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# Inflation, Unemployment and Economic Growth in a Schumpeterian Economy

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## Abstract

This study explores the long-run relationship between inflation and unemployment in a monetary Schumpeterian growth model with matching frictions in the labor market and cash-in-advance (CIA) constraints on consumption and R&D investment. Under the CIA constraint on R&D, a higher inflation that raises the opportunity cost of cash holdings leads to a decrease in innovation and economic growth, which in turn decreases labor-market tightness and increases unemployment. Under the CIA constraint on consumption, a higher inflation instead decreases unemployment in addition to stifling innovation and economic growth. Therefore, the two CIA constraints have drastically different implications on the long-run relationship between inflation and unemployment. We also calibrate our model to aggregate data in the US and Eurozone to explore quantitative implications on the relationship between inflation and unemployment.

*JEL classification:* E24, E41, O30, O40

*Keywords:* inflation, unemployment, innovation, economic growth

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# 1 Introduction

The relationship between inflation, unemployment and economic growth has long been a fundamental question in economics. This study provides a growth-theoretic analysis on this important relationship in a Schumpeterian model with equilibrium unemployment. Creative destruction refers to the process through which new technologies destroy existing firms. On the one hand, the destructive part of this process leads to job losses. On the other hand, new technologies also create new firms with new employment opportunities. In a frictionless labor market, these job destructions and job creations could offset each other leaving the labor market with full employment. However, given the presence of matching frictions between firms and workers, this continuous turnover in the labor market as a result of creative destruction leads to what Joseph Schumpeter (1939) referred to as "technological unemployment". At the first glance, it may seem that technological unemployment is a very specific kind of unemployment; however, as Schumpeter [1911] (2003, p.89) wrote, "[i]t doubtlessly explains a good deal of the phenomenon of unemployment, in my opinion its better half."

To explore the effects of inflation on unemployment and economic growth, we introduce money demand via cash-in-advance (CIA) constraints on consumption and R&D investment into a scale-invariant Schumpeterian growth model with equilibrium unemployment. Early empirical studies such as Hall (1992) and Opler *et al.* (1999) find a positive and significant relationship between R&D and cash flows in US firms. Bates *et al.* (2009) document that the average cash-to-assets ratio in US firms increased substantially from 1980 to 2006 and argue that this is partly driven by their rising R&D expenditures. Brown and Petersen (2011) provide evidence that firms smooth R&D expenditures by maintaining a buffer stock of liquidity in the form of cash reserves. Berentsen *et al.* (2012) argue that information frictions and limited collateral value of intangible R&D capital prevent firms from financing R&D investment through debt or equity forcing them to fund R&D projects with cash reserves. A recent study by Falato and Sim (2014) provides causal evidence that R&D is indeed an important determinant of firms' cash holdings. They use firm-level data in the US to show that firms' cash holdings increase (decrease) significantly in response to a rise (cut) in R&D tax credits, which vary across states and time. Furthermore, these effects are stronger for firms that have less access to debt/equity financing. These results suggest that due to the presence of financing frictions, firms need to hold cash to finance their R&D investment. We capture these cash requirements on R&D using a CIA constraint.

Under the CIA constraint on R&D, an increase in inflation that determines the opportunity cost of cash holdings raises the cost of R&D investment. Consequently, a higher inflation decreases R&D. Given that we remove scale effects<sup>1</sup> by considering a semi-endogenous-growth version of the Schumpeterian model in which the long-run rate of creative destruction is determined by exogenous parameters, a decrease in R&D leads to a decrease in the growth rate of technology only in the short run but decreases the level of technology in the long run. Although the rate of creative destruction decreases temporarily, the decrease in innovation in the long run decreases the number of labor-market vacancies relative to unemployed workers causing a positive effect on unemployment. In other words, due to the decrease in labor market tightness, a higher inflation increases unemployment in the long run. Under the CIA constraint on consumption, a higher inflation instead decreases unemployment in addition to stifling innovation and economic growth. Therefore, the two CIA constraints have drastically different implications on the long-run relationship between

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<sup>1</sup>See Jones (1999) for a discussion of scale effects in the R&D-based growth model.

inflation and unemployment. The empirical literature on inflation and unemployment also provides mixed results on the relationship between inflation and unemployment. For example, Ireland (1999), Beyer and Farmer (2007), Russell and Banerjee (2008) and Berentsen *et al.* (2011) document a positive relationship between inflation and unemployment in the US, whereas Karanassou *et al.* (2005, 2008) find a negative relationship between the two variables in the US and European countries. Our theoretical analysis provides a plausible and parsimonious explanation (via the relative magnitude of the two CIA constraints) on the different empirical relationships between inflation and unemployment. We calibrate our model to aggregate data in the US to explore quantitative implications and find that the model delivers a positive (negative) relationship between inflation and unemployment when we use data on M0 (M1) as the measure of money. Interestingly, when we calibrate the model to data in the Eurozone, we find that the model delivers a negative relationship between inflation and unemployment under both measures of money. We discuss intuition behind these results in the main text.

This study relates to the literature on Schumpeterian growth; see Segerstrom *et al.* (1990), Grossman and Helpman (1991) and Aghion and Howitt (1992) for seminal studies. However, these studies feature full employment rendering them unsuitable for the purpose of analyzing unemployment. Early contributions in the Schumpeterian theory of unemployment are Aghion and Howitt (1994, 1998), Cerisier and Postel-Vinay (1998), Mortensen and Pissarides (1998), Pissarides (2000), Şener (2000, 2001) and Postel-Vinay (2002).<sup>2</sup> The present study complements these seminal studies by introducing money demand into the Schumpeterian model with unemployment and analyzing the effects of inflation on unemployment and economic growth. To our knowledge, this combination of Schumpeterian growth, money demand and equilibrium unemployment is novel to the literature.

This study also relates to the literature on inflation and economic growth. In this literature, Stockman (1981) and Abel (1985) analyze the effects of inflation via a CIA constraint on capital investment in a monetary version of the Neoclassical growth model. Subsequent studies in this literature explore the effects of inflation in variants of the capital-based growth model. This study instead relates more closely to the literature on inflation and *innovation-driven* growth. In this literature, the seminal study by Marquis and Reffett (1994) analyzes the effects of inflation via a CIA constraint on consumption in a variety-expanding growth model based on Romer (1990). In contrast, we explore the effects of inflation in a Schumpeterian quality-ladder model. Chu and Lai (2013), Chu and Cozzi (2014) and Chu, Cozzi, Lai and Liao (2014) also analyze the relationship between inflation and economic growth in the Schumpeterian model. However, all these studies exhibit full employment due to the absence of matching frictions in the labor market. The present study provides a novel contribution to the literature by introducing equilibrium unemployment driven by matching frictions to the monetary Schumpeterian growth model. A recent study by Wang and Xie (2013) also analyzes the effects of inflation on economic growth and unemployment driven by matching frictions in the labor market. Their model generates money demand via CIA constraints on consumption and wage payment to production workers. In contrast, we model money demand via a CIA constraint on R&D. More importantly, they consider capital accumulation as the engine of economic growth whereas our analysis complements their interesting study by exploring a different growth engine that is R&D and innovation.

The rest of this study is organized as follows. Section 2 describes the Schumpeterian model. Section 3 provides a qualitative analysis on the effects of inflation on unemployment and economic growth. Section 4 presents our quantitative results. The final section concludes.

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<sup>2</sup>See also Parello (2010) who considers a Schumpeterian model with unemployment by efficiency wage.

## 2 A monetary Schumpeterian model with unemployment

In the Schumpeterian model, economic growth is driven by quality improvement. R&D entrepreneurs invent higher-quality products in order to dominate the market and earn monopolistic profits. When R&D entrepreneurs create new inventions, they open up vacancies to recruit workers from the labor market, in which the number of job separations is determined by creative destruction and the number of job matches is determined by an aggregate matching function and labor market tightness. Due to matching frictions between workers and firms with new technologies, the economy features equilibrium unemployment in the long run. Unlike the important precedent of Mortensen (2005), we (a) allow for population growth and remove the scale effect via increasing R&D difficulty as in Segerstrom (1998), (b) introduce money demand via CIA constraints on consumption and R&D investment as in Chu and Cozzi (2014), and (c) consider elastic labor supply.

### 2.1 Household

The representative household has  $L_t$  members, which increase at an exogenous rate  $g > 0$ . The household's lifetime utility function is given by

$$U = \int_0^{\infty} e^{-\rho t} [\ln c_t + \gamma \ln(L_t - l_t)] dt, \quad (1)$$

where  $c_t$  denotes the household's total consumption of final goods (numeraire) at time  $t$ . Each member of the household supplies one unit of labor, and  $l_t$  is the household's total supply of labor at time  $t$ . The parameter  $\rho > 0$  determines subjective discounting, and  $\gamma \geq 0$  determines leisure preference.

The asset-accumulation equation expressed in real terms is given by

$$\dot{a}_t + \dot{m}_t = r_t a_t - \pi_t m_t + i_t d_t + I_t - \tau_t - c_t. \quad (2)$$

$a_t$  is the real value of financial assets (in the form of equity shares in monopolistic intermediate goods firms) owned by the household.  $r_t$  is the real interest rate.  $\pi_t$  is the inflation rate.  $m_t$  is the real money balance accumulated by the household.  $d_t$  is the amount of money lent to R&D entrepreneurs subject to the following constraint:  $d_t + \xi c_t \leq m_t$ , where  $\xi \in [0, 1]$  parameterizes the strength of the CIA constraint on consumption. The interest rate on money lending  $d_t$  to R&D firms is the nominal interest rate,<sup>3</sup> which is equal to  $i_t = r_t + \pi_t$  from the Fisher identity.  $\tau_t$  is a lump-sum tax levied on the household.  $I_t$  is the total amount of labor income given by  $I_t \equiv w_t x_t + \omega_t R_t + b_t u_t$ ,<sup>4</sup> where  $w_t$  is the wage rate of production workers  $x_t$ ,  $\omega_t$  is the wage rate of R&D workers  $R_t$ , and  $b_t$  is unemployment benefits provided to unemployed workers  $u_t$  who are searching for jobs in the labor market. To ensure balanced growth, we assume that  $b_t = \bar{b} y_t / L_t$  is proportional to total output per capita, where  $\bar{b} \in (0, 1)$  is an unemployment-benefit parameter. Given the labor force  $l_t$ , the resource constraint on labor at time  $t$  is

$$x_t + R_t + u_t = l_t. \quad (3)$$

<sup>3</sup>It can be easily shown as a no-arbitrage condition that the interest rate on  $d_t$  must be equal to  $i_t$ .

<sup>4</sup>The household pools the different sources of labor income for sharing among all members.

The household chooses consumption  $c_t$  and labor supply  $l_t$  and accumulates assets  $a_t$  and money  $m_t$  to maximize (1) subject to (2), (3) and the CIA constraint  $d_t + \xi c_t \leq m_t$ . The resulting optimality condition for labor supply is

$$l_t = L_t - \frac{\gamma(1 + \xi i_t)c_t}{\omega_t}, \quad (4)$$

where the opportunity cost of leisure is the R&D wage rate  $\omega_t$  because individuals can freely choose between employment in the R&D sector and job search.<sup>5</sup> The intertemporal optimality condition is given by

$$-\frac{\dot{\zeta}_t}{\zeta_t} = r_t - \rho, \quad (5)$$

where  $\zeta_t$  is the Hamiltonian co-state variable on (2) and determined by  $\zeta_t = [(1 + \xi i_t)c_t]^{-1}$ . In the case of a constant nominal interest rate  $i$ , (5) becomes the familiar Euler equation  $\dot{c}_t/c_t = r_t - \rho$ .

## 2.2 Final goods

Final goods  $y_t$  are produced by perfectly competitive firms that aggregate a unit continuum of intermediate goods using the following Cobb-Douglas aggregator:

$$y_t = \exp \left\{ \int_0^1 \ln [A_t(j)x_t(j)] dj \right\}, \quad (6)$$

where  $A_t(j) \equiv q^{n_t(j)}$  is the productivity or quality level of intermediate good  $x_t(j)$ .<sup>6</sup> The parameter  $q > 1$  is the exogenous step size of each quality improvement, and  $n_t(j)$  is the number of innovations that have been invented *and implemented* in industry  $j$  as of time  $t$ . From profit maximization, the conditional demand function for  $x_t(j)$  is

$$x_t(j) = y_t/p_t(j), \quad (7)$$

where  $p_t(j)$  is the price of  $x_t(j)$  for  $j \in [0, 1]$ . All prices are denominated in units of final goods, chosen as the numeraire.

## 2.3 Intermediate goods

The unit continuum of differentiated intermediate goods are produced in a unit continuum of industries. Each industry is temporarily dominated by a quality leader until the arrival and implementation of the next higher-quality product. The owner of the new innovation becomes the next quality leader.<sup>7</sup> The current quality leader in industry  $j$  uses one unit of labor to produce one unit of intermediate good  $x_t(j)$ . We assume - as in Mortensen (2005) - that the employer has no outside

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<sup>5</sup>Given that R&D is essentially the search for a higher-quality product, there is no need to have it preceded by another search activity.

<sup>6</sup>Given we will assume that one unit of labor produces one unit of intermediate goods, we use  $x_t$  to denote both the quantity of intermediate goods and the quantity of production workers, for notational convenience.

<sup>7</sup>This is known as the Arrow replacement effect; see Cozzi (2007a) for a discussion of the Arrow effect.

option and the workers' outside option is unemployment benefit  $b_t$ . In this case, the generalized Nash bargaining game is<sup>8</sup>

$$\{x_t(j), w_t(j)\} = \arg \max\{[w_t(j) - b_t]x_t(j)\}^\beta \{[p_t(j) - w_t(j)]x_t(j)\}^{1-\beta}, \quad (8)$$

where the parameter  $\beta \in (0, 1)$  measures the bargaining power of workers. The bargaining outcome on wage is<sup>9</sup>

$$w_t(j) = \beta p_t(j) + (1 - \beta)b_t, \quad (9)$$

which is an average between the marginal revenue product  $p_t(j)$  of each worker and the value of unemployment benefit  $b_t$  weighted by the bargaining power of workers. The employer and workers commit to this wage schedule over the lifetime of the firm. Substituting (9) into (8) shows that the  $x_t(j)$  that maximizes (8) is the same as the  $x_t(j)$  that maximizes the following profit function:

$$\Pi_t(j) = [p_t(j) - w_t(j)]x_t(j) = (1 - \beta)[p_t(j) - b_t]x_t(j) = (1 - \beta)[y_t - b_t x_t(j)], \quad (10)$$

where the second equality uses (9) and the third equality uses (7).

In the original model in Grossman and Helpman (1991), the markup is assumed to be given by the quality step size  $q$ , due to limit pricing between the current and previous quality leaders. Here we follow Howitt (1999) and Dinopoulos and Segerstrom (2010) to consider a more realistic scenario in which new quality leaders do not engage in limit pricing with previous quality leaders because after the implementation of the newest innovations, previous quality leaders exit the market and need to search for workers before reentering. Given the Cobb-Douglas aggregator in (6), the unconstrained monopolistic price would be infinity (i.e.,  $x_t(j) \rightarrow 0$ ). We follow Evans *et al.* (2003) to consider price regulation under which the regulated markup ratio cannot be greater than  $z > 1$ .<sup>10</sup> The equilibrium price is

$$p_t(j) = z w_t(j) = z \frac{1 - \beta}{1 - \beta z} b_t, \quad (11)$$

where the second equality uses (9). We impose an additional parameter restriction given by  $\beta z < 1$ . Substituting (11) into (7) yields

$$x_t(j) = x_t = \frac{1 - \beta z}{(1 - \beta)z} \frac{y_t}{b_t} = \frac{1 - \beta z}{(1 - \beta)z \bar{b}} L_t, \quad (12)$$

where the last equality uses  $b_t = \bar{b} y_t / L_t$ . Finally, the amount of monopolistic profit is

$$\Pi_t(j) = \Pi_t = (p_t - w_t)x_t = \frac{z - 1}{z} y_t. \quad (13)$$

Given that the amount of monopolistic profit is the same across industries, we will follow the standard treatment in the literature to focus on the symmetric equilibrium, in which the arrival rate of innovations is equal across industries.<sup>11</sup>

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<sup>8</sup>Using a more general bargaining condition with the value functions of employment and unemployment would complicate the model without providing new insight; see for example footnote 3 in Mortensen (2005).

<sup>9</sup>This bargaining outcome can also be obtained from  $w_t(j) = \arg \max\{[w_t(j) - b_t]^\beta [p_t(j) - w_t(j)]^{1-\beta}\}$  (i.e., individual wage bargaining).

<sup>10</sup>This formulation enables us to separate the markup and the quality step size, allowing for a more realistic calibration exercise.

<sup>11</sup>See Cozzi (2007b) for a discussion of multiple equilibria in the Schumpeterian model. Cozzi *et al.* (2007) provide a theoretical justification for the symmetric equilibrium to be the unique rational-expectation equilibrium in the Schumpeterian model.

## 2.4 R&D

R&D is performed by a continuum of competitive entrepreneurs. If an R&D entrepreneur sinks  $\tilde{R}_t$  units of labor to engage in innovation in an industry, then she is successful in inventing the next higher-quality product in the industry with an instantaneous probability given by

$$\tilde{\delta}_t = \frac{h\tilde{R}_t}{A_t}, \quad (14)$$

where  $h > 0$  is an innovation-productivity parameter that captures the abilities of R&D entrepreneurs. We assume that innovation productivity  $h/A_t$  decreases in aggregate quality  $A_t \equiv \exp\left(\int_0^1 \ln A_t(j) dj\right)$  in order to capture increasing difficulty of R&D in the economy,<sup>12</sup> and this specification removes the scale effects in the innovation process of the quality-ladder model as in Segerstrom (1998).<sup>13</sup> The expected benefit from investing in R&D is  $V_t \tilde{\delta}_t dt$ , where  $V_t$  is the value of the expected discounted profits generated by a new innovation and  $\tilde{\delta}_t dt$  is the entrepreneur's probability of having a successful innovation during the infinitesimal time interval  $dt$ . To facilitate the payment R&D wages, the entrepreneur borrows money from the household, and the cost of borrowing is determined by the nominal interest rate  $i_t$ . To parameterize the strength of this CIA constraint on R&D, we assume that a fraction  $\sigma \in [0, 1]$  of R&D expenditure requires the borrowing of money from households. Therefore, the total cost of R&D is  $(1 + \sigma i_t) \omega_t \tilde{R}_t dt$ . Free entry implies

$$V_t \tilde{\delta}_t dt = (1 + \sigma i_t) \omega_t \tilde{R}_t dt \Leftrightarrow V_t = (1 + \sigma i_t) \omega_t A_t / h, \quad (15)$$

where the second equality uses (14).

## 2.5 Matching and unemployment

When an R&D entrepreneur has a new innovation, she is not able to immediately launch the new product to the market due to matching frictions in the initial recruitment of manufacturing workers.<sup>14</sup> Instead, she has to open up  $x_t$  vacancies to recruit  $x_t$  workers for producing and launching her products to the market. We follow the standard treatment in the search-and-matching literature to consider an aggregate matching function  $F(v_t, u_t)$ , where  $v_t$  is the number of vacancies in the labor market and  $u_t$  is the number of unemployed workers.  $F(v_t, u_t)$  has the usual properties of being increasing, concave and homogeneous of degree one in  $v_t$  and  $u_t$ . In the economy, the number of successful matches at time  $t$  is given by  $F(v_t, u_t)$ ; in other words, the number of workers who find jobs is  $F(v_t, u_t)$ . Therefore, the job-finding rate is

$$\lambda_t = F(v_t, u_t) / u_t = F(v_t / u_t, 1) \equiv M(\theta_t), \quad (16)$$

<sup>12</sup>See Venturini (2012) for empirical evidence based on US manufacturing data that supports the semi-endogenous growth model with increasing difficulty of R&D.

<sup>13</sup>Segerstrom (1998) considers an industry-specific index of R&D difficulty. Here we consider an aggregate index of R&D difficulty to simplify notation without altering the aggregate results of our analysis.

<sup>14</sup>Dinopoulos *et al.* (2013) consider an interesting setting, aimed at studying the importance of rent-seeking activities on unemployment, in which new firms are able to immediately recruit a fraction  $\phi \in (0, 1)$  of the desired number of workers  $x_t$ .



where  $\theta_t \equiv v_t/u_t$  denotes labor market tightness, and  $\lambda_t = M(\theta_t)$  is increasing in  $\theta_t$ . Similarly, the number of vacancies filled is also  $F(v_t, u_t)$ , so the vacancy-filling rate is

$$\eta_t = F(v_t, u_t)/v_t = M(\theta_t)/\theta_t, \quad (17)$$

where  $\eta_t = M(\theta_t)/\theta_t$  is decreasing in  $\theta_t$ . Following the usual treatment in the literature,<sup>15</sup> we assume that when matching occurs to a firm at time  $t$ , the firm matches with  $x_t$  workers simultaneously. In other words, the number of successful matches at time  $t$  is first determined by the matching function  $F(v_t, u_t)$ , and then, these matches are randomly assigned to  $F(v_t, u_t)/x_t$  firms. Therefore, the probability for a firm with opened vacancies to match with  $x_t$  workers at time  $t$  is also  $\eta_t$ . After an entrepreneur sets up her firm by having successful matches with  $x_t$  workers at time  $t$ , we assume for tractability that she can instantly recruit additional workers at the same wage schedule in (9) as demand  $x_t$  increases overtime.<sup>16</sup>

## 2.6 Asset values

Each unemployed worker faces the probability  $\lambda_t$  of being employed at any point in time. Once a worker is hired by a firm, he/she begins employment and faces the probability  $\tilde{\delta}_t$  of the next innovation being invented in his/her industry. After the innovation is invented, the worker faces the probability  $\eta_t$  of the next innovation being implemented and his/her firm being forced out of the market due to creative destruction. Let  $U_t$  denote the value of being unemployed. The familiar asset-pricing equation of  $U_t$  is

$$r_t = \frac{b_t + \dot{U}_t + \lambda_t(W_t - U_t)}{U_t}, \quad (18)$$

where  $\lambda_t$  is the rate at which an unemployed worker becomes employed and  $W_t$  denotes the value of being employed in an industry in which the subsequent innovation has not been invented. The asset-pricing equation of  $W_t$  is

$$r_t = \frac{w_t + \dot{W}_t + \tilde{\delta}_t(S_t - W_t)}{W_t}, \quad (19a)$$

where  $\tilde{\delta}_t$  is the rate at which the subsequent innovation is invented and  $S_t$  denotes the value of being employed in an industry in which the subsequent innovation has been invented but not yet been launched to the market.<sup>17</sup> The asset-pricing equation of  $S_t$  is

$$r_t = \frac{w_t + \dot{S}_t + \eta_t(U_t - S_t)}{S_t}, \quad (19b)$$

where  $\eta_t$  is the rate at which the subsequent innovation is launched to the market and the worker becomes unemployed. Given that a worker must be indifferent between being employed by an R&D

<sup>15</sup>See for example Mortensen (2005) and Dinopoulos *et al.* (2013).

<sup>16</sup>In other words, existing firms can hire additional workers without searching, but these additional workers are not necessarily newborn workers. It only happens to be the case that  $x_t$  grows at the same rate as  $L_t$ , as shown in (12). Here we assume  $g$  is sufficiently small such that it has negligible effects on the labor market.

<sup>17</sup>Unlike Mortensen (2005) who exogenously assumes that the current quality leader stops its operation as soon as the next innovation is *invented*, we allow the current quality leader to continue its operation until the next innovation is *implemented*. This generalization is rational for the current quality leader, who continues to earn profits, and also for the workers because  $S_t > U_t$ .

entrepreneur and engaging in job search, the wage of R&D workers is equal to

$$\omega_t = r_t U_t - \dot{U}_t. \quad (20)$$

The life cycle of an innovation can be described as follows. When an innovation is invented, its owner creates vacancies in the labor market to recruit workers, and the probability of successfully recruiting workers and beginning production at any point in time is  $\eta_t$ . Once an innovation is launched to the market, it faces the probability  $\tilde{\delta}_t$  of the next innovation being invented. The subsequent innovation cannot be invented until the current innovation has been launched to the market and directly observed.<sup>18</sup> After the next innovation is invented, the probability of it being launched to the market is  $\eta_t$ . Once the next innovation is launched to the market, the value of the current innovation becomes zero. Let  $V_t$  be the value of a new innovation for which its vacancies have not been filled. Its asset-pricing equation is given by

$$r_t = \frac{\dot{V}_t + \eta_t (Z_t - V_t)}{V_t}, \quad (21a)$$

where  $\eta_t$  is the rate at which the product is launched to the market. The asset-pricing equation of  $Z_t$ , which is the value of the innovation when its vacancies have been filled, is given by

$$r_t = \frac{\Pi_t + \dot{Z}_t + \tilde{\delta}_t (X_t - Z_t)}{Z_t}, \quad (21b)$$

where  $\tilde{\delta}_t$  is the rate at which the subsequent innovation is invented. The asset-pricing equation of  $X_t$ , which is the value of the current innovation when the subsequent innovation has been invented but not yet been launched to the market, is given by

$$r_t = \frac{\Pi_t + \dot{X}_t - \eta_t X_t}{X_t}, \quad (21c)$$

where  $\eta_t$  is the rate at which the subsequent innovation is launched to the market.

## 2.7 Government

The monetary policy instrument that we consider is the inflation rate  $\pi_t$ , which is exogenously set by the monetary authority. Given  $\pi_t$ , the nominal interest rate is endogenously determined according to the Fisher identity such that  $i_t = \pi_t + r_t$ , where  $r_t$  is the real interest rate. The growth rate of the nominal money supply is  $\mu_t = \pi_t + \dot{m}_t/m_t$ .<sup>19</sup> Finally, the government balances the fiscal budget subject to the following balanced-budget condition:  $\tau_t = b_t u_t - \mu_t m_t$ .

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<sup>18</sup>This assumption, shared by Mortensen (2005), captures the realistic feature of the intertemporal spillovers, of equally benefiting from patent description and actual use of the good. This aspect is often remarked in the microeconomic literature on innovation.

<sup>19</sup>It is useful to note that in this model, it is the *growth rate* of the money supply that affects the real economy in the long run, and a one-time change in the *level* of money supply has no long-run effect on the real economy. This is the well-known distinction between the neutrality and superneutrality of money. Empirical evidence generally favors neutrality and rejects superneutrality, consistent with our model; see Fisher and Seater (1993) for a discussion on the neutrality and superneutrality of money.

## 2.8 Steady-state equilibrium

We will define the *aggregate* innovation-arrival rate as  $\delta_t = (1 - f_t)\tilde{\delta}_t$ , where  $f_t$  is the measure of industries with unlaunched innovations. The outflow from the pool of firms searching for workers is given by  $\eta_t f_t$ , and the inflow into this pool is given by  $\delta_t$ . Therefore, in the steady state, we must have  $\eta_t f_t = \delta_t$ . The aggregate production function of final goods is given by  $y_t = A_t x_t$ , where (the log of) aggregate technology  $A_t$  is defined as

$$\ln A_t \equiv \int_0^1 \ln A_t(j) dj = \int_0^1 n_t(j) dj \ln q = \int_0^t \eta_v f_v dv \ln q, \quad (22)$$

where we have normalized  $A_0 = 1$  (i.e.,  $\ln A_0 = 0$ ). Differentiating (22) with respect to  $t$  yields  $\dot{A}_t/A_t = \eta_t f_t \ln q$ , where  $\eta_t f_t$  is the measure of industries with newly launched innovations at time  $t$ . The steady-state growth rate of  $A_t$  is

$$\frac{\dot{A}_t}{A_t} = \eta f \ln q = \delta \ln q = g, \quad (23)$$

where the third equality holds because  $\delta = hR_t/A_t$  must be constant on the balanced growth path implying that  $R_t$  and  $A_t$  must both grow at the exogenous rate  $g$  in the long run.<sup>20</sup> From the last equality of (23), the steady-state rate of creative destruction is determined by exogenous parameters such that  $\delta = g/\ln q$ .

On the balanced growth path, (20) becomes

$$\omega_t = (\rho + g) U_t. \quad (24)$$

Solving (18) and (19) yields the balanced-growth value of  $(\rho + g)U_t$  given by

$$(\rho + g)U_t = (\rho + g) \frac{(\rho + g + \eta)(\rho + g + \tilde{\delta})b_t + (\rho + g + \eta + \tilde{\delta})\lambda w_t}{(\rho + g + \eta)(\rho + g + \tilde{\delta})(\rho + g + \lambda) - \tilde{\delta}\lambda\eta}, \quad (25)$$

where  $\tilde{\delta} = \delta/(1 - f) = \delta/(1 - \delta/\eta)$ . From (21), the balanced-growth value of  $V_t$  is

$$V_t = \frac{\eta(\Pi_t + \tilde{\delta}X_t)}{(\rho + \eta)(\rho + \tilde{\delta})} = \frac{\rho + \eta + \tilde{\delta}}{(\rho + \eta)^2(\rho + \tilde{\delta})} \eta \Pi_t. \quad (26)$$

Substituting (24)-(26) into (15) yields

$$\frac{\rho + \eta + \tilde{\delta}}{(\rho + \eta)^2(\rho + \tilde{\delta})} \eta \Pi_t = \frac{A_t}{h} (1 + \sigma i) (\rho + g) \frac{(\rho + g + \eta)(\rho + g + \tilde{\delta})b_t + (\rho + g + \eta + \tilde{\delta})\lambda w_t}{(\rho + g + \eta)(\rho + g + \tilde{\delta})(\rho + g + \lambda) - \tilde{\delta}\lambda\eta}. \quad (27)$$

For convenience, we define a transformed variable  $\alpha_t \equiv A_t/L_t$ , which is the per capita level of aggregate technology. Substituting (11), (13) and  $b_t = \bar{b}y_t/L_t$  into (27) and then rearranging terms

<sup>20</sup>The semi-endogenous growth model does not require the growth rate of technology to be equal to the population growth rate. If we consider a more general specification  $\delta = hR_t/A_t^\chi$ , then  $\dot{A}_t/A_t = g/\chi$  in the long run. We consider a special case  $\chi = 1$  for simplicity. Furthermore, it is useful to note that it is the growth rate of R&D labor  $R_t$  that determines the growth rate of technology. However, in the long run, the growth rate of R&D labor coincides with the population growth rate to ensure a balanced growth path.

yield

$$\alpha = \frac{z-1}{(1+\sigma i)z\bar{b}} \frac{h}{(\rho+g)(\rho+\tilde{\delta})} \frac{(\rho+g+\eta)(\rho+g+\tilde{\delta})(\rho+g+\lambda) - \tilde{\delta}\lambda\eta}{(\rho+g+\eta)(\rho+g+\tilde{\delta}) + \lambda(\rho+g+\eta+\tilde{\delta})(1-\beta)/(1-\beta z)} \Theta(\theta), \quad (28)$$

where  $\tilde{\delta} = \delta/(1 - \delta/\eta)$ ,  $\lambda = M(\theta)$ ,  $\eta = M(\theta)/\theta$  and

$$\Theta(\theta) \equiv \frac{\eta}{\rho+\eta} \left( 1 + \frac{\tilde{\delta}}{\rho+\eta} \right).$$

We refer to (28) as the R&D free-entry (FE) condition, which contains two endogenous variables  $\{\alpha, \theta\}$ .<sup>21</sup> It is useful to note that the FE condition depends on the nominal interest rate  $i$  via the CIA constraint on R&D (i.e.,  $\sigma > 0$ ). From the R&D free-entry condition in (15), we have  $\alpha L = h[(1 + \sigma i)(\rho + g)]^{-1}V/U$ , where we have also used (24). Whenever an increase in labor market tightness  $\theta$  reduces the vacancy-filling rate  $\eta$  and increases the job-finding rate  $\lambda$ , it decreases the value  $V$  of an invention relative to the value  $U$  of unemployment, which in turn requires  $\alpha$  to fall in the long run in order for the R&D free-entry condition to hold. We summarize this result in Lemma 1.

**Lemma 1** *The FE curve describes a negative relationship between  $\alpha$  and  $\theta$  if  $\rho$  is sufficiently large.*

**Proof.** See Appendix A. ■

To close the model, we use the following steady-state condition that equates the inflow  $\delta$  into the pool of firms searching for workers to its outflow  $\eta f$ :

$$\delta = \eta f = \eta v/x = M(\theta)u/x, \quad (29)$$

where the second equality follows from  $fx = v$ , where  $f$  is the number of firms with opened vacancies and  $x$  is the number of vacancies per firm. The third equality in (29) follows from (17) and uses the definition of  $\theta \equiv v/u$ . Furthermore, we need to derive the equilibrium supply of labor  $l$ . Substituting (11), (24), (25),  $b_t = \bar{b}y_t/L_t$  and  $c_t = y_t$  into (4) yields

$$l(i, \theta)/L = 1 - \frac{\gamma(1+\xi i)}{(\rho+g)\bar{b}} \frac{(\rho+g+\eta)(\rho+g+\tilde{\delta})(\rho+g+\lambda) - \tilde{\delta}\lambda\eta}{(\rho+g+\eta)(\rho+g+\tilde{\delta}) + (\rho+g+\eta+\tilde{\delta})\lambda(1-\beta)/(1-\beta z)}, \quad (30)$$

which is increasing in  $\theta$  if  $\rho$  is sufficiently large as we will show in the proof of Lemma 2. Substituting (3), (12), (14) and (30) into (29) and applying the definition of  $\alpha \equiv A/L$  yield

$$\alpha = \frac{h}{\delta} \left\{ l(i, \theta)/L - \left[ 1 + \frac{\delta}{M(\theta)} \right] \frac{1-\beta z}{(1-\beta)z\bar{b}} \right\}. \quad (31)$$

We refer to (31) as the labor-market (LM) condition, which also contains two endogenous variables  $\{\alpha, \theta\}$ . It is useful to note that the LM condition depends on the nominal interest rate  $i$  via the CIA constraint on consumption (i.e.,  $\xi > 0$ ). From (14), we have  $\alpha = \frac{h}{\delta}R/L$ . An increase in

<sup>21</sup>Recall that  $\delta = g/\ln q$  is determined by exogenous parameters in the steady state.

labor-market tightness  $\theta$  reduces unemployment  $u$ , which in turn increases the supply of labor for R&D  $R$ . As a result of increased R&D, innovation becomes more difficult (i.e.,  $\alpha$  increases) in the long run, and this effect is present regardless of whether labor supply is elastic or inelastic. We summarize this result in Lemma 2. Finally, (28) and (31) can be used to solve for the steady-state equilibrium values of  $\{\theta, \alpha\}$ ; see Figure 1 for an illustration.

**Lemma 2** *The LM curve describes a positive relationship between  $\alpha$  and  $\theta$  if  $\rho$  is sufficiently large.*

**Proof.** See Appendix A. ■

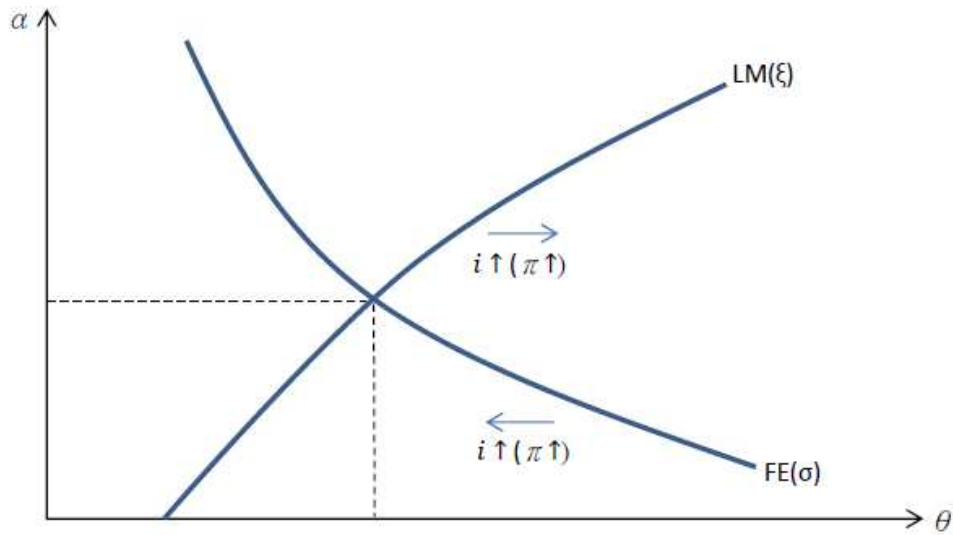


Figure 1: Steady-state equilibrium

### 3 Inflation, unemployment and economic growth

In this section, we explore the relationship between inflation, unemployment and economic growth. Section 3.1 considers the effects of inflation via the CIA constraint on R&D (i.e.,  $\sigma > 0$  and  $\xi = 0$ ). Section 3.2 considers the effects of inflation via the CIA constraint on consumption (i.e.,  $\sigma = 0$  and  $\xi > 0$ ).

#### 3.1 Inflation via the CIA constraint on R&D

In this subsection, we explore the effects of inflation on unemployment and economic growth under the CIA constraint on R&D. From the Fisher identity, we have  $i = \pi + r = \pi + \rho + 2g$ , where the second equality uses the Euler equation and  $\dot{c}_t/c_t = \dot{A}_t/A_t + g = 2g$ . Therefore, a one-unit increase

in the inflation rate leads to a one-unit increase in the nominal interest rate in the long run.<sup>22</sup> In Figure 1, we see that an increase in the nominal interest rate  $i$  (caused by an increase in inflation  $\pi$ ) shifts the FE curve to the left reducing labor market tightness  $\theta$  and the per capita level of technology  $\alpha$ . As for the resulting effect on unemployment  $u$ , we see from (29) that unemployment  $u = \delta x/M(\theta)$  (where  $\delta$  and  $x$  are determined by exogenous parameters and independent of  $i$ ) is decreasing in the job-finding rate  $M(\theta)$ . Therefore, the increase in inflation  $\pi$  raises unemployment  $u$  by reducing labor market tightness  $\theta$  and the job-finding rate  $M(\theta)$ . From (14), aggregate R&D is given by  $R = \alpha L\delta/h$ ; therefore, the higher inflation  $\pi$  (that decreases the level of technology  $\alpha$ ) also reduces R&D. Now we consider the effect of inflation on economic growth. The dynamics of per capita technology  $\alpha_t \equiv A_t/L_t$  is given by  $\dot{\alpha}_t/\alpha_t = \dot{A}_t/A_t - g$ . Therefore, given that a higher inflation  $\pi$  decreases the steady-state value of  $\alpha$ , it must also decrease the growth rate of  $A_t$  temporarily such that  $\dot{A}_t/A_t < g$  before  $\alpha_t$  reaches the new steady state. We summarize all these results in Proposition 1.

**Proposition 1** *Under the CIA constraint on R&D, a higher inflation has (a) a positive effect on unemployment, (b) a negative effect on R&D, (c) a negative effect on the growth rate of technology in the short run, and (d) a negative effect on the level of technology in the long run.*

**Proof.** Proven in text. ■

The intuition of Proposition 1 can be explained as follows. A higher inflation leads to an increase in the opportunity cost of cash holdings, which in turn increases the cost of R&D investment via the CIA constraint on R&D. As a result, R&D decreases resulting into a lower growth rate of technology in the short run and a lower level of technology in the long run. The negative relationship between inflation and R&D is consistent with the empirical evidence based on cross-sectional regressions in Chu and Lai (2013) and panel regressions in Chu, Cozzi, Lai and Liao (2014). The negative relationship between inflation and economic growth is also supported by the cross-country evidence in Fischer (1993), Guerrero (2006), Vaona (2012) and Chu, Kan, Lai and Liao (2014). Although the rate of creative destruction decreases temporarily, the decrease in innovation in the long run reduces labor-market vacancies relative to unemployed workers. Consequently, this reduction in labor-market tightness increases long-run unemployment. Therefore, under the CIA constraint on R&D, inflation and unemployment have a positive relationship in the long run, and this theoretical result is consistent with empirical studies, such as Ireland (1999), Beyer and Farmer (2007), Russell and Banerjee (2008) and Berentsen *et al.* (2011) who consider data in the US.

Finally, it is easy to see from the FE condition in (28) and Proposition 1 that relaxing the liquidity constraint on R&D (i.e., a decrease in  $\sigma$ ) would reduce unemployment and increase R&D and innovation.

### 3.2 Inflation via the CIA constraint on consumption

In this subsection, we explore the effects of inflation on unemployment and economic growth under the CIA constraint on consumption. In this case, Figure 1 shows that an increase in inflation  $\pi$  shifts

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<sup>22</sup>For example, Mishkin (1992) and Booth and Ciner (2001) provide empirical evidence for a positive relationship between inflation and the nominal interest rate in the long run.

the LM curve to the right increasing labor market tightness  $\theta$  and decreasing the level of technology  $\alpha$ . As for the resulting effect on unemployment  $u$ , we see from (29) that unemployment  $u = \delta x/M(\theta)$  is decreasing in the job-finding rate  $M(\theta)$ . Therefore, the increase in inflation  $\pi$  surprisingly reduces unemployment  $u$ . From (14), aggregate R&D is given by  $R = \alpha L\delta/h$ ; therefore, the higher inflation  $\pi$  also reduces R&D. As for the effect of inflation on economic growth, given that inflation  $\pi$  decreases the steady-state value of  $\alpha$ , it must decrease the growth rate of  $A_t$  temporarily before  $\alpha_t$  reaches the new steady state. We summarize these results in Proposition 2.

**Proposition 2** *Under the CIA constraint on consumption, a higher inflation has (a) a negative effect on unemployment, (b) a negative effect on R&D, (c) a negative effect on the growth rate of technology in the short run, and (d) a negative effect on the level of technology in the long run.*

**Proof.** Proven in text. ■

The intuition behind the negative relationship between inflation and unemployment can be explained as follows. A higher inflation leads to an increase in the opportunity cost of cash holdings, which in turn increases the cost of consumption relative to leisure. As a result, the household consumes more leisure and reduces labor supply. The decrease in labor supply reduces the number of workers searching for employment. The resulting increase in labor-market tightness decreases unemployment. Therefore, under the CIA constraint on consumption, inflation and unemployment have a negative relationship in the long run, and this theoretical result is consistent with empirical studies, such as Karanassou *et al.* (2005, 2008) who consider data in the US and Europe. Finally, it is easy to see from (30) and Proposition 2 that relaxing the liquidity constraint on consumption (i.e., a decrease in  $\xi$ ) would increase unemployment, R&D and innovation.

## 4 Quantitative analysis

In this section, we first calibrate the model to aggregate data in the US to explore quantitative implications. To facilitate this quantitative analysis, we follow the standard approach in the literature to specify a Cobb-Douglas matching function  $F(v_t, u_t) = \varphi v_t^\varepsilon u_t^{1-\varepsilon}$ , where the parameter  $\varphi > 0$  captures matching efficiency and the parameter  $\varepsilon \in (0, 1)$  is the elasticity of matches with respect to vacancies. Under this matching function, the job-finding rate becomes  $\lambda_t = \varphi \theta_t^\varepsilon$ , and the vacancy-filling rate becomes  $\eta_t = \varphi \theta_t^{\varepsilon-1}$ .

In summary, the model features the following structural parameters  $\{\rho, g, \beta, \bar{b}, z, q, \gamma, \xi, \sigma, \varepsilon, \varphi\}$  and a policy variable  $\pi_t$ . We follow Acemoglu and Akcigit (2012) to set the discount rate  $\rho$  to 0.05. We consider a long-run technology growth rate  $g$  of 1%. We follow Berentsen *et al.* (2011) to set  $\varepsilon = 1 - \beta = 0.28$ , so that the elasticity of matches with respect to vacancies is equal to the bargaining power of firms satisfying the Hosios (1990) rule. We calibrate  $\bar{b}$  to match data on unemployment benefits as a ratio of per capita income, which is about one quarter in the US. As for the inflation rate  $\pi$ , we consider a long-run value of 3%. Then, we calibrate the remaining parameters  $\{z, q, \gamma, \varphi, \sigma, \xi\}$  by targeting theoretical moments to empirical data. We calibrate the markup ratio  $z$  to match data on R&D as a share of GDP, which is about 3% in the US. We calibrate the quality step size  $q$ , which determines the rate of creative destruction  $\delta = g/\ln q$ , in order to match a long-run unemployment rate  $u/l$  of 6%. We calibrate the leisure parameter  $\gamma$  to match the

ratio of labor force to the working-age population (aged 16 to 64), which is about three quarters in the US. We calibrate matching efficiency  $\varphi$  to match a long-run average job-finding rate  $\lambda$  of 0.3, as estimated in Hall (2005). We calibrate the CIA-R&D parameter  $\sigma$  to match the semi-elasticity of R&D/GDP with respect to inflation  $\partial \ln(R\&D/GDP)/\partial \pi = 0.4$  estimated in Chu, Cozzi, Lai and Liao (2014). Finally, we calibrate the CIA-consumption parameter  $\xi$  to match the money-output ratio  $m/y$ . We consider two conventional measures of money: M0 and M1. In the US, the average M0-output ratio is about 0.06, whereas the average M1-output ratio is about 0.12. The calibrated parameter values are summarized in Table 1.

	$\rho$	$g$	$\bar{b}$	$\beta$	$\varepsilon$	$\varphi$	$z$	$q$	$\gamma$	$\xi$	$\sigma$
M0	0.05	0.01	0.25	0.72	0.28	0.17	1.30	1.65	0.24	0.05	0.43
M1	0.05	0.01	0.25	0.72	0.28	0.16	1.30	1.65	0.24	0.12	0.07

Given the above parameter values, we proceed to simulate the long-run Phillips curve (with inflation on the horizontal axis) in this calibrated US economy. Figure 2a shows an upward-sloping Phillips curve under the M0 specification, whereas Figure 2b shows a downward-sloping Phillips curve under the M1 specification. The intuition behind these contrasting results can be explained as follows. Under the M0 specification, the relatively low money-output ratio implies a small degree of CIA on consumption (i.e., a small  $\xi$ ). As a result, in order to match the empirical semi-elasticity of R&D with respect to inflation, the degree of CIA on R&D must be relatively large (i.e., a large  $\sigma$ ). In this case, the effect of inflation on unemployment works through mainly the R&D channel giving rise to a positive relationship between the two variables. Under the M1 specification, the relatively high money-output ratio implies a larger degree of CIA on consumption (i.e., a larger  $\xi$ ), which in turn is almost sufficient to deliver the empirical semi-elasticity of R&D with respect to inflation. As a result, the implied degree of CIA on R&D becomes much smaller (i.e., a much smaller  $\sigma$ ). In this case, the effect of inflation on unemployment works through mainly the consumption-leisure tradeoff giving rise to a negative relationship between the two variables. This ambiguous relationship between inflation and unemployment in the US is consistent with the contrasting empirical results in the literature.

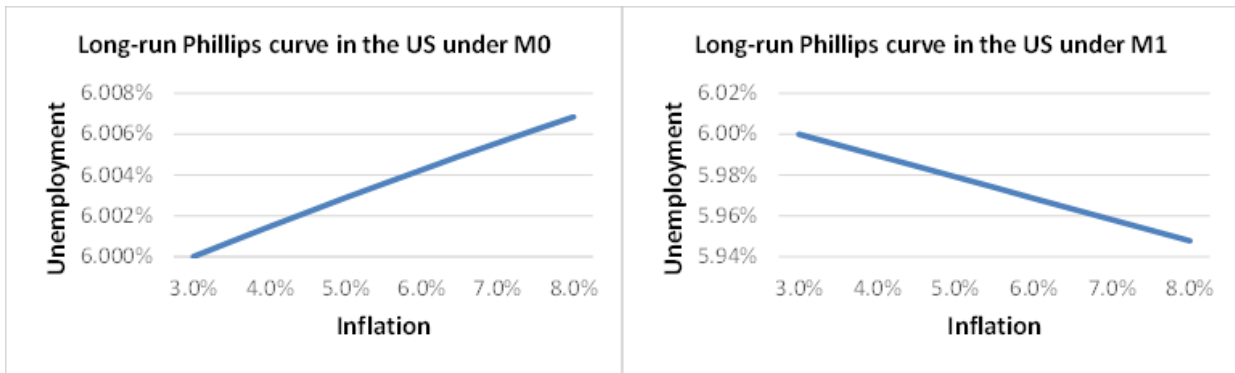


Figure 2a

Figure 2b

In the rest of this section, we recalibrate the model to the Eurozone, which features lower R&D, higher unemployment, lower job-finding rate, higher unemployment benefits and higher money-



output ratio than the US. Specifically, we consider an R&D-output ratio of 2%, a long-run unemployment rate of 9%, an average job-finding rate  $\lambda$  of 0.07,<sup>23</sup> and unemployment benefits as a ratio of per capita income of 0.4.<sup>24</sup> Finally, we consider the two measures of money as before: an average M0-output ratio of 0.08, and an average M1-output ratio of 0.4. Table 2 summarizes the calibrated parameter values.

	$\rho$	$g$	$\bar{b}$	$\beta$	$\varepsilon$	$\varphi$	$z$	$q$	$\gamma$	$\xi$	$\sigma$
M0	0.05	0.01	0.40	0.72	0.28	0.09	1.26	4.03	0.20	0.07	0.39
M1	0.05	0.01	0.40	0.72	0.28	0.09	1.26	4.03	0.20	0.40	0.04

Given the above parameter values, we proceed to simulate the long-run Phillips curve in this calibrated European economy. Figure 3a shows a downward-sloping Phillips curve under the M0 specification, whereas Figure 3b also shows a downward-sloping Phillips curve under the M1 specification. The reason why the Phillips curve is always downward sloping in this case is the stronger CIA friction on consumption, which in turn is implied by the higher money-output ratio in the Eurozone. Under the M0 specification, the calibrated value for the CIA-consumption parameter  $\xi$  is 0.07, compared to  $\xi = 0.05$  in the US. The stronger CIA friction on consumption in Europe implies that the effect of inflation on unemployment works through the consumption-leisure trade-off giving rise to a negative relationship between inflation and unemployment even under the M0 specification. This finding of a downward-sloping Phillips curve in Europe is consistent with the empirical evidence in Karanassou *et al.* (2005, 2008).

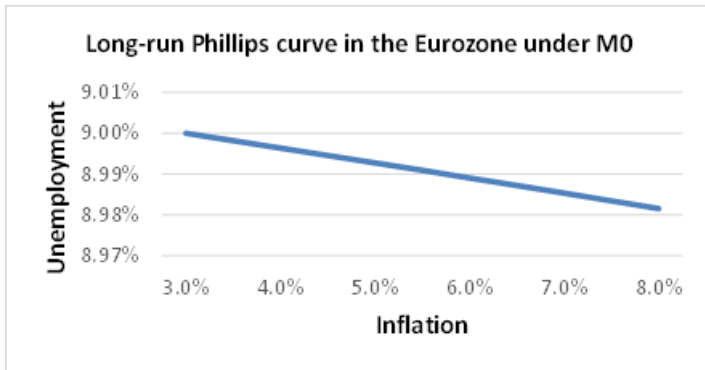


Figure 3a

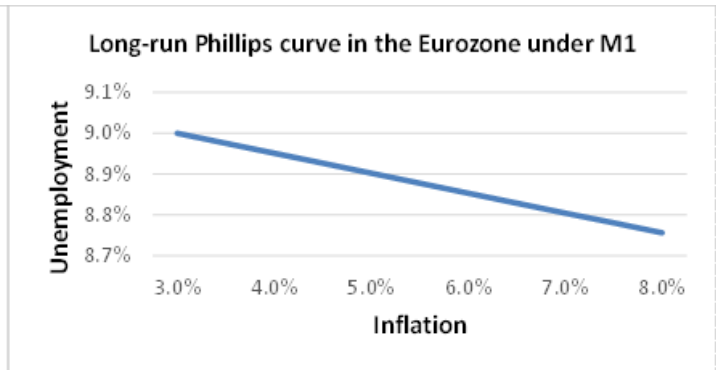


Figure 3b

## 5 Conclusion

In this study, we have explored a fundamental question in economics that is the long-run relationship between inflation, unemployment and economic growth. We consider a standard Schumpeterian

<sup>23</sup>See Hobijn and Sahin (2009) for estimates of the job-finding rates in a number of European countries.

<sup>24</sup>See Esser *et al.* (2013) for data on unemployment benefits in European countries.

growth model with the additions of money demand via CIA constraints and equilibrium unemployment driven by matching frictions in the labor market. In this monetary growth-theoretic framework with search frictions, we discover a positive (negative) relationship between inflation and unemployment under the CIA constraint on R&D (consumption), a negative relationship between inflation and R&D, and a negative relationship between inflation and economic growth. These theoretical predictions are largely consistent with empirical evidence.

An important policy implication from our analysis is that monetary expansion could be useful to reduce the rather high unemployment rate in the Eurozone, but that it would come at the expense of innovation and long-run technological competitiveness. A better policy prescription for the European banking authorities would be to manage to ease the liquidity problems that plague R&D activities. According to our results, this policy, unlike monetary expansion, would at the same time decrease unemployment and increase growth and technological competitiveness.

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## Appendix A

**Proof of Lemma 1.** First, we restrict the range of values for  $\theta$  to ensure that (a)  $\lambda = M(\theta) < 1$  (i.e., the number of workers who find jobs at a given point in time must be less than the number of workers searching for jobs at that time), (b)  $\eta = M(\theta)/\theta < 1$  (i.e., the number of vacancies filled at a given point in time must be less than the number of vacancies on the market at that time), and (c)  $\eta > \delta$  so that  $f = \delta/\eta < 1$  (i.e., the number of industries with unlaunched innovations must be less than the total number of industries, which is normalized to unity). Then, we examine each term on the right-hand side of (28) separately. The first term in (28) is independent of  $\theta$ , whereas the second term in (28) is decreasing in  $\theta$  given that  $\tilde{\delta}$  increases with  $\theta$ . The third term in (28) can be reexpressed as

$$\vartheta(\theta) \equiv (\rho + g) \frac{\rho + g + \tilde{\delta} + \lambda(1 + \frac{\tilde{\delta}}{\rho + g + \eta})}{\rho + g + \tilde{\delta} + \lambda(1 + \frac{\tilde{\delta}}{\rho + g + \eta})(1 - \beta)/(1 - \beta z)}. \quad (\text{A1})$$

Given  $(1 - \beta)/(1 - \beta z) > 1$ , we can show that  $\vartheta'(\theta) < 0$  holds if<sup>25</sup>

$$\{[1 - \delta\theta/M(\theta)]^2(\rho + g)/\delta + 1\}/\delta > 1/M'(\theta), \quad (\text{A2})$$

which holds if  $\rho$  is sufficiently large because  $1 - \delta\theta/M(\theta) = 1 - \delta/\eta > 0$ . As for the fourth term in (28), noting  $\eta = M(\theta)/\theta$  and  $\tilde{\delta} = \delta/[1 - \delta\theta/M(\theta)]$ , we can show that  $\Theta'(\theta) < 0$  holds if and only if<sup>26</sup>

$$\frac{\rho}{\delta} \underbrace{\left( [1 - \delta\theta/M(\theta)]^2 + \frac{2\delta [1 - \delta\theta/M(\theta)] \theta/M(\theta)}{\rho\theta/M(\theta) + 1} \right)}_{\equiv \chi(\theta)} > 1. \quad (\text{A3})$$

Note that  $\chi(\theta) > 0$  because  $\rho > 0$  and  $1 - \delta\theta/M(\theta) = 1 - \delta/\eta > 0$ . Therefore, we can conclude this proof by saying that a large value of  $\rho$  is a sufficient (but not necessary) condition for the FE curve in (28) to be downward sloping in  $\theta$ . ■

**Proof of Lemma 2.** By (30) and (A1),  $l(i, \theta)/L = 1 - \vartheta(\theta)\gamma(1 + \xi i)/((\rho + g)\bar{b})$ . From the proof of Lemma 1,  $\vartheta(\theta)$  is decreasing in  $\theta$  if  $\rho$  is sufficiently large. Together with (31), one can easily show that the LM curve is upward sloping in  $\theta$ . ■

<sup>25</sup>Note that  $\vartheta'(\theta) < 0$  holds if and only if

$$(\rho + g + \tilde{\delta}) \left[ \lambda \left( 1 + \frac{\tilde{\delta}}{\rho + g + \eta} \right) \right]' > \tilde{\delta}' \lambda \left( 1 + \frac{\tilde{\delta}}{\rho + g + \eta} \right),$$

which can be expressed as

$$\lambda(\rho + g + \tilde{\delta}) \left[ \frac{\tilde{\delta}'(\rho + g + \eta) - \eta'\tilde{\delta}}{(\rho + g + \eta)^2} \right] > [\tilde{\delta}'\lambda - (\rho + g + \tilde{\delta})\lambda'] \left( 1 + \frac{\tilde{\delta}}{\rho + g + \eta} \right).$$

Given  $\lambda' > 0$ ,  $\eta' < 0$ , and  $\tilde{\delta}' > 0$ , this holds if  $\tilde{\delta}'\lambda - (\rho + g + \tilde{\delta})\lambda' < 0$ , which is equivalent to (A2) by  $\lambda = M(\theta)$ ,  $\tilde{\delta} = \delta/[1 - \delta\theta/M(\theta)]$ , and  $\tilde{\delta}' = \tilde{\delta}^2 [M(\theta) - \theta M'(\theta)]/M(\theta)^2$ . Note that  $M(\theta) > \theta M'(\theta)$  by the properties of  $M(\theta)$ .

<sup>26</sup>Note that

$$\Theta'(\theta) = \frac{\varkappa'(\theta)}{[1 - \delta\varkappa(\theta)]^2 [\rho\varkappa(\theta) + 1]^2} \left[ \delta - \rho \left( [1 - \delta\varkappa(\theta)]^2 + \frac{2\delta\varkappa(\theta) [1 - \delta\varkappa(\theta)]}{\rho\varkappa(\theta) + 1} \right) \right],$$

where  $\varkappa(\theta) \equiv \theta/M(\theta)$  and thus  $\varkappa'(\theta) > 0$ .