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Abstract

The flexible price monetary model assumes that both the purchasing power parity (PPP) and uncovered interest parity (UIP) hold continuously. In addition, the model posits that money market equilibrium exists, which helps to determine the exchange rate. This paper explores exchange rate determination in low-income economies by applying a monetary model to Kenya to examine the exchange rate dynamics in a post-float exchange rate regime. We apply a multivariate cointegration and error correction model (ECM) to investigate whether the long-run exchange rate equilibrium and the rate of adjustment to the long-run equilibrium hold, respectively. Finally, we evaluate the relative performance of ECM versus a random walk framework in the out-of-sample forecasting. We find that the random walk performs better than the restricted model.

Key words: Exchange rate, volatility, regime changes and Kenyan Shilling

JEL classification: C32, C53, E58, F31

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The flexible price monetary model assumes that both the purchasing power parity (PPP) and uncovered interest parity (UIP) hold continuously. In addition, the model posits that money market equilibrium exists, which helps to determine the exchange rate. This paper explores exchange rate determination in low-income economies by applying a monetary model to Kenya to examine the exchange rate dynamics in a post-float exchange rate regime. We apply a multivariate cointegration and error correction model (ECM) to investigate whether the long-run exchange rate equilibrium and the rate of adjustment to the long-run equilibrium hold, respectively. Finally, we evaluate the relative performance of ECM versus a random walk framework in the out-of-sample forecasting. We find that the random walk performs better than the restricted model.

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1.0 INTRODUCTION

In the analysis of financial markets, the foreign exchange market is arguably the largest market in the world. This explains the vast interest and literature in analyzing the determinants, trends and forecasting of the exchange rate series. Generally, exchange rates play an important role in the global economy in determining relative prices of goods and services and relative prices of assets in different countries. Further, under the flexible exchange rate regime, the exchange rate can be influenced, and consequently it has influence on trade account balances and capital account balances. In many theoretical models of open macroeconomics the exchange rate is regarded as one of the endogenous variables of a large macroeconomic system and as an asset price in international finance. The former implies that the exchange rate is a slow-moving variable similar to consumption, investment and prices of goods and services, while the latter implies that it is a fast-moving variable just like stock prices. Hence, for small open economies the mismatch of the speeds of adjustment can be exploited to produce a result such as the overshooting model by Dornbusch (1976).

Over the years, attempts to produce a valid long-run equilibrium relationship, also referred to as purchasing power parity (PPP), as implied by the monetary model, have generally met with mixed success - particularly when the implicit restrictions of the model are applied. For instance, Meese (1986) and McNown and Wallace (1989) fail to find a valid long-run relationship for the conventional monetary model. However, Macdonald and Taylor (1993) report that the flexible price monetary model appears to hold as a long-run equilibrium condition in explaining the Deutsche-mark and the US dollar exchange rate from 1976-1990.¹. Similarly, the mixed results found when

analyzing PPP under the Balassa–Samuelson effects for small open economies can be explained by several factors. First, growth in these economies may be propelled by factor accumulations rather than productivity growth.² Second, the productivity growth may have been more uniform across tradables and non-tradables, while relative prices between these two may have stayed relatively constant in some of the developing economies. This implies that the PPP for tradables, an assumption central to the Balassa-Samuelson model, may have been violated. Even prices of tradables may rise in comparison with the industrialized countries because the compositions of tradables may quickly shift to more value-added and high-quality products, while adjustments for compositional or quality changes are not reflected in the data. Third, ambiguity in making clear-cut distinction between tradables and non-tradables exists. For instance, commonly assigning services and construction to non-tradables may not be right for service-oriented economies in some countries. Finally, foreign exchange restrictions may be loosened over the sample period, so that the artificial overvaluation may be corrected over time. This means that PPP may not hold if there is no controlling for any structural break in the time series.

Although the monetary model was the first approach applied in explaining the related phenomenon of exchange rate variations, its application is mostly confined to analyzing industrialized countries, whereas applications in emerging and low-income economies are limited. This paper is aimed at testing robustness of the monetary model for a small open economy by applying it to Kenya over 1990-2006, the period after it liberalized its exchange rate.

The rest of the paper is structured as follows: section II gives an overview of the flexible price model, data and estimation methodology. Section III discusses the empirical results, followed by the conclusion in section IV.

2.0 METHODOLOGY

The monetary approach to exchange rate is based on two foundations: the quantity theory of demand for money (QTM) and the PPP relationships. The QTM posits that the demand for real balances is a stable function of only a few variables in the domestic economy. Thus any change in the nominal money stock will have a direct effect on the price levels, because velocity of circulation and output are assumed to be constant (a doubling of the nominal money stock will result in doubling of the price level at any given real income). On the other hand, the PPP relationship is often tested as a theory to determine the exchange rate dynamics. In its absolute version, PPP implies that the equilibrium exchange rate equals the ratio of domestic to foreign prices. On the other hand, the relative version of PPP relates changes in the exchange rate to changes in the price ratios. Slow convergence to the PPP relationship is often called the "PPP puzzle". The standard money demand function can be specified as

$$m_t = p_t + \alpha y_t - \beta i_t \tag{1}$$

where m is the nominal demand for money, p is the domestic price level, y is the real income level and i is the nominal rate of interest. All variables, except the interest rate, are in logarithms. Foreign money demands are given by

$$m_{t}^{*} = p_{t}^{*} + \alpha y_{t}^{*} - \beta i_{t}^{*}$$
⁽²⁾

where * denotes foreign variable. It is assumed that absolute purchasing power parity (PPP) holds, so that

$$p_t = p_t^* + e_t \tag{3}$$

where e is the log of the nominal exchange rate. PPP is used only as a long-run equilibrium condition in this model; in the short run the error correction model allows deviations from PPP. The evidence on PPP as a long-run equilibrium condition is generally positive (Culver and Papell, 1999).

Substituting and rearranging equations (1) - (3) yields

$$e_{t} = \alpha_{0} + \alpha_{1}(m_{t} - m_{t}^{*}) - \alpha_{2}(y_{t} - y_{t}^{*}) + \alpha_{3}(i_{t} - i_{t}^{*})$$
(4)

The monetary approach assumes that domestic and foreign bonds are perfect substitutes so that Uncovered Interest Parity (UIP) holds.

$$i_{t} = i_{t}^{*} + [E(e_{t+1} | I_{t}) - e_{t}]$$
(5)

where $E(e_{t+1} / I_t)$ is the rational expectation of the exchange rate one period ahead, conditional on the currently available information set, I_t . By denoting the set of forcing variables as $Z_t = [\alpha_0 + \alpha_1(m_t - m_t^*) - \alpha_2(y_t - y_t^*)]$, substituting (5) into (4) and solving for the exchange rate yields

$$e_{t} = \frac{E\left(Z_{t+j} \middle| I_{t}\right)}{1+\alpha_{3}} + \frac{\alpha_{3}}{1+\alpha_{3}} E\left(e_{t+1} \middle| I_{t}\right)$$
(6)

Solving this equation by forward iteration gives

$$e_{t} = (1 + \alpha_{3})^{-1} \sum_{j=0}^{n} [\alpha_{3} / (1 + \alpha_{3})]^{j} E(Z_{t+j} | I_{t}) + \left(\frac{\alpha_{3}}{1 + \alpha_{3}}\right)^{n} E(e_{t+n} | I_{t})$$
(7)

Letting $j \to \infty$ (or assuming that the solution is free from arbitrary speculative bubbles) gives the forward-looking solution for the monetary exchange rate (FLME):³

$$e_{t} = (1 + \alpha_{3})^{-1} \sum_{j=0}^{\infty} \left[\alpha_{3} / (1 + \alpha_{3}) \right]^{j} E(Z_{t+j} | I_{t})$$
(8)

As outlined in Campbell and Shiller (1987) and Macdonald and Taylor (1993), the exchange rate should be cointegrated with the forcing variables Z_t . This is illustrated by subtracting Z_t from both sides of equation (7) to obtain

$$e_{t} - Z_{t} = -\frac{\alpha_{3}}{1 + \alpha_{3}} X_{t} + \frac{\alpha_{3}}{(1 + \alpha_{3})^{2}} E(X_{t+1} | I_{t}) + \frac{\alpha_{3}^{2}}{(1 + \alpha_{3})^{3}} E(X_{t+2} | I_{t}) + \dots \dots (9)$$

Rearranging into first differences (for all $j \rightarrow \infty$) yields

$$e_{t} - Z_{t} = \sum_{j=1}^{\infty} \left[\alpha_{3} / (1 + \alpha_{3}) \right]^{j} E(\Delta Z_{t+j} \mid I_{t})$$
(10)

Under rational expectations the forecasting errors are stationary; thus if the forcing variables in Z_t are I(1), then the right hand side of equation (10) must also be stationary. Consequently if e_t is also I(1), then the exchange rate must be cointegrated with the variables m_t, m_t^*, y_t and y_t^* .

Thus FLME is to test for cointegration between the exchange rate and the forcing variables.⁴ Hence the monetary approach to the exchange rate model to be estimated is given by:

$$e_{t} = \beta_{0} + \beta_{1}m_{t} + \beta_{2}m_{t}^{*} + \beta_{3}yt + \beta_{4}y_{t}^{*} + u_{t}$$
(11)

where u_t is a random error term and, $\beta_1 = -\beta_2$, $\beta_3 = -\beta_4$. A priori we expect that β_1 and $\beta_4 > 0$, β_2 and $\beta_3 < 0$.

According to the portfolio approach, the rise in wealth ought to facilitate an increase in the demand for money and a rise in the interest rate. In the process, higher interest rates should encourage more capital inflow, and increased demand for the domestic currency, which results in an appreciation of the domestic currency. To represent dynamic market adjustments, we can rewrite the equilibrium model of equation (11) as an error correction model (ECM):

$$\Delta e_{t} = b_{0} + b_{1} \Delta m_{t} + b_{2} \Delta m_{t}^{*} + b_{3} \Delta y_{t} + b_{4} \Delta y_{t}^{*} -\lambda [e_{t} - \beta_{1} m_{t} - \beta_{2} m_{t}^{*} - \beta_{3} y_{t} - \beta_{4} y_{t}^{*}]_{t-1} + v_{t}$$
(12)

where all terms must be stationary, that is, integrated of order zero I(0); v_t is a random error term with zero mean. Δ is the first difference operator, while the speed of adjustment is given by λ .⁵

3.0 EMPIRICAL RESULTS

The empirical estimation period is from June 1990 to December 2005 with monthly data extracted from *International Financial Statistics* (IFS) and the country's national accounts. The starting period was chosen to coincide with the time that Kenya adopted the flexible exchange rate regime. Real GDP is used as a proxy of income, while the narrow money (M1) is the proxy for changes in the monetary aggregates between U.S. and Kenya. Finally, nominal exchange rate of Kenyan Shilling (KSH) per U.S. dollar is utilized. All variables are expressed in their natural logarithms (denoted by lower case letters), and the estimated coefficients of the respective variables are the elasticities.

3.1 Unit Root Tests

To avoid spurious regression, we first conduct unit root tests on each variable to determine whether it is stationary or nonstationary. In carrying out the unit root tests, we consider a univariate autoregression for each series:

$$\Delta x_t = \mu + (\rho - 1)x_{t-1} + \sum_{i=1}^k \gamma_i \Delta x_{t-i} + e_t$$
(13)

where *x* is the log of the variables at time *t*. The regression above may also include a time trend as a way of capturing deterministic trends. To test for the existence of unit roots, we apply the augmented Dickey-Fuller (ADF) test, proposed by Dickey and Fuller (1979). The null hypothesis of the ADF test is $\rho = 1$. Lagged values of Δx_{t-i} will be added to remove serial correlation in the residuals. The resulting t-ratio of the estimated coefficients on x_{t-1} are the ADF statistics. The unit root test is performed on both levels and first difference of the variables.

Another test is the Phillips-Perron (PP) test proposed by Phillips and Perron (1988):

$$x_t = \alpha_0 + \alpha x_{t-1} + e_t \tag{14}$$

The difference between these two approaches lies in their treatment of "nuisance" serial correlation. The PP tends to be more robust to a wide range of serial correlation and time-dependent heretoskedasticity. In these tests, the null hypothesis of non-stationarity (presence of unit root) for ADF and PP are given by $\rho = 0$ and $\alpha = 1$ respectively. Rejection of the null implies stationarity of the series. The unit roots test results in levels and first differences are presented in table 1. The results show that we fail to reject the null hypothesis that the nominal exchange in levels is non-stationary for all the countries.

However, the null is rejected for the first difference. This implies that the series are integrated of order one I(1).

<TABLE 1 ABOUT HERE>

3.2 Cointegration Analysis

If a system (set) of the series is found to be cointegrated, they are linked together through a long-run relationship that prevents them from diverging. In a cointegration test involving three or more variables, we apply the maximum likelihood method suggested by Johansen (1988, 1991) and Johansen and Juselius (1990). It is based on a vector error-correction model of the form:

$$\Delta X_{t} = \mu + \Pi X_{t-k} + \sum_{i=1}^{k-1} \Gamma_{i} \Delta X_{t-i} + e_{t}$$
(15)

where X_t is a (m x 1) vector of exchange rates. The parameter matrix Π contains information as to whether there is a long-run relationship among variables. The rank of Π equals the number of cointegration vectors. If the rank of the matrix Π is zero, the system reduces to a standard vector autoregression model, implying no long-run relationship among variables. If Π has a full rank, then all the variables are stationary. Cointegration is implied when the rank of Π is intermediate. That is, if $0 < \operatorname{rank}(\Pi) < m$, there exists *r* cointegrating vectors which make the linear combination of X_t stationary. To test the rank of Π , Johansen and Juselius make use of maximum eigenvalue and trace statistics.

3.3 Estimated Results

The existence of long-run cointegrating vectors was tested using Johansen's Maximum Likelihood Procedure (see, for example, Johansen 1988; Johansen and Juselius 1990). The Johansen cointegration test is sensitive to the choice of lag length. To determine the most appropriate lag length, the Akaike Information Criteria (AIC) was used. In addition, the residuals in the Johansen VAR were checked for misspecification. To capture any serial correlation, extra lags were added until this was removed. According to Gonzalo (1994), the costs of over-parameterization in terms of efficiency loss is marginal, but this is not the case in the event of under-parameterization. Further, when testing for cointegration, the question of whether a trend should be included in the long-run relationship arises. As Hendry and Doornik (1994) pointed out, the trend is restricted to the cointegrating space, to take into account long-run exogenous growth which is not already included in the model.

<TABLE 2 ABOUT HERE>

The results for the cointegration test on the unrestricted model are presented in table 2. Based on AIC, a lag length of 6 was chosen. The maximum eigenvalue test statistic reveals one significant cointegrating relationship, whereas the trace statistic suggests there are two cointegrating vectors. This indicates the presence of one cointegrating relationship based on the evidence of the stronger maximum eigenvalue test (Johansen and Juselius, 1990). The results for the normalized equation are reported in table 3.

<TABLE 3 ABOUT HERE>

The results of the unrestricted error correction model are included in table 4. The residuals from the cointegrating vector, with one lag, act as the error correction term. This term captures the disequilibrium adjustment of each variable towards its long-run value. The coefficient on the error correction terms in each individual equation represents the speed of adjustment of this variable back to its long-run value. A significant error correction term implies long-run causality from the explanatory variables to the dependent variables (Granger, 1988).⁶

<TABLE 4 ABOUT HERE>

In Table 4 the first statistic represents the sum of the coefficients on the lagged differences of the variables. The second statistic (in the brackets)⁷ is a chi-square statistic indicating the significance levels of the sum of the coefficients. This can be interpreted as capturing the short-run dynamics in the model and indicates short-run causality between the variables.

For the exchange rate equation, there is evidence of short-run causality from the Kenyan and U.S. money supply to the exchange rate, as well as short-run causality from Kenyan income to the exchange rate. For money supply equations there is less evidence of short-run causality, particularly running from the exchange rate to money supply. This indicates that causality predominantly runs from money supply to the exchange rates. The explanation for this phenomenon is observed when one takes into consideration the impact of changes in money supply on the interest rate; that is, an increase in money

supply will lead to a decline in the interest rate. This will result in depreciation of the KSH due to capital flight.

The error correction results for the restricted model are included in Table 5. Once again the error correction term is only significant for the money supply equation. As with the unrestricted model, there is some evidence of short-run causality from money supply to the exchange rate, but no evidence of causality in the other direction. The main feature of the money supply equation is the strong causality to the exchange rate differential from previous differentials. Both equations are well specified, although the explanatory power is low.

<TABLE 5 ABOUT HERE>

Finally, a further test of the monetary approach to exchange rate dynamics model is how well it forecasts out of sample. The exchange rate equation was estimated from June 1990 to December 2004, and 2005 was used for forecasting. Following the lead of other studies in the literature, the forecasting performance is compared to a random walk. In addition, both the restricted and unrestricted models are compared to the forecasting performance of the Frankel Real Interest Differential model.⁸ The root-mean-square error (RMSE) statistics from all four models are compared in Table 6. Ironically the worst performer is the unrestricted model, while the best is the restricted model. The Frankel model fails to beat the random walk over short time horizons, but over longer time horizons is the second best forecaster of the exchange rate. In addition, the significance of each of the measures of forecast accuracy is tested using the Diebold and Mariano (1995) procedure, in which the squared forecast error differential (model forecast minus the benchmark random walk forecast) is regressed on a constant. Only the restricted model and Frankel model produce forecasts that are significantly different from the benchmark random walk model.

<TABLE 6 ABOUT HERE>

4.0 CONCLUSION

This paper has examined the relationship between the money supply, income (output) and exchange rate by applying the monetary model of exchange rate determination. The results indicate that in equilibrium, this version of the monetary model produces a cointegrating vector, in which the money supply variable is the most significant determinant of the exchange rate in Kenya. The dynamic results produce well specified error correction models. However there is very little evidence that exchange rates have a significant effect on money supply (i.e. reverse causality).

These findings suggest that, in general, models of the equilibrium exchange rate determination must be extended to encompass both internal and external factors. This can help in monetary policy coordination, for instance, to avert a financial crisis triggered by speculative attack on a small open economy. Finally, the restrictions implicit in the monetary model of the exchange rate appear to hold over the post exchange rate float period. This finding is supported by the forecasting performance of the models, in which the restricted model outperforms all the alternatives over short and long time horizons. These results add to other recent studies which portray the monetary models generally in a more favorable light, although more research on the monetary class of exchange rate models is still required.

FOOTNOTE

¹ Chrystal and Macdonald (1995) find evidence of a valid long-run relationship using divisia money while Choudhry and Lawler (1997) find evidence of a long-run relationship for the restricted monetary model using Canadian/US data for the 1950s float.

² This possibility was pointed out by Young (1992).

³ An advantage of using the FLME, is that it produces a model in which stock prices are the explanatory variables along with income and money. If the conventional monetary model, with static expectations or Frankel real interest rate model had been used, both long and short interest rates would have been incorporated into the model, which could have produced problems of collinearity between the interest rates and stock price returns in the ECMs. In general, the conventional FLME (without stock prices) is not widely used because it usually fails to produce evidence of a valid long-run equilibrium relationship and it is not a good predictor of the exchange rate.

⁴ Testing for cointegration between the exchange rate and forcing variables is also a test for the presence of bubbles in the exchange rate. If cointegration is found and certain restrictions prove to hold, then the speculative bubble hypothesis is rejected. However, this line of investigation is beyond the scope of this paper. Assuming UIP means the interest rate differential equals the expected rate of depreciation. In the absence of arbitrary bubbles, the rate of expected appreciation is some function of expected movements in fundamentals, and so equation (8) must be true.

⁵ For values of λ close to unity, adjustment is very rapid, with the disequilibrium being totally eliminated within one period of time. For $0 < \lambda < 1$ the dynamic adjustment path will be monotonically convergent.

⁶ Given that the Johansen maximum Likelihood procedure is essentially a vector autoregression (VAR) based technique, it is more appropriate to produce the complete ECM rather than a parsimonious specification , in which the non-significant lags are omitted.

⁷ See notes in Table 4 for details.

⁸ The unrestricted Frankel real interest model did provide evidence of cointegration; however, the restrictions on the domestic and foreign explanatory variables were rejected, so the restricted version of this model was not estimated.

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Variables	ADF Tests, $ au(ho)$		PP test, $z(t_{\alpha})$	
	Levels	First diff.	Levels	First diff.
е	-1.23(2)	-3.44 (5)**	-0.97(4)	19.23(2)***
m1	-2.40(4)	-14.22 (2)***	-1.04(6)	20.01(5)***
m1*	-2.85(2)	-15.88(4)***	-0.18(3)	18.73(2)***
у	-1.80(3)	-11.57 (6)***	-0.77(2)	24.11(4)***
y*	-0.53(5)	-10.97 (4)***	-1.34(4)	15.42(2)***

Table 1: Unit Root Tests

Notes: The critical ADF and PP values are taken from Dickey and Fuller (1981) and Philips and Perron (1988) respectively. The regressions were done with a constant term only and the lag length is based on AIC are in parentheses, which are selected to eliminate serial correlations. Seasonal dummies were included to control for seasonal unit roots (not reported here, but available from the authors upon request). *** and ** indicate 1% and 5% significance levels, respectively.

	Unrestricted Model		Restricted Model		
Vectors	Trace Test	Eigenvalue Test	Trace Test	Eigenvalue Test	
r = 0	177.92**	50.52**	78.00**	46.01**	
$r \leq 1$	127.41**	43.31	31.98	16.92	
$r \leq 2$	84.09	30.47	15.07	9.75	
$r \leq 3$	53.63	22.51	5.32	5.32	
$r \leq 4$	31.11	16.36			
$r \leq 5$	14.75	9.80			
$r \le 6$	4.96	4.96			

 Table 2- Johansen Maximum Likelihood Test for Cointegration of the Unrestricted and Restricted Models

Notes: Critical values of Johansen's Trace and Eigenvalue tests at the 95% level of significance for the unrestricted model are: r = 0, 147.27 and 49.32. $r \le 1$, 115.85 and 43.61. $r \le 2$, 87.17 and 37.86. $r \le 3$, 63.00 and 31.79. $r \le 4$, 42.34 and 25.42. $r \le 5$, 25.77 and 19.22. $r \le 6$, 12.39 and 12.39 respectively. For the restricted model: r = 0, 63.00 and 31.79. $r \le 1$, 42.34 and 25.42. $r \le 2$, 25.77 and 19.22. $r \le 6$, 12.39 and 12.39 respectively. For the restricted model: r = 0, 63.00 and 31.79. $r \le 1$, 42.34 and 25.42. $r \le 2$, 25.77 and 19.22. $r \le 3$, 12.39 and 12.39. Both tests included seasonal dummy variables. ** indicates significance at the 5% level.

	Unrestricted Model			Restricted model	
Variable	Coefficient	Significance	Variable	Coefficient	Significance
е	-1.000	0.651	Δe	-1.000	0.237
ml	1.318	0.513	Δm	-1.015	1.117
ml^*	0.139	0.024	Δy	0.858	0.036
у	4.394	4.724**			
v*	-6.360	5.904**			
-					

Table 3- Normalized Equations of the Cointegrating Vectors

Notes: The significance of the coefficients were tested using the LM statistic which tests the restriction that the coefficient is equal to zero. $(\chi_{0.5}^2(1) = 3.841)$.

** indicates significance at the 5% level.

Table 4- Error Correction Model Results for the Unrestricted Mode

	ΔE	Δy	Δy^{*}
Constant	0.017 [0.305]	-0.126 [0.607]	0.481 [2.529]**
res _{t-1}	-0.004 [0.328]	0.035 [0.736]	-0.107 [2.452]**
$\sum \Delta e$	0.096 (0.619)	-0.090 (1.900)	-0.031 (0.938)
$\sum \Delta m 1$	0.084 (0.343)	1.022 (2.774)	1.581 (8.594)**
$\sum \Delta m 1^*$	0.187 (0.645)	-0.478 (0.030)	1.504 (0.191)
$\sum \Delta y$	-0.318 (3.994)**	1.161 (4.283)**	-0.001 (0.073)
$\sum \Delta y^*$	0.324 (1.274)	-1.606 (4.839)**	-1.082 (1.236)
R^2	0.687	0.706	0.813
SC(12)	1.658	2.022	0.827
SC(6)	1.417	1.019	1.021
Reset	0.077	0.232	1.573
Heteroskedasticity	0.522	0.204	0.122
ARCH(12)	0.482	0.155	0.989

Notes: res denotes the error correction term; R^2 is the coefficient of determination; DW is the Durbin-Watson statistic; SC(i) are the *i*th order tests for serial correlation; ARCH(i) is Engle's (1982) test for the *i*th autoregressive conditional heteroskedasticity. These test statistics follow the F-distribution. Critical values are: F(6,222) = 2.14, F(12,216) = 1.80, F(1,227) = 3.89. The values in brackets represent t-statistics. The values in parentheses represent Wald statistics, which follow a chi-square distribution with critical value 3.842. All equations include seasonal dummies.

** indicates significance at the 5% level.

	Δe	Δy
Constant	0.003 (0.705)	0.034 (4.112)**
res_{t-1}	-0.001 (0.678)	0.147 (4.921)**
$\sum \Delta e$	-0.075 (0.418)	-0.691 (1.208)
$\sum \Delta m$	0.073 (0.545)	0.035 (1.311)
$\sum \Delta y$	0.061 (0.064)	1.266 (0.253)
R^2	0.08	0.189
SC(12)	1.592	0.746
SC(6)	0.320	0.524
Reset	1.510	3.913
Heteroskedasticity	1.025	0.007
ARCH(12)	0.795	0.920

Table 5- Error Correction Model for the Restricted Model

Notes: See Table 4

Table 6- RMSE Statistics for Forecasts using the Competing models (ECM and Random Walk)

Models	3 Months	6 Months	9 Months	12 Months
Random Walk	0.010	0.017	0.017	0.016
Unrestricted Model	0.013	0.017	0.018	0.017
Restricted Model	0.009	0.016**	0.016**	0.015**
Frankel Model	0.011	0.016**	0.016**	0.015**

Notes: ** indicates a significant Diebold-Mariano test statistic at the 5% level. The test uses the standard Newey-West adjustment, with Bartlett weights and a lag window of 2.