On the winning virtuous strategies for ultra high frequency electronic trading in foreign currencies exchange markets

Dimitri O. Ledenyov and Viktor O. Ledenyov

James Cook University, Townsville, Australia

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Abstract – In the Schumpeterian creative disruption age, the authors firmly believe that an increasing application of electronic technologies in the finances opens a big number of new unlimited opportunities toward a new era of the ultra high frequency electronic trading in the foreign currencies exchange markets in the conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities. Going from the academic literature, we discuss the probability theory and the statistics theory application to accurately characterize the trends in the foreign currencies exchange rates dynamics in the short and long time periods. We consider the financial analysis methods, including the macroeconomic analysis, market microstructure analysis and order flow analysis, to forecast the volatility in the foreign currencies exchange rates dynamics in the short and long time periods. We discuss the application of the Stratanovich-Kalman-Bucy filtering algorithm in the Stratanovich–Kalman–Bucy filter and the particle filter to accurately estimate the time series and predict the trends in the foreign currencies exchange rates dynamics in the short and long time periods. We research the influence by discrete information absorption on the ultra high frequency electronic trading strategies creation and execution during the electronic trading in the foreign currencies exchange markets. We formulate the Ledenyov law on the limiting frequency (the cut-off frequency) for the ultra high frequency electronic trading in the foreign currencies exchange markets.

JEL: G1, G10, G12, G14, G15, G20, C40, C42, C82, D0, D82, E42, F3, F4, F31.

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Keywords: absorption of information, diffusion of information, transmission of information, information theory, ultra high frequency electronic trading, processing frequency, algorithmic trading, informed trading, noise trading, currencies exchange rate, vehicle currency, interest rate, retail aggregator, liquidity aggregator, interdealer trade orders flow direction, stop-loss order, bid-ask spreads, price discovery process, capital inflow, capital outflow, carry trade strategy, financial liquidity, foreign currencies exchange market microstructure, foreign currencies exchange rate dynamics, Wiener filtering theory, Stratanovich-Kalman-Bucy filtering algorithm, Stratanovich–Kalman–Bucy filter, particle filter, nonlinearities, Ledenyov law on limiting frequency for ultra high frequency electronic trading in foreign currencies exchange markets, econophysics, econometrics, global foreign exchange market, global capital market.
Introduction

Since the time, when the first financial transactions were completed in the financial markets in Joseph Penso de la Vega (1668, 1996), the investors have been thinking about the optimal solutions finding for the complex investments decision making problems, the foreign currencies exchange rates estimation problems, and the financial risks assessment problems in the finances in Bernoulli (1738, 1954), Bagehot (1873, 1897). The application of the financial mathematics in the theory of value and prices by Fisher (1892) led to more accurate assessment of various financial variables in the process of evolution of the money market in Bagehot (1873, 1897). The intensive development of the probability theory in the mathematics in De Laplace (1812), Bunyakovsky (1846), Chebyshev (1846, 1867, 1891), Markov (1890, 1899, 1900, 1906, 1907, 1908, 1910, 1911, 1912, 1913), encouraged the adaptation of more sophisticated mathematical techniques to evaluate the financial risks, forecast the foreign currencies exchange rates and predict the returns-on-investments in the finances, namely Bachelier (1900) proposed his original idea to estimate the valuable financial papers prices evolution with the help of the probability theory in the mathematics. The ingenious research ideas on the application of probability theory in finances have been further developed in Slutsky (1922a, b, 1925a, b, 1927a, 1937a, b). In addition, in the course of development of the theory of financial speculations in Bachelier (1900), it was understood that a possible characterization of the complex financial systems within the financial markets can be done much more accurately, considering the existing theoretical models in the physics, for example: the model on the Brownian motion of molecules at the heat transfer process in the solids in Bunyakovsky (1825) as well as the Brownian movement of small particles suspended in a stationary liquid demanded by the molecular-kinetic theory of heat in Einstein (1905, 1956), Einstein, Smolukhovsky (1936). Sometime later, the role of the Brownian motion in the random processes has been summarized in Brush (1968, 1977). Moreover, Shiryaev, Grossinho, Oliveira, Esquivel (editors) (2006) write: “A.N. Kolmogorov, in his own landmark work Über die analytischen Methoden in der Wahrscheinlichkeitsrechnung, Math. Annalen 104 (1931), pp.415-458, credits Bachelier with the first systematic study of stochastic processes in continuous time.” The research propositions in Bachelier (1900) have been further developed in the mathematical theory of the Wiener processes in Wiener (1923, 1930, 1949). At later date, aiming to surpass the critical limitations of classical theoretical models like the fractional Brownian motion, the multi-fractals have been introduced in the finances from the physics in Mandelbrot (1960, 1963a, b, 1965, 1965, 1967a, b, 1969, 1971, 1972, 1975a, b, 1977, 1982, 1997), Mandelbrot, Taylor (1967), Mandelbrot, van Ness (1968),

During the *capitalism evolution process* with the *continuous innovation* and the *creative disruption,* the *disruptive innovation* is frequently generated by the means of the *innovation breakthrough processes* in Schumpeter (1911, 1939, 1947). The multiple discoveries of the *innovative disruptive technological advancements* in the *information communication technologies* in Shannon (1948), Ledenyov D O, Ledenyov V O (2012e) have been introduced in the *Schumpeterian creative destruction age,* resulting in the appearance of the technological and scientific advancements toward the **ultra high frequency electronic trading in the foreign currencies exchange markets.** In this empirical research article, we would like to discuss comprehensively the modern theories and practices toward the *ultra high frequency electronic trading in the foreign exchange markets* at an influence by the *discrete information absorption processes* in the *diffusion – type financial systems* with the *induced nonlinearities,* using the econometrical and econophysical principles, theories and perspectives in Schumpeter (1906, 1933), Bowley (1924), Box, Jenkins (1970), Grangel, Newbold (1977), Van Horne (1984), Taylor S (1986), Tong (1986, 1990), Judge, Hill, Griffiths, Lee, Lutkepol (1988), Hardle (1990), Grangel, Teräsvirta (1993), Pesaran, Potter (1993), Banerjee, Dolado, Galbraith, Hendry (1993), Hamilton (1994), Karatzas, Shreve (1995), Campbell, Lo, MacKinlay (1997), Rogers, Talay (1997), Hayashi (2000), Durbin, Koopman (2000, 2002, 2012), Ilinski (2001), Greene (2003), Koop (2003), Davidson, MacKinnon (2004), Campbell, Lo, MacKinlay (1996). In the conditions of the *highly volatile dynamics* of the *global financial system* in Aliber (2002), we would like to focus specifically on the application of the *probability theory* in De Laplace (1812), Bunyakovsky (1846), Chebyshev (1846, 1867, 1891), Markov (1890, 1899, 1900, 1906, 1907, 1908, 1910, 1911, 1912, 1913), Kolmogorov (1938, 1985, 1986), Wiener (1949), Brush (1968, 1977), Shiryaev (1995), Ledenyov (2004) to analyze the *nonlinear financial systems dynamics,* aiming to predict the *trends in the foreign currencies exchange rates* at an influence by the *discrete information absorption processes* in the *diffusion – type financial systems* with the *induced nonlinearities.*

Researching the *international financial markets* in Grabbe (1991), we are particularly interested in the research results on the modern applications of the *optimal filtering and prediction algorithms* in the frames the *theory of optimal non-linear filtering of random functions* in Stratonovich (1959a, b, 1960 a, b), aiming to forecast the foreign exchange rates at the *ultra high frequency electronic trading in the foreign currencies exchange markets* at an influence by the *discrete information absorption processes* in the *diffusion – type financial systems* with the *induced nonlinearities.* The *Stratanovich – Kalman – Busy filtering algorithm* would be a main subject of our research interest, when attempting to solve the *foreign currencies*
Pursuing these research goals, we will apply the differential equations theory in Gikhman, Skorohod (1968), Sharkovsky, Maistrenko, Romanenko (1986), Protter (2005) with the purpose to accurately characterize the time-dependent random processes with the independent increments in Skorohod (1967), Ledenyov V O, Ledenyov O P, Ledenyov D O (2002) during the ultra high frequency electronic trading in the foreign currencies exchange markets at an influence by the discrete information absorption processes in the diffusion – type financial systems with the induced nonlinearities.

Let us begin the innovative advanced research by making a short introductory review on the subject of our research interest, following by both the thoughtful consideration on the modern technological trends in the ultra high frequency electronic trading in the foreign exchange markets, and the discussion on the possible impacts by the various information absorption processes on the ultra high frequency electronic trading strategy creation and execution in the foreign exchange markets at an influence in the diffusion – type financial systems with the induced nonlinearities. We would like to note that some additional attention would also be paid to the innovative research proposals, regarding the possible improvement of the existing electronic trading systems in the foreign exchange economics in DeGrauwe (editor) (2005). Thus, we would like to move forward by providing a few concise definitions on the electronic trading in the foreign exchange markets by various authors, aiming to clarify the term’s meaning from the scientific point of view.

Gençay, Gradojevic (2009) write: “The FX market can generally be described as decentralized and worldwide, but the actual trading is processed in the bookkeeping of particular markets, with the major ones being London, New York and Tokyo. Thus, the total trading activity of informed and uninformed traders is comprised of the geographic contributions of individual market centers. The hours of operation of the market centers are different, but they jointly contribute to the aggregate market trading activity. For instance, the London Stock Exchange (LSE) and the New York Stock Exchange (NYSE) are both open from 09:30 to 11:30 EST. In contrast, the lowest market presence outside weekends can be found during the lunch break at the Tokyo Stock Exchange (TSE), when it is night in North America and Europe.”
Gallardo, Heath (2009) continue to explain: “The development of electronic broking and trading systems represents one of the most significant catalysts of structural change in foreign exchange markets over the past decade or so.”

Heath, Whitelaw (June 2011) state: “The introduction of electronic broking to the foreign exchange market in the early 1990s signaled the start of a process of innovation that has driven significant change.” Heath, Whitelaw (June 2011) continue to write: “Electronic trading has been a significant factor behind a number of changes in the structure of the foreign exchange market and the way the market operates. These developments include improvements in the price discovery process, a concentration of activity among a relatively small number of large global banks, a blurring of the traditional activities of different market participants, a marked increase in the activity of non-bank participants and the emergence of new market segments.”

The research article will cover the following research topics:

1. Introduction.
2. The discussion on the probability theory and the statistics theory to accurately characterize the trends in the foreign currencies exchange rates dynamics at the electronic trading in the foreign currencies exchange markets over a selected time period.
3. The discussion on the financial analysis methods, including the macroeconomic analysis, market microstructure analysis and order flow analysis, to forecast the foreign currencies exchange rates dynamics during the electronic trading process in the foreign currencies exchange markets.
4. The discussion on the application of the Stratanovich-Kalman-Bucy filtering algorithm in the Stratanovich – Kalman – Bucy filter and the particle filter to accurately estimate the time series and predict the trends in the foreign currencies exchange rates dynamics during the electronic trading in the foreign currencies exchange markets.
5. The discussion on the influence by discrete information absorption on the ultra high frequency electronic trading strategies creation and execution during the electronic trading in the foreign currencies exchange markets in the diffusion-type financial system with the induced nonlinearities.
6. The discussion on the Ledenyov law on the limiting frequency (cut off frequency) for the ultra high frequency electronic trading in the foreign currencies exchange markets in conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities.
7. Concluding remarks.
Probability theory and statistics theory application to accurately characterize trends in foreign currencies exchange rates dynamics in foreign currencies exchange markets in short and long time periods

Let us begin our research on the various aspects of the electronic trading in the foreign currencies exchange markets at an influence by the nonlinear information absorption, diffusion and transmission processes by making a comprehensive historical overview on the subject of our research interest with a particular accent on the original contributions to the field of research.

Yamaguchi (2001) states: “An ET system is a facility that provides some or all of the following services:

1) electronic order routing (the delivery of orders from users to the execution system),
2) automated trade execution (the transformation of orders into trades), and
3) electronic dissemination of pre-trade (bid/offer quotes and depth) and post-trade information (transaction price and volume data).”

Yamaguchi (2001) explains: “Electronic systems are currently used to varying degrees for trading in the markets for foreign exchange and fixed income. Penetration differs between markets, between market segments, between instruments, between types of trading and between the various stages of the trading process. Moreover, the situation is changing rapidly; a dominant system can give way to another in as quickly as a few months. The main impact of ET so far relates to the inter-dealer (voice) broker, who is increasingly being replaced by electronic systems. This does not necessarily imply that brokerage firms are going out of business as they may reinvent themselves by offering an electronic service. Furthermore, electronic trading makes the direct dealing relationships redundant, i.e. the interaction in the inter-dealer market is becoming increasingly multilateral.”

Fig. 1 shows the interaction between the market participants prior to the electronic trading, and Fig. 2 depicts the interaction between the market participants after the introduction of electronic trading in Yamaguchi (2001).
Fig. 1. Interaction between market participants prior to electronic trading (after Yamaguchi (2001)).

Fig. 2. Interaction between market participants after introduction of electronic trading (after Yamaguchi (2001)).
Stoll (2006) explains: “The idea of electronic trading is not new. In 1971, Fischer Black suggested steps toward a fully automated exchange that would eliminate the need for specialists and market-makers. He noted that “a stock exchange can be embodied in a network of computers, and the costs of trading can be sharply reduced, without introducing any additional instability in stock prices, and without being unfair either to small investors or large investors” Black (1971, part II). He had in mind a world in which investors would interact with one another with little or no human intervention. That world is near, but Fischer Black (were he still alive) would be surprised at how long it has taken. The automation at ECNs has achieved what Fischer Black had in mind...”. Stoll (2006) lists the following ECN advantages: “ECNs have a number of advantages.

1) They are automatic. Once an order is submitted, trade execution proceeds without human intervention according to price/time priority, unlike traditional markets, where orders might be held by dealers.

2) They are anonymous. The identity of traders is not revealed, which can be of importance to certain traders.

3) They are low cost. ECNs earn income by charging a fee to market orders of about 3 cents per share, while they pay for orders that supply liquidity.

4) They are fast. Execution and confirmation are electronic and occur in less than a second.

5) They can be programmed to offer complex orders. For example, ECNs can offer contingent trades where the price is adjusted for changes in index prices or in the prices of other stocks.”

Gallardo, Heath (2009) write: “One of the most significant developments in the foreign exchange market over recent decades has been the introduction and growth of new electronic trading technologies. In addition to increasing the efficiency of foreign exchange markets, the diffusion of this technology has allowed new market segments to develop.” Gallardo, Heath (2009) continue to explain: “In 1989 Reuters began offering participants in the interbank market a so-called electronic broking service, whereby trading is carried out through a network of computer terminals linked among participating users, and new orders are matched with outstanding orders already in the system. In the early 1990s a consortium of banks launched EBS to provide a similar service. Electronic broking systems allow banks to make a “one-way” price quote and, in addition to the best bid and offer prices, display information about the closest bids and offers in the system. The resulting transparency of prices obviates the need to spend resources on price discovery activities, as interbank price quotes are now available at all times to
participating interbank dealers. Another important feature of these systems is that a large order can be matched with several small ones, which allows banks to make a one-way price quote for smaller amounts. Access to these systems therefore enabled smaller institutions to deal at more favourable spreads that had previously been available only to large institutions. Reuters Matching and EBS continue to dominate in the interdealer market, although they cover somewhat different currencies: while Reuters Matching specializes in major Commonwealth currencies, EBS has much more trading in the US dollar, Euro, Yen and Swiss Franc.”

Gallardo, Heath (2009) mention: “The downward trend in bid-ask spreads had leveled off by the mid-2000s but increased significantly following the failure of Lehman Brothers in September 2008. As volatility in foreign exchange markets spiked to nearly three times normal levels (Reserve Bank of Australia (2009)), bid-ask spreads for many major currency pairs more than doubled between September and December (Graph 1, left-hand panel),” as vividly demonstrated in Fig. 3. Gallardo, Heath (2009) note: “The high fixed costs of making the investment required to put in place and maintain the systems that can handle high volumes of transactions have been one of the factors behind the increased concentration of liquidity provision and market making in the interbank market (ECB (2003); see also Graph 1, right-hand panel),” as presented in Fig. 3.

Characterizing the interbank spot foreign exchange market activity, Gallardo, Heath (2009) comment: “Turnover on EBS and Reuters, which grew rapidly over most of the past decade, also reversed course in late 2008 (Graph 2). Though activity in interbank markets in many currency pairs leveled off in mid-2007, growth resumed in some major currency pairs, such as the euro/US dollar, in 2008. But in late 2008, activity levels dropped sharply across the board: turnover for the three most traded currency pairs in EBS roughly halved between the end of September and the end of the year,” as shown in Fig. 4.

Fig. 3 presents the bid-ask spreads and the foreign exchange market concentration, and Fig. 4 shows the interbank spot foreign exchange market activity in Gallardo, Heath (2009).
Fig. 3. Bid-ask spreads and foreign exchange market concentration (after Gallardo, Heath (2009)).

Fig. 4. Interbank spot foreign exchange market activity (after Gallardo, Heath (2009)).
Let us demonstrate that the rapid expansion of the electronic trading in the foreign exchange markets takes place in the finances in various countries, using the data analytics in Gallardo, Heath (2009): “In total, around one third of all foreign exchange transactions are executed electronically. Disaggregating the triennial survey by transaction type shows that electronic execution methods are most prevalent in the spot market, accounting for over half of turnover on a global basis (Table 1). Electronic broking systems, such as Reuters Matching or EBS, account for around 32% of all spot market transactions, while single- and multibank electronic trading platforms represent 17% and 8%, respectively. Among non-electronic methods, the most important way of executing spot transactions is directly between banks and their customers (“customer direct”).” The foreign exchange market turnover by the execution method is shown in Tab. 1 in Gallardo, Heath (2009).

Gallardo, Heath (2009) state: “Electronic execution methods are extensively used across all counterparties. Around 35% of interbank transactions are executed electronically, with almost two thirds of this accounted for by electronic broking systems (Table 2). Almost half of all interbank transactions occur directly between dealers (the category “inter-dealer direct”), and voice brokers execute the remainder.” The foreign exchange market turnover by counterparty is shown in Tab. 2 in Gallardo, Heath (2009).

Gallardo, Heath (2009) write: “Given the relatively rapid growth in turnover between banks and other financial institutions as well as non-financial customers (BIS (2007)), and the importance of multibank and single-bank trading systems for these counterparty categories, these data suggest that turnover through these trading systems has increased significantly faster than that executed on electronic broking systems. Data from the Foreign Exchange Committee on foreign exchange turnover in the United States, which show that turnover through electronic trading systems (both multibank and single-bank) has grown at an exceptionally rapid pace, support this conjecture (Graph 3).” The FX turnover in the United States by execution method is presented in Fig. 5 in Gallardo, Heath (2009).

Gallardo, Heath (2009) explain: “The importance of electronic execution in foreign exchange markets across different economies varies widely (Table 3). In a number of cases, the share of electronic methods is consistently high (or low) across all instruments and counterparties. For example, it is consistently high across all market segments for Switzerland and Germany, but consistently low for Denmark, Latin America and smaller financial centres in Asia.” The global foreign exchange market turnover by execution method is shown in Tab. 3 in Gallardo, Heath (2009).
**Tab. 1.** Foreign exchange market turnover by execution method (after Gallardo, Heath (2009)).

**Tab. 2.** Foreign exchange market turnover by counterparty (after Gallardo, Heath (2009)).

**Fig. 5.** FX turnover in the United States by execution method after Gallardo, Heath (2009)).
Tab. 3. Global foreign exchange market turnover by execution method
(after Gallardo, Heath (2009)).

Gençay, Gradojevic (2009) conclude with a comment: “EBS operates as an electronic limit order book and is used for global interdealer spot trading. It is dominant for the EUR-USD and USD-JPY currency trading, while the GBP-USD currency pair is traded primarily on Reuters Chaboud et al (2008). The average daily EUR-USD trading volume (in USD) on EBS in 2003 was between 50-70 billion dollars, which is well above that of the NYSE (40 billion dollars).”

Heath, Whitelaw (June 2011) make the following statements: “Electronic trading in the foreign exchange market effectively began in the interdealer market with the introduction of electronic broking systems provided by Reuters (in 1992) and EBS (in 1993). Demand for these services came from institutions participating in the interdealer market looking for efficiency gains they were already realizing from electronic trading in other markets, in particular the equity market. The electronic broking systems offered by Reuters and EBS largely replicated the role played by the existing brokers (now differentiated by the term ‘voice brokers’) but provided an enhanced service. The platforms displayed, in real time, the best bid and offer as well as the
The increased penetration of electronic trading in the foreign exchange market has led, directly or indirectly, to several important changes in the way the market is structured and operates:

1. **The increased efficiency and transparency of price discovery delivered initially by the electronic broking systems and then by the single-bank and multi-bank trading platforms have driven a marked decline in transaction costs, as measured by the difference between the price at which participants can buy and sell a currency at a point in time, known as the bid-ask spread** (Fig. 6).

2. **Price discovery now takes place across multiple venues, a development sometimes described as ‘liquidity fragmentation’**. In a margin trading model, the retail investor places a deposit with the broker in a margin account. The broker lends additional funds to the investor against the security of the funds in the margin account. The investor can then establish positions in the foreign exchange market up to the sum of their own funds and the funds provided by the broker. If the investor’s position sustains revaluation losses, these will be set off against the funds in the margin account and the investor will be required to deposit additional funds. The broker protects its exposure to the investor by ensuring the position is unwound prior to the loss exceeding the margin account balance. Fragmentation could make price discovery less efficient. However, market participants can now aggregate real-time price streams from multiple venues and execute on any one of them, effectively treating multiple markets as one. Some have also argued that the ability to post prices for a single trade across multiple venues creates the perception of greater market liquidity than is actually available. The implications of this ‘liquidity mirage’ are not entirely clear.

3. **There has been a marked increase in the concentration of foreign exchange activity across the books of a relatively small number of large global banks** in Fig. 7 in Gallardo and Heath (2009). This reflects, to a large extent, the impact of the single-bank platforms on the distribution of foreign exchange business. It is notable that the most recent surveys of market concentration indicate a modest decline in concentration as other global banks look to emulate the success of the early movers using this model Euromoney (2011).
4. Increasingly, banks are sourcing foreign currency liquidity for their customers from the large global banks. In some cases, this can involve an arrangement known as white labeling, where a bank provides streaming prices to its customer through a proprietary electronic interface. The streaming prices appear to be from the customer’s bank but are, in fact, being provided directly but anonymously by another bank. In other cases, banks have become customers of the global banks for some foreign currency liquidity, particularly in the major currency pairs, but they continue to provide liquidity directly to their customers and to other banks, including the global banks, in their domestic currencies.

5. There has been some breakdown in the distinction between the traditional interdealer and customer markets. With direct electronic access and, where required, prime broker sponsorship, some non-banks can now directly access pricing and liquidity that was traditionally only available to banks. In addition, there has been some blurring between the roles of banks and their customers. As noted, many banks now participate in the foreign exchange market as customers of the largest banks while some non-banks now post bids and offers on electronic platforms, effectively competing with banks as market makers.

6. There has been a significant increase in the volume of foreign exchange business undertaken by dealers with their customers, which include other financial institutions, such as hedge funds, and non-financial institutions (Fig. 8, left panel). Greater access to both single-bank and multi-bank platforms, broader support from prime brokers and reduced transaction costs are among the factors behind this trend. The increase in the volume of customer business is also reflected in a rise in the share of total foreign exchange activity globally that is executed by dealers with their customers (Fig. 9, right panel). However, this increase also reflects the increasing internalization of customer business by the large dealers; a given volume of customer business will now lead to less activity between dealers than it would have 10 years ago.

7. Electronic trading has also enabled new customer market segments to develop. As noted earlier, retail investors have become an increasingly important part of the market. This is particularly true in Japan where retail margin trading has generated large enough foreign exchange flows to help explain developments in specific exchange rate pairs Terada, Higashio and Iwasaki (2008); D’Arcy and Zurawski (2009). More recently, attention has increasingly focused on the role of high-frequency traders, for whom the ability to trade electronically is a precondition. Although the development of high-frequency trading was noted as an important new market segment before 2007 Galati and Heath (2007), there appears to have been particularly strong growth in this market segment between 2007 and 2010 Nightingale et al (2010); King and Rime (2010).
Heath, Whitelaw (June 2011) summarize their most important research findings on the electronic trading by saying that: “Developments in electronic trading technologies over the past two decades have been an important driver of change in the global foreign exchange market. For banks, three key developments have been

1) a marked increase in the concentration of foreign exchange activity,
2) a change in the relationship between banks in the interdealer market, and
3) a significant increase in the volume and share of business conducted with non-bank customers.”

King, Osler, Rime (2012) describe the electronic trading evolution: “When introduced on FX trading floors in the late 1980s, Thomson Reuters Dealing replaced the telephone with an electronic system for dealers to exchange messages, allowing for speedier and more efficient interdealer trading. The more important change occurred in the early 1990s when Reuters
introduced the first electronic limit-order market for FX, now known as Thomson Reuters Matching, while a consortium of dealers launched a competing platform, Electronic Broking Service (EBS). These systems revolutionized the interdealer segment, but remained inaccessible to end-customers. The landscape changed dramatically in the late-1990s, however, when a number of multibank trading platforms were launched that targeted end-customers directly. These systems enhanced transparency, improved operating efficiency, and reduced trading costs at the expense of greater concentration among the top dealers who streamed quotes to these platforms. Over the next decade, massive investments in the IT infrastructure by dealers and market participants opened the door to algorithmic trading, with hedge funds and high-frequency traders gaining direct access to interdealer markets from 2005 onwards King and Rime (2010). Starting in the early 2000s, the top banks launched proprietary single-bank trading platforms for their customers, allowing them to create pools of liquidity that are not visible to the market.”

King, Osler, Rime (2012) write: “Electronic trading has enabled individuals of modest wealth, previously shut out of the market, to trade speculatively for their own account. This trading generally takes place over a new type of electronic trading platform known as the retail aggregator. By bundling many small retail trades into trades that meet the minimum $1 million size for interdealer trades, retail aggregators can provide narrow spreads on even tiny trades. Retail trading has grown rapidly and was estimated to have reached $125–150 billion per day by 2010, or 8 to 10 percent of the market King and Rime (2010). Since retail customer order flow is generally uninformed Heimer and Simon (2011), these customers are a profitable group to serve. Currently there is fierce competition for such business among the large banks, since they can effectively use these traders to provide liquidity for more informed customers. Evidence on retail trading remains quite limited, and represents a potentially fruitful area for future research.”

Discussing the short-run exchange-rate dynamics, King, Osler, Rime (2012) explain: “It is now recognized that currency traders hold heterogeneous beliefs and have access to different information, some of which is private. While financial customers appear to be the best informed, their trades have only a transitory impact. Corporations are typically less informed, provide liquidity in overnight markets, and may contribute to the persistent impact of order flow on exchange rates. This interaction between informed and uninformed agents is key to modeling short-run exchange-rate dynamics.”

Fig. 10 shows the average daily interdealer trading activity by the hour across the different currencies in King, Osler, Rime (2012).
Fig. 10. Average daily interdealer trading activity by the hour across different currencies (after King, Osler, Rime (2012)).

Note: The horizontal axis shows hour of day (GMT), and the vertical axis shows the average number of trades. The five lines are for 1997, the three 4-year average for 1998-01, 2002-05, and 2006-09, respectively, and finally for 2010. From e.g. GBP/USD (figure c) we see the growth in number of trades since 1997. The exchange rates EUR/USD and USD/JPY are now primarily traded on the competing platform EBS, hence the decrease in number of trades from 1997 to 2010 for these two exchange rates. Source: Thomson Reuters Matching.
Maurer, Schäfer (2010) take a one step further and provide a definition of the algorithmic trading: “Algorithmic trading covers all trading activities where a computer algorithm autonomously decides on certain characteristics of an order. These characteristics include but are not limited to the instrument(s) to be traded, order limit, order volume, timing of order insertion, and choice of execution venue. However, an algorithm does not need to decide on all of these characteristics in order to represent algorithmic trading. Key to algorithmic trading, however, is the usage of strategies implemented on computer systems and the fact that the computer represents a driving element in order placement.

The above definition encompasses – but is not limited to – the following practices:

1) Automated identification of investment opportunities (e.g. through statistical arbitrage);

2) Activities targeting optimal placement of orders created outside of the algorithm, e.g. placed with the trading desk by an external customer, with respect to time and order volume (e.g. volume weighted average-strategies);

3) Deciding optimal order placement with respect to execution venue taking into account potential execution price including implicit and explicit transaction costs (smart order routing).”

Let us point out to the fact that Hong Kong has a well developed financial market in Lo (2000). Yiu, Ho, Ma, Tsang (2010) wrote an article, explaining that the exchange rates and the economic fundamentals are interconnected nonlinearly. Yiu, Ho, Ma, Tsang (2010) write: “The modified [target zone] model allows non-trivial portfolio choices between risk-free monetary assets and risky equities. In the model, the Hong Kong-dollar exchange rate movements depend on both the changes in the expected equity-return differential between Hong Kong and the US (i.e. the equity fundamental) and in the monetary fundamental. The typical S-shaped relationship between the exchange rate and the economic fundamentals in a target zone model becomes steeper taking into consideration the equity fundamental. In other words, the exchange-rate dynamics are more sensitive to the underlying movements of the fundamentals than implied by the conventional target zone models.”

The interest rates differential can be written as in Yiu, Ho, Ma, Tsang (2010)

\[
1 + i_{t,m}^{HKD} = \frac{E\left[S_{t}^{t+m}\right]}{S_{t}}
\]

where \(i_{t,m}\) is the stands for LIBOR or HIBOR with a maturity of \(m\) months, \(E\) is the expectation of the \(m\)-month forward exchange rate; \(S\) is the spot exchange rate.

Fig. 11 shows the Hong Kong-dollar exchange rate in Yiu, Ho, Ma, Tsang (2010).
Fig. 11. Hong Kong-dollar exchange rate (after Yiu, Ho, Ma, Tsang (2010)).

Fig. 12 shows the *S-shaped* relationship between the Hong Kong-dollar exchange rate and the monetary fundamental; Fig. 13 depicts the tilted *S-shaped* relationship at the different correlations between the monetary and the equity fundamentals in Yiu, Ho, Ma, Tsang (2010).

Fig. 12. *S-shaped* relationship between the Hong Kong-dollar exchange rate and monetary fundamental (after Yiu, Ho, Ma, Tsang (2010)).

Let us write the mathematical formulas and provide some graphical illustrations to review the modern theoretical conceptions on the electronic trading in the foreign exchange markets. To achieve this goal, we prefer to rely on the consistent scientific explanations with mathematical formulas by Prof. Albert N. Shiryaev, Steklov Mathematical Institute and Moscow
State University in Shiryaev (1998a, 1999). Before starting the review, let us note that the DEM currency is no longer in the use in Germany. In a general case, the “ask price” $S^a_t$ of the Currency$^1$ in relation to the Currency$^2$ can be written as in the proposed formula, and the dynamics of the foreign currencies exchange rate can change approximately as in Fig. 14 in Shiryaev (1998a)

$$S^a_t = \left( \frac{\text{Currency}^1}{\text{Currency}^2} \right)_t^a, \quad t \geq t_0.$$ 

The foreign currencies exchanges rates dynamics is usually characterized by the high frequency changes, which are called the ticks, as explained in Goodhart (1988, 1989, 1992), Goodhart, Demos (1990, 1991a, b), Goodhart, Curcio (1991), Goodhart, Figliuoli (1991), Goodhart, Hall, Henry, Pesaran (1993), Goodhart, Hesse (1993), Goodhart, Ito, Payne (1995, 1996), Goodhart, O’Hara (1995), Goodhart, O’Hara (1997), Goodhart, Love, Payne, Rime (2002). The statistics of ticks is analyzed with the purpose to understand the nature of the foreign currencies exchanges rates dynamics. The graph with the average number of ticks over the certain time period is shown in Fig. 15 in Ghysels, Jasiak (1995), Shiryaev (1998a), aiming to illustrate the exchange rate activity at the FX market from Monday to Friday with 5min time interval.

In addition, the change dynamics of an average number of ticks of the selected foreign currencies exchange rate over 24 hours from 05.10.92 to 26.09.93 is demonstrated in Fig. 16 in Schnidrig, Würtz (1995), Shiryaev (1998a).

Speaking about of the discrete statistical data, let us assume that $S^a_t = S^a_0 e^{Ht}$ is the ask price, $S^b_t = S^b_0 e^{Ht}$ is the bid price, $S^a_t - S^b_t$ is the difference or the spread, then we can write in Shiryaev (1998a)

$$S_t = \sqrt{S^a_t \cdot S^b_t}$$

The modification of the discrete-change process $(S_t)$ on the continuous-change process $(\tilde{S}_t)$ in the foreign currencies exchange rate dynamics over the time is presented in Fig. 17 in Shiryaev (1998a), where the discrete-change process in the foreign currencies exchange rate dynamics over the time is given as in Shiryaev (1998a)

$$S_t = S_0 + \sum_{k=1}^{\infty} \xi_k I(\tau_k \leq t),$$

the continuous-change process in the foreign currencies exchange rate dynamics over the time can be written as in Shiryaev (1998a)
\[ \tilde{S}_t = S_{y_{k+1}} \frac{t - \tau_k}{\tau_{k+1} - \tau_k} + S_{y_{k}} \frac{\tau_{k+1} - \tau}{\tau_{k+1} - \tau_k}, \quad \tau_k < t \leq \tau_{k+1}. \]

During the statistical analysis of financial data, the various types of statistical distributions can be applied, and the possible deviations of registered parameters can be measured with the \textit{Q-Q quantile analysis method} as shown in Figs. 18 and 19. In Fig. 18, we can see the \textit{Q-Q quantile analysis} of the DEM/USD currencies exchange rate with the interval \( \Delta = 20 \text{ min} \), using the data by the \textit{Reuters} agency from 05.10.92 to 26.09.93, where the quantiles \( \hat{Q}_p \) of empirical distribution of the values \( \tilde{h}_k = \tilde{h}_k^{(s)} \), \( t_k = k\Delta \), \( k = 1,2,... \) are shown along the vertical axis; the quantiles \( Q_p \) of normal distribution are depicted along the horizontal axis in \textit{Schnidrig, Würzt (1995), Shiryaev (1998a)}. In Fig. 19, the typical graphs of the empirical density \( \tilde{h}_k = \tilde{h}_k^{(s)} \), \( k = 1,2,... \), and the corresponding theoretical (normal) density are presented in \textit{Shiryaev (1998a)}.

Discussing the one dimensional distributions of the relative changes of prices, it is necessary to note the two things, namely that the “\textit{long tails}” effect can be approximated with the application of a number of different statistical distributions; and the \textit{scaling behaviour} can be observed in the \textit{foreign currencies exchange rates changes dynamics}, the schematic graph of behaviour of \( \log_{10} P_0^{(s)}(x) \) at the two various values of \( \Delta \) is drawn in Fig. 20 in \textit{Mantegna, Stanley (1995), Shiryaev (1998a)}.

Speaking about the volatility, the Figs. 21 and 22 illustrate the daily inhomogeneity and periodicity of volatility in the selected week \( \nu_{((k-1)\Delta, k\Delta)}(H; \Delta) = [\tilde{h}_k] \) on the time intervals \( ((k-1)\Delta, k\Delta), k = 1,2,... \) during the week. Fig. 21 shows the daily volatility of the DEM/USD exchange rate \( \Delta = 1 \text{ hour} \) going from the data by the \textit{Reuters} agency from 05.10.92 to 26.09.93 in \textit{Schnidrig, Würzt (1995), Shiryaev (1998a)}. Fig. 22 depicts the weekly volatility of the DEM/USD exchange course \( \Delta = 1 \text{ hour} \) during the week in \textit{Schnidrig, Würzt (1995), Shiryaev (1998a)}. The intervals \( (0,1], \ldots,(167, 168] \) correspond to the time intervals \( (0:00, 1:00], \ldots, (23:00, 24:00] \) in the \textit{Greenwich mean time}. The data belong to the \textit{Reuters} agency (05.10.1992 - 26.09.1993).

Discussing the \textit{statistics of volatility}, Fig. 23 illustrates the fractal structure of \( \Delta \) volatility \( \hat{\nu}_f (\Delta) \) in \textit{Shiryaev (1998a)}. The \( \ln \hat{\nu}_f (\Delta) \) values are placed along the vertical axis as a function of \( \ln \Delta \) (the horizontal axis). It can be seen that the volatility \( \ln \hat{\nu}_f (\Delta) \) as a function of

Considering the correlation properties of stationary time series, it is necessary to note that the empirical autocorrelation function \(\hat{\rho}(k)\) of increments sequence \(\hat{h}_n\) in the DEM/USD exchange rate with \(\Delta = 1\) min is pictured in Fig. 24 in Guillaume, Dacorogna, Dave, Müller, Olsen, Pictet (1997), Shiryaev (1998a)

\[
\hat{\rho}(k) = \frac{\mathbb{E} \left[ \hat{h}_n \hat{h}_{n+k} \right]}{\sqrt{\mathbb{E} \left[ \hat{h}_n^2 \right] \mathbb{E} \left[ \hat{h}_{n+k}^2 \right]}},
\]

where \(\hat{h} = (\hat{h}_1, \hat{h}_2, \ldots)\) is the stationary time series.

The empirical autocorrelation function \(\hat{R}(k)\) of increments sequence \(\hat{h}_n\) in the DEM/USD exchange rate, where \(k=504\) corresponds to 1 week, \(k=2016\) relates to 4 weeks, with the Reuters agency data (05.10.1992 - 26.09.1993) is shown in Fig. 25 in Dacorogna, Müller, Nagrel, Olsen, Pictet (1993), Guillaume, Dacorogna, Dave, Müller, Olsen, Pictet (1997), Shiryaev (1998a), aiming to demonstrate the cyclical nature of the autocorrelation function \(R(k)\)

\[
R(k) = \frac{\mathbb{E} \left[ \hat{h}_n \hat{h}_{n+k} \right]}{\sqrt{\mathbb{E} \left[ \hat{h}_n^2 \right] \mathbb{E} \left[ \hat{h}_{n+k}^2 \right]}},
\]

where \(\hat{h} = (\hat{h}_1, \hat{h}_2, \ldots)\) is the stationary time series.

The empirical autocorrelation function \(\hat{R}^\star(\theta), \theta \geq 0\) of the increments sequence \(\hat{h}_n^\star\) of the de-volatized values in the operational “\(\theta\)–time” with the interval \(\Delta \theta=20\) min in the DEM/USD exchange rate is presented in Fig. 26 in Dacorogna, Müller, Nagrel, Olsen, Pictet (1993), Shiryaev (1998a).
Fig. 27 illustrates the process of conversion of the operational time \( t = \tau(0) \) into the real physical time \( t = \tau(\theta) \) in Dacorogna, Müller, Nagrel, Olsen, Pictet (1993), Shiryaev (1998a). The dependence \( t = \tau(\theta) \) is linear during 5 business days, but it is nonlinear at the end of the week.

In Fig. 28, the solid line represents a periodic part in activity of the CHF/USD exchange rate, 168 hours = 1 week, in Dacorogna, Müller, Nagrel, Olsen, Pictet (1993), Shiryaev (1998a).

Fig. 29 presents the description of the clustering effect in \( \tilde{h}_k = \tilde{h}_k^{(s)} \) values in the DEM/USD exchange rate, \( \Delta = 20 \text{min}, k=504 \) corresponds to 1 week, \( k=2016 \) corresponds to 4 weeks. Clots with “small” and “big” values of \( |\tilde{h}_k| \) are clearly visible in Schnidrig, Würtz (1995), Shiryaev (1998a).


Fig. 14. Behaviour of currencies exchange rate \( S_t \), (after Shiryaev (1998a)).

Fig. 15. DEM/USD exchange rate activity from Monday to Friday with 5min interval, average number of ticks vs time (after Shiryaev (1998)).

Fig. 16. Average number of ticks per day in DEM/USD exchange rate from 05.10.92 to 26.09.93 (after Shiryaev (1998a)).

Fig. 17. Modification of discrete-change process \( \{S_t\} \) on continuous-change process \( \{\tilde{S}_t\} \) of foreign currencies exchange rate dynamics (after Shiryaev (1998a)).
Fig. 18. \( \hat{Q}_P \) quantile analysis of DEM/USD currencies exchange rate with interval \( \Delta = 20 \) min (after Shiryaev (1998a)).

Fig. 19. Typical graph of empirical density \( \tilde{h}_k = \tilde{h}_{\Delta}^{(k)} \), \( k = 1, 2, \ldots \) and corresponding theoretical (normal) density (after Shiryaev (1998a)).

Fig. 20. Schematic graph of behaviour of \( \log_{10} p_0^{(k)} (x) \) at two various values of \( \Delta \) (after Shiryaev (1998a)).

Fig. 21. Daily volatility of DEM/USD exchange rate \( \Delta = 1 \) hour (after Shiryaev (1998a)).

Fig. 22. Weekly volatility of DEM/USD exchange course \( \Delta = 1 \) hour (after Shiryaev (1998a)).

Fig. 23. Illustration of fractal structure of \( \Delta \) volatility \( \hat{v}_T (\Delta) \) (after Shiryaev (1998a)).
**Fig. 24.** Empirical autocorrelation function $\hat{\rho}(k)$ of increments sequence $\hat{h}_n$ in DEM/USD exchange rate, $\Delta = 1$ min (after Shiryaev (1998a)).

2003a, b), Dominguez, Frankel (1993a, b, c), Bollerslev (1986, 1990), Baillie, Bollerslev (1989
(1986), Grammatikos, Saunders, Swary (1986), Harris (1986, 1990), Hart, Kreps (1986), Lyons
Shleifer, Summers (1990), Sweeney (1986), DeLong, Shleifer, Summers, Waldmann (1990),
Allen, Karjalainen (1999), Courakis, Taylor (1990), Diebold, Nason (1990), Flood, Hodrick
(1990), Foster, Viswanathan (1993), Holthausen, Leftwich, Mayers (1990), De Long, Shleifer,
Summers, Waldmann (1990), Domowitz (1990, 1993), Domowitz, Steil (1999), Johansen,
Melino, Turnbull (1990, 1995), Mishkin (1990), Müller, Dacorogna, Olsen, Pictet, Schwarz,

**Financial analysis methods application, including macroeconomic analysis, market microstructure analysis and order flow analysis, to forecast foreign currencies exchange rates dynamics during electronic trading process in foreign currencies exchange markets.**

Let us begin the research discussion on the financial analysis methods. The foreign currencies exchange markets greatly contribute to the sustainable development of strongly interconnected economy of the global knowledge society in Hayek (1945), evolving toward the global cloud society, which can be characterized by such distinctive factors as:

1. The increasing information streams generation,
2. The reconfigurable-topologies communication networks appearance, and
3. The decreasing integration of economic agents with the particular territories.

In the research on the foreign currencies exchange markets, the financial forecasting problem is considered as one of the central research problems to understand in Dornbusch (1976). The forecast of the trends in the foreign currencies exchange rates dynamics is a complicated research task in the frames of the financial forecasting problem in Frankel, Froot (1990c). The actual forecast of the trends in the foreign currencies exchange rates dynamics can be done, going from the macroeconomics principles and the microeconomics principles.

Discussing the macroeconomic forecast models, Frankel, Galli, Giovannini (editors) (1996) note: “The basic macro model of the exchange rate implies that all information pertaining to the current and future "fundamental" determinants of exchange rates, that is, all information that implies a current and/or future change in the return on assets denominated in different currencies, has an immediate and unambiguous effect on exchange rates.” There is a number of econometric models to forecast the trends in the foreign currencies exchange rates dynamics in the macroeconomics in Lam, Fung, Yu (2008):

1. The Purchasing Power Parity model,
2. The Uncovered Interest Rate Parity model,
3. The Sticky Price Monetary model,
4. The Bayesian Averaging Technique model, and
5. The Combined Forecast model, including all the above models with benchmarks given by the random-walk model and the historical average return.
Let us continue our research discussion on the present research progress in the foreign currencies exchange market microstructure analysis method. Uncovering the microeconomic forecast models, Frankel, Galli, Giovannini (editors) (1996) answer an important question: “Why study foreign exchange market microstructure? The interest in the working of the foreign exchange markets stems, at least in part, from some of the problems that the asset market macro models have displayed. The first is a prima facie contradiction between the models and reality. As noted, such models imply the absence of trading in assets. By contrast, one of the most important empirical facts about the foreign exchange market is the high volume of transactions that occur daily. This inconsistency raises the question of whether the failure of the standard models to account for the volume of foreign exchange transactions is a symptom of more serious problems, which might cause the lack of success at explaining other empirical phenomena on which researchers have concentrated.

These empirical phenomena include the behavior of excess returns in the foreign exchange market, the near total inability to predict exchange rates at short horizons, the inability to explain exchange rate movements even ex post, and the volatility of exchange rates. Standard models have been unable to explain these phenomena satisfactorily. In particular, asset pricing formulas implicit in the standard macro models seem, to date, to have fared poorly. For example, even though the existence of ex ante (i.e., forecastable) returns in the foreign exchange markets can in theory be explained as risk premia, the estimated returns in practice do not match what is predicted by asset pricing models based on the covariances among asset returns.

Furthermore, models seem to have a difficult time predicting future movements in exchange rates, suggesting that the information contained in the macro variables that are usually included in these models is of limited value. Finally, the volatility of these macro variables is generally smaller than the observed volatility of exchange rates, suggesting that—unless certain variables have especially strong effects on the spot exchange rate, as, for example, in the case of large overshooting in reaction to monetary disturbances—the information affecting exchange rate movements may be in part extraneous to the variables belonging to standard macroeconomic models. Theories of rational speculative bubbles and speculative attacks can in one sense account for the existence of excess volatility. But they are inherently unsatisfying in that they have nothing to say about how or when such bubbles and attacks get started or how they end.

It is only natural to ask whether these empirical problems of the standard exchange rate models—problems that stem from the assumptions on asset market equilibrium—might be solved if the structure of foreign exchange markets was to be specified in a more realistic
fashion. *This suggests a sort of micro-foundations approach to the foreign exchange markets, according to which a more satisfactory description of the foreign exchange market microstructure might help sort out some of the problems displayed by existing macro models.*”

Frankel, Galli, Giovannini (editors) (1996) continue: “*A second reason to study market microstructure* is only loosely related to the first. Like any market, *the foreign exchange market is an interesting subject for research that attempts to identify the economic effects of its organization*. This is, as opposed to the macroeconomic approach to foreign exchange microstructure, the *microeconomic approach*. The questions that are addressed with this approach include, for example, *transparency, decentralization, the use of brokers (vs. market-makers, vs. auctioneers), the location of trading, the efficiency of clearing of foreign exchange transactions, the relation between spot and derivative markets, and the importance of systemic risk in the market.*”

Discussing the most important research results, obtained during the *market microstructure analysis*, Frankel, Galli, Giovannini (editors) (1996) highlight the following facts: “*The study of market microstructure has already produced at least one empirical regularity: the high intraday correlation of trading volume and volatility*. As noted above, standard macroeconomic exchange rate models have little hope of explaining *trading volume*. Typically, they assume *homogeneity of market participants*. If all traders are the same, why should they trade? Of course, the standard models do not attempt to explain volume, considering it of little relevance except to those who make their living trading. But the observed correlation between volume and volatility suggests something of more general interest. Frankel and Froot (1990b), for example, find a high contemporaneous correlation between volume and volatility. They also find some evidence that dispersion of traders' forecasts, as reflected in survey data, *Granger-causes both volume and volatility*. Given that trading volume seems to be relevant, there are two possible broad interpretations. One is that the market is processing information in an efficient way. Here, efficient is not to be understood as in the narrowest definition of the *efficient markets hypothesis*, where all traders are homogeneous, all information is instantly and fully reflected in the market price, and there are no profits to be made by trading. Rather, the *microstructure perspective presupposes heterogeneity*, is often based (more specifically) on *asymmetric information*, and allows that relatively more skillful or informed traders may succeed at the expense of those who are less skillful or less informed or of customers who must transact because they need to eliminate exposure ("liquidity traders"). The first interpretation is simply that the market works to aggregate the individual bits of information available to each trader in a relatively rapid and
smooth way. The chapters here shed light on a number of leading models of asymmetric information and the need for liquidity.”


Let us focus on the research discussion toward a present state of progress in the foreign currencies exchange market customer transactions order flow analysis methods. Frankel, Galli, Giovannini (editors) (1996) write: “Lyons sheds some light on how bits of such information are processed, in the form of a statistically significant effect of orders received by traders on the prices at which they transact.”

Evans, Lyon (2005, 2006) showed that:

1. “both the aggregate and disaggregated customer flows received by Citibank are positively auto-correlated;
2. contemporaneous correlations across flow segments are low at the daily frequency, but high at the monthly frequency;
3. some customer segments do produce negative coefficients in contemporaneous return regressions;
4. the proportion of excess return variation that segment flows can account for rises with the horizon; and
5. about one-third of order flows power to forecast exchange rates one month ahead comes from flows ability to forecast future flow.”

Evans, Lyons (2007) researched the transaction flows, exchange rates, and future fundamentals, making the following predictions: “The predictions are borne out in four empirical findings that define this paper's main contribution:
1. Transaction flows forecast future macro variables such as output growth, money growth, and inflation,

2. Transaction flows forecast these macro variables significantly better than the exchange rate does,

3. Transaction flows (proprietary) forecast future exchange rates, and

4. The forecasted part of fundamentals is better at explaining exchange rates than standard measured fundamentals.”

Tab. 5 shows the summary statistics for the weekly data in Evans, Lyons (2007): “The statistics in Panel A show that weekly changes in the log spot rate, $\Delta s_t = s_t - s_{t-1}$, have a mean very close to zero and display no significant serial correlation. In Panel B: First, the order flows are large and volatile. Second, they display no significant serial correlation. Summary statistics for the weekly changes in the real-time estimates are reported in Panel C.”

<table>
<thead>
<tr>
<th>Table 1: Summary Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<tr>
<td><strong>A: Exchange Rate</strong></td>
</tr>
<tr>
<td>(i) $\Delta s_t$ (x100)</td>
</tr>
<tr>
<td>(ii) Corporate US</td>
</tr>
<tr>
<td>(iii) Corporate Non-US</td>
</tr>
<tr>
<td>(iv) Traders US</td>
</tr>
<tr>
<td>(v) Traders Non-US</td>
</tr>
<tr>
<td>(vi) Investors US</td>
</tr>
<tr>
<td>(vii) Investors Non-US</td>
</tr>
<tr>
<td><strong>B: Order Flows</strong></td>
</tr>
<tr>
<td>(ii) Corporate US</td>
</tr>
<tr>
<td>(iii) Corporate Non-US</td>
</tr>
<tr>
<td>(iv) Traders US</td>
</tr>
<tr>
<td>(v) Traders Non-US</td>
</tr>
<tr>
<td>(vi) Investors US</td>
</tr>
<tr>
<td>(vii) Investors Non-US</td>
</tr>
<tr>
<td><strong>C: Real-Time Data</strong></td>
</tr>
<tr>
<td>(viii) US Output</td>
</tr>
<tr>
<td>(ix) US Prices</td>
</tr>
<tr>
<td>(x) US Money</td>
</tr>
<tr>
<td>(xi) German Output</td>
</tr>
<tr>
<td>(xii) German Prices</td>
</tr>
<tr>
<td>(xiii) German Money</td>
</tr>
</tbody>
</table>

Notes: The table reports summary statistics for the following variables sampled at the weekly frequency between January 1993 and June 1999: (i) the weekly change in the log spot rate $\times$100, (ii)-(vii) order flows from end-user segments cumulated over a week, and (viii)-(xiii) weekly changes in real-time estimates measured in annual percent. The last four columns on the right report autocorrelations $\rho_i$ at lag $i$ and p-values for the null that $\rho_i = 0$ in parentheses.

Tab. 5. Summary statistics for weekly data (after Evans, Lyons (2007)).
Evans, Lyons (2007) draw the attention to an interesting fact: “Evans and Lyons (2002a,b) show that order flows account for between 40 and 80 percent of the daily variation in the spot exchange rates of major currency pairs.”

Evans, Lyons (2007) make the following conclusion: “We also showed that proprietary transaction flows have significant forecasting power for future exchange returns and that this forecasting power reflects their ability to predict how the market will react to the flow of information concerning macro fundamentals. In sum, we found strong support for the idea that exchange rates vary as the market assimilates dispersed information regarding macro fundamentals from transaction flows.”

Finally, Evans, Lyons (2007) highlight a fact: “Most readers of this micro literature have adopted the same view: Transaction flow effects on exchange rates are about pricing errors, not about fundamentals. Our findings, by contrast, suggest that transaction flows are central to the process by which expectations of future macro variables are impounded into exchange rates.”


In addition to the above listed econometric models, the prediction of the trends in the foreign currencies exchange rates dynamics in the frames of the financial forecasting problem
can also be done, using the time series estimation techniques based on the filtering theories in the econophysics. After the formulation of the Wiener filtering theory in Wiener (1923, 1930, 1949), the various important research problems in the Wiener filtering theory have been researched in Ito (1944, 1951a, b, 2000). The Pugachev filtering theory has been outlined by Vladimir S. Pugachev in Pugachev (1944, 1956a, b, 1960, 1961, 1962, 1971, 1973, 1974, 1975, 1974, 1978, 1979a, b, 1980a, b, 1981, 1982a, b, 1984, 1985, 1986), Pugachev, Sinitsyn (1986, 1989, 1990, 1999, 2004), Pugachev, Sinitsyn, Shin (1986a, b, 1987a, b, c). The intensive research led to the creation of the optimal non-linear filtering theory in Stratonovich (1959a b, 1960a, b, 1961, 1964, 1966), and the subsequent development of the Stratonovich – Kalman – Bucy filtering algorithm in Stratonovich (1959a, b, 1960a, b), Kalman, Koepcke (1958, 1959), Kalman, Bertram (1958, 1959), Kalman (1960a, b, 1963), Kalman, Bucy (1961). Let us cite a few sentences on the description of the Stratanovich-Kalman-Bucy filtering algorithm in Ledenyov D O, Ledenyov V O (2013g): “Analyzing the time series, Ruslan L. Stratonovich created the optimal non-linear filtering theory in 1959 in Stratonovich (1959a, b, 1960a, b). During next few years, the optimal non-linear filtering theory has been extensively complemented by the various research findings; and its foundational principles have been used to develop the Stratonovich – Kalman – Bucy filtering algorithm in 1959-1963 in Stratonovich (1959a, b, 1960a, b), Kalman, Koepcke (1958, 1959), Kalman, Bertram (1958, 1959), Kalman (1960a, b, 1963), Kalman, Bucy (1961 ).” In the process of the financial forecasting problem solution finding, the Stratanovich-Kalman-Bucy filtering algorithm can be applied to predict the trends in the foreign currencies exchange rates dynamics with a greatly improved accuracy during the electronic trading process in the foreign currencies exchange markets. The authors have already researched the Stratanovich-Kalman-Bucy filtering algorithm, Stratanovich – Kalman – Bucy filters and particle filters in Ledenyov D O, Ledenyov V O (2013g, h). Therefore, let us cite the definitions of the Stratanovich – Kalman – Bucy filters in Ledenyov D O, Ledenyov V O (2013h):

1. “The Stratanovich – Kalman – Bucy filters have been well described in Ledenyov D O, Ledenyov V O (2013g): “The Kalman filter, also known as Linear Quadratic Estimation (LQE), is an algorithm that uses a series of measurements observed over time, containing noise (random variations) and other inaccuracies, and produces estimates of unknown variables that tend to be more precise than those based on a single measurement alone. More formally, the Kalman filter operates recursively on streams of noisy input data to produce a statistically optimal estimate of the underlying system state.”
2. **The particle filters** have been accurately characterized in Roncalli, Weisang (2008): “Particle filtering methods are techniques to implement recursive Bayesian filters using Monte-Carlo simulations. The key idea is to represent the posterior density function by a set of random samples with associated weights and to compute estimates based on these samples and weights [7, 20, 25, 26, 27, 28].”

Wolff (1987) published his research article titled: “The forward foreign exchange rates, expected spot rates, and premia: A signal-extraction approach,” proposing to apply a **state-space model** with the Stratanovich-Kalman-Bucy filtering algorithm to predict the risk premiums in the foreign currencies exchange market. Recently, Yu, Fung, Hongyi (2005) have discussed the possible mathematical techniques to evaluate the exchange rate risk premiums in Hong Kong dollar, using the **signal-extraction approach** for the research data analysis. Let us write a set of equations to describe the signal-extraction approach in Yu, Fung, Hongyi (2005):

\[
E_t(S_{t+1}) = f_t, \quad (1)
\]

where \( E(\ldots) \) is the conditional expectation, based on information available at time \( t \); \( S \) and \( f \) are the natural logarithm of the spot and forward exchange rates respectively.

\[
S_{t+1}f_t + \epsilon_{t+1} \quad (2)
\]

where \( \epsilon_{t+1} \) is the rational expectation forecast error: a white-noise process with zero-mean.

\[
\Delta S_{t+1} = \alpha + \beta(f_t - S_t) + \epsilon_{t+1} \quad (3)
\]

where \( \Delta \) is the differencing operator, and \( \Delta S_{t+1} \) is defined as \( S_{t+1} - S_t \).

\[
f_t = E_t(S_{t+1}) + rp_t \quad (4)
\]

\[
f_t - S_{t+1} = rp_t + \eta_{t+1} \quad (5)
\]

where \( \eta_{t+1} \) is the expectation error, it is assumed to be serially uncorrelated with zero-mean.

\[
f_{t+1}^{f,m} - S_{t+m} = rp_{t+m} + \eta_{t+m} \quad (6)
\]

where \( f_{t+1}^{f,m} \) is the natural logarithm of the forward exchange rate at time \( t \) for contracts delivered at \( m \) periods later, \( St+m \) is the corresponding natural logarithm of spot exchange rate at time \( t+m \), \( r_{p,t,m} \) is equal to \( f_{t+1}^{f,m} - E_t(S_{t+m}) \), which is the time-varying risk premium on forward contracts for delivery at \( m \) periods later.

\[
\eta_{t+m} = e_{t+m} + \theta_1e_{t+m-1} + \theta_2e_{t+m-2} + \ldots + \theta_{m-1}e_{t+1} \quad (7)
\]

where \( e_{t+j} \sim N(0, V), j = 1, \ldots, m \), i.e. \( e_{t+j} \) is assumed to distribute normally with mean zero and variance \( V \).
\[ r_{p,t,m} = \sum_{i=1}^{\delta} \delta_{i} r_{p,t-i,m} + \mu_{r,m} \]  

\[ \mu_{r,m} \sim N(0, U) \]

where \( \eta_{t,m} \) and \( \mu_{t,m} \) are assumed to be independent for all \( t \). Yu, Fung, Hongyi (2005) note that the equations (6) to (9) in the state-space form are estimated by the maximum likelihood method through the application of the Kalman filter in Tabs. 6, 7, 8, 9 and Figs. 30, 31.

**Table 1. Autocorrelations (AC) and Partial Autocorrelations (PAC) of Excess Forward Return Series**

<table>
<thead>
<tr>
<th>Lag</th>
<th>AC</th>
<th>PAC</th>
<th>1-month</th>
<th>3-month</th>
<th>6-month</th>
<th>12-month</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.319</td>
<td>0.319</td>
<td>0.698</td>
<td>0.813</td>
<td>0.854</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>0.303</td>
<td>0.303</td>
<td>0.475</td>
<td>0.567</td>
<td>0.616</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>0.224</td>
<td>0.224</td>
<td>0.424</td>
<td>0.603</td>
<td>0.671</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>0.111</td>
<td>0.111</td>
<td>0.297</td>
<td>0.476</td>
<td>0.569</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.166</td>
<td>0.166</td>
<td>0.329</td>
<td>0.490</td>
<td>0.581</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>0.071</td>
<td>0.071</td>
<td>0.294</td>
<td>0.439</td>
<td>0.534</td>
<td></td>
</tr>
</tbody>
</table>

**Table 2. Estimation Results of State-Space Model**

\[ f_{r,m} = \sum_{i=1}^{\delta} \delta_{i} e_{r,m-i} + \eta_{r,m} \]

\[ \eta_{r,m} = \epsilon_{r,m} + \theta_{1} \epsilon_{r,m-1} + \ldots + \theta_{k} \epsilon_{r,m-k} + \mu_{r,m} - N(0, U) \]

<table>
<thead>
<tr>
<th>( m = )</th>
<th>Forward exchange rate for contracts delivered at</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-month</td>
<td>3-month</td>
</tr>
<tr>
<td>( \delta_{1} )</td>
<td>0.85* (0.00)</td>
</tr>
<tr>
<td>( \lambda (10^{-4}) )</td>
<td>1.20* (0.00)</td>
</tr>
<tr>
<td>( U (10^{5}) )</td>
<td>0.22 (0.20)</td>
</tr>
<tr>
<td>Log-likelihood</td>
<td>584.19</td>
</tr>
<tr>
<td>Mean of ( r_{p} ) (in percent)</td>
<td>0.02</td>
</tr>
<tr>
<td>Variance of ( r_{p} ) (in percent)</td>
<td>0.01</td>
</tr>
<tr>
<td>Q(10)</td>
<td>7.07</td>
</tr>
<tr>
<td>Sample period from Jan 96 to Aug 05</td>
<td>Jun 05</td>
</tr>
<tr>
<td>Observations</td>
<td>116</td>
</tr>
</tbody>
</table>

**Notes:** * indicates significant at the 5% confidence level. Figures in parentheses are p-values.

All series start from January 1996. The estimated moving average parameters of the error terms are not reported. Forward exchange rates and spot exchange rate are in natural logarithm. Q(10) is the Ljung-Box Q-statistics based on the first ten serial correlation coefficients of the levels of standardized residuals. Q(10) is asymptotically distributed as \( \chi^{2} \) with 10 degrees of freedom. The critical value of \( \chi^{2}(10) \) at the 5% confidence level is 18.31.

**Table 7. Estimation results of state-space model (after Yu, Fung, Hongyi (2005)).**
Fig. 30. Estimated risk premiums of Hong Kong dollar forwards contracts delivered at different horizons (after Yu, Fung, Hongyi (2005)).

Fig. 31. Ex post excess forward returns and estimated risk premiums (after Yu, Fung, Hongyi (2005)).
Table 3. Out-of-Sample Forecast Errors

<table>
<thead>
<tr>
<th></th>
<th>1-month</th>
<th>3-month</th>
<th>6-month</th>
<th>12-month</th>
</tr>
</thead>
<tbody>
<tr>
<td>MSE (in pips)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>State-space</td>
<td>1.85</td>
<td>5.60</td>
<td>7.30</td>
<td>20.63</td>
</tr>
<tr>
<td>estimates of risk</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>premiums</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Random Walk</td>
<td>1.23</td>
<td>4.10</td>
<td>3.90</td>
<td>4.60</td>
</tr>
<tr>
<td>MAE (in pips)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>State-space</td>
<td>101.48</td>
<td>182.76</td>
<td>205.11</td>
<td>399.14</td>
</tr>
<tr>
<td>estimates of risk</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>premiums</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Random Walk</td>
<td>75.46</td>
<td>190.25</td>
<td>151.67</td>
<td>188.58</td>
</tr>
</tbody>
</table>

Notes: Numbers reported in the tables are mean squared errors (MSE) and mean absolute errors (MAE) of one-month ahead *ex ante* forecasts. The forecasting period is from October 2004 to September 2005.

**Tab. 8. Out-of-Sample forecast errors (after Yu, Fung, Hongyi (2005)).**

Table 4. Determinants of Risk Premiums

\[ \Delta r_{p,t,m} = C + \alpha \Deltaaggbal_t + \beta \Delta NDF_{t,m} + \epsilon_{t+1} + \phi_1 \epsilon_{t+m-1} + \phi_2 \epsilon_{t+m-2} + \ldots + \phi_{m-1} \epsilon_{t+1} \]

<table>
<thead>
<tr>
<th>Estimated risk premiums with delivery horizon m of</th>
<th>1-month</th>
<th>3-month</th>
<th>6-month</th>
<th>12-month</th>
</tr>
</thead>
<tbody>
<tr>
<td>C (x 10^{-3})</td>
<td>-0.01</td>
<td>-0.01</td>
<td>-0.01</td>
<td>-0.08</td>
</tr>
<tr>
<td></td>
<td>(0.81)</td>
<td>(0.95)</td>
<td>(0.85)</td>
<td>(0.67)</td>
</tr>
<tr>
<td>\Deltaaggbal_t (x 10^{-3})</td>
<td>-0.16*</td>
<td>-0.23*</td>
<td>-0.13*</td>
<td>-0.53*</td>
</tr>
<tr>
<td></td>
<td>(0.00)</td>
<td>(0.00)</td>
<td>(0.03)</td>
<td>(0.00)</td>
</tr>
<tr>
<td>\Delta NDF_{t,1}</td>
<td>-0.00</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>(0.78)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>\Delta NDF_{t,3}</td>
<td>-</td>
<td>0.03*</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>(0.00)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>\Delta NDF_{t,6}</td>
<td>-</td>
<td>-</td>
<td>0.01*</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>(0.00)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>\Delta NDF_{t,12}</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.05*</td>
</tr>
<tr>
<td></td>
<td>(0.00)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>R-squared</td>
<td>0.21</td>
<td>0.47</td>
<td>0.62</td>
<td>0.53</td>
</tr>
<tr>
<td>Q(12)</td>
<td>10.64</td>
<td>5.79</td>
<td>13.84</td>
<td>5.47</td>
</tr>
<tr>
<td>Sample period</td>
<td>Aug 05</td>
<td>Jun 05</td>
<td>Mar 05</td>
<td>Sep 04</td>
</tr>
<tr>
<td>Observations</td>
<td>80</td>
<td>78</td>
<td>75</td>
<td>68</td>
</tr>
</tbody>
</table>

Notes: * indicates significant at the 5% confidence level. Figures in parentheses are p-values. All estimations start from January 1999. The estimated moving average parameters of the error terms are not reported. Q(12) is the Ljung-Box Q-statistics which is asymptotically distributed as a \( \chi^2 \) with 12 degrees of freedom. The critical value of \( \chi^2 \) (12) at the 5% confidence level is 21.03.

**Tab. 9. Determinants of risk premium (after Yu, Fung, Hongyi (2005)).**
As it can be seen in Yu, Fung, Hongyi (2005), the forward exchange rate can be viewed as the sum of two components: an expected future spot rate and a time-varying risk premium, hence it is possible to use the signal-extraction approach to identify and measure the unobserved risk premiums from the Hong Kong dollar forward exchange rates.

Ultra high frequency electronic trading strategies creation and execution under influence by discrete information absorption during ultra high frequencies electronic trading in foreign currencies exchange markets in diffusion-type global financial system with induced nonlinearities


Let us consider the factors, which can have an influence on the information absorption capacity, assuming that the information is a valuable capital in the hands of experienced financiers in 21st century in Shapiro, Varian (1999), and it can be thoroughly used in the fundamental and technical models of the foreign currencies exchange rates determination in Rosenberg (1996). First of all, let us explain that, in the process of the information-based electronic trading in the foreign currencies exchange market, there are the information diffusion, absorption and dispersion processes, which can precisely describe the individual traders, trading firms, trading banks on one side as well as to accurately characterize the electronic trading systems, financial systems, foreign currencies exchange markets on other side. The information diffusion, absorption and dispersion processes during the ultra high frequency electronic trading in the foreign currencies exchange markets in the diffusion-type financial systems with the induced nonlinearities have been researched by scientists. Franke, Hess (1997, 2000) investigated the problem of the information diffusion in the electronic and floor trading. Bacchetta, van Wincoop (2003) researched the information dispersion to explain the exchange rate disconnect puzzle. Evans, Lyons (2005b) researched one of the aspects of the information absorption: “Do currency markets absorb the news quickly?” De Zwart, Markwat, Swinkels, van Dijk (2009) considered the economic value of the fundamental and technical information in the emerging currency markets. Bjønnes, Osler, Rime (2011) researched the possible sources of the information advantage in the foreign exchange currencies market. Rime (2000) researched the private and public information in the foreign currencies exchange markets. Chinn, Moore (2008) researched a role of the private information in the monetary model of exchange rates.
Moore, Payne (2011) identified the main sources of private information in the foreign currencies exchange markets. We assume that these information diffusion, absorption and dispersion processes are present during the ultra high frequency electronic trading in the foreign currencies exchange markets in the diffusion-type financial systems with the induced nonlinearities.

Continuing our research discussion on the absorption phenomena in the econophysics, which is researched in the frames of the evolving learning process at the various practical settings and theoretical considerations in the econophysics in the finances, we would like to say that a new perspective on the learning and innovation with the particular research focus on the absorptive capacity has been presented in Cohen, Levinthal (1990), Farina (2008), Hussinger (2010, 2012). There are a number of innovative studies, which have been focused on the knowledge and information absorptive capacity by the firm in Farina (2008): “According to Cohen and Levinthal’s (1990) “absorptive capacity” concept, firms’ ability to get knowledge and information from their external environment is a function of the firms’ specialization choices and experiences. In particular, firms operating in many market segments are likely to possess more internal capabilities than firms operating in few market segments since, as the volume and complexity of information in the environment increase, the organization needs to have correspondingly high levels of information processing capacity (Miller and Chen (1994); Hambrick, (1982); Khandwalla (1973)).” Farina (2008) continues to explain: “In fact firms’ ability to use network ties for accessing information about opportunities and choices otherwise not available is depending on internal resource endowments and in particular on “absorptive capacity”.

We make a theoretical proposition that the trader’s ability to select the winning virtuous strategies in the process of the information-based electronic trading in the foreign currencies exchange market strongly depends on the trader’s information absorption capacity. In our research approach, we assume that, in the process of decision making process on the winning virtuous strategy, the traders select the winning virtuous strategies by way of the information absorption and its subsequent analysis on an available set of choices in the frames of the creative imperative integrative intelligent conceptual co-lateral adaptive logarithmic thinking process with the application the inductive, deductive and abductive logics in Martin (1998-1999, 2005-2006) in the frames of the strategic choice structuring process, that is the winning through the distinctive choices process in Martin (1998-1999a, 2005-2006a, 2004, 2009), Moldoveanu, Martin (2001), Lafley, Martin (2013). In other words, the absorbed information creates a knowledge base, which is necessary for the successful completion of
decision making process. Let us remind the meanings of the **deep knowledge** and the **broad knowledge** as described in Moldoveanu, Martin (2001): “The **general knowledge** – knowledge that can be easily taught and transferred by means of formalized dialects – and **specific knowledge** – knowledge that cannot be easily encoded and transferred. However, within each different kind of knowledge we can talk of a distinction between the depth of the knowledge and the breadth of the knowledge. **Knowledge is deep when it is of the sort that can answer many concatenated ‘why?’ questions.** The physicist’s and the mathematician’s knowledge are examples of deep knowledge. It has a hierarchical structure, with a few basic propositions at the top of the hierarchy, from which all other propositions follow by self-evident steps. **Knowledge is broad when it can be used to answer many questions of the type: ‘what?’, ‘where?’, ‘who?’ and ‘how?’**. The economist’s and the biologist’s knowledge are examples of **broad knowledge**. There are few key fundamental; assumptions that can compress all of this knowledge, which consists of a large set of empirical findings and basic causal mechanisms which only work when certain conditions come about.”

In the practical case of the **ultra high frequency electronic trading strategy creation and execution** processes in the **foreign currencies exchange markets** in the conditions of the **continuous and discrete information absorption processes** in the **diffusion-type global financial system** with the **induced nonlinearities**, the authors applied the **developed software program**, which performs the following routines:

1. The execution of the **embedded optimized Stratanovich-Kalman-Bucy filtering algorithm** in the Stratanovich – Kalman – Bucy filter and the particle filter to accurately estimate the **time series** and predicted the **trends in the foreign currencies exchange rates dynamics** during the **electronic trading** in the **selected foreign currencies exchange market**.

2. The execution of the **embedded optimized macroeconomic analysis, market microstructure analysis and order flow analysis algorithms** to precisely forecast the **foreign currencies exchange rates optional dynamics** during the **electronic trading process** in the **selected foreign currencies exchange markets**, using the **original information gathering and aggregation engines** from the computer servers.

3. The execution of the **embedded optimized comparative analysis algorithm** to compare the **obtained data streams** from the completed algorithms 1 and 2, to select and execute the **winning virtuous trading strategy** during the **ultra high frequency electronic trading** in the **foreign currencies exchange markets** in the **diffusion-type financial system** with the **induced nonlinearities**.
Thus, we developed a complex software program with the embedded Stratonovich – Kalman - Bucy filtering algorithm and the particle filtering algorithm, aiming to accurately forecast the trends in the foreign currencies exchange rates dynamics during the electronic trading process in the foreign currencies exchange markets in the practical cases of the non-Gaussian non-linear chaotic distributions of the financial variables in the time domain. The developed tested software program can operate with the commonly traded foreign currencies pairs in the foreign currencies exchange markets, making the accurate forecasts on the trends in the foreign currencies exchange rates dynamics during the electronic trading process in the selected foreign currencies exchange markets. The increased accuracy of computations has been reached by the application of a combination of the prediction models, including the econometric forecast models and the Stratanovich – Kalman – Bucy filtering algorithm estimation models.

We also propose the Ledenyov law: The processing frequency of electronic trading systems in the foreign currencies exchange markets in the diffusion - type financial systems with the induced nonlinearities will double every two years, which has been formulated in an analogy with the Moore’s law, which describes the integrated circuits capacity doubling every 18 – 24 months in Moore (1995, 2003).

In addition, we would like to make a few interesting concluding remarks that the modern absorption theory in the finances and economics as well as the physics and chemistry has been intensively developed by the prominent distinguished researchers at the world class research institutions and the top league “red bricks” universities in a number of countries over the recent centuries. In this connection, it makes sense to note a remarkable fact that the nature of absorption processes of the different chemical compounds in the various physical – chemical systems has been comprehensively researched by the authors together with their scientific collaborators in the physics and chemistry over the last 45 years. Let us list the selected theoretical and experimental research programs to study the absorption phenomena in the material science, which have been completed by the authors together with their scientific collaborators in recent decades:

2. The absorption of the electromagnetic signals in the condensed matter (the high pure metals and superconductors) at the ultrasonic frequencies has been investigated in the solid state physics in Ledenyov O P (2012a, b, c), Ledenyov V O, Ledenyov D O, Ledenyov O P, Tikhonovsky (2012), Ledenyov O P, Fursa V P (2012), Shepelev, Ledenyov O P, Filimonov (2012a, b, c, d, e), etc.


Conclusion

In the Schumpeterian creative disruption age, the authors firmly believe that an increasing application of electronic technologies in the finances opens a big number of new unlimited opportunities toward the ultra high frequency electronic trading in the foreign currencies exchange markets in the conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities.

This scientific paper applied the innovative thinking to research the ultra high frequency electronic trading strategies in the foreign currencies exchange markets in the conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities, based on the academic literature.

Going from the academic literature, we discussed the probability theory and the statistics theory application to accurately characterize the trends in the foreign currencies exchange rates dynamics in the short and long time periods. We considered the financial analysis methods, including the macroeconomic analysis, market microstructure analysis and transactions order flow analysis, to forecast the volatility in the foreign currencies exchange rates dynamics in the short and long time periods. We investigated the application of the Stratanovich-Kalman-Bucy filtering algorithm in the Stratanovich – Kalman – Bucy filter and the particle filter to accurately estimate the time series and predict the trends in the foreign currencies exchange rates dynamics in the short and long time periods. We researched the influence by discrete information
absorption on the ultra high frequency electronic trading strategies creation and execution during the electronic trading in the foreign currencies exchange markets. We formulated the Ledenyov law on the limiting frequency (the cut-off frequency) for the ultra high frequency electronic trading in the foreign currencies exchange markets.

We believe that this paper extends the understanding of the complex research problems, connected with the ultra high frequency electronic trading strategies in the foreign currencies exchange markets in the conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities.

We think that the application of the multidisciplinary research skills in the finances, economics, econometrics, econophysics, electronics and computer science will lead to the creation and execution of the winning virtuous ultra high frequency electronic trading strategies in the foreign currencies exchange markets in the conditions of the discrete information absorption processes in the diffusion-type financial systems with the induced nonlinearities.

Acknowledgement

This condensed research article is mainly aimed for the young scientists, professors, subject experts, financial analytics, experienced financiers, foreign exchange traders and business leaders, who would like to learn more on the ultra high frequency electronic trading in the foreign exchange markets at an influence by the discrete information absorption processes in the diffusion–type financial systems with the induced nonlinearities, and it is written, applying the theoretical econometrical and econophysical approaches in the academic literature. The research article is written on the basis of a series of invited lectures on the ultra high frequency electronic trading in the foreign exchange markets at an influence by the continuous and discrete information absorption processes in the diffusion–type financial systems with the induced nonlinearities, which has been presented by the authors at the leading universities around the World in recent years.

The first author’s knowledge on the origins of the nonlinearities in the complex systems in the electrical, electronic, computer and financial engineering has been obtained during the intensive innovative scientific collaboration with Prof. Janina E. Mazierska, Personal Chair, Electrical and Computer Engineering Department, James Cook University, Townsville, Australia and former Dean, Electrical and Computer Engineering Department, James Cook University, Townsville, Australia, and former IEEE Director Region 10 in Australia, and IEEE Fellow. The first author would like to acknowledge Prof. Janina E. Mazierska by expressing his
sincere gratitude for the kind scientific advices on how to develop the logical mathematical analysis skills, the scientific problems analytic solving ability and the abstract scientific thinking to tackle the complex scientific problems on the nonlinearities in the microwave superconductivity as well as on the nonlinearities in the finances, applying the interdisciplinary scientific knowledge together with the advanced computer modeling techniques in the course of the cutting-edge highly innovative research projects at James Cook University in Townsville in Queensland in Australia in 2000 – 2014 after the graduation from V. N. Karazyn Kharkov National University in Kharkov in Ukraine in 1994 – 1999.

There would be appropriate to say that, in an information age, the first author’s special efforts have been primarily directed towards the scientific information gathering, systematization and detailed analysis in the frames of this research projects on the ultra high frequency electronic trading in the foreign exchange markets at an influence by the discrete information absorption processes in the diffusion – type financial systems with the induced nonlinearities; hence the first author would like to thank the professional stuff at the central library at James Cook University in Townsville, Queensland, Australia for providing the first author with all the necessary technical support in relation to the literature search on the subjects of his multidisciplinary research interest in the national and international electronic research databases at Australian universities, replying to the numerous chaotic research requests timely, and making everything possible to assist with the completion of the highly innovative advanced research on the ultra high frequency electronic trading in the foreign exchange markets at presence of the discrete information absorption processes in the diffusion – type financial systems with the induced nonlinearities at the James Cook University in Townsville, Queensland in Australia in 2000 – 2014.

The first author would like to comment that the informative scientific discussions on the accurate characterization of the foreign currencies exchange rates dynamics during the ultra high frequency electronic trading in the foreign currencies exchange markets at an impact by the discrete information absorption processes in the diffusion – type financial systems with the induced nonlinearities, which have been conducted by the first author with the M.Sc. students, Ph.D. candidates, professors, visiting scientists and other faculty members during the numerous scientific seminars and research meetings at James Cook University in Townsville in Queensland in Australia, are generously appreciated, because these valuable scientific opinions exchanges encouraged the first author to generate the new original scientific ideas and make the creative imperative integrative intelligent conceptual co-lateral adaptive logarithmic thinking with the
application of the inductive, deductive and abductive logics analysis as far as the ultra high frequency electronic trading in the foreign currencies exchange markets is concerned.

A certain part of this condensed research article has been written during the first author’s visit to the City of Kuala Lumpur and the Island of Langkawi (www.holidaylangkawi.com) in Malaysia in January, 2014. Therefore, it is a first author’s great pleasure to see that the 6th London School of Economics Asia Forum 2014 has been also conducted in the City of Kuala Lumpur, Malaysia this year. It makes sense to comment that the first author did learn enormously from the research articles, written by Prof. Charles A. E. Goodhart, London School of Economics and Political Science, London, UK, who presented an invited talk at the above mentioned conference in Malaysia in 2014. In addition, in the present research article, the first author decided to use the important research findings and the financial analysis data on the global foreign currencies exchange market, presented in the invited speech by Prof. Andrew Sheng, Graduate School of Economics and Management, Tsinghua University, Beijing, P. R. China; the University of Malaya, Kuala Lumpur, Malaysia former President of Fung Global Institute, a Chief Adviser to the China Banking Regulatory Commission, a Board Member of Khazanah Nasional Berhad, Malaysia, a member of the International Advisory Panel to the Australian Treasury's Financial System Inquiry, and an advisor to the United Nations Environment Program Inquiry into the Design of a Sustainable Financial System.

Summing up all the above comments, the first author acknowledges the “numerous meetings without the ties” with the great Australian philosophers, professors, scientists, businessmen, lawyers, governmental officials and political leaders in the relaxing trusted mutual-respect atmosphere, characterized by the pluralism of research opinions on the discussed topics, during the Yara valley and Mornington-Peninsula limo tours (www.yaravalleylimotours.com.au), which fascinated the first author’s mind, stimulated the abstract thinking on the theoretical ideas or assumptions, and inspired to work consistently to complete the writing of this highly innovative condensed research article on the ultra high frequency electronic trading in the foreign currencies exchange markets in the case, when the discrete information absorption processes are present in the diffusion – type financial systems with the various types of induced nonlinearities, at James Cook University in Townsville, Brisbane, and Gold Coast in Queensland in Australia in 2014.

The second author would like to kindly acknowledge the numerous private communications with the participants of the V. Ya. Bunyakovsky international conference with the special focus on the V. Ya. Bunyakovsky’s research contributions to the mathematical theory of probability and its modern applications in the econophysics and econometrics, which had
place during a tour to the Town of Bar in Vinnytsya Region in Ukraine in the time of the conference, organized by the Institute of Mathematics of National Academy of Sciences of Ukraine (NASU), Kyiv, Ukraine on August 20 – 21, 2004. Absorbing the brilliant research ideas during a fruitful exchange by the scientific opinions among the conference attendees, the second author came up with a remarkable conclusion that the foundations of the mathematical theory of probability by V. Ya. Bunyakovsky enable us to perform a more accurate scientific analysis and characterization of the complex research problems on the ultra high frequency electronic trading in the foreign currencies exchange markets in the circumstances, when the discrete information absorption processes are present in the diffusion – type financial systems with the various types of induced nonlinearities.

It is a real pleasure to comment that some fundamental issues on the electronic trading in the foreign currencies exchange markets have been researched by the second author during his intensive research work on a number of the complex research problems at the Electronic Trade Laboratory, Rotman School of Management, University of Toronto, Canada in 2005 - 2006. Having said that, the second author would like to state that the Electronic Trade Laboratory at the Rotman School of Management, University of Toronto, Canada has became a global hub of innovative scientific thinking in the finances mainly due to the high level organizational efforts by Prof. Roger L. Martin, former Dean, Rotman School of Management, University of Toronto, Canada on that time. It is important to underline the fact that the Electronic Trade Laboratory, Rotman School of Management, University of Toronto, Canada can be characterized as a global financial center of gravity, where the highly innovative research work has been conducted by the second author from the early morning hours until the deep night, being occasionally interrupted by the thoughtful scientific discussions on a variety of problems in the finances with Profs. John C. Hull and Roger L. Martin, Rotman School of Management, University of Toronto, Canada in 2005 - 2006.

We are glad to mention a remarkable fact that the authors spent a great deal of time, analyzing the numerous mathematical formulas and research data by many distinguished scientists, and aiming to understand the nature of the foreign currencies exchange rate dynamics; hence we are very grateful to a big number of professors for their kind permissions to apply the derived mathematical formulas and selected theoretical models from their published research articles. Especially, the authors would like to acknowledge the extensive use of some important research results on the macroeconomics analysis, market microstructure analysis and transactions order flow analysis methods in connection with the foreign currencies exchange rates prediction problems by Richard K. Lyons, Bank of America Dean and Professor of
Business and Kruttschnitt Family Chair in Financial Institution at Walter A. Haas School of Business at University of California-Berkeley in Berkeley, California in the USA. In our opinion, the unconventional research thinking and brilliant scientific ideas on the foreign currencies exchange rates dynamics by Prof. Richard K. Lyons definitely deserve more focused research attention from the side of the financiers, traders and professors in the leading financial institutions and “red bricks” universities.

As always, we are very grateful to Prof. Michael E. Porter, Bishop William Lawrence University Professor and former Dean of Harvard Business School, Harvard University, who is considered by the authors as a father of the modern business strategy, for his valuable personal efforts and time to write a number of interesting informative research articles and books, providing us with his professional expertise, exceptional quality professional advices and wise opinions in the field of competitive strategy in the 21st century.

Playing the tennis at the tennis courts or the golf at the golf play grounds with our research collaborators, business partners, friends in various developing and developed countries around the World regularly, we have already conducted many hundreds of thoughtful discussions on various research topics, hence we would like to thank all our Friends for their interesting ideas, suggestions and shared experiences on the subject of our research interest in the finances.

*E-mail: dimitri.ledenyov@my.jcu.edu.au

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**Finances Science, Economics Science, Foreign Currencies Exchange Markets Science:**


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