Endowment Effects in Contests

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2011
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January 31, 2011

Abstract
We experimentally study overbidding in contests and find that overbidding is significantly higher when subjects are given a large per-experiment endowment rather than when the endowment is given per-period. Risk-aversion and non-monetary utility of winning can partially explain our findings.

JEL Classifications: C72, C91, D72
Keywords: rent-seeking, contest, experiments, overbidding, endowment

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We want to thank Tim Cason, Will Masters, as well as seminar participants at Purdue University and participants at the June 2009 Economic Science Association meeting for helpful comments. This research has been supported by National Science Foundation Grant. Any remaining errors are ours.
1. Introduction

Contests are games in which players compete in order to win a prize. It is well documented in experimental contest literature that subjects overbid relative to Nash equilibrium predictions and thus they incur substantial losses (Morgan et al., forthcoming; Sheremeta, forthcoming). A number of studies have tried to identify means by which overbidding can be reduced. To date, researchers have found that overbidding decreases with the repetition of the contest (Davis and Reilly, 1998), groups make lower bids than individuals (Sheremeta and Zhang, 2010), and constraining individual endowments reduces overbidding (Sheremeta, forthcoming). This last study suggests that a portion of overbidding can be attributed to the size of the endowment i.e., endowment effects.

The purpose of this paper is to study the amount of overbidding in contests when the endowment is given at the beginning of each contest (per-period) versus a single equivalent endowment given at the beginning of the sequence of contests (per-experiment). We find that overbidding is significantly higher when subjects are given the large per-experiment endowment than when the endowment is given per-period. Risk-aversion and non-monetary utility of winning play important roles in explaining our findings.

2. Theoretical Model

We consider a lottery contest with $N$ identical risk-neutral players with initial endowment levels $W$. Player $i$ chooses his bid, $b_i$, to win the prize of value $V$. The probability that a player $i$ wins the prize, $p_i(b_i, b_{-i})$, is given by the lottery contest success function:

$$p_i(b_i, b_{-i}) = b_i / \sum_j b_j. \quad (1)$$
That is, the probability of winning depends on player $i$’s own bid relative to the sum of all player’s bids. Given (1), the expected payoff for player $i$, $E(\pi_i)$, can be written as

$$E(\pi_i) = p_i(W + V - b_i) + (1 - p_i)(W - b_i) = p_iV - b_i + W.$$  

(2)

Differentiating (2) with respect to $b_i$ and accounting for the symmetric Nash equilibrium leads to the classic solution (Tullock, 1980),

$$b^* = V(N - 1)/N^2.$$  

(3)

3. Experimental Design and Procedures

Two commonly used protocols in experimental studies of contests are per-experiment and per-period endowments. We refer to the “per-experiment” protocol as “E” and the “per-period” as “P”. The E protocol has been used by Davis and Reilly (1998), Barut et al. (2002), Gneezy and Smorodinsky (2006), and Noussair and Jonathon (2006). In these studies, each subject receives a large participation fee, announced at the beginning of the experiment. This participation fee can be used to pay off any losses incurred during the series of contests. The P protocol has been used by Potters et al. (1998), Anderson and Stafford (2003), Morgan et al. (forthcoming), and Sheremeta and Zhang (2010). Under the P protocol, each subject receives a small per-period endowment which can be used to make bids in that period of the experiment. At the beginning of the next period, subjects receive a new endowment and bidding again occurs. No endowment from the previous period is allowed to be carried over.

In each treatment of our experiment, there are 4 players ($N = 4$) competing with each other for the prize which is valued at 120 experimental francs ($V = 120$). From (2) and (3), we see that the equilibrium bid is 22.5 and the expected payoff is 7.5. In the E treatment, subjects receive a show up fee of $10 (equivalent to 600 francs) to play a contest for 30 periods, 5 of
which are randomly selected for payment at the end of the experiment. In the P treatment, instead of a show up fee, subjects receive a per-period endowment of 120 francs to play a contest for 30 periods. Again, 5 out of the thirty periods are randomly selected for payment at the end of the experiment. An important aspect of the design is the equivalence of the two endowment types. Although we cannot rule out any perceived differences the subjects may have about the E and P endowments, we can argue that the two endowments are quantitatively similar. For example, a subject who chooses to make no bids earns the same under the two endowments. Additionally, there are no theoretical differences between the two treatments since the endowment does not enter the equilibrium bid (3). Consequentially, there is no reason \textit{a-priori} that the subject’s bidding behavior would vary across the two treatments.

The experiment involved 96 undergraduate subjects from Purdue University. The computerized experimental sessions were run using z-Tree (Fischbacher, 2007). We ran 4 sessions of the E treatment and 4 sessions of the P treatment. In each session, there were a total of 12 subjects and the session proceeded in three parts. Instructions were given to subjects at the beginning of each part and the experimenter read the instructions aloud.\footnote{Instructions are available upon request.}

In the first part, subjects made 15 choices in simple lotteries, similar to Holt and Laury (2002).\footnote{Subjects were asked to state whether they preferred safe option A or risky option B. Option A yielded $1 payoff with certainty, while option B yielded a payoff of either $3 or $0. The probability of receiving $3 or $0 varied across all 15 lotteries. The first lottery offered a 0\% chance of winning $3 and a 100\% chance of winning $0, while the last lottery offered a 70\% chance of winning $3 and a 30\% chance of winning $0.} This method was used to elicit subjects’ risk preferences. In the second part, subjects participated in a total of 30 periods of the bidding contest. At the beginning of each period, subjects were randomly re-grouped to form a 4-player group. Subjects were then allowed to make bids between 0 and 120 for a prize of 120 francs. After all subjects submitted their bids, the computer chose the winner by implementing a simple lottery rule: the chance of receiving the
prize is calculated by the number of francs a subject bids divided by the total number of francs all 4 subjects in the group bid. In the third part of the experiment, subjects were asked to bid for a prize with a value of zero francs. Subjects were told that they would be informed whether they won the contest or not and that all subjects would have to pay their bids. This procedure was used to measure how important it is for subjects to win when winning is costly and there is no monetary reward for winning.

At the conclusion of the experiment, 1 of the 15 lottery choices subjects made in part one was randomly selected for payment. Subjects were also paid for 5 of the 30 periods in part two and for the 1 decision they made in part three. The earnings were converted into US dollars at the rate of 60 francs to $1. Average earnings were $12 per subject and the experiment lasted for about 40 minutes.

4. Results

Table 1 summarizes average bids and payoffs. Overall, subjects in both treatments significantly overbid relative to the risk-neutral Nash equilibrium prediction (for both treatments p-value < 0.01). The difference is also significant when we run Wilcoxon signed-rank tests for the bids made in the first period (p-value < 0.01). As a result of significant overbidding, average payoffs are negative. In the E treatment subjects receive the average payoff of -12.8 and in the P treatment they receive -22.2.

It is often argued that subjects need to get some experience in order to learn how to play the equilibrium. For that reason, Figure 1 displays the average bid over all 30 periods of the

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3 We ran a random effects model on a constant and session dummy-variables separately for each treatment. Then we tested whether the constant coefficients are equal to the predicted theoretical values as in Table 1. We found that these differences are significant for both treatments (p-value < 0.01).
experiment. As players become more experienced, the average bids in both treatments decrease. The declining trend over the periods in each treatment is significant based on the estimation of a random effects model (p-value < 0.01), where the dependent variable is a bid and the independent variable is an inverse of a period trend. Nevertheless, even in the last period of the experiment subjects overbid relative to the Nash equilibrium.

Table 1: Average Bid and Payoff

<table>
<thead>
<tr>
<th>Treatment</th>
<th>Treatment P</th>
<th>Treatment E</th>
<th>Equilibrium</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average Bid</td>
<td>42.8 (0.87)</td>
<td>52.2 (0.97)</td>
<td>22.5</td>
</tr>
<tr>
<td>Average Payoff</td>
<td>-12.8 (1.37)</td>
<td>-22.2 (1.38)</td>
<td>7.5</td>
</tr>
</tbody>
</table>

Standard error of the mean in parentheses

Figure 1: Average Bid over Periods

The presence of overbidding in numerous experimental studies, including our own, suggests that winning may be a component in a subject’s utility (Sheremeta, 2010). In our experiment, at the end of each session we presented subjects with a trivial task similar to the thirty periods of bidding that they have completed in E and P treatments. The only difference is that now the prize was valued at zero francs. Again, subjects were explicitly told that they would
have to pay their bids. Almost 50% of all subjects made positive bids, with 20% of subjects making bids higher than 30 francs (30 francs is equivalent to $0.5). This finding suggests that a non-monetary value of winning may significantly contribute to overbidding in our experiment.

The focus of this study is to determine if individual behavior is similar under the two theoretically-equivalent protocols commonly used in the literature. Table 1 indicates that subjects bid 22% more in the E treatment than in the P treatment (52.2 versus 42.8). This difference is significant based on the estimation of a random effects model, where the dependent variable is the bid and the independent variables are a period trend, session and treatment dummy-variables ($p$-value = 0.03). Moreover, the average bids in the E treatment are higher than the average bids in the P treatment over all periods of the experiment. The difference is marginally significant in the first 15 periods ($p$-value = 0.08) and it is significant in the last 15 periods ($p$-value = 0.02) of the experiment.

One possible explanation of the treatment differences is due to loss aversion theory (Kahneman and Tversky, 1979). Nevertheless, it is unlikely that loss aversion can explain treatment differences because, relative to the initial endowment, subjects’ decisions have identical consequences for gains and losses in both treatments. Additionally, the quantal response equilibrium model, designed to capture individual mistakes, is also unlikely to explain our results because in both treatments the strategy space is between 0 and 120 and therefore predictions for both treatments are exactly the same (Sheremeta, forthcoming).

Another possible explanation may be risk preferences. Table 2 reports the estimation results of four random effects models, where the dependent variable is the subject’s bid and the independent variables are period, risk-aversion, and non-monetary variables. All regressions
and also include dummy-variables to capture session effects (not shown in the table) and lagged variables to capture the dynamic nature of the experiment.

### Table 2: Determinants of Bid

<table>
<thead>
<tr>
<th>Dependent variable, bid</th>
<th>Treatment</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>P</td>
<td>E</td>
</tr>
<tr>
<td><strong>Specification</strong></td>
<td></td>
<td>(1)</td>
<td>(2)</td>
</tr>
<tr>
<td>period</td>
<td></td>
<td>-0.19*</td>
<td>-0.37**</td>
</tr>
<tr>
<td>[period trend]</td>
<td></td>
<td>(0.08)</td>
<td>(0.10)</td>
</tr>
<tr>
<td>risk-aversion</td>
<td></td>
<td>-0.91**</td>
<td>-0.22</td>
</tr>
<tr>
<td>[number of safe options A]</td>
<td></td>
<td>(0.33)</td>
<td>(0.44)</td>
</tr>
<tr>
<td>non-monetary</td>
<td></td>
<td>0.20**</td>
<td>0.11**</td>
</tr>
<tr>
<td>[bid in a contest with a prize of value zero]</td>
<td></td>
<td>(0.03)</td>
<td>(0.02)</td>
</tr>
<tr>
<td>bid-lag</td>
<td></td>
<td>0.61**</td>
<td>0.56**</td>
</tr>
<tr>
<td>[bid in period t-1]</td>
<td></td>
<td>(0.03)</td>
<td>(0.03)</td>
</tr>
<tr>
<td>win-lag</td>
<td></td>
<td>1.68</td>
<td>1.92</td>
</tr>
<tr>
<td>[1 if win in t-1]</td>
<td></td>
<td>(1.62)</td>
<td>(1.77)</td>
</tr>
<tr>
<td>otherbid-lag</td>
<td></td>
<td>0.01</td>
<td>-0.01</td>
</tr>
<tr>
<td>[sum of opponents' bids in period t-1]</td>
<td></td>
<td>(0.01)</td>
<td>(0.01)</td>
</tr>
<tr>
<td>Observations</td>
<td></td>
<td>1392</td>
<td>1392</td>
</tr>
</tbody>
</table>

* significant at 5%, ** significant at 1%.

Random effect models account for individual characteristics of subjects. In each regression we include dummy-variables to control for session effects.

The *risk-aversion* variable is defined as the number of safe options chosen by a subject in part one of the experiment (for the details see footnote 2). A higher number corresponds to more risk-aversion. Specifications (1) and (3) indicate that risk-aversion elicited from lotteries has significant negative influence on bidding behavior of subjects in the P treatment. On the other hand, risk-aversion does not have a significant effect on bidding behavior in the E treatment (specifications 2 and 4). One possible explanation of why risk-aversion seems to be important only in the P treatment is that subjects may perceive the endowment of 600 francs in the E treatment as a level of initial wealth. If this is the case, subjects with a high level of initial wealth may feel more inclined to disregard risks in the P treatment, and thus such subjects may be more inclined to overbidding in contests (Hillman and Katz, 1984). This explanation is
consistent with Thaler and Johnson (1990), who document that after a prior gain, such as a large endowment, people behave as less risk-averse which leads to more aggressive bidding behavior.

The non-monetary variable is defined as the amount of bidding in a contest with the prize valued at zero. The results indicate a significant and positive correlation between a subject’s bid and the non-monetary variable, suggesting that winning is a component in a subject’s utility and that non-monetary utility of winning is an important factor which may explain overbidding in contests.

5. Conclusions

Beyond the obvious benefit of understanding human behavior this study contributes to our understanding of several economic phenomena. A common topic in the finance literature is the concept of the Free Cash Flow Hypothesis (FCFH). Although the root problem in the FCFH is the misalignment of incentives in the principle-agent relationship, our research also shows that having a large reserve of “free cash” within a corporation may precipitate the wasteful use of resources (Jensen, 1986). Our study also yields important results for experimental methodology. Merlo and Schotter (1999) find that the manner in which subjects are paid may have an impact on what they choose to learn from the experiment. Similarly, our results have potential consequences for experimental methodology since they indicate that the manner in which subjects receive their endowments may have an impact on their decisions.
References


