Policy-Induced Changes in Income Distribution and Profit-Led Growth in A Developing Economy

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Policy-Induced Changes in Income Distribution and Profit-Led Growth in A Developing Economy

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Abstract

In a demand-side growth model, we show that a developing economy may experience a steady positive equilibrium growth rate of investment and profit-as long as investment in the economy is responsive to the aspirations of the richer section of the population to match the consumption level of the developed world and imitation of foreign production technology is not very expensive irrespective of any changes in income distribution. If the process is accompanied by no change in the distribution of income then the employment share of the technologically stagnant sector producing for the poor increases at the cost of declining growth rate of real wage. On the other hand if the growth process is accompanied by an exogenous change in the distribution of income induced by shift in economic policy regime then the positive and stable equilibrium growth rate of investment is associated with an increasing growth rate of output though more is gained in terms of increase in output growth when income distribution improves rather than worsens. On the other hand, growth rate of employment for the entire economy might decline.

Keywords: Profit-led Growth, Luxury Consumption, Investment, Technology Transfer, Policy Regimes, Income Distribution

JEL Classification: E12, E2, O11, O41, O43, O33

1 Introduction

Over the last three decades most of the developing countries have adopted a more or less universal set of economic policies, often known as the neo-liberal policies. These policies aim at liberating the market from government intervention so as to achieve allocative efficiency. Therefore a particular significance is attached to restricting the size of budget deficit. Many economists have argued that this has resulted in

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worsening of income inequality in these countries. Assuming this to be true, the post-Keynesian/Kaleckian growth literature seems to suggest that these economies should stagnate unless they manage to continuously increase their trade surplus. However some of these economies have put up very decent growth performance in the face of decreasing budget deficits. At same time failing to consistently maintain trade surplus and even have experienced increasing trade deficit. The post-1991 Indian growth experience, particularly the last decade, being a stand out example.

The post-Keynesian/Kaleckian growth literature places the central emphasis, while examining the growth process of an economy, in the generation of aggregate demand. Aggregate demand in the economy is the sum of consumption, investment, budget deficit and trade surplus. In the absence of budget deficit and trade surplus, dynamics of consumption and investment explain the growth path of the economy. Consumption is described by the classical savings assumption wherein the entire wage income is consumed and a fixed proportion of the profit is saved, wage and profit being the only income categories. On the other hand, investment is assumed to be a function of demand in the economy. In this set up, a worsening of income distribution is expected to cause stagnation in the economy. This is because, according to Kalecki (1971), investment in any given period depends upon decisions taken in previous periods and these decisions depend upon the level of demand in the previous periods. Since the entire wage income is consumed, investment generates savings out of profit equal to itself in the equilibrium. If profit share is fixed by the ‘degree of monopoly’ then the fixed level of investment determines the level of output. If income distribution worsens, due to an increase in the ‘degree of monopoly’, then in the equilibrium output level would be less than what it would be in case there is no change in the income distribution. Since the output is less than what it would be without worsening of distribution, investment in the next period would be less too.

Bhaduri and Marglin (1990) pointed out that the profit rate can be decomposed into the profit share and capacity utilization, where the latter indicates the level of demand. They proposed that the investment rate in the economy is a function of both profit share and capacity utilization. In the case where sensitivity of investment rate to profit share is greater than that of the savings rate, capacity utilization in the economy increases with increase in the profit share. They term this as the exhilarationist regime contrary to the stagnationist regime where the opposite happens. However, as pointed out by Rowthorn (1982) and Dutt (1984), if income distribution is fixed, we will expect that an exogenous increase in the profit share will decrease the growth rate due to the resulting fall in consumption out of wages. Moreover Blecker (2002) using linear and Cobb-Douglas specifications for Bhaduri and Marglin’s investment function has pointed out that exhilarationism either do not arise or arise only under extreme elasticity assumption on the investment function.

Kalecki (1971) argued that technological innovation is one major factor which can sustain the growth process. Technological innovation not only leads to obsolescence
of old machinery and plants leading to their replacement by new ones but also provides a strong stimulus for investment by opening up new investment opportunities. In fact he argued that the impact of a steady stream of innovations on investment is comparable with the impact of a steady increase in profit because both give rise to “certain additional investment decisions”.\footnote{Kalecki (1969), pp. 58} He also emphasized that despite this demand-stimulating nature of technological innovation, there is no guarantee that the degree of utilization of resources stays at a constant level. Patnaik 2007 argues that in developing countries the richer section of the population aspire to match the consumption standards of the developed countries. As income distribution worsens, they are in a position to afford more and more of goods consumed in the developed countries. With increase in demand for goods consumed in developed countries, the incentive of firms to produce such goods, by imitating foreign production techniques, also increases. Thus he argues that growth and technological change in the developing countries are induced by the growing demand of the richer section of the population to consume goods available in the advanced countries as a result of increase in inequality. Patnaik terms this process as ‘structural-cum-technological’ change. He however concludes that though it is possible for such developing countries to experience high rates of growth but the growth process is highly unstable and any sufficiently strong negative shock to investment can take the economy to a state of stagnation.

In this paper we first show that a developing country can experience a positive equilibrium growth rate of investment and surplus as long as – investment in the economy is responsive to the aspirations of the richer section of the population to match the consumption level of the developed world and imitation of foreign production technology is not very expensive. Unlike Patnaik (2007), the growth process need not be unstable but rather can be stable under certain conditions. Moreover worsening of income distribution is not required to sustain this kind of growth process but a sufficiently unequal initial distribution of income is enough to propel it. Next, we show that the technologically dynamic sector producing for the rich is incapable in generating much employment. If the process is accompanied by no change in the distribution of income then the employment share of the the technologically stagnant sector producing for the poor increases at the cost of declining growth rate of real wage. In case the growth process is accompanied by an exogenous change in the distribution of income induced by shifts in economic policy regime then the positive and stable equilibrium growth rate of investment is associated with an increasing growth rate of output though more is gained in terms of increase in output growth when income distribution improves rather than worsens. On the other hand, growth rate of employment for the entire economy might decline.

As for the structure of the paper, in the next section we describe the major assumptions of our model. In section 3 and 4, we discuss the existence and local-stability
of a positive equilibrium growth rate of investment respectively. In section 5, we consider change in income distribution caused by changes or shifts in the economic policy paradigm/regime, for example the government adopting neo-liberal reforms or becomes more mindful of equity consideration. We consider regime changes which either worsen (by increasing profit share) or improve (by decreasing profit share) the income distribution over a period of time. We discuss the impact of such changes in the distribution of income on the growth rate of output along the equilibrium growth path of investment. In section 6, we discuss the implications for growth rates of employment and labour productivity in the economy. And finally section 7 contains concluding remarks where we summarise and discuss the results.

2 Model

Consider a closed economy model with no government budget. This economy is neatly divided into two classes- capitalists and workers. The capitalists own all the means of production, i.e. capital. They carry out production by combining their capital with hired labour in order to earn profit. The workers have only labour which they sell to the capitalists in return for wages. The capitalists and the workers consume entirely different goods. The workers consume a subsistence good whereas the capitalists consume a variety of luxury goods but not the subsistence good. Luxury goods are defined to be goods which have been developed in the advanced countries and are initially available for consumption only in these economies. These luxury goods are substitutes to each other in the sense as new luxury goods are introduced in the market the old tend to disappear because their demand falls. We assume that luxury goods are made available in this economy only through imitation of foreign production technologies.

There are two sectors in the economy- the luxury sector and the non-luxury sector. In the luxury sector, luxury goods for the capitalists and investment goods required to produce luxury goods are produced. Similarly in the non-luxury sector, the subsistence good for the workers and the investment goods required to produce the subsistence good are produced. There is no technological progress in the non-luxury sector. On the other hand, following Patnaik 2007, we assume that the production technology associated with new luxury goods are more labour saving. Over time, goods with more sophisticated technologies and higher labour productivity are introduced in the advanced countries. We will assume that there exists a ranking of the luxury goods that are introduced in the economy under consideration, such that the production techniques of newer luxury goods are associated with higher labour productivity.

Labour productivity is defined as value of output per unit labour. Values are expressed in terms of the subsistence good, which is assumed to be the numeraire.
2.1 Consumption and savings

The workers spend all their wages on the consumption of the subsistence good. The capitalists consume a part of their profit and save the rest. We assume that the level of consumption out of profit increases not only when the level of profit increases but also when, given a level of profit, more and more new luxury goods make their way into the market. In other words, we assume that consumption out of profit is directly related to both the level of profit and the rate at which new luxury goods are introduced in the market.

We will assume that the faster is the rate at which new luxury goods are introduced in this economy, the higher is the rate of change in the labour productivity of the luxury goods sector, $\dot{a}$. This is because if at any point of time new luxury goods are introduced at a faster rate then at that point of time the proportion of new luxury goods demanded and produced would be greater compared to a situation where there is a slower rate of introduction of luxury goods. Labour productivity of the luxury goods sector, $a$, will increase at a higher rate because one, a faster rate of introduction means that there are more new luxury goods with higher labour productivities are produced. And two, since the luxury goods are substitutes in the sense described above, the output share of old luxury goods is smaller when new luxury goods are introduced at a faster rate compared to a slow rate. Thus we use the rate of change in the labour productivity of the luxury goods sector to proxy the rate at which new luxury goods are introduced in the market.

We can therefore describe consumption out of profit, $C$, by the following function,

$$C = C(\Pi, \dot{a})$$  \hspace{1cm} (1)

with $0 < C_\Pi < 1$ and $C_\dot{a} > 0$, where $\Pi$ is the level of profit, $\dot{a}$ is that rate of change in the labour productivity of the luxury sector which proxies for the rate of introduction of new luxury goods. Since workers do not save, savings for the economy is given by

$$S = \Pi - C(\Pi, \dot{a}) = S(\Pi, \dot{a})$$  \hspace{1cm} (2)

with $0 < S_\Pi < 1$ and $S_\dot{a} < 0$.

2.2 Investment

Net investment in this economy is assumed to depend on the current level of profit and the rate at which new luxury goods are introduced in the market. A high current level of profit is the predictor of a high future level of demand in the economy and also a high level of profit eases the financing constraints on the capitalists’ decision to invest.\(^3\) Therefore, we assume investment in the economy to positively depend on the current level of profit.

\(^3\)Kalecki, M., 1969
The relationship between the rate at which new luxury goods are introduced and investment is ambiguous and depends on the ease with which firms can imitate the production techniques of the new goods. Given our assumptions about consumption demand out of profit, a higher rate of introduction new luxury goods into the market is associated with more opportunities to invest for the firms and all firms would like to invest at a higher rate in the production of new luxury goods.

On the other hand, if cost of imitation is very high, say due to strict enforcement of intellectual property rights, then at any point of time only a few firms will invest in the production of new luxury goods. Since we have assumed that as new luxury goods are introduced in the market older ones tend to disappear, firms producing old luxury goods, unable to get access to production techniques of the relatively new luxury goods, will hold back new investment on their existing plants and let their capital stock depreciate. Moreover if some of the old luxury goods are forced out of the market as new luxury goods are introduced, firms producing these goods will have to shut down in case they can not imitate production technology of new luxury goods.

Thus investment in the economy, $I$, is given by the following function,

$$I = I(\Pi, \dot{a})$$

with $I_\Pi > 0$ where $I_\Pi$, while there is no restriction on the sign of $I_\dot{a}$. $\dot{a}$ in (3) is again the proxy for the rate of introduction of new luxury goods.

### 2.3 Technological change in the luxury goods sector

Technological change in the luxury goods sector is endogenously driven by the growth of profit in the economy. Any increase in the growth rate of profit in the economy impacts both the demand and supply of luxury goods. On one hand, increase in the growth rate of profit increases the incomes of the profit earners at a faster rate. Thus their ability to consume at the high-end of the goods available in the developed world increases at a faster rate. On the other hand, the ability of the firms to meet the cost of imitation also increases at a faster rate as the growth rate of profit increases. Therefore when the growth rate of profit increases it becomes profitable to introduce more of the high-end goods available in the developed world. The high-end goods in the developed world are associated with higher labour productivities than the existing luxury goods in this economy. This combined with our assumption that the old luxury goods tend to disappear from the market with the introduction of the new luxury goods, implies that the labour productivity of the luxury goods sector tends to increase at higher rates.

The current technological capabilities of firms in the economy are commensurate with the technological requirements of the existing luxury goods being produced within

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4Henceforth by investment we mean net investment.

5Patnaik 2007
the economy. It is reasonable to assume that as one moves up the hierarchy of goods being produced in the advanced countries, technological requirements of production become more sophisticated compared to the current technological capabilities of firms in the economy. Thus as more and more new luxury goods are introduced in the economy at a point in time, the actual cost of imitation and introduction of additional new luxury goods increases. Therefore we assume that at any point of time, the rate of growth of labour productivity of the luxury goods sector in this economy increases with an increase in the growth rate of profit but at a decreasing rate. This relationship between the growth rate of labour productivity in the luxury goods sector, $g_a$ and the growth rate of profit is given by the following equation.

$$g_a = \phi(g_\Pi)$$

(4)

with $\phi(0) = 0$ and for all $g_\Pi \in [0, \infty)$, $\phi'(g_\Pi) \geq 0$, $\phi''(g_\Pi) > 0$ and $\phi'''(g_\Pi) < 0$.6

2.4 Demand-induced changes in the growth rate of profit

Whenever investment in the economy is greater than savings, either price adjustment happens which raises the share of profit in output leaving aggregate output level constant or the level of aggregate output increases leaving share of profit in the aggregate output unchanged or both the adjustments happen simultaneously. In any case whenever investment is more than savings, the level of profit will rise. Similarly when investment is less than savings, the level of profit will fall and when investment is equal to savings, the level of profit will remain unchanged. This process of change in the level of profit due to mismatch between investment and savings is conveniently captured by the following equation.

$$(\ln \Pi) = \alpha[\ln(I/S)] = \alpha(\ln I - \ln S)$$

(5)

where $\alpha$ is a positive constant.

Differentiating equation (5) with respect to time we get,

$$\dot{g}_\Pi = \alpha(g_I - g_S)$$

(6)

6Patnaik 2007 assumes that the growth rate of labour productivity is an increasing convex function of the growth rate of investment, which in turn is an increasing function of the growth rate of profit. It is argued that in a developing economy where technology is just imitated from abroad, there is no given set of knowledge to be progressively used up but rather with increasing investment more investments in new projects will be taken up. This we feel implicitly assumes that as the economy moves up the hierarchy of goods in the developed economies at any point of time, the cost of moving from one step to the next in the hierarchy goes down. Since at any given point in time, the technological capabilities in the economy are fixed, it is difficult to believe that at the margin the cost of introducing new luxury goods will go down. Therefore we think $\phi'''(g_\Pi) < 0$ to be a more plausible assumption than $\phi''(g_\Pi) > 0$. 7
where \( \alpha > 0 \) and \( g_{\Pi} \) is the rate of change in \( g_{\Pi} \) the growth rate of profit, \( g_I \) is the rate of growth of investment and \( g_S \) is the rate of growth of savings.\(^7\) From (2) and (3) growth rates of savings and investment are

\[
g_S = \sigma_{S,\Pi} g_{\Pi} + \sigma_{S,\dot{a}} \frac{1}{\dot{a}} \frac{d\dot{a}}{dt}
\]

(7)

and

\[
g_I = \sigma_{I,\Pi} g_{\Pi} + \sigma_{I,\dot{a}} \frac{1}{\dot{a}} \frac{d\dot{a}}{dt}
\]

(8)

respectively. \( \sigma_{i,j} \) is elasticity of \( i \) with respect to \( j \) where \( i = I, S \) and \( j = \Pi, \dot{a} \). \( \sigma_{S,\Pi} > 0, \sigma_{S,\dot{a}} < 0 \) for \( \dot{a} > 0 \) and \( \sigma_{I,\Pi} > 0 \). \( \sigma_{i,j} \)'s are assumed to be constant throughout.

Substituting for \( g_I \) and \( g_S \) from (7) and (8) in equation (6), we obtain

\[
g_{\Pi} = \alpha(\sigma_{I,\Pi} - \sigma_{S,\Pi}) g_{\Pi} + \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \frac{1}{\dot{a}} \frac{d\dot{a}}{dt}
\]

(9)

From equation (4), using the definition of growth rate and logarithmic differentiation, we obtain

\[
\frac{1}{\dot{a}} \frac{d\dot{a}}{dt} = \phi(g_{\Pi}) + \rho \frac{g_{\Pi}}{g_{\Pi}}
\]

(10)

where \( \rho = \frac{g_{\Pi}}{\phi(g_{\Pi})} \phi'(g_{\Pi}) \) is the elasticity of the growth rate of labour productivity in the luxury goods sector with respect to the growth rate of profit and \( \rho > 0 \) as \( \phi' > 0 \). We assume that \( \rho \) is a constant.

Substituting for \( \frac{1}{\dot{a}} \frac{d\dot{a}}{dt} \) in equation (9) from equation (10) and then re-arranging the terms we obtain,

\[
g_{\Pi} = \frac{\alpha g_{\Pi}[(\sigma_{I,\Pi} - \sigma_{S,\Pi}) g_{\Pi} + (\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \phi(g_{\Pi})]}{[g_{\Pi} - \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho]}
\]

(11)

where \( g_{\Pi} \) is not defined for \( g_{\Pi} = \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho \). This implies that \( g_{\Pi} \) is not defined when \( \phi(\alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho) = \alpha(\sigma_{I,\Pi} - \sigma_{S,\Pi})(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho \). We will assume that \( \phi(\alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho) \neq \alpha(\sigma_{I,\Pi} - \sigma_{S,\Pi})(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho \).\(^8\)

\(^7\)Bhaduri 2006 uses a general form function, instead of the natural logarithm function used in our model, to derive an expression for the rate of change in the growth rate of output, \( g_Y \), similar to equation (5), i.e., \( g_Y = \alpha[g_I - g_S] \) with \( \alpha > 0 \) by assuming that any mismatch between investment and savings gives rise only to output adjustments. However to get the expression \( g_Y = \alpha[g_I - g_S] \) from the general form function it is assumed that any deviation of investment, \( I \), from an initial commodity market clearing equilibrium, \( I = S \), stays arbitrarily close to the value of investment at the initial equilibrium. Moreover it is assumed that whenever \( I = S \), output grows at some equilibrium rate, \( g_Y \), in contrast to our contention that \( g_{\Pi} = 0 \) whenever \( I = S \). We simply argue that demand side adjustment in the economy, which is the focus of our model, stops whenever \( I = S \).

\(^8\)By re-arranging equation (11) we get,

\[
g_{\Pi} g_{\Pi} - \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho = \alpha g_{\Pi}[(\sigma_{I,\Pi} - \sigma_{S,\Pi}) g_{\Pi} + (\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \phi(g_{\Pi})]
\]

Substituting \( \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho \) for \( g_{\Pi} \) in the above expression gives \( \phi(\alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho) = \alpha(\sigma_{I,\Pi} - \sigma_{S,\Pi})(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}) \rho \).
Equation (11) expresses the rate of change of the growth rate of profit, $\dot{g}_\Pi$, as a function of the growth rate of profit, $g_\Pi$, in the economy.

3 Positive equilibrium growth rate of profit

An equilibrium for equation (11), i.e., $\dot{g}_\Pi = 0$ implies either $g_\Pi = 0$ or $[(\sigma_{I,\Pi} - \sigma_{S,\Pi})g_\Pi + (\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\phi(g_\Pi)] = 0$. Therefore it is obvious that a positive equilibrium growth rate of profit exists if and only if the equation

$$[(\sigma_{I,\Pi} - \sigma_{S,\Pi})g_\Pi + (\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\phi(g_\Pi)] = 0$$

has a positive solution. This implies that $\sigma_{I,\Pi} \neq \sigma_{S,\Pi}$ and $\sigma_{I,\dot{a}} \neq \sigma_{S,\dot{a}}$. Re-arranging the above equation gives us,

$$\phi(g_\Pi) = zg_\Pi$$

(12)

where $z = \frac{\sigma_{S,\Pi} - \sigma_{I,\Pi}}{\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}}}$, a constant. Notice that the assumptions on the function $\phi(g_\Pi)$, mentioned in section 2.3, ensure a positive solution of equation (12) as long as $z > 0$.

In figure 1, $g^*_{\Pi}$ denotes the positive equilibrium growth rate of profit. Given that profit grows at the positive equilibrium rate $g^*_{\Pi}$, investment and savings in the economy grow at constant positive rates $g^*_I = \sigma_{I,\Pi}g^*_{\Pi} + \sigma_{I,\dot{a}}\phi(g^*_{\Pi})$ and $g^*_S = \sigma_{S,\Pi}g^*_{\Pi} + \sigma_{S,\dot{a}}\phi(g^*_{\Pi})$. Thus the equilibrium growth rates of investment and savings depend, apart from the equilibrium growth rate of profit, on the responsiveness of investment and savings to profit and the rate of introduction of new luxury goods in the economy and on the form.
of the function $\phi$. Moreover from the definition of $g^*_\Pi$ we know that in equilibrium $g^*_I = g^*_S$.

The fact that under certain conditions a positive equilibrium growth path of profit exists in the economy implies that at every instance of time on it investment is greater than savings by a fixed proportion. Notice that we can re-write equation (4) as

$$g_{\Pi} = \alpha [\ln(\frac{I}{S})]$$  \hspace{1cm} (13)

Substituting $g^*_\Pi$ in equation (13) and then re-arranging it, we get the following.

$$\frac{g^*_I}{\alpha} = \ln(\frac{I}{S})$$  \hspace{1cm} (14)

Since $\frac{g^*_I}{\alpha}$ is a positive constant, $\frac{I}{S}$ must be a constant greater than one. Investment-savings ratio being a constant greater than one means that the short-run macroeconomic equilibrium characterised by the equality investment and savings in the \textit{ex-ante} sense is never realized on the equilibrium growth path of profit in the economy. This is because profit growth in our model is fueled by the excess of investment over savings in the \textit{ex-ante} sense.

4 Stability

Local stability of the equilibrium requires that $\frac{dg_{\Pi}}{dg_{\Pi}}$ at $g_{\Pi} = g^*_I$ is less than zero, where $g^*_I$ is the positive equilibrium growth rate of profit. Differentiating (11) with respect to $g_{\Pi}$ and then substituting $g^*_I$ for $g_{\Pi}$, we get

$$\frac{dg_{\Pi}(g^*_I)}{dg_{\Pi}} = \frac{\alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})g^*_I(\phi'(g^*_I) - z)}{[g^*_I - \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})]\rho}$$  \hspace{1cm} (15)

where $\frac{dg_{\Pi}(g^*_I)}{dg_{\Pi}}$ is $\frac{dg_{\Pi}}{dg_{\Pi}}$ evaluated at $g_{\Pi} = g^*_I$. Now $\alpha$ and $g^*_I$ are positive constants. Existence of positive equilibrium growth rate of profit implies that ($\phi'(g^*_I) - z) < 0$. To see this notice that $\phi(g_{\Pi}) - zg_{\Pi} = 0$ at both $g_{\Pi} = 0$ and $g_{\Pi} = g^*_I$. The claim then necessarily follows from Rolle’s Theorem\textsuperscript{9} and the assumption $\phi''(g_{\Pi}) < 0$. Thus the necessary and sufficient conditions for local stability of $g^*_I$ are $g^*_I > \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\rho$ and $\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}} > 0$.

The first condition, $g^*_I > \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\rho$, requires that the equilibrium growth rate of profit is sufficiently large. We can re-write (11) as

$$\dot{g}_{\Pi} = \alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\psi(g_{\Pi}) + \frac{\alpha(\sigma_{I,\dot{a}} - \sigma_{S,\dot{a}})\rho}{g_{\Pi}}\dot{g}_{\Pi}$$  \hspace{1cm} (16)

where $\psi(g_{\Pi}) = \phi(g_{\Pi}) - zg_{\Pi}$. The right hand side of equation (16) is the impact of excess of growth rate of investment over the growth rate of savings, which for the sake

\textsuperscript{9}See, for example Albrecht and Smith 2003, 106
of simplicity let us call the growth rate of the I/S ratio, on the the rate of change in the growth rate of profit. Notice the first term in this expression is zero when \( g_{II} = 0 \), i.e., \( (\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}}) \psi(g_{II}) = 0 \) when \( g_{II} = 0 \), while the second term is zero when \( g_{II} = 0 \), i.e., \( \frac{(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\rho}{g_{II}} \) when \( g_{II} = 0 \). Therefore we can think of \((\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\psi(g_{II})\) as the component of the growth rate of the I/S ratio explained by \( g_{II} \) and \( \frac{(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\rho}{g_{II}} \) as the component of the growth rate of the I/S ratio explained by \( g_{II} \). From equation (14), it is clear that the rate of change in the growth rate of profit \( \dot{g}_{Π} \) has the same sign as the component of the growth rate of the I/S ratio explained by \( g_{II} \). The second condition, \( \sigma_{I,\hat{a}} - \sigma_{S,\hat{a}} > 0 \), requires that either investment responds non-negatively to changes in the rate of introduction of new luxury goods or even when it responds negatively, the responsiveness of savings is more than the responsiveness of investment.10 In either case, the indirect impact of a positive growth rate of profit on its rate of change is always positive, i.e., \( \alpha(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\phi(g_{II}) > 0 \). Since \( z > 0 \), \( \sigma_{I,\hat{a}} - \sigma_{S,\hat{a}} > 0 \) implies that \( \sigma_{S,II} - \sigma_{I,II} > 0 \). So the direct impact of a positive growth rate of profit on its rate of change is negative, i.e., \((\sigma_{I,II} - \sigma_{S,II})g_{II} < 0 \).

Figure 1 shows two values of \( g_{II} \), \( g_{II}^a \), and \( g_{II}^b \), close to \( g_{II}^h \). Let us assume that \( g_{II}^a > \alpha(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\rho \). This means \( g_{II} \) has the same sign as the component of the growth rate of the I/S ratio explained by \( g_{II} \). At \( g_{II}^a \), \( \phi(g_{II}^a) > zg_{II} \), thus \( \psi(g_{II}^a) > 0 \). Therefore, from the definition of \( \psi(g_{II}) \), \( \alpha(\sigma_{S,II} - \sigma_{I,II})g_{II}^a < \alpha(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\phi(g_{II}^a) \). The direct negative impact of the growth rate of profit on its rate of change is less than the indirect positive impact. Thus the component of the growth rate of I/S ratio explained by \( g_{II} \) at \( g_{II}^a \) is positive, which increases \( g_{II} \). Similarly at \( g_{II}^b \), since \( \psi(g_{II}^b) < 0 \) we have \( \alpha(\sigma_{S,II} - \sigma_{I,II})g_{II}^b > \alpha(\sigma_{I,\hat{a}} - \sigma_{S,\hat{a}})\phi(g_{II}^b) \). In this case the direct negative impact of the growth rate of profit on its rate of change dominates the indirect positive impact. Therefore, \( g_{II} \) decreases at \( g_{II}^b \). Thus \( g_{II}^h \) is locally stable.

5 Changes in income distribution and output growth

In this and the next section we will consider change in the distribution of income induced by exogenous shifts in the economic policy regime and examine its effect on output and employment growth in the economy. When policy regime changes many policy measures are adopted that are expected to have an impact on the distribution of income in the economy. For example, let us consider government going in for neo-liberal reforms. In that case many policy changes like easing the norms for mergers and acquisition, labour reforms, privatization of state run enterprises, reduction of corporate income tax, etc., would take place that tend to increase the ‘degree of monopoly’ in the economy. As a result we would expect the profit share to gradually rise over a period of time. On the other hand, suppose the government

\[10\text{Notice that since } \sigma_{S,\hat{a}} < 0, \sigma_{I,\hat{a}} - \sigma_{S,\hat{a}} > 0 \text{ implies either } \sigma_{I,\hat{a}} \geq 0 \text{ or } (\sigma_{I,\hat{a}} < 0 \text{ and } |\sigma_{I,\hat{a}}| < |\sigma_{S,\hat{a}}|).\]
under popular pressure tries to orient its economic policy towards consideration of equity. In that case policies like employment guarantee and minimum wages would be adopted which tend to reduce the ‘degree of monopoly’ and we would expect the profit share to gradually decrease over a period of time.

In the analysis that follows we consider shifts in policy regime which either improve or worsen the distribution of income and assume that whenever such shifts in policy regime happen, then the profit share changes continuously at a constant rate over a period of time. Moreover, we assume that such shifts in policy regime do not have any independent effect on investment and savings in the economy but through changes in the level of profit and therefore do not have any independent impact on the investment-savings gap in the economy. This implies that the equilibrium growth rate of profit derived in section 3 remains unaffected. Nonetheless, there is an impact on the adjustment process because any excess of investment over savings increases profit in order to generate savings. As share of profit gradually change due to shift in policy regime, it affects the level of profit and also puts pressure on the adjustment required in the level of profit in response of the investment-savings gap.

In order to examine this clearly and also for closing the model we will assume that the adjustment in the level of profit in response to investment-savings gap is achieved only through output increase in the absence of any policy induced increase in the profit share. In periods along the equilibrium growth path of profit, when there is a policy induced worsening of the income distribution, i.e., \( \dot{h} > 0 \), a part of the increase in profit required due to excess of investment over savings is automatically achieved by the exogenous rise in the profit share while the rest is achieved through endogenous output increase. On the other hand in case of an improvement in the distribution of income, i.e., \( \dot{h} < 0 \), decline in profit share will decrease the the level of profit and thus the excess of investment over savings will result into a greater endogenous adjustment in the level of output.

By definition \( \Pi = Yh \), where \( Y \) is the total output of the economy and \( h \) is share of profit in output. Therefore the growth rate of profit is \( g_\Pi = g_Y + \frac{\dot{h}}{h} \), where \( g_Y \) is the growth rate of output and \( \frac{\dot{h}}{h} \) is the growth rate of profit share. On the equilibrium growth path of profit, the growth rate of output is,

\[
\frac{g_Y}{g_\Pi} = \frac{\dot{h}}{h} (17)
\]

We will assume that the change in profit share, \( \dot{h} \), is an exogenously given policy determined parameter. Thus output grows at a rate equal to the equilibrium growth rate of profit when income distribution does not change, that is \( \dot{h} = 0 \). When profit share increases, that is \( \dot{h} > 0 \), then \( g_Y < g_\Pi^* \) whereas when profit share decreases, that is \( \dot{h} < 0 \), \( g_Y > g_\Pi^* \).

The growth rate of output, after these aforementioned changes, however is not constant but increases in both the cases. First suppose \( \dot{h} > 0 \), then profit share, \( h \),
increases over time. This implies $\frac{\dot{h}}{h}$ decreases as $\dot{h}$ is fixed. Thus it follows from (17) that $g_Y$ increases as $\dot{h} > 0$. Next suppose $\dot{h} < 0$, then the profit share, $h$, decreases over time. This implies $|\frac{\dot{h}}{h}|$ increases as $\dot{h}$ is fixed. Since $\dot{h} < 0$, it follows again from (17) that $g_Y$ increases. Nonetheless growth rate of output is always higher in the case of economic policy regime shifting in favour of the workers than the case where the shift is in favour of the capitalists. This is because when $\dot{h} > 0$ then the increase in growth rate follows a discrete drop from $g^*_\Pi$ and also the increase must taper off at some point less than $g^*_\Pi$ as $h$ can never become greater than one. On the other hand when $\dot{h} < 0$, then growth rate of output at first jumps above $g^*_\Pi$ and then keeps on increasing as long as impact of a shift in policy regime in favour of the workers on the profit share remains.

### 6 Growth of labour productivity and employment

Labour productivity of the entire economy is the weighted average of labour productivities in the luxury goods sector and the non-luxury goods sector with the weights being their respective employment shares. Thus the labour productivity of the entire economy, $x$ is given by the following equation.

$$x = al_a + b(1 - l_a)$$

(18)

where $b$ is a positive constant which is always less than $a$. $a$ and $b$ are the labour productivities of the luxury goods sector and the non-luxury goods sector respectively. $l_a$ is the employment share of the luxury goods sector. From (18), the growth rate of labour productivity in the economy is,

$$g_x = \frac{l_a}{x} \left\{ ag_a + (a - b)g_a \right\}$$

(19)

where $g_x$, $g_a$ and $g_a$ are respectively the growth rates of labour productivity for the entire economy, the luxury goods sector and the employment share of the luxury goods sector.

Since only capitalists consume luxury goods, we would expect the share of luxury goods output in total output to increase as the share of profit in output increases. Therefore we assume the share of luxury goods output in total output to be an increasing function of the profit share as described below.

$$\frac{Y_a}{Y} = f(h)$$

(20)

where $0 \leq f(h) \leq 1$ and $f'(h) > 0$. $Y_a$ is the output of the luxury goods sector.

Using the definition of $l_a$ and (20) we obtain,

$$l_a = \frac{f(h)x}{a}$$

(21)
From (21) the growth rate of the employment share of the luxury goods sector is,

\[ g_a = \frac{f'(h)}{f(h)} \dot{h} + g_x - g_a \]  \hspace{1cm} (22)

Substituting for \( l_a \) and \( g_{la} \) respectively from equations (21) and (22) in equation (19) the re-arranging the terms, we obtain the following expression for the growth rate of labour productivity in the economy.

\[ g_x = \frac{bf(h)g_a + (a - b)f'(h)\dot{h}}{\{1 - f(h)\}a + f(h)b} \]

On the equilibrium growth path of profit \( g_a = \phi(g^*_\Pi) \), therefore \( g_x \) is,

\[ g_x = \frac{bf(h)\phi(g^*_\Pi) + (a - b)f'(h)\dot{h}}{\{1 - f(h)\}a + f(h)b} \]  \hspace{1cm} (23)

Thus the growth rate of labour productivity in the economy at any instant along the equilibrium growth path of profit depends on the constant growth rate of labour productivity in the luxury goods sector, labour productivities of the two sectors, the share of luxury goods sector’s output in the total output and the exogenously given rate of change in the profit share. Since \( a \) grows at a constant rate \( g_x \) is not constant along the equilibrium growth path of profit. In the absence of any exogenous change in the distribution of income, i.e., when \( \dot{h} = 0 \), from equation (23) we know that the growth rate of labour productivity in the economy continuously declines over time. The growth rate of employment in the economy on the equilibrium growth path of profit is \( g_L = g^*_\Pi - g_x \). As \( g_x \) falls over time the growth rate of employment increases to approach \( g^*_\Pi \). This is obvious because when income distribution is fixed then the employment share of the luxury goods sector declines and approaches zero as its labour productivity grows at a constant rate. Since labour productivity in the non-luxury sector is fixed, the growth rate of labour productivity in the economy must decline and approach zero and the growth rate of employment approaches \( g^*_\Pi \). The entire gain in the employment in the economy comes in the non-luxury sector and moreover this decline in \( g_x \) gets translated into a decline in the growth rate the real wage which ultimately become stagnant.

However in periods the distribution of income changes (i.e. \( \dot{h} \neq 0 \)) due to shifts in policy regime, then \( g_x \) need not always decline but can also increase. Let us consider the case of a period when there is worsening of income distribution. Along the equilibrium growth path of profit \( \dot{h} > 0 \). Since now both \( a \) and \( h \) are not constants but grow over time from (23) we can not say whether \( g_x \) will decline or increase over time. The increase in labour productivity of the luxury goods sector tends to decrease its employment share but this is countered by increasing share of its output due to worsening of income distribution. When the latter tendency out-weighs the former, \( g_x \) rises along the equilibrium growth path of profit leading to a possibility of declining growth rate of employment. We derive some conditions when \( g_x \) declines in periods when \( \dot{h} > 0 \) in appendix 1. Similarly in periods when \( \dot{h} < 0 \) too the behaviour of \( g_x \) and \( g_L \) over time are ambiguous.
7 Conclusion

The basic idea on which the paper is based is that not only the level of demand but also its composition is important while studying economic growth. In the closed economy model presented in the paper, we have shown that in a developing country consumption demand of the richer section of the population for goods available in developed countries can sustain a positive and steady growth rate of investment and profit. The consumption demand of the rich for goods available in developed countries is an incentive to the firms for investing in the production of such goods by imitating foreign production techniques. In order to capture the aspirations of the rich in the economy to match the consumption standards in the developed countries, we have postulated that the consumption out of profit is not only an increasing function of the level of profit but also of the rate of introduction new luxury goods in the economy, which are goods that are already available in developed countries. Since a faster rate of introduction of new luxury goods increases the consumption demand of the richer section of the population, it also provides an incentive to the producers to invest in production of such goods, therefore has a tendency to increase net investment. On the other hand, if imitation is very costly net investment might also decline because the luxury goods are substitute goods in nature. In fact one condition for the local stability of equilibrium is that even if investment responds negatively to the rate of introduction of new luxury goods its responsiveness should be less than that of savings.

Assuming that overtime goods introduced in the developed countries are more sophisticated and are associated with higher labour productivities, we have proxied the rate of introduction of new luxury goods in the model by the rate of change in the labour productivity of the luxury sector, \( \dot{a} \). The growth process is associated with a particular kind of technological change such that the labour productivity in the luxury sector grows at a constant rate whereas by assumption there is no technological change in the non-luxury sector. The technological change in the luxury sector is induced by the growth rate of profit which indicates the richer section of the population’s ability to afford sophisticated goods available in the developed countries. This is captured by a Kaldor kind of technological progress function given by equation (4). The equilibrium growth rate of profit and investment depends upon the responsiveness of investment and savings functions to changes in the level of profit and the rate of change in the labour productivity of the luxury sector along with the form of the function \( \phi \). It is obvious from figure 1 that the equilibrium growth rate of profit (and the growth rate of investment) increases with exogenous increase in \( \sigma_{I,\Pi}, \sigma_{I,a} \) and \( |\sigma_{S,a}| \) because they decrease \( z \). On the other hand any increase in \( \sigma_{S,\Pi} \) decreases the equilibrium growth rate of profit (and the growth rate of investment) because it increases \( z \). Similarly any upward shift in the curve of the the function \( \phi \) increases the equilibrium growth rate of profit (and the growth rate of investment).

If income distribution in the economy is fixed then growth of output along the equilibrium growth path of profit, is constant and equal to positive equilibrium growth.
rate of profit. From equation (20), it then follows that the growth rate of employment in the luxury sector is \( g_{L_a} = (1 - z)g^*_\Pi \). Thus the growth rate of employment in luxury sector is positive if and only if \( z < 1 \), i.e., \( \sigma_{S,\Pi} + \sigma_{S,\dot{a}} < \sigma_{I,\Pi} + \sigma_{I,\dot{a}} \). However in section 6, we have seen that along the equilibrium growth path of profit, employment share of the luxury sector continuously declines and approaches zero because labour productivity in the economy declines while in the luxury sector increases at a constant rate. Since labour productivity in the economy declines, the growth rate of employment in the economy increases to approach \( g^*_\Pi \). The gain in employment comes majorly in the non-luxury sector where technology is stagnant. This gain in employment growth comes at the cost of decline in the growth rate of real wage which ultimately becomes stagnant.

In section 5, we have considered shifts in economic policy regime of the government, that are either in favour of the capitalists or the workers, on the growth rate of output along the equilibrium growth path of profit. Whenever such shifts in the policy regime occur, many policy changes occur that tend to gradually increase the income share of the class towards which the regime shift is biased. We have assumed the profit share changes at a constant rate for a period of time when such regime shifts happen. Assuming that in absence of changes in policy regime only output adjustment takes place, we show in conformity with the existing post-Kaleckian literature that the growth rate of output declines when there is an exogenous increase in the profit share and increases when there is a decrease in the profit share. However in both cases growth rate of output is not constant but increasing because the impact of the redistribution on the growth rate of profit share diminishes overtime. As a result a shift in economic policy regime in favour of the capitalists does create a spectacle of increasing output growth for sometime but only after an initial decrease. Nonetheless much more is to be gained in terms output growth by a shift of policy regime in favour of the workers, i.e., by improving income distribution rather than worsening it, because growth rate of output not only increases immediately when policy regime shifts in favour of the workers but the increase is also sustained.

In section 6 we have seen that in periods when \( \dot{h} \neq 0 \), labour productivity growth in the economy can increase or decrease both. This is because labour productivity in the economy is weighted average of the labour productivities in the two sectors with the weights being their respective employment share. Any change in the income distribution tends to change the output share of the luxury sector which might counter the impact on the employment share of the luxury sector due to continuous increase in its labour productivity. The analysis of impact of government policy induced changes in income distribution on the growth process presented in the paper is however limited to only those kinds of policy measures which are less likely to have any direct bearing upon investment and savings in the economy. In case the change in income distribution due to shifts in policy regime has independent impact on investment and savings then the entire analysis would change. This and allowing for simultaneous adjustment in profit share and output in response to investment-savings gap are on
the agenda for future research.

References


Appendix 1

The total differential of $g_x$ is

$$dg_x = \frac{\partial g_x}{\partial a} da + \frac{\partial g_x}{\partial h} dh$$

where $dg_x$, $da$ and $dh$ are the changes in $g_x$, $a$ and $h$ respectively with $da > 0$ and $dh > 0$; and $\frac{\partial g_x}{\partial a}$ and $\frac{\partial g_x}{\partial h}$ are the respective partial derivatives of $g_x$ with respect to $a$ and $h$.

From equation (23) the partial derivative of $g_x$ with respect to $a$ is,

$$\frac{\partial g_x}{\partial a} = \frac{f'(h)\dot{h}}{[(1 - f(h))a + f(h)b]} - \frac{(1 - f(h))\{bf(h)\phi(g^*_{11}) + (a - b)f'(h)\dot{h}\}}{[(1 - f(h))a + f(h)b]^2}$$

and the partial derivative of $g_x$ with respect to $h$ is,

$$\frac{\partial g_x}{\partial h} = \frac{bf'(h)\phi(g^*_{11}) + (a - b)f''(h)\dot{h}}{[(1 - f(h))a + f(h)b]} + \frac{(a - b)f'(h)\{bf(h)\phi(g^*_{11}) + (a - b)f'(h)\dot{h}\}}{[(1 - f(h))a + f(h)b]^2}$$
Substituting for $\frac{\partial g}{\partial a}$ and $\frac{\partial g}{\partial h}$ in equation (24) and then re-arranging the terms we get,

$$dg_x = \frac{f'(h)\dot{a}da}{(1 - f(h))a + f(h)b} + \frac{bf'(h)\phi(g^*_\Pi) + (a - b)f''(h)\dot{h}dh}{[(1 - f(h))a + f(h)b]^2}$$

$$+ \frac{[(a - b)f'(h)\dot{h} - (1 - f(h))\dot{a}]bf(h)\phi(g^*_\Pi) + (a - b)f'(h)\dot{h}}{[(1 - f(h))a + f(h)b]^2}$$

Since $\phi(g^*_\Pi)$, $\dot{h}$, $a$, and $b$ are all positive with $a > b$ and $0 < f(h) < 1$, it follows from the above equation that if $f''(h) \geq 0$ and $(a - b)f'(h)\dot{h} - (1 - f(h))\dot{a} \geq 0$ then $dg_x$ is positive. Otherwise $dg_x$ can be negative. Since $adh > 0$ and $\frac{da}{dt} = \dot{a} = a\phi(g^*_\Pi)$ and $\frac{dh}{dt} = \dot{h}$, $(a - b)f'(h)\dot{h} - (1 - f(h))\dot{a} \geq 0$ implies,

$$(a - b)f'(h)\dot{h} \geq a(1 - f(h))\phi(g^*_\Pi)$$

If we assume that the share of luxury goods output increases at a constant or an increasing rate as the profit share increases, i.e., $f''(h) \geq 0$, then in periods when government policy changes result in worsening of income distribution, the growth rate of labour productivity increases as long as the inequality (25) is satisfied.