The Entropic Linkage between Equity and Bond Market Dynamics

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Abstract: An alternative derivation of the yield curve based on entropy or the loss of information as it is communicated through time is introduced. Given this focus on entropy growth in communication the Shannon entropy will be utilized. Additionally, Shannon entropy’s close relationship to the Kullback–Leibler divergence is used to provide a more precise understanding of this new yield curve. The derivation of the entropic yield curve is completed with the use of the Burnashev reliability function which serves as a weighting between the true and error distributions. The deep connections between the entropic yield curve and the popular Nelson–Siegel specification are also examined. Finally, this entropically derived yield curve is used to provide an estimate of the economy’s implied information processing ratio. This information theoretic ratio offers a new causal link between bond and equity markets, and is a valuable new tool for the modeling and prediction of stock market behavior.

Keywords: Shannon entropy; Kullback–Leibler divergence; yield curve; volatility; Cauchy distribution; phase transition

1. Introduction

Entropy and information theory have been used in the past to study issues in economics and finance. Thiel and Lenders [1] and Fama [2] utilized information theory to test for dependence between price changes in the Amsterdam and New York Stock Exchanges respectively. Evidence of dependence would cast doubt on the random walk hypothesis. The Amsterdam market exhibited a much greater degree of dependence than the NYSE’s minimal level. Philippatos and Nawrocki [3] used the same techniques and a later data set found stronger evidence of dependence in the NYSE than Fama.

Bariviera et al. [4] and Zunino et al. [5,6] analyzed the informational efficiency of the oil, sovereign bond, and corporate bond markets using permutation entropy and permutation statistical complexity. Employing these concepts the authors described the time evolution of the efficiency these markets and the relative efficiencies of separate market components. Risso [7] utilized entropic concepts to study the relationship between informational efficiency and the probability of large declines in various stock markets. Risso found that as informational efficiency decreases the probability of a market crash rises. Using a different model this paper will look at the relationship between information processing inefficiencies and the emergence of bear markets.

Parker [8] demonstrated how changes in the level and variance of the information processing rate in a securities market could lead to various regimes of return volatility behavior. This framework is now extended with the presentation of an entropically motivated yield rate curve. As demonstrated empirically, this novel structure provides an important new causal link between the dynamics of the bond and equity markets.
2. Materials and Methods (Entropic Yield Curve)

Because of its fundamental importance in the communications theory, Shannon entropy will be used to develop the communications based model used in this paper. While Shannon entropy shares some structural similarities with the Thermodynamic Entropy there are some important differences. Ben-Naim [9] discusses these differences in detail. One important distinction relevant for this paper is the fact that Shannon entropy can change over time whereas the Thermodynamic Entropy of a closed system does not. As will be shown the growth of Shannon entropy in the entropic yield curve represents the loss of information in the economy.

The loss of information or the growth of entropy in the economy is assumed to arise from two primary sources. These sources are the natural decay of the current set of information about the economy over time and a non-zero error in the processing of that current information set. This interplay of information diffusion and processing errors determines the total entropy of an economy. The entropic yield curve defines the average growth rate of entropy at any time \( t \).

If all information is perfectly incorporated into prices with no error, prices will evolve identically with information Ross [10]. However physical limits on information processing make perfect contemporaneous reflection of all information in prices impossible Sims [11]. Instantaneous and perfect utilization of all economic information would imply economic agents with infinite bandwidth and faster than light communication and processing. There will always be at least a non-zero time lag in information processing and arguably some error in that processing. The time lag ultimately results in a trade off in terms of completeness of information collection and processing speed.

2.1. Entropic Yield Curve Initial Derivation

The zero rate curve is also known as the yield curve since it is the yield of a zero-coupon bond with maturity \( t \), where \( r = r(0, t) \) is the zero rate between time 0 and \( t \) (see Stefanica [12]). In this section a new yield curve will be developed based on entropic arguments. To help facilitate the derivation, the finding of Theorem 2 from Ross [10] will be assumed. Specifically, Ross utilized a martingale no-arbitrage approach to prove that the variance of price change must equal the variance of information flow or else arbitrage would be possible. Ross additionally proved with Theorem 2 that price and information changes are perfectly correlated.

Information and bond price will be assumed to be driven by the Brownian motion type processes below respectively:

\[
P_t = P_0 \sqrt{t}; \quad I_t = I_0 \sqrt{t}
\]

(1)

Solving for \( \sqrt{t} \) and equating both expressions results in the ratio below:

\[
\frac{P_t}{P_0} = \frac{I_t}{I_0}
\]

(2)

Bond growth and information diffusion assumptions:
An interest rate \( r \) is defined by the typical relationship between intertemporal prices:

\[
P_t = P_0 e^{rt}; \quad \frac{P_t}{P_0} = e^{rt}
\]

(3)

Substituting \( \frac{P_t}{P_0} = e^{rt} \) and \( I_t = I_0 \sqrt{t} \) into the ratio (2) yields:

\[
e^{rt} = \frac{I_0 \sqrt{t}}{I_0}
\]

(3)

\[
e^{rt} = \sqrt{t}
\]

(4)
Therefore with errorless and instantaneous processing:

\[ r = \frac{\ln \sqrt{t}}{t} \]  

(5)

The assumption of perfect price and information correlation will now be relaxed to allow for the introduction of errors in the price response. Assume a computational error or processing lag affects the price response as seen below. Depending on the value of the error term \( \sigma \) price diffusion could be magnified or suppressed:

\[ P_t = \frac{P_0}{\sigma} \sqrt{t}; \quad I_t = I_0 \sqrt{t} \]  

(6)

\[ e^{rt} = \frac{\sqrt{t}}{\sigma} \]  

(7)

\[ rt = \ln \sqrt{t} - \ln \sigma \]  

(8)

\[ r = \frac{\ln \sqrt{t} - \ln \sigma}{t} \]  

(9)

The equation above represents the total time averaged loss of information by the economy through time period \( t \). A more precise description of the entropic yield curve follows from the perspective of a weighted Kullback–Leibler divergence follows.

2.2. Entropic Yield Curve, Kullback–Leibler Divergence, and the Implied Information Processing Rate

The Shannon entropy is intimately related to another fundamental quantity from information theory, the Kullback–Leibler divergence. In fact the Shannon entropy can be easily represented in the form of Kullback–Leibler divergence. Despite this equivalence, the Kullback–Leibler provides another informative perspective from which to analyze the entropic yield curve.

The relative entropy \( D(p \| q) \) is a measure of the inefficiency of utilizing distribution \( q \) instead of the true distribution of \( p \) Cover [13]:

\[
D(p \| q) = \sum_{x \in X} p(x) \log \frac{p(x)}{q(x)} = E_p \log \left( \frac{p(x)}{q(x)} \right) 
\]

(10)

\[
= \sum_{x \in X} p(x) \log(p(x)) - \sum_{x \in X} p(x) \log(q(x)); \quad H(x) = E_p \log(q(x)) 
\]

(11)

\[
= -H(x) - E_p \log(q(x)). 
\]

(12)

Use of the approximate distribution \( q \) implies \( H(x) + D(p \| q) \) bits instead of \( H(x) \) bits on average to describe a random variable. In other words, information in the amount of \( D(p \| q) \) bits is being lost as entropy increases through this inefficiency.

Let:

\[
\text{Total Entropy} = \quad \text{Entropy of True System} \\
\]  

+ Entropy gain (information loss) due to approximation

\[
\text{Entropy of True System} = \sum_{x \in X} E_p \log(p(x)) = (1) * \ln \left( \sqrt{t} \right) = \ln \left( \sqrt{t} \right) 
\]

(13)

\[
\text{Entropy gain (information loss) due to approximation} = D(\sqrt{t} \| \sigma) \\
= \sum_{x \in X} p(x) \ln \sqrt{t} - \sum_{x \in X} p(x) \ln \sigma \\
= H(x) + D(p \| q) \text{ bits on average} 
\]

(14)

\[
= -\ln \left( \sqrt{t}^{-1} \right) + D \left( \sqrt{t}^{-1} \| \sigma \right) 
\]

(15)
\[
= \ln(\sqrt{t}) + \sum_{x \in X} p(x)\ln\left(\frac{\sqrt{t}}{\sigma}\right)
\]

(17)

\[
= \ln(\sqrt{t}) + E_p\ln\left(\frac{\sqrt{t}}{\sigma}\right)
\]

(18)

\[
= \ln(\sqrt{t}) - (p)\ln(\sqrt{t} - 1) - (p)\ln(\sigma)
\]

(19)

\[
= \ln(\sqrt{t}) - (p)\ln(\sqrt{t}) - (p)\ln(\sigma)
\]

(20)

\[
= (1 - p)\ln(\sqrt{t}) - (p)\ln(\sigma)
\]

(21)

Information is lost as it is collected, modeled and communicated through time in a fashion similar to the more familiar concept of information loss as it is communicated through space as studied by Shannon [14] and Burnashev [15]. In the equation above \( p \) represents the probability of an error and also serves as the weighting in the Kullback–Leibler divergence.

In the extreme if there is perfect information processing without error or time lag then \( p = 0\% \) and \( r \) is only determined by the diffusion of information:

\[
r = \frac{\ln(\sqrt{t})}{t}
\]

(22)

In the converse if information processing is completely flawed then \( p = 100\% \):

\[
r = \frac{\ln(\sigma)}{t}
\]

(23)

Further developing the metaphor, the communication of information in the economy will be modeled as a discrete memory less channel (DMC) with feedback. This system will utilize variable length codes to transmit information. This description is motivated by both in the realism and practicality.

The assumption of this structure is based on the fact that DMC’s with feedback are ubiquitous in computer and communication networks and thus ultimately a major component our economic system’s communication structure Polyanskiy et al. [16]. DMC’s use feedback to reduce error in transmissions. If a transmission has been received with an error, the receiver can request that the transmitter resend the message. Alternatively the transmitter may await confirmation that the message has been received without error before sending the next message. If this confirmation is not received within a specified time the message is automatically resent.

The practicality of the DMC model in this context results from the fortunate availability of a precise computational tool to estimate the reliability of such communication. In 1976 Burnashev [15] published the groundbreaking result of being able to characterize the reliability of a (DMC) with feedback utilizing variable length codes (see also Polyanskiy et al. [16] and Berlin et al. [17]). This reliability can be precisely computed at all rates of transmission with a relatively simple formula:

\[
p = e^{-C_1(1 - \xi)}
\]

(24)

where \( R \) is a transmitted message and \( C \) is the channel capacity of the transmitter.

The Burnashev error exponent is used to represent \( p \) or probability of error in the entropic yield curve. The rate of interest as modeled by the entropic yield curve is the average rate of entropy growth or information loss over the time period \( t \):

\[
r = (1 - p)\frac{\ln(\sqrt{t})}{t} - (p)\frac{\ln(\sigma)}{t}
\]

(25)
\[ r = \left( 1 - e^{-C_1(1-\xi)} \right) \frac{\ln(\sqrt{t})}{t} - \left( e^{-C_1(1-\xi)} \right) \frac{\ln(\sigma)}{t} \]  

(26)

\( \frac{R}{C} \) is the implied relative information processing rate

The Implied Information Processing Rate (IIPR) or \( \frac{R}{C} \) can be estimated by matching the entropic yield curve to the observed yields in the markets and then solving for IIPR. Despite their seemingly disparate theoretical origins, the entropic yield curve and the popular Nelson–Siegel [18,19] model share deep similarities as seen in the next section.

2.3. The Entropic Yield Curve vs. the Nelson–Siegel Specification

Figures 1 and 2 below illustrates the contribution of the two main terms to the structure of the entropic yield curve (ignoring for now the \( p \) factor) compared to the Nelson–Siegel specification. The structures bear a striking resemblance to one another despite their different derivations. Just as with the Nelson–Siegel specification almost any conceivable structure of the yield curve can be constructed with the appropriate parameterization and combination of the two decomposed curves making up the entropic yield curve.

Figure 1. Decomposed Entropic Yield Curve.

Figure 2. Decomposed Nelson–Siegel Yield Curve (See Nelson Siegel, 1985).

Nelson and Siegel [18,19] derived a popular and parsimonious technique for modeling the yield curve. Nelson–Siegel first modeled forward rate curves as the solutions to ordinary...
differential equations. Their yield curve could be then modeled as an average of these forward rate curves. They further used simulations to drop extra parameters and develop a final efficient form. The parameters of their model are ultimately “initial conditions” empirically derived to adjust the shape of their yield curve to fit reality. The parameters have no traditional economic or financial meaning. Although less theoretically rigorous in its construction than other methods, the Nelson Siegel model has proven to be more accurate than other yield curve modeling methods subsequently developed by academics.

Nelson and Siegel [18,19] demonstrated that a transformation of their yield curve by manipulation of the parameter \( \alpha \) (or \( -\beta_2 \)) produced most of the typical shapes of the yield curve as seen in the reproduction below. This parameter had no true economic, financial or other interpretation, other than its demonstrated utility in adjusting the curve to fit those observed in reality.

The Nelson–Siegel parameter \( \alpha \) (or \( -\beta_2 \)) has an equivalent representation (in terms of function) in the Entropic Yield Curve. This equivalent parameter is the ratio at the heart of this paper \( R/C \).

As the values of \( R/C \) vary from 1.9 to 0.1 (bottom to top) the resulting curves appear nearly identical to the variety and style produced by varying Nelson–Siegel’s nondescript parameter as seen below in Figure 3 using the parameter settings in Table 1:

Nelson–Siegel [18,19]:

\[
 r(m) = B_0 + (B_1 + B_2) \left( \frac{1-e^{-\frac{m}{\tau}}}{m\tau} \right) - B_2 e^{-\frac{m}{\tau}} 
\]  

(27)

Entropic Yield Curve:

\[
 r_{parker} = B_0 + \frac{\ln(\sqrt{7})}{\tau} \left( 1 - e^{-C_1(1-\frac{R}{C})} \right) - \frac{\ln(\sigma_0)}{\tau} \left( e^{-C_1(1-\frac{R}{C})} \right) 
\]  

(28)

![Figure 3. Yield Curve Shapes (R/C = 1.9 to 0.1).](image)

**Table 1.** Parameter settings used in Entropic Yield Curve above. (Time starts at \( t = 1 \))

<table>
<thead>
<tr>
<th>( R )</th>
<th>( C )</th>
<th>( \sigma )</th>
<th>( C_1 )</th>
<th>( B_0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.9 to 0.1</td>
<td>1</td>
<td>1.1</td>
<td>0.9</td>
<td>2</td>
</tr>
</tbody>
</table>

However unlike the Nelson–Siegel specification, in the Entropic Yield Curve the various shapes are generated by a variable with an intuitive origin. The normal upward sloping yield curve is
generated in an environment where the information arrival and processing rates are approximately equal as seen in the center curve ($R/C \approx 1$). When $R/C \gg 1$ or $\ll 1$ information is either arriving much faster or much slower than it can be processed in the economy resulting in the curves at the bottom and top of the chart respectively.

Currency in economy that cannot process current information efficiently is inherently less valuable than that of an economy accurately processing all arriving information. The amount of interest needed to separate currency holders from their money when $R/C \gg 1$, is significantly less than when $R/C \approx 1$. Alternatively when an economy is able to absorb all information the value of its currency will likely rise and the associated interest needed to separate the fortunate currency holder from her money will rise.

2.4. The Various Regimes of the Entropic Yield Curve

The various typical regimes of the yield curve are presented below in Figure 4. The three most familiar are the normal increasing, inverted, and flat below. The normal curve generated when $R$ is equal to or slightly greater than $C$, and is typically associated with a healthy and growing economy. On the other hand an inverted yield curve is generated when $C$ is much greater than $R$ in indicative of a slowdown in the economy. As the economy fluctuates between these two regimes in either direction, a flat yield curve may arise as seen in the lower left of Figure 4.

![Figure 4. Entropic Yield Curve Regimes.](image)

2.5. Simulation: Level of $R/C$ vs. Variance of $R/C$

Next a simulation was run to better understand the dynamics of the $R/C$. Specifically the variance of $R/C$ over different levels of $R/C$ varied was examined. To isolate the relationship between the $R/C$ level and variance, the variance of interest rates was held constant throughout.

The variance of $R/C$ was modified by the adjustment of a multiplier $M$ as seen in the equation below. $M$ is multiplied by a variable which is $N \sim (0, 1)$. At each mean value of $R/C$ from 0.1 to 2.1, $M$ was adjusted such that the average variance of the rates $r(t)$ remained constant at each level of $R/C$. This simplifying assumption highlights the relationship between the level and variance of $R/C$ without the confounding effect of interest rate variability changes:

$$
\frac{R}{C} (Total) = \left( \frac{R}{C} + M \ast N \sim (0, 1) \right)
$$

(29)
The level of the average variance of the solved interest rates was held constant by solving for a multiplier $M$ at each $R/C$

$$r(t) = \left(1 - e^{-C_1(1 - \frac{x}{(\text{Total}))}}\right) \frac{\ln\left(\sqrt{t}\right)}{t} - \left(e^{-C_1(1 - \frac{x}{(\text{Total}))}}\right) \frac{\ln(\sigma)}{t}$$  \hspace{1cm} (30)

where:

$$\frac{R}{C}(\text{Total}) = \left(\frac{R}{C} + M * N(0,1)\right)$$  \hspace{1cm} (31)

The results of the simulation are presented in Figure 5 below. There is an inverse relationship between the level and variance of $R/C$. The potential causes and implications of changes in the variance of $R/C$ are presented in the next section.

![Figure 5. Variance of $R/C$ versus Level of $R/C$.](image)

2.6. Harbinger of the Bears

Next the ratio $R/C$ will be used to elucidate a new entropic linkage between the bond and equity markets. Parker [8] demonstrated:

... that ratio of these rates $R/C$ or $(CC_A/CC_L)$ can determine different regimes of normal and “anomalous” behaviors for security returns”. As this ratio evolves over a continuum of values, security returns can be expected to go through phase transitions between different types of behavior. These dramatic phase transitions can occur even when the underlying information generation mechanism is unchanged. Additionally when the information arrival and processing rates are assumed to fluctuate independently and normally, the resulting ratio $(CC_A/CC_L)$ is shown to be Cauchy distributed and thus fat tailed . . .

—Edgar Parker [8]

For more information on the Cauchy distribution as the ratio of Normal variables see Marsaglia [20].

Parker [8] also showed how an increase in the variance of $C$ could lead to a similar outcome as a simple increase in the level of $C$. If initially $R$ is assumed to be $N \sim (0, 1)$ and $C$ constant, then the ratio $R/C$ is also normally distributed. However when both $R$ and $C$ are normally distributed it can be shown that the ratio $R/C$ will then be Cauchy Distributed. Cauchy distributions actually have nonfinite (or undefined) means and variances. This results in fatter tails which cause extreme events to occur much more frequently compared to a process modeled with the normal distribution. The transformation of $R/C$ from a normal to a Cauchy type distribution resulting from a change in $C$ from constant to $N \sim (0, 1)$ is illustrated in Figure 6 below.

The transformation of the relative information processing ration $R/C$ from a normal to Cauchy distribution leads to unpredictable explosions and collapses in the amount of unprocessed information
in the economy. Companies cannot efficiently process information and massive information loss (or entropy growth) occurs relative to periods of more stable information and information processing growth. Additionally future information processing resource allocation and planning cannot be reliably made during such unstable periods. These factors ultimately lead to a collapse in economic growth and to the stock market collapses Parker [8], and by similar reasoning the emergence of bear markets.

Figure 6. Cauchy vs. normal distributions.

3. Results

Empirical data from the Treasury and Equity markets will be utilized to further motivate the discussion. All R/C historical data used in the paper is available online at http://www.relativechannelcapacity.com/r-c.html and all Treasury Yield Curve rates can be found at https://www.treasury.gov/resource-center/data-chart-center/Pages/index.aspx. Figure 7 presents graphs of the actual daily closing value of the SP500 and the calculated R/C over the period 1990–2016. A simple daily estimate of R/C is calculated by first fixing the values of the parameters $C, C_1$, and $\sigma$ all equal to 1 and the long term factor $B_0 = 30$ year rate. $R$ is then estimated by minimizing the RMSE of the estimated $(1, 3, 6)$ monthly yield rates, and $(1, 2)$ year yields rates vs. the corresponding true yield rates. See the Supplementary Materials for a copy of the excel file with the macro used to estimate R/C. More precise curve fitting methods such as those commonly used for Nelson–Siegel (and other models) could be utilized, but this simple method is sufficient for the purposes of the demonstration that follows:

$$r = B_0 + \left(1 - e^{-C_1 \left(1 - \frac{\varepsilon}{t}\right)}\right) \frac{\ln\left(\sqrt{t}\right)}{t} - \left(e^{-C_1 \left(1 - \frac{\varepsilon}{t}\right)}\right) \frac{\ln(\sigma)}{t}$$

(32)

During the bull markets in zones I, III, and V, the ratio R/C is relatively stable. This means that information growth and processing growth are relatively balanced, stable and predictable. The economy is efficiently processing available information and there is processing capacity which is being added at a stable rate.

However in periods II and IV the variance of R/C changes dramatically. Excess or unprocessed information levels explode and collapse in an unpredictable fashion. The relationship between information growth and processing growth is no longer predictable. Companies cannot effectively allocate processing resources and overall processing suffers. The economy falters and the bear markets emerge immediately after the zone of dramatic instability in R/C.

As discussed earlier the dramatic changes in the nature of R/C may be due to a transition in the variability of $C$. Over an economic expansion such as period I both $R$ and $C$ steadily rise. Towards the end of an expansion the growth of $C$ may be limited by the available level of technology while $R$ growth can be effectively infinite. Once $C$ nears its maximum level, its variability may increase (Similar to communication networks or computers near their channel capacities or information processing
maximums). The phase transition in the stability of $R/C$ may also be due to shocks in $R$ and/or $C$. As $R/C$ moves into a more Cauchy like behavior markets peak and begin to fall. Some companies go out of business while others reorganize resources. Information processing stabilizes even as markets fall, and eventually the economy recovers as seen in periods III and V.

Figure 7. $R/C$ vs. SP500 (1990–2016).

Figure 7 (above) presents graphs of the actual daily closing value of the SP500 and the calculated implied $R/C$ over the period 1990–2016 while Table 2 below presents the calculated mean and variance of $R/C$ during the indicated time periods. In the final Figure 8 below a rolling window of the variance of $R/C$ is presented. Figures 7 and 8 show that the mean and variance of $R/C$ in zones II and IV are undefined which is indicative of a Cauchy type distribution. Note the inverse relationship between the variance and level of $R/C$ which are similar to the results of the simulation.

Table 2. Mean and Variance of $R/C$.

<table>
<thead>
<tr>
<th>Time Period</th>
<th>Mean</th>
<th>Variance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total (1990–2016)</td>
<td>0.10</td>
<td>267.61</td>
</tr>
<tr>
<td>I</td>
<td>3.41</td>
<td>0.41</td>
</tr>
<tr>
<td>II</td>
<td>−56.78</td>
<td>1097.03</td>
</tr>
<tr>
<td>III</td>
<td>3.88</td>
<td>0.35</td>
</tr>
<tr>
<td>IV</td>
<td>−24.35</td>
<td>1302.45</td>
</tr>
<tr>
<td>V</td>
<td>4.07</td>
<td>0.10</td>
</tr>
</tbody>
</table>

Figure 8. Variance of $R/C$ vs. SP500 (1990–2016).
4. Discussions

This paper has provided a new framework to understand and study the relationships between the dynamics of the bond and equity markets. This new theory is based on alternative derivation of the yield curve based on entropy or the loss of information over time. Despite their disparate foundations the traditional yield curve as modeled by the popular Nelson–Siegel specification and the entropically motivated yield share deep similarities. As shown using empirical data, the implied information processing rate $R/C$ can be useful in the prediction of market downturns. Further studies of entropically motivated variables such as $R/C$ will probably reveal other useful information theoretic relationships in economics and finance.

Supplementary Materials: The excel file with macro used to estimate R/C are available online at www.mdpi.com/1099-4300/19/6/292/s1.

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