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The Impact of Demand Shocks on Firm-level Offshoring Behavior: Theory and Evidence

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Abstract

This paper extends the model of Antras et al. (2014) to disentangle the link between demand shocks and firm-level offshoring decisions. The model predicts that a positive demand shock increases the firm-level purchases of imported intermediates in both the extensive and intensive margins. Using a difference-in-difference approach, we examine the response of Chinese exporters to a quota removal on textile and clothing products, which is equivalent to a positive demand shock. The findings indicate that firms import more varieties and higher volumes of intermediates after the quota removal. The results are robust to different regression designs.

Keywords: Intermediates Offshoring · Textile and Clothing · Demand Shock · Quota Removal

JEL Classification: F10-F14-L11

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1. Introduction

A key feature of global trade in the new century is the rapid growth of offshoring. Yeats (2001) documents that in 1995 approximately thirty percent of world manufacturing products trade is comprised by intermediate input trade. Ramnarayan (2006) finds very similar patterns for OECD countries. The benefits of offshoring is to enhance firm-level production efficiency. Bergin et al. (2011), for example, indicates that a considerable number of American manufacturing firms contract to carry out particular stages of productions abroad. This work sharing design decreases production costs. Antras et al. (2014) further document the fact that firms engaged in offshoring are larger and more productive than firms that never import. Therefore, it is of importance to academics and policy makers to analyze firms’ offshoring behaviors.

A growing literature investigates the benefits of offshoring and its impact on the labor market (Bergin et al., 2011; Hummels, et al., 2011), how information frictions and trade agreement affect firm-level offshoring behavior (Allen, 2015; Dasgupta et al., 2014; Bernard et al., 2014; Antras and Staiger, 2012), and what intermediates are more likely to be offshored (Furusawa et al., 2015). Little research has been done to assess the link between the shocks to the final product demand and offshoring behavior in intermediates. Demand shocks are often associated with trade liberalization: a reduction in trade costs in final products is often accompanied by an increase in demand for these products. Chinese textile and clothing exporters, for instance, import almost twice as many varieties and 20 per-
cent more volume of intermediates after the Phase IV quotas removal\textsuperscript{1}. The lack of research investigating the impact of a demand shock to final products on firm-level offshoring behavior leaves the mechanism behind the above mentioned empirical evidence uncovered, and the benefits of trade liberalization underestimated.

This paper theoretically and empirically studies how export firms’ offshoring behavior is associated with demand shocks in the final products. We are particularly interested in how a demand shock affects the number of intermediates a firm imports. Bernard et al. (2009) find that the extensive margins of imports accounts for approximately 65 percent of the cross-country variation in U.S. imports. Bergin et al. (2011) document that both the extensive and intensive margins of offshoring affects the volatility of economic activities, such as the fluctuations in employment in Mexico, which is influenced by its offshoring industries. As a result, analyzing firm-level offshoring of the extensive and intensive margin is of economic importance.

This work extends the model of Antras et al. (2014) who build on Eaton and Kortum (2002), to endogenize the firm-level offshoring decision. In this model, all firms produce final goods by assembling a series of intermediates either purchased domestically or offshored from foreign countries. To offshore from foreign countries, firms have to pay a fixed search cost to learn the prices of intermediates in these countries. After searching, each firm offshores the intermediates from the cheapest country they have searched.\textsuperscript{2} Differing form Antras et al. (2014), we

\textsuperscript{1}In 1994, the Agreement on Textile and Clothing (ATC) gradually removed the quota imposed on textile and clothing products. The quotas were eliminated over four phases in January 1, 1995, 1998, 2002 and 2005, respectively. The quotas removal in January 1, 2005 is referred to as the Phase IV quotas removal.

\textsuperscript{2}For simplicity, I assume that the prices of intermediates in domestic market are observable
allow final products to be exported to foreign countries. As a result, any demand shock in foreign markets will change firm-level offshoring behavior. Intuitively, if the demand faced by a firm increases, this firm would choose to search more countries and offshore, on average, more varieties and a greater volume of intermediates. This is because that searching more countries decreases the unit cost of final products and the benefits of cost reduction is larger after the increase of demand in final products.

We then empirically examine the theoretical predictions using a comprehensive data set which contains all Chinese firms producing textile and clothing products during 2000-2006. On January 1, 2005 Phase IV of the Agreement on Textile and Clothing (ATC) removed all the remaining quotas on products belonging to textile and clothing categories. This event offers a natural experiment to test firm-level offshoring responses to a demand shock. A rich set of literature has investigated the impact of the quota removal on Chinese textile exporters’ performance. Khandelwal et al. (2013) document the rapid export growth of Chinese textile firms to the U.S. after 2005 quota removal. Ahn et al. (2011) further show that the quota removal lead to larger-than-expected gains for Chinese textile exporters. Rotunno et al. (2013) find that while the quota removal on textile products increased Chinese textile exports to US, its exports to Africa dropped significantly. To the best of our knowledge, this is the first paper, which attempts to document the impact

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The increase demand requires a greater volume of intermediate inputs, which increases the firm’s incentive to search for lower price of each intermediate. On the one hand, this leads to an increase in the offshoring probability for each intermediate, and more intermediates will be offshored. On the other hand, larger demand and lower intermediate prices drive up the imported volume of intermediates.
of the quota removal on firm-level offshoring behavior.

We employ a difference-in-difference approach to test the the impact of the quota removal on the firm-level extensive and intensive offshoring margins. Notice that the number of intermediates being offshored is discrete and following Puhani (2012), a nonlinear difference-in-difference estimation has been conducted as a robustness check. Using the firm-level export and import data from textile and clothing industry in China, we find that the firm-level offshoring varieties and volumes of intermediates increase significantly after the quota removal.

This work contributes to the growing literature on the determinants of global production sharing. It disentangles the link between demand shocks in final products and firm-level offshoring behavior. This paper is closely related to Furusawa et al. (2015) who document the determinants of firm-level offshoring decisions, but neglect the influence of foreign demand on firm-level offshoring behavior. This paper finds results similar to Antras and Staiger (2012), who show the impact of trade agreements on the intensive margin of offshoring. Nonetheless, Our model predicts that after accounting for firm search behavior, the impact of trade agreements on the firm-level intensive margin of offshoring is larger. This is because firm search lowers its own marginal cost, which further increase offshoring volumes. This work is also in line with Bergin et al. (2011) who document that the firm-level offshoring is determined by the relative intermediate production costs in foreign and domestic countries. An exogenous shock to foreign intermediates cost shrinks the domestic firms’ offshoring varieties of intermediates. A similar mechanism works in this framework, but in a multi-country setting the relative intermediates cost in foreign and domestic markets is affected by firm-level endogenous searching.
Demand shocks change firm-level offshoring behavior through changes in the firm-level search behavior. In contrast to Bernard et al. (2014), who claim that lowering search cost leads to more offshoring and hence an increase in the demand for final products, this paper emphasizes reverse channel; an increase in demand motivates the firm-level extensive and intensive margins for offshoring intermediates.

The rest of the paper proceeds as follows. Section 2 presents the theoretical model. Section 3 introduces the background of the multifiber agreement (MFA) and Chinese textile and clothing exports. Section 4 describes the data. Section 5 discusses the regression design and reports the results. Section 6 concludes.

2. Model

In this section, we extend Antras et al. (2014) model to investigate the impact of demand shocks on extensive and intensive margins of offshoring at firm-level.

2.1. Demand

Suppose there are \( J \) countries in the world. The representative consumer’s preferences for final goods takes the CES form:

\[
U = \left( \int_{\omega \in \Omega_j} q_{jt}(\omega)^{(\sigma-1)/\sigma} \right)^{\sigma/(\sigma-1)},
\]

where \( \Omega_j \) is the set of all final goods available to consumers in country \( j \), and \( \sigma \) denotes the elasticity of substitution across final products. The preference leads
to the following demand for final good $\omega$ in country $j$ at period $t$:

$$q_{jt}(\omega) = A_{jt}p_{jt}(\omega)^{-\sigma},$$  \hspace{1cm} (2)

where $p_{jt}(\omega)$ is the price of final good $\omega$, and $A_{jt}$ is the residual demand of $\omega$ in country $j$ at period $t$. To simplify notation in following sections, we define $B_{jt}$ and $B_t$ as follows:

$$B_{jt} = \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{(1-\sigma)} A_{jt} \tau_{ijt}^{1-\sigma}. \hspace{1cm} (3)$$

$$B_t = \sum_{j \in J_{i}^{ex}(\varphi, B_{i}^{w})} B_{jt}, \hspace{1cm} (4)$$

where $B_{jt}$ is the transportation cost adjusted residual demand in country $j$ at period $t$. Note that $B_{jt}$ is proportional to the residual demand in country $j$ at period $t$, $A_{jt}$. $B_{i}^{w} = (B_{1t}, B_{2t}, ..., B_{Jt})$, is a vector that contains every country’s transportation cost adjusted residual demand in period $t$, and $B_t$ is the aggregate adjusted residual demand of all countries to which a firm exports.\(^4\) We allow $B_{i}^{w}$ to vary over time, in order to capture exogenous demand shocks. $\tau_{ij}$ is the ice-berg transportation cost between country $i$ and $j$, where $\tau_{ijt} = 1$ if $i = j$. $J_{i}^{ex}(\varphi, B_{i}^{w}) \subseteq J$ is the set of countries a firm located in base country $i$ at period $t$ exports to, given its productivity level, $\varphi$, and the vector of world adjusted residual demand, $B_{i}^{w}$.

\(^4\)Note that the set of countries to which the firm exports depends on $B_{i}^{w}$, not on $B$. 

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2.2. Supply

In order to produce the final goods, each firm needs to assemble a series of intermediates. Following Antras et al. (2014), intermediates can be offshored and the model’s equilibrium will imply the location of the production of different intermediates. Intermediates are assumed to be imperfectly substitutable with each other at a constant elasticity substitution $\rho$, and distributed continuously over the range $[0,1]$.

All intermediates are produced under the constant return to scale technology. Denote $a_j(v)$ the labor requirement associated with the production of intermediate input $v \in [0,1]$ in country $j \in J$.\footnote{Similar to the transportation cost, $a_j(v)$ is assumed to be time invariant. This assumption is to exclude the impact of country-level productivity changes on firms’ offshoring behavior.} free-on-board price for intermediate $v$ from country $j$ in period $t$ is given by $a_j(v)\omega_{jt}$, where $\omega_{jt}$ is the wage rate in country $j$ at period $t$. As such, the cost of importing one unit of intermediate $v$ from country $j$ to country $i$ in period $t$ can be written as:

$$c_{ijt}(v) = \tau_{ijt}a_j\omega_{jt}$$  \hspace{1cm} (5)

The parameter $a_j$ represents country $j$’s efficiency in producing intermediates. For a given wage rate $\omega_{jt}$, a lower labor requirement, lower $a_j$, implies that country $j$ has greater competitiveness in the production of intermediates. Following Eaton and Kortum (2002), we assume the country specific efficiency $a_j$ follows a Frechet distribution:

$$\Pr(a_j(v) \geq a) = e^{-T_ja^\theta}, \text{ with } T_j > 0,$$  \hspace{1cm} (6)
where $T_j$ governs the state of the technology in country $j$. A larger $T_j$ implies a higher country specific efficiency. $\theta$ reflects the amount of variation within the distribution where larger $\theta$ implies less variability. Two features of equation (6) are worth addressing: first, a country’s efficiency in an intermediate is independent of its type; second, a country with a higher $T_j$ will be, on average, more efficient in all intermediates.

With all the above assumptions, the unit assembly cost of final goods for a firm located in country $i$, with productivity $\varphi$ in period $t$ is:

$$c_{ft}(\varphi) = \frac{1}{\varphi} \left( \int_0^1 (\tau_{ij}(v)t(v)a_{j(v)}\omega_{j(v)}t)^{1-\rho} dv \right)^{\frac{1}{1-\rho}}, \quad \text{(7)}$$

where $j(v)$ denotes the country from which intermediate $v$ is imported. Note that the final goods production cost relies on the firm’s productivity, $\varphi$. This is to capture the fact that more productive firms can assemble the series of intermediates more efficiently. Different from Antras et al. (2014), we assume the final goods can be sold in both domestic and international markets.

Firms cannot observe $a_j$ for any country, unless it pays a fixed search cost, $f_{ij}\omega_{it}$. Denote $J^i_t(\varphi, B_t) \subseteq J$ the set of countries a firm based in $i$ with productivity $\varphi$ has searched. $J^i_t(\varphi, B_t)$ is called the searching strategy of this firm. Different than Antras et al. (2014), the searching strategy not only depends on the firm-level productivity, but also the aggregate residual demand of the countries the firm exports to. The intuition is that as aggregate transportation cost adjusted residual demand, $B_t$ increases, so do the benefits of searching for cheaper intermediates.

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As in Melitz (2003), the firm-level productivity, $\varphi$, is fixed after the initial productivity draw. However, the marginal costs may vary over time due to changes in the offshoring behavior.
2.3. Firms’ Behavior Conditional on a Offshoring Strategy

Given a searching strategy, a firm based in country $i$ chooses to purchase each required intermediate input from the cheapest country it has searched. The offshoring probability of any intermediate is given by:

$$
\chi(\varphi, B_t) = 1 - \frac{T_i \omega_i^{-\theta}}{\Theta_i(\varphi, B_t)}, \quad (8)
$$

where

$$
\Theta_i(\varphi, B_t) = \sum_{k \in J_i(\varphi, B_t)} T_k (\tau_{ikt} \omega_{kt})^{-\theta}. \quad (9)
$$

Equation (8) and (9) imply that the offshoring probability of any intermediate is increasing in $\Theta_i(\varphi, B_t)$, the offshoring capability.

After choosing the cheapest country to import the corresponding intermediates from, the marginal cost of the final goods for the firm with productivity $\varphi$ is:

$$
c_{ft}(\varphi) = \frac{1}{\varphi} (\gamma \Theta_i(\varphi, B_t))^{-1/\theta}, \quad (10)
$$

where, $\gamma = \left[ \Gamma\left(\frac{\theta+1-\rho}{\theta}\right) \right]^{\theta/(1-\rho)}$. Equation (10) conveys the information that given the firm’s searching strategy, more productive firms will have lower marginal costs for assembling final goods. More importantly, a firm which has searched more countries, will have lower marginal costs. The intuition is that, when a firm searches more countries, the expected price for each intermediate falls.

Firms in base country $i$ can export to any country $j$ after paying a fixed cost $f_{ij}^{ex} \omega_{it}$. The superscript $ex$ indicates export, which is to distinguish from the fixed search cost, $f_{ij}^{s} \omega_{it}$. From the demand function, we can derive the firm-level profits.
as:

\[
\pi_i(\varphi, B_t) = \varphi^{\sigma - 1} (\gamma \Theta_i(\varphi, B_t))^{(\sigma - 1)/\theta} B_t - \omega_i \sum_{j \in I_t^e(\varphi, B_t)} f_{ij}^e - \omega_i \sum_{j \in I_t^m(\varphi, B_t)} f_{ij}^m. \tag{11}
\]

### 2.4. Firms’ Optimization

Each firm needs to make a series of decisions to maximize its per-period profit. The sequence of the game is as follows. Each firm draws a productivity, \( \varphi \), from a given distribution after paying an entry cost. A demand shock in country \( j \), \( \Delta B_{jt} \), occurs at the beginning of period \( t \), and is observed by all firms. Each firm decides which country it will export to, from which to offshore and set the optimal price in each market. All decisions are made at the beginning of each period. The subsequent sections will show the responses of firm-level offshoring behavior to a demand shock.

To guarantee the model is solvable, we assume that this game is a simultaneous game and each firm makes its own decision in each period before observing other firms’ responses. In particular, a representative firm at the beginning of period \( t \) forecast all state variables, except the demand shock, take the same values as in period \( t - 1 \). For instance, at the beginning of period \( t \), a firm expects the residual demand in country \( j \) to be \( B_{j,t-1} + \Delta B_{jt} \), where \( \Delta B_{jt} \) is the observed demand shock in country \( j \) at the period \( t \). In another words, in a simultaneous setting, a firm does not observe other firms’ strategic responses to a demand shock. Instead, it only observe other firms’ responses in the subsequent period.\(^7\)

\(^7\)A representative firm could expect the overall response of other firms in response to a positive demand shock, i.e. increase their exports, which would reduce the representative firm’s residual...
In this model, we only characterize the firm-level optimization in a short period, which allows us to neglect the equilibrium input of demand shocks on local wages. Intuitively, a positive demand shock in country $j$, $\Delta B_{jt}$, will encourage more domestic firms to start offshoring or search more countries for cheaper intermediates. This change in offshoring behavior reduces firm-level marginal costs and hence changes the labor demand in the home country. In a long period, all firms expect the wage effect caused by demand shocks. As such, each firm further adjusts its exporting and offshoring strategies. This interdependence between wages and offshoring strategies makes it difficult to characterize optimal firm behavior in a long period.

2.4.1. Optimal Offshoring Decisions

A firm’s optimal offshoring strategy balances the gain from marginal cost reductions against the search costs which arise from searching an additional country. The optimal offshoring strategy depends both on firm-level productivity, $\varphi$, and expected aggregate residual demand, $EB_t$. The two variables determine the firm-level returns from searching one more country. The optimal offshoring strategy at demand, and further dampen the overall firm-level response to the demand shock. However, the aggregate effect of the demand shock and other firms’ responses would still increase $B_{jt}$. 

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period $t$ maximizes expected profit:

$$
\max_{I_{ijt} \in \{0,1\}} E_t \pi_i (\varphi, B_t, I_{1it}, \ldots, I_{2it}) = \varphi^{\sigma-1} \left( \gamma \sum_{j=1}^{J} I_{ijt} T_j (\tau_{ijt} \omega_{j,t-1})^{-\theta} \right)^{\frac{\sigma-1}{\sigma}} E B_t
$$

$$
- \omega_{i,t-1} \left[ \sum_{j=1}^{J} I_{ijt} f_{ij}^s + \sum_{j \in J_{\sigma}(\varphi, E B_t)} f_{ij}^{ex} \right],
$$

(12)

where, with incomplete information $E B_t = B_{t-1} + \Delta B_t$ and $E B_w = B_{t-1}^{w} + \Delta B_t^{w}$. This implies that when a firm maximizes its profit at the beginning of period $t$, it is based on the realized world residual demand vector in period $t$, $B_{t-1}^{w}$ and the demand shock, $\Delta B_t^{w}$. The economy is assumed to be in an equilibrium before the demand shock, as such, $B_{1}^{w} = B_{2}^{w} = \ldots = B_{t-1}^{w}$. Firm-level optimal strategies are identical from period 1 to period $t - 1$.

Similar to the proof in Antras et al. (2014), it can be shown that given the firm-level productivity, $\varphi$, the searching strategy under a low expected aggregate adjusted residual demand is a subset of the searching strategy under a high expected aggregate adjusted residual demand. This point is formally presented in the following proposition:

**Proposition 1.** Whenever $(\sigma - 1)/\theta > 1$ and the economy is in an equilibrium before period $t$, which implies $E B_{t-1} = B_{t-1} = \ldots = B_1$. $J^i(\varphi, E B_t) \supseteq J^i(\varphi, B_{t-1})$ for $E B_t > B_{t-1}$, where $J^i(\varphi, E B_t) = \{ j : I_{ijt}(\varphi, E B_t) = 1 \}$.

Proposition 1 implies that if a demand shock at period $t$ increases the expected aggregate demand facing a firm, the set of countries a firm searches will be larger or equal to that at period $t - 1$. This is because the benefits from a reduction
in marginal costs by searching an additional country is larger after the shock. The proof is in the Appendix. In particular, the export decisions and searching strategies are interdependent. A positive shock to the expected aggregate residual demand, $EB_t$, increases the firm-level searching strategy, $J^s_t(\varphi, EB_t)$. This increase further lowers firm-level assembly costs. The firm may choose to enter more foreign markets because of its increased competitiveness, which could further increase the aggregate residual demand faced by the firm. The set of countries to which the firm searches for intermediates could increase again. This process lasts until the firm does not export to any new foreign market and no longer searches new countries for intermediates.

Notice that the demand shock is at country level, $\Delta B_{kt}$. It can be proved that the expected aggregate residual demand faced by any firm $EB_t$ is not decreasing in $EB_{kt}$, for $\forall k$:

$$
\frac{\partial EB_t}{\partial EB_{kt}} = \begin{cases} 
sign(\Delta J^{ex}) \sum_{\Delta J^{ex}} EB_{jt} & \text{if } k \notin J^{ex}(\varphi, B_{\omega t} - 1) \\
1 + sign(\Delta J^{ex}) \sum_{\Delta J^{ex}} EB_{jt} & \text{if } k \in J^{ex}(\varphi, EB_{\omega t} - 1) 
\end{cases} \geq 0, \quad (13)
$$

where $\Delta J^{ex} = J^{ex}(\varphi, EB_{\omega t}^t) - J^{ex}(\varphi, B_{\omega t}^{t-1})$ is the set of countries to which a firm exports after the positive demand shock, $\Delta B_{kt}$. $EB_{t}^t = \{B_{1,t-1}, B_{2,t-1}, ..., B_{k,t-1} + \Delta B_{kt}, ..., B_{J,t-1}\}$, is the expected world residual demand at period $t$ and $B_{t-1}^t = \{B_{1,t-1}, B_{2,t-1}, ..., B_{k,t-1} - 1, ..., B_{j,t-1}\}$ is its counterpart vector before the demand shock. Before the demand shock, the economy was in equilibrium, we have $EB_{jt} = EB_{j,t-1} = B_{j,t-1} = ... = B_{j,1}$. This implies $EB_{t}^t = B_{t-1}^t + \Delta B_{k,t}$. The term $\sum_{\Delta J^{ex}} EB_{jt}$ captures the expected aggregate residual demand change caused by exporting to a larger or smaller number of countries after the demand shock. If the
firm exports to more countries, $\text{sign}(\Delta J^{ex})$ is positive and otherwise is negative or zero. The proof of inequality (13) is in the Appendix. Intuitively, the country-level demand shock affects the aggregate residual demand, $EB_t$, faced by a firm in two interdependent channels: on one hand, some of the countries experiencing a demand shock belong to the firm’s export set. As such, the country-level demand shock has a positive influence on the expected aggregate residual demand faced by this firm. On the other hand, the firm may choose to export to an additional country, whose residual demand has increased. A firm may chooses to search more countries for cheaper intermediates which enable it to enter a previously nonprofitable market. Either one increases the aggregate residual demand faced by this firm. Therefore, the expected aggregate residual demand, $EB_t$, faced by a firm is non-decreasing in $EB_{kt}$, $k \in J$.

Note that, if a firm does not export to countries experiencing demand shocks neither before nor after the shocks, the firm’s exporting and offshoring strategies would be unaffected by the demand shocks. The reason is that these firms, with incomplete information, face the same state variables in period $t$ and $t - 1$. As such, these firms’ exporting and offshoring strategies would be the same in both periods. This implies that only firms whose export set contains countries experiencing demand shocks will change their offshoring behavior in response to demand shock.\(^8\)

When a firm’s searching strategy is non-decreasing in the expected aggregate residual demand of the countries to which it exports, equation (9) implies that the

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\(^8\)The countries experiencing demand shock either belong to these firms’ export set as of $t - 1$ or are added to the export set at period $t$. 
firm’s offshoring capability, $\Theta_i(\varphi, EB_t)$, is non-decreasing in $EB_t$.\footnote{Equation (9) indicates that the offshoring capability, $\Theta_i(\varphi, EB_t)$, increases in $J_s^*(\varphi, EB_t)$, and $J_s^*(\varphi, EB_t)$ is non-decreasing in $EB_t$. Therefore, $\Theta_i(\varphi, EB_t)$ is non-decreasing in $EB_t$.} From equation (8) the offshoring probability of any intermediate input is also non-decreasing in $EB_t$. This further implies that the firm will import more varieties of intermediates in period $t$ relative to period $t - 1$ as long as the demand shock increases the expected aggregate residual demand the firm faces. Formally, we have the following proposition:

**Proposition 2.** Whenever $(\sigma - 1)/\theta > 1$, the firm-level offshoring probability for any intermediate is increasing in the expected aggregate residual demand, $EB_t$. As such, a positive demand shock, which influences the expected aggregate residual demand a firm faces, increases the firm-level imported varieties of intermediates.

Proposition 2 indicates that only firms, whose expected aggregate residual demands are increasing in demand shocks, increase their offshored varieties of intermediates.\footnote{Two types of firms are affected by the demand shock: the countries which experience the demand shock must belong to the firms’ export set either in period $t - 1$ or period $t$.} Instead, the firms, whose expected aggregate residual demands are unaffected by the demand shock, would keep their offshoring strategies.

Since the total cost of intermediates is proportional to total revenue, $C_i^{\text{tot}}(\varphi, EB_t) = \frac{z - 1}{\sigma} R_i(\varphi, EB_t)$, along with Proposition 1 and 2, the firm-level intensive margin of imports is increasing in the expected aggregate residual demand faced by the firm. Greater expected aggregate residual demand implies higher firm-level revenues and greater offshoring probabilities. Both of them determine the higher-level of import intermediates. As such, demand shocks which increase the expected aggregate residual demand faced by a firm, increases the firm’s intensive margin of imports.
This point is formally summarized in the following proposition, and the proof is in the Appendix.

**Proposition 3.** Whenever \( (\sigma - 1)/\theta > 1 \), the firm-level intensive margin of imports is increasing in the expected aggregate residual demand faced by the firm. As such, a positive demand shock increases the firm-level intensive margin of exports, for those whose expected aggregate residual demands are affected.

Quota removal could be treated as a positive shock on the residual demand in some foreign countries. For exporters, whose expected aggregate residual demand, \( EB_t \), is affected by the demand shock, Proposition 2 and 3 provide two testable predictions that these firms, on average, import more intermediates, in terms of extensive margin (more varieties) and intensive margin (larger volumes).\(^{11}\) The next section models the connection between the removal of quotas and the expected aggregate demand increase.

### 2.5. The Impact of Quota Removal on Firms’ Behaviors

Under an export quota restriction, the government typically allocates export quotas by auction (Khandelwal et al., 2013). Therefore, each exporter needs to pay a unit license fee for their exports. The export price in market \( j \) at period \( s \) is given

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\(^{11}\)Proposition 1 is not testable, because the set of countries from which the firm imports is not identical to the set of countries it searches. For instance, suppose a firm originally searches and imports from 3 countries, denoted by \( \{1,2,3\} \). After the removal of quotas, it searches country 4. The prices of all intermediates are lower in the 4th country, and so the firm imports all intermediates from the 4th country. In this case, after the removal of quotas the set of countries from which it imports is \( \{4\} \), but the set of countries from which it searches is \( \{1,2,3,4\} \).
by equation (14)
\[ p_{js}(\varphi) = \frac{\sigma}{\sigma - 1} (\tau_{ijs} c_{fs}(\varphi) + l_j), \]

where \( l_j \) is the unit license fee for firms exporting quota restricted products to country \( j \) at period \( s \). \( l_j > 0 \) for \( s = 1, 2, ..., t - 1 \) and \( l_j = 0 \) for \( s \geq t \).\(^{12}\) Let \( \hat{\tau}_{ijs} = \tau_{ijs} + \frac{l_j}{c_{fs}(\varphi)} \) denote the ice-berg cost for shipping 1 unit of a quota restricted product from country \( i \) to country \( j \) at period \( t \). We have \( \hat{\tau}_{ijs} > \tau_{ijs} \) for any product exported under a quota. Using the definition of \( B_{jt} \) in equation (3), it is straightforward to show that the removal in period \( t \) leads to the following inequality:

\[
EB_{jt} = \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{1-\sigma} A_j \tau_{ij}^{1-\sigma} > \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{1-\sigma} A_j \hat{\tau}_{ij}^{1-\sigma} = B_{jt-1},
\]

where \( B_{jt-1} \) is the residual demand in country \( j \) at period \( t - 1 \). Inequality (15) indicates that a quota removal in country \( j \) at period \( t \) is equivalent to an increase in the residual demand in country \( j \). This property offers a natural experiment to test Proposition 2 and 3: the quota removal leads firms, which previously exported under quota restriction, to import more intermediates both in terms of varieties and volumes.\(^{13}\)

The next section introduces the Multifibre Agreement and its later cancellation.

\(^{12}\) As the economy has been assumed to be in an equilibrium before period \( t \), the unit license fee is assumed to be constant from period 1 to \( t - 1 \).

\(^{13}\) Strictly speaking, the impact of a quota removal on residual demand varies across firms. This is because firms with different productivities, \( \varphi \), will have different unit costs \( c_{f}(\varphi) \). As a result, \( \hat{\tau}_{ij} \) reduces more for firms with high productivities after the quota removal.
3. Background of MFA and ATC

China’s textile and clothing industry accounts for a nonnegligible share of China’s overall exports and the world exports of textile and clothing. In 2004, China’s textile and clothing exports account for 15% of its total exports and 23% of the world textile and clothing exports.

The Multifibre Agreement (MFA) had been used to restrain the import of textiles, especially from developing countries. It was initially used by the United States to limit textile imports from Japan in 1955. A consequence of the MFA is that the textile and clothing products were held out of the multinational trade negotiation. In 1994, the Uruguay Round of trade negotiations included the Agreement on Textile and Clothing (ATC), which was to end the MFA and gradually remove the quota imposed on textile and clothing products. The quotas were eliminated over four phases by integrating textile and clothing products into GATT/WTO rules. The U.S., E.U., and Canada were required to remove textile and clothing quotas on January 1, 1995, 1998, 2002 and 2005, respectively. In the first three phases the the countries have to integrate products representing 16, 17, and 18 percent of their 1990 import volumes, and in Phase IV this figure increased to 49 percent. A considerable share of quotas removed in Phase IV were binding.\textsuperscript{14} In particular, about 65 percent quotas are binding in the U.S., E.U. and Canada. The detailed quota binding rates in each region are reported in Table 1.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|}
\hline
Region & Quota Binding Rate \\
\hline
U.S. & 65\% \\
E.U. & 65\% \\
Canada & 65\% \\
\hline
\end{tabular}
\caption{Quota Binding Rates in Each Region}
\end{table}

\textsuperscript{14}Following Evans and Harrigan (2005); Brambilla et al. (2009), if a quota’s fill rate exceeds 90\%, the quota is treated as binding.
Table 1 shows that about 1,500 types of textile and clothing products exported to the U.S., E.U., or Canada were under quota restrictions, and more than 900 quotas were binding in 2004.

Removing the binding quotas lead to a surge of textile and clothing exports. China, for instance, saw its textile and clothing exports to the U.S. almost double after the Phase IV quota removal, while the exports to the rest of the world increased by less than 3%. More details are reported in Table 2.

[Table 2 is to be here]

The distinct growth patterns between the rest of the world and the regions removing quotas indicate the significant role quotas played in restricting firm exports. Under a quota restriction, firms have to pay a unit license fee for their exports (e.g. Demidova et al., 2011). This license fee increases each firm’s export price and, as such, its demand in the foreign market shrinks. The removal of quotas reduces the license fee to zero and hence, all other things equal, increases the foreign demand for each firm. As such, the Phase IV quota removal offers an ideal setting to analyze Chinese export firms’ offshoring response to a demand shock.

4. Data

The empirical exercises require data from two sources. One is the Chinese Custom data collected by the Chinese Custom Trade Statistics (CCTS), which report the firm-level exports and imports at HS8 disaggregated level. In addition, this dataset reports the firm-product specific export destinations. The other data source is
MFA/ATC quotas, which provides the product-level quota information in the U.S., E.U. and Canada.\footnote{The data have been sorted by Peter Schott, and is downloadable at his homepage: http://faculty.som.yale.edu/peterschott/sub_international.htm}

The first step is to clean the CCTS data by deleting all firms which never exported textile or clothing products in 2004 and 2005. Second, we carefully match the two pieces of data using the HS code provided in both of them. The matched sample offers the following information: 1. the number of each firm’s imported intermediates; 2. the firm-level import values; 3. countries to which each firm’s products are exported; 4. the country-product specific quota status;\footnote{The information reflects whether exported product is subject to a quota in a given country, and what the quota fill rate is.} 5. the number of products each firm exports. The matched sample exhibits a clear increase pattern in the number of imported intermediates for firms exporting textile and clothing to the U.S., E.U., or Canada. Detailed results are reported in Table 3.

\begin{table}[h]
\begin{tabular}{|c|c|c|}
\hline
Column 1 & Column 2 & Column 3 \\
\hline
Part A & Part B & \\
\hline
\end{tabular}
\caption{Average number of imported varieties and total value of imported intermediates}
\end{table}

Part A and Part B of Table 3 report the average number of imported varieties and the total value of imported intermediates for firms exporting to different destinations, respectively. Column 1 of Part A reports the average number of varieties imported intermediates by firms exporting to the rest of the world (ROW) other than U.S., E.U., and Canada. Columns 2-4 of Part A show the figures for firms exporting to the U.S., E.U., or Canada, respectively, while columns 5-8 show the same information for firms engaged ordinary trade.\footnote{A firm is treated as an exporter to a destination if the firm exports at least one product to}
among firms engaged in ordinary trade, the number of imported varieties more than doubled between 2004 to 2005 on average. Part B suggests a similar pattern for average firm-level import values between 2004 and 2005, except for firms exporting to ROW in the full sample. Whereas, it is unclear whether the increase trend is caused by Phase IV quota removal or simply represents a time trend.

Making use of the quota information, we can classify firms into treatment and control groups based on the quota status of their exports. According to the model, the treated group contains firms whose expected residual demands are affected by the quota removal, while all other firms belong to the control group. In 2004, there are 12,137 firms that export textile and clothing products, of which 3,843 firms export under binding quotas. The classification rules are discussed in detail in the next section. By comparing the offshoring responses across treatment and control groups, we can identify the impact of the quota removal on firms’ offshoring behavior.

5. Estimation and Results

In this section, we use a difference-in-difference strategy to analyze how firm offshoring behavior changes after the quota removal on textile and clothing on January of 2005. The identification relies on the comparison between firms in the affected product category (the treatment group) and those in the unaffected prod-

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this destination. Therefore, if a firm exports to the U.S., E.U. and Canada, this firm will be used repeatedly in Table 3. Furthermore, in China firms can be engaged in international trade through two regimes: ordinary trade or processing trade. The processing trade firms usually assemble materials provided by foreign suppliers, and hence their offshoring behaviors are not driven by demand shocks.
uct category (the control group). Firms are classified into treatment and control groups in several ways.

In the baseline regression, firms which never export quota restricted products belong to the control group, while all other firms make up the treatment group. There are several issues that are worth addressing here. First, consider a product that is subject to a quota restriction only in the U.S., but a firm which exports this product to a country without any quota restrictions (South Africa, for instance). In the baseline regression, this firm is considered to be treated. One reason for this is that Chinese textile and clothing exporters often use third countries as quota-hopping export platforms (Rotunno et al., 2013). Therefore, a quota removal in the U.S. might still have an impact on the firm’s expected aggregate residual demand. This sensitivity of our results to our classification of firms will be evaluated in our robustness checks.

Second, it could be the case that some firms export quota restricted products in 2004, but stopping export these products in 2005. In this case, these firms experience a negative demand shock. It seems problematic to treat these firms as treated. To address this concern, we calculate the share of firms dropping quota restricted products in a treated group and find that they represent less than 4% of all firms. Dropping these firms and re-estimating the baseline model, we find very similar results.

Third, to demonstrate the validation of the DID approach, we draw the importing trends of the treated and control groups before and after the Phase IV ATC quota removal. In particular, we calculate the average monthly imported number

18The full sample contains firms exporting textile or clothing products at least in one year.
of varieties and imported values by treatment and control groups, respectively.

[Figure 1 is to be here]

In Figure 1, X-axis denotes month, and Y-axis denotes the number of imported varieties. The solid and dash curves separately denote the importing trends of treatment and control groups, and the dash vertical line denotes the time when the Phase IV of ATC becomes applicable (January 2005). These curves exhibit similar trends before January 2005 for both groups, but the imported number of varieties by treatment groups strikingly increases in January 2005, while no systematic different trend has been observed for control group. Furthermore, in all subsequent periods, the imported number of varieties by the treatment group is clearly higher than that of the control group. The imported values exhibit very similar trend.\footnote{We also notice that the termination of ATC in January 2005 surges China’s export to the US and the EU, but such phenomenon only lasts for several months. The US and EU quickly respond to the surge of Chinese textile exports by restricting the annual growth rate of Chinese textile export to 7.5\% and 10\% until 2008, respectively. Comparing these figures with the growth rate of Chinese textile exports to the ROW in Table 2, which is 2.83\%, we argue that the export growth rates in the US and EU are still higher than that in the ROW. As such, we still expect different importing trends between treated and control groups. In addition, firms make their importing scheme before production and exporting, and it is normally costly to adjust the importing and production scheme. The responses of the US and EU are not expected by textile firms, and hence, we still expect a large increase in firm-level import in both extensive and intensive margins in the whole year of 2005. As such, our DID approach is still validated.}

The baseline regression is as follows:

$$y_{it} = \beta_1 \text{Treatment}_i + \beta_2 \text{Post}_t + \beta_3 \text{Treatment}_i \times \text{Post}_t + \beta_4 x_{it} + \epsilon_{it}, \quad (16)$$

where $y_{it}$ represents the firm-level outcome variables including the number and
logarithm total values of imported intermediates by firm $i$ in year $t$.\textsuperscript{20} $Treatment_i$ is a dummy variable which takes value 1 if firm $i$ belongs to the treatment group, 0 otherwise. $Post_t$ is the time dummy variable taking the value 1 after year 2004, 0 otherwise. $x_{it}$ are control variables, including the number of products each firm exports, the firm-level total export values ownership fixed effect and product fixed effects.\textsuperscript{21} The reason we include the firm-level exporting number of products and the total export values in the regression is to proxy the firm-level productivity.\textsuperscript{22} According to equations (8) and (9), the importing probability of a particular intermediate is increasing in the firm-level productivity.

Note that one of the dependent variables, the number of varieties of imported intermediates, is discrete. This count data feature suggests that a Poisson regression to evaluate the treatment effect:

$$f(y|z) = \Phi(\beta z),$$

$$\Phi(\beta z) = \exp\left[-\exp(\beta z)\right] \left[\exp(\beta z)\right]^y/y!,$$

$$\beta z = \beta_1 Treatment_i + \beta_2 Post_t + \beta_3 Treatment_i \times Post_t + \beta_4 x_{it} + \epsilon_{it}.$$ 

We make use of regression (17) to evaluate the treatment effect as a robustness check of the baseline model. Puhani (2012) points out that the nonlinear treatment

\textsuperscript{20}The imported values are in US dollars.

\textsuperscript{21}The product fixed effect are to control for the influence of firm-level exports on firm-level importing behavior. The product fixed effect is aggregated at HS2 level as a vast number of firms export multiple products, and we cannot define their sectors at a more disaggregate level. The ownership fixed effect is to control for different import behaviors among state-owned firms, private-owned firms and foreign-owned firms. i.e., foreign-owned firms may have better connection with international markets, and more likely to offshore from international markets.

\textsuperscript{22}Firms with a higher core productivity normally export more varieties and at higher export values (e.g. Bernard et al., 2011; Manova and Zhang, 2012; Nocke and Yeaple, 2014).
effect is different from a linear treatment effect. In particular, in the nonlinear case, the treatment effect is not the cross difference, but the difference between two cross differences. Mathematically, the treatment effect is:

\[ treatment = \Phi(\beta_1 + \beta_2 + \beta_3 + \beta_4 x_{it}) - \Phi(\beta_1 + \beta_2 + \beta_4 x_{it}). \]  

(18)

We calculate the marginal effects of each regressor in Poisson regressions according to equation (18). The results from the baseline regression for the extensive and intensive margin of offshoring are reported in Table 4 and Table 5.

[Table 4 is to be here]

[Table 5 is to be here]

Table 4 reports the treatment effects of the quota removal on the extensive margin of offshoring, which are estimated using OLS and Poisson regressions, respectively. Columns 1-4 in Table 4 report the treatment effect results by dividing all textile products exporters into treatment and control groups. In contrast, columns 5-8 report the treatment effect results by restricting the sample to firms engaged in ordinary trade. All coefficients are the marginal effect in Poisson regressions (in column 3, 4, 7 and 8). The results indicate a positive impact of the quota removal on offshoring decisions. Specifically, the quota removal, on average, increases firm-level imported number of varieties by 0.2 – 1.7 units. In addition, the productivity proxies, the firm-level export number of products and export values have positive impact on the firm-level extensive margin of importing. This is consistent with our model that more productive firms are, on average, importing more varieties.
At the same time, Table 5 reports the treatment effects of the quota removal on the intensive offshoring margin. Similar to Table 4, columns 1-2 show the treatment effect for all firms, and columns 3-4 report the results by restricting the sample to exporters operating under the ordinary trade regime. The results indicate that for the Phase IV ATC quota removal increases the value of imported intermediates by $9 - 15\%$.

In January 2005, the U.S., E.U., and Canada were the only regions removing quotas on textile and clothing products from developing countries. This implies that the quota removal mainly influences firms which export textile products to the set of countries lifting the quota restrictions. For example, shipments of “men’s or boy’s jackets” (HS 610339) were subjected to an import quota in the U.S., E.U., and Canada in 2004 but not in the other countries. In this case, the impact of quota removal on firm-level offshoring behavior is much more limited among firms exporting to countries other than the U.S., E.U., and Canada.

It is also possible that a firm exports textile products to regions with quota restrictions, but the fill rate, which is defined as the percentage a quota that is used, does not bind. For instance, China’s exports of “Multiple or Cabled Yarn” (HS 550912) to the U.S. is exported under an unbinding quota. In this case, classifying firms which export products subject to an unbinding quota into the treatment group may be inappropriate.

To check if the classification of firms into treatment and control groups in the baseline regression biases the evaluation of the treatment effect, we redefine firms

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23Following the definition of Khandelwal et al. (2013), if the quota fill rate is less than 90%, the quota is treated as not binding.
as belonging to the treatment group if 1. firms export to the U.S., E.U., or Canada;
2. at least one of the products they export is subject to a binding quota. All other
firms belong to the control group.

Using the newly defined treatment and control groups we re-estimate equation
(16) and (17), respectively. The results are reported in Table 6 and Table 7:

| Table 6 is to be here |
| Table 7 is to be here |

The results in Table 6 indicate that the quota removal had a positive impact
on the number of imported varieties regardless of our estimation methodology.
For firms engaged in ordinary trade, the quota removal increases, on average, the
number of imported intermediates by 1.2 – 2 units. For the full sample the effect
is even stronger; we find that the quota removal increases the average number of
imported intermediates by more than 1.7 – 2.2 units. This might suggests that
firms engaged in processing trade respond more to the quota removal than firms
engaged in ordinary trade. One possible interpretation is that firms engaged in
processing trade exporting multi products and require more types of intermedi-
ates.\textsuperscript{24} Therefore, they are more sensitive to the quota removal and increase the
number of imported varieties in a faster speed. At the meanwhile, the results in
Table 7 show that the quota removal tends to increase the values of imported in-
termediates by 20 and 27 percent for the full sample and firms engaged in ordinary
trade, respectively.

\textsuperscript{24}In the next specification, we find that more than 90% single-product exporters in the textile
sector are firms operating under ordinary trade regime.
Another concern is that multi-product firms often introduce new products or drop old products. The products-switching within multi-product firms may have a significant impact on the firm-level offshoring behavior. For instance, a firm which begins importing more varieties of intermediates might also be introducing products. Thus may confuse product-switching with the removal of quotas. In contrast, some multi-product firms might export only a small share of its products to quota restricted regions. As a result, the impact of the quota removal on these multi-product firms may be relatively small. For the above reason, classifying these multi-product firms as treated firms may be controversial. To exclude the impact of within-firm product and destination churning on their importing behaviors, we restrict attention to firms exporting single products, and it is straightforward to track their export decisions over time. This leads to our observations decrease from 89,433 to 39,095, and more than 90% single product firms operating under ordinary trade regime. These single product firms are classified into treatment and control groups based on the destination that their product is exported to and the quota fill rate as in the second specification. The results are reported in Table 8 and Table 9:

[Table 8 is to be here]

[Table 9 is to be here]

All results in Table 8 and Table 9 exhibit a very similar pattern to those in Table 6 and Table 7. Relative to the control group, the firms in the treatment group tend to import more intermediates, both on the extensive and intensive margins, after the quota removal. In particular, the quota removal increases the firm-level imported number of varieties by $1.7 - 3.2$ units and import values by $12\% - 28\%$. 

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These figures are higher than those obtained from the baseline regression (Table 4). This suggests that the impact of quota removal on firm-level importing behaviors is underestimated in the baseline regression, and the third specification provides the precise results by restricting the focus on single-product exporters.

6. Conclusions

This paper presents a model that disentangles the link between a demand shock in final product market and the firm-level offshoring behavior. The model predicts that higher final product demand causes firms to search more countries for cheaper intermediates. This is because the higher demand increases firm profitability, which in turn covers higher fixed search costs. After firms search more source countries, more varieties and higher volumes of intermediates will be offshored instead of being purchased from the domestic market.

Using the textile and clothing export and import data from China, we find that the removal of quotas on textile and clothing products increases the number of varieties and volume of intermediates offshored. This implies that a positive demand shock on final products enhances exporters’ participation in offshoring. The empirical results are robust to different regression designs.

Documented by a number of research papers, the global work sharing is an effective way to enhance firm-level production efficiency. One implication of this paper is that increased final product demand encourages global offshoring, and im-

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25 In the baseline regression, some firms, which are classified into the treatment group, are not or trivially affected by the quota removal. This implies that the impact of the Phase IV ATC quota removal is possibly underestimated.
proves firm-level production efficiency. Neglecting this effect suggests the benefits of trade liberalization may be underevaluated.
Reference


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Appendix (Figures and Tables)

a. The Trend of the Imported Number of Varieties

b. The Trend of the Imported Values

Figure 1
### Table 1: Quota Fill Rate

<table>
<thead>
<tr>
<th></th>
<th>All Three Regions</th>
<th>U.S.</th>
<th>E.U.</th>
<th>cCAN</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Number of Quotas</strong></td>
<td>1,415</td>
<td>467</td>
<td>507</td>
<td>441</td>
</tr>
<tr>
<td><strong>Number of Binding Quotas</strong></td>
<td>917</td>
<td>426</td>
<td>287</td>
<td>204</td>
</tr>
<tr>
<td><strong>Fill Rate</strong></td>
<td>64.81%</td>
<td>91.22%</td>
<td>56.61%</td>
<td>46.26%</td>
</tr>
</tbody>
</table>

Notes: A quota is defined as a binding quota when its fill rate exceeds 90%. The products are disaggregated at HS8 digit level.

### Table 2: The Export Values and Growth Rate

<table>
<thead>
<tr>
<th>Year</th>
<th>ROW</th>
<th>U.S.</th>
<th>E.U.</th>
<th>CAN</th>
<th>Growth Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>2004</td>
<td>589</td>
<td>70</td>
<td>76</td>
<td>10.7</td>
<td>2.83%</td>
</tr>
<tr>
<td>2005</td>
<td>605</td>
<td>139</td>
<td>140</td>
<td>17.5</td>
<td>97.91%</td>
</tr>
</tbody>
</table>

Notes: Table 2 reports the export revenue growth of textiles and clothing to the U.S., E.U., Canada, and rest of the world, respectively. Revenues are measured in 10 million US dollars.

### Table 3: The Average Number of Imported Intermediates

#### A: Average Imported Varieties

<table>
<thead>
<tr>
<th>Year</th>
<th>ROW</th>
<th>U.S.</th>
<th>E.U.</th>
<th>CAN</th>
<th>Ordinary Trade</th>
<th>ROW</th>
<th>U.S.</th>
<th>E.U.</th>
<th>CAN</th>
</tr>
</thead>
<tbody>
<tr>
<td>2004</td>
<td>1.90</td>
<td>2.81</td>
<td>2.51</td>
<td>2.31</td>
<td>2.47</td>
<td>1.86</td>
<td>2.07</td>
<td>1.38</td>
<td></td>
</tr>
<tr>
<td>2005</td>
<td>2.59</td>
<td>3.10</td>
<td>2.74</td>
<td>3.50</td>
<td>2.59</td>
<td>4.67</td>
<td>4.33</td>
<td>7.05</td>
<td></td>
</tr>
</tbody>
</table>

#### B: Average Imported Values

<table>
<thead>
<tr>
<th>Year</th>
<th>ROW</th>
<th>U.S.</th>
<th>E.U.</th>
<th>CAN</th>
<th>Ordinary Trade</th>
<th>ROW</th>
<th>U.S.</th>
<th>E.U.</th>
<th>CAN</th>
</tr>
</thead>
<tbody>
<tr>
<td>2004</td>
<td>1.47</td>
<td>1.29</td>
<td>1.38</td>
<td>1.68</td>
<td>1.05</td>
<td>0.92</td>
<td>0.91</td>
<td>0.92</td>
<td></td>
</tr>
<tr>
<td>2005</td>
<td>1.49</td>
<td>1.32</td>
<td>1.45</td>
<td>1.60</td>
<td>1.10</td>
<td>0.97</td>
<td>1.04</td>
<td>0.97</td>
<td></td>
</tr>
</tbody>
</table>

Notes: Table 3 reports the average number of imported varieties and the total value of importing intermediates for firms exporting to the U.S., E.U., CA, and the rest of the world. The varieties of intermediates are defined at HS6 disaggregate level, and the value are measured in 10 thousand of USD.
Table 4: The Impact of Quota Removal on Firms’ Extensive Importing Margin

<table>
<thead>
<tr>
<th></th>
<th>OLS</th>
<th>Poisson</th>
<th>OLS</th>
<th>Poisson</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>Treatment</td>
<td>1.7161***</td>
<td>(0.3897)</td>
<td>1.1830***</td>
<td>(0.3897)</td>
</tr>
<tr>
<td></td>
<td>1.15e-07***</td>
<td>(8.53e-10)</td>
<td>5.72e-07***</td>
<td>(6.91e-11)</td>
</tr>
<tr>
<td># of Product</td>
<td>0.2658***</td>
<td>(0.0032)</td>
<td>0.0103***</td>
<td>(0.0003)</td>
</tr>
<tr>
<td>Ownership FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Product FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R-square</td>
<td>0.13</td>
<td>0.13</td>
<td>0.13</td>
<td>0.13</td>
</tr>
<tr>
<td>Obs</td>
<td>89,433</td>
<td>89,433</td>
<td>89,433</td>
<td>89,433</td>
</tr>
</tbody>
</table>

Notes: Table 4 presents the treatment effect of the quota removal on the numbers of imported varieties at the firm-level. The treatment group contains firms exporting textile products which were subject to quota restrictions before 2005. Column 1-4 reports the results for all firms exporting textile products, while column 5-8 reports the results for firms exporting textile products under ordinary trade regime. Marginal Effects are reported in column 3, 4, 7 and 8, and the R-square in these columns are pseudo R-square. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
Table 5: The Impact of Quota Removal on Firms’ Intensive Importing Margin

<table>
<thead>
<tr>
<th></th>
<th>Full Sample</th>
<th></th>
<th>Ordinary Trade</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Treatment</td>
<td>0.0991**</td>
<td>0.0968**</td>
<td>0.1552***</td>
<td>0.1537***</td>
</tr>
<tr>
<td></td>
<td>(0.0402)</td>
<td>(0.0401)</td>
<td>(0.0447)</td>
<td>(0.0447)</td>
</tr>
<tr>
<td># of Product</td>
<td>0.0007**</td>
<td></td>
<td>0.0009**</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.0003)</td>
<td></td>
<td>(0.0004)</td>
<td></td>
</tr>
<tr>
<td>lnEXP</td>
<td>5.68e-11</td>
<td></td>
<td>1.53e-11</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(5.52e-11)</td>
<td></td>
<td>(7.12e-11)</td>
<td></td>
</tr>
<tr>
<td>Ownership FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Product FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R-square</td>
<td>0.45</td>
<td>0.45</td>
<td>0.45</td>
<td>0.45</td>
</tr>
<tr>
<td>Obs</td>
<td>89,433</td>
<td>89,433</td>
<td>57,718</td>
<td>57,718</td>
</tr>
</tbody>
</table>

Notes: Table 5 presents the treatment effect of the quota removal on firm-level total import volume. The treatment group contains firms exporting textile products to the U.S., Canada, or EU with a quota fill rate above 90%. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
**Table 6:** The Impact of Quota Removal on Firms’ Extensive Importing Margin (Fill Rate)

<table>
<thead>
<tr>
<th></th>
<th>Full Sample</th>
<th></th>
<th>Ordinary Trade</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>OLS Poisson</td>
<td>OLS Poisson</td>
<td>OLS Poisson</td>
<td>OLS Poisson</td>
</tr>
<tr>
<td>Treatment</td>
<td>2.2898***</td>
<td>2.958***</td>
<td>1.7329***</td>
<td>1.7900***</td>
</tr>
<tr>
<td></td>
<td>(0.4912)</td>
<td>(0.4913)</td>
<td>(0.0547)</td>
<td>(0.0520)</td>
</tr>
<tr>
<td># of Product</td>
<td>0.9651***</td>
<td>0.5777***</td>
<td>0.8421***</td>
<td>0.4021***</td>
</tr>
<tr>
<td></td>
<td>(0.0167)</td>
<td>(0.0053)</td>
<td>(0.0178)</td>
<td>(0.0079)</td>
</tr>
<tr>
<td>EXP</td>
<td>1.43e-07***</td>
<td>4.83e-09***</td>
<td>2.30e-07***</td>
<td>7.65e-09***</td>
</tr>
<tr>
<td></td>
<td>(2.49e-09)</td>
<td>(4.29e-11)</td>
<td>(3.87e-09)</td>
<td>(1.81e-10)</td>
</tr>
<tr>
<td>Ownership FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Product FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R-square</td>
<td>0.14</td>
<td>0.14</td>
<td>0.14</td>
<td>0.25</td>
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<tr>
<td></td>
<td>89,433</td>
<td>89,433</td>
<td>89,433</td>
<td>57,718</td>
</tr>
<tr>
<td>Obs</td>
<td>89,433</td>
<td>89,433</td>
<td>89,433</td>
<td>57,718</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: Table 6 presents the treatment effect of the quota removal on the firm-level imported varieties of intermediates at firm-level. The treatment group contains firms exporting textile products to the U.S., Canada, or EU with a quota fill rate above 90%. Column 1-4 reports the results for all firms exporting textile products, while column 5-8 reports the results for firms exporting textile products under ordinary trade regime. Marginal Effects are reported in column 3, 4, 7 and 8, and the R-square in these columns are pseudo R-square. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
<table>
<thead>
<tr>
<th></th>
<th>Full Sample</th>
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<th>Ordinary Trade</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td><strong>Treatment</strong></td>
<td>0.1922***</td>
<td>0.2097***</td>
<td>0.2677***</td>
</tr>
<tr>
<td></td>
<td>(0.0607)</td>
<td>(0.0457)</td>
<td>(0.0760)</td>
</tr>
<tr>
<td><strong># of Product</strong></td>
<td>0.0054***</td>
<td></td>
<td>0.0346***</td>
</tr>
<tr>
<td></td>
<td>(0.0005)</td>
<td></td>
<td>(0.0025)</td>
</tr>
<tr>
<td><strong>lnEXP</strong></td>
<td></td>
<td>0.0178*</td>
<td>0.02625**</td>
</tr>
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<td>(0.0101)</td>
<td>(0.0138)</td>
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<tr>
<td><strong>Ownership FE</strong></td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td><strong>Product FE</strong></td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td><strong>R-square</strong></td>
<td>0.53</td>
<td>0.53</td>
<td>0.53</td>
</tr>
<tr>
<td><strong>Obs</strong></td>
<td>89,433</td>
<td>89,433</td>
<td>57,718</td>
</tr>
</tbody>
</table>

Notes: Table 7 presents the treatment effect of quota removal on firm-level total import volume. The treatment group contains firms exporting textile products to the U.S., Canada, or EU with a quota fill rate above 90%. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
### Table 8: The Impact of Quota Removal on Firms’ Extensive Importing Margin (Single Product)

<table>
<thead>
<tr>
<th></th>
<th>Full Sample</th>
<th></th>
<th></th>
<th>Ordinary Trade</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>OLS</td>
<td>Poisson</td>
<td></td>
<td>OLS</td>
<td>Poisson</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Treatment</td>
<td>2.9754***</td>
<td>2.4437***</td>
<td>2.1196***</td>
<td>2.2335***</td>
<td>3.2823***</td>
<td>2.9264***</td>
<td>1.6641***</td>
</tr>
<tr>
<td></td>
<td>(0.6273)</td>
<td>(0.6405)</td>
<td>(0.0791)</td>
<td>(0.0793)</td>
<td>(0.7573)</td>
<td>(0.7710)</td>
<td>(0.0840)</td>
</tr>
<tr>
<td># of Product</td>
<td>1.7054***</td>
<td>1.0281****</td>
<td></td>
<td>1.8241****</td>
<td>0.8675****</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.0169)</td>
<td>(0.0016)</td>
<td></td>
<td>(0.0235)</td>
<td>(0.0017)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>EXP</td>
<td>5.90e-08***</td>
<td>3.24e-09***</td>
<td></td>
<td>7.38e-08***</td>
<td>6.92e-09***</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(7.55e-10)</td>
<td>(2.92e-11)</td>
<td></td>
<td>(1.15e-09)</td>
<td>(2.87e-11)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ownership FE</td>
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<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Product FE</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R-square</td>
<td>0.24</td>
<td>0.24</td>
<td>0.25</td>
<td>0.25</td>
<td>0.24</td>
<td>0.24</td>
<td>0.25</td>
</tr>
<tr>
<td>Obs</td>
<td>39,095</td>
<td>39,095</td>
<td>39,095</td>
<td>39,095</td>
<td>37,112</td>
<td>37,112</td>
<td>37,112</td>
</tr>
</tbody>
</table>

Notes: Table 8 presents the treatment effect of the quota removal on the number of imported varieties at the firm-level. The treatment group contains firms exporting a single textile product to the U.S., Canada, or EU with a quota fill rate above 90%. Column 1-4 reports the results for all firms exporting textile products, while column 5-8 reports the results for firms exporting textile products under ordinary trade regime. Marginal Effects are reported in column 3, 4, 7 and 8, and the R-square in these columns are pseudo R-square. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
Table 9: The Impact of the Quota Removal on Firm-level Intensive Import Margins (Single Product)

<table>
<thead>
<tr>
<th></th>
<th>Full Sample</th>
<th>Ordinary Trade</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>Treatment</td>
<td>0.2822***</td>
<td>0.1443***</td>
</tr>
<tr>
<td></td>
<td>(0.0779)</td>
<td>(0.0483)</td>
</tr>
<tr>
<td># of Product</td>
<td>0.0398***</td>
<td>0.0603***</td>
</tr>
<tr>
<td></td>
<td>(0.0021)</td>
<td>(0.0038)</td>
</tr>
<tr>
<td># of Product</td>
<td></td>
<td>0.0237**</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.0124)</td>
</tr>
<tr>
<td>Ownership FE</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Product FE</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R-square</td>
<td>0.54</td>
<td>0.54</td>
</tr>
<tr>
<td>Obs</td>
<td>39,095</td>
<td>39,095</td>
</tr>
</tbody>
</table>

Notes: Table 9 presents the treatment effect of the quota removal on firm-level total imported volumes. The treatment group contains firms exporting textile products to the U.S., Canada, or EU with a quota fill rate above 90%. Standard errors are in parenthesis. ***, ** and * denote significance at the 1%, 5%, and 10% levels, respectively.
Appendix (Proofs)

Proof of Proposition 1

Proof. Similar to Antras et al. (2014), when \((\sigma - 1)/\theta > 1\), the profit function in (12) exhibits increasing differences in \((I_{ijt}, I_{ikt})\) for \(j, k \in \{1, \ldots, J\}\) with \(j \neq k\). Furthermore, it also features increasing difference in \((I_{ijt}, EB_t)\) for \(j \in J\). Making use of Topkis’s monotonicity theorem, I can then conclude that for any demand shock such that \(EB_t > B_{t-1}\), there must be \((I_{i1t}(\varphi, EB_t), I_{i2t}(\varphi, EB_t), \ldots, I_{iJt}(\varphi, EB_t)) \geq (I_{i1t}(\varphi, B_{t-1}), I_{i2t}(\varphi, B_{t-1}), \ldots, I_{iJt}(\varphi, B_{t-1}))\). Therefore, this inequality rules out a situation in which \(I_{ijt}(\varphi, EB_t) = 0\) but \(I_{i1t}(\varphi, B_{t-1}) = 1\), and as a result the conclusion \(J_i(\varphi, EB_t) \supseteq J_i(\varphi, B_{t-1})\) for \(EB_t > B_{t-1}\) holds.

Proof of Intensive Margin of Imports

Proof. The total cost of intermediates is proportional to operating revenue, that is:

\[
C_i^{\text{tot}}(\varphi, EB_t) = \frac{\sigma - 1}{\sigma}R_i(\varphi, EB_t) = \frac{\sigma - 1}{\sigma}\varphi^{\sigma - 1}(\gamma \Theta_i(\varphi, EB_t))^{(\sigma - 1)/\theta}EB_t. \tag{A1}
\]

where \(R_i(\varphi, EB_t)\) and \(C_i^{\text{tot}}(\varphi, EB_t)\) are the total revenue and costs of a firm with productivity \(\varphi\) based in country \(i\), respectively. From Proposition 1, for any demand shock in period \(t\) such that \(EB_t > B_{t-1}\), it follows that \(J_i(\varphi, EB_t) \supseteq J_i(\varphi, B_{t-1})\). This inequality further implies that the offshoring capability is increasing in the demand shock, which in turn increases the expected aggregate
residual demand, $EB_i$:

$$\Theta_i(\varphi, EB_t) > \Theta_i(\varphi, B_{t-1}). \quad (A2)$$

Inequality (A1) and (A2) imply that positive correlation between expected aggregate residual demand (or demand shocks) and the total cost of intermediates:

$$C_{i}^{\text{tot}}(\varphi, EB_t) > C_{i}^{\text{tot}}(\varphi, B_{t-1}). \quad (A3)$$

Recall that Proposition 2 implies that the offshoring probability of each intermediate, $\chi(\varphi, EB_t)$, is non-decreasing in the expected aggregate residual demand, $EB_t$, or $\chi(\varphi, EB_t) > \chi(\varphi, B_{t-1})$. Along with inequality (A3), the costs of importing are increasing in the residual demand:

$$C_{i}^{\text{im}}(\varphi, EB_t) = C_{i}^{\text{tot}}(\varphi, EB_t)\chi(\varphi, EB_t) > C_{i}^{\text{tot}}(\varphi, B_{t-1})\chi(\varphi, B_{t-1}) = C_{i}^{\text{im}}(\varphi, B_{t-1}). \quad (A4)$$

Inequality (A4) implies that the imported value of intermediates is increasing in the demand shock, which affects the expected residual demand a firm faces.

**Proof of Inequality (13)**

**Proof.** There are two situations when a demand shock takes place in country $k$ at period $t$: country $k$ does not belong to a firm’s export set at period $t-1$, $k \notin J^{ex}(\varphi, B_{t-1})$, or country $k$ belongs to a firm’s export set at period $t-1$, $k \in J^{ex}(\varphi, B_{t-1})$.

Case 1: When country $k$ does not belong to a firm’s export set in period $t-1$
\[
\frac{\partial EB_t}{\partial EB_{kt}} = \text{sign}(\Delta J^x(\varphi, B^\omega)) \sum_{\Delta J^x(\varphi, B^\omega)} EB_{jt},
\]

(A5)

\[
\Delta J^x(\varphi, B^\omega) = J^x(\varphi, EB^\omega_t) - J^x(\varphi, B^\omega_{t-1}).
\]

(A6)

where \( EB^\omega_t = \{B_{1,t-1}, B_{2,t-1}, ..., B_{k,t-1} + \Delta B_{kt}, ... B_{J,t-1} \} \) is the expected world residual demand vector in period \( t \), and \( B^\omega_{t-1} = \{B_{1,t-1}, B_{2,t-1}, ..., B_{k,t-1}, ... B_{J,t-1} \} \) is the counterpart before the demand shock. Note that the economy is in an equilibrium before the demand shock, as such, the residual demand in each country is constant before period \( t \). The expected residual demand in each country equals to its realization. I claim that if \( \Delta B_{kt} > 0 \), equation (A6) must be positive. Suppose the opposite is true, \( \Delta B_{kt} > 0 \), but \( J^x(\varphi, EB^\omega_t) - J^x(\varphi, B^\omega_{t-1}) < 0 \).

From Proposition 1, we must have

\[
J^s_i(\varphi, EB_t) \subseteq J^s_i(\varphi, B_{t-1}),
\]

(A7)

where \( EB_t \) and \( B_{t-1} \) are the expected aggregate residual demand faced by a firm in period \( t \) and \( t-1 \), respectively. Condition (A7) says that when the demand shock is in the country not belonging to the firm’s export set, and this shock causes this firm to export to fewer countries, \( EB_t < B_{t-1} \). Condition (A7) further implies that the offshoring capability

\[
\Theta(\varphi, EB_t) < \Theta(\varphi, B_{t-1}).
\]

This indicates that if a positive demand shock in country \( k \) at period \( t \) shrinks
a firm’s export set, it also reduces this firm’s offshoring capability. All of the above discussion shows that when the firm faces a world residual demand vector $EB_t$, it maximizes its profit by exporting to fewer countries and searching fewer countries than it did when facing the world residual demand vector $B_{t-1}^\omega$. This is a contradiction because this firm could search and export to the same set of countries after the demand shock, which will result in firm the same expected profit as that before the demand shock. The profit associated with the original search and export strategies must be higher than the current profit, otherwise, this firm does not maximize its profit when facing the aggregate residual demand before the demand shock, $B_{t-1}$.

Therefore, if country $k$ does not belong to a firm’s export set, after a positive demand shock, this firm must keep its original export set of countries or export to more countries. This implies $\frac{\partial EB_t}{\partial EB_{kt}} \geq 0$.

Case 2: country $k$ belongs to a firm’s export set.

$$\frac{\partial EB_t}{\partial EB_{kt}} = 1 + \text{sign}(\Delta J^{ex}(\varphi, B^\omega)) \sum_{\Delta J^{ex}(\varphi, B^\omega)} EB_{jt}. \quad (A8)$$

If $\text{sign}(\Delta J^{ex}(\varphi, B^\omega)) \sum_{\Delta J^{ex}(\varphi, B^\omega)} EB_{jt} < -1$, which implies $\frac{\partial EB_t}{\partial EB_{kt}} < 0$, following the same logic as in case 1, we can show the contradiction. It is straightforward to show $\text{sign}(\Delta J^{ex}(\varphi, B^\omega)) > 0$. Since $\frac{\partial EB_t}{\partial EB_{kt}} > 0$, from Proposition 1 $J_i^s(\varphi, EB_t) \supseteq J_i^s(\varphi, B_{t-1})$. This further implies $\Theta(\varphi, EB_t) \supseteq \Theta(\varphi, B_{t-1})$. After the demand shock, the firm increases its search set, and hence reduces its marginal assembly costs. If a country belongs to this firm’s export set before the shock, it must belong to the set after the shock. This is because, the profit from exporting to any country
belonging to the original export set increases after the cost reduction. Furthermore, with reduced marginal costs, this firm could penetrate other countries which do not belong to its export set before the demand shock. Therefore, \( \text{sign}(\Delta J^{ex}(\varphi, B^-)) > 0 \).

In sum, a firm’s export set and search set are both non-decreasing for a positive demand shock in any country.

**Proof for Inequality (15)**

**Proof.** The unit export costs for a firm exporting from base country \( i \) to country \( j \) in period \( s \), under the unit license fee is:

\[
c_{fs}^{\text{quota}}(\varphi) = \tau_{ij} c_{fs}(\varphi) + l_j.
\]  

(A9)

where \( c_{fs}^{\text{quota}}(\varphi) \) is the unit assembly cost under the quota restriction. \( l_j > 0 \) if country \( j \) is subject to an import quota and \( s < t \), while \( l_j = 0 \) if \( t \geq s \) or country \( j \) does not impose as import quota. The unit export cost under the unit license fee becomes:

\[
p_{js}(\varphi) = \frac{\sigma}{\sigma - 1}(\tau_{ij} c_{fs}(\varphi) + l_j).
\]  

(A10)

Equation (A10) implies that the unit license fee accounts for a larger cost share for firms with higher productivity. This further means that a quota removal would have a larger impact on more productive firms’ price, quantity, and profit. Let \( \hat{\tau}_{ij} = \tau_{ij} + \frac{l_j}{c_{fs}(\varphi)} \), the profit in market \( j \) in period \( s \) without considering any fixed cost is:

\[
\pi_{js} = \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{1-\sigma} A_j \hat{\tau}_{ij}^{1-\sigma} c_{fs}(\varphi)^{1-\sigma}.
\]  

(A11)
Similar to equation (3), we can show inequality (15) as follows:

\[ B_{j,t-1} = \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{(1 - \sigma)} A_{j}^{\alpha_{ij}^{1 - \sigma}} < \frac{1}{\sigma} \left( \frac{\sigma}{1 - \sigma} \right)^{(1 - \sigma)} A_{j}^{\tau_{ij}^{1 - \sigma}} = E B_{j,t}. \]  

(A12)