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30 January 2018

Online at <https://mpra.ub.uni-muenchen.de/84474/>

MPRA Paper No. 84474, posted 14 February 2018 23:06 UTC

The Effects of Temporal Aggregation on Search Engine Data

By

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Abstract

Using structured machine learning, this paper examines the effect that temporal aggregation has on big data from Google Analytics and Google Trends. Specifically, daily and weekly data from the Charleston Area Convention and Visitors Bureau (CACVB) website from January 2008 to March 2009 via Google Analytics and weekly, monthly, and quarterly data from Google Trends for seven economic variables from 2004 to 2011 are examined. Taking into account the different levels of aggregation, the CDFs and the estimated regression results are examined. The Kolmogorov-Smirnov test rejects the null of equivalent data distributions in the vast majority of cases for the CACVB data, but this is not the case for the economic variable. Through data mining, this paper also finds that aggregation has the potential of affecting the level of integration and the regression results for both the CACVB data and the seven economic variables.

KEYWORDS: Big Data, Machine Learning, Data Mining, Aggregation, Unit roots, Scaling Effects, Normalization Effects

JEL Classification Codes: C55, C43, C19

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1. Introduction

Search engine data is one form of big data and it is a new source for time series data, which is able to capture economic and societal trends almost instantaneously. This has led to the relatively new field of nowcasting in economics, finance, and business. Big data lends itself exceedingly well to machine learning and data mining, which refers to the ability to obtain new information from the existing data (Jun, Yoo, and Choi 2017; Fürnkranz, Gamberger, and Lavrač 2012). Nowcasting refers to using the past to predict the present or the very near future and structured machine learning techniques permit us to find these trends.

One type of big data used in this paper is from Google Trends, which provides an index of the volume of web searches for a specific key word or phrase such as '*mortgage defaults*' in the U.S.¹ Graph 3A demonstrates that pre-2005, the search for '*mortgage defaults*' is virtually non-existent, but gradually, interest begins to build in March 2007 until it hits a peak in September 2008, which is consistent with the start of the Financial Crisis of 2008. A similar story unfolds in Graph 3B regarding '*gold price*,' which hits its peak in March 2008 since investors turn to gold during times of economic turmoil.

With this new source of data generating a great deal of research especially in machine learning area, it is important to understand the properties of this data given that this data has been previously normalized and scaled. Specifically, this paper studies the effect of aggregation on Google Analytics, another source of big data, and Google Trends data by examining the cumulative distribution functions (CDFs) and the estimated regression output, which are important for forecasting and policy-making decisions.

If the data characteristics are being distorted with higher levels of aggregation, then this could cause a loss of information. Many of the economic models use either monthly or quarterly data and, often, the data is transformed in

¹ Google Trends was formerly known as Google Insights. The web address for Google Insights is: <http://www.google.com/insights/search/>, which now take you to the same website for Google Trends, <http://www.google.com/trends>. Additional sources of search engine data can be obtained from Google Analytics, <http://www.google.com/analytics/> (Horák, Ivan, Kukuliač, Inspektor, Devečka, and Návratová 2013)

order to obtain the desired level of aggregation, which is why it is crucial to better understand the effects of aggregation on regressions results.

Previous work relating to aggregation and the use of normalized and scaled variables posed some problematic findings.² For instance, in the field of information technology (IT), as it relates to the central processing unit, memory, bandwidth usage, etc., Marvasti (2010) has found that aggregation affects the data distribution and decreases the data range, which affects the tail regions. Analogously, when using search engine data, Tierney and Pan (2013) find that the level of dispersion generally changes from under- to over-dispersion when using daily and weekly data to examine the relationship between website traffic and search volume data.

Along the lines of Marvasti (2010), this paper examines the effect of temporal aggregation on the CDFs of time series data obtained from Google Trends and Google Analytics through the use of the two-sample Kolmogorov-Smirnov (KS) test.

Regarding the estimated regression results, the averaging or aggregation of data has the potential of adversely affecting the estimated parameters of the model and the RSS, which specifically affects the variance and the estimated test statistics (Granger and Siklos 1995, Rossana and Seater 1995, Marcellino (1999), Garrett 2002).

According to Garrett (2002), the aggregated coefficient is supposed to be the sum of the coefficients from the regression using the less aggregated data. This paper does not find this to be the case when using data from either Google Analytics or Google Trends.

In order to study the effects of temporal aggregation on search engine data, this paper uses data from two sources. The first source of data is daily and weekly data for six search volume time series that are obtained from the Charleston Area Convention and Visitors Bureau (CACVB) website from January 2008 to March 2009 which is obtained using Google Analytics.³ The second source of data involves weekly data from Google Trends for seven variables of potential economic interest,

² Aggregation has the potential to add 'noise' while making it harder to separate the trend, i.e. long-run fluctuations from the cycle, which refers to short-run fluctuations (Garrett 2002).

³ The web address of the CACVB website is as follows: www.charlestoncvb.com.

which from now on will be referred to as the economic dataset. These variables are *'unemployment,' 'inflation,' 'mortgage defaults,' 'US deficits,' 'GDP,' 'economic growth,'* and *'gold price.'*

The CDFs of the daily and weekly data of the CACVB website are tested using the two-sample KS test evaluated at the 5% significance level in order to determine if they are statistically equivalent. Regarding the economic dataset, the weekly data is transformed into monthly and quarterly data. The KS test is used to compare the CDFs of the weekly data against the aggregated versions of monthly and quarterly data.

The structure of this paper is as follows: Section 2 presents a brief discussion of the data; Section 3 presents the methodology; and Section 4 contains the empirical results and Section 5 conclusion.

2. Discussion of the Data

Google Trends does not provide the raw big data; it readily provides weekly data, and it can provide daily and weekly data that requires a specialized program in order to obtain the daily search volume results, which is how the CACVB data has been obtained. Both the daily and weekly data have been normalized and then scaled. Each data point reflects the ratio of the number of searches for a particular key word or phrase to the total number of searches done on using the Google search engine during a given week (Google Trends 2011c).

The normalization process refers to dividing the dataset by a particular variable in order to remove the variable's effect of the data so that the absolute rankings may be obtained. This is to remove the effect of geographic areas with the largest search volumes from always being ranked higher. The problem when it comes to interpreting the data is that the same index number for two different regions does not reflect the same search volume levels but how likely they are to search for a particular key word or phrase (Google Trends 2011a). The scaling process reduces the range of the data to be between 0 and 100 with each data point being divided by the highest value or 100 (Google Trends 2011b).

The CDFs obtained from five quarters of daily data are tested against the CDFs of the weekly data of the CACVB website, which are obtained from Google Analytics. Four of the CACVB search volume variables are obtained from a universal search in all categories and are denoted by *(all)*, which follows the variable. The remaining two of the CACVB search volume variables are restricted to searches only within the travel category and are followed by the term *(travel)*. The variables are as follows: 'charleston sc' *(all)*, 'charleston hotels' *(all)*, 'charleston restaurants' *(all)*, 'charleston travel' *(all)*, 'charleston sc' *(travel)*, and 'charleston hotels' *(travel)*. Table 1A provides a summary of the variables along with their abbreviations, Table 2A provides the number of observations, and Table 3A provides their exact data samples, which ranges from January 2008 to March 2009.

To construct the CDFs, the level data is used while the log forms of the data are used for the structured machine learning, which pertains to the regressions with the intent of data mining, i.e. obtaining new information using big data (Fürnkranz, Gamberger, and Lavrač 2012). The log forms of the data aids in the interpretation of the estimated regression coefficients and it helps to reduce the magnitude of the regressand, which is "*Y_all_visits*" *(all)* for the regressions involving the CACVB data. "*Y_all_visits*" *(all)* is all the website traffic, i.e. the number of hits to the CACVB website during the given time period and its frequency is in both the daily and weekly versions.

The regressand "*Y_all_visits*" *(all)* is data that has not been normalized and scale, and so it is possible to see the magnitude of big data with respect to just the CACVB website. The mean for the weekly version of "*Y_all_visits*" *(all)* is 24,808.90 hits with the minimum being 13,893 and the maximum being 32,773 hits from January 2008 to March 2009.

Search engine data is count data but it is also time series data, which means there could be stationarity issues.⁴ It is important to test for unit roots because it impacts the test statistics from the structured machine learning results. To test for stationarity, the Augmented Dickey-Fuller (ADF) and the Elliott-Rothenberg-Stock

⁴ Hellström (2002), Pavlicek, J. and Kristoufek, L. (2015), and Kristoufek, Moat, and Preis (2016) found unit roots when working with count data or search engine data.

Point Optimal Test, which is now referred to as ERS, are used (Said and Dickey 1984, Elliot, Rothenberg, and Stock 1996).

One interesting finding of this paper is that the level of stationarity can differ with the level of aggregation. A summary of the unit root results with the inclusion of a constant term and a time trend for the CACVB data can be found in Table 7A.⁵ A unit root is found in both the daily and weekly data of "*Y_all_visits*" (*all*), *charleston hotels*' (*all*), and *charleston sc*' (*travel*). The daily and weekly data of *charleston restaurants*' (*all*) are found to be stationary.

Both the ADF and ERS tests find the daily data of *charleston travel*' (*all*) and *charleston hotels*' (*travel*) to be stationary while the weekly version to contain a unit root. When the level of integration differs with the level of aggregation, this makes comparing the regression output much more difficult.

Unit root tests are known to have low power, so it is understandable that there would be some conflicting results.⁶ The ADF and ERS test obtain conflicting results with respect to the weekly data of *charleston sc*' (*all*). The ADF test finds a unit root while the ERS test does not.

The ADF and ERS tests find the regressand, the log of "*Y_all_visits*" (*all*) to contain a unit root for both the daily and weekly data. Hence, the first difference of the log of "*Y_all_visits*" (*all*) is used in all the estimated regressions involving the CACVB data.

Table 1B presents a list of the search volume variables examined, which are *unemployment*, *inflation*, *mortgage defaults*, *US deficits*, *GDP*, *economic growth*, and *gold price* with Table 2B presenting the number of observations for the weekly, monthly, and quarterly data. The data range for the economic dataset is from 2004 to 2011 with more detail being presented in Table 3B.

For the regressions, the log versions of *unemployment*, *inflation*, *GDP*, *economic growth*, and *gold price* are used since *mortgage defaults* and *US deficits*

⁵ Sequential testing of the data using the ADF and ERS tests have been applied to the data and the aforementioned results hold.

⁶ Having low power refers to the occurrence of a Type II error, which is failing to reject the null when the null is actually false (have a false negative). In other words, a Type II error is made if we fail to reject H_0 when H_1 is true.

have too many missing observations. The unit root testing of the economic dataset proved to be more conflicted as is shown in Table 7B.

The ADF and ERS tests find unit roots in the weekly and monthly versions of ‘unemployment’ but they differ with respect to quarterly data. The ADF finds a unit root while the ERS test does not. The weekly and monthly versions of ‘inflation,’ are stationary. The ADF test using quarterly data of ‘inflation’ finds stationarity while the ERS test finds a unit root. There appears to be stationarity in the weekly and monthly data of ‘GDP’ and a unit root in the quarterly data of ‘GDP’ according to both the ADF and ERS tests.

The ADF and ERS tests are in disagreement regarding ‘economic growth’ except for the weekly data version where they find stationarity. For the monthly version of ‘economic growth,’ the ADF test finds it to be stationary and the quarterly version to be non-stationary and the ERS test obtains the opposite results.

For ‘gold price,’ the ADF and ERS tests find the weekly version to be stationary and the quarterly version to be non-stationary. There is dissent with respect to the monthly version of ‘gold price.’ The ADF finds the monthly version to be stationary while the ERS test finds a unit root.

3. The Methodology

3.1 Examining the CDFs

The reason for utilizing the two-sample KS test over some other empirical density test is that it permits the comparison of two empirical CDFs.⁷ For this paper, the CDFs of the aggregated data is compared to a benchmark CDF in the two-sample KS test, which is a nonparametric test for comparing two empirical distributions (Kim 1969, Kim and Jennrich 1973, Marvasti 2010). In this case the term, nonparametric refers to comparing two empirical CDFs of the variables, X and Y with the total number of observations being M and N respectively. The empirical CDFs for X and Y are as follow:

$$F_X(x) = P(X \leq x) = \frac{1}{M} \sum_{m=1}^M I(X_m \leq x) \quad (1)$$

⁷ The other empirical density tests are designed to compare one empirical CDF against an alternate pre-specified CDF such as the normal CDF.

and

$$F_Y(y) = P(Y \leq y) = \frac{1}{N} \sum_{n=1}^N I(Y_n \leq y) \quad (2)$$

The benefits of using the KS test are that it is robust, not sensitive to scaling, and works well when the data is not from the normal distribution. The KS test is problematic when the data is normal. Hence, it is important to test for the normality of the data, which is done using the following normality tests: Lilliefors, Cramer-von Mises, Anderson-Darling, and Watson empirical distribution tests and the Jarque-Bera Normality Test (Stephens 1970, Stephens 1974). The null hypothesis for the aforementioned tests is that the data is normal.

There are various forms of the KS test, especially as it pertains to obtaining the critical values (CV), so it is important to discuss the specific form used, which is the one specified by Capon (1965). Regarding the KS test, the hypothesis test concerns the CDFs of X and Y and is of the following form: $H_0 : F_X = F_Y$ versus $H_1 : F_X \neq F_Y$. F_X and F_Y will differ by some amount δ , and so the KS test amounts to measuring the distance, D_x between the F_X and F_Y that is greater than δ , i.e.

$$D_x = \sup_{x \in \mathbb{R}} |F_X(x) - F_Y(x)| > \delta \quad (3)$$

The KS test statistic, KS_x is as follows:

$$KS_x = \left(\frac{mn}{m+n} \right)^{1/2} \sup_x |F_X(x) - F_Y(x)| \quad (4)$$

If the null hypothesis fails, then

$$KS_x = \left(\frac{mn}{m+n} \right)^{1/2} D_x > \left(\frac{mn}{m+n} \right)^{1/2} \delta \quad (5)$$

which means that a threshold g needs to be determined based on the CV that is 5% for this paper. The CV depends upon the threshold g and the KS distribution $H(\cdot)$ and is as follows:

$$\alpha = P \left[\left(\frac{mn}{m+n} \right)^{1/2} \delta \neq H_0 | H_0 \right] = P(KS_x > g | H_0) \approx 1 - H(g). \quad (6)$$

Hence, the KS test amounts to testing:

$$H_0 : KS_x \leq g = \left(\frac{mn}{m+n} \right)^{1/2} * (\text{CV of the KS distribution})$$

$$H_1 : KS_x > g = \left(\frac{mn}{m+n} \right)^{1/2} * (\text{CV of the KS distribution})$$

with the CV values for the large sample approximation obtained from Massey (1951) and the tables of Miller (1956). For this paper, the CV for the CACVB data is 1.33 using the tables provided by Miller (1956) and is 1.33 for the KS test involving monthly data and 1.32 when using quarterly data for the economic dataset. The large sample CV approximation is 1.36 for both datasets.

3.2 Examining the Estimated Structured Machine Learning Results

The type of machine learning used in this paper is structured machine learning in the form of regression analysis (Alpaydin 2009; Fürnkranz, Gamberger, and Lavrač 2012). The purpose of these regressions is to compare the effect of aggregation on the estimate regression coefficients and the RSS. According Garrett (2002), estimated regression results demonstrate a certain pattern. The sum of the estimate coefficients from the less aggregated data should sum to the estimate coefficient of the aggregated data. For the CACVB dataset, the regressand is the log of "*Y_all_visits*" (*all*) and the regressors being the log verisons of '*charleston sc*' (*all*), '*charleston hotels*' (*all*), '*charleston restaurants*' (*all*), '*charleston travel*' (*all*), '*charleston sc*' (*travel*), and '*charleston hotels*' (*travel*) with each being run as a separate regression.

For example, for the daily CACVB data, the first difference of the log of "*Y_all_visits*" (*all*) is regressed onto the log of '*charleston sc*' (*all*) and six lags to account for the 7-day week. With the exclusion of the constant term, the seven estimated regression coefficients are summed and then compared to the estimated coefficients of the weekly data with the regressand also being the first difference of the log of "*Y_all_visits*" (*all*). This is done for the remaining regressors taking into account the level of stationarity of each.

Regarding the economic dataset, an AR(p) model is used with the p-lags depending on the level of aggregation. The weekly data is compared to the monthly data and the monthly data is compared to the quarterly data. Hence, the regressions with the weekly data have 4 lags, which are then compared to their monthly counterparts, which have only 1 lag. Alternatively, when comparing the monthly data to the quarterly data, the regressions with the monthly data have 3 lags while the regressions with the quarterly data have only 1 lag.

4. Empirical Results

4.1 Empirical Results of the CDFs

Since access to the raw data is not permitted due to Google's privacy policy, each of the CDFs of the daily data is measured against the weekly data in the CACVB dataset (Barbaro and Zeller 2006). Analogously, in the economic dataset, the weekly dataset is used at the benchmark against the monthly and quarterly data.

The results for the tests for normality of Lilliefors, Cramer-von Mises, Anderson-Darling, and Watson empirical distribution tests and the Jarque-Bera Normality Test are presented in Table 5A for the CACVB data and in Table 5B for the economic data. The p-values in bold print in Tables 5A and 5B indicate that the null of normality is rejected at the 5% significance level. Due to the low power of the normality tests, there are some contradictory findings. All the normality tests *reject normality* for the variable '*charleston sc*' (*all*) in the second, third, fourth, and fifth quarters except for the Lilliefors test in the fourth quarter and the Jarque-Bera test in the fifth quarter when using daily data. When using weekly data, the null of normality is rejected for all the normality tests except for the Jarque-Bera test with respect to the variable '*charleston sc*' (*all*). For the variable '*charleston restaurants*' (*all*), *the null of normality fails to be rejected* for most of the hypothesis tests when using daily data in the first, second, and third quarters as well as in the weekly data. The Lilliefors test *rejects the null of normality* in the second quarter of daily data for '*charleston restaurants*' (*all*) and the Jarque-Bera test rejects the null of normality

the second quarter of daily data and for the weekly data as well. The majority of the normality tests for the remaining quarters using daily data *fails to reject normality*.

The CDFs of the six search volume variables using the daily data from the fourth quarter and the weekly data of the CACVB website demonstrates that there is a noticeable gap between both CDFs, which is shown in Graphs 1A through 1F. The ranges of the CACVB data is given in Table 4A. The range for the search volume index of 'charleston hotels' (all) for weekly data is from 3 to 7 and the range for the daily data is from 26 to 100, which accounts for the CDFs in Graph 1B.

Table 6A provides the KS test results with the statistically significant results in bold print. With only three exceptions of the first quarter of 'charleston sc' (all) and the first and third quarter of 'charleston sc' (travel), the null of statistically equivalent CDFs is rejected even when using the more conservative CV of 1.36 as is provided by Massey (1951).

Concerning the economic dataset, the *null of normality fails to be rejected* for the vast majority of variables as is demonstrated in Table 5B for the monthly and quarterly aggregated search volume variables. The ranges of the variables of the economic dataset are presented in Table 4B and as Marvasti (2010) noted, the ranges decrease with higher levels of aggregation.

The *null of normality is rejected* at the 5% significance level for weekly, monthly, and quarterly 'unemployment' data except for the Jarque-Bera test when using quarterly data. Weekly 'mortgage defaults,' 'US deficits,' 'GDP,' 'economic growth,' and 'gold price,' all reject the null of normality at the 5% significance level, which is not necessarily the case when using monthly and quarterly data. 'inflation' fails to reject the null of normality except for the Lilliefors test when using weekly data. Hence, there are conflicting results with respect to the normality tests and the various levels of aggregation concerning the economic dataset.

The CDF graphs of the weekly and quarterly data for the economic dataset are presented in Graphs 2A through 2G, and as one can see that there is very little difference between the two CDFs. The graph with the largest difference between the CDF of the weekly and quarterly data involves the graph of 'GDP,' which produces the largest KS test statistic of 1.214 for the economic dataset, but since it is

less than the CV of 1.36, the null of equivalent empirical CDFs fails to be rejected. In fact, the null of equivalent empirical CDFs fails to be rejected for the two-sample KS test involving either monthly or quarterly data.

4.2 Estimated Structured Machine Learning Results

Just as with the comparison of the CDFs, when using the CACVB dataset, the estimated structured machine learning results also find there to be no agreement between the daily and weekly data, which are given in Tables 8 and 9. Tables 8 and 9 provide the regressions results for the first difference and the level version of the log of the regressors when there is disagreement between the ADF and ERS tests or disagreement with the level of integration based on the aggregation level.

As indicated by Garrett (2002), the RSS of the regressions in the less aggregated data, i.e. the daily data are greater than the RSS of the regressions using the weekly data as is demonstrated in Table 9. So, it is not surprising that most of the estimated coefficients of the regressions using the weekly data are statistically significant with the exception of '*charleston travel*' (*all*) since the RSS are smaller.

The sum of the estimated regression coefficients when using the daily data also differs from its weekly data counterpart. For instance, the sum of the daily coefficients of all the regressors are negative with the exception of "*charleston travel*" (*all*) and the estimated coefficient from the regression with the weekly data are all positive.

As has been previously stated, the monthly and quarterly versions of the data in the economic dataset are formed from weekly data. Aggregating data before performing a regression is commonplace in most fields such as economics, finance, and business. This paper analyzes the effect of aggregating the data before performing a regression.

Furthermore, comparing regressions results from data with different levels of aggregation and different levels of integration is proving to be problematic especially with respect to the economic dataset. In terms of statistical significance, the regressions using the weekly data fare better than the regressions using the monthly data.

The regression results for the economic dataset are provided in Tables 10 and 11. The estimated coefficient of the first lag in the regression using monthly data are statistically insignificant except for the regression involving the level form of inflation, where the estimated coefficient is 0.0001. In this instance, the opposite of what Garrett (2002) expects is obtained. The sum of the estimate coefficients using the weekly data do not match their monthly counterpart. The RSS of the regressions using monthly data are smaller than the regressions using weekly data.

It should be noted that the R-squared terms for the regressions using monthly data is 0.00 or 0.01 for the first difference of the log of '*unemployment*,' '*inflation*,' '*GDP*,' '*economic growth*,' and '*gold price*.' Actually, this is not surprising because the monthly versions of '*inflation*' and '*GDP*' are stationary and the ADF and ERS tests are conflicted when it comes to monthly '*economic growth*,' and '*gold price*.'

Regarding the comparison of the estimated regressions coefficients of monthly and weekly data, the only statistically significant coefficients are the level form of the log versions of '*inflation*,' '*economic growth*,' and '*gold price*.' The ADF and ERS tests produce contrary results for the quarterly versions of '*inflation*' and '*economic growth*,' but quarterly '*gold price*' is considered to be stationary. It should be noted that the regression using the first difference of the log of '*gold price*' has an R-squared value of 0.00, meaning that the model is not captured by an AR(1), which makes it difficult to compare estimated regression results.

As is the case with the CACVB dataset, the sum of the estimated coefficients of the regressions revolving monthly data are not equivalent of their quarterly counterpart as is shown in Table 11.

Hence, when it comes to estimating regressions, caution needs to be used in aggregating the data and more importantly, in interpreting the data. For example, estimated regression results obtained from less aggregated data should not be used to draw conclusions for more aggregated data.

5. Conclusion

This paper looks at two sources of big data with the intent of examining whether or not temporal aggregation affects the CDFs and the estimated structured machine learning results. Specifically, two different types of data are examined: the CACVB dataset, which uses data from Google Analytics, and the economic dataset, which uses data from Google Trends.

The CACVB data provides daily and weekly data that already have been normalized and scaled. Regarding the economic dataset, the monthly and quarterly versions of the economic dataset are aggregated from the normalized and scaled weekly data, which is a regularly used method of aggregation in the field of economics.

Regarding the CDFs of the CACVB data and the economic dataset, the KS test rejects the null of equivalent data distributions in the vast majority of cases for the CACVB data using daily and weekly data with only three exceptions, which are the first quarter of *'charleston sc' (all)* and the first and third quarter of *'charleston sc' (travel)*.

The findings in the economic dataset are opposite of that of the CACVB dataset with respect to the CDFs. For the economic data set, the CDFs of the weekly data is compared to the CDFs of the monthly and quarterly data. Based upon the two-sample KS test, it appears that aggregating the data after it has been normalized and scaled does not affect the data distribution but it does decrease the range as evidenced by the results regarding the economic dataset.

Regarding the structured machine learning portion of this paper, it is important to test for the unit roots with each level of aggregation. It is possible for less aggregated data to be stationary while higher levels of aggregation can be non-stationary, which occurs in both the CACVB and the economic datasets.

In addition, when both the CACVB dataset and the economic data set are used in regressions, which is the form of structured machine learning used in this paper, it appears that aggregation affects the estimated coefficients. The sum of the estimated coefficients of the regressions using daily data do not come close to the

estimated coefficients of the regressions using weekly data. For the economic dataset, the same pattern of the sum of the estimated coefficients of the regressions using less aggregated data do not come close to the estimated coefficients of the regressions using more aggregated data.

In conclusion, when using big data from Google Analytics and Google Trends, it is important to take note of the structure of the data for data mining purposes. Inferences pertaining to less aggregated data cannot be extrapolated to higher levels of aggregation as has been demonstrated using both the CACVB and the economic datasets.

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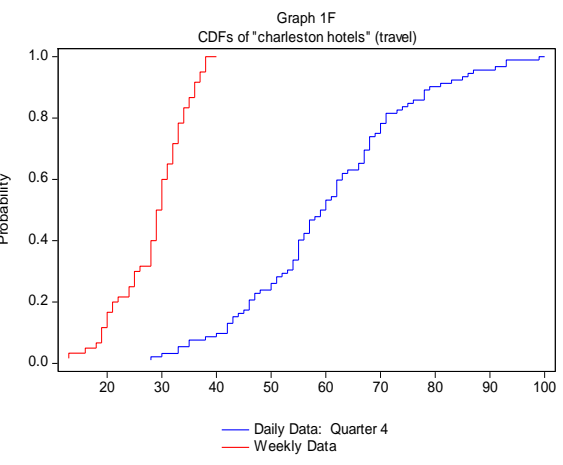
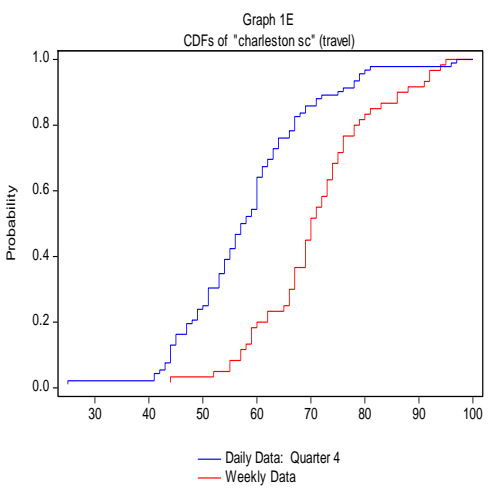
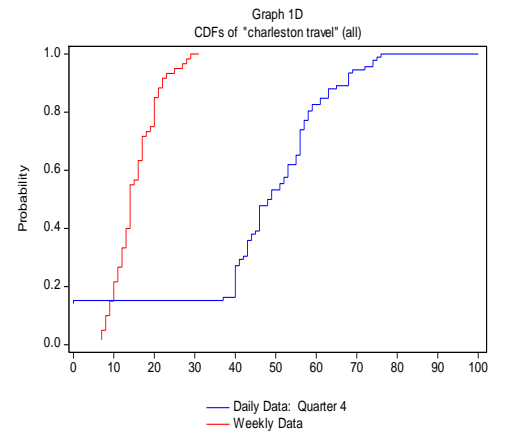
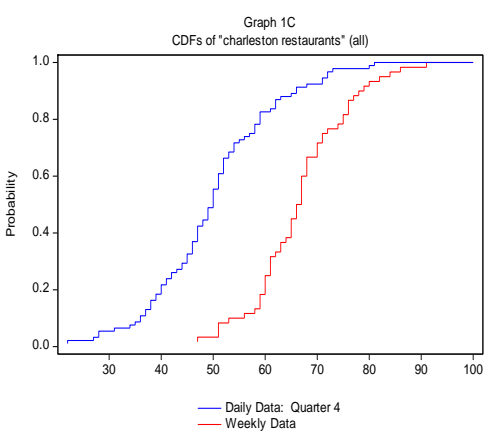
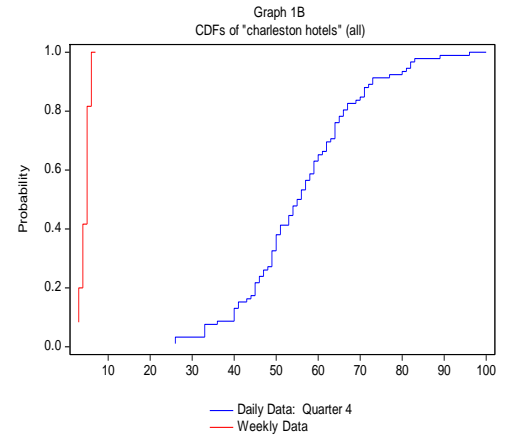
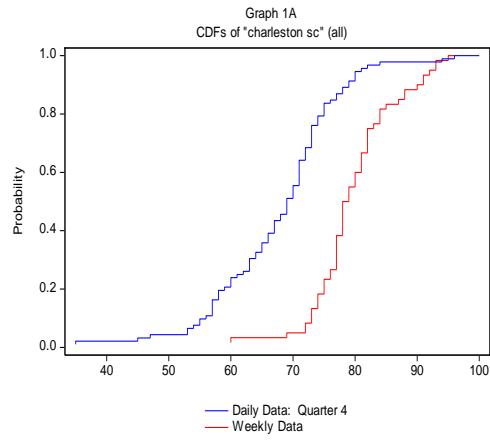
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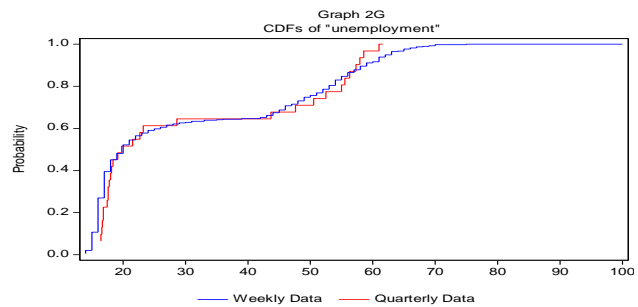
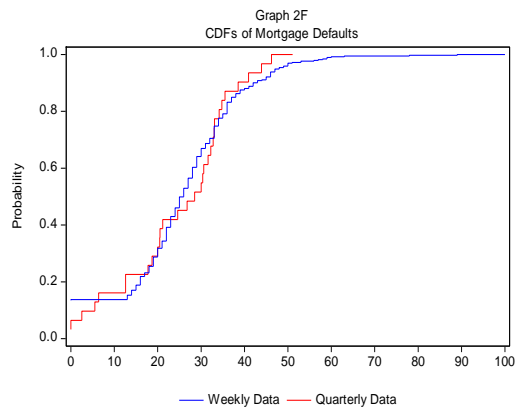
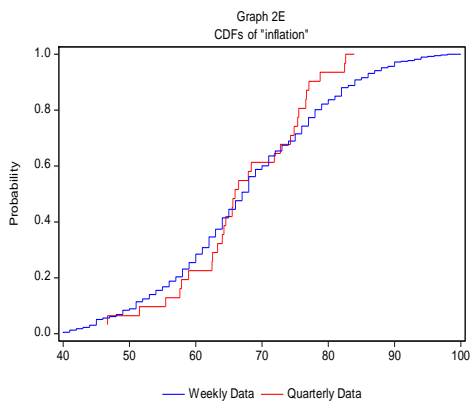
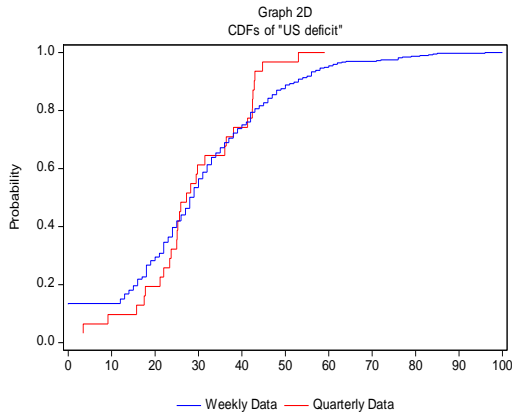
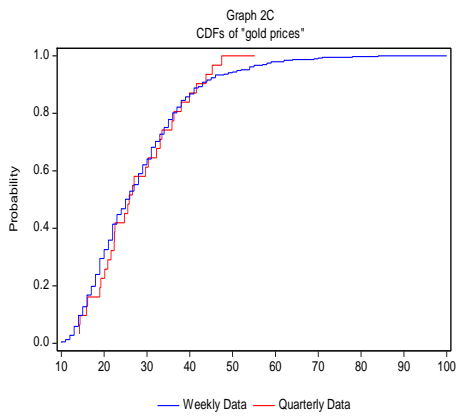
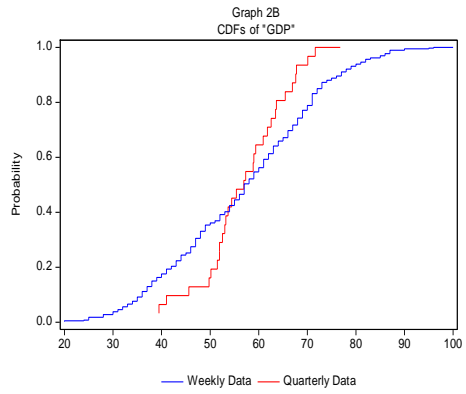
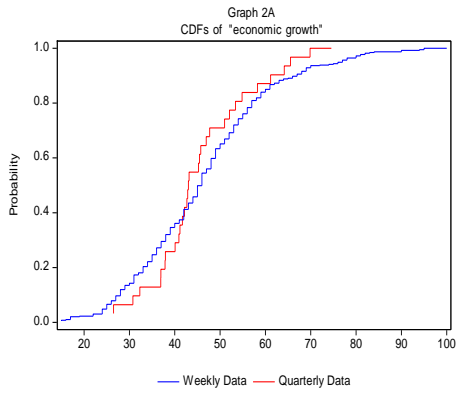
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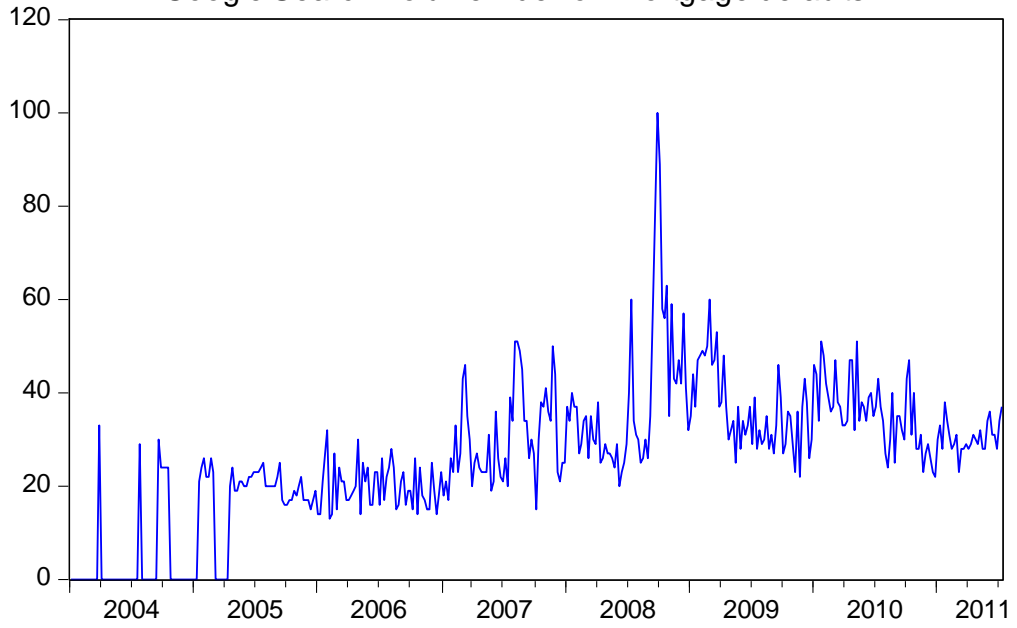
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Graph 3A
Google Search Volume Index of "mortgage defaults"



Graph 3B
Google Search Volume Index of "gold prices"

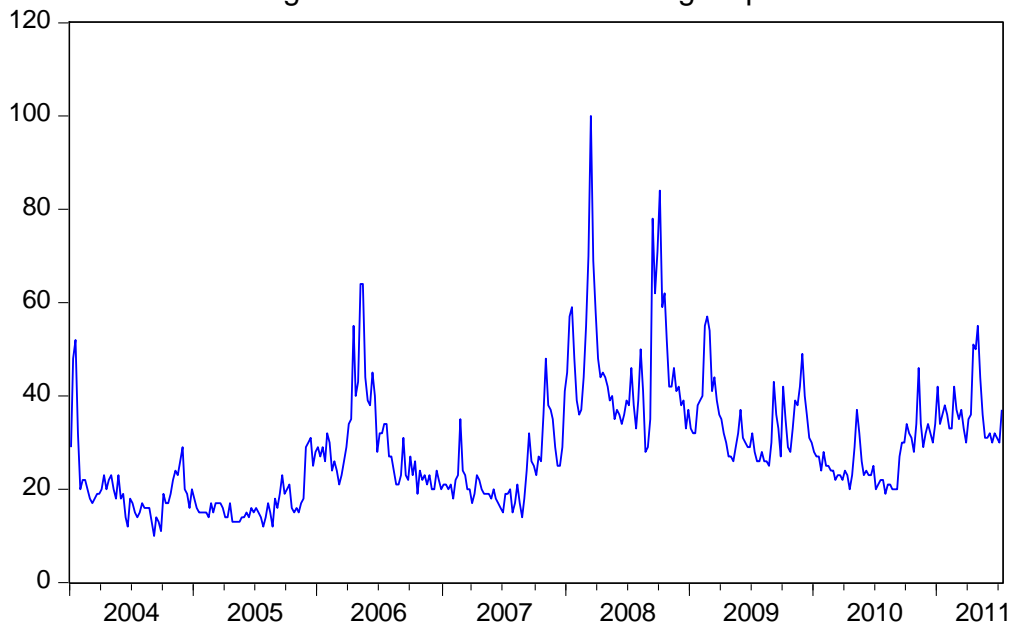


Table 1A: Legend of CACVB Data

Variables	Abbreviations of Variables	Type of Searches
"charleston sc" (all)	ch sc (all)	All Category
"charleston hotels" (all)	ch hotels (all)	All Category
"charleston restaurants" (all)	ch restaurants (all)	All Category
"charleston travel" (all)	ch travel (all)	All Category
"charleston sc" (travel)	ch sc (travel)	Travel Category
"charleston hotels" (travel)	ch hotels (travel)	Travel Category

Table 1B: Legend of Economic Data

Variable	Abbreviations of Variables	Type of Searches
"unemployment"	UNEMP	All Category
"inflation"	INFL	All Category
"mortgage defaults"	MORTDEF	All Category
"US deficits"	GOVDEF	All Category
"GDP"	GDP	All Category
"economic growth"	ECONGRO	All Category
"gold prices"	GOLDP	All Category

Table 2A: Number of Observations of CACVB Data

Variables	Daily-Q1	Daily-Q2	Daily-Q3	Daily-Q4	Daily-Q5	Weekly
"charleston sc" (all)	83	91	92	92	75	60
"charleston hotels" (all)	83	91	92	92	75	60
"charleston restaurants" (all)	83	91	92	92	75	60
"charleston travel" (all)	83	91	92	92	75	60
"charleston sc" (travel)	83	91	92	92	75	60
"charleston hotels" (travel)	83	91	92	92	75	60

Table 2B: Number of Observations of Economic Data

Variables	Weekly	Monthly	Quarterly
"unemployment"	393	91	30
"inflation"	393	91	30
"mortgage defaults"	393	91	30
"US deficits"	393	91	30
"GDP"	393	91	30
"economic growth"	393	91	30
"gold prices"	393	91	30

Table 3A: Data Samples of CACVB Data

Frequency	Data Sample
Daily-Q1	Jan 9, 2008 to Mar 31, 2008
Daily-Q2	Apr 1, 2008 to Jun 30, 2008
Daily-Q3	Jul 1, 2008 to Sep 30, 2008
Daily-Q4	Oct 1, 2008 to Dec 31, 2008
Daily-Q5	Jan 1, 2009 to Mar 16, 2009
Weekly	Jan 13 thru Jan 19, 2008 to Mar 1 thru Mar 7, 2009

Table 3B: Data Samples of Economic Data

Frequency	Data Sample
Weekly	Jan 4 thru Jan 10, 2004 to Jul 10 thru Jul 16, 2011
Monthly	Jan 2004 to Jul 2011
Quarterly	Jan 2004 to Jun 2011

Table 4A: Ranges of the CACVB Data

		<i>ch sc (all)</i>	<i>ch hotels (all)</i>	<i>ch restaurants (all)</i>	<i>ch travel (all)</i>	<i>ch sc (travel)</i>	<i>ch hotels (travel)</i>
Daily: Q1	Min	62	47	35	42	54	41
	Max	100	100	100	100	100	100
Daily: Q2	Min	58	46	30	41	52	36
	Max	100	100	100	100	100	100
Daily: Q3	Min	51	44	32	0	50	41
	Max	100	100	100	100	100	100
Daily: Q4	Min	35	26	22	0	25	28
	Max	100	100	100	100	100	100
Daily: Q5	Min	63	49	23	0	57	51
	Max	100	100	100	100	100	100
Weekly	Min	44	3	47	7	60	13
	Max	100	7	100	31	96	40

Table 4B: Ranges of the Economic Data

		<i>UNEMP</i>	<i>INFL</i>	<i>MORTDEF</i>	<i>GOVDEF</i>	<i>GDP</i>	<i>ECONGRO</i>	<i>GOLDP</i>
Weekly	Min	14.00	40.00	0.00	0.00	20.00	15.00	10.00
	Max	100.00	100.00	100.00	100.00	100.00	100.00	100.00
Monthly	Min	15.50	43.60	0.00	0.00	32.25	25.75	12.00
	Max	75.75	94.25	67.25	84.50	91.25	80.75	70.40
Quarterly	Min	16.46	46.69	0.00	3.46	39.46	26.50	14.23
	Max	61.62	83.92	51.08	59.08	76.77	74.54	55.15

Table 5A: Normality Test Results for CACVB Data

	Normality Tests	<i>ch sc (all)</i>	<i>ch hotels (all)</i>	<i>ch restaurants (all)</i>	<i>ch travel (all)</i>	<i>ch sc (travel)</i>	<i>ch hotels (travel)</i>
Q1	Lilliefors	> 0.1	> 0.1	> 0.1	0.03	> 0.1	> 0.1
	Cramer-von Mises	0.33	0.49	0.42	0.00	0.35	0.59
	Watson	0.31	0.46	0.50	0.01	0.32	0.54
	Anderson-Darling	0.32	0.39	0.32	0.00	0.27	0.53
	Jarque-Bera	0.77	0.36	0.36	0.01	0.99	0.62
Q2	Lilliefors	0.00	> 0.1	0.01	> 0.1	> 0.1	> 0.1
	Cramer-von Mises	0.00	0.58	0.08	0.58	0.01	0.33
	Watson	0.00	0.53	0.11	0.53	0.02	0.32
	Anderson-Darling	0.00	0.54	0.09	0.54	0.00	0.26
	Jarque-Bera	0.02	0.83	0.00	0.07	0.18	0.38
Q3	Lilliefors	0.00	> 0.1	> 0.1	0.08	> 0.1	> 0.1
	Cramer-von Mises	0.00	0.31	0.88	0.28	0.89	0.35
	Watson	0.00	0.33	0.87	0.28	0.87	0.35
	Anderson-Darling	0.00	0.34	0.89	0.07	0.87	0.15
	Jarque-Bera	0.00	0.48	0.67	0.04	0.83	0.54
Q4	Lilliefors	0.09	> 0.1	0.01	0.00	0.03	> 0.1
	Cramer-von Mises	0.03	0.32	0.03	0.00	0.02	0.69
	Watson	0.02	0.45	0.04	0.00	0.04	0.74
	Anderson-Darling	0.02	0.28	0.05	0.00	0.01	0.65
	Jarque-Bera	0.01	0.10	0.00	0.00	0.00	0.50
Q5	Lilliefors	0.00	0.09	> 0.1	> 0.1	> 0.1	> 0.1
	Cramer-von Mises	0.00	0.43	0.03	0.24	0.44	0.24
	Watson	0.00	0.44	0.04	0.21	0.42	0.21
	Anderson-Darling	0.00	0.48	0.02	0.20	0.45	0.16
	Jarque-Bera	0.11	0.69	0.00	0.00	0.98	0.32
W	Lilliefors	0.02	0.00	> 0.1	0.01	> 0.1	0.00
	Cramer-von Mises	0.01	0.00	0.17	0.09	0.09	0.01
	Watson	0.01	0.00	0.20	0.13	0.08	0.02
	Anderson-Darling	0.01	0.00	0.20	0.08	0.10	0.02
	Jarque-Bera	0.75	0.11	0.03	0.14	0.42	0.21

Table 5B: Normality Test Results for Economic Data

	Normality Tests	<i>UNEMP</i>	<i>INFL</i>	<i>MORTDEF</i>	<i>GOVDEF</i>	<i>GDP</i>	<i>ECONGRO</i>	<i>GOLDP</i>
Weekly	Lilliefors	0.00	0.03	0.00	0.00	0.02	0.00	0.00
	Cramer-von Mises	0.00	0.21	0.00	0.00	0.00	0.00	0.00
	Watson	0.00	0.18	0.00	0.00	0.00	0.00	0.00
	Anderson-Darling	0.00	0.19	0.00	0.00	0.00	0.00	0.00
	Jarque-Bera	0.00	0.15	0.00	0.00	0.04	0.00	0.00
Monthly	Lilliefors	0.00	> 0.1	0.08	> 0.1	> 0.1	> 0.1	0.05
	Cramer-von Mises	0.00	0.25	0.11	0.58	0.38	0.17	0.01
	Watson	0.00	0.22	0.09	0.59	0.34	0.28	0.02
	Anderson-Darling	0.00	0.42	0.02	0.48	0.26	0.08	0.00
	Jarque-Bera	0.00	0.71	0.46	0.08	0.39	0.10	0.00
Quarters	Lilliefors	0.00	> 0.1	> 0.1	> 0.1	> 0.1	0.07	> 0.1
	Cramer-von Mises	0.00	0.46	0.27	0.25	0.87	0.03	0.25
	Watson	0.00	0.43	0.27	0.22	0.84	0.04	0.30
	Anderson-Darling	0.00	0.55	0.33	0.35	0.90	0.05	0.26
	Jarque-Bera	0.10	0.73	0.69	0.93	0.95	0.29	0.36

Table 6A

Results of the Two-Sample Kolmogorov-Smirnov (KS) Test of CACVB—Daily v. Weekly

Variable	KS Stat-Q1	KS Stat-Q2	KS Stat-Q3	KS Stat-Q4	KS Stat-Q5
"charleston sc" (all)	0.91	2.59	4.61	3.78	2.02
"charleston hotels" (all)	5.90	6.01	6.03	6.03	5.77
"charleston restaurants" (all)	1.42	3.43	1.95	3.91	3.79
"charleston travel" (all)	5.90	6.01	5.96	5.17	5.70
"charleston sc" (travel)	1.20	2.17	0.71	3.18	1.81
"charleston hotels" (travel)	5.90	5.95	6.03	5.50	5.77

Table 6B

Results of the Two-Sample Kolmogorov-Smirnov (KS) Test using Weekly Economic Data

Variable	KS Test Stat--Monthly Data	KS Test Stat--Quarterly Data
"unemployment"	0.608	0.567
"inflation"	0.623	0.727
"mortgage defaults"	0.528	0.587
"US deficits"	0.662	0.702
"GDP"	0.625	1.214
"economic growth"	0.545	0.931
"gold prices"	0.447	0.510

Table 7A: Unit Root Tests for CACVB Data

	ADF Test: Trend & Const			Outcome	ERS: Trend & Const		Outcome
	Est. T-Stat	5% CV	P-value	Unit Root?	Est. P-Stat	5% CV	Unit Root?
<i>"Y_all_visits" (all)</i>							
Daily	-1.01	-3.42	0.94	Yes	32.60	5.62	Yes
Weekly	-0.89	-3.49	0.95	Yes	21.72	5.70	Yes
<i>"charleston sc" (all)</i>							
Daily	-2.93	-3.42	0.15	Yes	6.67	5.62	Yes
Weekly	-3.43	-3.49	0.06	Yes	5.41	5.70	No
<i>"charleston hotels" (all)</i>							
Daily	-3.30	-3.42	0.07	Yes	5.93	5.62	Yes
Weekly	-2.05	-3.49	0.56	Yes	9.84	5.70	Yes
<i>"charleston restaurants" (all)</i>							
Daily	-6.71	-3.42	0.00	No	1.74	5.62	No
Weekly	-4.68	-3.49	0.00	No	4.36	5.70	No
<i>"charleston travel" (all)</i>							
Daily	-12.52	-3.42	0.00	No	0.93	5.62	No
Weekly	-2.71	-3.49	0.24	Yes	7.45	5.70	Yes
<i>"charleston sc" (travel)</i>							
Daily	-2.83	-3.42	0.19	Yes	7.61	5.62	Yes
Weekly	-1.29	-3.49	0.88	Yes	16.60	5.70	Yes
<i>"charleston hotels" (travel)</i>							
Daily	-12.64	-3.42	0.00	No	0.60	5.62	No
Weekly	-0.72	-3.49	0.97	Yes	25.16	5.70	Yes

Table 7B: Unit Root Tests for Economic Data

	ADF Test w/ Trend & Const			Outcome	ERS Trend & Const		Outcome
	Est. T-Stat	5% CV	P-value	Unit Root?	Est. P-Stat	5% CV	Unit Root?
<i>"unemployment"</i>							
Weekly	-2.81	-3.42	0.20	Yes	18.54	5.62	Yes
Monthly	-2.49	-3.46	0.33	Yes	28.48	5.66	Yes
Quarterly	-2.81	-3.60	0.21	Yes	0.95	5.72	No
<i>"inflation"</i>							
Weekly	-6.55	-3.42	0.00	No	1.40	5.62	No
Monthly	-8.26	-3.46	0.00	No	1.97	5.66	No
Quarterly	-3.74	-3.60	0.04	No	16.13	5.72	Yes
<i>"GDP"</i>							
Weekly	-6.95	-3.42	0.00	No	1.30	5.62	No
Monthly	-6.29	-3.46	0.00	No	1.58	5.66	No
Quarterly	-2.10	-3.60	0.52	Yes	7.31	5.72	Yes
<i>"economic growth"</i>							
Weekly	-7.54	-3.42	0.00	No	0.91	5.62	No
Monthly	-5.63	-3.47	0.00	No	25.80	5.66	Yes
Quarterly	-3.08	-3.61	0.13	Yes	0.08	5.72	No
<i>"gold price"</i>							
Weekly	-5.06	-3.42	0.00	No	2.18	5.62	No
Monthly	-3.92	-3.46	0.02	No	9.24	5.66	Yes
Quarterly	-2.74	-3.57	0.23	Yes	9.92	5.72	Yes

Table 8: Regressand-First Difference of log of Y_all Visits-Comparing Estimated Coefficients using CACVB Data

Regressor-Log Variable	Daily							Sum	Weekly
	b _{D1}	b _{D2}	b _{D3}	b _{D4}	b _{D5}	b _{D6}	b _{D7}		
"charleston sc" (all) (1st Diff)	0.53	-0.33	-0.36	-0.30	-0.29	-0.34	0.33	-0.76	0.73
"charleston sc" (all) (Level)	0.41	-0.91	0.00	0.07	-0.03	-0.02	0.51	-1.66	0.38
"charleston hotels" (all) (1st Diff)	0.28	-0.02	-0.22	-0.27	-0.25	-0.26	-0.07	-0.80	0.24
"charleston restaurants" (all) (Level)	-0.14	-0.04	0.16	0.07	0.03	-0.02	-0.06	-0.01	0.23
"charleston travel" (all) (1st Diff)	0.02	0.18	0.18	0.05	-0.03	-0.03	-0.06	0.30	0.22
"charleston travel" (all) (Level)	0.03	0.17	0.01	-0.13	-0.08	0.02	0.00	0.02	0.08
"charleston sc" (travel) (1st Diff)	0.25	-0.15	-0.34	-0.32	-0.35	-0.30	0.01	-1.19	0.55
"charleston hotels" (travel) (1st Diff)	0.15	-0.12	-0.23	-0.21	-0.24	-0.24	-0.05	-0.94	0.31
"charleston hotels" (travel) (Level)	0.16	-0.27	-0.11	0.02	-0.03	-0.01	0.22	-0.02	0.09

Table 9: Comparing RSS and R-Squared Terms using CACVB Data

Regressor-Log Variable	RSS		R-squared	
	Daily	Weekly	Daily	Weekly
"charleston sc" (all) (1st Diff)	6.02	0.23	0.51	0.40
"charleston sc" (all) (Level)	6.42	0.32	0.48	0.16
"charleston hotels" (all) (1st Diff)	9.16	0.31	0.25	0.16
"charleston restaurants" (all) (Level)	11.21	0.32	0.09	0.16
"charleston travel" (all) (1st Diff)	10.13	0.32	0.09	0.15
"charleston travel" (all) (Level)	10.23	0.36	0.08	0.04
"charleston sc" (travel) (1st Diff)	9.28	0.18	0.24	0.53
"charleston hotels" (travel) (1st Diff)	9.71	0.27	0.21	0.28
"charleston hotels" (travel) (Level)	9.75	0.35	0.21	0.08

Table 10: Comparing Weekly v. Monthly Economic Data Using AR Models

Log Variable	Weekly					Monthly	RSS		R-Squared	
	b_{w1}	b_{w2}	b_{w3}	b_{w4}	Sum	b_M	Weekly	Monthly	Weekly	Monthly
<i>UNEMP</i> (1st diff)	-0.31	-0.13	-0.13	0.09	-0.47	-0.01	2.51	0.99	0.12	0.00
<i>INFL</i> (1st diff)	-0.11	-0.16	-0.14	-0.04	-0.45	0.03	4.68	1.49	0.04	0.00
<i>INFL</i> (level)	0.83	-0.06	0.00	0.07	0.84	0.00	4.44	1.26	0.67	0.45
<i>GDP</i> (1st diff)	0.10	-0.05	-0.13	-0.09	-0.18	-0.01	10.06	4.80	0.04	0.00
<i>GDP</i> (level)	1.00	-0.15	-0.09	0.03	0.80	0.53	9.21	3.71	0.72	0.28
<i>ECONGRO</i> (1st diff)	-0.04	-0.11	-0.19	-0.09	-0.42	0.07	13.55	3.72	0.05	0.01
<i>ECONGRO</i> (level)	0.91	-0.09	-0.09	0.11	0.84	0.72	12.82	3.30	0.70	0.51
<i>GOLDP</i> (1st diff)	-0.12	-0.13	-0.08	-0.04	-0.37	-0.11	9.91	4.06	0.03	0.01
<i>GOLDP</i> (level)	0.88	-0.04	0.03	0.07	0.93	0.82	9.92	4.16	0.84	0.69

Table 11: Comparing Monthly v. Weekly Economic Data-Using AR Models

Log Variable	Monthly				Quarterly	RSS		R-Squared	
	b_{M1}	b_{M2}	b_{M3}	Sum	b_Q	Monthly	Quarterly	Monthly	Quarterly
<i>UNEMP</i> (1st diff)	-0.01	-0.17	0.12	-0.06	0.37	0.92	0.37	0.05	0.14
<i>INFL</i> (1st diff)	-0.02	-0.22	-0.30	-0.54	-0.35	1.27	0.52	0.13	0.12
<i>INFL</i> (level)	0.83	-0.25	0.02	0.60	0.41	1.18	0.41	0.47	0.17
<i>GDP</i> (1st diff)	-0.07	-0.23	-0.32	-0.62	-0.19	4.03	0.96	0.15	0.04
<i>GDP</i> (level)	0.64	-0.21	-0.14	0.30	0.27	3.25	0.63	0.35	0.08
<i>ECONGRO</i> (1st diff)	0.02	-0.14	-0.41	-0.53	-0.34	3.02	0.92	0.19	0.11
<i>ECONGRO</i> (level)	0.86	-0.22	-0.04	0.60	0.54	2.92	0.76	0.52	0.35
<i>GOLDP</i> (1st diff)	-0.16	-0.09	-0.21	-0.46	-0.03	3.80	2.09	0.07	0.00
<i>GOLDP</i> (level)	0.78	0.06	0.01	0.85	0.73	3.74	1.91	0.71	0.52