propensity to Invest</td>
</tr>
<tr>
<td>$G$</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>TR</td>
<td>Net Government Transfers payments</td>
</tr>
<tr>
<td>$t$</td>
<td>Income tax rate</td>
</tr>
</tbody>
</table>
### Table 2.3: Output

<table>
<thead>
<tr>
<th>acronymous</th>
<th>Parameter/Variable</th>
<th>formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>NMP</td>
<td>Net Marginal Propensity to consume</td>
<td>$c(1 - t)$</td>
</tr>
<tr>
<td>Multiplier</td>
<td>Keynesian Multiplier</td>
<td>$\frac{1}{1-c(1-t)-d}$</td>
</tr>
<tr>
<td>Eq. Income</td>
<td>Equilibrium Income</td>
<td>$Y_e$</td>
</tr>
<tr>
<td>Eq. Consumption</td>
<td>Equilibrium Consumption</td>
<td>$C_e$</td>
</tr>
<tr>
<td>Balance</td>
<td>Government Surplus</td>
<td>$tY_e - (G + TR)$</td>
</tr>
<tr>
<td>ΔIncome</td>
<td>Income Variation</td>
<td>$Y_{e,t} - Y_{e,t-1}$</td>
</tr>
</tbody>
</table>

### Table 2.4: Graph

<table>
<thead>
<tr>
<th>EAD</th>
<th>Autonomous Aggregate Demand</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Y$</td>
<td>Income</td>
</tr>
<tr>
<td>$tY$</td>
<td>income tax</td>
</tr>
<tr>
<td>$C$</td>
<td>Consumption</td>
</tr>
<tr>
<td>$I$</td>
<td>Investment</td>
</tr>
<tr>
<td>$D$</td>
<td>Government Surplus</td>
</tr>
<tr>
<td>$B$</td>
<td>Government Debt</td>
</tr>
</tbody>
</table>
3. The Model II: the Samuelson’s Multiplier Accelerator Model

In this version of the model we introduce the "Principle of Acceleration" as in Samuelson (1939). The model assumes that consumption depends on the previous income. In formulas, we have that

\[ C_t = \bar{C} + cTR + c(1 - t)Y_{t-1} \]  \hspace{1cm} (2.44)

and the investment on the variation of consumption.

\[ I_t = T + n(C_t - C_{t-1}) \]  \hspace{1cm} (2.45)

In this case it is possible to write:

\[ I_t = T + nc(1 - t)(Y_{t-1} - Y_{t-2}) \]  \hspace{1cm} (2.46)

or

\[ I_t = T + \phi dY_{t-1} \]  \hspace{1cm} (2.47)

where \( \phi = nc(1 - t) \).

For \( \phi > 0 \) the APP shows only the dynamic results. Hereafter, we report some examples.
Figure 2.12: Case 3: Some Examples

(a) $c=0.5; n=0; \phi=0, t=0$
(b) $c=0.5; n=0.98; \phi=0.49, t=0$
(c) $c=0.8; n=1.25; \phi=1, t=0$
(d) $c=0.6; n=2; \phi=1.2, t=0$
3.1. Legenda of the Income-Expenditure Model II

Legenda

Table 2.5: Input

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C$</td>
<td>Autonomous (exogenous) Consumption</td>
</tr>
<tr>
<td>$I_0$</td>
<td>Net Investment</td>
</tr>
<tr>
<td>$NX$</td>
<td>Net Export</td>
</tr>
<tr>
<td>$c$</td>
<td>Marginal Propensity To Consume</td>
</tr>
<tr>
<td>$\phi$</td>
<td>Accelerator parameter</td>
</tr>
<tr>
<td>$G$</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>TR</td>
<td>Net Government Transfers payments</td>
</tr>
<tr>
<td>$t$</td>
<td>Income tax rate</td>
</tr>
</tbody>
</table>
Table 2.6: Output

<table>
<thead>
<tr>
<th>acronymous</th>
<th>Parameter/Variable</th>
<th>formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>NMP</td>
<td>Net Marginal Propensity to consume</td>
<td>$c(1 - t)$</td>
</tr>
<tr>
<td>Multiplier</td>
<td>Keynesian Multiplier</td>
<td>$\frac{1}{(1 - c(1-t) - d)}$</td>
</tr>
<tr>
<td>Eq. Income</td>
<td>Equilibrium Income</td>
<td>$Y_e$</td>
</tr>
<tr>
<td>Eq. Consumption</td>
<td>Equilibrium Consumption</td>
<td>$C_e$</td>
</tr>
<tr>
<td>Balance</td>
<td>Government Surplus</td>
<td>$tY_e - (G + TR)$</td>
</tr>
<tr>
<td>∆Income</td>
<td>Income Variation</td>
<td>$Y_{e,t} - Y_{e,t-1}$</td>
</tr>
</tbody>
</table>

Table 2.7: Graph

<table>
<thead>
<tr>
<th>EAD</th>
<th>Autonomous Aggregate Demand</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Y$</td>
<td>Income</td>
</tr>
<tr>
<td>$tY$</td>
<td>income tax</td>
</tr>
<tr>
<td>$C$</td>
<td>Consumption</td>
</tr>
<tr>
<td>$I$</td>
<td>Investment</td>
</tr>
<tr>
<td>$D$</td>
<td>Government Surplus</td>
</tr>
<tr>
<td>$B$</td>
<td>Government Debt</td>
</tr>
</tbody>
</table>
Chapter 3

The IS-LM model

1. The Real Sector (IS Curve)

We begin to consider the neoclassic Investment function in which the investment depends on the interest rate \( r \). The function is:

\[
I = I_0 - br + \theta Y
\]  

(3.1)

with \( b > 0 \)

The model now becomes:

\[
Y = AD
\]

\[
AD = C + I + G + NX
\]

\[
C = \bar{C} + cTR + c(1 - t)Y
\]

\[\text{In the IS-LM, the prices level } \overline{P} \text{ is constant, as to say, the inflation } (\pi) \text{ is equal to zero. For the Fisher equation, the nominal interest rate } (i) \text{ is equal to real rate } (r) \text{ plus inflation } i = r + \pi. \text{ In this model } \pi = 0, \text{ so the nominal interest rate } (i) \text{ is equal to real interest rate } (r).\]
\[ I = T - br + \theta Y \]

\[ TR = TR \]

\[ NX = NX \]

The real sector is in equilibrium when the supply \( Y \) is equal to the demand \( AD \)

\[ Y = AD \]

\[
Y = \frac{1}{(1 - c(1 - t) - \theta)} \left[ \bar{C} + \bar{G} + c\bar{TR} + \bar{NX} + I - br \right] \tag{3.2}
\]

This is the IS equation in which the income \( Y \) is function of real interest rate \( r \). It is possible to rewrite the 3.2 as:

\[
Y = \frac{1}{(1 - c(1 - t) - \theta)} [\bar{A} - br] \tag{3.3}
\]

where

\[
\bar{A} = \bar{C} + \bar{G} + c\bar{TR} + \bar{NX} + I \tag{3.4}
\]

2. The Monetary Market (LM Curve)

The Money Supply of the Central Bank is \( \bar{M} \). The Prices Level \( \bar{P} \) is exogenous. So the real money supply is:

\[
\frac{\bar{M}}{\bar{P}} \tag{3.5}
\]

The demand of real money balance, or Liquidity \( L \), is increasing in income
(Y), and decreasing in interest rate $r_{lt}$.

\[ L = \frac{M}{P} = L(Y, r) \]  \hspace{1cm} (3.6)

with $L_Y > 0$ and $L_r < 0$

It is possible to distinguish two cases. $L_r = 0$ is the case of classic school: interest rate is not a monetary variable and the demand of Money depends only on income (Y). On the contrary $L_r \to \infty$ is the case the Keynesian liquidity trap. the demand of money is infinite.

As functional form we use a linear equation.

\[
L = \begin{cases} 
  kY - hr & \text{if } r > r_{lt} \\
  \infty & \text{if } r = r_{lt}
\end{cases}
\]

with $k > 0$, $h \geq 0$ and $r_{lt} \geq 0$

In order to encompass the "Liquidity Trap" hypothesis, we define $r_{lt}$ as the "Liquidity Trap" interest. At this level of interest, the demand of real money is infinite.

The Equilibrium in the Monetary Market is given by:

\[
\frac{M}{P} = L
\]  \hspace{1cm} (3.7)

\[
\frac{M}{P} = kY - hr
\]  \hspace{1cm} (3.8)

It is also possible to write the last equation as:

\[
Y = \frac{1}{k} \left( \frac{M}{P} + hr \right)
\]  \hspace{1cm} (3.9)

or

\[
r = \frac{1}{h} \left( kY - \frac{M}{P} \right)
\]  \hspace{1cm} (3.10)
The 3.10 is the LM curve.

3. The IS-LM Equilibrium

The Equilibrium is given by the system of the two equation:

\[ Y = \frac{1}{(1 - c(1 - t) - \theta)} [C + cTR + NX + I - br + G] \]

\[ Y = \frac{1}{k} \left( \frac{M}{P} + hr \right) \]

The Equilibrium income is equal to:

\[ Y = \frac{h}{(1 - c(1 - t) - \theta)h + bk} \left( A \right) + \frac{b}{(1 - c(1 - t) - \theta)h + bk} \left( \frac{1}{P} \right) M \] (3.11)

or

\[ Y = \frac{1}{(1 - c(1 - t) - \theta) + \frac{bk}{hk} \left( A \right) + \frac{b}{(1 - c(1 - t) - \theta) + bk} \left( \frac{1}{P} \right) M} \] (3.12)

while the Equilibrium interest rate is:

\[ r = \frac{k}{h} \left( \frac{1}{(1 - c(1 - t) - \theta) + \frac{bk}{hk} \left( A \right)} \right) + \frac{1}{h} \left( \frac{kb}{(1 - c(1 - t) - \theta)h + bk} - 1 \right) \left( \frac{1}{P} \right) M \] (3.13)
4. **The impact of Fiscal Policy and of the Monetary Policy**

We write again the equation 3.16 distinguishing which part affect the fiscal policy, and which one the monetary policy.

\[
Y = \frac{h}{(1-c(1-t)-\theta)h + bk} (\overline{A}) + \frac{b}{(1-c(1-t)-\theta)h + bk} (\overline{\frac{1}{P}}) \overline{M} \tag{3.14}
\]

The impact of an increasing in \(G\) is equal to:

\[
\frac{dY}{dG} = \frac{h}{(1-c(1-t)-\theta)h + bk} \tag{3.15}
\]

The impact of an increasing in \(M\) is equal to:

\[
\frac{dY}{dM} = \frac{b}{(1-c(1-t)-\theta)h + bk} \overline{\frac{1}{P}} \tag{3.16}
\]

4.1. **The Classic Hypothesis**

a.1) \(b \rightarrow \infty\)

The impact of an increasing in \(G\) is equal to:

\[
\frac{dY}{dG} = 0 \tag{3.17}
\]

The impact of an increasing in \(M\) is equal to:

\[
\frac{dY}{dM} = \frac{1}{k} \overline{\frac{1}{P}} \tag{3.18}
\]

a.2) \(h = 0\)
The impact of an increasing in $\bar{G}$ is equal to:

$$\frac{dY}{d\bar{G}} = 0 \quad (3.19)$$

The impact of an increasing in $\bar{M}$ is equal to:

$$\frac{dY}{d\bar{M}} = \frac{1}{k \bar{P}} \quad (3.20)$$

4.2. The Keynesian Hypothesis

b.1) $b = 0$

The impact of an increasing in $\bar{G}$ is equal to:

$$\frac{dY}{d\bar{G}} = \frac{1}{(1 - c(1 - t) - \theta)} \quad (3.21)$$

The impact of an increasing in $\bar{M}$ is equal to:

$$\frac{dY}{d\bar{M}} = 0 \quad (3.22)$$

b.2) $h \to \infty$

The impact of an increasing in $\bar{G}$ is equal to:

$$\frac{dY}{d\bar{G}} = \frac{1}{(1 - c(1 - t) - \theta)} \quad (3.23)$$

The impact of an increasing in $\bar{M}$ is equal to:

$$\frac{dY}{d\bar{M}} = 0 \quad (3.24)$$
MACRO MODELS
AN APP FOR MACROECONOMIC MODELS.
USER MANUAL 2.0

I↓→(Y↓; BS↓)

\[
\begin{align*}
\text{Aim : } Y \uparrow & \quad \{ [1.1.1](G \uparrow) \rightarrow (Y \uparrow; C \uparrow; r \uparrow; I \downarrow; BS \downarrow) \} \\
\text{FP} & \quad \{ [1.1.2](TR \uparrow) \rightarrow (YD \uparrow; C \uparrow; Y \uparrow; r \uparrow; I \downarrow; BS \downarrow) \} \\
\text{s. policy} & \quad \{ [1.1.3](t \downarrow) \rightarrow (YD \uparrow; C \uparrow; r \downarrow; I \uparrow; Y \uparrow; BS \downarrow) \} \\
\end{align*}
\]

\[
\begin{align*}
\text{Monetary policy} & \quad \{ \{ [1.2.1](G \uparrow TR \downarrow) \rightarrow (Y \uparrow; C \uparrow; BS =) \} \} \\
\text{policy − mix} & \quad \{ \{ [1.2.2](G \downarrow TR \uparrow) \rightarrow (Y \uparrow; C \uparrow; BS =) \} \} \\
\end{align*}
\]

\[
\begin{align*}
\text{FP + MP} & \quad \{ (G \uparrow; M^s \uparrow) \rightarrow (Y \uparrow; C \uparrow; r =; I =; BS \uparrow) \} \\
\end{align*}
\]

\[
\begin{align*}
\text{Aim : } BS \uparrow & \quad \{ [3.1.1](G \downarrow) \rightarrow (BS \uparrow; Y \downarrow; C \downarrow) \} \\
\text{single policy} & \quad \{ [3.1.2](TR \downarrow) \rightarrow (BS \uparrow; YD \downarrow; C \downarrow; Y \downarrow) \} \\
\text{FP} & \quad \{ [3.1.3](t \uparrow) \rightarrow (BS \uparrow; YD \downarrow; C \downarrow; Y \downarrow) \} \\
\end{align*}
\]

\[
\begin{align*}
\text{policy − mix} & \quad \{ [3.2.1](G \uparrow TR \downarrow) \rightarrow (BS \uparrow; YD \downarrow; C \downarrow; Y) \} \\
\text{MP} & \quad \{ (G \uparrow; M^s \uparrow) \rightarrow (Y \uparrow; C \uparrow; r =; I =; BS \uparrow) \} \\
\end{align*}
\]

\[
\begin{align*}
\text{FP + MP} & \quad \{ (G \downarrow; M^s \uparrow) \rightarrow (Y \uparrow; C \downarrow; r \downarrow; I \uparrow; BS \uparrow) \} \\
\end{align*}
\]
Figure 3.1: Case 3.1 Fiscal Policy : $G \uparrow$;
Figure 3.2: Case 3.2 Monetary Policy: $M \uparrow$
Figure 3.3: Case 3.3 Fiscal Policy + Monetary Policy: $G \uparrow$ (at $t_1$); $M \uparrow$ (at $t_2$)
Figure 3.4: Case 3.4 Fiscal Policy + Monetary Policy: $G \downarrow$ (at $t_1$); $M \uparrow$ (at $t_2$)
4.3. **Legenda of the IS-LM Model**

Legenda

*Table 3.1: Input Real Economy - Government*

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C$</td>
<td>Autonomous (exogenous) Consumption</td>
</tr>
<tr>
<td>$I_0$</td>
<td>Net Investment</td>
</tr>
<tr>
<td>$NX$</td>
<td>Net Export</td>
</tr>
<tr>
<td>$c$</td>
<td>Marginal Propensity To Consume</td>
</tr>
<tr>
<td>$d$</td>
<td>Marginal Propensity to Invest</td>
</tr>
<tr>
<td>$G$</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>TR</td>
<td>Net Government Transfers payments</td>
</tr>
<tr>
<td>$t$</td>
<td>Income tax rate</td>
</tr>
</tbody>
</table>
Table 3.2: Financial Market

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k$</td>
<td>Sensibility of money demand to income</td>
</tr>
<tr>
<td>$h$</td>
<td>Sensibility of money demand to interest rate</td>
</tr>
<tr>
<td>$P$</td>
<td>Prices level</td>
</tr>
<tr>
<td>$l_{ti}$</td>
<td>Liquidity trap interest rate</td>
</tr>
<tr>
<td>$M$</td>
<td>Money supply</td>
</tr>
</tbody>
</table>

Table 3.3: Output

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fisc Multiplier</td>
<td>Fiscal Multiplier</td>
</tr>
<tr>
<td>Mon Multiplier</td>
<td>Monetary Policy Multiplier</td>
</tr>
<tr>
<td>Eq. Income</td>
<td>Equilibrium Income</td>
</tr>
<tr>
<td>Eq. Consumption</td>
<td>Equilibrium Consumption</td>
</tr>
<tr>
<td>Eq. Investment</td>
<td>Equilibrium Investment</td>
</tr>
<tr>
<td>Balance</td>
<td>Government Surplus</td>
</tr>
<tr>
<td>Income</td>
<td>Income Variation</td>
</tr>
</tbody>
</table>
Table 3.4: Graph

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y</td>
<td>Income</td>
</tr>
<tr>
<td>C</td>
<td>Consumption</td>
</tr>
<tr>
<td>I</td>
<td>Net Investment</td>
</tr>
<tr>
<td>G</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>i_r</td>
<td>Interest rate</td>
</tr>
<tr>
<td>BS</td>
<td>Government Surplus</td>
</tr>
</tbody>
</table>
Chapter 4

The IS-MP model

1. The IS Curve

The real sector is given by the following system:

\[ Y = AD \]

\[ AD = C + I + G + NX \]

\[ C = c + cTR + c(1 - t)Y \]

\[ I = T - br + \theta Y \]

\[ G = G \]

\[ TR = TR \]

\[ NX = NX \]
In equilibrium the supply $Y$ is equal to the demand $AD$, $Y = AD$:

$$Y = \bar{C} + cTR + C(1-t)Y + \bar{I} + \theta Y - br + \bar{G} + NX$$  \hspace{1cm} (4.1)

or:

$$Y_e = \frac{1}{(1-c(1-t)-\theta)}[\bar{C} + \bar{G} + cTR + NX + \bar{I} - br]$$  \hspace{1cm} (4.2)

$$Y_e = \frac{1}{(1-c(1-t)-\theta)}[A - br]$$  \hspace{1cm} (4.3)

where

$$A = \bar{C} + \bar{G} + cTR + NX + \bar{I}$$  \hspace{1cm} (4.4)

\section{The Monetary Market: the Taylor’s rule}

Here we introduce the simply Taylor’s rule (Taylor, 1993) as in Romer (2006). It is based on two elements. Firstly, the nominal interest rate rise more than one-for-one with inflation. In other words, the real rate increases when inflation rises. Secondly, the interest rate rises (falls) when the output $Y_t$ is above (below) the normal level $Y^*$. In formulas;

$$i = a + \pi_t + \alpha_\pi \pi_t + \beta_y (Y_t - Y^*)$$  \hspace{1cm} (4.5)

with $\alpha_\pi > 0$ and $\beta_y > 0$.

$$i - \pi_t = a + \alpha_\pi \pi_t + \beta_y (Y_t - Y^*)$$  \hspace{1cm} (4.6)

Taking into account the Fisher’s equation

$$i = r + \pi_t$$  \hspace{1cm} (4.7)
or

\[ r = i - \pi_t \] (4.8)

It is possible to write the Curve MP (Monetary Policy):

\[ r = a + \alpha_\pi \pi_t + \beta_y (Y_t - Y^*) \] (4.9)

When \( Y_t = Y^* \), we obtain:

\[ r^* = a + \alpha_\pi \pi^* \] (4.10)

\[ \pi^* = \frac{r^* - a}{\alpha_\pi} \] (4.11)

\[ a = r^* - \alpha_\pi \pi^* \] (4.12)

\[ r = r^* - \alpha_\pi \pi^* + \alpha_\pi \pi_t + \beta_y (Y_t - Y^*) \] (4.13)

and finally:

\[ r = r^* + \alpha_\pi (\pi_t - \pi^*) + \beta_y (Y_t - Y^*) \] (4.14)

that can be written as:

\[ r = K + \beta_y (Y_t - Y^*) \] (4.15)

where:

\[ K = r^* + \alpha_\pi (\pi_t - \pi^*) \] (4.16)

The system to be solved is:
\[ Y = A + [c(1 - t) + \theta]Y - br \]  \hspace{1cm} (4.17)

\[ r = K + \beta_Y(Y_t - Y^*) \]  \hspace{1cm} (4.18)

The solution is:

\[ Y = A + [c(1 - t) + \theta]Y - b[K + \beta_Y(Y_t - Y^*)] \]  \hspace{1cm} (4.19)

\[ Y = A + [c(1 - t) + \theta - b\beta_Y]Y - bK + b\beta_Y Y^* \]  \hspace{1cm} (4.20)

\[ Y - [c(1 - t) + d - b\beta_Y]Y = A - bK + b\beta_Y Y^* \]  \hspace{1cm} (4.21)

The Equilibrium income is

\[ Y_e = \frac{1}{1 - c(1 - t) - d + b\beta_Y (A - bK + b\beta_Y Y^*)} \]  \hspace{1cm} (4.22)

The Equilibrium interest is:

\[ r_e = K + \beta_Y(Y_e - Y^*) \]  \hspace{1cm} (4.23)

or

\[ r_e = K + \beta_Y \left( \frac{1}{1 - c(1 - t) - \theta + b\beta_Y} (A - bK + b\beta_Y Y^*) - Y^* \right) \]  \hspace{1cm} (4.24)

The Fiscal Multiplier is:

\[ \frac{1}{1 - c(1 - t) - \theta + b\beta_Y} \]  \hspace{1cm} (4.25)

The Monetary Multiplier is:
\[ \frac{-c}{1 - c(1 - t) - \theta + b\beta Y} \] (4.26)

Equilibrium Consumption:

\[ C_e = \bar{C} + cY_e \] (4.27)

Equilibrium Investment:

\[ I_e = \bar{I} + \theta Y_e - b\beta_e \] (4.28)

Here is a graphic example.
Figure 4.1: Case 3.1 Fiscal Policy: $G \uparrow$

(a) IS-MP static

(b) IS-MP dynamics
2.1. **Legenda of the IS-MP Model**

Legenda

**Table 4.1: Input Real Economy - Government**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\bar{C}$</td>
<td>Autonomous (exogenous) Consumption</td>
</tr>
<tr>
<td>$I_0$</td>
<td>Net Investment</td>
</tr>
<tr>
<td>$NX$</td>
<td>Net Export</td>
</tr>
<tr>
<td>$c$</td>
<td>Marginal Propensity To Consume</td>
</tr>
<tr>
<td>$d$</td>
<td>Marginal Propensity to Invest</td>
</tr>
<tr>
<td>$G$</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>TR</td>
<td>Net Government Transfers payments</td>
</tr>
<tr>
<td>$t$</td>
<td>Income tax rate</td>
</tr>
</tbody>
</table>
### Table 4.2: Money Market - Central Bank

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>Nominal Interest Rate</td>
</tr>
<tr>
<td>$r^*$</td>
<td>Long run or equilibrium real interest rate</td>
</tr>
<tr>
<td>$\pi^*$</td>
<td>Central Bank's inflation objective</td>
</tr>
<tr>
<td>$\pi$</td>
<td>Current period inflation rate</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Weight concerning income gap</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Weight concerning inflation gap</td>
</tr>
</tbody>
</table>

### Table 4.3: Output

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fisc Multiplier</td>
<td>Fiscal Multiplier</td>
</tr>
<tr>
<td>Mon Multiplier</td>
<td>Monetary Policy Multiplier</td>
</tr>
<tr>
<td>Eq. Income</td>
<td>Equilibrium Income</td>
</tr>
<tr>
<td>Eq. Consumption</td>
<td>Equilibrium Consumption</td>
</tr>
<tr>
<td>Eq. Investment</td>
<td>Equilibrium Investment</td>
</tr>
<tr>
<td>Balance</td>
<td>Government Surplus</td>
</tr>
<tr>
<td>Income</td>
<td>Income Variation</td>
</tr>
</tbody>
</table>
### Table 4.4: Graph

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable / Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y</td>
<td>Income</td>
</tr>
<tr>
<td>C</td>
<td>Consumption</td>
</tr>
<tr>
<td>I</td>
<td>Net Investment</td>
</tr>
<tr>
<td>G</td>
<td>Government purchase of goods and services</td>
</tr>
<tr>
<td>R</td>
<td>Interest rate</td>
</tr>
<tr>
<td>BS</td>
<td>Government Surplus</td>
</tr>
</tbody>
</table>
Bibliography


