The Dynamics of Parallel Economies. Measuring the Informal Sector in México

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by

José BRAMBILA MACIAS

Abstract

The existence of parallel economies that operate in the shadows of informality within most Latin American countries is widely recognized by the economic literature. However, its composition, size and effects on economic growth are still open questions. In this paper, we estimate the size and the evolution of the Mexican informal economy in the last three decades using a vector error correction model. In addition to the standard explanatory variables traditionally used in the currency demand approach, we include remittances given their relevance in the Mexican economic system. The results indicate that informality prior to the late 1980’s accounted for at least two thirds of GDP, while stabilizing around one third of GDP in the last decade. Furthermore, our estimates provide evidence of a positive long run relationship between informality and economic growth.

JEL Classification Numbers: C32, E41, F24, O17.

Keywords: Informal Sector, currency demand, VEC, Remittances.

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A. Introduction

Economies in most of the developing world are characterized by huge informal sectors. In a
globalized world dominated by immense economic flows, understanding the causes, the size and the
effects of these phenomena represents a priority in the economic literature. Although the problem of
informality is not new, an agreement on a unique unanimously accepted definition, a
comprehensive theoretical model as well as a clear measuring method are still missing. This
confirms the difficulty posed by a phenomenon that operates in the shadows of illegality and whose
causes and resources vary among countries. From now on, we will refer to informality as all the
income generating activities that are unregulated by institutions. One of the first authors that
analysed informality in the developing world was De Soto (1989), who studied the informal sector
in Peru, giving insights and evidence on the development and interactions of Peru’s underground
economy. However, the first rigorous treatment can be tracked back to Loayza (1997), who used an
AK endogenous growth model to study informality causes, and the multiple indicators multiple
causes method (MIMIC) to measure the size of informality in Latin America. Unfortunately,
estimates of the informal sector are done using cross section analysis that study short periods of
time, thus precluding us from capturing its evolution over time and reaction to economic shocks. In
this paper, we will focus on measuring the size and evolution of informality in Mexico, in order
to contribute to the understanding of the interactions and effects of the underground economy not
observable in previous regional studies.

The Mexican economy, as the rest of Latin America, has always been characterized by a parallel
economy. Street vendors and their micro businesses, known as “vendedores ambulantes”, plague
huge areas of all the major urban centres in the country. These irregular economic agents form part
of the daily reality of the Mexican life. Far from what could be thought, they are well organized and
are under the protection of specific groups in charge of negotiating with, or bribing the authorities.
Their presence is a source of discontent and negative externalities to the formal establishment that
continuously lobby for their removal. Informality distorts prices and forces wages below its
optimum equilibrium, giving to formal, national or foreign economic agents the perception of an
institutional void, that could have long run consequences for the economy.

As Roubaud (1995) pointed out, economic agents react to economic shocks adopting new survival
strategies. In the case of Mexico, and probably the rest of Latin America, these new survival
strategies include the establishment of micro businesses in the shadow of the informal sector.
Employment in this sector appears as a natural alternative to cope with sharp decreases in income,
high unemployment rates, continuous economic crisis and adverse business regulations.

In this context, measuring the size of the Mexican informal sector becomes relevant, since it
certainly affects the macroeconomy and development of the country. Its magnitude and effects on
growth (positive or negative relationship) are still open questions in the literature.

The Mexican authorities are aware of this; so, the Mexican National Statistics Institute (INEGI)

See Portes et al. (1989), and Portes and Haller (2005).


Previous empirical studies have found contradictory evidence on the relationship between informality and growth. On
one hand, Helderberg and Kneipel (1988), Loayza (1997), and Kaufmann and Kaliberda (1996), among others, find a
negative relation. On the other hand, Tedds (1998), Giles and Tedds (2002) and more recently Chaudhuri et al. (2006)
find a positive impact of informality on growth.
conducts surveys in an attempt to measure the quantity of agents that work in the informal sector.\textsuperscript{5} The surveys indicate that almost 30 percent of the Economic Active Population (EAP) is engaged in the underground economy. Empirical estimates by Schneider (2002) and Vuletin (2006) attribute a size of 33.2 and 28.2 percent of GDP respectively to the informal sector. Unfortunately, these estimates refer to the late 1990’s early 2000’s, and are usually point estimates, precluding their use to analyse in deep the phenomenon and its possible evolution over time. Therefore, we decided to estimate a specific informal sector time series for the Mexican economy. In order to do so, we used the “classic” currency demand approach, going back in time as much as the data constraints allowed us.

The rest of the paper is structured as follows. In section B, we provide a brief description of the currency demand approach. Section C briefly summarizes the data and methodology. In section D, we present our results for the vector error correction model (VEC). Next, we used the VEC estimates to compute the size of the informal sector in Mexico. The procedure and the results are summarized in section E. Furthermore, in Section F we use the estimated time series for the informal sector to analyse its relationship with economic growth, and, finally, in Section G we offer some final remarks and policy recommendations.

**B. The Currency Demand Approach**

Before jumping into the technicalities of the currency demand approach, we will describe briefly the whole set of techniques available in the literature to measure informality. We can classify them into three categories:\textsuperscript{6}:

(1) Direct Methods: these methods refer usually to public or private surveys\textsuperscript{7} and target directly potential informal workers in an attempt to quantify participation into the underground economy.

(2) Indirect Methods: these methods use discrepancies in official records (differences between official and actual labour force, discrepancies between national income and consumption, different monetary methods, etc.) as proxies of the size of the informal sector.\textsuperscript{8}

(3) MIMIC or Model Approach: although this approach seems to belong to the indirect methodology, it differs from the previous methods, since it is able to link unobserved variables to observed indicators, using structural equations that model causal relationships among the unobserved variables.\textsuperscript{9}

\textsuperscript{5} The survey started in 2000 and annual averages are available in the Appendix.

\textsuperscript{6} See Schneider (2002) for a detailed description.

\textsuperscript{7} In Mexico, these type of surveys are conducted by the National Statistics Institute (INEGI), while surveys covering a wider sample of countries are conducted by the International Labour Organization (ILO).

\textsuperscript{8} Examples of these methods can be found in Kauffman and Kaliberda (1996), and Tanzi (1983).

\textsuperscript{9} The use of the MIMIC approach for estimation of the informal sector was first introduced by Frey and Weck-Hanneman (1984).
The currency demand approach can be classified among the indirect methods. This approach has been widely used in the past decades to estimate informality mainly in developed countries\textsuperscript{10}.

The family of monetary methods dates back to Cagan (1958), Gutmann (1977) and Feige (1979), but it was Tanzi (1983) that made the currency demand approach very popular among economists. The main assumption supporting this type of approach is that transactions in the informal sector use mostly cash, in order to maintain their activities in the shadows, away from any kind of formal record. So, if we could estimate the amount of cash used for informal transactions, we should be able to infer the size of the informal sector in the economy.

The idea behind the currency demand methods used in the literature is well summarized in a recent critical assessment by Ahumada, Alvarado and Canavese (2006). Following their work, a typical Cagan (1958) type currency demand function can be written as:

\[
C_0 = A(1 + \Theta) \gamma Y_0^\beta \exp(-\gamma i) \quad (1)
\]

where \(C_0\) stands for observed cash and \(\Theta\) represents the variable that gives incentives to make hidden transactions. This is the key variable behind all currency models\textsuperscript{11}. Traditionally this incentive variable has been approximated using government consumption normalized by GDP, tax rates (direct taxes, indirect taxes, etc.) or tax revenues to GDP. An increase in \(\Theta\) is expected to have a positive impact on currency demand, since agents will have more incentives to go to the informal sector, demanding more currency for their transactions. \(Y_0\) is the registered GDP. This variable approximates the level of transactions in the economy. Alternative measures are GDP per capita or consumption per capita. Finally, \(i\) is the interest rate and \(A, \alpha, \beta, \gamma\) represent positive parameters.

Estimating equation (1), we obtain \(C\). Setting the incentive variable \(\Theta\) to zero, and leaving the coefficients of the other variables unchanged, we get \(\bar{C}\). The difference between \(\dot{C}\) and \(\bar{C}\) allows us to estimate extra currency, i.e. the amount of currency holdings that are tax induced. In other words, the difference measures the amount of illegal money in the economy. Now, assuming that the velocity of money\textsuperscript{12} is the same in both the formal and informal sector\textsuperscript{13}, we can obtain an estimate of the size of the informal economy multiplying illegal money (\(\dot{C} - \bar{C}\)) by the velocity of money (\(v = Y/C\)).


\textsuperscript{11}Some of the critics to this type of approach refer precisely to the use of taxes as the only incentive for informality, claiming that not all underground activities are due to taxes, so the estimates obtained using the currency method are not able to capture the real level of informality.

\textsuperscript{12}This assumption is quite reasonable in the Mexican context. According to the “Comision Nacional Bancaria y de Valores” (CNBV) credit cards remain largely an untapped market, and in 2005 Mexicans used cash for more than 86 percent of their transactions. Furthermore, Mexico underwent the privatization of its banking system during the late 1990’s and the entrance of foreign banks during the early 2000’s; nevertheless, private saving decreased. See Bulíř and Swiston (2006).

\textsuperscript{13}This assumption has been criticized and, as Ahumada et al. (2006) claim, even if the velocity is the same, previous works that find \(\beta \neq 1\) (i.e. income elasticity different from 1) are incorrect. Therefore, they propose an alternative way of correcting the estimates.
C. Methodology and Data

This study uses annual data series that cover a period from 1970 to 2006. The main sources used to collect the data are: the IMF’s International Financial Statistics, the World Bank’s World Development Indicators, the Mexican Central Bank (online) database and the Mexican National Statistics Institute (INEGI). A more exhaustive description of the variables and their sources is provided in the Appendix.

As pointed out by Guissarri (1987), one of the first decisions to be taken in a currency demand model is how to deflate the currency series. In the classical approach popularized by Tanzi (1983), the standard procedure imposes currency deflation using M2\(^{14}\). However, this assumption was widely criticized. Spiro (1996) claims that the use of M2 is inadequate, since it contains amounts that correspond to long-term wealth accumulation, while currency is used mainly for transaction processes. Refinements went on and, nowadays, economists studying the informal sector use currency and currency per capita in real terms (see Schneider and Enste, 2000, and Öğüncü and Yilmaz, 2000). So, we decided to deflate our series using the national GDP deflator and, in order to capture the long run relationships of the explanatory variables on currency demand, we set up the following model\(^{15}\):

\[
C_t = \beta_0 + \beta_1 Y_t + \beta_2 TAX_t + \beta_3 R_t + \beta_4 REM_t + \nu_t
\]

where:

- \(C\) corresponds to the natural logarithm of currency in circulation outside the banks normalized by the GDP deflator;
- \(Y\) is the log of GDP in real terms;
- \(TAX\) represents the log of total tax revenues normalized by GDP;
- \(R\) refers to the log of the simple average of existing nominal interest rates;
- \(REM\) indicates the log of the amount of remittances received normalized by GDP.
- \(\nu\) is the error term.

The above specification captures the long-run relationships between the explanatory variables and the currency demand. Note that in addition to the standard independent variables, we decided to include remittances. With globalization and massive migrations to the developed world, remittances magnitude has surpassed the one of foreign direct investment in many developing countries, prompting a peak of interest on their economic implications and their role in the long-run. The text figure plots the evolution of FDI and remittances in Mexico during the past three decades. Although modest during the 1970’s, remittances have grown almost exponentially in the past twenty years, gaining weight in the Mexican economic scenario. Indeed, according to the World Bank (2006), remittances

\(^{14}\) Tanzi (1983) estimated the following equation: \(Ln(C/M2) = a_0 + a_1 Ln T + a_2 Ln (WS / NI) + a_3 Ln R + a_4 Ln Y + e\), where \(C/M2\) is the ratio of currency holdings to money, \(T\) is a tax variable, \(WS/NI\) is the ratio of wages and salaries in national income, \(R\) is a time deposit interest rate and \(Y\) is the real per capita income.

\(^{15}\) The model can be interpreted as a log-linearization of equation (1).
in 2003 were the nation’s second largest source of external finance after oil revenues\textsuperscript{16} (see text figure), surpassing traditional flows as foreign direct investment (FDI) and tourism revenues. Remittances are expected to have a positive impact on currency demand, especially because they enter the country in the form of money orders or as foreign currency (mainly U.S. dollars) in the pockets of migrant workers. It is important to point out that the series that we are using correspond to “recorded” remittances, which can be seen as a lower bound, since the actual amount is much more above. The World Bank’s estimates indicate that the actual amount of remittances could be 50 percent higher\textsuperscript{17}.

Another reason to include remittances as an explanatory variable has to do directly with informality. Although the former have not been totally associated with money laundry, it is well recognized that migrant workers usually engage in what is known as “smurfing”—separating transfers into smaller packages or different accounts, in order to avoid reporting and fulfilling local requirements such as taxation on larger amounts—giving birth to different kinds of informal flows\textsuperscript{18}. The opaqueness of these channels restraints in deep analysis. However, although the Mexican economy is closely link to the U.S. dollar, local transactions are made mostly using the national currency. So, migrant workers or their families are forced in one way or another to convert (using formal or informal channels) their dollars into Mexican pesos, thus increasing the demand for currency.

Summarizing, we expect a positive impact on currency demand for GDP, taxes and remittances (\( \beta_1, \beta_2, \beta_4 > 0 \)), since an increase in these variables will put pressure on currency demand\textsuperscript{19}. On the other hand, interest rate increases are expected to have a negative effect, prompting economic agents to get ride of their currency holdings (\( \beta_3 < 0 \)).

Before proceeding with the estimation, we tested our series for the presence of unit roots and cointegration\textsuperscript{20} in our main specification. All series turn out to be strongly non-stationary and integrated of order 1. Trace tests on one hand indicate two cointegrating equations at the 5 percent level and one at the 1 percent level, while the eigenvalue test indicates one cointegrating equation at the 1 percent level. This allows us to conclude that there exists one cointegration relationship\textsuperscript{21}.

\[\begin{align*}
\text{Oil Revenues vs. Remittances as % of Total Government Revenues} \\
\end{align*}\]

Sources: World Development Indicators (World Bank) and Banxico.
Notes: Data is presented as percentages of Total Government Revenues

\textsuperscript{16} According to the Energy Information Administration (EIA), in 2004 Mexico ranked number five as one of the top oil producers of the world. For more details see \url{www.eia.doe.gov/emeu/cabs/}.


\textsuperscript{18} We refer interested readers to a special report from the World Bank by Hernandez-Coss (2005) dealing with the U.S.-Mexico remittances corridor.

\textsuperscript{19} Note that the positive impact of taxes on currency demand can be interpreted in Tanzi’s spirit as follows: as the level of taxation rises, economic agents will be encouraged to engage tax-evading activities, that are facilitated by the use of currency, due to the intractability of cash; as a consequence, the use of currency rises.

\textsuperscript{20} The detailed analysis and tests can be found in the Appendix.

\textsuperscript{21} The existence of only one cointegration vector in our system means that there is a long-run equilibrium relationship between \( C, Y, TAX, R, \) and \( REM \).
Given the non-stationarity of our series and the presence of a common stochastic trend, traditional estimation methods are ruled out. So, in order to estimate equation (2) and measure the size of the informal sector, we decided to tackle the problem using a vector error-correction model (VECM). This type of models present a series of improvements with respect to standard approaches, allowing us to analyse short and long-run effects.

Examples of error correction models to measure informality can be found in works by Bovi (1999), Bovi and Castellucci (2001) and, more recently, in Chiarini and Marzano (2004) with respect to Italy.

The different VECM’s estimated in this paper can be defined as follows:

\[ \Delta Y_t = \delta + \Gamma_1 \Delta Y_{t-1} + \Pi Y_{t-1} + \epsilon_t \]

where \( Y \) is a vector formed by the \( n \) variables used in our currency demand model (i.e. \( C, Y, TAX, R \) and \( REM \)). \( \Pi \) and \( \Gamma \) are 5x5 matrices made up by the system coefficients. If the rank of cointegration \( r \) is less than \( n \), then \( \Pi = \gamma \beta' \), where \( \gamma \) represents the adjustment coefficients and \( \beta \) the cointegrating vectors. Finally, \( \epsilon \) corresponds to our system residuals and \( \delta \) is a constant term which can be separated in two parts —a trend term and the intercept— in the cointegrating relation.

**D. Results and Their Robustness**

In order to test the robustness of our model, we also estimate equation (2) without remittances, in addition, following Guissarri’s (1987) specification we estimate the model using government consumption normalized by GDP instead of tax burden and finally we use an approximation of the classical Tanzi (1983) model. The long-run cointegrating coefficients are reported in Table 1.

As expected, in model (1), which corresponds to equation (2), the coefficients for output, tax burden and remittances have a positive long-run effect, while interest rates take the pressure off on currency demand. All coefficients are strongly significant and assign relevant weight to GDP with a coefficient of 0.76 and taxes with 0.49, while leaving a moderate but not negligible effect to remittances with a coefficient of 0.12.

The performance of Model (2) is weaker compared to Model (1) and the TAX variable is barely significant; moreover it still retains significance among all its coefficients. On the other hand, Models (3) and (4) fail to maintain significance in all their variables except for taxes and interest rates.

In Model (4) we are forced to approximate Tanzi’s original specification using only income per capita, taxes and interest rates in order to explain variations in the currency ratio (C/M2). This is mainly due to data constraints. Hence, we are not able to include the ratio of wages and salaries, as in the original specification. Nevertheless, the model can be used to measure the explanatory power of this type of specification for the Mexican context, and as we can see from Table 1, this type of modelling has very little explanatory power with respect to the currency ratio in the economy. Furthermore, the interest rates present a negative sign in the cointegrating coefficient (-0.34), which

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22 The International Bank for Reconstruction and Development / The World Bank (2007), among others, address the issue of potential endogeneity of remittances. So, we include remittances in the set of endogenous variables.
can be interpreted as having a positive effect on currency holdings, which is in contradiction with the economic theory.

Table 1

<table>
<thead>
<tr>
<th>Normalized Cointegrating Coefficients&lt;sup&gt;23&lt;/sup&gt;</th>
<th>Model</th>
<th>(1)&lt;sup&gt;a&lt;/sup&gt;</th>
<th>(2)&lt;sup&gt;a&lt;/sup&gt;</th>
<th>(3)&lt;sup&gt;a&lt;/sup&gt;</th>
<th>(4)&lt;sup&gt;b&lt;/sup&gt;</th>
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<tbody>
<tr>
<td>Trace Statistic 5%</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>1%</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Max Eigenvalue Statistic 5%</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1%</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>C&lt;sub&gt;t-1&lt;/sub&gt;</td>
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<td>1.00</td>
<td>1.00</td>
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</tr>
<tr>
<td>C/M2&lt;sub&gt;t-1&lt;/sub&gt;</td>
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<td></td>
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<tr>
<td>Y&lt;sub&gt;t-1&lt;/sub&gt;</td>
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<td>-0.63***</td>
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<td>(0.04)</td>
<td>(0.07)</td>
<td>(0.18)</td>
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<td>0.18***</td>
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<tr>
<td>REM&lt;sub&gt;t-1&lt;/sub&gt;</td>
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<td>(0.03)</td>
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<td>GOV&lt;sub&gt;t-1&lt;/sub&gt;</td>
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<td>(1.10)</td>
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<td>(23.44)</td>
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<td>Log Likelihood</td>
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<td>141.17</td>
<td>21.42</td>
<td>11.19</td>
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</tr>
</tbody>
</table>

Note: All series used in the models are I(1). The complete details of the analysis as well as the matrix of adjustment coefficients can be found in the appendix. The number of lags in the models were determined using the Akaike’s information criterion (AIC), Schwarz’s Bayesian information criterion (SBIC) and the Hannan and Quinn information criterion (HQIC).

a. Model was estimated using two lags
b. Model was estimated using four lags
All models we estimated assume one cointegrating equation. Standard errors are in parentheses.
***indicates significance at the 1 percent level
** indicates significance at the 5 percent level
*indicates significance at the 10 percent level

<sup>23</sup> All variables are in natural logs. In addition to the previously described variables in section C, we have:
- C/M2: the ratio between currency outside the banks and M2 (broad money);
- Gov: the ratio between government consumption and GDP;
- Ypc: GDP per capita.
E. The Size of the Informal Sector

After estimating the vector error correction model (VECM)\textsuperscript{24} and obtaining the coefficients for the long-run relationship of equation (2) reported as Model (1) in Table 1, we proceed to estimate the size of the informal economy.

In order to obtain an estimate of the size of the informal sector, first, we compute \( \hat{C} \) using all the coefficients in equation (4). Then, we set the tax variable equal to zero and re-estimate the equation keeping all the other coefficients unchanged to obtain \( \tilde{C} \).

\[
C = 2.75 + 0.76Y + 0.49TAX - 0.09R + 0.12\text{Rem}
\]  

(4)

The difference between these two variables — \( \hat{C} \) and \( \tilde{C} \) — give us the amount of extra currency in the economy. Following Tanzi (1983), we assume equal velocity in both the formal and informal sector, and estimate it as follows:

\[
\frac{Y}{M1 - EC} = v
\]  

(5)

Equation (5) yields the velocity of money in the Mexican economy. \( Y \) is the GDP, \( M1 \) corresponds to total currency and deposits in circulation, and \( EC \) stands for extra currency or illegal money. The difference between \( M1 \) and \( EC \) can be interpreted as the amount of legal money used in the economy. Once we estimate the velocity from equation (5), the size of the informal sector can be obtained multiplying \( EC \) by the velocity of money:

\[
EC \ast v = Y_{\text{informal}}
\]  

(6)

Using equation (6), we can infer the size of the informal sector in formal GDP terms. From Table 1 we can also observe that our coefficient for \( Y \) is different from 1. So, in the Ahumada et al. (2006) spirit, we proceed to correct our estimates using their suggested method\textsuperscript{25}:

\[
\frac{Y_{\text{informal}}}{Y_{\text{formal}}} = \left( \frac{C_{\text{informal}}}{C_{\text{formal}}} \right)^{\frac{1}{\beta}} = \left( \frac{\hat{Y}_{\text{informal}}}{\hat{Y}_{\text{formal}}} \right)^{\frac{1}{\beta}}
\]  

(7)

where \( Y \) and \( C \) are the GDP and money respectively, while \( \beta \) is the income elasticity. The correction basically deflates the “wrong” ratio \( \frac{\hat{Y}_{\text{informal}}}{\hat{Y}_{\text{formal}}} \) that we obtained using inappropriately the assumption \( \beta = 1 \). Equation (7) corrects our estimates when \( \beta \neq 1 \).

Our original and corrected results normalized by the formal GDP are summarized below (see text figure). As we can see, informality in the 1990’s and early 2000’s stabilizes around 20-30 percent of

\textsuperscript{24}The long-run relationship between our variables was derived normalizing \( C \).

\textsuperscript{25}Ahumada et al. (2006) show that it is wrong to assume the same velocity of money when the hypothesis \( \beta = 1 \) is rejected by the econometric estimation of the currency demand model. This is our case, since our model gives us a coefficient \( \beta = 0.76 \).
GDP, which is in line with previous studies.\textsuperscript{26} The rest of the series, unfortunately, cannot be compared; so, inference should be taken with caution. Informality fluctuated between 50 and 60 percent of GDP during the 1970’s and presents a huge jump in the 1980’s, reaching almost 85 percent of GDP in 1988. Although at first sight this magnitude could seem out of proportion, we should clarify that this period was characterized by great economic and political turmoil in Mexico and the rest of Latin America. Moreover, deep crises and hyperinflation affected the south of the continent, and Mexico registered inflation rates above 100 percent (see Figure 2 in the Appendix).

So, in this period, inflation and macroeconomic instability clearly played a major role on currency demand. However, to which extent inflation or informality can explain this peak is difficult to assess. Inflation rates above 100 percent occurred in 1983, 1987 and 1988, while hyper-informality is registered in 1988 and 1989.

Figure 1: Mexican Informal Sector

Figure 1 plots both formal and informal series in real terms. If we compare both series, the presence of a parallel economy in Mexico can be appreciated. This underground economy grew continuously during the early 1970’s and the late 1980’s, accounting on average for almost two thirds of GDP. Informality then fell abruptly in the early 1990’s and remained stable around one third of GDP until our days.

\textsuperscript{26} See, for example, Vuletin (2006), Schneider (2002) and Loayza (1997).
F. Informal Sector and Economic Growth

As we explain in the previous sections of the paper, one of the aims of this study is to estimate a series for the informal sector, in order to use it to establish its long-run relationship with economic growth. To do so, once we have our informal economy series we have decided to apply the general to specific approach. This methodology starts by setting a large general model that encompasses many explanatory variables (the idea behind this is that the model will lose more explanatory power if relevant variables are omitted rather than if irrelevant variables are included) and slowly start eliminating variables with not significant coefficients until we reach a simpler, but more robust model.

For this part of the study we use annual data starting in 1970 and going all the way until 2006. The sources are again the IMF’s International Financial Statistics, the World Bank’s World Development Indicators and the Mexican Central Bank (online) database.

We start from an over-parameterized model and slowly pin down variables until we are left with the most significant model. Equation (8) describes the general economic growth model. In addition to the traditional variables we include the so called Parallel Economy (the informal sector).

\[
\Delta Y_t = a_1 \Delta Trade_t + a_2 \Delta Gov_t + a_3 \Delta Infla_t + a_4 \Delta Pop_t + a_5 \Delta PE_t + a_6 \Delta FDI_t + \\
+ (b_7 - 1) \left[ Y_{t-1} + \beta_1 + \beta_2 \text{Trade}_{t-1} + \beta_3 \text{Gov}_{t-1} + \beta_4 \text{Infla}_{t-1} + \\
+ \beta_5 \text{Pop}_{t-1} + \beta_6 \text{PE}_{t-1} + \beta_7 \text{FDI}_{t-1} \right] + \nu_t
\]

(8)

where:

- \( Y \) is real GDP per capita;
- \( Trade \) corresponds to (Exp+Imp)/GDP;
- \( Gov \) is Government consumption as percentage of GDP;
- \( Pop \) indicates demographic developments;
- \( PE \) is the parallel economy;
- \( FDI \) corresponds to foreign direct investment as percentage of GDP.

From equation (8) we are interested in obtaining a simpler model specification from which we can infer the long-run relationship between economic growth and parallel economies.

The results from the various specifications are presented in Table 2. As expected, the initial model, specification (1), although presenting the highest \( R^2 \), includes only two statistically significant variables, \( TRADE \) and \( Gov \). So, we start eliminating variables whose coefficients are not significant and that we believe are not relevant for the long-run relationship between growth and informality. Therefore, in specification (3), we eliminate FDI and inflation, that we believe will have more impact in the short-run, indeed, we start getting significance for the Parallel economy variable (\( PE_t \)), the long-run coefficient 0.031 becomes significant at the 10 percent level.

It is important to point out that trade and government consumption remain significant throughout all the models, highlighting their relevance for the Mexican economy. Going on, we arrive at specification (6), where all variables are significant and the parallel economy turns out to have a positive effect on economic growth.

\(^{27}\) See for example Hendry (1995).
Table 2.

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<td>0.082*</td>
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<td>0.051***</td>
<td>0.050***</td>
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<td>0.146*</td>
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<td>$Cons$</td>
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<tr>
<td>$R^2$</td>
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<td>0.027</td>
<td>0.026</td>
<td>0.025</td>
<td>0.026</td>
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</table>

The regressions were estimated using annual data starting in 1970 until 2006. Robust Standard errors in parentheses.

***indicates significance at the 1 percent level
** indicates significance at the 5 percent level
*indicates significance at the 10 percent level

So, using specification (6) we can derive the long-run relationship between the remaining variables and the Mexican economic growth. The long-run model is presented below as equation (9).

\[
Y = 29.59 + 0.11PE + 0.19TRADE + 0.64GOV
\] (9)

The former equation shows us the weights of each variable in the long-run and their effects on the Mexican economic growth. We can see that Government consumption represents the biggest driving force of the Mexican economy, being almost 3 times higher than international trade.
E. Concluding Remarks

The existence of a parallel economy in Mexico and other Latin American economies is well documented and accepted by the economic literature. It is the size and composition of this sector as well as the measuring methodology that are open to debate. In this paper, we used the currency demand approach to obtain a measure of informality in Mexico from the early 1970’s until 2006.

Our results provide an example of the evolution of informality in a developing country. First, the underground economy in Mexico grows constantly during the 1970’s until it reaches its maximum in the late 1980’s. Then, it decreases sharply and stabilizes around 30 percent of GDP. This is not entirely good news. In a country with nearly 100 million inhabitants and 840 billion U.S. dollars of GDP, this amount of informality represents a huge weight on the formal establishment, creating negative externalities, anchoring the nation and precluding it from reaching its real economic potential.

Furthermore, the stagnation of informality that characterized the past decade reflects the failure or lack of public policies targeting the informal sector, which consequently has left a large proportion of economic agents at the margins of the legal framework. Government lack of interest in this area will certainly have a deep impact and a huge cost on output in the long-run.

So, it is imperative to elaborate long-term strategies, in order to help to channel informal agents and their economic flows —i.e. remittances— back to formality. The Mexican government should create the conditions in order to allow informal remittances and income to be converted into productive investment. Successful policies will alleviate pressure on public finances and formal establishments in the short-run, allowing the re-direction of new resources needed to finance growth. On the other hand, in the long-run, the entry of informal agents into the legal framework will add fair competitiveness to the markets rising salaries and production quality.

Finally, Mexican policy makers should focus on the development of a slimmer regulation framework (i.e. less bureaucratic procedures, quick times and low costs, but above all less corrupt system), attractive enough to incentive effectively informal agents to come back to the formal economy.
### Appendix

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Sources</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>C</strong></td>
<td>Natural logarithm of currency over GDP deflator. 1970-2006 in national currency</td>
<td>International Financial Statistics, (IMF), the series is also available entirely or partially at the Mexican Central Bank Web page (<a href="http://www.banxico.com">www.banxico.com</a>)</td>
</tr>
<tr>
<td><strong>Y</strong></td>
<td>Natural logarithm of real GDP 1970-2006 in national currency</td>
<td>International Financial Statistics, (IMF), the series are also available at INEGI and Banxico’s web page.</td>
</tr>
<tr>
<td><strong>TAX</strong></td>
<td>Natural Logarithm of 1 + total of tax revenues over GDP 1970-2006</td>
<td>This series is partially available online, data before the late 1980’s are available only on paper records. The series used in this paper comes mainly from the Mexican Central Bank online database (<a href="http://www.banxico.com">www.banxico.com</a>). Alternative Sources are: The Mexican Secretariat for Public Finance (SHCP), The National Statistics Institute (INEGI), and the Mexican Senate Economic Affairs Center.</td>
</tr>
<tr>
<td><strong>R</strong></td>
<td>Natural logarithm of the average of time deposit interest rates 1970-2006</td>
<td>This series was calculated using the CPP (<em>costo porcentual promedio</em>) that corresponds to the simple average of nominal interest rates. The registry of this type of index started in 1975, so the series was extended back to 1970. Sources: Mexican Central Bank, alternative source: <em>Diario Oficial de la Nacion</em></td>
</tr>
<tr>
<td><strong>REM</strong></td>
<td>Natural logarithm of remittances normalized by GDP 1970-2006</td>
<td>World Development Indicators (World Bank) and Banxico. The series was used in national currency</td>
</tr>
<tr>
<td><strong>M1</strong></td>
<td>1970-2006 in local currency</td>
<td>International Financial Statistics (IMF) and Banxico</td>
</tr>
<tr>
<td><strong>Inflation</strong></td>
<td>1970-2006</td>
<td>International Financial Statistics (IMF)</td>
</tr>
<tr>
<td><strong>Unemployment</strong></td>
<td>Rate of unemployment respect to Economic active population in urban areas 1976-2006</td>
<td>World Economic Outlook (IMF) and INEGI. Note: the first estimations were computed by INEGI using as sample only 3 major cities. Nowadays estimates are done in a much wider sample.</td>
</tr>
<tr>
<td><strong>Foreign Direct Investment</strong> (<strong>FDI</strong>)</td>
<td>Net Inflows (BoP current US dollars) 1970-2005</td>
<td>World Development Indicators (World Bank)</td>
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## Unit Root Tests

<table>
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<th>R</th>
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<td>First Difference</td>
<td>-6.72***</td>
<td>-4.12***</td>
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<td>-4.80***</td>
<td>-4.83***</td>
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Above we present the test statistics for both the Augmented Dickey-Fuller and the Phillips-Perron tests. The lag length was chosen using the Schwarz Information Criterion. Null Hypothesis: variable has a unit root.

Note: *** indicate rejection of the null hypothesis at 1 percent level. 
** indicate rejection of the null hypothesis at 5 percent level 
* indicate rejection of the null hypothesis at 10 percent level 
a. test was conducted using an intercept 
b. test was conducted using a trend and intercept 
c. no trend nor intercept included
Cointegration Test

Johansen Cointegration Test

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<th>5% Value</th>
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Given the small size of our series we used a maximum of two lags running the tests. No deterministic trend.

Estimated Matrix of Adjustment coefficients

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<td>(0.09)</td>
<td>(0.34)</td>
<td>(1.36)</td>
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Standard errors in parentheses

INEGI Survey

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<td>2001</td>
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<tr>
<td>2004</td>
<td>28.76</td>
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<td>2005</td>
<td>28.13</td>
</tr>
<tr>
<td>2006</td>
<td>27.20</td>
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</table>

Source: INEGI, Mexico.
Note: Annual Averages

Given the small size of our series we used a maximum of two lags running the tests. No deterministic trend.
Figure 2. Inflation, Unemployment and Remittances in Mexico (1970-2006)

Sources: INEGI, International Financial Statistics (IMF), World Development Indicators (World Bank), Mexican Central Bank (Banxico), INEGI.

Note: Right axis corresponds to inflation, both axis in percentage. Unemployment corresponds to the percentage of Economic Active Population, while remittances are in percentage of GDP in national currency.
References


