Macroeconomic Implications of Modeling the Internal Revenue Code in a Heterogeneous-Agent Framework

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Macroeconomic Implications of Modeling the Internal Revenue Code In a Heterogeneous-Agent Framework∗†

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Abstract

Fiscal policy analysis in heterogeneous-agent models typically involves the use of smooth tax functions to approximate present tax law and proposed reforms. We argue that the tax detail omitted under this conventional approach has macroeconomic implications relevant for policy analysis. In this paper, we develop an alternative approach by embedding an internal tax calculator into a large-scale overlapping generations model that explicitly models key provisions in the Internal Revenue Code applied to labor income. While both approaches generate similar policy-induced patterns of economic activity, we find that the similarities mask differences in key economic aggregates and welfare due to variation in the underlying distribution of household labor supply responses. Absent sufficient tax detail, analysis of specific policy changes — particularly those involving large, discrete effects on a relatively small group of households — using heterogeneous-agent models can be unreliable.

JEL Codes: C63, E62, H30
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1 Introduction

Fiscal policy analysis in macroeconomic models requires the incorporation of a tax system that can approximate both present law and proposed deviations. One challenge is that policy changes affect each taxpayer differently. Early heterogeneous-agent models often approximate the tax system using a single parameterized tax function that smoothly maps household income into tax liabilities or effective tax rates, such as those developed in Easterly and Rebelo (1993), Gouveia and Strauss (1994), Bénabou (2002), and Li and Sarte (2004). While the recent work of DeBacker et al. (2017) builds upon this literature by using a large number of tax functions, shortcomings remain: Functional form assumptions for effective tax rates and the imposition of smoothness on the tax system are questionable approximations of the actual tax system that risk introducing counterfactual tax changes and behavioral responses into the analysis. This conventional approach omits tax detail which has macroeconomic implications relevant for policy analysis.

In this paper, we develop an alternative approach that incorporates the tax detail typically absent: We embed a tax calculator in a large-scale overlapping generations (OLG) model that explicitly models tax provisions in the Internal Revenue Code (IRC) applied to labor income. We model the present law statutory rate schedule, the standard deduction, earned income credit, the child tax credit, the home mortgage interest deduction, state and local income, sales and property tax deductions, the charitable giving deduction, the net investment income and Medicare surtaxes, and the dependent care credit. Unlike the conventional approach, we do not impose functional form assumptions on the effective tax rate schedules. Instead, endogenous household behavior generates deviations from the statutory tax rate schedule either by employment choices, which could affect tax credits, or consumption choices, which could affect deductions. This is important because policy proposals may include many measures with potentially offsetting effects on incentives which vary across households (Gravelle and Marples, 2015). Our approach ensures that tax policy changes involving large, discrete effects on a relatively small group of households are not washed out as a smaller change for the wider population.

To demonstrate the importance of tax detail we simulate specific tax policy changes with the internal tax calculator and alternatively with the commonly-used Bénabou (2002) tax function. First, the tax calculator can target specific households affected by a policy change. Homeownership is a choice in the model, so if the home mortgage interest deduction were repealed, for example, only househoks claiming that deduction would experience an increase in their tax liability. Alternatively, the tax function would shift for every household, indiscriminately. The second advantage of the tax calculator is that households have the opportunity to react optimally to the policy change. If the deduction is repealed, renters who would purchase a house in the near future under present law may continue to rent, or decide to purchase a smaller property. Under the tax function, the extent to which households are affected by the repeal is implicitly assumed.

We simulate two policy changes: (i) a ten percent reduction in statutory rates on ordinary income; and (ii) an expansion of the earned income tax credit for childless adults.

\footnote{Non-smooth tax functions have been used in Ventura (1999) and Altig and Carlstrom (1999).}
\footnote{Counterfactual tax changes may arise from specification error, for example. Akhand (1996) provides evidence of misspecification for the Gouveia and Strauss (1994) tax function.}
\footnote{Our reference to present law includes those changes to the IRC from passage of PL 115-97, which is colloquially known as the `Tax Cuts and Jobs Act of 2017'.}
\footnote{For an early discussion on the use appropriate use of statutory and effective marginal tax rates, see Barro and Salasakul (1983) and Easterly and Rebelo (1993).}
We find that both tax systems replicate the aggregate average and effective marginal tax rate changes that summarize the aggregate behavioral incentives associated with each specific policy change, and that both generate similar policy-induced patterns of short- and long-run economic activity. Despite qualitative similarities, we find quantitative differences in aggregates and welfare, driven by changes in the distribution of household labor hours across tax systems. The labor response from some household demographics deviates from that predicted by theory when using the tax function, because the function can fail to correctly model incentives for all households. The tax calculator avoids this problem. An implication of this finding is that while smooth tax functions may be appropriate for general analysis of tax progressivity, such as in Heathcote et al. (2017) and Holter et al. (2017), they are less suitable for analysis of specific policy changes. As a result, quantitative fiscal policy analyses omitting sufficient tax detail may therefore fall short of capturing within economic aggregates the idiosyncratic behavioral responses of heterogeneous households, and therefore be unreliable.

2 Model

In this section, we specify a large-scale OLG model —where market interactions take place between households, firms, a financial intermediary, and government —in which we embed a tax calculator to explicitly model IRC provisions that determine the tax treatment of labor income: Households make consumption, saving, labor supply, and residential choices. Firms hire labor and rent capital to produce a composite output good that can be transformed into either a consumption or residential good, or a financial asset. The financial intermediary takes in deposits of financial assets from households and allocates the funds to consumer and mortgage loans, federal government bonds, rental housing capital, and productive private business capital, remitting the return on this portfolio back to deposit-holding households. Federal, state and local governments collect tax liabilities owed by households and firms, and make consumption expenditures, public capital expenditures and facilitate transfer payments. While all agents have perfect foresight regarding the path economic aggregates, prices, and fiscal variables associated with a given policy, households face mortality risk.

The household sector is developed to exhibit heterogeneity along specific dimensions so that the tax calculator can explicitly model the desired IRC provisions applied to labor income. We include ex ante heterogeneity in age, labor productivity, family composition, and wealth endowments which imply ex post heterogeneity in residential choice and tenure, as well as the path of lifetime financial wealth. For the specification of several parameters and targets relevant for these dimensions, as well as for the internal tax calculator, calibration of the model relies heavily on the Joint Committee on Taxation’s Individual Tax Model (ITM), which makes use of data from individual tax returns filed with the Internal Revenue Service (IRS) and compiled by the IRS Statistics of Income Division.\(^5\) The calibration methodology is described in Section 3.

Exogenous population growth and technical progress are both present in the model. The framework is therefore structured to be consistent with the existence of a Balanced Growth Path (BGP), allowing for the application of stationary solution methods to compute equilibrium. The trend-stationary form of the model consistent with a BGP is specified as a dynamic program in Appendix B. Furthermore, since households face a set

\(^5\)For a description of the JCT’s Individual Tax Model, see JCT (2015).
of decision-making frictions that generate decision rules that will be non-differentiable over some subsets of the state space, we rely on a discrete state-space solution method. The value function iteration - direct solution hybrid algorithm used to solve the model is described in Appendix C.

2.1 Demographics

The economy is populated by \( J = |J| \) overlapping generations of finitely-lived households where \( J \) is the set of all possible discrete household ages with a maximum age of \( J \). In each time period, a new generational cohort of households enters the economy while the oldest generation leaves. For working ages \( j = \{1, \ldots, R\} \in J \), individuals in households decide how much to work, save, and consume on housing and non-housing goods and services. All individuals must retire by the end of household age \( R \) and continue to make saving, housing and non-housing consumption choices for ages \( j = \{R + 1, \ldots, J\} \in J \). Households are assumed to survive all possible working ages with a probability \( \pi_j = 1 \), and begin to face mortality risk upon reaching the maximum retirement age with the associated conditional probability of surviving from age \( j \) to \( j + 1 \) of \( 1 > \pi_j > 0 \) until the maximum age of \( J \) where \( \pi_J = 0 \) such that the household dies with certainty.

Following Fullerton and Rogers (1993), each generational cohort of age \( j \) consists of discrete household groups, indexed by \( z \in \{1, \ldots, nz\} \equiv Z \), who differ in terms of age-varying labor productivity profiles \( z^j \) which are strictly increasing in \( j \). In addition, we allow households within each cohort of age \( j \) and productivity \( z \) to exogenously differ in family composition, indexed by \( f \), which takes one of two discrete values, \( f = s \) for a single individual and \( f = m \) for a married couple. In each period, \( J \times nz \times 2 \) structurally distinct households are making economic decisions.

The initial population is normalized to unity: \( P_0 = 1 \). The population grows exogenously at rate \( \nu_p \). Letting \( \Upsilon_p = (1 + \nu_p) \), the measure of total population at any time \( t \) is then:

\[
P_t = \Upsilon_p P_{t-1} = \Upsilon_p^t \tag{2.1}
\]

Let \( \Omega_{t,j}^{z,f} \) be the measure of household family composition \( f \), age \( j \) and labor productivity type \( z \) so that at any time \( t \), the population may be broken down by the measure of singles and married couples by age and productivity:

\[
P_t = \int_Z \int_J \left( \Omega_{t,j}^{z,s} + \Omega_{t,j}^{z,m} \right) \ dj \ dz \tag{2.2}
\]

While the age-productivity-family demographic distribution of households remains constant over time, the measure of each combination of attributes grows deterministically at the gross rate \( \Upsilon_p \). Formally, the total measure of productivity type \( z \), family composition \( f \), and age \( j \) of households at time \( t \), relative to their measure at time \( t - 1 \) is expressed as:

\[
\Omega_{t,j}^{z,f} = \Upsilon_p \Omega_{t-1,j}^{z,f} \tag{2.3}
\]

Note that integrating both sides of the above equation over age and productivity, while summing over family composition yields equation (2.1).
2.2 Households

Households have the objective to make consumption, saving, labor supply, and residential decisions that maximize the present discounted value of their lifetime utility, where utility is derived from consuming non-housing and housing goods and services, and disutility encountered from market work. The optimization problem is formulated to permit a single individual state variable for each household of permanent productivity type \( z \) and family composition \( f \), which allows for only a single intertemporal problem to be solved at each age \( j \). We specify functional forms that allow optimal quantities of choice variables to be directly expressed in terms of the state variable. Combined with restrictions on choice sets, these specifications mitigate curse-of-dimensionality problems that may arise with the level of heterogeneity incorporated for purposes of the internal tax calculator.

Let \( V_{t,j}^{z,f}(y_j) \) denote the value function representing the maximum attainable expected present discounted value of utility for the remaining life for a household of age \( j \), with labor productivity type \( z \), and family composition \( f \) at time \( t \). The value function explicitly depends on a single individual state variable, current net worth \( y_j \), which is defined as the sum of the beginning-of-period (net) stock of financial assets \( a_j \) and the owner-occupied housing stock \( h_o^s \). Given their current level of net worth, households optimally choose their future level of net worth \( y_{j+1} \) and current market labor supply \( n_j \) as those levels associated with the choices of ordinary consumption \( c^s_j \), charitable giving \( c^g_j \), financial asset holdings \( a_j \), rental housing \( h^r_j \), and owner-occupied housing which maximize their instantaneous utility function \( U_{t,j}^{z,f} \). Utility is derived from rental housing and owner-occupied housing in terms of a housing service consumption composite good \( h_s \), and derived from ordinary consumption and charitable giving in terms of a non-housing consumption composite good \( c_j \). These composite goods nest each single good — and are themselves nested into a third composite good \( x_j \) — all in a CES fashion. Ordinary consumption can be obtained from consumption of market-produced goods \( c^M_j \) or home production \( c^h_j \). Leisure \( l_j \) is obtained from the portion of unitary time endowments not spent on market labor or non-market labor \( n^h_j \). Upon reaching retirement, individuals no longer supply market labor and begin to receive social security payments \( s^s_{j,t} \).

We follow Gervais (2002) and Cho and Francis (2011) in our specification of the housing choice problem, and assume that the two residential options are perfect substitutes so that a household will either rent or own, but never both. As in the former work, we interpret housing services as the household’s stock of durable goods plus the stock of residential capital to allow for households taking out relatively larger mortgages in order to finance the purchase of durables. As in the latter work, households face a transaction cost \( \xi_j^H \) associated with changing residential status from a renter to a home-owner or vice versa to limit the frequency of status changes.

So that households have an incentive to make charitable gifts, we assume a ‘warm-glow’ motive (Andreoni, 1989). Charitable gifts are made in terms of final goods, and are assumed to be received by agents outside of the model.\(^6\)

Market labor supply operates along both an extensive and intensive margin so that changes to aggregate employment can be broken down into movement of workers into or out of the labor force as well as changes in hours per worker. The former component is important because it has been determined as the primary driver of aggregate employment

\(^6\)Alternatively, it may be assumed that charitable gifts are made in terms financial assets which are then spent on final goods by the recipients. This would be equivalent to our specification if it is assumed that the recipients are non-taxable and operate costlessly subject to an intra-period balanced budget.
fluctuations (Kydland, 1995; Fiorito and Zanella, 2012). We follow Chang et al. (2011) and specify indivisible market labor supply \( n_j \in \mathbb{N} \equiv \{0, n^{PT}, n^{FT}\} \) such that individuals may choose between no work, part-time work, or full-time work. While somewhat restrictive, this specification allows us to capture the observation that working hours tend to bunch around part-time and full-time levels (Keane and Wasi, 2016).

Drawing from the observation that employed individuals spend less time on housework than the unemployed (Krueger and Mueller, 2012), we assume that the time each individual spends on home production exogenously varies inversely with their chosen quantity of market labor, so that the amount of home work is determined by the amount of market work through the function \( n_j^h(n_j) \). Since housework can largely be outsourced, we further assume that all households derive the same value of home-produced consumption from each non-market labor hour through the function \( c_j^h(n_j^h) \). Despite this simple structure of home production, its incorporation helps to sustain heterogeneity in market labor hours as observed by Kuhn and Lozano (2008): First, higher earning individuals in the model tend to supply relatively more hours in the market than lower earning individuals. Second, as households age and become more productive on the market, variance of the net return to labor increases and drives greater variation in market hours at older ages.

Total costs to market work include a utility cost, a monetary cost, and a consumption cost. Following Holter et al. (2017), single households face a fixed utility loss of \( F^s \) if the individual enters the labor force, while married households face a fixed utility loss of \( F^m \) if the secondary earner works. The monetary cost \( \kappa^{z,f}_j \) captures child-care costs (Guner et al., 2011), and is a function the number of qualifying dependents within that household, \( \nu^{z,f}_j \), and the market work hours of the single or secondary worker. This cost allows for the model to capture variation in lifecycle market labor and foregone earnings due to child-rearing (Adla et al., 2017). Finally, defining ordinary consumption as the sum of market and home-produced consumption goods, our specification of time use for home production implies that households face a loss in ordinary consumption which varies positively with market labor hours. Rogerson and Wallenius (2013) show that such a consumption cost helps to replicate the mostly abrupt nature of retirement observed empirically. The presence of this cost in our model can induce individuals of different demographics to choose full retirement at different ages prior to the required retirement age. Further, these features help generate the empirically observed extent and intensity of labor force participation across different demographic groups, without imposing exogenous lifecycle variation in labor disutility, see (Cogan, 1981).

Consider a single individual. The objective of this household’s optimization problem for a known policy regime is:\footnote{While prices, taxes and utility are time dependent, the household keeps track of choice variables over time using age. To reduce notational clutter, we omit the time subscript where able until aggregation.}

\[
V_{t,j}^{z,s}(y_j) = \max_{y_{j+1}; n_j \in \mathbb{N}} U_{t,j}^{z,s}(x_j, n_j) + \beta \pi_j V_{t+1,j+1}^{z,s}(y_{j+1}) \tag{2.4}
\]

\[
U_{t,j}^{z,s}(x_j, n_j) \equiv \max_{a_j, h_j^o, h_j^p} \log(x_j) - \psi^s \frac{n_j^{1+\zeta^s}}{1+\zeta^s} - F^s \tag{2.5}
\]

where:

\[
y_j \equiv h_j^o + a_j \tag{2.6}
\]
\[
x_j \equiv (\sigma c^\eta_j + (1 - \sigma)h s^\eta_j)^{1/\eta} \\
c_j \equiv (c^i_j)^{\theta_s} (c^g_j)^{1 - \theta_s} \\
h s_j \equiv \max \{h^o_j, h^r_j\} \\
n_j = \begin{cases} 
1 - l_j - n^h_j(n_j) & \forall j \leq R \\
0 & \forall j > R 
\end{cases} \\
F^s = \begin{cases} 
\phi^s & \text{if } n_j > 0 \\
0 & \text{if } n_j = 0 
\end{cases} \\
c^i_j \equiv c^M_j + c^h_j(n^h_j) 
\]

The functional form for instantaneous utility in equation (2.5) is chosen because it is consistent with a BGP in the presence of fixed utility costs from working.\(^8\)

All households have their feasible choice set restricted by a budget constraint: The sum of expenditures on market consumption \(c^M_j\), charitable giving \(c^g_j\), and rental housing \(p_i^r h^r_j\), as well as the choice of the next-period stock of financial assets \(a_{j+1}\) and owner-occupied housing \(h^o_{j+1}\), can be no larger to the resources currently available to the household. Available resources consist of the gross return on beginning-of-period financial assets \((1 + r^p_i) a_j\) held by a financial intermediary, the after-tax bequests received from those who died at the end of the previous period \(b eq_t\), the stock of beginning-of-period owner-occupied housing less maintenance costs and economic depreciation \((1 - \delta^o) h^o_j\), the flow of income \(i^z_{t,j}\) which is equal to labor income \(n_j w \sigma_j^z\) during working years and equal to social security payments \(ss^z_{z,s} j\) during retirement. These resources may be reduced by net tax liabilities \(T^z_{t,j}\), child-care costs \(\kappa^z_{j} s\), and housing transaction costs \(\xi^H_j\). Formally the budget constraint takes the form:

\[
c^M_j + c^g_j + p_i^r h^r_j + a_{j+1} + h^o_{j+1} \leq (1 + r^p_i) a_j + beq_t + (1 - \delta^o) h^o_j + i^z_{t,j} - T^z_{t,j} - \kappa^z_{j} s - \xi^H_j 
\]

where:

\[
i^z_{t,j} \equiv n_j w \sigma_j^z + ss^z_{z,s} 
\]

\[
\kappa^z_{j} s = cc^z_{z,s} \nu^z_{j} s n_j 
\]

\[
\xi^H_j = \begin{cases} 
\phi^o h^o_{j+1} & \text{if } h^o_j = 0 \\
\phi^r h^r_{j+1} & \text{if } h^o_j > 0 
\end{cases} 
\]

and \(cc^z_{z,s}\) is an exogenous scale parameter for cost per child. The determination of net tax liabilities \(T^z_{t,j}\) are detailed in Section 2.5.

Households are permitted to borrow and accumulate debt in excess of savings subject to the following restrictions:

\(^8\)See Holter, Krueger, and Stepanchuk (2017) for the proof of balanced growth path consistency.
\[ y_j \geq \begin{cases} \sum \tau^{z,s} & \text{if } h^o_j = 0 \\ \gamma h^o_j & \text{if } h^o_j > 0 \end{cases} \] (2.17)

where \( \tau^{z,s} < 0 \) is the lower-bound of the net worth support and the parameter \( 0 \leq \gamma \leq 1 \) can be interpreted as the down-payment ratio, or the minimum equity which a homeowner may hold in their home. This condition implies that while renters are able to accumulate unsecured debt up to the amount of \( \tau^{z,s} \), homeowners must maintain a minimum equity balance of \( \gamma h^o_j \). Homeowners have access to larger loans, using their home as collateral for borrowing up to \( (1 - \gamma)h^o_j \).

Both rental housing and owner-occupied housing are subject to minimum sizes, where \( h^r < h^o \) making rentals relatively more affordable. Similarly, ordinary consumption must be at least as large as a subsistence level \( c^i \). We further assume that households do not make charitable gifts if ordinary consumption is at this subsistence level:

\[ hs_j \geq h^r, \quad c^i_j \geq c^i \] (2.18)
\[ h^o_j \geq h^o \quad \text{if } h^o_j > 0 \] (2.19)
\[ c^j = c^i_j \quad \text{if } c^i_j = c^i \] (2.20)

As discussed in Section 2.5.2, the federal government will provide a conditional welfare transfer to any household that cannot afford both \( c^i \) and \( h^r \).

It is assumed that households enter the economy with initial financial assets of \( a_1 \) and zero owner-occupied housing. Should a household live to the maximum age \( J \), they are assumed to die with zero net-worth. This is not to say that savings, \( a_{J+1} \), equal zero at the end of life, as owner-occupied housing capital could be positive, allowing agents to die with mortgage debt. In this way, the model allows for reverse mortgages. Formally, we impose the initial and terminal conditions:

\[ y_1 = a_1 \] (2.21)
\[ h^o_1 = y_{J+1} = 0 \] (2.22)
\[ V^{z,s}_{t,J+1} = 0 \] (2.23)

Married households face a similar constrained optimization problem to that of single households. They make choices along the same margins to maximize the present discounted value of lifetime utility with the following objective function:

\[ V^{z,m}_{t,j}(y_j) = \max_{y_{j+1},x^1_j} \max_{n^1_j,n^2_j \in \mathbb{N}} U^{z,m}_{t,j}(x^1_j, n^1_j, n^2_j) + \beta \pi_j V^{z,m}_{t+1,j+1}(y_{j+1}) \]

with the associated instantaneous utility function allowing for two potential earners:

\[ U^{z,m}_{t,j}(x^1_j, n^1_j, n^2_j) \equiv \max_{a_j, h^r_j, h^o_j} \log(x^1_j) - \psi^{m,1}(n^1_j)^{1+\zeta^{m,1}} - \psi^{m,2}(n^2_j)^{1+\zeta^{m,2}} - F^m \]
Married households similarly face equations (2.6) through (2.23), indexed \( f = m \) instead of \( f = s \), with the exception of equations (2.10)-(2.12) and (2.14)-(2.15). First, equation (2.10) applies to labor supply for each of the married household’s potential earners individually, so that \( n^1_j \) and \( n^2_j \) denote the primary and secondary labor supply. Each worker gives up the same quantity of home production hours to work in the market. Second, since it is assumed that the costs associated with working apply only to the secondary earner, we have:

\[
n^\epsilon_j = \begin{cases} 
1 - l^\epsilon_j - n^h_j(n^\epsilon_j) & \forall j \leq R, \quad \epsilon = 1, 2 \\
0 & \forall j > R
\end{cases}
\]

\[
F^m = \begin{cases} 
\phi^m & \text{if } n^2_j > 0 \\
0 & \text{if } n^2_j = 0
\end{cases}
\]

\[
\kappa^z,m_j = cc^z,m n^z,m_j n^2_j
\]

Home production and income depend on the labor of both individuals in a household:

\[
c^i_j = c^M_j + c^h,2_j(n^h,1_j) + c^h,1_j(n^h,2_j)
\]

\[
\hat{t}^z,m_{i,j} = (n^1_j + \mu^z n^2_j)w_t z^m_i + ss^z,m
\]

where \( 0 < \mu^z \leq 1 \) is an exogenous productivity wedge between the primary and secondary workers. Note that the secondary earner’s effective wage rate depends on the productivity-type specific term \( z^z,m_j \), which also determines the primary worker’s effective wage rate given the prevailing market real wage rate \( w_t \). This specification is intended to capture both the observed earnings differential of workers within a married household and positive assortative mating (Greenwood et al., 2016, 2014; Eika et al., 2014).

Finally, since households can unexpectedly die when aged \( R < j < J \), they may leave behind wealth that they have accumulated over their lifetime. Should a household die before reaching the maximum age \( J \), a proportion \( \Lambda \) of their net worth is allocated to end-of-life consumption expenditures and the remaining \( (1 - \Lambda) \) proportion is costlessly liquidated and collected by the government, taxed, and redistributed in a lump-sum fashion among the living. While this specification is chosen primarily so that the observed level of aggregate bequests can be targeted through the value of \( \Lambda \), it also captures the observed increase in medical expenditures at the end of life (French et al., 2006). Furthermore, our perfect-foresight assumption implies that all agents can predict the quantity of wealth left behind by the dead, allowing for us to specify contemporaneous redistribution in the following manner:

\[
beq_t = (1 - \Lambda) \int_Z \int_J (1 - \pi_j) \sum_{f=s,m} y_{t+1,j+1} \Omega_{z,f}^t dj dz - T^beq_t
\]

where \( T^beq_t \) is the aggregate amount of taxes collected by the government on accidental bequests left at the end of period \( t \).
2.3 Firms

Identical firms hire labor directly from households in a perfectly competitive labor market and rent capital from a financial intermediary to produce and sell output in a competitive goods market at profit maximizing levels. Production technology is assumed to be of the Cobb-Douglas form:

\[ Y_t = G_t^g K_t^\alpha (A_t N_t)^{1-\alpha-g} \] (2.25)

where \( G_t = G_t^{fed} + G_t^p \) the sum of beginning-of-period public capital from owned by the federal government as well as the state and local governments, \( K_t \) and \( N_t \) are beginning-of-period productive private capital and effective labor units used in production, and \( A_t \) is the level of labor-augmenting technological progress which evolves as \( A_{t+1} = \Upsilon A_t \), where \( \Upsilon_A = (1 + \nu_A) \) is the exogenous annual gross rate of technological growth. The final output good \( Y_t \) is the numéraire and can costlessly be transformed by households into a consumption good, owner-occupied housing services, or a financial asset as in Gervais (2002), Fernández-Villaverde and Krueger (2010), and Cho and Francis (2011), or into a charitable gift.

Aggregate effective labor \( N_t \) is the sum of efficiency-weighted labor hours:

\[ N_t = \int_z \int_j z^s n_{z,j} \Omega_{z,j}^s + z^m (n_{z,j}^{1} + \mu z^{2} n_{z,j}^{2}) \Omega_{z,j}^m \, dj \, dz \] (2.26)

where \( \Omega_{z,j}^s \) is the measure of each productivity and age group for singles at time \( t \), \( \Omega_{z,j}^m \) is the corresponding measure for married households, and labor hours for singles, married primary and married secondary earners are \( n_{z,j}^s \), \( n_{z,j}^{1} \) and \( n_{z,j}^{2} \) respectively.

Under this environment, the production sector can be modeled from the perspective of a representative firm which has the objective to choose the quantity of inputs \( K_t \) and \( N_t \) at factor prices \( r_t \) and \( w_t \) to produce output \( Y_t \) at a level that maximizes after-tax profits each period, taking the stock of public capital \( G_t \) as given. Assuming that wage expenses are fully deductible from all business-level taxes, profits \( \Pi_t \) for the representative firm are given by:

\[ \Pi_t = \max_{K_t, N_t} \left\{ (1 - \tau^\text{bus}_t)(1 - \tau^\text{slb}_t) \left( G_t^g K_t^\alpha (A_t N_t)^{1-\alpha-g} - w_t N_t \right) + \tau^\text{bus}_t lsd^\text{bus}_t - r_t K_t \right\} \] (2.27)

where \( \tau^\text{bus}_t \) and \( \tau^\text{slb}_t \) are linear business-level tax rates applied to taxable profits at the federal level and the combined state-local level respectively, and \( lsd^\text{bus}_t \) is a lump-sum deduction against the federal tax liabilities. State and local business-level taxes are assumed to be fully deductible from federal business-level tax liabilities.

While the presence of public capital gives rise to economic rents, perfect competition in the goods market implies that firms will earn zero economic profits in equilibrium. To account for this we assume that the financial intermediary has sufficient market power over the firm to extract this rent, which accrues to the owners of capital. Firms then hire private factors at the given prices such that:

\[ w_t = (1 - \alpha - g)G_t^g K_t^\alpha (A_t N_t)^{-\alpha-g} \] (2.28)

\[ r_t = \frac{1}{K_t} \left( (1 - \tau^\text{bus}_t)(1 - \tau^\text{slb}_t)(\alpha + g)(G_t^g K_t^\alpha (A_t N_t)^{1-\alpha-g}) + \tau^\text{bus}_t lsd^\text{bus}_t \right) \] (2.29)
2.4 Financial Intermediary

A representative financial intermediary pools the net stock of savings chosen by households into deposits to be invested in capital markets. Beginning-of-period aggregate deposits are expressed as:

\[ D_t = \int_2 \int_1 \sum_{f,s,m} \Omega_{i,j}^{z,f} \int_2 \sum_{f,s,m} a_{i,j}^{z,f} d\Omega_{i,j}^{z,f} d\Omega_{i,j}^{z,f} dz \] (2.30)

Each period the intermediary pays households the principle plus a portfolio return on their savings chosen in the previous period, \((1 + r_{t+1}^p)D_t\), and takes in new deposits \(D_{t+1}\), for which it decides an investment allocation. The financial intermediary can invest in productive private business capital, \(K_{t+1}\), rental housing \(H_{t}^r\), and government bonds \(B_{t+1}\). The equations of motion for these stocks are as follows:

\[ K_{t+1} = (1 - \delta^K)K_t + I^K_t - \Xi_t \] (2.31)
\[ H_{t}^r = (1 - \delta^r)H_{t-1}^r + I^r_t \] (2.32)
\[ B_{t+1} = B_t + NB_t \] (2.33)

There is a convex adjustment cost \(\Xi_t\) for deviating from the ‘break-even’ level of investment that would keep growth-adjusted private capital per capita constant:

\[ \Xi_t = \frac{\xi_K}{2} (\frac{K_{t+1} - \Upsilon_p \Upsilon_A}{K_t})^2 K_t \] (2.34)

Net investment in business capital and rental housing chosen by the financial intermediary are \(I^K_t\) and \(I^r_t\), while new bond issues by the government and purchased by the intermediary are denoted \(NB_t\). While investment in business capital and government bonds at time \(t\) yields returns \((r_{t+1} + \delta^K)\) and \(\rho_{t+1}\) at time \(t+1\), investment in rental housing is assumed to be immediately available to households and thus yields contemporaneous return \(p^r_t\). The intermediary incurs expenses from the economic depreciation of their stocks of business capital and rental housing capital, as well as potential business capital adjustment cost expenses. Table 1 summarizes the assets and liabilities held by the intermediary at the end of period \(t\), as well as their contemporaneous income and expense flows over the period.

The objective of the financial intermediary is to choose the sequence of business capital and rental housing which maximize their net cash flow:

\[ \mathcal{I}_t = \max_{K_{s+1},H_{s+1}^r} \sum_{s=t}^{\infty} \left( (1 + r_s - \delta^K)K_s + (1 - \delta^r)H_{s-1}^r + p^r_s H_{s-1}^r + (1 + \rho_s)B_s + D_{s+1} \right. \]
\[ \left. - (1 + r^p_s)D_s - K_{s+1} - \Xi_s - H_{s+1}^r - B_{s+1} \right) \] (2.35)

subject to the resource constraint:

\[ D_{s+1} \geq K_{s+1} + H_{s+1}^r + B_{s+1} \quad \forall s \] (2.36)

and the equations of motion for capital stocks, equations (2.31) through (2.33), with \(K_s\), \(B_s\), and \(H_{s-1}^r\) given.
The resource constraint (2.36) states that business capital and government bonds at the end of any given period plus current rental housing stock held by the intermediary must be less than or equal to the end-of-period stock of savings deposited by households. Given the objective of the financial intermediary, the price of rental housing is set so that the intermediary is indifferent between investing in rental housing or business capital, which yields the no-arbitrage condition:

\[ p_t^r = r_{t+1} - \delta K + \delta r - \left( \frac{\partial \Xi_t}{\partial K_t} + \frac{\partial \Xi_{t+1}}{\partial K_{t+1}} \right) \]  

(2.37)

We assume that government bonds, which are all held directly by the intermediary, enjoy a low “safe” interest rate \( \rho_t \) relative to the return on productive capital. Since there is no uncertainty in this model, we accomplish this by introducing an exogenous, time-invariant wedge \( \varpi \) between \( \rho_t \) and \( r_t \).

\[ \rho_t = r_t - \varpi \]  

(2.38)

Finally, noting the contemporaneous income and expenses at time \( t \) from the income statement of the representative financial intermediary above, the imposition of a zero-profit condition on the financial intermediary implies that households receive a return on their deposits equal to:

\[ r_p^t = \frac{(r_t - \delta K) K_t - \Xi_t + p^r H_t^r - \delta^r H_{t-1}^r + \rho_t B_t}{D_t} \]  

(2.39)

### 2.5 Government

#### 2.5.1 Household Income Taxation

In this section we detail the tax treatment of household income, which involves the specification of a federal labor income tax, capital income tax, payroll tax, the special tax treatment of social security benefits as well as state and local taxes. We specify the general framework of labor income taxation under the internal tax calculator (ITC) developed in this paper and, for purposes of comparison, under the Bénabou Tax Function (BTF) (Bénabou, 2002). Since the goal of this paper to demonstrate the importance of the labor income tax detail contained in the ITC relative to a conventional tax function such as the BTF, we use the same framework for modeling all other taxes regardless of whether the ITC or the BTF is used in simulation.

To convert the household’s economic income into a corresponding taxable income concept, a ‘calibration ratio’ is introduced to reflect the portion of a particular flow of economic income which may be subject to taxation. The productivity type - family composition specific calibration ratio for labor income, \( \chi^{i_z,f}_t \), and ratio for capital income, \( \chi^a_t \), ensure the correct tax base. A household’s adjusted gross labor income \( \hat{i}^{z,f}_t \), and adjusted gross capital income \( r^p a^{z,f}_t \), are obtained by applying the corresponding calibration ratio, such that:

\[
\begin{align*}
\hat{i}^{z,f}_{t,j} &\equiv \chi^{i_z,f}_{t,j} i^{z,f}_{t,j} \\
\hat{a}^{z,f}_{t,j} &\equiv \chi^a_t a^{z,f}_{t,j}
\end{align*}
\]  

(2.40)
Equation (2.41) summarizes the tax liability for a given household. Net tax liability $\mathcal{T}_{i,j}^{z,f}$ is equal to taxes owed on labor income, $\text{tax}_{i,j}^{z,f}$ — which may be determined either by the ITC or the BTF — plus tax liability on returns to saving, $\tau_{i,j}^{p} \tilde{a}_{i,j}^{z,f}$, plus tax liabilities associated with the Social Security system for retirees, $\tau_{i,j}^{pr} \tilde{i}_{i,j}^{z,f}$, less federal transfer payments, $\text{trfs}_{i,j}^{z,f}$, plus state and local tax liabilities, $\text{slt}_{i,j}^{z,f}$.

$$\mathcal{T}_{i,j}^{z,f} = \text{tax}_{i,j}^{z,f} + \tau_{i,j}^{p} \tilde{a}_{i,j}^{z,f} + \tau_{i,j}^{pr} \tilde{i}_{i,j}^{z,f} - \text{trfs}_{i,j}^{z,f} + \text{slt}_{i,j}^{z,f}$$

(2.41)

We now describe the specification of each fiscal instrument.

**Taxation of Capital Income and Retirement**

Average tax rates on capital income are determined by age group-family composition specific tax functions: There is a unique function estimated each for working single, working married, retired single, and retired married household. We consider working-age households separately from retirees to more accurately capture the observed differential in capital income tax liabilities, since workers tend to save through tax-deferred savings vehicles. We assume that a household’s average tax rate on capital income is a monotonically increasing function of their asset holdings relative to the asset distribution $f(a_{l}|f,j)$, which is conditional on family composition and whether the household is of working age or retired:9

$$\tau_{l}^{a} = q \left( a_{l,j}^{z,f}, f(a_{l}|f,j) \right)$$

(2.42)

We choose this specification over one that depends on a household’s predetermined productivity type because asset income tends to have large variance over the lifecycle, which raises the potential for a household to move in and out of several different asset income quantiles over their lifetime.

Working households pay into the Social Security program at proportional payroll tax rate on labor income each period, which applies to all taxable labor income up to a specified threshold. Retired households pay a proportional tax on their receipts of Social Security income, which depends on the level of Social Security income itself. Formally:

$$\tau_{i,j}^{pr} = \begin{cases} p \left( z_{i,j}^{z,f} \right) & j \leq R \\ r \left( s_{i,j}^{z,f} \right) & j > R \end{cases}$$

(2.43)

Finally, we allow for taxes on accidental bequests left by deceased households. Since accidental bequests are redistributed in a lump-sum fashion among all living households, we specify that the tax rate $\tau_{l}^{beq}$ is linear in bequests and unrelated to either the benefactor or beneficiary household’s other income.

**Taxation of Labor Income: Internal Tax Calculator**

Under the ITC tax system, household tax liability on labor income, $\text{tax}_{i,j}^{z,f}$, is determined by application of a statutory marginal tax rate schedule, deductions, and credits. This mapping from choice variables, state variables and demographic characteristics to a tax liability is developed to be as close to the actual IRC as possible for the provisions modeled. The effective marginal tax

---

9Since all households receive the same return on their savings, $r_{l}^{p}$, and face the same calibration ratio $\chi_{a}$, an ordering of households by their financial asset holdings is equivalent to an ordering by the taxable income from these assets.
rate on labor income is therefore not the statutory tax rate, but the marginal liability on incremental labor income after these deductions and credits have been applied.

The average tax rate on labor income before tax credits, \( \tau^i_t \), is determined by the statutory tax rate schedule in the tax calculator, adjusted gross labor income \( \hat{i}_{z,j}^{i,z,f} \), adjusted gross ordinary capital income \( krd_{z,j}^{i,z,f} \), and deductions \( ded_{z,j}^{i,z,f} \). Deductions are a function of adjusted gross labor income, adjusted gross ordinary capital income, and tax-preferred consumption choices made by the household. Credits \( crd_{z,j}^{i,z,f} \) are not only a function of labor income and family composition, but of other tax variables as well due to the refundability, or lack thereof, of various credits. Formally:

\[
tax_{z,j}^{i,z,f} = \max \left\{ \tau_t^{i,z,f}, 0 \right\} - crd_{z,j}^{i,z,f} - tra_{z,j}^{i,z,f}
\]

\[
\tau_t^{i,z,f} = \tau(\hat{i}_{z,j}^{i,z,f} + krd_{z,j}^{i,z,f} - ded_{z,j}^{i,z,f})
\]

\[
krd_{z,j}^{i,z,f} = k(r^a_{z,j})
\]

\[
ded_{z,j}^{i,z,f} = d(\hat{i}_{z,j}^{i,z,f}, krd_{z,j}^{i,z,f}, h_{z,j}^o, c_{z,j}^a)
\]

\[
crd_{z,j}^{i,z,f} = c(\hat{i}_{z,j}^{i,z,f}, krd_{z,j}^{i,z,f}, \kappa_{z,j}^{i,z,f}, ded_{z,j}^{i,z,f})
\]

\[
tra_{z,j}^{i,z,f} \begin{cases} 
\neq 0 & \text{if } n_j > 0 \text{ and } f = s \\
\neq 0 & \text{if } n_1^j > 0 \text{ and } f = m \\
0 & \text{otherwise}
\end{cases}
\]

where bold emphasis denotes a function. The last term in equation (2.44), is a productivity type - family composition specific transfer payment \( tra_{z,j}^{i,z,f} \), which is used as a non-distortionary method of ensuring that households within a given \((z,f)\) demographic group on average face a target average tax rate on labor income. This transfer may be positive or negative for different household groups, and is only nonzero for working households. Using equation (2.44) into equation (2.41) gives household tax liabilities when the treatment of labor taxation is as specified in the ITC tax system. Under this tax system, households consider the tax implications of their realized capital income when making their joint labor supply and savings decisions.

**Taxation of Labor Income: Bénabou Tax Function** This section describes the benchmark tax system for labor income that we use as a comparison to the internal tax calculator, the Bénabou tax function (BTF). It is a commonly-used tax function (Bénabou, 2002; Heathcote et al., 2017; Holter et al., 2017) that generates average tax rates and effective marginal tax rates over income. Like other commonly-used tax functions, the BTF is continuously differentiable,\(^{10}\) it allows for negative average tax rates to capture the effect of refundable tax credits, and it is easily parameterized with the exogenous specification of an effective marginal tax rate and average tax rate at the desired level of aggregation.

The BTF takes the form:

\(^{10}\)Other examples of smooth tax functions include, Easterly and Rebelo (1993), Gouveia and Strauss (1994), Li and Sarte (2004), and DeBacker et al. (2017).
\[
tax_{i_{t,j}} = \hat{z}_{i_{t,j}}^{f} - \lambda_{1}^{f}(\hat{z}_{i_{t,j}}^{f})^{1-\lambda_{2}^{f}}
\]  
(2.50)

where \(\lambda_{1}^{f}\) and \(\lambda_{2}^{f}\) are parameters which together determine the income-weighted average tax rate and effective marginal tax rate applied to labor income at each family composition. Using equation (2.50) into equation (2.41) gives household tax liabilities under the BTF tax system for labor income.

2.5.2 Federal Government

The federal government collects taxes from households and firms to finance non-valued government consumption expenditures, \(C_{t_{f}}^{fed}\), investment in productive public capital, \(I_{t_{f}}^{fed}\), social security payments for retirees, and other transfer payments to households. Budget deficits are financed through the sale of one-period bonds at the interest rate \(\rho_{t}\). Total government expenditures must be less than or equal to total tax revenue net of transfer payments \(T_{t_{f}}^{fed}\), plus new debt issues, less interest paid on old debt:

\[
I_{t_{f}}^{fed} + C_{t_{f}}^{fed} \leq T_{t_{f}}^{fed} + B_{t+1} - (1 + \rho_{t})B_{t}
\]  
(2.51)

where \(B_{t}\) is the beginning-of-period stock of outstanding one-period bonds. Total federal tax receipts \(T_{t_{f}}^{fed}\) are equal to the sum of current aggregate federal net tax receipts from households, \(T_{t_{f}}^{hh}\), taxes collected on accidental bequests, \(T_{t_{f}}^{beq}\), and the current federal tax receipts from firms, \(T_{t_{f}}^{bus}\), so that \(T_{t_{f}}^{fed} \equiv T_{t_{f}}^{hh} + T_{t_{f}}^{beq} + T_{t_{f}}^{bus}\). The law of motion for federal public capital is:

\[
G_{t_{f}}^{fed} + 1 = (1 - \delta^{g})G_{t_{f}}^{fed} + I_{t_{f}}^{fed}
\]  
(2.52)

The budget constraint in equation (2.51) implies: (i) in a macroeconomic steady state, the government rolls over a constant level of debt so that only finance charges \(\rho B\) are paid each year, and (ii) during transition paths, government debt may grow or shrink. To rule out explosive debt paths, we maintain the no-Ponzi condition:

\[
\lim_{k \to \infty} \frac{B_{t+k}}{\prod_{s=0}^{k-1}(1 + \rho_{t+s})} = 0
\]  
(2.53)

which implies that the current stock of debt is equal to the present-discounted value of all future primary surpluses along any equilibrium path.

Retired households get an annual social security payment \(ss_{i_{t,j}}^{z,f}\) from the federal government, which is assumed to be a function of payroll-taxable average earnings over working years for their particular productivity type - family composition. The federal government also utilizes three other transfer instruments: First, households uniformly receive lump-sum transfers \(trl_{t}\), which are intended to account for a specified share of current federal government transfers. Second, the government levies a lump-sum tax \(lst_{t}\) on households to incorporate those taxes specified to have only an income effect. Finally, to ensure that there exists a feasible choice set over the current net worth state space given the presence of lower bound constraints on housing and ordinary consumption, we specify conditional transfers \(trw_{i_{t,j}}^{z,f}\) for the purposes of welfare and housing assistance to low-income households. Letting the right-hand side of the household budget constraint in equation (2.13) be denoted with \(bdgt_{i_{t,j}}^{z,f}\):

\[
trw_{i_{t,j}}^{z,f} = \max \left\{ 0, c_{i}^{z} + p_{h}^{z} - bdgt_{i_{t,j}}^{z,s} \right\}
\]  
(2.54)
This means that requires a household both to be unable to afford the consumption and housing minimums, as well as have non-positive net worth in their next year of life in order to be a recipient of welfare transfers.

From a unified budget perspective, net income taxes collected by the federal government from households, \( T_{hh} \), consist of labor and capital income tax liabilities less credits, transfers and social security payments:

\[
T_{hh} = \int \int \sum_{f=s,m} \left( \text{tax}_{i,j}^z + \tau_t^{a_t} d_{i,j}^z + \tau_t^{pr} s_{i,j}^z - \text{trs}_{i,j}^z - ss_{i,j}^z \right) \Omega_{i,j}^z \, dz \, dj \quad (2.55)
\]

where:

\[
\text{trs}_{i,j}^z = \text{trw}_{i,j}^z + \text{trl}_t - \text{lst}_t
\]

From equation (2.27), and the deductibility of state and local taxes, business-level federal tax liabilities \( T_{t}^{bus} \) take the form:

\[
T_{t}^{bus} = \tau_t^{bus} \left( 1 - \tau_{slb}^t \right) \left( Y_t - w_t N_t \right) - \text{lsd}_{t}^{bus} \quad (2.56)
\]

The federal government is assumed to collect all accidental bequests at the end of each period, and redistribute them in a lump-sum fashion the following period after applying a tax. Taxes collected on accidental bequests left at the end of the previous period are therefore:

\[
T_{t}^{beq} = \tau_t^{beq} (1 - \Lambda) \int \int \sum_{f=s,m} y_{t+1,j+1} \Omega_{i,j}^z \, dz \, dj \quad (2.57)
\]

### 2.5.3 State and Local Government

Taxation at lower levels of government is incorporated both to account for their distortionary properties, for their deductibility from households' and firms' federal tax liabilities. For simplicity, we assume that household tax liabilities owed at the state and local level can be expressed as a proportion of taxable labor income and owner-occupied housing:

\[
\text{slt}_{i,j}^z \equiv \tau_t^{sl} t_{i,j}^z + \tau_t^{slp} h_{i,j}^o
\]

where \( \tau_t^{sl} \) is a linear tax rate taken to represent potentially deductible state and local income and sales tax and \( \tau_t^{slp} \) is a linear average tax rate on owner-occupied property. Aggregate household state and local tax liabilities can then be expressed as:

\[
T_{t}^{slh} = \int \int \sum_{f=s,m} \text{slt}_{i,j}^z \Omega_{i,j}^z \, dz \, dj \quad (2.59)
\]

Aggregate business state and local tax receipts are:

\[
T_{t}^{slb} = \tau_t^{slb} (Y_t - w_t N_t)
\]

where \( \tau_t^{slb} \) is the state and local business tax rate and the second term is business profits from equation (2.27). Total state and local taxes \( T_{t}^{sl} \) are equal to the sum of taxes collected
from businesses and households: \( T_{sl}^t = T_{slb}^t + T_{slh}^t \). These receipts are assumed to be spent on non-valued state and local composite government consumption expenditures \( C_{sl}^t \) and investment in productive public capital \( I_{sl}^t \) subject to an intraperiod balanced-budget condition:

\[
I_{sl}^t + C_{sl}^t = T_{sl}^t
\]  

(2.61)

where the law of motion for state and local public capital is:

\[
C_{sl}^{t+1} = (1 - \delta^g)C_{sl}^t + I_{sl}^t
\]  

(2.62)

### 2.6 Equilibrium

In order to exhibit a balanced growth path in steady state equilibrium, the model must be transformed into trend stationary form. The transformation is described in Appendix B.1 and the model is respecified as a stationary recursive dynamic program in Appendix B.2. Equilibrium for a given tax system is formally defined in Appendix B.3 as a collection of household decision rules that maximize households’ utility subject to household budget constraints, a collection of economic aggregates that are consistent with household behavior and the associated measure of households, profit-maximizing behavior by firms, a set of prices that facilitate clearing in factor, asset and goods markets, and an associated set of policy aggregates that are consistent with government budget constraints. In a steady state equilibrium, macroeconomic aggregates are growing at a constant rate equal to the sum of technological and population growth rates.

### 3 Baseline Calibration

We specify that discrete time in the model passes at an annual frequency. The set of parameters to be calibrated include both non-tax and tax policy parameters, both of which rely heavily on use of the Individual Tax Model (ITM) for specification, which makes use of data from individual tax returns filed with the Internal Revenue Service (IRS) and compiled by the IRS Statistics of Income (SOI) Division. We vary the use of long-run historical data, recent observations, and projections to construct parameter values in targeting the current economic environment and present (2018) tax law as closely as possible for the initial steady-state baseline equilibrium. We attempt to make the initial steady-state as comparable as possible across the internal tax calculator and the Bénabou tax function by imposing the same calibration targets on each, the key of which are summarized in Tables A1 and A2. To maintain focus on the tax details of our model, we discuss the calibration strategy for non-tax policy parameters in Appendix A; select exogenous parameters used are summarized in Table A3. The calibration of tax policy parameters is described in the following section.

#### 3.1 Tax Policy Parameters and Targets

We let households of working ages \( j = \{1, \ldots, R\} \) coincide with actual ages 25 through 64, and retired households aged \( j = \{R + 1, \ldots, J\} \) coincide with actual ages 65 through 90. As discussed in Appendix A.1.3, we construct productivity types \( z = \{1, \ldots, 5\} \) to represent a notion of lifetime labor income quintiles for both single and married households.
respectively. Finally, we take the family composition \( f = m \) to coincide with married households filing taxes jointly and, take \( f = s \) to represent all single- and non-joint filing households. We consider the age of a given married household filing jointly to correspond with the age of the primary filer.

This paper is primarily focused on modeling the taxation of labor income at the household level. However, we incorporate the taxation of household capital income and the business-level taxation of income to more completely approximate the federal tax system’s set of incentives and distortions, which are likely to affect labor supply and demand choices in general equilibrium. To map the flows of income received by households to their empirical counterparts, we consider: (i) gross labor income to correspond to the sum of a NIPA-comparable wage income concept described in Appendix A.1.3 and a \((1 - \alpha - g)\) share of pass-through business income, and (ii) gross capital income to correspond to the sum of interest income, dividends, realized capital gains, and an \((\alpha + g)\) share of pass-through business income. We consider the business-level tax liabilities to correspond with those due by C-corporations.

The calibration ratios for labor and capital income, \( \chi_{i,z,f} \) and \( \chi^a \), transform each household’s economic income flow into a taxable base as specified in equation (2.40). We allow for productivity type-family composition specific calibration ratios for labor income to capture the variation in nontaxable labor compensation received by households over lifetime income quintiles. These are set exogenously as the ratio of taxable labor income to NIPA-comparable wage income as calculated by the ITM. There is a single calibration ratio for capital income, which allows for the model to generate the desired level of federal receipts from the capital income tax for a given specification of the capital income average tax rate function in equation (2.42). It is set endogenously so that aggregate capital income tax receipts relative to aggregate output in the model’s present-law steady state equilibrium are equal to 2.04%, which is the level of total household capital income tax liabilities as calculated by the ITM relative to GDP in 2018 as projected by the Congressional Budget Office11 (CBO).

3.1.1 Federal Government Taxation Household Income

Taxation of Capital Income and for Retirement Since all households face the same rate of return on deposits and calibration ratio applied to capital income, an ordering of households by capital assets is equivalent to an ordering of households by taxable capital income. We exploit this equivalence and specify an average tax rate function for capital income that depends on the relative location of a household’s asset holdings in the cross-sectional distribution of assets, each for working single, working married, retired single, and retired married households as in equation (2.42). These functions allow household’s tax liability on capital income, which may vary significantly over their lifecycle, to be independent of their permanent productivity type. We assume that this function takes a quadratic form:

\[
\tau_i^a = q_{0j}^f + q_{1j}^f(\alpha_{i,j}) + q_{2j}^f(\alpha_{i,j})^2
\]

These functions are fit to the observed present-law average tax rates ordered by taxable capital income as calculated by the ITM for each age group - family composition demographic. The functions are then mapped to the model-generated cross-sectional distribution of capital assets for each demographic, restricting tax rates to be non-negative.

11 The Budget and Economic Outlook: 2018 to 2028, April 2018
The average tax rate on capital income for a household is determined by evaluating this mapping at their relative level of capital asset holdings and demographic group \((f,j)\).

Taxes associated with the retirement system in our model include the OASDI portion of the payroll tax, which finances the Social Security system, as well as special tax treatment of the benefits received by retirees. The OASDI payroll tax applies to all labor income up to the threshold specified under present-law at a rate of 12.4%\(^2\). The ratio for the taxable base of adjusted gross labor income adjusts endogenously and uniformly across taxpayers so that total payroll tax receipts relative to output are about 4.3%, as is projected by the CBO for 2018. To accurately capture the special tax treatment of Social Security income, the average tax rate on benefits in equation (2.43) for retirees is set for each productivity type - family composition demographic to match the associated income-weighted average tax rates calculated by the ITM.

Due to uncertain lifespans, households will die leaving accidental bequests behind. To account for the high end-of-life costs including medical expenses, some \(\Lambda\) fraction of these assets will be allocated to consumption services. The remainder will be taxed at the average rate \(\tau_{\text{beq}}\) and then distributed uniformly to the living population. The parameters \(\Lambda\) and \(\tau_{\text{beq}}\) are jointly and endogenously determined so that average after-tax bequests received by households are approximately 0.9% of aggregate output\(^3\) while estate and gift tax revenue is approximately 0.12% of GDP, as projected by the CBO for 2018.

**Taxation of Labor Income: Internal Tax Calculator** The internal tax calculator consists of a schedule of statutory marginal tax rates for ordinary income, deductions, and credits, the latter two of which are functions of labor and consumption choices. The statutory marginal tax rate schedule follows that specified under present-law from the 2018 IRC, which allows households to take into account that extra labor income or ordinary capital income could push them into a higher marginal tax bracket. Each household’s effective marginal tax rate applied to labor income is determined by the behavioral decisions made that imply deviations from the statutory tax rate schedule.

Using the eligibility criteria stated in the IRC, we construct the internal tax calculator to directly model the following provisions: the statutory rate schedule, the standard deduction, earned income credit, the child tax credit, the home mortgage interest deduction, state and local income, sales, and property tax deductions, the charitable giving deduction, the net investment income and Medicare surtaxes, and the dependent care credit. In doing so, we explicitly account for any phase-in and/or phase-out regions of the tax provisions, which could cause substantial deviation of the effective marginal tax rate from the statutory marginal tax rate for some households. To construct each household’s ordinary income tax base, we add a portion of taxable capital income to their taxable labor income; the portion of taxable capital income treated as ordinary is set to exogenously decrease over realized taxable capital income as computed from the ITM. Tax minimization behavior is assumed within the tax calculator such that any provision which may reduce tax liabilities is taken-up, including itemization of deductions (for state and local taxes, home mortgage interest, and charitable giving) in favor of the standard deduction.

The number of dependents claimed by a household matters for certain credits. While any qualifying dependent is counted for personal exemptions and earned income tax credit

\(^{12}\)While in practice employers and employees each remit payment of half the payroll tax liability, we assume the employee remits the full liability for simplicity.

\(^{13}\)This number reflects bequests that are left to recipients other than a spouse on average in the US from 1996-2012. See Wang (2016) for a summary of US bequest data.
(EITC) calculations, the child tax credit applies to dependents under the age of 17, and the child care credit and employer-provided child care deduction applies to dependents under the age of 13. Household averages for each of these three kinds of dependents are taken from the ITM and exogenously associated with each \((j, z, f)\) demographic within the model. For some calculations the frequency distribution for the number of qualifying dependents within a particular household demographic is also used. The frequency distribution is especially important for modeling the EITC as it increases in the number of children nonlinearly.

By incorporating dependents in the model, we create another source of heterogeneity which has the potential to influence economic choices. For example, the data indicate that young, single households have fewer dependents on average than young, married households. If both young, single and married households would be in the EITC phase-in range at the same level of earnings, the marginal and average tax rates will be higher for the single household than for the married household as the EITC will be larger for the married household given more qualifying dependents. If the EITC amount is then changed for households with zero dependents, for example, then the single household will be affected more than the married household. The differential change to marginal and average tax rates could induce different behavior across these two households.

To impose discipline on the tax liabilities generated by the internal tax calculator, we use productivity type - family composition specific transfers \(tra^{z,f}\), chosen so that income-weighted average tax rates on labor income generated by the model in either the present-law baseline or in the alternative-law scenario, \(ATR^{z,f}\), match the income-weighted average tax rate targets generated by the ITM, \(ATR^{z,f}\). The income-weighted average tax rate on labor income generated by the internal tax calculator for a given working household of productivity type - family composition is:

\[
ATR^{z,f}_i = \frac{\int_j tax^{z,f}_{i,j} \Omega^{z,f}_{i,j} \, dj}{\int_j \tilde{\Omega}^{z,f}_{i,j} \, dj} = \frac{\int_j \left( \max \left\{ \tau^{z,f}_{i,j}, 0 \right\} - crd^{z,f}_{i,j} - tra^{z,f}_{i,j} \right) \tilde{\Omega}^{z,f}_{i,j} \, dj}{\int_j \tilde{\Omega}^{z,f}_{i,j} \, dj}
\]

where \(\tilde{\Omega}^{z,f}_{i,j}\) is a new measure constructed for this calculation which only weights households with positive labor income, therefore eliminating unemployed and retired households:

\[
\tilde{\Omega}^{z,f}_{i,j} = \begin{cases} 
\Omega^{z,s}_{i,j} & \text{if } n_j > 0 \text{ and } f = s \\
\Omega^{z,m}_{i,j} & \text{if } n_j > 0 \text{ and } f = m \\
0 & \text{otherwise}
\end{cases}
\]

(3.1)

Setting \(ATR^{z,f} = ATR^{z,f}\) solving the above equation for \(tra^{z,f}\) gives us the desired level of productivity type - family composition specific transfer payments:

\[
tra^{z,f} = \frac{\int_j \left( \max \left\{ \tau^{z,f}_{i,j}, 0 \right\} - crd^{z,f}_{i,j} - ATR^{z,f} \tilde{\Omega}^{z,f}_{i,j} \right) \tilde{\Omega}^{z,f}_{i,j} \, dj}{\int_j \tilde{\Omega}^{z,f}_{i,j} \, dj}
\]

(3.2)

**Taxation of Labor Income: Bénabou Tax Function** The Bénabou tax function parameters \(\{\lambda_1^f, \lambda_2^f\}\) are calibrated so that the income-weighted average and effective

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14 Time subscripts are suppressed for steady state calculations.
marginal tax rate for each family composition $f$, $\overline{ATR}_f$ and $\overline{MTR}_f$ respectively, match those generated in baseline equilibrium under the ITC. Given the specification of the BTF in equation (2.50), the income-weighted average tax rate for family composition $f$ can be expressed as:

$$ATR_f = \frac{\int_Z \int_J ax_i z_{ij} \dot{\Omega}_j z_{ij} dj dz}{\int_Z \int_J \dot{\Omega}_j z_{ij} dj dz} = \frac{\int_Z \int_J \left( \dot{i}_{ij} z_{ij} - \lambda_f (i_{ij} z_{ij})^{1-\lambda_f} \right) \dot{\Omega}_j z_{ij} dj dz}{\int_Z \int_J \dot{\Omega}_j z_{ij} dj dz}$$

where $\dot{\Omega}_j z_{ij}$ is defined as in equation (3.1). Setting $ATR_f = \overline{ATR}_f$ and rearranging for $\lambda_f^1$ yields:

$$\lambda_f^1 = (1 - ATR_f) \left( \frac{\int_Z \int_J (\dot{i}_{ij} z_{ij}) \dot{\Omega}_j z_{ij} dj dz}{\int_Z \int_J (\dot{i}_{ij} z_{ij})^{1-\lambda_f} \dot{\Omega}_j z_{ij} dj dz} \right)$$

(3.3)

Analogously, the income-weighted effective marginal tax rate for family composition $f$ can be expressed as:

$$MTR_f = \frac{\int_Z \int_J \left( \frac{\partial tax_i z_{ij}}{\partial \dot{i}_{ij}} \right) \dot{i}_{ij} z_{ij} \dot{\Omega}_j z_{ij} dj dz}{\int_Z \int_J \dot{i}_{ij} z_{ij} \dot{\Omega}_j z_{ij} dj dz} = 1 - (1 - \lambda_f^2) (1 - ATR_f)$$

Setting $MTR_f = \overline{MTR}_f$ and $ATR_f = \overline{ATR}_f$, the above equation can be solved for $\lambda_f^2$ in terms of only exogenous tax rate targets:

$$\lambda_f^2 = \frac{MTR_f - ATR_f}{ATR_f - 1}$$

(3.4)

A Comparison of the ITC and the BTF: In Figure 1 we show the relationship between adjusted gross labor income and the portion of household tax liabilities attributed to labor income for both the ITC (top) and the BTF (bottom) in the initial present-law steady state equilibrium. The BTF smoothly maps taxable labor income into the associated tax liabilities, with the relationship determined by two parameters. The ITC, on the other hand, is a non-smooth mapping that allows for sources of variation in labor income tax liabilities other than taxable labor income. Variation in a household’s taxable ordinary capital income, number and age of dependents, and tax-preferred consumption choices all affect tax liabilities attributed to labor since key IRC provisions are explicitly modeled in the tax calculator.

Differences between the two specifications are especially stark at the low and high ends of the income distribution. At the low end, tax liability falls below -$5,000 for some households under the ITC, but never falls below -$2,500 under the BTF. At the high end, married households earning the same amount of labor income, about $355,000, have tax liability ranging from $60,000 to $71,000 under the ITC. Tax liability is approximately linear in adjusted gross labor income at this range under the BTF. In Section 4, we show that the additional tax detail contained in the ITC has both macroeconomic and welfare implications for tax policy changes that are not captured by the BTF.
3.1.2 Federal Government Taxation of Business Income

We model a combined business sector without distinguishing between corporate and pass-through production, when only the former files business-level returns separate from individual returns. To account for this, we assume that 73.44% of the combined business sector represents corporate entities with the residual representing pass-through entities. This figure is the average corporate share of total value-added in production over 2007-2016 as computed from the Federal Reserve Bank Financial Accounts.

We take a linear tax rate \( \tau_{bus} \) to represent the federal effective marginal corporate tax rate, and exogenously set it to 73.44% of the respective rate computed to the JCT’s Corporate Tax Model.\(^{15}\) We then set the federal lump-sum deduction \( lsd_{bus} \) endogenously so that federal business tax liabilities relative to aggregate output in the model’s present-law steady state equilibrium are equal to 1.19%, which is the projected federal corporate tax liabilities relative to GDP as projected by the CBO for 2018.

3.1.3 Federal Government Transfer Payments

A retiree’s current Social Security benefits depend on their past OASDI-covered labor income through payroll taxes. Modeling this explicit dependence under the assumption of full rationality requires households to consider off-equilibrium paths with respect to social security benefits when labor supply decisions are actually made. Since this approach would add substantial computational time, we assume that households are boundedly-rational in this dimension and do not contemplate the effects on their future social security benefits when making current labor supply decisions. That is, labor supply choices —and hence past OASDI-covered labor income—are consistent with actual social current security benefits only for the on-equilibrium path for each \((z, f)\) household demographic on average for a given cohort. Benefits are assumed to be a function of average lifetime earnings according to the benefit calculator available from the Social Security Administration.\(^{16}\)

The purpose of welfare transfers \( trw_{z,f} \) in our model is to ensure there exists a feasible solution at very low levels of consumable resources in the presence of positive lower bounds on housing and non-housing consumption. These transfers are subject to the means test in equation (2.54), which allows for a household without savings, and whose labor income is not high enough to afford consumption and rent minimums, to consume \( c \) and \( h \). The lump-sum transfer \( trl_t \) is uniform across all households and set endogenously to about 3.07% of aggregate output, which reflects the CBO’s projection\(^{17}\) for the share of current federal government transfers unrelated to transfers for OASI and Medicare, as well as the outlay portion of refundable tax credits for 2018. Lastly, the lump-sum taxes \( lst_t \) are set endogenously to about 0.71% of aggregate output, which reflects the CBO’s 2018 projection for excise tax liabilities and miscellaneous penalties.

\(^{15}\)For a description of the Joint Committee on Taxation’s Corporate Model, see JCT (2011)
\(^{16}\)While in practice OASDI covered earnings from the highest 35 years are used in the benefit calculation, for simplification purposes we assume benefits depend on the full 40 years of working life for households. See https://www.ssa.gov/pubs/EN-05-10070.pdf for a description of the benefit calculation.
\(^{17}\)An Update to the Budget and Economic Outlook: 2017-2027
3.1.4 State and Local Government Taxation

We incorporate household state and local tax liabilities using the linear tax rate $\tau_{sl}^t$ applied to households' adjusted gross labor income and the linear tax rate $\tau_{slp}^t$ applied the value of owner-occupied housing. The former rate is exogenously set to an effective rate representing the greater of state and local tax income or sales tax liabilities for each tax unit as computed by the ITM for 2018. The latter rate is exogenously set to 0.0105 $\times$ 0.7174 = 0.0075, which is the product of the national average property tax rate computed using state-level estimates from the National Association of Homebuilders for 2010-2014, and the the average portion of total residential capital that is not consumer durables as reported by NIPA for 2007-2016. The latter term in the product is included to account for the fact that our definition of housing services includes consumer durables.

For business-level taxation at the state and local level, we set the linear tax rate $\tau_{slb}^t$ endogenously so that state and local business tax liabilities relative to aggregate output in the model's present-law steady state equilibrium are equal to 0.38%, which is the historical average state and local corporate tax liabilities relative to GDP as computed from the National Income and Product Accounts over 2007-2016.

4 Policy Experiments

We demonstrate the implications of explicitly modeling tax provisions applied to labor income by simulating two policy changes in turn: (i) a ten-percent reduction in statutory tax rates applied to ordinary income, and (ii) an expansion of the earned income tax credit (EITC) for childless adults. To this end, we assume in all of the simulations in this paper that any tax provision set to expire after 2018 is instead permanent, including the major provisions associated with P.L. 115-97 which are set to expire in 2026.$^{18}$

Transition Analysis: We analyze the transition following implementation of alternative tax policy beginning from an initial steady state associated with present tax law in 2018. To compare responses across tax systems we report changes to key macroeconomic variables over the first ten years following the policy change to coincide with the 'budget window' used by the United States Congress to inform legislative decision-making. For each tax system, the series are expressed relative to initial steady state levels.

Following the announcement and implementation of a policy change in 'year 1', which is assumed to be unanticipated in the 'year 0' initial steady state, agents in the model have perfect foresight regarding the future time path of policy and the economy. Any policy-generated federal budget deficits or surpluses are financed by borrowing or used to pay down existing debt for the first 30 years following a policy change. Non-valued government consumption expenditures and lump-sum transfers subsequently adjust by equal amounts to maintain long-run fiscal sustainability, which is phased in over years 31 through 40, so that the Federal budget is balanced thereafter. A sufficient number of time periods is chosen for the transition path so that the economy reaches a new steady state associated with alternative tax law.

Steady State Analysis: We also compare the economic and welfare differences from the initial present-law steady state to the alternative-law steady states across each tax

$^{18}$See JCT (2018) for a list of expired and expiring tax provisions for years 2016 through 2027.
Changes to economic aggregates and prices across steady states are reported as percent differences from initial steady state to alternative steady state. In measuring changes to welfare for households, we compute the proportional change to the lifetime path of the consumption composite \( x_j \) for households born in the alternative steady state that would be needed to make them indifferent between being born in either steady state. For a single household this is:

\[
\sum_{j=1}^{J} (\beta_j^{-1} - 1)\pi_j U_{j}^{z,f} ((1 + \omega^{z,f})x^A_j, n^A_j) = \sum_{j=1}^{J} (\beta_j^{-1} - 1)\pi_j U_{j}^{z,f} (x^I_j, n^I_j)
\] (4.1)

where \( \omega^{z,f} \) is the proportional change in the consumption composite required to obtain indifference between steady states, and the \( A \) and \( I \) superscripts denote equilibrium choice variables associated with the alternative and initial steady states respectively. A negative value of \( \omega^{z,f} \) implies that a household demographic \((z,f)\) would prefer birth in the final steady state relative to the initial steady state. To compute changes to aggregate welfare, we integrate both sides of equation (4.1) for both single and married households over productivity type and age-of-household:

\[
\int \sum_{j=1}^{J} \beta_j^{-1} \pi_j \left\{ U_{j}^{z,s} ((1 + \bar{\omega})x^A_j, n^A_j) \Omega_{j}^{z,s} + U_{j}^{z,m} ((1 + \bar{\omega})x^A_j, n^1A_j, n^2A_j) \Omega_{j}^{z,m} \right\} dz
\]

\[
= \int \sum_{j=1}^{J} \beta_j^{-1} \pi_j \left\{ U_{j}^{z,s} (x^I_j, n^I_j) \Omega_{j}^{z,s} + U_{j}^{z,m} (x^I_j, n^1I_j, n^2I_j) \Omega_{j}^{z,m} \right\} dz
\] (4.2)

where \( \bar{\omega} \) is the aggregate proportional change in the consumption composite needed to make the households indifferent — on average — to being born in either steady state.

Finally, for purposes of our steady-state analysis, federal debt is held fixed while non-valued government consumption expenditures adjust to fully balance the federal budget. The choice of this instrument over lump-sum transfers avoids the income effect on household labor choice that would occur if lump-sum transfers were used to balance the budget. In holding federal debt fixed across steady states, we abstract away from the variation in the extent of crowding-out (crowding-in) that may occur under each tax system due to different paths of debt accumulation (deaccumulation).

### 4.1 Tax Instruments and Policy Changes

Both tax systems are calibrated for a policy change by holding constant income and choice variables associated with the initial steady state present-law equilibrium, and adjusting the tax instruments to target the five-year total conventional revenue effect over 2019-2024 as calculated by the Individual Tax Model (ITM).\(^{20}\) Changes to labor income taxation under the ITC are explicitly incorporated in the tax calculator, and transfers \( tra^{z,f} \) are altered as needed to match the average changes to tax liability predicted by the ITM.
for each \((z, f)\) demographic. For the BTF, changes to average tax rates and effective marginal tax rates applied to labor income are made by parameterizing the tax function to match those changes predicted by the ITM for each \(f\) demographic, with the average tax rate change scaled as needed to match the predicted labor income tax liability change. Changes to capital income taxation are implemented identically in each system. Equation (3.1) is re-estimated to match the changes to average tax rates applied to capital income predicted by the ITM for the capital income quintile specific to the each \((f, j)\) demographic, as well as changes to the calibration ratio to match predicted change to capital income tax liabilities.

To evaluate how well the aggregate behavioral incentives associated with a given policy change are captured in each tax system, we compare the changes to aggregate average tax rates and effective marginal tax rates to the analogous changes predicted by the ITM. In Table 2, we report errors for the changes to income-weighted average tax rates and effective marginal tax rates applied to labor income, holding constant present-law equilibrium household income levels and choice variables. The small errors indicate that both tax systems comparably replicate the tax rate changes predicted by the ITM. Consequentially we have confidence that both tax systems are calibrated well to capture the aggregate behavioral incentives associated with each policy change.

Despite the identical calibration targets described above, the tax function deviates from the tax calculator even before behavioral responses are incorporated. We highlight some key properties of the BTF tax function relevant for our purposes in Figure 2, which shows tax liability on labor income as a function of adjusted gross labor income for single and married households before and after each policy change under the BTF tax system, holding constant initial income levels. On the top panels we see that, due to the fixed functional form, instead of a strict shift downward in response to a ten percent tax rate cut for all households, the slope of the function decreases at each point. This implies a counterfactual increased net tax liability for singles earning less than $24,000 and married households earning less than $57,000. We see on the bottom panels that the EITC expansion does not face this same problem; the tax decrease is mostly extended to the targeted demographic - lower income single households. Nonetheless, the smooth tax function cannot capture the explicit earnings thresholds associated with the EITC; the figure shows that the single households above the earnings threshold (described in Section 4.3) experience a reduction in tax liabilities. We show in the following sections that these points are not innocuous: Each tax system produces different labor responses for both policy changes which can be traced by to these properties of the tax function.

4.2 Policy Experiment 1: 10% Statutory Rate Reduction

The first policy experiment is a permanent ten percent reduction in statutory tax rates for ordinary income - which include wage income, interest income, short-term capital gains, nonqualified dividends, and pass-through business income. While a small portion of the conventional revenue effect from this policy is due to the change in tax treatment of capital income, nearly all it results from the change in tax treatment of labor income.

4.2.1 Transition Years

Households respond to the rate reductions by increasing their work hours, although by a larger amount under the ITC than the BTF, shown in Figure 3. While the initial increases
in effective (productivity-weighted) labor supply taper off under both tax systems over time, labor hours remain higher than effective labor supply under the ITC at a level about 1.7% higher than baseline. As this does not occur under the BTF, this indicates that the net increase in hours is relatively more concentrated with lower-productivity workers on average over the first decade post-policy with the ITC.

In Table 3, we decompose the employment response across single, married primary, and married secondary individuals. Under the ITC, single individuals move from part-time to full-time, while under the BTF, they move from part-time to both full-time and unemployment. Although the intensive margin movement under both tax systems is consistent with the incentives provided by the policy change under analysis, we find the extensive margin movement under the BTF to be inconsistent. This particular employment change is most concentrated among the low-productivity singles, who under the BTF, face the counterfactual increase in tax liabilities (explained in Section 4.1). Married primary workers show some modest movement from part-time to full-time under both systems, while married secondary workers exhibit the largest movement into full-time employment as they move from both unemployment and part-time work. As a household, married individuals increase hours by a relatively more under the ITC.

While the two tax systems exhibit qualitatively similar patterns of expanded economic activity following the tax cut, there are quantitative differences present throughout the transition across other aggregates as a result of variation in the employment response of households: Following the larger increase in effective labor supply under the ITC, firms observe a higher marginal product of capital and respond by increasing their use of capital and producing more output. This accumulation of capital happens at the expense of housing and market consumption of households. Capital accumulation tapers off over the first decade as public debt begins to crowd-out private capital. As relatively larger taxable income bases result under the ITC than the BTF, the federal tax revenue loss is smaller under the former tax system, which results in a smaller accumulation of public debt over the first decade.

4.2.2 Steady State Comparison

A comparison of select aggregates across steady stats is shown in the two left columns of Table 4 for each tax system. As with the transition path, both tax systems exhibit a similar pattern of expanded macroeconomic activity, but with different magnitudes: The increase in effective labor supply from the rate reduction is larger in the ITC than in the BTF. This results in relatively more business capital, output, and taxable bases that mitigate the federal tax revenue loss. Since budget short-falls are completely financed by a reduction in non-valued government consumption in the alternative steady state, private capital is not crowded-out by public accumulation. The increase in deposits which finance private capital formation earn households a return that allows for increased housing and market consumption.

Unlike the transition path, the alternative steady state has reduced labor hours, even though effective labor supply is higher. This implies that there is a sufficiently large net increase in the labor hours of high-productivity workers offsetting the decrease in hours of other workers from an income effect. Despite this qualitative similarity, the source of declining labor hours differs across tax systems. The most significant difference is among single households, where net labor hours decline only under the BTF. Nearly two percentage points of individuals working part-time in the initial steady state leave
the labor force under the alternative steady state. This change, as in the transition path, is partially due to the counterfactual increase in tax liabilities associated with the properties of the tax function for this policy change. Married primary individuals under both tax systems enjoy more leisure by switching to part-time work in the years before retirement, decreasing full-time work. While some (mostly lower-productivity) secondary earners also switch from full-time to part-time work close to retirement, other (mostly higher-productivity) secondary earners move into full-time work from part-time during middle working-age years. While in the transition path the substitution effect dominates for lower-productivity individuals, the increased strength of the income effect is apparent in the alternative steady state.

Table 5 reports the percent change in lifetime consumption in the alternative steady state that would be needed to make households indifferent to being born in the initial steady state. At the aggregate level, the ITC exhibits a relatively larger welfare improvement than the BTF, with respective consumption equivalent variation (CEV) of -0.7% and -0.5%. The source of this difference in aggregate welfare improvements can be traced to differences in CEV by productivity-type. For both single and married households of the first productivity type in particular, there is a substantial welfare loss from the policy change under the BTF but a small welfare improvement under the ITC. Since these households are largely unaffected directly from the tax changes, we find the result under the BTF an artifact of the counterfactual tax liability increase at low-income levels associated with the tax function. Outside of these low-income levels, welfare improvements are comparable across tax systems.

4.3 Policy Experiment 2: Expansion of EITC

We simulate a permanent expansion of the EITC that increases the maximum credit and changes the phase-in and phase-out regions for low-income, childless households. In particular, the maximum credit is increased from its 2018 value of $519 to $2,000 for both single and married childless households. The credit, which remains fully refundable, is completely phased-in for households of either family composition at a labor income level of $10,180. It begins to phase out at labor income levels of $16,250 and $21,930 for single and married households respectively, becoming completely phased-out at $32,750 and $38,430. The expanded schedule is shown graphically in Figure 4, juxtaposed against the present law schedule for childless households and households with one child.

Single individuals account for most of the conventional revenue effect both because they are more likely to be childless than married couples and because they fall within the income range to qualify for the expanded credit. Under the present-law schedule, the lowest-productivity single workers are the primary credit recipients. Under the alternative-law schedule, holding constant initial labor income, the lowest three productivity types would largely qualify for the credit with the fourth productivity type qualifying only at younger and older ages due to lifecycle patterns of dependents and labor productivity. While the lowest productivity singles would be located along the phase-in region of the alternative-law schedule, the second through fourth productivity types would be on the flat or phase-out region of the schedule and further from the maximum credit region as their income rises. This initial positioning around the alternative-law schedule creates an incentive for these individuals to change their labor hours and hence labor income towards the maximum credit region.21

21It has been documented that the Earned Income Tax Credit is associated with substantial overclaims
4.3.1 Transition Years

The implications of explicitly modeling this policy change, targeted at specific taxpayers, are visualized in Figure 5. We decompose the employment response among single workers across productivity types for the ITC (top) and the BTF (bottom). Consistent with Eissa and Liebman (1996), we find that for both tax systems single workers exhibit an extensive margin movement into the labor force over the first five years following the credit expansion, even as the cost of participation includes forgone home production (Gelber and Mitchell, 2012). Along the intensive margin, however, we find that under the BTF net movement out of full-time work dominates net movement out of part-time work, decreasing labor hours among singles. The ITC instead exhibits a response where the movement out of part-time work dominates along the intensive margin, increasing labor hours in a manner consistent with the findings of Chetty et al. (2013). While high-productivity singles show nearly zero movement in employment for the ITC, their employment response is substantial under the BTF. Since this group earns labor income well above the credit eligibility threshold, we find the response under the BTF counterfactual to the policy.

Due to a greater extent of employment changes to take advantage of the expanded credit, the loss in federal tax revenue is greater under the ITC on average over the first decade following the policy change, as shown in Figure 6. While effective labor supply is up more under the ITC, the substantially larger increase in hours indicates that the increase in labor supply is more low-productivity-driven. This underlying difference persists over the first decade of the new policy, as cumulative deficits generate a relatively larger increase in federal debt held by the public. As a result, public debt accumulation begins to crowd out private capital accordingly in each tax system over the second five years. Firms in both tax systems respond to the increasing rental price of private capital by using less in production, which in turn decreases output and the demand for labor input over the second five years.

4.3.2 Steady State Comparison

Changes to select aggregates across steady states are reported in the right column of Table 4. Output is only marginally different across steady states for both tax systems, while the stock of household savings and business capital remain approximately unchanged. However, similarly small decreases in effective market labor supply coinciding with large differences in market labor hours imply substantial variation in demographic responses across tax systems. Under the ITC, the increase in labor hours of 0.4% is indicative of a substantial increase in labor hours by low-productivity workers outweighing a decrease in labor hours of middle-productivity workers. This contrasts with the response under the BTF, where the net change in labor hours of -0.4% reflects a relatively small increase in labor hours by low-productivity individuals that is more than offset by a decrease in labor hours of middle-productivity individuals. This negative net change in labor hours is inconsistent with the general findings of the literature, which suggests a resulting positive net hours response when considering all margins of labor adjustment simultaneously.22

Under both tax systems, the small increase in housing and market consumption is driven (IRS, 2014) and incomplete take-up (Pfeueger, 2009), which in dollar terms have offsetting effects on total credit outlays. Nonetheless, we assume full-compliance and take-up in our simulations so that the ITC and BTF tax systems can analyzed in a comparable fashion.

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22 See Nichols and Rothstein (2016) for a recent survey of the literature on labor supply and the EITC.
by low-productivity single workers who generally increase labor hours. The relatively larger response for the ITC reflects the larger increase in labor hours of these workers.

We report the consumption equivalent variation (CEV) in Table 6 to show the extent to which the different behavioral responses are captured in changes to household welfare across steady states. At the aggregate level, the ITC tax system exhibits an average welfare improvement smaller than the BTF tax system, with CEV of -0.2% and -0.7% respectively. To determine the source of this non-negligible difference in welfare improvement across tax systems, we examine the CEV by family-type and productivity-group. First, consistent with the notion that this particular policy change leaves most married households unaffected directly, we observe that married households have welfare changes that are substantially below that of single households. Second, as the largest beneficiaries of the expanded credit are the lowest two productivity-type singles for both tax systems, we observe similarly large welfare improvements among this demographic. However, we find the difference among the third and fourth productivity-type single households the most striking as the primary source of aggregate CEV differences, as the welfare improvement for the BTF is substantially larger than that of the ITC. Since the measure of third and fourth productivity singles who have income levels below the eligibility threshold is small, this result reflects the inability of the BTF to capture the discrete nature of this policy with a smooth approximation. Relative to the ITC, the result is an overstatement of welfare improvement sufficiently strong to affect the CEV at the aggregate level.

5 Conclusion

Since heterogeneous-agent models have become relatively common tools for macroeconomic analysis of fiscal policy, we have examined the extent to which incorporating explicit tax detail within an internal tax calculator is advantageous relative to the conventional use of a smooth tax function for the tax treatment of labor income. In the context of a large-scale OLG model, we have found that the ability of the tax calculator to target specific households affected by a policy change, and to allow for households’ tax liabilities to result from optimal behavioral responses in lieu of assigning effective rates according to a fixed function, both have macroeconomic implications. In particular, the quantitative differences in policy-induced economic activity arising from the use of the internal tax calculator over a smooth tax function are due to differences in household labor hours responses across the two alternative tax treatments. We find that labor responses that are counterintuitive to the policy change are due to counterfactual rate changes for some households when using the tax function. An implication of this finding is that while smooth tax functions may be appropriate for general analysis of tax progressivity, they are less suitable for analysis of specific policy changes. Consequentially, fiscal policy analysis of targeted tax changes using heterogeneous-agent models in the absence of sufficient tax detail may be unreliable.
6 Tables and Figures

Table 1: Financial Intermediary Balance Sheet and Income Statement

<table>
<thead>
<tr>
<th>Assets</th>
<th>Liabilities</th>
<th>Income</th>
<th>Expenses</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_{t+1}$</td>
<td>$r_t^p D_t$</td>
<td>$r_t^p K_t$</td>
<td>$K_t + \Xi_t$</td>
</tr>
<tr>
<td>$K_{t+1}$</td>
<td>$\delta^K K_t$</td>
<td>$\delta^K K_t + \Xi_t$</td>
<td></td>
</tr>
<tr>
<td>$H_t^r$</td>
<td>$p_t^r H_t^r$</td>
<td>$\delta^H H_{t-1}$</td>
<td></td>
</tr>
<tr>
<td>$B_{t+1}$</td>
<td>$\rho_t B_t$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2: Absolute Errors for Aggregate Tax Rates Changes on Labor Income

<table>
<thead>
<tr>
<th></th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rate Reduction</td>
<td>0.15</td>
<td>0.14</td>
<td>0.13</td>
<td>0.13</td>
</tr>
<tr>
<td>EITC Expansion</td>
<td>0.13</td>
<td>0.00</td>
<td>0.06</td>
<td>0.00</td>
</tr>
</tbody>
</table>

All errors expressed as absolute percentage point differences from ITM rate change.

Table 3: Rate Reduction: Percentage Point Change in Employment Status by Worker Type - Average Over First Ten Years of New Policy

<table>
<thead>
<tr>
<th></th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unemployed</td>
<td>0.0</td>
<td>1.5</td>
<td>0.0</td>
<td>0.0</td>
<td>-1.1</td>
<td>-2.1</td>
</tr>
<tr>
<td>Part-Time</td>
<td>-1.5</td>
<td>-3.1</td>
<td>-0.6</td>
<td>-0.2</td>
<td>-3.9</td>
<td>-1.2</td>
</tr>
<tr>
<td>Full-Time</td>
<td>1.5</td>
<td>1.5</td>
<td>0.6</td>
<td>0.2</td>
<td>5.0</td>
<td>3.3</td>
</tr>
</tbody>
</table>
Table 4: Steady State Comparison

<table>
<thead>
<tr>
<th></th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aggregates (%)</td>
<td></td>
<td></td>
<td>Rate Reduction</td>
<td>EITC Expansion</td>
</tr>
<tr>
<td>Output</td>
<td>1.2</td>
<td>0.8</td>
<td>-0.1</td>
<td>-0.2</td>
</tr>
<tr>
<td>Business Capital Stock</td>
<td>1.7</td>
<td>1.2</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>Effective Labor Supply</td>
<td>1.0</td>
<td>0.6</td>
<td>-0.2</td>
<td>-0.3</td>
</tr>
<tr>
<td>Labor Hours</td>
<td>-0.1</td>
<td>-0.5</td>
<td>0.4</td>
<td>-0.4</td>
</tr>
<tr>
<td>Market Consumption</td>
<td>1.7</td>
<td>1.3</td>
<td>0.1</td>
<td>0.0</td>
</tr>
<tr>
<td>Housing Service Consumption</td>
<td>1.6</td>
<td>1.4</td>
<td>0.2</td>
<td>0.1</td>
</tr>
<tr>
<td>Federal Tax Revenue</td>
<td>-3.0</td>
<td>-3.2</td>
<td>-1.1</td>
<td>-0.9</td>
</tr>
<tr>
<td>Deposits</td>
<td>3.2</td>
<td>2.5</td>
<td>0.0</td>
<td>0.0</td>
</tr>
</tbody>
</table>

All variables are expressed as percent differences across steady states.
Table 5: CEV (%) for Rate Reduction

<table>
<thead>
<tr>
<th>Productivity</th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Single Households</td>
<td>Married Households</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>-0.1</td>
<td>1.0</td>
<td>-0.2</td>
<td>1.0</td>
</tr>
<tr>
<td>2</td>
<td>-0.0</td>
<td>0.1</td>
<td>-0.6</td>
<td>-0.2</td>
</tr>
<tr>
<td>3</td>
<td>-0.5</td>
<td>-0.3</td>
<td>-0.9</td>
<td>-0.7</td>
</tr>
<tr>
<td>4</td>
<td>-1.1</td>
<td>-0.8</td>
<td>-1.3</td>
<td>-1.2</td>
</tr>
<tr>
<td>5</td>
<td>-1.6</td>
<td>-1.5</td>
<td>-2.4</td>
<td>-2.4</td>
</tr>
</tbody>
</table>

Table 6: CEV (%) for EITC Expansion

<table>
<thead>
<tr>
<th>Productivity</th>
<th>ITC</th>
<th>BTF</th>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Single Households</td>
<td>Married Households</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>-1.3</td>
<td>-1.5</td>
<td>-0.2</td>
<td>-0.2</td>
</tr>
<tr>
<td>2</td>
<td>-1.7</td>
<td>-1.4</td>
<td>0.1</td>
<td>-0.1</td>
</tr>
<tr>
<td>3</td>
<td>-0.1</td>
<td>-1.1</td>
<td>-0.1</td>
<td>-0.0</td>
</tr>
<tr>
<td>4</td>
<td>-0.0</td>
<td>-0.5</td>
<td>-0.1</td>
<td>-0.1</td>
</tr>
<tr>
<td>5</td>
<td>-0.1</td>
<td>0.2</td>
<td>-0.1</td>
<td>-0.0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>ITC</th>
<th>BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aggregate</td>
<td>-0.7</td>
</tr>
</tbody>
</table>
Figure 1: Labor Income and Tax Liabilities: Internal Tax Calculator vs. Tax Function
Figure 2: Labor Income and Tax Liabilities: Policy Changes with the Tax Function
Figure 3: Rate Cut: Aggregates During Transition Relative to Initial Steady State
Figure 4: Policy Experiment: EITC Expansion
Figure 5: EITC Expansion: Percentage Point Change in Employment Status by Productivity Type for Single Households - Average Over First Five Years of New Policy
Figure 6: EITC Expansion: Aggregates During Transition Relative to Initial Steady State
References


A Calibration

A.1 Non-Tax Policy Parameter Values and Targets

A.1.1 Demographics

Discrete time in the model passes at an annual frequency. At the end of each period, all individuals aged \( j = R = 40 \) retire and begin to face mortality risk while those aged \( j = J = 66 \) die with certainty. Model age \( j = 1 \) is set to correspond with actual age 25 so that model age \( j = 40 \) corresponds with actual age 64, and model age \( j = 66 \) corresponds with actual age 90.

The population growth rate is set to \( \nu_P = 0.0075 \), which is the average annual U.S. population growth rate projected by the Census Bureau for years 2018-2028. The rate of technological progress is set so that the steady state growth rate of aggregate output is equivalent to the average annual real GDP growth rate of 1.93% projected by the Congressional Budget Office\(^1\) (CBO) for years 2018-2028. Since aggregate output grows at rate \( \nu_P + \nu_A \) in a macroeconomic steady state, we set \( \nu_A = 0.0118 \).

Conditional survival probabilities \( \pi_j \) are set to \( \pi_j = 1 \) for ages \( j < R \), as households in the model only begin to face mortality risk upon retirement. We calibrate the latter conditional survival probabilities using the Social Security Administration’s 2013 Actuarial Life Table. We compute a weighted average over males and females for each given age to obtain a single age-variant series which we apply to all households.

The measure of households \( \Omega_{j,f}^z \) is constructed in four steps.\(^2\) First, given the constant rate of population growth and time-invariant mortality, we construct a stationary age profile of households as \( \Omega_{j+1} = (\Omega_j \pi_j)/\Upsilon_P \). Next, the joint density \( \Omega_j^f \) is constructed directly by computing the shares of joint and non-joint tax units out of total units over each age 25 through 90 projected for 2018 using the ITM. Third, the density \( \Omega^z \) is constructed independently of age and family composition under the assumption that the mass of each age - family composition group is equivalent for each of the \( nz \) productivity types, which implies \( \Omega^z = 1/nz \forall z \in \mathbb{Z} \). Finally, \( \Omega_{j,f}^z \Omega^z \) is normalized to have the property:

\[
\int_J \int_Z \sum_{f=s,m} \Omega_{j,f}^z = 1
\]

A.1.2 Firm Production Technology and Housing

To calculate the share of output in production for private and public capital respectively, we borrow from the method of Cooley and Prescott (1995) which allocates the ambiguous components of aggregate income in proportion to each factor’s share in measured output.\(^4\) Using data from the National Income and Product Accounts (NIPA) of the

---

\(^1\)Unless otherwise indicated, projections from the Congressional Budget Office are from The Budget and Economic Outlook: 2018 to 2028, April 2018

\(^2\)The time subscript is omitted for a cleaner exposition.

\(^3\)This is a natural assumption because, as described in Section A.1.3, productivity groups will be taken to represent lifetime labor income quintiles.

\(^4\)While Cooley and Prescott (1995) calculate factor income share of GNP, we follow their methodology to instead calculate factor income shares in GDP.

\(^5\)We consider ambiguous components to be proprietor’s income, the statistical discrepancy, taxes on production and imports, and the current surplus of government enterprises less subsidies. While the latter
Bureau of Economic Analysis for 2007-2016, we first calculate 36.17% as the joint share of GDP for both public and private non-residential capital. We then repeat the calculation private non-residential capital only, we yields private capital's share of production $\alpha = 0.3265$. Finally, we take public capital's share of production to be the residual of the joint share and private capital's share so that $g = 0.0352$.

As in Fernández-Villaverde and Krueger (2010), rates of economic depreciation on productive capital and housing capital are calculated using the steady state expression for the investment to capital ratio. For productive private capital this expression is $I^K/K = (\Upsilon_A \Upsilon_P - 1 + \delta^K)$. Solving for the depreciation rate yields $\delta^K = \left(\left(\frac{I^K}{K}\right) - \Upsilon_A \Upsilon_P + 1 \right)$. Using the average annual investment flows and stocks of private non-residential capital as reported by NIPA for years 2007-2016 yields $\delta^K = 0.0799$. Using the analogous expression for public capital, which we take here to include federal, state, and local capital, we compute $\delta^G = 0.0317$ over the same period. For housing capital, we calculate the depreciation rates using the average annual investment flows and stocks of private residential capital and consumer durables as reported by NIPA for years 2007-2016. The expression for the owner-occupied housing capital depreciation is the same as that for private capital, which obtains $\delta^o = 0.0555$. The depreciation rate on rental housing capital differs from owner-occupied housing capital because rental housing investment is assumed to be usable contemporaneously with investment flows. For rental housing capital, the investment to capital ratio is $I^r/H^r = (\Upsilon_A \Upsilon_P - 1 + \delta^r)/(\Upsilon_A \Upsilon_P)$, which has the associated depreciation rate $\delta^r = \Upsilon_A \Upsilon_P \left(\left(\frac{I^r}{H^r}\right) - 1 \right) = 0.0570$.

The financial intermediary faces quadratic costs of capital adjustment equal to $\Xi_t = \frac{\xi^K}{2} (\frac{K_{t+1}}{K_t} - \Upsilon_P \Upsilon_A)^2 K_t$. Given the rates of population growth and technological progress, this adjustment cost function is parameterized by $\xi^K$, which for purposes of the simulations is set to 6.

Following Gervais (2002), Fernández-Villaverde and Krueger (2010), and Cho and Francis (2011), we set the minimum down-payment required on owner-occupied home purchases to $\gamma = 0.20$. This figure also closely corresponds to the median loan-to-value ratio of 77% for owner-occupied housing units manufactured between 2010-2015 as reported in the Census Bureau’s 2015 American Housing Survey. Furthermore, as in Gruber and Martín (2003), we assume transaction costs associated with changing your housing status unit are symmetric for buying and selling. While the authors find median costs of 7% and 2.5% of housing value for selling and purchasing respectively, we conservatively choose the midpoint value so that $\phi^o = \phi^r = 0.05$.

To restrict households from purchasing unfeasibly small residences, we assume there is a lower bound on the support of rental housing $h^r$ and owner-occupied housing $h^o$ such that $0 < h^r \leq h^o$. The lower bound on owner-occupied housing value is set to target a homeownership ratio of 0.637 as reported for 2015 by the American Housing Survey. Reflecting the ratio of housing to food spending for the lowest decile of households in 2016 as reported by the Bureau of Labor Statistics (BLS) in the Consumer Expenditure Survey, the lower bound on rental housing value is set to be 2.525 times the average minimum consumption levels across family composition.
A.1.3 Household Characteristics and Preferences

The rate at which households discount future utility is set to target the observed private business investment to GDP ratio of 0.162 as calculated from NIPA for 2016. We set the subjective discount factor as $\beta = 0.94$ to target this figure under both tax systems.

Individual labor productivity $z_{j}^{i,f}$ is assumed to consist of two independent components: (i) an age-varying component $z_{j}$ and (ii) an age-invariant component that depends both on productivity type and family composition $z^{i,f}$, so that $z_{j}^{i,f} \equiv z_{j}^{i} z^{i,j}$. We let the number of productivity types $n_{z} = 5$ so that each type $z$ approximates average annual household labor income quintiles. Since a household of productivity type $z$ remains that type over their lifetime, our calibration is consistent with the notion of ‘lifetime’ labor earnings quintiles. This leads to a natural sorting of households by their labor income characteristics, where we define labor income to be the sum of a NIPA-comparable wage income concept and a $(1 - \alpha - g)$ share of pass-through business income.$^{6,7}$

To calibrate the age-varying component of labor productivity, we adopt the smoothed numerical wage profiles estimated in Rupert and Zanella (2015) for all individuals, normalizing the mean to unity. For the age-invariant component of labor productivity, we set $z^{i,j}$ for $z = \{1, \ldots, 5\}$ and $f = \{s, m\}$ endogenously so that average annual labor income over ages $j = \{1, \ldots, R\}$ in the model matches the ITM’s 2018 extrapolated values of average annual labor income over ages 25-64 for each respective group, when in present-law baseline equilibrium.$^{8}$ While both potential workers in married households face the same individual labor productivity term $z_{j}^{i,j}$, there is an exogenous productivity wedge $\psi^{i}$ between primary and secondary workers. This wedge is taken to represent the hourly earnings of secondary workers relative to primary workers, and is computed using the total wage and business income quintiles of primary filers and their spouses as reported by the Medical Expenditures Panel Survey (MEPS) for 2015.

Individual labor supply $n$ is indivisible, and is assumed to correspond with either full-time employment $n^{FT}$, part-time employment $n^{PT}$, or unemployment. Following the BLS, we consider full-time employment to correspond with at least 35 weekly hours of work and part-time employment to correspond with at least 1 but no more than 34 weekly hours of work. Using data from the BLS, we find that in 2016 the median full-time and part-time employees work 44.4 and 22.4 hours per week respectively, which are equivalent to about 2310 and 1163 working hours per year. As the BLS reports in the 2016 American Time Use Survey that the average individual spends about 3208.4 hours sleeping per year, full-time and part-time work correspond with 41.6% and 21.0% of waking hours spent working. We therefore normalize individual total time endowments to unity, and set $n^{FT} = 0.416$ and $n^{PT} = 0.210$.

The labor disutility coefficients $\psi^{i}, \psi^{m,1}, \psi^{m,2}$, and fixed cost of employment parameters $\phi^{i}, \phi^{m}$, are set so that model-generated lifecycle labor supply approximates the

---

$^{6}$The BEA does not report distributional characteristics of NIPA wage income. To approximate the desired NIPA wage income quintiles, we derive a ‘NIPA-comparable’ measure using the ITM by adding to AGI wage income (i) combat pay, (ii) employers’ share of the FICA tax, (iii) deferred 401k compensation, (iv) employers’ share of 401k compensation, (v) employer provided dependent care, (vi) employer health-insurance compensation, (vii) employer HSA compensation, and (viii) employer life-insurance compensation. See Ledbetter (2007) for a comparison of AGI income and NIPA income.

$^{7}$The pass-through business income considered here includes income flows from sole proprietorship, partnerships, S-corporations, estates and trusts, and rents and royalties.

$^{8}$To match the demographics explicitly modeled, we restrict our attention to households of these ages who are not receiving retirement income, e.g. 401(k), IRA, pension, or social security income.
distribution of employment status by earner type — single, married primary, or married secondary — as observed in the MEPS for 2015 and reported in Table A1. The fixed cost of employment parameter largely determines the workforce participation rate. The extensive margin elasticity, which determines the sensitivity of workers moving into or out of employment in response to changes in the after-tax wage rate, is determined endogenously by the distribution of reservation wages which itself partially depends on the fixed costs associated with working.

The intensive margin elasticity, which determines the sensitivity of workers choosing to supply more or less hours of work in response to changes in the after-tax wage rate conditional on already being employed, depends on the utility function curvature parameters $\zeta^s, \zeta^{m,1}, \zeta^{m,2}$ only in models of continuous labor choice. In models of discrete labor choice such as the one used here, Chang et al. (2011) show that these parameters are largely unrelated to the intensive margin elasticity. Rogerson and Wallenius (2009) and Keane and Rogerson (2012) show that higher values of these parameters imply that aggregate employment fluctuations depend more heavily on changes in the duration of working life, rather than changes in hours worked while employed. Estimated elasticities for secondary earners from their model simulation are systematically higher despite having the same curvature parameter as the primary earner. Perhaps most importantly for calibration purposes, movement along the intensive margin should account for one-third of aggregate employment fluctuations on average over 1970-2009, see Fiorito and Zanella (2012). Taking this into consideration, we choose the same relatively high uniform value for workers and set $\zeta^s = \zeta^{m,1} = \zeta^{m,2} = 5$.

The amount of hours spent on home production have a fixed, inverse relationship to the amount of labor hours. We used the 2016 American Time Use Survey to find the average housework hours for full time, part time, and unemployed individuals. Full time workers reported spending 0.62 hours per day, part time workers reported 1.52 hours per day, and unemployed individuals reported 1.73 hours. Normalizing available (non-sleep) time to unity yields the following mapping for home work time as a function of labor hours for singles and each married individual:

$$ N = [0.000, 0.210, 0.416] \rightarrow N^h = [0.114, 0.100, 0.041] $$

Empirically, the value of home production has been measured by multiplying hours spent on housework by the wage rate of domestic workers, see Bridgman (2016). We take a similar approach to calculating the value of home production as a function of non-work hours:

---

9MEPS reports the employment status of each individual in a married household, but does not specify who is the primary earner. Rather than erroneously using gender as an indicator of primary or secondary earnings status, we consider the amount of hours worked. If both individuals are unemployed, we consider the primary earner to be the one who is unemployed. If both individuals are working part time, or one is working part time and one is unemployed, we consider the primary earner to be the one employed part time. Lastly, if at least one earner is employed full time, we consider the primary earner to be the one employed full time. BLS consistent definitions of full-time, part-time and unemployed are used in construction of these targets.


11We summed four variables for home work averages: housework, food prep and cleanup, interior maintenance and exterior maintenance. We chose variables that can be reasonably outsourced for pay, and sounded most like chores, rather than hobbies or leisure activities.
\[
\ell_h(n^h_j) = \begin{cases} 
  w_{i}x_{n^h_j} & \text{if } f = s \\
  w_{i}x_{n^h_j + n^h_j} & \text{if } f = m
\end{cases}
\]
where \( w_{i}x_{n^h_j} \) is the average wage rate for the lowest productivity type single household.

Childcare expenses take the form \( \kappa_{z,f}^{j} \equiv cc_{z,f}^{j}v_{z,f}^{j}n_{j} \), where labor supply is evaluated at the quantity supplied by the secondary worker for married households. Given the average number of dependents under 13 within a household \( v_{z,f}^{j} \), we set the childcare cost scale parameter \( cc_{z,f}^{j} \) exogenously so that childcare expenses on average for each \((z, f)\) demographic when labor supply is evaluated as the employment targets discussed above match those values imputed by the ITM for 2018.

Given the specification of the non-housing consumption composite in equation (2.8), the relative optimal quantities of ordinary consumption and charitable giving can be expressed for those households not itemizing tax deductions as:

\[
\frac{c^g_j}{c^i_j} = \left( \frac{1 - \theta_{z,f}^{j}}{\theta_{z,f}^{j}} \right)
\]

Let \((\bar{c}^{g}/\bar{i})^{z,f}\) denote average charitable giving as a proportion of labor income targets for each \((z, f)\) combination as computed from the ITM for 2018. Then the consumption composite function can be parameterized endogenously by setting \(\theta_{z,f}^{j}\) such that:

\[
\theta_{z,f}^{j} = \left( 1 + (\bar{c}^{g}/\bar{i})^{z,f} \sum_{j=1}^{R} c_{z,f}^{j} \right)^{-1}
\]

which implies that in baseline equilibrium the model reproduces charitable giving targets on average for the working-age population.

The elasticity of substitution between housing and non-housing consumption is set to \( \eta = 0.487 \) as estimated by Li et al. (2016). The non-housing consumption preference parameter \( \sigma \) is set to target the ratio of private business investment to total private investment of 0.465 as calculated from the 2016 NIPA. The lower bound on permissible ordinary consumption levels \( c^i_j \) is set to be an arbitrary 5% larger than the maximum amount of home production consumption that may be obtained from choosing unemployment so that this constraint can potentially bind.

A.1.4 Government: Public Capital and Debt

Productive public capital held by the federal government and the state and local government are both set endogenously so that in present-law baseline they exhibit a value of 18.4% and 55.1% respectively of aggregate output. This value reflects an average over 2007-2016 from NIPA. Given this target, and the assumption that public capital remains fixed under proposed law simulations, the level of investment in public capital can be computed from the equation of motion.

The CBO projects that federal debt held by the public less financial assets relative to GDP will grow from 65.7% in fiscal year 2018 to 84.0% in fiscal year 2028. Because of this large projected increase we calibrate federal debt held by the public in the present-law baseline so that it approximately 74.6% of aggregate output, the average projected value over fiscal years 2028-2028. Furthermore, the United States Treasury reports in the December 2017 Treasury Bulletin that 21.7% of debt held by the public was held by
Federal Reserve Banks at the beginning of fiscal year 2018. Since this portion of public debt does not necessarily crowd out private capital, we endogenously set the net stock of government debt, $B$, in the present-law baseline so that its level relative to aggregate output is approximately 58.4%.

It is also projected by the CBO that net interest payments on federal debt relative to GDP will be growing over fiscal years 2018-2028. We therefore endogenously set the wedge between rate of return to private capital and government debt, $\varpi$, so that net interest payments relative to output match the average projected value of 2.60% over this time period.

### A.2 Endowment Heterogeneity

As shown in Hugget et al. (2011) for models of this class, differences in initial wealth contribute to a substantial portion differences in lifetime wealth. To account for this relationship we introduce variation in endowments of initial financial wealth $a_i$ over each demographic, which is indexed by $e = \{1, \ldots, ne\} \in \mathcal{E}$.

To specify beginning-of-period endowments for households entering the economy at age $j = 1$, we draw ratios of financial wealth to labor income, $A_j^f$, from the following distribution:

$$\sinh^{-1}(A_j^f) \sim N(\mu_j^f, \sigma_j^2)$$

where $\mu_j^f$ and $\sigma_j^2$ are taken to be the sample mean and variance of the inverse hyperbolic sine of financial wealth to labor income ratios for single and married families headed by a 25 year old in the *Survey of Consumer Finances* for 2013, respectively $\bar{x}^f = \{-0.0439, 0.0045\}$ and $s^2_j = \{0.7464, 0.6153\}$.

Letting $\bar{z}_j^f$ denote the average lifetime labor income targets, and $z_j$ be the age-varying component of individual labor productivity, we take the product $\bar{z}_j^f z_1$ as an approximation of average labor income for the youngest cohort of households. Treating single and married households as separate distributions, we take $ne = 40$ random draws of $A_j^f$ for each productivity type, we obtain initial endowments of financial wealth:

$$a_1^{e,z,f} = A_j^f \left( \frac{\bar{z}_j^f z_1}{\bar{z}_j^f z_1} \right)$$

where the denominator on the right-hand side normalizes initial endowments by the average labor income of the highest productivity type. Furthermore, we take the minimum drawn value of endowments for each labor productivity type $z$ and family composition $f$ as the lower-bound of wealth support for the respective demographic:

$$\Sigma_{z,f} = \arg \min(a_1^{e,z,f})$$

While this variation in endowment level does not change the dynamic optimization

---

12 We choose the inverse hyperbolic sine transformation to approximate a natural log transformation while allowing for negative values. See Pence (2006) for a discussion.

13 We define financial wealth as financial assets (balances of checking accounts, savings accounts, money market mutual accounts, call accounts at brokerages, prepaid cards, certificates of deposits, total directly-held mutual funds, stocks, savings and other bonds, IRAs, thrift accounts, future pensions, cash value of whole life insurance, trusts, annuities, managed investment accounts with equity interest and miscellaneous other financial assets) less debt (credit card balances, educational loans, installment loans, loans against pensions and/or life insurance, margin loans and other miscellaneous loans).
problem, endowment heterogeneity does add an additional layer of aggregation such that for any variable $x$:

$$x_{t,j}^{z,f} = \int \chi_{t,j}^{z,f,e} \Omega^e \, de$$

where $\Omega^e = \frac{1}{ne}$ is the measure of endowment level $e$. Therefore in each year of the simulation, $n f \times n z \times ne$ households enter the model. This level of aggregation is implicit in Appendix B.3.

**B Dynamic Programming Problem**

**B.1 Stationarity**

Along a steady-state balanced growth path, aggregate and individual variables will be growing at a constant rate. In order to apply numerical solution techniques for stationary economies we express these variables in trend-stationary form to adjust for the source of growth, which could be either population growth, technological progress, or both.\(^{14}\)

Letting the tilde accent denote a variable transformed to stationary form, Table A4 lists selected growth-adjusted variables.

Consider aggregate labor supply, $N$, which in a steady state will be growing due to population growth. While aggregate labor supply will therefore be growing at a rate of $\upsilon_P$, the stationary variable $\tilde{N}$ will be constant. Every other aggregate variable will be growing in a steady state due to both population growth and technological progress. Therefore, they can be made stationary by dividing each with the product $AP$. While each of these non-stationary aggregates will be growing at the rate of $\upsilon_P + \upsilon_A$ in a steady state, the stationary variable will be constant.

The measure of households' age and productivity, $\Omega$, will be growing at a rate of $\upsilon_P$ due solely to population growth, and therefore can be made stationary by dividing by the total population. Every other individual variable grows at a rate of $\upsilon_A$ in a steady state due solely to technological progress. These variables can therefore be made stationary by dividing each with the level of technology.

**B.2 Stationary Recursive Formulation**

The model described in Section 2 can be expressed as a trend stationary dynamic program. We formulate the problem from the perspective of households who take prices, bequests, and government policy as given. In each period of their life, households compare the indirect utility generated by decisions associated with owning a home against the welfare generated by decisions associated with renting:

$$V_{t,j}^{z,f}(\tilde{y}_{j}) = \max\{V_{t,j}^{o,z,f}, V_{t,j}^{r,z,f}\}$$

where $V_{t,j}^{o,z,f}$ and $V_{t,j}^{r,z,f}$ are the current period value functions associated with owning and renting respectively for a household of demographic $(j, z, f)$.

\(^{14}\)See King et al. (2002) for a detailed discussion of trend stationarity.
As a subset of the full set of constraints for this optimization problem, the household considering being a homeowner in period $t$ is:

$$V^{\alpha,z,f}_{t,j}(\tilde{y}_j) = \begin{cases} 
\max_{\tilde{y}_{j+1} : \tilde{x}_j, n_j \in \mathbb{N}} U^{\alpha,z,s}_{t,j}(\tilde{x}_j, n_j) + \beta \pi_j V^{z,s}_{t+1,j+1}(\tilde{y}_{j+1}) & \text{if } f = s \\
\max_{\tilde{y}_{j+1} : \tilde{x}_j, n^1_j, n^2_j \in \mathbb{N}} U^{\alpha,z,m}_{t,j}(\tilde{x}_j, n^1_j, n^2_j) + \beta \pi_j V^{z,m}_{t+1,j+1}(\tilde{y}_{j+1}) & \text{if } f = m
\end{cases}$$  \hspace{1cm} (B.2)

where:

$$U^{\alpha,z,f}_{t,j} \equiv \begin{cases} 
\max_{c_j, c^2_j, h^s_j} \log(\tilde{x}_j) - \psi^s \frac{n^1 + \zeta^s}{1 + \zeta^s} - F^s & \text{if } f = s \\
\max_{c_j, c^2_j, h^s_j} \log(\tilde{x}_j) - \psi^m \frac{n^1 + \zeta^m}{1 + \zeta^m} - \psi^m \frac{n^2 + \zeta^m}{1 + \zeta^m} - F^m & \text{if } f = m
\end{cases}$$  \hspace{1cm} (B.3)

$$\tilde{x}_j \equiv \left( \sigma c^2_j + (1 - \sigma) (\tilde{h}^o_j)^n \right)^{1/\eta}$$  \hspace{1cm} (B.4)

As a subset of the full set of constraints for this optimization problem, the household considering being a homeowner in period $t$ faces:

$$\tilde{c}^M_j + \tilde{c}^o_j + (r^p + \delta^o) \tilde{h}^o_j + \tilde{y}_{j+1} Y_A \leq (1 + r^p) \tilde{y}_j + b \tilde{c}_t + \tilde{r}^{z,f}_t - \tilde{T}^{z,f}_{t,j} - \tilde{r}^{z,f}_j - \phi^o \tilde{h}_{j+1} Y_A$$  \hspace{1cm} (B.5)

$$\tilde{h}^o_j \geq \tilde{h}^o$$  \hspace{1cm} (B.6)

$$\tilde{y}_j \geq \gamma \tilde{h}^o_j$$  \hspace{1cm} (B.7)

$$\tilde{r}^{z,f}_j = 0$$  \hspace{1cm} (B.8)

The value function for a household that will be a renter takes the form:

$$V^{r,z,f}_{t,j}(\tilde{y}_j) = \begin{cases} 
\max_{\tilde{y}_{j+1} : \tilde{x}_j, n_j \in \mathbb{N}} U^{r,z,s}_{t,j}(\tilde{x}_j, n_j) + \beta \pi_j V^{z,s}_{t+1,j+1}(\tilde{y}_{j+1}) & \text{if } f = s \\
\max_{\tilde{y}_{j+1} : \tilde{x}_j, n^1_j, n^2_j \in \mathbb{N}} U^{r,z,m}_{t,j}(\tilde{x}_j, n^1_j, n^2_j) + \beta \pi_j V^{z,m}_{t+1,j+1}(\tilde{y}_{j+1}) & \text{if } f = m
\end{cases}$$  \hspace{1cm} (B.9)

where:

$$U^{r,z,f}_{t,j} \equiv \begin{cases} 
\max_{c_j, c^2_j, h^s_j} \log(\tilde{x}_j) - \psi^s \frac{n^1 + \zeta^s}{1 + \zeta^s} - F^s & \text{if } f = s \\
\max_{c_j, c^2_j, h^s_j} \log(\tilde{x}_j) - \psi^m \frac{n^1 + \zeta^m}{1 + \zeta^m} - \psi^m \frac{n^2 + \zeta^m}{1 + \zeta^m} - F^m & \text{if } f = m
\end{cases}$$  \hspace{1cm} (B.10)

$$\tilde{x}_j \equiv \left( \sigma c^2_j + (1 - \sigma) (\tilde{h}^o_j)^n \right)^{1/\eta}$$  \hspace{1cm} (B.11)

As a subset of the full set of constraints for this optimization problem, the household considering being a renter in period $t$ faces:

$$\tilde{c}^M_j + \tilde{c}^o_j + p^r_t \tilde{h}^r_j + \tilde{y}_{j+1} Y_A \leq (1 + r^p_t) \tilde{y}_j + b \tilde{c}_t + \tilde{r}^{z,f}_t - \tilde{T}^{z,f}_{t,j} - \phi^o \tilde{h}_{j+1} Y_A - \tilde{r}^{z,f}_j$$  \hspace{1cm} (B.12)
\[ \tilde{h}_j^r \geq \tilde{h}_j^r \]  \hspace{1cm} (B.13)

\[ \tilde{y}_j \geq \tilde{y}_j^{z,f} \]  \hspace{1cm} (B.14)

\[ \tilde{h}_j^o = 0 \]  \hspace{1cm} (B.15)

Regardless of residential status, all households face the following equality and inequality constraints, employment fixed and variable costs, and initial and terminal conditions:

\[ \tilde{y}_j \equiv \tilde{h}_j^o + \tilde{a}_j \]  \hspace{1cm} (B.16)

\[ \tilde{c}_j \equiv (\tilde{c}_j^o)^{\theta^z} \tilde{y}_j^{(1-\theta^z)} \]  \hspace{1cm} (B.17)

\[ n_j^\epsilon = \begin{cases} 1 - l_j^\epsilon - n_j^h(n_j^r) & \forall j \leq R \\ 0 & \forall j > R \end{cases} \quad \epsilon = 1, 2 \]  \hspace{1cm} (B.18)

\[ \tilde{z}^{z,f}_{i,j} = \begin{cases} n_j \tilde{w}_i z_{j,s} + \tilde{s}_j z_{j,m} & \text{if } f = s \\ (n_j^1 + \mu^1 n_j^2) \tilde{w}_i z_{j,m} + \tilde{s}_j z_{j,m} & \text{if } f = m \end{cases} \]  \hspace{1cm} (B.19)

\[ \tilde{\kappa}_j^{z,f} = \begin{cases} \tilde{c} z_{j,s} n_j & \text{if } f = s \\ \tilde{c} z_{j,m} n_j^2 & \text{if } f = m \end{cases} \]  \hspace{1cm} (B.20)

\[ F^s = \begin{cases} \phi^s & n_j > 0 \\ 0 & n_j = 0 \end{cases} \]  \hspace{1cm} (B.21)

\[ F^m = \begin{cases} \phi^m & n_j^2 > 0 \\ 0 & n_j^2 = 0 \end{cases} \]  \hspace{1cm} (B.22)

\[ \tilde{c}_{i,j} \equiv \begin{cases} \tilde{c}^M_j + \tilde{c}^h(n_j^h) & \text{if } f = s \\ \tilde{c}^M_j + \tilde{c}^{h,2}(n_j^{h,1}) + \tilde{c}^{h,1}(n_j^{h,2}) & \text{if } f = m \end{cases} \]  \hspace{1cm} (B.23)

\[ \tilde{T}_{i,j}^{z,f} \equiv t a x_{i,j} + \tau^a t a_{i,j} + \tau^p r^{p_{i,j}} + (\tau^s t^z_{i,j} - l s t_t) + \tau^s t a_{i,j} + \tau^s t p h^o_{i,j} \]  \hspace{1cm} (B.24)

\[ \tilde{c}_{j} \geq \tilde{c}^i \]  \hspace{1cm} (B.25)

\[ \tilde{c}_j = \tilde{c}_j^i \quad \text{if} \quad \tilde{c}_j^i = \tilde{c}^i \]  \hspace{1cm} (B.26)

\[ \tilde{y}_1 = \tilde{a}_1 \]  \hspace{1cm} (B.27)

\[ \tilde{h}_1^o = \tilde{y}_{j+1} = 0 \]  \hspace{1cm} (B.28)

\[ V_{i,j+1}^{z,f} = 0 \]  \hspace{1cm} (B.29)
B.3 Equilibrium

For each household age cohort, \( j \), productivity type, \( z \), and family composition \( f \), households have ordinary consumption, \( \tilde{c} \), charitable giving, \( \tilde{c}^g \), market labor hours, \( n \), \( n^1 \), and \( n^2 \), owner-occupied housing services consumption, \( h^o \), rental housing services consumption \( h^r \), and future net worth \( \tilde{y}' \), as control variables. Households have current net worth \( \tilde{y} \) as their endogenous individual state variable, and their age, productivity type, as family composition as their exogenous state variables. Endogenous aggregate state variables are effective market supply \( \tilde{N} \), owner-occupied housing capital \( \tilde{H}^o \), rental housing capital \( \tilde{H}^r \), deposits \( \tilde{D} \), private business capital \( \tilde{K} \), public capital \( \tilde{G} \), federal government debt \( \tilde{B} \), and federal, state, and local tax instruments and transfer payments associated with given tax system, the set of which are denoted by \( \Gamma \). Then:

**Definition 1.** A perfect-foresight stationary recursive equilibrium is comprised of a measure of households \( \tilde{N}_{t,f} \), a value function \( V_{t,f}^z(\tilde{y}) \), a collection of household decision rules \( \{ \tilde{c}_{t,j}^z(\tilde{y}), \tilde{c}_{t,j}^g(\tilde{y}), \tilde{n}_{t,j}^z(\tilde{y}), \tilde{n}_{t,j}^{z,m^1}(\tilde{y}), \tilde{n}_{t,j}^{z,m^2}(\tilde{y}), \tilde{h}_{t,j}^{o,z}(\tilde{y}), \tilde{h}_{t,j}^{r,z}(\tilde{y}), \tilde{y}_{t,j}(\tilde{y}), \tilde{z}_{t,j}(\tilde{y}) \} \), prices \( \{ \tilde{w}_{t}, \tilde{r}_{t}, \tilde{p}_{t}, \tilde{\rho}_{t}, \tilde{r}_{t}^{P} \} \), aggregates \( \{ \tilde{N}_t, \tilde{H}^o_t, \tilde{H}^r_t, \tilde{D}_t, \tilde{K}_t, \tilde{G}_t, \tilde{B}_t, \tilde{C}_t, \tilde{I}_t, \tilde{G}_t \} \), and the set of tax instruments and transfers \( \Gamma \) associated with given tax system such that:

1. Household decision rules are the solutions to the constrained optimization problem in equations \((B.1)-(B.29)\).

2. Macroeconomic aggregates are consistent with household behavior such that:

\[
\tilde{N}_t = \int Z \int J \int \tilde{\Omega}_{t,j}^{z,s} \tilde{z}_{t,j}^{s} n_{t,j}^{z,s}(\tilde{y}) + \tilde{\Omega}_{t,j}^{z,m} \tilde{z}_{t,j}^{m} \left( n_{t,j}^{z,1}(\tilde{y}) + n_{t,j}^{z,2}(\tilde{y}) \right) \, dj \, dz
\]

\[
\tilde{H}^o_t = \int Z \int J \sum_{f=s,m} \tilde{\Omega}_{t,j}^{z,f} \tilde{h}_{t,j}^{o,z}(\tilde{y}) \, dj \, dz
\]

\[
\tilde{H}^r_t = \int Z \int J \sum_{f=s,m} \tilde{\Omega}_{t,j}^{z,f} \tilde{h}_{t,j}^{r,z}(\tilde{y}) \, dj \, dz
\]

\[
\tilde{D}_t = \int Z \int J \sum_{f=s,m} \tilde{\Omega}_{t,j}^{z,f} \tilde{a}_{t,j}(\tilde{y}) \, dj \, dz
\]

\[
\tilde{C}_t = \int Z \int J \sum_{f=s,m} \tilde{\Omega}_{t,j}^{z,f} \left( \tilde{c}_{t,j}^z(\tilde{y}) - \tilde{c}_{t,j}^{h,z}(\tilde{y}) \right) + \tilde{c}_{t,j}^{g,z}(\tilde{y}) + \tilde{n}_{t,j}^{z,f} \right) \, dj \, dz + \tilde{c}_{t}^{z,od}
\]

3. Firms hire private factors of production to produce output at profit-maximizing levels while taking public capital and factor prices consistent with the following as given:

\[
\tilde{w}_t = (1 - \alpha - g) \tilde{G}_t^{\alpha} \tilde{K}_t^{1-\alpha} \tilde{N}_t^{\alpha-g}
\]

\[
r_t = \tilde{K}_t^{-1} \left( (1 - \tau_t^{bus} \alpha / (\alpha + g) (\tilde{G}_t^{\alpha} \tilde{K}_t^{1-\alpha}) + \tau_t^{bus} \tilde{d}_t^{bus} \right)
\]

4. The asset market clears such that:

\[
\tilde{D}_{t+1} = \tilde{K}_{t+1} + \tilde{H}_t^{r} \left( \tilde{Y}_p \tilde{Y}_A \right)^{-1} + \tilde{B}_{t+1}
\]

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where the financial intermediary optimally allocates deposits into productive private capital and rental housing so that the following no-arbitrage condition holds:

\[ p_t^r = r_{t+1} - \delta^K + \delta^r - \left( \frac{\partial \tilde{z}_t}{\partial K_{t+1}} + \frac{\partial \tilde{z}_{t+1}}{\partial K_{t+1}} \right) \]

and is willing to accept ‘safe-asset’ pricing of federal government bonds so that:

\[ \rho_t = r_t - \omega \]

Furthermore, the rate of return paid to households on deposits is determined by application of a zero profit condition so that:

\[ r_t^p = D_t^{-1} \left( (r_t - \delta^K) K_t - \Xi_t + p_t H_t^r - \delta^r H_{t-1}^r (Y_P Y_A)^{-1} + \rho_t B_t \right) \]

5. The goods market clears such that:

\[ F(\tilde{G}, \tilde{K}_t, \tilde{N}_t) = \tilde{C}_t + \tilde{I}_t + \tilde{G}_t \]

where private aggregate investment is defined as:

\[ \tilde{I}_t \equiv \tilde{I}_K^t + \tilde{I}_o^t + \tilde{I}_r^t + \tilde{\Phi}_t^H \]

with:

\[ \tilde{I}_K^t = K_{t+1} (Y_P Y_A) - (1 - \delta^K) K_t + \Xi_t \]
\[ \tilde{I}_o^t = \tilde{H}_o^{t+1} (Y_P Y_A) - (1 - \delta^o) \tilde{H}_o^t \]
\[ \tilde{I}_r^t = \tilde{H}_r^t - (1 - \delta^r) \tilde{H}_r^{t-1} \Phi_{t+1}^r (Y_P Y_A)^{-1} \]
\[ \tilde{\Phi}_t^H = \int \int \sum_{f=s,m} \tilde{G}_{t+1}^{s,m} \left( \phi_o h_{t+1,j+1}^o (\tilde{y}) + \phi_r h_{t+1,j+1}^r (\tilde{y}) \right) dj dz \]

and where aggregate government expenditures is defined as:

\[ \tilde{G}_t \equiv \tilde{C}_t^{fed} + \tilde{C}_t^{sl} + \tilde{I}_t^{fed} + \tilde{I}_t^{sl} \]

with:

\[ \tilde{I}_t^{fed} = G_t^{fed} (Y_P Y_A) - (1 - \delta^g) G_t^{sl} \]
\[ \tilde{I}_t^{sl} = G_t^{sl} (Y_P Y_A) - (1 - \delta^g) G_t^{fed} \]

6. The federal government’s debt follows the law of motion:

\[ \tilde{B}_{t+1} (Y_P Y_A) = \tilde{C}_t^{fed} + \tilde{I}_t^{fed} - (\tilde{T}_t^{hh} + \tilde{T}_t^{bus} + \tilde{T}_t^{eq}) + (1 + \rho_t) \tilde{B}_t \]

and maintains a fiscally sustainable path so that:
\[
\lim_{k \to \infty} \frac{\hat{B}_{t+k}}{\prod_{s=0}^{k-1} (1 + \rho_{t+s})} = 0
\]

where net federal tax receipts from households, firms, and bequests are:

\[
\hat{T}_{t}^{bh} = \int_{Z} \int_{J} \sum_{f,s,m} \hat{\Omega}_{t,j}^{z,f} \left( \hat{t}_{x}^{z,f} \hat{p}_{x}^{z,f} + \hat{p}_{x}^{pr} \hat{r}_{x}^{z,f} - (\hat{r}_{x}^{z,f} + \hat{\beta}_{x}^{z,f} - \hat{s}_{x}^{z,f}) \right) dz \]

\[
\hat{T}_{t}^{bus} = \tau_{t}^{bus} \left( (1 - \tau_{t}^{slb})(\hat{Y}_{t} - \hat{w}_{t} \hat{N}_{t}) - \hat{lsd}_{t}^{bus} \right)
\]

\[
\hat{T}_{t}^{beq} = \tau_{t}^{beq} (1 - \Lambda) (\hat{Y}_{t} - \hat{w}_{t} \hat{N}_{t})
\]

7. The state and local composite government maintains a balanced budget:

\[
\hat{T}_{t}^{slh} + \hat{T}_{t}^{slb} = \hat{C}_{t} + \hat{I}_{t}^{sl}
\]

where net state and local tax receipts from households and firms are:

\[
\hat{T}_{t}^{slh} = \int_{Z} \int_{J} \sum_{f,s,m} \hat{\Omega}_{t,j}^{z,f} \left( \tau_{t}^{sl} \hat{\nu}_{t,j}^{z,f} + \tau_{t}^{spl} \hat{p}_{x}^{z,f} \right) dz \]

\[
\hat{T}_{t}^{slb} = \tau_{t}^{slb} \left( \hat{Y}_{t} - \hat{w}_{t} \hat{N}_{t} \right)
\]

8. The measure of households is time-invariant:

\[
\hat{\Omega}_{t+1,j}^{z,f} = \hat{\Omega}_{t,j}^{z,f}
\]

9. The net worth of households that die before reaching the maximum age J is allocated to end-of-life consumption expenditures to bequests among the living such that:

\[
\hat{c}_{t}^{col} = \Lambda (\hat{Y}_{A}) \int_{Z} \int_{J} (1 - \pi_{j}) \sum_{f,s,m} \hat{\Omega}_{t,j}^{z,f} \hat{y}_{t+1,j+1} dz
\]

\[
\hat{b}_{ct} = (1 - \tau_{t}^{beq})(1 - \Lambda) (\hat{Y}_{A}) \int_{Z} \int_{J} (1 - \pi_{j}) \sum_{f,s,m} \hat{\Omega}_{t,j}^{z,f} \hat{y}_{t+1,j+1} dz
\]

**Definition 2.** A steady-state perfect-foresight stationary recursive equilibrium is a perfect-foresight stationary recursive equilibrium, where every growth-adjusted aggregate variable is time invariant.


C Description of Solution Algorithm

C.1 Steady State

1. Given the set of tax instruments and transfers $T$ and a starting guess for accidental bequests $\tilde{b}_{eq}$, make a guess for the set of endogenous aggregate state variables $\{\tilde{N}_t, \tilde{H}_t^o, \tilde{H}_t^r, \tilde{K}_t, \tilde{G}_t, \tilde{B}_t\}$, and use these guesses to compute the of prices $\{\tilde{w}_t, \tilde{r}_t, \tilde{p}_r, \tilde{\rho}_t, \tilde{r}_p\}$.

2. For each household family composition $f = s, m$ and labor productivity type $z \in Z$, obtain the optimal household decision rules associated with the value function in equation (B.1) at each age $j \in J$ by backwards recursive iterations, subject to equations (B.2)-(B.29):
   
   (a) Beginning with the maximum age $J$, analytically compute the optimal choices of housing, ordinary consumption, and charitable giving in terms of a grid of discrete values for current net worth $\tilde{y}_J$, both for the optimization problem particular to current period renters and homeowners as described in Section B.2.\footnote{Since the model is solved backwards, optimal choices for a household aged $j+1$ are known before those of a household aged $j$. Therefore $\tilde{h}_t^o, \tilde{h}_t^r$ and $\tilde{c}_t^f$ are used as proxies for $\tilde{h}_t^o, \tilde{h}_t^r$ and $\tilde{c}_t^f$ for purposes of computing itemized tax deductions during the optimization step. This allows for a substantial reduction in computational burden by avoiding a search over some specified support for $\tilde{h}_t^o$ and $\tilde{c}_t^f$ in addition to the search needed over labor supply in order to know $i_t^z:z$ for the working-age population. The approximation error introduced by this proxy is limited both the share of households which itemize tax deductions, and the lifecycle smooth path of these variables.} Use these choices to compute the value functions associated with renters and homeowners respectively, setting the value function to a large negative number for those choices that violate inequality constraints. For each net worth node, set $V_{t,j}^{z,f}(\tilde{y}_J)$ equal to the maximum of $V_{t,j}^{z,f}$ and $V_{t,j}^{z,f}$. Store the household choices associated with the optimal housing status at each net worth node.

   (b) For ages $j \in \{J-1, \ldots, 1\}$, repeat part (a) for every possible $(\tilde{y}_j, \tilde{y}_{j+1})$ combination of net worth nodes to obtain the optimal household choices each age.

3. Use the optimal household decision rules obtained from the previous step to simulate lifecycle choices for each demographic with the initial conditions for net worth of $\tilde{y}_1 = \tilde{a}_1$ and owner-occupied housing $\tilde{h}_1^o = 0$. Simulation includes net endowment levels from each demographic for a total of $nf \times nz \times J \times ne$ simulations. Compute all aggregates and implied prices.

4. Compare the new set of aggregates $\{\tilde{N}_t, \tilde{H}_t^o, \tilde{H}_t^r, \tilde{K}_t, \tilde{G}_t, \tilde{B}_t\}$ and accidental bequests $\tilde{b}_{eq}$ to the initial guesses. If the value of these new aggregates are sufficiently close to the guessed values, then a steady-state equilibrium is obtained and the program can be terminated. If not, update each guess by taking a linear combination of the original guess and the new value obtained from application of equilibrium conditions. Use these new guesses to compute new values for the set of prices $\{\tilde{w}_t, \tilde{r}_t, \tilde{p}_r, \tilde{\rho}_t, \tilde{r}_p\}$. Return to step 2.
C.2 Transition Path

1. Choose the number of transition periods, $tp$, sufficiently large so that the economy reaches a steady state following a policy change.

2. Compute the initial steady state for the policy baseline and the final steady state under the new policy.

3. Provide an initial guess for the time path of the set of aggregate variables.

4. Compute the transition path.
   (a) For years before policy change, use decision rules from steady state.
   (b) Starting the first year of policy change, compute new decision rules for agents of each demographic for the price guesses for that time period.
   (c) Run simulation starting $J$ years before policy change so that by the first transition year, there are $J$ ages. Use new decision rules and price guesses to simulate forward $tp$ periods.
   (d) Compute new aggregates and prices for each time period.

5. Compare the initial guess for the time path of the aggregate variables to their new time path obtained from the previous step. If time paths are sufficiently close, terminate the program. If not, update the guesses by taking a linear combination of the new time path and the old time path. Return to Step 4.
## Tables

**Table A1:** Targeted and Baseline Actual Employment Status by Type of Worker

<table>
<thead>
<tr>
<th>Type of Worker</th>
<th>Data</th>
<th>Model: ITC</th>
<th>Model: BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>FT</td>
<td>PT</td>
<td>U</td>
</tr>
<tr>
<td>Single</td>
<td>0.61</td>
<td>0.24</td>
<td>0.15</td>
</tr>
<tr>
<td>Married Primary</td>
<td>0.90</td>
<td>0.08</td>
<td>0.25</td>
</tr>
<tr>
<td>Married Secondary</td>
<td>0.42</td>
<td>0.32</td>
<td>0.26</td>
</tr>
</tbody>
</table>

*Totals may not sum to 1 due to rounding*

**Table A2:** Targeted and Baseline Actual Aggregate Ratios

<table>
<thead>
<tr>
<th>Target Ratio</th>
<th>Data</th>
<th>Model: ITC</th>
<th>Model: BTF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Homeownership ratio</td>
<td>0.64</td>
<td>0.65</td>
<td>0.65</td>
</tr>
<tr>
<td>Private business investment to total private investment ratio</td>
<td>0.47</td>
<td>0.47</td>
<td>0.47</td>
</tr>
<tr>
<td>Private business investment to output ratio</td>
<td>0.16</td>
<td>0.17</td>
<td>0.17</td>
</tr>
</tbody>
</table>
Table A3: Select Exogenous Parameters

<table>
<thead>
<tr>
<th>Demographics</th>
<th></th>
<th></th>
<th></th>
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</thead>
<tbody>
<tr>
<td>Terminal ages</td>
<td>$R, J$</td>
<td>40, 66</td>
<td></td>
</tr>
<tr>
<td>Rate of population growth</td>
<td>$v_p$</td>
<td>0.0075</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Production</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Rate of technological progress</td>
<td>$v_A$</td>
<td>0.0118</td>
<td></td>
</tr>
<tr>
<td>Private capital share of output</td>
<td>$\alpha$</td>
<td>0.3265</td>
<td></td>
</tr>
<tr>
<td>Public capital share of output</td>
<td>$g$</td>
<td>0.0352</td>
<td></td>
</tr>
<tr>
<td>Private capital depreciation rate</td>
<td>$\delta_K$</td>
<td>0.0799</td>
<td></td>
</tr>
<tr>
<td>Private capital adjustment cost parameter</td>
<td>$\xi_K$</td>
<td>6</td>
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</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Housing</th>
<th></th>
<th></th>
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</thead>
<tbody>
<tr>
<td>Owner-occupied housing minimum down-payment</td>
<td>$\gamma$</td>
<td>0.20</td>
<td></td>
</tr>
<tr>
<td>Housing status adjustment cost</td>
<td>$\phi^o, \phi^r$</td>
<td>0.05, 0.05</td>
<td></td>
</tr>
<tr>
<td>Housing services depreciation rate</td>
<td>$\delta^o, \delta^r$</td>
<td>0.0555, 0.0570</td>
<td></td>
</tr>
<tr>
<td>Owner-occupied housing minimum (ITC)</td>
<td>$h^o$</td>
<td>1.22</td>
<td></td>
</tr>
<tr>
<td>Owner-occupied housing minimum (BTF)</td>
<td>$h^o$</td>
<td>1.14</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Preferences</th>
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</thead>
<tbody>
<tr>
<td>Subjective discount factor</td>
<td>$\beta$</td>
<td>0.940</td>
<td></td>
</tr>
<tr>
<td>Non-housing consumption share of composite</td>
<td>$\sigma$</td>
<td>0.187</td>
<td></td>
</tr>
<tr>
<td>Housing/non-housing consumption substitution elasticity</td>
<td>$\eta$</td>
<td>0.487</td>
<td></td>
</tr>
<tr>
<td>Utility curvature parameter</td>
<td>$\zeta^f, \epsilon$</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>Intensive labor margin disutility (ITC)</td>
<td></td>
<td>$\psi^s, \psi^{m,1}, \psi^{m,2}$</td>
<td>395.1, 264.6, 176.7</td>
</tr>
<tr>
<td>Intensive labor margin disutility (BTF)</td>
<td></td>
<td>$\psi^s, \psi^{m,1}, \psi^{m,2}$</td>
<td>396.3, 279.9, 177.6</td>
</tr>
<tr>
<td>Extensive labor margin fixed cost (ITC)</td>
<td></td>
<td>$\phi^s, \phi^m$</td>
<td>0.354, 0.155</td>
</tr>
<tr>
<td>Extensive labor margin fixed cost (BTF)</td>
<td></td>
<td>$\phi^s, \phi^m$</td>
<td>0.393, 0.151</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Government</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Public capital depreciation rate</td>
<td>$\delta^g$</td>
<td>0.0317</td>
<td></td>
</tr>
</tbody>
</table>
Table A4: Trend Stationary Transformations for Selected Variables

<table>
<thead>
<tr>
<th>Aggregate Variables:</th>
<th></th>
<th>Individual Variables:</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tilde{C}_i^a \equiv \frac{C_i^a}{A_tP_t}$</td>
<td>$\tilde{H}_i^o \equiv \frac{H_i^o}{A_tP_t}$</td>
<td>$\tilde{c}_i^a \equiv \frac{c_i}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{H}_i^a \equiv \frac{H_i^a}{A_tP_t}$</td>
<td>$\tilde{H}_i^r \equiv \frac{H_i^r}{A_tP_t}$</td>
<td>$\tilde{h}_i^o \equiv \frac{h_i^o}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{H}_i^l \equiv \frac{H_i^l}{A_tP_t}$</td>
<td>$\tilde{D}_l \equiv \frac{D_l}{A_tP_t}$</td>
<td>$\tilde{h}_i^r \equiv \frac{h_i^r}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{K}_t \equiv \frac{K_t}{A_tP_t}$</td>
<td>$\tilde{\tilde{K}}_t \equiv \frac{K_t}{A_tP_t}$</td>
<td>$\tilde{c}_i^o \equiv \frac{c_i^o}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{C}_i^g \equiv \frac{C_i^g}{A_tP_t}$</td>
<td>$\tilde{B}_t \equiv \frac{B_t}{A_tP_t}$</td>
<td>$\tilde{a}_t \equiv \frac{a_t}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{H}_o \equiv \frac{H_o}{A_tP_t}$</td>
<td>$\tilde{G}_t \equiv \frac{G_t}{A_tP_t}$</td>
<td>$\tilde{h}_o \equiv \frac{h_o}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{H}_r \equiv \frac{H_r}{A_tP_t}$</td>
<td>$\tilde{T}_t \equiv \frac{T_t}{A_tP_t}$</td>
<td>$\tilde{i}_t \equiv \frac{i_t}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{D}_t \equiv \frac{D_t}{A_tP_t}$</td>
<td>$\tilde{N}_t \equiv \frac{N_t}{P_t}$</td>
<td>$\tilde{T}_t \equiv \frac{T_t}{A_tP_t}$</td>
</tr>
<tr>
<td>$\tilde{H}_l \equiv \frac{H_l}{A_tP_t}$</td>
<td>$\tilde{S}_t \equiv \frac{S_t}{A_tP_t}$</td>
<td>$\tilde{tr}_s \equiv \frac{tr_s}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{T}_t \equiv \frac{T_t}{A_tP_t}$</td>
<td>$\tilde{\tilde{T}}_t \equiv \frac{T_t}{A_tP_t}$</td>
<td>$\tilde{ss}_t \equiv \frac{ss_t}{A_t}$</td>
</tr>
<tr>
<td>$\tilde{N}_t \equiv \frac{N_t}{P_t}$</td>
<td>$\tilde{\tilde{T}}_t \equiv \frac{T_t}{A_tP_t}$</td>
<td>$\tilde{\tilde{T}}_t \equiv \frac{T_t}{A_tP_t}$</td>
</tr>
<tr>
<td>$\tilde{\tilde{N}}_t \equiv \frac{N_t}{P_t}$</td>
<td>$\tilde{\tilde{N}}_t \equiv \frac{N_t}{P_t}$</td>
<td>$\tilde{\tilde{T}}_t \equiv \frac{T_t}{A_tP_t}$</td>
</tr>
</tbody>
</table>

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