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One Lab, Two Firms, Many Possibilities: on R&D outsourcing in the biopharmaceutical industry*

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Abstract

We draw from documented characteristics of the biopharmaceutical industry to construct a model where two firms can choose to outsource R&D to an external unit, and/or engage in internal R&D, before competing in a final market. We investigate the distribution of profits among market participants, and the incentives to coordinate outsourcing activities or to integrate R&D and production. Consistent with the empirical evidence, we find that the sign and magnitude of an aggregate measure of direct (inter-firm) and indirect (through the external unit) technological externalities drives the distribution of industry profits, with higher returns to the external unit when involved in development (clinical trials) than in early-stage research (drug discovery). In the latter case, the delinkage of investment incentives from industry value, together with the ability of firms to transfer risks to the external unit, imply a vulnerability of early-stage investors' returns to negative shocks, and the likely abandonment of projects with economic and medical value. We also find that competition in the equity market makes a buyout by one of the two firms more profitable to a research biotech than to a clinical services unit, and can stimulate early-stage investments. However, this long-term incentive can be minimal, notably if the superior efficiency of outsourced operations originates from economies of scope that can hardly be exploited when a firm takes control of the external unit exclusively for itself. R&D outsourcing thus does not always qualify as a relevant pathway to address the declining productivity in innovation that has characterized the industry over several decades.

JEL classification: L13; L65; O31.

Keywords: research; development; biotechnology; pharmaceuticals; externalities.

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1 Introduction

A decline in R&D (research and development) productivity has been observed in the biopharmaceutical industry over several decades (Munos, 2009; Pammolli et al., 2011). While the number of new molecular entities and biologics that are approved annually by the US Food and Drug Administration (FDA) has remained around the same level since 1950, when measured per billion US dollars spent on R&D this number has halved roughly every 9 years (Scannell et al., 2012). The scale of the productivity problem can be gauged by considering changes in the average full cost estimate of bringing a new compound to the market. This estimate is \$451 million in DiMasi et al. (1991), \$1,031 million in DiMasi et al. (2003), and \$2,558 million in DiMasi et al. (2016).¹

There is also evidence that pharmaceutical companies that engage in internal R&D increasingly outsource specific tasks: “The global drug discovery outsourcing market was USD 14.9 billion (2014) and is expected to reach USD 25 billion by 2018, while the market for CRO [contract research organization]-conducted clinical trials was USD 23.1 billion (2014) and is expected to increase to USD 35.8 billion by 2020 ”(Schuhmacher et al., 2016, p. 8). It is believed in the industry that R&D outsourcing can reduce costs by increasing efficiency in the discovery and testing steps toward new medicines (e.g., Taylor et al., 2016; Sancheti et al., 2018). On the demand side of the R&D market, the tasks that pharmaceutical companies choose to contract out cover a large range of activities, including target validation, genetic engineering, chemical synthesis, compound screening, lead compounds evaluation, preclinical studies, and clinical (in-human) trials. On the supply side, science-based biotech firms specialize in early-stage research activities for the discovery of new chemical or biological molecules, while CROs deliver later-stage development services for the safety and efficacy assessment of drug or vaccine candidates.

Despite the observed decline in R&D productivity, as gross margins in medication markets have evolved in parallel with R&D spending, the net profit returns in the biopharmaceutical industry have remained persistently high at the aggregated level since the early 1960s (Scherer, 2001, 2010). However, the average profitability of biotech units that specialize in the discovery of new treatments

¹Here we refer to studies based on the same methodology to estimate costs, which include out-of-pocket R&D costs and time cost (i.e., cost of capital). The estimates in DiMasi et al. (1991, 2003) have been updated to US\$ 2011 prices in Mestre-Ferrandiz et al. (2012), and the one in DiMasi et al. (2016) is in 2013 prices. The three estimates are based on compound-level data, with initial human testing that occurred during the periods 1970-1982, 1983-1994, and 1995-2007, respectively.

or preventives has remained low since the emergence of genetic engineering in the 1970s (Pisano, 2006a, 2010). Biotech firms also face greater financial risk and are more sensitive to policy shocks that affect expected future profitability than the average large pharmaceutical company (Golec and Vernon, 2009). A recent empirical analysis of a comprehensive sample of 1,066 companies in the period 1930-2015 confirms these observations by disaggregating the financial performance across the pharmaceutical and biotech subsectors: “[o]ur empirical results show that investments in the pharmaceutical industry have outperformed the broader stock market over a long period of time, whereas investments in the biotech industry have underperformed the market” (Thakor et al., 2017, p. 1154), and the performance differential appears especially pronounced after 2001. Moreover, by decomposing the risk of the pharma and biotech portfolios into factors arising from general economic conditions (systematic risk) and factors that are unique to the individual company or project (idiosyncratic risk), it is found that the majority of the total risk for the pharmaceutical subsector is of the systematic type while, in contrast, “the biotech portfolio has both systematic risk and idiosyncratic risk, with a much higher idiosyncratic risk than in the pharma portfolio” (p. 1153). Moreover, the systematic risk in biotech firms is as large as – and in some periods can even be substantially higher than – that of the pharma companies. The latter empirical analysis does not include the subsector of CROs involved in the clinical assessment of drug or vaccine candidates. For these organizations, business information abounds that describes more favourable financial conditions, such as “high visibility of revenues, excess cash generation, strong balance sheets and limited exposure to a number of risks that commonly affect biopharma companies ...” (Bali et al., 2013, p. 3). As a consequence, unlike biotech firms, “CROs have historically traded at a 21% premium to the S&P 500 over the past 14 years” (Wilson et al., 2016, p. 41).

How does the distribution of industry profits among pharma companies, biotech firms, and CROs, relate to the functioning of the R&D market? Can technological characteristics of contracted-out operations explain the low average profitability of biotech units, and the higher financial returns of CROs? Are the risks inherent to discovery and clinical development activities mitigated by outsourcing contracts? What are the consequences for early-stage investment incentives? In order to answer these questions, we draw on documented characteristics of the biopharmaceutical industry to construct a model in which a for-profit upstream external unit (e.g., a biotech startup, or a contract research organization) conducts specific R&D tasks as solicited non-cooperatively by two downstream firms (big pharma), which also run R&D operations internally before competing in a final market.

The external unit interacts with the two firms by responding to their contract offers, and can choose to serve both firms, only one, or none. The firms can substitute internal resources for some or all of the external unit's operations, and their contract offers reflect multi-stage strategic interactions in the intermediate R&D market and in the final product market. Overall, the formal analysis leads to new insights on the functioning of R&D outsourcing and its implications for biopharmaceutical firms and their external partners, with strong and intelligible connections to the recent empirical evidence on the relation between contracted-out and in-house technological activities, on the nature of knowledge externalities in discovery and (distinctively) clinical development, and on merger activity in the equity market.

More specifically, our main results establish simple conditions on the model primitives for the total equilibrium R&D benefits to be either fully appropriated by the two firms, or partially retained by the external unit. These conditions, which can explain the persistently low average profitability of biotech firms, relate to indirect and direct technological externalities. There are *indirect* technological externalities if the cost of R&D, as conducted by the external unit for the two firms, reflects economies or diseconomies of scope. There are *direct* technological externalities if some of the knowledge received or produced by a firm impacts the gross profit of its competitor. We connect the sign and magnitude of these externalities with the distribution of profits among participants in the intermediate market for R&D.

Situations of positive indirect (through the external unit) and direct (inter-firm) externalities correspond mainly to early-stage discovery activities, in which biotech units are typically involved, and where economies of scope across research projects and significant inter-firm knowledge spillovers have been evidenced in the empirical literature (Henderson and Cockburn, 1996).² In the theoretical context of our model, we find that the external unit exactly breaks even, and hence investors have no positive incentive to engage financial resources, precisely in circumstances where outsourcing the tasks of the most fundamental nature can reduce the costs of discovering new medicines. We also demonstrate that downstream firms can use *risk-proof* contract offers in order to transfer – at least partly – the burden of unfavorable realizations of uncertainty to the external unit, via adjusted payments. With an expected payoff at the upstream stage equal to zero, an unfavorable realization of uncertainty then implies a negative return, and thus possibly leads the external unit to shut down,

²In a survey, Hernandez-Villafuerte et al. (2017) observe that, although the evidence is mixed, in biomedical and health research the literature more often points to the existence of positive economies of scope than diseconomies.

although its activities generate a positive – and possibly very high – industry profit. This (intermediate) market failure outcome suggests that protection measures for the external unit (e.g., a lower bound to milestone payments in case of adverse events) can be necessary to avoid the abandonment of socially valuable research projects.

However, in our model, when an aggregate measure of technological externalities is negative, the external unit can appropriate a positive share of total profits that can be derived analytically. In that case the downstream firms earn only their marginal contribution to the industry value, and the payoff to the external unit depends on the magnitude of externalities. This situation is consistent with the empirical studies that identify diseconomies of scope and nonexistent spillovers in the late-phase clinical trials of candidate drugs (Danzon et al. 2005; Macher and Boerner, 2006), such as conducted by specialized CROs. Then the positive profit to the external unit is an effect of competition between the contract offers of the two firms for the orientation of R&D resources toward specific needs. The intensity of that competition depends on the nature of R&D activities – as conducted by the external unit and by the two firms – and then on the effect of these activities on downstream cost and demand characteristics, which in the end also impact final market interactions.

We also connect the technological conditions that drive the distribution of R&D benefits to the firms' incentives to participate in the equity market, where big pharma companies acquire specialized innovative units involved in promising research or clinical development programs. For example, in the oncology domain, AbbVie agreed to buy Pharmacyclics for \$21 billion in 2015, and Pfizer acquired Medivation for \$14 billion in 2016. Such acquisitions, which substitute for contractual outsourcing relations, are viewed by industry leaders as another response to the declining R&D productivity problem (Comanor and Scherer, 2013). Still the high transaction prices observed in the equity market suggest that pharmaceutical firms pay more for R&D by acquiring an external unit than by contracting with it as a partner, or by carrying out the R&D internally (Pisano, 2015). Acquisitions usually conclude a bidding contest where several big pharma rivals compete for the same buyout target,³ leading to equity valuations often considered excessive by industry analysts and experts.⁴

³For example, “[f]or several days, Johnson & Johnson was considered the most likely acquirer of Pharmacyclics ... But AbbVie stepped in with a higher bid ...” (www.nytimes.com, March 5, 2015). In the same vein, “AstraZeneca Plc and Pfizer Inc. are among firms considering a counteroffer for Medivation Inc., challenging Sanofi’s \$9.3 billion bid for the company ...” (www.bloomberg.com, April 29, 2016).

⁴To illustrate, “AbbVie shares were down 3% in Thursday trading, as some investors and analysts expressed concern the company was overpaying for Pharmacyclics ...” (www.wsj.com, May 5, 2015); and “GlaxoSmithKline CEO Andrew Witty questioned the ... valuations of recent deals” ... and stated that “[s]ome of these valuations look stretched.” (www.firstwordpharma.com, May 11, 2015).

Two categories of cases are identified that depend on the ability of firms to bid or not for the external unit, in relation to financial, managerial, or governance constraints of all kinds. If such constraints are binding, either positive technological externalities dominate and the firms remain independent, or negative externalities lead the firms to choose to coordinate horizontally their R&D outsourcing (as in Majewski, 2004). Otherwise, should the firms be unable to commit to *not* unilaterally considering vertical integration, one of them does acquire the external unit. Whether one or the other firm is the acquirer occurs with equiprobability, independently of firm asymmetries. The main outcome is that the competition for the control of the external unit leads to overbidding (an issue discussed in Higgins and Rodriguez, 2006), although the premium can be nil in the case of negative externalities (diseconomies of scope and inexistant inter-firm spillovers), as characteristic of late-stage development tasks. We thus obtain that biotech founders engaged in early-stage research – more than owners of contract research organizations – may reappropriate in the equity market part of the value transferred to their sponsors in the R&D market.

The paper is organized as follows. Characteristics of the biopharmaceutical industry, in relation to our analysis, are presented in Section 2. The theoretical and empirical literature is reviewed in Section 3. The model specifications are introduced in Section 4. The distribution of industry profits is characterized in Section 5, and incentives to shift to a more integrated structure are investigated in Section 6. Final remarks are in Section 7. All proofs are relegated to the Appendix.

2 The Industry Context

We derive our theoretical results from model specifications that are carefully related to documented characteristics of the biopharmaceutical “market for technology” (Arora et al., 2001, 2004a), where the industry usually divides research and development activities into two sets. The early-stage research (“R”) consists of the discovery of new chemical compounds, vaccine candidates, or other biologics. The later-stage development (“D”) tasks aim at assessing the safety and efficacy of the therapeutic or prophylactic properties of a candidate medicine on increasingly large populations of individuals.

Outsourced R&D activities include early-stage research in the biotechnology field, where from the early years onward, “[b]ecause different commercial products were based on similar basic technologies, the costs ... could be shared by clients” (Pisano, 1991, p. 241) and then “[v]irtually every

new entrant ... formed at least one, and usually several, contractual relationships with established pharmaceutical ... companies” (Pisano, 2006a, p. 87).⁵ A historical example involves the pioneering biotech firm Genentech, which started collaborations with Ely Lilly in 1978 for the synthesis of human insulin, and with Hoffman-LaRoche the same year for the synthesis of interferons. A more recent example involves CureVac, which contracted with Crucell (a Johnson & Johnson company) in 2013, and with Sanofi Pasteur in 2014, for the funding of R&D operations toward prophylactic vaccines. Another recent example involves Moderna Therapeutics, which partnered with AstraZeneca in 2016, and with Merck a few months later, for the co-discovery and development of RNA-based candidates for the treatment or prevention of a range of cancers. In our model, accordingly, an external unit can serve up to two client firms simultaneously.⁶

Another important characteristic of the current market for biotechnology is that established pharmaceutical firms do not only give a biotech firm (external unit) access to finance and to manufacturing or marketing resources, they also operate internal biotechnology functions. The situation was different when the biotechnology market emerged in the late 1970s. At that time there was a clear dichotomy in the R&D focus of suppliers and buyers. On the supply side, a typical new biotech firm used advances in biological sciences – e.g., recombinant DNA technology – for the design of a therapeutic agent. On the demand side, the established pharmaceutical firms, whose technological competence focused on the random screening of compounds against disease targets, procured research in the market for biotechnology before engaging in clinical development. Since then, the largest pharmaceutical firms have acquired capabilities in cell and molecular biology (Galambos and Sturchio, 1998; Rydzewski, 2008), so that the dichotomy has eroded: “[e]stablished firms have embraced biological approaches, including genomics, to drug discovery, while ‘biotech firms’ employ chemistry” (Pisano, 2006a; p. 17).

Outsourced R&D also relates to late-stage development activities. Once a new compound, or a candidate vaccine, has been discovered, and tested in animal models, it must go through clinical trials conducted on human subjects. These trials need to produce evidence of safety and efficacy, as required for regulatory approval by government agencies (e.g., the FDA) before market introduction.

⁵According to Higgins (2007), who uses a large data set of alliances in the biopharmaceutical industry, from 1994 to 2001 each biotechnology firm had on average six alliance partnerships with large pharmaceutical firms.

⁶Although the biotech and CRO industries are highly fragmented (see Argyres and Liebeskind, 2002, and Getz, 2007, respectively), the specification that only one external unit faces two client firms is consistent with the observation that several big pharma companies usually compete for a differentiated technology or expertise as specifically supplied by a given entity among several others (a case of monopolistic competition).

There are three phases that involve increasingly large samples of subjects (from a few dozen in phase 1 to, in case of success, several hundred in phase 2, and then to several thousand subjects in phase 3). As in the case of biotechs, a CRO that supplies clinical trial services can enter in simultaneous contractual relationships with several clients. For example, Parexel entered in 2011 into multi-year contractual agreements with both Merck and Pfizer. The contracting firms do not restrict their strategies to either make or buy clinical trial services as “[f]or a given study, sponsors can choose to retain some functions in house while contracting out others” (Azoulay, 2004; p. 1594). By outsourcing the latter tasks the firms attempt to benefit from economies of scale and scope (Macher and Boerner, 2006), and thereby to reduce their clinical trial costs, which are estimated at around US\$220 million for a new drug (Mestre-Ferrandiz, Sussex, and Towse, 2012).⁷

In our model, the respective efforts of the external unit and its client firms are endogenous, so that the vertical division of R&D activities can occur at any point between total outsourcing and full integration. This specification is consistent with the observation that the collaboration of big pharma firms with biotech units or clinical trial providers creates joint inputs across the two sides of the contractual relationship, with an exact balance that might vary significantly on a case by case basis.

The large pharmaceutical firms on the demand side of the intermediate market for technology are likely to design the contracts that organize the relationship with an external supplier of discovery or clinical trial services. This is explained by the fact that, when internal resources are available, the capacity of established pharmaceutical firms to “go for it alone” – though possibly at a higher cost – increases their bargaining power (Arora et al., 2004b). Other factors include the severe financial constraints faced by specialized biotech units (Lerner and Merges, 1998; Golec and Vernon, 2009), together with a high rate of entry on the fragmented supply side (Rothaermel, 2001; Argyres and Liebeskind, 2002) while incumbents on the demand side remain highly concentrated. Although the latter structural features describe a “buyer’s market”, we show that they cannot fully explain the persistently low average profitability of biotech firms since the late 1970s (Pisano, 2006a, 2010). Indeed, in the analysis that follows we identify circumstances where the external unit appropriates the total industry profit, for any probability of success, with client firms that behave as principals and are no less informed than the common independent contractor.

⁷The out-of-pocket cost of clinical testing depends on the number of patients required to collect sufficient data as demanded from regulatory agencies. It is even higher in the case of preventive vaccine candidates, as the size of human subject test samples is often larger than for drugs (Scherer, 2011; Keith et al., 2013).

R&D contracts can incorporate complex clauses to fine tune the financial mechanism (equity participation, milestone payments, licensing fees, royalties, ...) ⁸ with the technology or services supplied (or not) by the external unit to other client firms. Non-compete clauses delineate the know-how or expertise that the external unit may or may not use with or provide to a third party, except as expressly notified. ⁹ For example, in an early-stage agreement between the pharma company Glaxo and the Canadian research unit BioChem, the latter “shall have the right to contract with third parties for the performance of work, or the provision of consulting services, in connection with the sponsored research program, provided that Glaxo shall have the opportunity to review, comment on and approve any such proposed contract prior to its execution”(p. 9). ¹⁰ Other clauses modulate the payments received by the external unit from the pharma sponsor in connection to the technology that can be supplied to a competitor. To illustrate, a research, development, and license agreement between the pharma company Bristol-Myers Squibb (BMS) and the biotech Ligand Pharmaceuticals (Ligand) stipulates that “[i]n the event that ... Ligand or a Ligand Affiliate, or a Third Party with whom Ligand had collaborated with respect to the development of a Competing Product ... sell such Competing Product in any country in the Territory in which BMS ... is then marketing a Product, ... then ... all royalty rates payable by BMS in each such country shall be reduced by *** during the period that both such products are marketed in such country”(pp. 27-28). ¹¹ Accordingly, in our model each firm can condition its payment on the verifiable operations conducted inside the external unit, including those that relate to a third party. ¹² This assumption does not mean that a technology received from the external unit cannot partly benefit a competitor. Unsolicited and non-contractible knowledge spillovers, both through the external unit and across firms, are introduced in the analysis. ¹³

⁸In practice, biotech firms typically receive an upfront fee, milestone payments conditioned on the occurrence of a pre-determined event, and sales-based royalties if their intellectual property is in-licensed by the downstream partner, while CROs usually receive a negotiated fee for development services.

⁹Non-compete clauses typically include a “right of first refusal” (Folta, 1998; Hagedoorn and Heslen, 2007) that allows a firm to purchase the rights – or only a selection – to R&D outcomes before such an option is offered to other firms.

¹⁰The features of this contractual agreement, dated Jan. 1990, are discussed in Robinson and Stuart (2000).

¹¹The contract, dated January 1st 1990, is available at: <http://contracts.onecle.com/alpha>, where the signs *** refer to undisclosed confidential information.

¹²The common agency model in Section 4 is thus of the *public* kind (Martimort, 2007). This specification, in line with the stylized facts presented in section 2, differs from most papers that focus on consumer goods markets where less sophisticated non-compete clauses, hardly verifiable activities, and various antitrust regulations can justify the assumption that a principal can contract exclusively on what it specifically receives from the agent, with no possible connection between payments and the other activities of the agent that benefit a competitor (e.g., Bernheim and Whinston, 1998).

¹³In Cohen et al. (2000) survey data show that firms in the pharmaceutical domain rely more on patents as a protection mechanism than in any other industries. Patenting is an important source of technological spillovers, as it “involves a leakage of a certain portion of the knowledge to the public in the process of filing a patent application”(Bhattacharya and Guriev, 2006, p. 1114).

Circumstances have been studied in the economics literature where a research unit can (re)sell secretly its technology, and is more knowledgeable than its downstream clients.¹⁴ In the biopharmaceutical context, secret reselling is unlikely when biotech firms and clinical trial suppliers alike enhance their reputation by communicating on their contractual partners and on the content of agreements.¹⁵ It can also be the case that pharma firms with internal R&D operations are more informed on the technological potential of a research program than an external unit engaged in the “least intimate” form of fee-for-service agreement (Pisano, 2006a, p. 108), for example to perform systematic tests on a compounds library, or than a CRO involved in the most “routinized part” (Shuchman, 2007, p. 1367) of clinical trials services. So in our theoretical framework the two firms are not less competent than the external unit, and are not threatened by some form of misbehavior. Our model specifications are rather motivated by the observation that, in science-based businesses, “[p]rofound and persistent uncertainty, rooted in the limited knowledge of human biological systems and processes, makes drug R&D highly risky” (Pisano, 2006b; p. 119) to *all* undertakings. We thus focus on situations of “symmetric uncertainties” (Arora and Gambardella, 2010, p. 788), where all parties have the same information on the distribution of a technological parameter, with the state of nature being unknown at the contracting stage.

3 The Related Literature

3.1 The Theory

Our analysis relates to theoretical contributions that adopt a general approach, with no specific reference to the biopharmaceutical domain, as in the paper by Aghion and Tirole (1994) who compare the relative efficiency of separating or integrating an external research unit and a firm. In their model the two entities have fully distinct roles, with an exclusive division of R and (separately) D tasks. This setting describes complementary activities, since only the external unit can produce an innovation, and only the firm can develop it into a marketable product.¹⁶ A contract specifies *ex ante* whether

¹⁴For example, in Bhattacharya and Guriev (2006) an external unit can sell its technology to one of two client firms, then secretly to a competitor. In Bhattacharya and Guriev (2013) the external unit also chooses a non-verifiable research effort that conditions the value of the technology needed for downstream firms to innovate.

¹⁵Moreover, “the identities of partners and descriptions of alliances figure prominently in biotechnology companies’ securities registration statements” when an initial public offering is in preparation (Stuart et al., 1999, p. 327).

¹⁶In the terminology of Mowery (1983), complementarity here can be seen as “structural”, in that in-house and external R&D operations are not substitutable by assumption.

R and D tasks will occur under separation or integration, the license fee received by the research unit, and the firm's investment level. It is found that separation – a case of research outsourcing – is more efficient (i.e., joint expected value is maximized) than integration when the marginal efficiency of the research unit's effort is large enough relative to the one of the firm's investment. However, if the firm writes the contract, and the external unit is financially constrained, then integration can be inefficiently retained in equilibrium, with no value earned by the external unit.

In Anton and Yao (1994) the value of the new technology does not depend on the level of either R (upstream) or D (downstream), so the focus is on profit distribution, not on efficiency. There are two possible client firms, approached sequentially by the external research unit, and which can proceed to the development stage before competing in a final market. Because there is no patent protection, if the external unit discloses its discovery to one of the two firms, then that firm can imitate it at no cost and appropriate all innovation benefits. However, a firm can choose not to imitate but instead pay for the technology to incentivize the external unit not to contract subsequently with the other firm. The main result is that provided the external unit's *ex ante* wealth is sufficiently limited, it can appropriate a share of the value of its discovery by first disclosing it to one of the two firms to get a contract offer from that informed client, without transferring any knowledge to the other firm.

In our formal setting, both the value generated by technological operations and its distribution among players are endogenous. As in Aghion and Tirole (1994), a firm can outsource research efforts to an external unit and simultaneously invest in internal development operations, although it can also possibly rely exclusively on internal resources, in which case all R&D activities are conducted downstream. As in Anton and Yao (1994), the external unit can supply new technology to two client firms that can benefit from (or be penalized by) knowledge externalities, although in our model the two firms interact simultaneously in the market for technology.

Bhattacharya and Guriev (2006, 2013) combine some of the specifications of the seminal models by Aghion and Tirole (1994) and Anton and Yao (1994). Again the output of the external research unit is needed for innovation, along with the endogenous development efforts chosen non-cooperatively by two client firms, who then compete in the final market. The external unit can decide to sell its technology to one of the two firms, then secretly to the competitor. Although selling twice means additional revenue, it also reduces the *ex-post* final-market value to the first firm, and thereby induces a lower payment from the latter to the research unit. Bhattacharya and Guriev (2006) concentrate on

the development choices of client firms (the R part of R&D is not considered). For a given level of the external unit's output, the parties can opt for two alternative licensing modes. In the "open" mode, a patent describes the new technology, that the external unit can then license to one of the two firms exclusively in exchange for a lump sum transfer, with some knowledge that leaks to the competitor. In the "closed" mode, the external unit discloses the non-patented technology to one of the firms in exchange for a share of final-market revenues, which must be sufficiently high for the external unit not to resell secretly. The latter mode occurs more frequently, with no reselling to the competitor, if the external unit's output level is high and the technological leakage with patenting is substantial. In Bhattacharya and Guriev (2013) the external unit chooses *ex ante* a non-verifiable research effort that conditions the value of its technological output (the R part of R&D is thus reintroduced, with no possible reallocation of the two types of activities). Then integration with one of the firms, plus closed governance (no patenting, exclusive transfer to the acquirer, sharing of *ex-post* revenues), can result in a higher *ex ante* effort than separation.

Although we depart from the assumption that technology reselling is secret and not verifiable, we share with Bhattacharya and Guriev (2006, 2013) the specification that industry efficiency depends on endogenous choices by the external unit and/or two firms that also interact in a final market.

In another set of papers, R and D operations are not considered separately, but are viewed as a single activity that is fully performed either by an external unit or, exclusively so, internally by a firm, so the external and internal R&D activities are substitutable.

Both Lai, Riezman, and Wang (2009) and Ho (2009) assumed that a single client firm (a principal) offers a contract to the external unit (an agent), although some technological information can be leaked subsequently to a competitor, a decision that cannot be verified by a Court. In Lai, Riezman, and Wang (2009) the firm chooses a lump-sum amount plus a revenue percentage to be paid in exchange for a specific cost-reducing technology. In the process some information on the firm's operating environment is learnt by the external unit, which can then decide to leak that knowledge in secret to the firm's competitor. When writing the contract, the firm trades-off between the benefit of the external unit's superior R&D efficiency and the revenue loss caused by the leakage. For some parameter values, the firm finds it profitable to externalize R&D with a lump-sum contract even though this allows the leakage to occur.

In Ho (2009) the external unit can supply a cost-reducing technology with some non-zero prob-

ability by incurring a fixed cost. The outsourcing firm commits contractually to transfer a payment that is a function of the reported success of the R&D process. Both the external unit's decision to invest and the result of its R&D effort (success/failure) are private information. After the external unit accepts the contract and incurs the fixed cost, if successful then it can secretly offer the technology to an *ex ante* symmetric final-market competitor of the principal, possibly for a higher total revenue, before reporting the failure to the outsourcing firm. As a main result, any contract that incentivizes the external unit not to leak the technology necessarily results in a lower net profit to the principal than the status quo (no outsourcing).

R&D operations are also formalized as a single activity in Vencatachellum and Versaavel (2009), but the model departs from the possible secret recontracting assumption, and the two firms simultaneously offer competing contracts to the external unit for the delivery of specific technological services (a common agency situation). An observable "active" leakage occurs when the contracts incentivize the external unit to serve both firms, together with a "passive" (unsolicited) leakage captured by an inter-firm spillover parameter. With positive economies of scope, but limited spillovers, the two firms receive R&D and earn higher equilibrium profits than by relying on internal resources.

In Spulber (2013), a set of competing external inventors engage in uncertain R&D projects for a new production technology (a unit cost of production drawn independently of other inventors from a given distribution). They compete in the market for technology to sell their invention to a set of firms, which compete in a final market. After the R&D takes place upstream, the firms observe the inventions together with their respective inventors' two-part royalty offers, and simultaneously make adoption and product pricing decisions. In equilibrium, the inventor with the most efficient process technology charges a combination of lump-sum and per-unit royalties to the firms, which all adopt the technology. It is found that competitive entry of inventors generates more R&D than a multi-project monopoly inventor, and that an increase in the number of downstream firms (without free entry) and a lower entry cost (when there is free entry) both increase entry of competing inventors. When the downstream firms vertically integrate R&D and production operations, and agree to share the best invention obtained from all projects before competing in prices in the final market, the R&D activity is suboptimal.

Allain, Henry, and Kyle (2015) adopt another approach with separated R and D periods. An external research unit, which generates new technology of uncertain value, faces a set of potential

client firms that compete in an auction for the exclusive benefit of the technology, and again possibly interact in a final market. Consistently with the biopharmaceutical context (the theoretical model is motivated by an empirical analysis with data collected in that industry), there is full patent protection, so that no secret technology transfer occurs. A development phase is needed to establish the value of the innovation. The research unit can decide either to engage in it, at a given high cost, before selling the new technology with known value, or to first sell the innovation before its value is known and let a firm proceed to the development phase, at a lower cost, so the external and internal development efforts are substitutable. When the research unit is *ex ante* more confident about the value of the innovation than the firms, it chooses to develop it on its own for a higher expected benefit if and only if its cost disadvantage is not too large. The latter situation is more likely if, following an increase in the number of firms, the positive effect on the license fee resulting from the auction (more bidders participate) dominates the negative effect on gross profits (more downstream competition).¹⁷

Our approach is complementary to the latter two recent papers. As in Spulber (2013), an appropriability problem may lead to integrate R&D and production vertically, and as in Allain et al. (2015) the vertical division of labor in R&D operations is driven by the nature of competition among client firms. A distinctive feature of our model is that the intensity of competition is a consequence of the exact effects of external and internal technological operations on cost and demand conditions, not on the number of downstream firms. We also share with Ho (2009) and Lai et al. (2009) the assumption that the downstream firms write contract offers, to which the external unit responds, and which can lead to multi-contracting. Moreover, in our model the firms condition their payments on a measure of the external unit's operations, as in Vencatachellum and Versaevel (2009). It follows that the external unit's operations are *not* conducted *before* the client firms' choice of payment schemes, consistently with contractual situations in the biopharmaceutical context. These payment schemes are the firms' instruments that determine the equilibrium distribution of industry profit among contracting parties.

¹⁷Allain et al. (2015) also construct a large dataset on exclusive licensing deals and investigate the drivers of the decision, by a research unit that has discovered a drug candidate, to proceed also to development operations. They find an inverted U-shaped relation between the number of potential licensees and the probability that a research unit engages in the later phases of clinical trials before licensing, instead of leaving the whole development process to its licensee.

3.2 The Empirical Evidence

The endogeneity of the respective efforts of the external unit and its client firms, in our model, captures the observation that the distribution of tasks between a R&D supplier and its sponsors might vary significantly on a case by case basis. Several empirical papers identify a number of factors that cause this variation.

Arora and Gambardella (1990) use data on agreements that involve large chemical and/or pharmaceutical producers. They establish that several types of linkages, including investments in the capital stock of biotech companies and joint R&D with other producers, complement each other. In a transaction costs approach, Pisano (1991) analyzes data on biotechnology projects that are either the sole responsibility of an independent partner or fully conducted internally by a pharma firm. Pisano finds that internal sourcing is more likely in the biotechnology product areas in which expertise is concentrated in fewer R&D suppliers. In an incomplete contracts perspective, Lerner and Merges (1998) use a database of agreements between biotechnology suppliers and pharmaceutical firms. They find support for the conjecture that the allocation of control rights to the R&D entity (e.g., right to manage clinical trials, to undertake process development, to terminate alliance, ...) increases with its financial resources. The latter result justifies our specification that big pharma firms, which have deeper pockets than biotech units and CROs, are those that write contracts in the intermediate market for R&D.

Our formal approach of the circumstances in which contracted-out technology either stimulates or reduces in-house operations connects also to other papers that characterize the interaction between external and internal R&D activities in the biopharmaceutical industry. In an early contribution to that literature, Arora and Gambardella (1994) use a sample of client firms in the biotech market, and find support for the hypothesis that firms need internal know-how to evaluate alternative projects and to use the technology more effectively. More recently, Belderbos, Kelchtermans and Leten (2010) use panel data on the patenting and publication activities of large pharmaceutical firms and find that the magnitude of the effect of external basic research exploitation is significantly greater if firms conduct more internal basic research. Hagedoorn and Wang (2012) also use a panel sample of incumbent pharmaceutical firms, with the innovative output (the dependent variable) measured as the number of annual biotechnology patents granted to these firms. They find that the level of internal R&D expenditure drives the interactive effect between external and internal R&D strategies. Above (below) a

threshold level of internal R&D investments, the marginal returns to internal R&D are higher (lower) when new technology is sourced externally through alliances or acquisitions, which indicates complementarity (substitutability). An ambiguous conclusion is also reached by Ceccagnoli, Higgins, and Palermo (2014), who use another panel dataset from the pharmaceutical industry to estimate the partial cross-derivative of an innovation production function (the output is the yearly stock of compounds in a firm's pipeline) with respect to external (in-licensing) and internal R&D expenditure. Their results suggest that external and internal R&D are neither complements nor substitutes, and that complementarity increases with a few drivers (e.g., prior licensing experience). Our first formal proposition, in Section 5, accords with these empirical results.

Another set of papers use data collected at the firm level and at the level of individual R&D projects in order to distinguish between economies of scale and economies of scope in the production of intellectual property. The evidence depends on the nature of technological activities. Henderson and Cockburn (1996) find economies of scope and significant knowledge spillovers in early-stage drug "discovery" tasks (those on with biotech units typically focus). Conversely, Danzon, Nicholson, and Sousa Pereira (2005), and Macher and Boerner (2006), identify diseconomies of scope and nonexistent spillovers in the late-phase clinical trials of candidate medicines (the "development" activities that are usually outsourced to specialized CROs). Our main theoretical propositions echo these contrasted empirical results, and show their relevance for explaining the distribution of industry profits between an external unit and its downstream sponsors.

A few other recent papers point to the ability of client firms, in the biopharmaceutical industry, to contractually control the behavior of external technology suppliers. Robinson and Stuart (2007) study the features of early-stage (discovery) research contractual agreements, in which large firms sponsor small biotech companies. They notably find that partners choose to contract for actions that might be costly, or even impossible, to verify. A suggested interpretation is that a client firm can obtain broader termination rights when provisions on unverifiable research decisions are included in a contract, and thus enhance the *ex ante* incentives of the external research unit to uphold the contract. Higgins (2007) analyzes R&D alliances between a firm and a biotech company. There is a milestone payment structure in 90 percent of the contracts. Because they condition further financing on clearly identified objectives, milestone payments protect the client firm from misbehavior. Lerner and Malmendier (2010) examine agreements that involve a biotech firm as an R&D provider. Termination rights are

assigned to the financing firm in 96 percent of the contracts, and can be coupled with the reversion to the same firm of all intellectual property rights as generated through the contractual relationship. Termination rights thus incentivize the subcontractor to remain focused on the objectives specified in the agreement, and our model specifications are consistent with this conclusion.¹⁸

Another set of papers focuses on the drivers or implications of mergers and acquisitions in the pharma industry. By using a sample of transactions that each involve a target biotech firm, Folta (1998) finds support for the hypothesis that contractual agreements are used to defer acquisition of a target R&D supplier and economize on the cost of committing resources to a technology with uncertain value. Our choice to study first the profit distribution in a decentralized setting, before characterizing incentives to integrate in the R&D market, is thus compatible with industry practice. Higgins and Rodriguez (2006) examine the performance of acquisitions by established pharmaceutical firms of smaller competitors and/or biotech units to understand the effect of R&D outsourcing acquisitions on an individual firm's R&D productivity. In their analysis, each acquiring firm had been involved, on average, in four contractual relationships with the target prior to the acquisition. They notably find that acquisitions supplement a firm's internal R&D efforts, and that firms with greater R&D intensity are more likely to engage in acquisitions. Danzon, Epstein, and Nicholson (2007) examine the determinants and effects of a sample of operations that include the purchase by pharmaceutical firms of an equity stake in biotech firms. They find in particular that financially strong firms are less likely to be part of an acquisition, either as a target or as an acquirer. We use these findings to comment our results in Section 6.

4 The Model

In this section we draw on the industry characteristics described above to construct a formal model. There are two related research and development (R&D) stages in an intermediate market for technology, and a final product market. Upstream, a for-profit independent unit (hereafter, "the lab") conducts R&D activities. Downstream, two firms can outsource R&D to the lab, and/or also conduct in-house R&D operations, before competing in the final market where they supply substitutable

¹⁸In a model that precedes their empirical analysis, Lerner and Malmendier (2010) show that if the R&D supplier is not financially constrained, the termination rights coupled with transfer payments can result in the same outcome as a simple complete contract.

products.

Information — The two risk-neutral firms (principals) know the strategies available to the other players and the related payoffs, while the risk-neutral lab (an agent) needs not know the downstream cost and demand conditions. Technological uncertainty is described by a parameter $\theta \in \Theta$ whose distribution is known by all parties, with the state of nature being unknown *ex-ante* (at the contracting stage, that is before the lab tests technological options) but observable and verifiable *ex-post* (so that payments can be made contingent on it and the firms are committed to their contracts).¹⁹

Profit functions — The non-negative *external* R&D levels, as chosen by the lab specifically for each firm, are described by $\mathbf{x} = (x_1, x_2)$. The *internal* R&D levels and the final-market commercial strategies, as non-cooperatively chosen by the firms, are described by $\mathbf{y} = (y_1, y_2)$ and $\mathbf{z} = (z_1, z_2)$, respectively.²⁰

The lab's net profit is

$$v_0(\mathbf{x}, \theta) = t_1(\mathbf{x}, \theta) + t_2(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta), \quad (1)$$

where f_0 is the lab's cost, and t_i is firm i 's transfer payment, both functions of \mathbf{x} and θ . As a transfer can include an upfront part, it can be rewritten as $t_i(\mathbf{x}, \theta) = \underline{t}_i + k_i(\mathbf{x}, \theta)$, where the function k_i formalizes the fine tuning of each firm's contingent transfer payment with the technology effectively supplied by the lab (after uncertainty is realized), as made possible by complex non-compete clauses and a well-functioning legal environment (see section 2).

Each firm i 's net profit is

$$v_i(\mathbf{x}, \mathbf{y}, \mathbf{z}, \theta) = g_i(x_i + y_i, x_j, y_j, \mathbf{z}, \theta) - f_i(y_i, \theta) - t_i(\mathbf{x}, \theta), \quad (2)$$

$i, j = 1, 2, j \neq i$, where f_i is the firm-specific cost of generating y_i internally, and g_i is a gross profit function. In the latter function, firm i 's external and internal R&D levels x_i and y_i are added as an argument, which formalizes the technological assumption that all R&D tasks can be *a priori* performed either externally or internally. However, the respective equilibrium values are the outcome of distinct decision processes that can result in external and internal efforts being substitutes or complements (y_i^* can be either decreasing or increasing in x_i in Proposition 1, below). The competitor's variables x_j and y_j are arguments of the same function, allowing for technological spillovers received indirectly

¹⁹R&D contracts usually include provisions for dispute resolution and point to an external private arbitrager, or to a specific Court, in case of litigation (e.g., Robinson and Stuart, 2007).

²⁰The argument \mathbf{z} can represent prices or quantities, indifferently, or refer to more elaborate competitive interactions.

through the lab and directly from the competitor. The gross profit also depends on final-market non-cooperative strategies, \mathbf{z} . (Several examples are discussed below that adapt specific algebraic forms from the R&D literature, with a focus on the effect of uncertainty in Examples 2 and 3.)

Timing — There are four stages, as follows:

(i) The two firms simultaneously and non-cooperatively choose a transfer function $t_i(\mathbf{x}, \theta) \geq 0$, $i = 1, 2$, offered to the lab as a contract.

Each contract offer thus connects a payment to the lab's chosen R&D levels for any possible state of nature, and the specification that payments are non-negative formalizes the assumption that the institutional environment allows the firms to reduce payments but not to impose penalty fees to the lab in cases of unsuccessful outcomes. More specifically, in what follows, we assume that both t_i and $k_i(\mathbf{x}, \theta)$ are non-negative.

(ii) The lab accepts either both contract offers simultaneously, or only one, or none, and chooses the firm-specific R&D levels \mathbf{x}^* that maximize its expected profit $E_\theta[v_0(\mathbf{x}, \theta)]$.

If accepted contracts include an upfront payment, the lab receives t_i from each contracting firm.

At this stage the lab refuses all contracts if they imply a lower benefit than the reservation value $v_0 = 0$, and it takes only one of the two contracts if this implies a higher benefit than accepting the two offers.²¹ Formally, for any given t_j offered by firm j , the lab accepts firm i 's contract offer only if

$$E_\theta[v_0(\mathbf{x}^*, \theta)] \geq \sup \left\{ 0, \max_{\mathbf{x}} E_\theta[t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)] \right\}, \quad (3)$$

for some $\mathbf{x}^* \geq (0, 0)$, $i, j = 1, 2$, $j \neq i$. As the firms' contract offers cannot be negative, in equilibrium (3) is always exactly satisfied.²² This however does not imply that the equilibrium R&D levels and transfer functions are symmetric, nor that payments are both positive. It can be the case that firm i offers a “null” contract, where $t_i(\mathbf{x}, \theta) = 0$, all (\mathbf{x}, θ) , and still receives technology, if for example limiting inter-firm technological spillovers is prohibitively costly for the lab.

²¹ As the lab (an agent) can choose to accept only a subset of contracts offered by the two firms (principals), this is a “delegated common agency” model in the terminology introduced by Bernheim and Whinston (1986a).

²² Should in equilibrium the for-profit lab contract exclusively with, say, firm 1, to deliver $\tilde{\mathbf{x}} \in \arg \max_{\mathbf{x}} E_\theta[t_1(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$, for any non-negative contract offer t_2 the lab would earn in expectation $E_\theta[t_1(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] < E_\theta[t_1(\tilde{\mathbf{x}}, \theta) + t_2(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]$, a contradiction, so (3) is always satisfied. Moreover, should the lab supply $\hat{\mathbf{x}}$ to earn the expected payoff $E_\theta[t_1(\hat{\mathbf{x}}, \theta) + t_2(\hat{\mathbf{x}}, \theta) - f_0(\hat{\mathbf{x}}, \theta)] > E_\theta[t_1(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]$, then firm 2 would find it profitable to adapt its contract offer to t'_2 verifying $E_\theta[t'_2(\hat{\mathbf{x}}, \theta)] = E_\theta[t_2(\hat{\mathbf{x}}, \theta)] - \varphi$, where $\varphi = E_\theta[(t_1(\hat{\mathbf{x}}, \theta) + t_2(\hat{\mathbf{x}}, \theta) - f_0(\hat{\mathbf{x}}, \theta)) - (t_1(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta))]$, and hence (3) holds with equality.

(iii) Given the accepted contracts, and on the basis of their expected returns, the firms simultaneously and non-cooperatively choose their own internal R&D level $y_i \geq 0$.

Uncertainty realizes and the state of nature is revealed to all parties.

(iv) Given the realized state of nature, and the outcome of *ex-ante* chosen R&D levels, the firms simultaneously and non-cooperatively choose their final-market commercial strategy $z_i(\theta) \geq 0$.

The firms transfer their respective contingent payments $k_i(\mathbf{x}, \theta) = t_i(\mathbf{x}, \theta) - \underline{t}_i$ to the lab.

The net profits to the lab and to each firm, after contingent payments have been transferred, are derived from the following equilibrium concept.

Equilibrium concept — For any (\mathbf{x}, \mathbf{y}) and any realization of θ , henceforth we assume that (i) there exists a unique final-market Nash equilibrium $\mathbf{z}^*(\mathbf{x}, \mathbf{y}, \theta)$, and (ii) for any \mathbf{x} , and given the distribution of θ , there exists a unique internal-R&D stage Nash equilibrium $\mathbf{y}^*(\mathbf{x})$, so that we may introduce

$$\tilde{g}_i(\mathbf{x}, \theta) = g_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x}), \mathbf{z}^*(\mathbf{x}, \mathbf{y}^*(\mathbf{x}), \theta), \theta) - f_i(y_i^*(\mathbf{x}), \theta),$$

that is firm i 's concentrated profit net of internal R&D costs. Finally, for any given $\mathbf{t} = (t_1, t_2)$, and again given the distribution of θ , we denote by $X(\mathbf{t})$ the set of R&D choices that maximize the lab's profits in expectation, that is $X(\mathbf{t}) = \arg \max_{\mathbf{x}} E_{\theta} [v_0(\mathbf{x}, \theta)]$.

The following definitions are needed before introducing the solution concept:

(1) for any $\mathbf{x} \in X(t_i, t_j)$ and $\mathbf{x}' \in X(t'_i, t_j)$, firm i 's transfer function t_i is a *best response* to the other firm's t_j if $E_{\theta}[\tilde{g}_i(\mathbf{x}, \theta) - t_i(\mathbf{x}, \theta)] \geq E_{\theta}[\tilde{g}_i(\mathbf{x}', \theta) - t'_i(\mathbf{x}', \theta)]$, all t'_i ;

(2) the transfer function t_i is *truthful* relative to firm i 's payoff with \mathbf{x}^0 if $t_i(\mathbf{x}, \theta) = \sup\{0, \tilde{g}_i(\mathbf{x}, \theta) - [\tilde{g}_i(\mathbf{x}^0, \theta) - t_i(\mathbf{x}^0, \theta)]\}$.²³

The solution concept is the truthful subgame-perfect Nash equilibrium (TSPNE). The four-tuple $(\tilde{\mathbf{t}}, \tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}})$ is a TSPNE if, for $i, j = 1, 2, j \neq i$: (i) $\tilde{\mathbf{z}} = \mathbf{z}^*(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \theta)$; (ii) $\tilde{\mathbf{y}} = \mathbf{y}^*(\tilde{\mathbf{x}})$; (iii) $\tilde{\mathbf{x}} \in X(\tilde{\mathbf{t}})$; (iv) \tilde{t}_i is a best response to \tilde{t}_j ; and (v) \tilde{t}_i is truthful relative to firm i 's payoff with $\tilde{\mathbf{x}}$. It follows that $\tilde{t}_i(\mathbf{x}, \theta) = \sup\{0, \tilde{g}_i(\mathbf{x}, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)\}$, where $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) = [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)]$ is firm i 's equilibrium payoff as a function of the realization of θ .

²³When the gross profit $\tilde{g}_i(\mathbf{x}, \theta)$ exceeds the firm's expected net profit at \mathbf{x}^0 , that is $\tilde{g}_i(\mathbf{x}^0, \theta) - t_i(\mathbf{x}^0, \theta)$, the difference between $t_i(\mathbf{x}, \theta)$ and $t_i(\mathbf{x}^0, \theta)$ is equal to the difference between $\tilde{g}_i(\mathbf{x}, \theta)$ and $\tilde{g}_i(\mathbf{x}^0, \theta)$; otherwise the transfer $t_i(\mathbf{x}, \theta)$ is set equal to zero. For each θ , on its positive part a truthful contract offer thus exactly reflects firm i 's valuation of \mathbf{x} relative to the value for \mathbf{x}^0 .

Truthfulness is a standard refinement in delegated common agency games, and two properties in the theoretical literature offer a strong justification for using it (Bernheim and Whinston, 1986b; Laussel and Le Breton, 2001; Martimort, 2007). A first property is that, for any set of transfer offers by any of the two firms, there exists a truthful strategy in the other firm's best-response correspondence. A firm can thus restrict itself to truthful strategies at no cost. A second property is that, when firms can communicate with each other, all truthful Nash equilibria are coalition-proof. Therefore, the two firms' joint net profits in a TSPNE are not lower than in any other subgame-perfect Nash equilibrium.²⁴ The proofs of several propositions in Section 5 present the technical challenge of extending fundamental results of this common agency literature to a context where firms not only interact as principals in the intermediate market for external R&D, but also compete in internal technological decisions and in final-market commercial strategies.²⁵

Technological assumptions — The results in the next sections refer to properties of the lab's and the two firms' expected costs $\hat{f}_0(\mathbf{x}) = E_\theta[f_0(\mathbf{x}, \theta)]$ and $\hat{f}_i(y_i) = E_\theta[f_i(y_i, \theta)]$, $i = 1, 2$, which are (weakly) increasing in their respective arguments, and to the firms' expected gross profit²⁶ $\hat{g}_i(x_i + y_i, x_j, y_j) = E_\theta[g_i(x_i + y_i, x_j, y_j, \mathbf{z}^*(\mathbf{x}, \mathbf{y}, \theta), \theta)]$, $i, j = 1, 2, j \neq i$. The latter expression is (weakly) increasing in the firm's own R&D levels received from the lab or sourced internally (formally $\partial \hat{g}_i / \partial s_i \geq 0$ where $s_i = x_i + y_i$, $i = 1, 2$), but can be decreasing, or not, in the rival's arguments x_j and y_j . In any case a firm's expected gross profit is (weakly) more impacted by its own R&D, as either purchased from the lab or produced in-house, than by its rival's arguments:

$$\frac{\partial \hat{g}_i}{\partial x_i} \geq \left\| \frac{\partial \hat{g}_i}{\partial x_j} \right\|, \quad (4)$$

$$\begin{array}{c} \parallel \\ \vee \\ \frac{\partial \hat{g}_i}{\partial y_i} \geq \left\| \frac{\partial \hat{g}_i}{\partial y_j} \right\|, \end{array} \quad (5)$$

$i, j = 1, 2, j \neq i$. The vertical comparison of the terms on the RHS of the inequality sign in (4)

²⁴A Nash equilibrium is coalition-proof if it is robust to credible threats of deviations by any subset of principals (for a formal definition see Bernheim, Peleg, and Whinston, 1987). With two principals only, a coalition-proof equilibrium is Pareto-efficient among principals (Bernheim and Whinston, 1986b). For a discussion on truthfulness as an equilibrium refinement, see Martimort (2007).

²⁵In appendix the proofs of Lemmas A.1 and A.2 establish formal conditions which, in combination with theorems by Laussel and Le Breton (2001) and extensions by Billette de Villemeur and Versaveel (2003), lead to Propositions 2, 3, and 5.

²⁶Here we follow Amir et al. (2003) by suggesting that the reduced-form expected gross profit function \hat{g}_i can be interpreted as the overall payoff of a multi-stage game in the product market. Then R&D choices are seen as long-term decisions, on which we focus, followed by a series of short-term final-market decisions.

and (5) specifies that the R&D leaks emanating from the lab are (weakly) more informative than the technological spillovers received from the competitor's internal facilities.²⁷

For both firms, returns to R&D can be either non-increasing (that is, $\partial^2 \hat{g}_i / \partial s_i^2 \leq 0$, $i = 1, 2$), or increasing. The sign of all partial cross-derivatives can also be either non-positive (that is, $\partial^2 \hat{g}_i / \partial x_i \partial x_j \leq 0$, $\partial^2 \hat{g}_i / \partial x_i \partial y_j \leq 0$, $\partial^2 \hat{g}_i / \partial y_i \partial x_j \leq 0$, and $\partial^2 \hat{g}_i / \partial y_i \partial y_j \leq 0$, $i, j = 1, 2$, $j \neq i$), or positive. In all cases, the second-order impact of a firm's R&D, either produced in-house or received from the lab, on its own expected gross profit, is higher than the second-order effect of its competitor's R&D:

$$\left\| \frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_i} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_j} \right\|, \quad (6)$$

|| ∇|

$$\left\| \frac{\partial^2 \hat{g}_i}{\partial y_i^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial y_i \partial y_j} \right\|, \quad (7)$$

$i, j = 1, 2$, $j \neq i$. The vertical comparison of cross-derivatives in (6) and (7) indicates that each firm's marginal expected gross profit is (weakly) more impacted by the technological leakages that emanate from the lab than from its competitor. These technological assumptions are very mild as they bear only on expected profit expressions, and they encompass many possible specifications encountered in the literature (we illustrate with examples of specific algebraic forms in the next section).

Standalone values — The lab can guarantee for itself the value $\underline{v}_0 = 0$ (a normalization). As for the firms, to define their outside option suppose that j has *exclusive* access to the lab, so that their contractual relationship results in $\mathbf{x}_j^* \in \arg \max_{\mathbf{x}} \{E_{\theta}[\tilde{g}_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\}$. Then firm i can only rely on internal resources, and it chooses $y_i^*(\mathbf{x}_j^*)$ to earn the standalone expected value $\underline{v}_i = E_{\theta}[\tilde{g}_i(\mathbf{x}_j^*, \theta)]$. Here $\mathbf{x}_j^* = (x_i^*, x_j^*)$, with $x_i^* \geq 0$, so firm i can possibly receive technology, without financial compensation, despite firm j 's exclusive relationship with the lab. For an equilibrium to exist, with technology outsourcing, it must be the case that $v_i^* = E_{\theta}[\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{f}_i(\tilde{\mathbf{x}}, \theta)] \geq \underline{v}_i$, for both firms.²⁸

²⁷In the words of Lai, Riezman, and Wang (2009), "information leakage is much more severe in the absence of internal controls when R&D is outsourced" (p. 487).

²⁸In the proofs of Propositions 2 and 3 we check that this condition holds in equilibrium (see Appendix A.4).

5 Technological Conditions and Equilibrium Analysis

In this section, we investigate the circumstances in which technology outsourcing either reduces or stimulates internal R&D levels, before deriving conditions for the lab to appropriate a share of R&D profits, or to exactly break-even to the benefit of the outsourcing firms.

As a first result, we find that in equilibrium each firm's internal R&D level y_i^* can be substitutable or complementary to the level x_i received from the lab. The sign of the relation between y_i^* and x_i depends on the nature of R&D returns, but not on technological spillovers.

Proposition 1 (external/internal R&D) *The equilibrium level of a firm's internal R&D activity y_i^* is decreasing in the contracted external lab's activity x_i if and only if the gross profit functions \hat{g}_i have decreasing returns in $s_i = x_i + y_i$, $i = 1, 2$. More formally:*

$$\frac{dy_i^*}{dx_i} \leq 0 \Leftrightarrow \frac{\partial^2 \hat{g}_i}{\partial s_i^2} \leq 0. \quad (8)$$

A first message in this proposition is that whether contracted-out R&D reduces or raises internal activity does not depend on inter-firm technological spillovers, because the second-order effect in (8) bears only on each firm i 's own argument s_i , not on x_j or y_j , $i, j = 1, 2$, $j \neq i$. This property contrasts with the well-known lesson received from many papers that adopt the analytical framework of d'Aspremont and Jacquemin (1988) in order to focus on *horizontal* technological interactions. In these papers, the strategic substitutability or complementarity of the firms' technological choice variables depends entirely on whether a spillover parameter is low or high, respectively. In our model, the firms also interact *vertically* by competing in their contract offers to the external unit. This vertical interaction appears to dominate the horizontal effects for what regards the substitutability/complementarity outcome.

Another message in Proposition 1 is that the relationship between external and internal sourcing is formally ambiguous. This ambiguity is structural, in that it depends on the functional form of firms' expected gross profit. Here contracted-out R&D reduces internal activity if and only if there are decreasing returns to the introduction of a new technology in downstream operations. In real-world circumstances, returns to R&D in the biopharmaceutical domain depend on a number of factors,

²⁹More specifically, $\frac{dy_i^*}{dx_i} = 0$ if and only if either (i) $\frac{\partial^2 \hat{g}_i}{\partial s_i^2} = 0$, or (ii) $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} = \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} < 0$, $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} = \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} < 0$, and $\frac{\partial^2 \hat{f}_j}{\partial y_j^2} = 0$, where $i, j = 1, 2$, $j \neq i$ (see Appendix A.2).

including the therapeutic area (for example, the discovery of new antibiotics does not present the same challenges as the discovery of a universal influenza vaccine) or the relative exploratory nature of a scientific approach (cell therapies against cancer are only emerging, unlike chemotherapy). Our proposition predicts that situations of decreasing returns imply more concentration of R&D activities than with increasing returns, either upstream in external units or downstream in pharma companies.

This result is reminiscent of several recent empirical analyses that indicate a context-specific relationship between external and internal R&D sources in the biopharmaceutical industry. In Hagedoorn and Wang (2012) the estimated sign of the marginal effect of internal R&D expenditure on the innovative output is negative, with internal and external R&D turning out to be complements only at higher levels of in-house R&D investments. In Ceccagnoli et al. (2014), the estimated sign of the partial cross-derivative of an innovation production function with respect to external and internal R&D expenditure is found to depend on a series of factors. These empirical investigations and our formal characterization share the conclusion that external and internal R&D are neither complements nor substitutes *per se*, the exact connection between the two channels being rather context related, as captured here by the sign of a second-order effect.

In what follows we build on Proposition 1 by first considering separately situations of non-increasing returns ($\partial^2 \hat{g}_i / \partial s_i^2 \leq 0$), before discussing the robustness of our results when we shift to non-decreasing returns ($\partial^2 \hat{g}_i / \partial s_i^2 \geq 0$). In either cases, to characterize the distribution of R&D profits among the intermediate R&D market participants we need defining as a value function the highest expected joint profit for the lab together with any subset of firms, that is

$$v(S) = \max_{\mathbf{x}} \left(E_{\theta} \left[\sum_{i \in S} \tilde{g}_i(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta) \right] \right), \quad (9)$$

where $S \in \{\emptyset, \{1\}, \{2\}, \{1, 2\}\}$.

We assume that $v(\emptyset) = \underline{v}_0 = 0$, which describes the no contract situation, and that $v(\{i\}) \geq \underline{v}_i$, implying that firm i 's exclusive control of the lab dominates its standalone value, $i = 1, 2$. Hereafter, for conciseness we denote the maximum expected industry profit $v(\{1, 2\})$ by Λ .

The value function $v(\cdot)$ in (9) is instrumental for the characterization of equilibrium outcomes in the intermediate market for technology, as it captures the interplay of indirect and direct technological externalities: there are *indirect* technological externalities if the lab's cost f_0 of conducting

firm-specific R&D tasks is characterized by economies or diseconomies of scope; there are *direct* externalities if the R&D received or generated by firm i enters in the gross profit function \hat{g}_j of its competitor, $i, j = 1, 2, j \neq i$.³⁰ Indirect (through the lab) and direct (inter-firm) technological externalities can differ in magnitude and in sign, and an *aggregate measure* of the combination of both categories of externalities is given by the structural parameter

$$\epsilon = \Lambda - v(\{1\}) - v(\{2\}). \quad (10)$$

If $\epsilon < 0$, that is $v(\cdot)$ is strictly subadditive, the maximization in \mathbf{x} of joint profits generates less value than the sum of individual profits as obtained by each firm when it exclusively controls the lab, a situation where negative externalities dominate. Otherwise $v(\cdot)$ is superadditive, and positive externalities (weakly) dominate.

■ **Non-increasing returns to R&D.** In this section we assume that

$$\frac{\partial^2 \hat{g}_i}{\partial s_i^2} \leq 0, \quad (11)$$

$i = 1, 2$. Simple sufficient conditions on the primitives of the model can now be derived that determine the sign of the aggregate measure of externalities, and whether the equilibrium expected industry profit is fully appropriated by the two firms or partly retained by the lab. These conditions bear on the sign of indirect and direct R&D externalities, hence on the lab's expected costs $\hat{f}_0(\mathbf{x})$ and firms' expected gross profits $\hat{g}_i(x_i + y_i, x_j, y_j)$, respectively.

Non-negative R&D externalities — Suppose, as a first case, that indirect and direct R&D externalities are non-negative. Formally, for $i, j = 1, 2, j \neq i$,

$$\frac{\partial^2 \hat{f}_0}{\partial x_i \partial x_j} \leq 0, \quad (12)$$

$$\frac{\partial \hat{g}_i}{\partial x_j} \geq 0, \quad \frac{\partial \hat{g}_i}{\partial y_j} \geq 0. \quad (13)$$

³⁰Recall that $\tilde{g}_i(\mathbf{x}, \theta) = g_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x}), \mathbf{z}^*(\mathbf{x}, \mathbf{y}^*(\mathbf{x}), \theta), \theta) - f_i(y_i^*(\mathbf{x}), \theta)$, so that firm i 's profit does not depend only on the R&D generated by the rival internally ($y_j^*(\mathbf{x})$), but also on the technology received by the latter firm from the lab (x_j).

Proposition 2 (non-negative R&D externalities) *Conditions (12-13) imply that $\epsilon \geq 0$ ($v(\cdot)$ is superadditive). Then there exists a continuum of firm equilibrium expected payoffs $(v_1^*, v_2^*) \geq (\underline{v}_1, \underline{v}_2)$ that verify*

$$v_1^* + v_2^* = \Lambda, \quad (14)$$

and the lab exactly breaks even in expectation, that is

$$v_0^* = 0. \quad (15)$$

In (12) the non-positive sign of the cross-derivatives of \hat{f}_0 in the dimensions of \mathbf{x} describes economies of scope in the production of R&D inside the external lab. Selecting a higher x_i , as demanded by firm i , makes it less costly for the lab to satisfy firm j .³¹ This condition is consistent with empirical investigations that evidence the presence of economies of scope mainly in drug discovery (Henderson and Cockburn, 1996) and only to some extent in clinical trials (Cockburn and Henderson, 2001).³²

For an interpretation of the conditions in (13), recall from the structure of each firm's gross profit function in (2) that R&D decisions generate not only inter-firm technological spillovers (x_j and y_j are arguments of g_i , $j \neq i$) but also a product-market rivalry effect (firm j 's external and internal R&D impacts firm i 's strategy z_i , $j \neq i$). As the two non-negative derivatives in (13) relate to the reduced-form \hat{g}_i of the gross profit expression, they capture situations where technological spillovers dominate the negative business stealing effect. This specification points to situations of substantial spillovers, as observed by Henderson and Cockburn (1996) between pharmaceutical firms. It is also consistent with Bloom et al. (2013) where significant technological spillovers are found in the case of pharmaceuticals, together with strategic complementarity in R&D (for a formal illustration see Example 4, below, case $\beta \geq 1/2$).

Examples of complementarities in pre-clinical research include the use of mRNA (messenger ribonucleic acid) to produce medicines that code for the production of proteins by cells in the body, as the same biological mechanism can lead in principle to the treatment of many different diseases. The same applies to research activities in the immuno-oncology domain, as the understanding of how immune responses are controlled by "checkpoints" can result in drugs against a large set of different targets.³³ In that domain, a molecule approved for the treatment of a given type of cancer can be

³¹As Pisano (2006a) puts it, "knowledge and capabilities accumulated in the pursuit of one therapeutic area can often be leveraged to others" (p. 101).

³²"It may be the case ... that success in drug development is purely a function of success in drug discovery" (Cockburn and Henderson, 2001, p. 1053).

³³"The modulation of immune checkpoints using monoclonal antibodies can have a universal effect on immune re-

extended to other indications – a kind of market expansion effect – with competing pharma companies learning from each other the indications toward which their respective research efforts can be targeted.

Non-negative indirect and direct externalities reflect circumstances of weak technological rivalry among the two firms, both in their contract offers to the lab and in their internal operations, implying a limited ability of the external lab to appropriate R&D benefits. This theoretical characterization is consistent with the empirical observation that the average profitability of biotech units is persistently low. Proposition 2 actually establishes that the two firms appropriate all industry profits, and in expectation the lab exactly breaks even. Therefore:

Corollary 1 *When conditions (12-13) hold, incentives to invest upstream, in the external unit, are delinked from the value generated by R&D, to the exclusive benefit of downstream sponsors.*

The following (deterministic) example illustrates Propositions 1 and 2 with specific cost and demand functional forms borrowed from the R&D literature.

Example 1 \square Each firm i 's inverse demand is $p_i(\mathbf{q}) = S \left(1 - \frac{2q_i}{u_i^2} - \frac{\sigma}{u_i} \frac{q_j}{u_j} \right)$, $i, j = 1, 2, j \neq i$, where S is the number of identical consumers, $\sigma \in (0, 2)$ captures horizontal product differentiation, and u_i measures product quality (e.g., increased drug efficacy), as in Symeonidis (2003). Specifically, let $u_i = \varepsilon (s_i)^{1/4} + \varepsilon \beta (s_j)^{1/4}$, where $\varepsilon > 0$ is an inverse cost measure, $\beta \in [0, 1]$ is an inter-firm technological parameter, $s_i = x_i + y_i$ and $s_j = x_j + y_j$, $i, j = 1, 2, j \neq i$.³⁴ For simplicity, we set $S = \sigma = \varepsilon = 1$, $\beta = 1/2$, and the production cost to zero, before solving for the Cournot-Nash quantities $(q_1^*(\mathbf{x}, \mathbf{y}), q_2^*(\mathbf{x}, \mathbf{y}))$. Inserting the latter expressions in $g_i(s_i, x_j, y_j, \mathbf{q}) = p_i(\mathbf{q})q_i$ leads to $\hat{g}_i(s_i, x_j, y_j)$. As $\partial^2 \hat{g}_i / \partial s_i^2 < 0$ (decreasing returns) for all $s_i > 0$, from Proposition 1 we have $dy_i^* / dx_i < 0$ (substitutability). Moreover $\partial \hat{g}_i / \partial x_j > 0$ and $\partial \hat{g}_i / \partial y_j > 0$ (positive direct externalities) for all $x_i, x_j > 0$, so (13) is satisfied.³⁵ Then any additive cost function for the lab (e.g., $\hat{f}_0(\mathbf{x}) = x_1 + x_2$) satisfies (12), in which case from Proposition 2 the downstream firms appropriate the industry profit. \square

Negative R&D externalities — Suppose now that indirect and direct R&D externalities are neg-

sponses that is not dependent on tumour histologies or individual cancer-specific antigens" (Hoos, 2016, p. 235).

³⁴If $x_1 = x_2 = 0$ we have the same specification as in Symeonidis (2003), where the functional form for u_i is adapted from Motta (1992).

³⁵The expressions of derivatives are omitted for space limitation. They are available from the authors on request.

ative, that is for $i, j = 1, 2, j \neq i$,

$$\frac{\partial^2 \hat{f}_0}{\partial x_i \partial x_j} > 0, \quad (16)$$

$$\frac{\partial \hat{g}_i}{\partial x_j} \leq 0, \quad \frac{\partial \hat{g}_i}{\partial y_j} \leq 0. \quad (17)$$

Proposition 3 (negative R&D externalities) *Conditions (16-17) imply that $\epsilon < 0$ ($v(\cdot)$ is strictly subadditive). Then there is a unique pair of firm equilibrium expected payoffs (v_1^*, v_2^*) , which are*

$$v_i^* = v(\{i\}) - |\epsilon| \geq \underline{v}_i, \quad (18)$$

$i = 1, 2$, and the lab appropriates a share of expected industry profits

$$v_0^* = |\epsilon| > 0. \quad (19)$$

The condition on \hat{f}_0 in (16) formalizes a case of congestion, or diseconomies of scale, in the production of R&D by the external lab. Supplying more R&D to a given firm makes it more costly to serve the other firm. The conditions on \hat{g}_i in (17) describe circumstances in which more of firm j 's R&D, as sourced externally or produced internally, weakly reduces firm i 's reduced-form gross profit, all other things remaining equal. Together, these formal conditions relate to real-world circumstances that strongly differ from the ones captured by conditions (12-13). Unlike the empirical evidence mentioned in the previous section on early-stage discovery activities that involve biotech entities, diseconomies of scope (Macher and Boerner, 2006) and nonexistent technological spillovers (Danzon et al. 2005; Macher and Boerner, 2006) have been found in later-stage development activities, notably in phase 2 and phase 3 clinical trials, which involve CROs. The formal conditions in (16) and (17) thus point to these development activities.

To illustrate, recent advances in immuno-oncology have induced clinical trials in the hundreds that test new antibodies or combinations (Tang et al., 2018), implying that the enrollment of patients by a CRO for several competing sponsors has become problematic. Moreover, regulatory constraints such as data exclusivity – i.e., a firm that applies for marketing approval cannot refer to the clinical data generated by a competitor over a given time period – entail limited inter-firm spillovers.

In such cases of negative indirect and direct externalities, the client firms compete for the control of the lab's operations in the intermediate R&D market, and are also penalized by the in-house activity of their competitor. These circumstances are favorable to the lab. Proposition 3 establishes

that negative externalities fully drive the distribution of R&D benefits. Unlike the payoff in the previous section, the lab here appropriates a positive share of industry profits, in direct proportion to $-\epsilon$ which is positive. Each firm's payoff is equal to $v(\{i\})$, $i = 1, 2$, as would be earned by controlling the lab exclusively, truncated by $|\epsilon|$. The latter payoff can be shown to be greater than the standalone value \underline{v}_i .³⁶ The theoretical outcome that the external unit extracts a positive share is consistent with the observation that CROs involved in clinical trials, unlike biotech units, on average earn superior financial returns.

The conditions used in Proposition 3, rewritten in discrete form, apply in the following example.³⁷

Example 2 \square Assume that $\mathbf{x}, \mathbf{y} \in \{0, 1\}^2$, so the decision to invest in a cost-reducing program implies a lump-sum expenditure. The lab's R&D costs are $\hat{f}_0(0, 0) = 0$, $\hat{f}_0(0, 1) = \hat{f}_0(1, 0) = 1$, and $\hat{f}_0(1, 1) = +\infty$, so that the discrete form of condition (16) is satisfied. Here anti-complementarities imply that the lab serves at most one firm profitably.³⁸ Firm i 's internal R&D costs are $\hat{f}_i(y_i) = \gamma y_i$, with $\gamma \geq 1$ capturing a relative inefficiency vis-à-vis the lab (cost cutting is a driver of the use of contract service providers). The unit cost of production is a positive constant $c_i(x_i + y_i)$, with $c_i(0) = c_H$ and $0 \leq c_i(1) = c_i(2) = c_L < c_H$. The two firms sell a homogeneous good, with total demand $q = \sup\{0, a - p\}$, with $p \geq 0$ and $a > c_H$. Given (\mathbf{x}, \mathbf{y}) , defining $\pi = (c_H - c_L)(a - c_H)$, and solving for Bertrand-Nash prices, leads to $\hat{g}_i(x_i + y_i, x_j, y_j) = \pi > 0$ if $x_i + y_i \geq 1$ and $x_j + y_j = 0$, and $\hat{g}_i(x_i + y_i, x_j, y_j) = 0$ otherwise, so the discrete form of condition (17) is also satisfied. We assume that internal R&D is worth undertaking, that is $\gamma / \pi < 1$. To compute equilibrium payoffs, we consider the following two cases: (1) If the lab is inactive ($x_1 = x_2 = 0$), there exists a unique Nash equilibrium in mixed strategies (α_i^*, α_j^*) of internal R&D investments, verifying

$$\alpha_i^* \times (-\gamma) + (1 - \alpha_i^*) \times (\pi - \gamma) = \alpha_i^* \times 0 + (1 - \alpha_i^*) \times 0,$$

$i = 1, 2$. By symmetry,³⁹ $\alpha_i^* = \alpha_j^* = 1 - \frac{\gamma}{\pi}$, which leads to the payoff $v_i(\alpha_1^*, \alpha_2^*) = \underline{v}_i = 0$, $i = 1, 2$.⁴⁰ So the

³⁶See Appendix A.4. From (10) the payoff can be rewritten as firm i 's marginal contribution to industry profit, that is $v_i^* = \Lambda - v(\{j\})$, $i, j = 1, 2, j \neq i$.

³⁷In the whole paper differentiability is adopted for notational convenience, but is not required as illustrated by Example 2. So the condition in (16) can be rewritten in discrete form as $\hat{f}_0(\mathbf{x} \wedge \mathbf{x}') + \hat{f}_0(\mathbf{x} \vee \mathbf{x}') - \hat{f}_0(\mathbf{x}) - \hat{f}_0(\mathbf{x}') \geq 0$, all \mathbf{x}, \mathbf{x}' , with a strict inequality whenever \mathbf{x} and \mathbf{x}' cannot be compared with respect to \geq (strict supermodularity). The conditions in (17) can also be rewritten as $\hat{g}_i(x_i + y_i, x_j, y_j) \geq \hat{g}_i(x_i + y_i, x'_j, y'_j)$ for all $(x'_j, y'_j) \geq (x_j, y_j)$. In Appendix A.4 the proofs of Propositions 2 and 3 are written for any \hat{f}_0 which is either weakly submodular or strictly supermodular, respectively.

³⁸The cost specification in this example is borrowed from Laussel and Le Breton (2001). The extreme supermodularity of \hat{f}_0 , with $\hat{f}_0(1, 1) = +\infty$, here helps illustrating the effect of negative externalities on the distribution of industry profits.

³⁹Given that in this example firms are assumed to be symmetric, we leave aside the two asymmetric equilibria in pure strategies $(y_1^* = 0, y_2^* = 1)$ and $(y_1^* = 1, y_2^* = 0)$.

⁴⁰In this example, when firm i does not participate in the R&D market, its rival j receives technology from the relatively

firms are willing to transact with the lab. (2) When the lab is active, from the assumption on \hat{f}_0 only one firm is served ($x_i = 1 > x_j = 0$), and no firm invests in internal R&D since $\hat{g}_i(1 + 1, 0, y_j) - \hat{f}_i(1) < \hat{g}_i(1 + 0, 0, y_j) - \hat{f}_i(0)$, all y_j , and $\hat{g}_j(0 + 1, 1, y_i) - \hat{f}_j(1) < \hat{g}_j(0 + 0, 1, y_i) - \hat{f}_j(0)$, all y_i . Therefore, industry value is $v(\{1, 2\}) = v(\{1\}) = v(\{2\})$, so that $v_0^* = v(\{1, 2\}) = \pi - 1$, and $v_i^* = v(\{1, 2\}) - v(\{j\}) = 0$, from Proposition 3. Firms' interests are so antagonistic in this example as to make the lab fully appropriate industry value. \square

Uncertainty — The structural conditions in Propositions 2 and 3 also capture circumstances in which R&D outcomes are uncertain for all parties. To see that, consider again Example 2, but with the lab and the firms being successful in R&D with probability $\theta < 1$. The unit cost of production $c(x_i + y_i)$ is now $c(0) = c_H$ with certainty, $c_i(1) = c_L$ with probability θ and $c_i(1) = c_H$ with probability $1 - \theta$, and $c_i(2) = c_L$ with probability $1 - (1 - \theta)^2$ and $c_i(2) = c_H$ with probability $(1 - \theta)^2$. The distribution of (un)favorable events is assumed to be common knowledge *ex ante*, and the true state is discovered only through the realization of R&D tasks (between stages (iii) and (iv) in the timing described in Section 4) so firms' payments can be made contingent on it. Condition (16) remains unchanged, and although the process is now uncertain, condition (17) also remains valid in expectation, as the choice of firm j to attempt to innovate always reduces firm i 's expected profit. Thus Proposition 3 still holds. We assume as above that R&D is worth undertaking, even internally, that is $\gamma/(\theta\pi) < 1$. Provided that the probability of success θ remains sufficiently close to 1 so that $1 - \theta < \gamma/(\theta\pi)$, again a firm will not engage in R&D if its rival receives technology from the lab or sources it internally, and we can directly generalise the baseline example: (1) If the lab is inactive ($x_1 = x_2 = 0$), there exists a unique symmetric Nash equilibrium in mixed strategies

$$\alpha_i^*(\theta) = \alpha_j^*(\theta) = \frac{1}{\theta} \left(1 - \frac{\gamma}{\theta\pi}\right),$$

for a payoff which again is the same as the standalone value $\underline{v}_i(\theta) = 0$, $i = 1, 2$, so the firms have an incentive to transact with the lab. (2) When the lab is active, again from the assumption on \hat{f}_0 only one firm is served ($x_i = 1 > x_j = 0$), and limited uncertainty does not modify the outcome that no firm invests internally since expected net profits verify $\hat{g}_i(1 + 1, 0, y_j) - \hat{f}_i(1) < \hat{g}_i(1 + 0, 0, y_j) - \hat{f}_i(0)$, all y_j , and $\hat{g}_j(0 + 1, 1, y_i) - \hat{f}_j(1) < \hat{g}_j(0 + 0, 1, y_i) - \hat{f}_j(0)$, all y_i . The payoff to the firm that does more efficient lab (so $x_j^* = 1$), exclusively so ($x_i^* = 0$), and finds it profitable not to operate internally ($y_j^* = 0$). Then in this Bertrand context firm i maximizes profits by not investing in internal R&D, and its standalone value is $\underline{v}_i = \hat{g}_i(0 + y_i^*, 1, 0) - \hat{f}_i(y_i^*) = \hat{g}_i(0 + 0, 1, 0) - \hat{f}_i(0) = 0$, $i = 1, 2$.

not receive external R&D is nil, so that $v(\{1,2\}) = v(\{1\}) = v(\{2\})$. Then $v_0^* = v(\{1,2\})$, and $v_i^* = v(\{1,2\}) - v(\{j\}) = 0$, $i, j = 1, 2, j \neq i$, from Proposition 3. With these specifications, the lab's expected equilibrium payoff is $\theta\pi - 1$, the firm that benefits from the lab's output exactly breaks even, and its rival earns its standalone value.

In the next example, we show that our results also apply to the polar situation with highly uncertain R&D. We obtain that, when the competitor or its external contractor might fail with a high probability, it can be a dominant strategy for the firms to engage in R&D as well.

Example 3 \square We consider the specifications of Example 2 with the extension to uncertain R&D as above, and focus on the case of rare successful outcomes. Internal R&D can be profitable, that is $\gamma/(\theta\pi) < 1$, although θ is sufficiently close to 0 for $\gamma/(\theta\pi) < (1 - \theta)^2$ to hold. In this case, the likelihood that the competitor and the lab succeed in R&D is so low as to make the probability of simultaneous success negligible. Then everything happens as if, when deciding to engage or not in R&D, each firm were focusing on its own probability of success only, abstracting from the other players' actions. Investing in internal R&D is a dominant strategy: (1) If the lab is inactive ($x_1 = x_2 = 0$), the firms' expected payoff is $(1 - \theta)\theta\pi - \gamma$, which is slightly higher than the standalone level $\underline{v}_i(\theta) = (1 - \theta)^2\theta\pi - \gamma$, $i = 1, 2$. (2) When the lab is active, again the form of \hat{f}_0 implies that only one firm is served ($x_i = 1 > x_j = 0$). Still the distinctive feature here, in comparison to the previous example, is that both firms choose to invest internally as well: $\hat{g}_i(1 + 1, 0, y_j) - \hat{f}_i(1) > \hat{g}_i(1 + 0, 0, y_j) - \hat{f}_i(0)$, all y_j , and $\hat{g}_j(0 + 1, 1, y_i) - \hat{f}_j(1) > \hat{g}_j(0 + 0, 1, y_i) - \hat{f}_j(0)$, all y_i , for $i, j = 1, 2, j \neq i$. Thus $v(\{i\}) = (1 - (1 - \theta)^2)(1 - \theta)\pi - \gamma - 1$ (i.e., π is earned by firm i when the latter player and the lab do not both fail while firm j fails) and the expected industry value is now $v(\{1, 2\}) = (3 - 2\theta)(1 - \theta)\theta\pi - 2\gamma - 1$ (i.e., the sum of firm i 's expected gross payoff $(1 - (1 - \theta)^2)(1 - \theta)\pi$ and of firm j 's gross payoff $(1 - \theta)^2\theta\pi$ net of total R&D costs). Therefore, from Proposition 3 we have $v_0^* = (1 - \theta)\theta\pi - 1 > 0$, and $v_i^* = v(\{1, 2\}) - v(\{j\}) = (1 - \theta)^2\theta\pi - \gamma$, which is positive but only equal to the standalone level (the profit earned when the competitor controls the lab to its exclusive benefit). By competing for the lab's resources, here the firms earn less than if the lab does not exist. \square

There is more in Examples 2 and 3 than an illustration of the applicability of a theoretical proposition to specific algebraic forms. Only in the latter example, where the probability of success of R&D operations is assumed to be low, both the lab and its sponsor engage in R&D efforts. This outcome is consistent with the empirical evidence (Guedj, 2005) that projects with a low probability of success

are more often conducted through a contractual alliance between a large firm and a smaller biotech company (as in Example 3) than conducted entirely within the same entity (as in Example 2). The comparison of Examples 2 and 3 thus rationalizes the general observation that the reduction in drug R&D productivity over the last decades – which is formally captured here by a lower probability of success – has coincided with increasingly frequent situations where large pharma firms and smaller external biotech units contribute jointly to research and development (Pisano, 2006a; Rydzewski, 2008; Scannell et al., 2012). This is a sufficiently high level of uncertainty, in our theoretical framework, that triggers an investment by all industry participants.

Another interesting equilibrium property illustrated by examples 2 and 3 is that the firms (principals), whose payments to the lab (agent) are truthful, are shielded from the uncertainty that is specific to external R&D operations. The lab, however, bears the risk inherent to its technological activities. These findings, beyond specific examples, can be generalized to all situations described in Propositions 2 and 3, for any distribution of θ , by establishing that each firm can adjust within boundaries its contract offer to the lab, without changing the equilibrium strategies and the related equilibrium expected payoffs to all parties, in order to guarantee for itself a constant payoff whenever possible. This adjusted transfer function, t_i^o , is characterized by the following lemma.

Lemma 1 *Suppose that $(\tilde{\mathbf{t}}, \tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}})$ is a TSPNE. Define, for each θ , the lower bound of firm i 's gross payoff over all possible efficient choices⁴¹*

$$\underline{g}_i(\theta) = \inf_{\mathbf{x} \in X^*} [\tilde{g}_i(\mathbf{x}, \theta)],$$

and the function $h : \Theta \rightarrow \mathbb{R}$, whose value depends on the realized state only, with

$$E_\theta [h(\theta)] = 0, \tag{20}$$

$$v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta) \leq h(\theta) \leq v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta), \tag{21}$$

all $\theta \in \Theta$. Then $t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\}$ is a truthful best reply to t_j that incentivizes the lab to choose an action which is undistinguishable from $\tilde{\mathbf{x}}$, in that it yields the same expected payoffs to all parties. However, for any realized θ the (ex-post) equilibrium payoffs are:

$$v_0(\tilde{\mathbf{x}}, \theta) + h(\theta), \quad v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta), \quad v_j(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta),$$

$i, j = 1, 2, j \neq i$.

⁴¹Unless there exists a multiplicity of optima, $\underline{g}_i(\theta)$ does not differ from the equilibrium gross payoff $\tilde{g}_i(\tilde{\mathbf{x}}, \theta)$. In the proof of Proposition 4, in Appendix A.7, we assume that $\underline{g}_i(\theta) \geq 0$ for almost all θ (that is, no one expects adverse events to be so extreme as to more than annihilate the gross value of a principal's operations).

The condition in (20) is needed for all profit expressions to remain unchanged in expectation, although the lab receives more than the expected level for some values of θ , and less for others. In (21) the first inequality implies that contract offers to the lab are non-negative, and the second one that the equilibrium payoff to the firm is also non-negative in all states of nature.⁴²

By introducing in the payment strategy an adjustment term $h(\theta)$, as defined in Lemma 1, a firm can condition its financial transfers on the realization of the technological risk, and thereby protect its *ex-post* payoff from adverse events. In unfavourable circumstances where uncertainties imply that the gross equilibrium profit can be so low as to be strictly lower than the expected equilibrium payoff v_i^* with positive probability, then each firm can adjust its payment to earn the lower bound $\underline{g}_i(\theta) < v_i^*$ if an adverse event occurs (e.g., the lab's efforts are unsuccessful, or they cost much more than expected), or a superior profit level $\bar{v}_i \geq v_i^*$ that does not depend on θ otherwise. In more favourable circumstances where uncertainty does not prevent the gross equilibrium profit to be higher than the expected net equilibrium value v_i^* for almost all θ , each firm can guarantee for itself the latter value as an *ex-post* payoff, which is thus independent of the realized state of nature.

Toward a more formal characterization of adjusted payment strategies, that is *risk-proof* contract offers, we define the set $\underline{\Theta}(\bar{v}_i)$ such that $\underline{g}_i(\theta) \leq \bar{v}_i$, for all $\theta \in \underline{\Theta}(\bar{v}_i)$, with $\bar{v}_i \geq v_i^*$. Then:

Proposition 4 Suppose that $(\tilde{\mathbf{t}}, \tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}})$ is a TSPNE:

(i) If $\underline{g}_i(\theta) \geq v_i^*$ for almost all $\theta \in \Theta$, firm i can guarantee for itself the expected net equilibrium value v_i^* as an *ex-post* payoff for almost all states of nature, by addressing to the lab the risk-proof contract offer

$$t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - v_i^*\}.$$

(ii) If $\underline{g}_i(\theta) < v_i^*$ for a subset of Θ of strictly positive measure, firm i can guarantee for itself an *ex-post* payoff equal to the lower bound $\underline{g}_i(\theta)$ for all $\theta \in \underline{\Theta}(\bar{v}_i)$, and to a higher constant $\bar{v}_i \geq v_i^*$ for all $\theta \in \Theta \setminus \underline{\Theta}(\bar{v}_i)$, by addressing to the lab the risk-proof contract offer

$$t_i^o(\mathbf{x}, \theta) = \begin{cases} 0 & \text{if } \theta \in \underline{\Theta}(\bar{v}_i), \\ \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - \bar{v}_i\} & \text{if } \theta \in \Theta \setminus \underline{\Theta}(\bar{v}_i). \end{cases}$$

There exists a unique constant \bar{v}_i such that the expected payoff to firm i remains equal to $v_i^* = E_\theta[v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)]$.

⁴²The adjusted contract offer introduced in Lemma 1 remains compatible with an upfront part t_i^o paid to the agent. Supposing that $t_i^o(\tilde{\mathbf{x}}, \theta) > 0$ for almost all θ , the upfront payment is bounded from above by the non-negative threshold $\bar{T}_i = \max_{T>0} \{T \mid \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) \geq T, \text{ for almost all } \theta\}$. Indeed, as long as $t_i^o \leq \bar{T}_i$, equilibrium contingent payments $k_i^o(\tilde{\mathbf{x}}, \theta) = t_i^o(\tilde{\mathbf{x}}, \theta) - \underline{t}_i^o$ verify $k_i^o(\tilde{\mathbf{x}}, \theta) \geq \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{T}_i \geq 0$, for almost all θ .

In other words, in unfavorable circumstances where the distribution of θ can result in the gross payoff $\underline{g}_i(\theta)$ to be strictly lower than v_i^* with positive probability, firm i 's contract offer specifies a high *ex-post* payoff $\bar{v}_i \geq v_i^*$ if the realization of the technological risk implies that $\underline{g}_i(\theta) > \bar{v}_i$, and a payoff limited to the lower bound $\underline{g}_i(\theta)$ otherwise (with no transfer to the lab), so that in expectation the equilibrium payoff remains equal to v_i^* (see Appendix A.7.2 for a formal characterization of \bar{v}_i).

Proposition 4 establishes that truthful contract offers are available to the firms that shield them (at least partly) from adverse technological events by transferring (some or all of) the burden of risk to the upstream lab. This insurance property holds in particular when R&D externalities are non-negative ($\epsilon \geq 0$), implying from Proposition 2 that the equilibrium payoff to the lab, in expectation, is exactly zero. In that case, valuable projects at the industry level are vulnerable since an unfavorable draw necessarily yields, *ex-post*, a negative net return to the external lab. This vulnerability is made more acute when strategies are used that pass on the downside effect of uncertainty through risk-proof contingent payments. (Of course such a negative outcome can generalize to situations where profits are positive, as in Proposition 3, and still sufficiently close to zero.) As a direct implication, risk-averse investors are deterred to finance projects on the supply side of the intermediate market for technology, and “fewer projects being funded means a weaker industry pipeline, and fewer new drugs”(Cockburn and Lerner, 2009, p. 5).

Some safeguarding measures can be designed that aim at avoiding the abandonment of projects that contribute positively to the total industry profit, but are characterized by a high degree of technological uncertainty. Such measures, in light of our results and their connections to the empirical evidence, appear less relevant for clinical development than for early-stage research characterized by significant economies of scope and technological spillovers. The financial back-up of a partner university, as commonly observed for startups since the emergence of biotech engineering, can be interpreted as a relevant attempt to insure promising spin-offs from unfavorable events. Our formal analysis also points to the introduction of regulatory constraints on the adjustment of payments, by big pharma companies, on the realization of technological risks.

We now consider cases with increasing returns to R&D.

■ **Non-decreasing returns to R&D.** In this section, for $i = 1, 2$, we assume that

$$\frac{\partial^2 \hat{g}_i}{\partial s_i^2} \geq 0, \quad (22)$$

where $s_i = x_i + y_i$. We identify simple conditions for Propositions 2 and 3 to remain valid.

Proposition 5 *Suppose that returns to R&D are non-decreasing, as in (22). If $\partial^2 \hat{g}_i / \partial x_i \partial x_j > 0$ (i.e., x_i and x_j are complementary for firm i , with $i, j = 1, 2, j \neq i$), which implies that $dy_i^* / dx_j > 0$, then Propositions 2 and 3 still hold. Otherwise, a sufficient condition is $dy_i^* / dx_j > -1$.*

The interplay of contracted-out and internal R&D levels is central to that result. From Proposition 1 we already know that, for each firm i , non-decreasing R&D returns imply that internal and contracted-out R&D are strategic complements: $dy_i^* / dx_i \geq 0$. Then, there are two cases: (1) If x_j and x_i are complements inside firm i 's gross payoff function, that is $\partial^2 \hat{g}_i / \partial x_i \partial x_j \geq 0$, then y_i^* is monotone increasing with the *other* firm's contracted-out R&D level x_j , that is $dy_i^* / dx_j \geq 0$. In that case, the respective effects of x_i , x_j , y_i and y_j on firms' gross profits are all congruent and Propositions 2 and 3 remain valid with non-decreasing returns as well. (2) When x_i and x_j are substitutes, in that $\partial^2 \hat{g}_i / \partial x_i \partial x_j < 0$, then y_i^* decreases with the *other* firm's contracted-out R&D level x_j , that is $dy_i^* / dx_j < 0$. Here more R&D received from the lab reduces the competitor's internal R&D level, so firm i 's gross profit may be impacted negatively. In the most extreme circumstances, the latter effect could possibly result in $d\hat{g}_i / dx_i$ being negative when $\partial \hat{g}_i / \partial x_j$ and $\partial \hat{g}_i / \partial y_j$ are both positive. The latter property however does not occur when the substitution effect is limited, more specifically when $dy_i^* / dx_j > -1$.

The next (deterministic) example illustrates all cases predicted by Proposition 5. It shows that while external and internal R&D tasks are complementary (a consequence of non-decreasing returns to R&D from Proposition 1), the client firms may fully appropriate industry profit (as in Proposition 2) or concede to the lab a positive share of it (as in Proposition 3).

Example 4 □ *The external lab's R&D cost is $\hat{f}_0(\mathbf{x}) = \gamma(x_1^2 + x_2^2)/2 - \delta x_1 x_2$, with $\delta \in [-\gamma, \gamma)$, $\gamma > 0$, and the firms' internal R&D costs are $\hat{f}_i(y_i) = \kappa + y_i^2$, $i = 1, 2$, $\kappa > 0$. The downstream marginal cost of production is $c > 0$, the final-market inverse demands are $p_i(\mathbf{q}) = \sup \{0, a_i(\mathbf{x}, \mathbf{y}) - q_i - q_j\}$, $i, j = 1, 2$, $j \neq i$, where p_i is the price, (q_i, q_j) are quantities, and $a_i(\mathbf{x}, \mathbf{y}) = (a + s_i + \beta s_j)$ is the price intercept,*

which involves spillovers measured by the parameter $\beta \in [0, 1]$ borrowed from d'Aspremont and Jacquemin (1988). Then $s_i = x_i + y_i$ can be interpreted as the sum of $R(x_i)$ and $D(y_i)$, as in Vonortas (1994), here toward a quality improvement (e.g., increased drug safety). Non-cooperative profit maximization in quantities leads to $q_i^*(\mathbf{x}, \mathbf{y}) = [(a - c) + s_i(2 - \beta) + s_j(2\beta - 1)] / 3$. We have $\partial^2 \hat{g}_i / \partial s_i^2 = 2(2 - \beta)^2 / 9 > 0$, so condition (22) is satisfied for all parameter values (increasing R&D returns). Then, whether Proposition 2 or 3 applies depends on δ and β : (i) if $\delta \geq 0$ (< 0) then condition (12) (resp. condition (16)) holds; (ii) if $\beta \geq 1/2$ ($< 1/2$) then condition (13) (resp. condition (17)) holds, directly from $\partial \hat{g}_i / \partial x_j = \partial \hat{g}_i / \partial y_j = (2/3)(2\beta - 1)q_i^*(\mathbf{x}, \mathbf{y})$. Moreover, $\partial^2 \hat{g}_i / \partial x_j \partial x_i = (2/9)(2 - \beta)(2\beta - 1) \geq 0$ only if $\beta \geq 1/2$, and we have $dy_i^* / dx_j = 3(2\beta - 1)(\beta - 2) / [(\beta^2 - \beta + 7)(\beta^2 - 3\beta - 1)] > -1$ for $\beta < 1/2$. Therefore, in this example the non-negative R&D externalities case of Proposition 2 applies if $\beta \geq 1/2$ and $\delta \geq 0$, and the negative externalities case of Proposition 3 applies if $\beta < 1/2$ and $\delta < 0$. \square

An important lesson of Propositions 2 and 3 is that the interplay of indirect (through the lab) and direct (inter-firm) technological externalities drives the additivity status of the value function v in (9), which in the end determines the distribution of industry profits. This characterization applies in all situations where the two types of externalities have the same sign, as formalized by the easy-to-use conditions (12-13) and (16-17). It applies also in “mixed” cases where indirect externalities are negative, while direct externalities are not, or *vice versa*. For an illustration, consider again the previous example by setting $\delta = \beta = 0$, $\gamma > 1$, and by assuming that the firms rely exclusively on the external lab ($y_1 = y_2 = 0$). Here we have non-negative indirect but negative direct externalities ($\partial^2 \hat{f}_0 / \partial x_1 \partial x_2 = 0$ and $\partial \hat{g}_i / \partial x_j < 0$ for all positive final-market quantities). Then, for γ approaching 1 from above, one finds $v(\{1\}) = v(\{2\}) = (a - c)^2 / 5$, and $\Lambda = (a - c)^2 / 4$, a case of strict subadditivity, implying from (18) that equilibrium payoffs are $v_1^* = v_2^* = v_0^* / 3 = (a - c)^2 / 20$.

6 Incentives for More Integration

The distribution of industry profits can be modified by a shift to a more integrated structure that unifies the lab with one of the two firms, or both. The analysis of incentives to integrate vertically, after having characterized the equilibrium profit distribution in the decentralized common agency setting, is consistent with industry practice as the acquisition of an R&D unit by a big pharma company often follows a period of collaboration (Folta, 1998; Danzon and Grabowski, 2012).

Supposing that the owners of the lab and the two firms can participate in the equity market in order to depart from the initial outsourcing equilibrium characterized in the previous section, we assume that (i) initially, each entity is owned by distinct sets of individuals (no one can simultaneously be a seller and a buyer); (ii) when the lab and only one firm integrate vertically, the unified entity can agree to supply R&D to the other firm by bargaining with it over the sharing of industry profits; and (iii) transaction costs are nil.

Consider first the situation in which the lab and the two firms *all* participate in some form of integration in the intermediate R&D market. This occurs if the lab acquires the two firms and controls them as subsidiaries, or if the two firms share the ownership of the lab and control it as a joint venture, with choices of internal R&D and final-market strategies remaining non cooperative (no collusion). In these two cases there is no gain in joint profits to be earned vis-à-vis equilibrium payoffs of the common agency structure. This is because the truthfulness of the firms' equilibrium payment strategies implies that the lab is offered two transfer schedules which exactly reflect the respective shapes of the firms' gross profit functions (that is, $\tilde{g}_i(\mathbf{x}, \theta)$, $i = 1, 2$). The lab thereby internalizes both direct and indirect externalities, and thus is incentivized to supply R&D outputs that maximize the joint profits of all participants. It follows that the net share of joint profits accruing to each buyer of another firm's equity cannot improve on the amount of net profits received in the common agency equilibrium. Forward integration (i.e., the two users become subsidiaries of the lab) would imply the payment of v_i^* by the lab to the firms' owners. Backward integration (i.e., the lab becomes a joint venture) would require the total payment of v_0^* by the two firms for the ownership of the upstream assets. The equality $v_0^* + v_1^* + v_2^* = \Lambda$ holds in all cases, so there is no incentive for the lab and the two firms to form a unique entity, unless further assumptions are introduced (e.g., cost or demand parameters become a function of the governance structure). More formally:

Proposition 6 *In the initial outsourcing equilibrium, the firms' non-cooperative transfers and the lab's for-profit R&D operations result in a maximum expected industry profit: $\tilde{\mathbf{x}} \in \arg \max_{\mathbf{x} \in X} E_\theta[\tilde{g}_1(\mathbf{x}, \theta) + \tilde{g}_2(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$. Therefore, unless the firms coordinate internal R&D operations (\mathbf{y}) or collude in final-market commercial decisions (\mathbf{z}), there is no incentive for the lab to acquire the two firms and control them as subsidiaries, nor for the firms to share the ownership of the lab and control it as a joint venture.*

As for uncertainty, it can only reduce incentives for the two firms to acquire and control the lab jointly, since by doing so they internalize the part of risks that can be transferred via adjusted pay-

ments to the supply side of the R&D market. The viewpoint of the lab's owners is different though, as by acquiring the two firms they alleviate the burden of risk they bear in the initial outsourcing situation. Nevertheless, Proposition 6 establishes that the integrated structure cannot generate the value that is needed to finance such possible risk dilution benefits. The integration of all market participants can be financed only if the firms neutralize downstream strategic interactions by coordinating internal R&D activities or/and final-market strategies.

It remains to investigate all alternative forms of integration that can allow the owners of the lab, or of the two firms, to privately appropriate a larger share of the industry maximum Λ than in the decentralized outsourcing initial situation. Toward an equilibrium industry structure in the equity market, we consider the following discrete set of possible arrangements: the horizontal integration of firms 1 and 2 for the joint procurement of external R&D (internal R&D and final-market choices remaining non cooperative), the vertical integration of the lab with firm 1, or with firm 2. We consider in turn the situations in which the value function v , in (9), is superadditive ($\epsilon \geq 0$, as in Proposition 2), then strictly subadditive ($\epsilon < 0$, as in Proposition 3), depending on the interplay of indirect (through the lab) and direct (inter-firm) technological externalities. The two cases are illustrated respectively by Figures 1 and 2, which represent the space of possible partitions of the maximum industry profit Λ as a 2-simplex, with full appropriation by the lab (i.e., $v_0 = \Lambda$) at the top vertex, and by either of the two firms at the bottom vertices. More generally, the payoffs to the lab and each of the two firms are proportional to the distance of the allocation point to the edge opposite to their respective vertex.

Non-negative R&D externalities — When indirect and direct R&D externalities are both non-negative, or in “mixed” situations with positive and negative externalities where the former dominate, so that v is superadditive ($\epsilon \geq 0$), from Proposition 2 the lab only breaks even in equilibrium of the common agency structure, that is its expected profit is $v_0^* = 0$, and the two firms thus expect to appropriate the total industry profit, $v_1^* + v_2^* = \Lambda$ (where $v_i^* \geq \underline{v}_i$, $k = 1, 2$). As there exists a continuum of firm equilibrium expected payoffs, the exact distribution (v_1^*, v_2^*) can only reflect circumstances outside of the initial model specifications. Hereafter we formalize such circumstances by the bargaining powers (ϕ_1, ϕ_2) in $[0, 1]^2$, with $\phi_1 + \phi_2 = 1$. They verify

$$v_k^* = \underline{v}_k + \phi_k (\Lambda - \underline{v}), \quad (23)$$

where $k = 1, 2$, and $(\underline{v}_1, \underline{v}_2)$ is the disagreement point, with $\underline{v} = \underline{v}_1 + \underline{v}_2$, so that,

$$\phi_k = \frac{v_k^* - \underline{v}_k}{\Lambda - \underline{v}}. \quad (24)$$

Although with non-negative externalities joint R&D procurement cannot increase the firms' joint profit, a larger individual share can be earned by a firm if it deviates unilaterally from the outsourcing equilibrium to acquire the lab. By exclusively controlling the lab, the vertically integrated entity $\{0, i\}$ benefits from a stronger bargaining position. In case of disagreement its payoff becomes $v(\{i\}) \geq \underline{v}_i$, while its rival j 's payoff remains at \underline{v}_j , the standalone value. The bargaining process, in case of vertical integration, thus determines an expected payoff to the unified entity equal to

$$v_{0+i}^{\{0,i\}} = v(\{i\}) + \phi_i (\Lambda - v(\{i\}) - \underline{v}_j) > v_i^*, \quad (25)$$

and an expected payoff to the outsider equal to

$$v_j^{\{0,i\}} = \underline{v}_j + \phi_j (\Lambda - v(\{i\}) - \underline{v}_j) < v_j^*, \quad (26)$$

with the weights (ϕ_i, ϕ_j) as defined in (24), $i, j = 1, 2, j \neq i$.⁴³

As they face two competing alternatives, the lab's owners can choose the firm to integrate with.⁴⁴ By selling out to firm i , they may expect to earn $v_{0+i}^{\{0,i\}} = v_{0+i}^{\{0,i\}} - v_i^{\{0,i\}}$, the difference between the expected payoff to the unified entity and the acquirers' residual claim. The two firms' respective owners thus compete in the equity market, and their willingness to pay is the difference between the profit they earn by acquiring the lab and the profit they earn should the lab integrate with the other firm. In comparison to the initial equilibrium situation, the firm that does not integrate, say firm j , is forced to concede what the other firm appropriates by acquiring the lab. Firm i 's willingness to pay, as an acquirer, is thus the sum of what it appropriates, and what the other would have appropriated, that is

$$v_{0+i}^{\{0,i\}} - v_i^{\{0,i\}} = \phi_j (v(\{i\}) - \underline{v}_i) + \phi_i (v(\{j\}) - \underline{v}_j) > 0, \quad (27)$$

⁴³An equality sign replaces the strict inequality signs in (25) and (26) only if the exclusive control of the lab by firm i entails no benefit vis-à-vis the standalone value, that is $v(\{i\}) = \underline{v}_i$.

⁴⁴For completeness, if the exclusive control of the lab strictly dominates the standalone option only for firm i , so that $v(\{i\}) > \underline{v}_i$ and $v(\{j\}) = \underline{v}_j$, then $v_{0+j}^{\{0,j\}} = v_j^*$. If $v(\{i\}) = \underline{v}_i$ as well, then no firm is interested in acquiring the lab.

$i, j = 1, 2, j \neq i$.⁴⁵ Therefore, although firms are asymmetric, and appropriate different amounts by acquiring the lab, the willingness to pay is the same across the two firms. Competition in the equity market is thus frontal, and it leads to the integration of the lab with any of the two firms, indifferently.

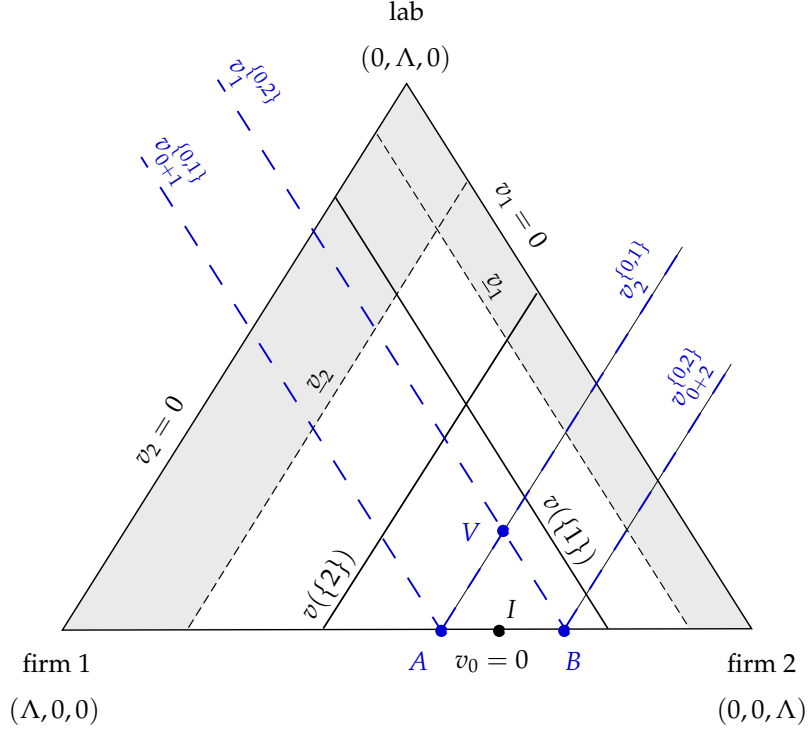


Figure 1: v is superadditive ($\epsilon \geq 0$), so the loci for $v(\{1\})$ and $v(\{2\})$ intersect inside the simplex. In the initial equilibrium (point I), in expectation the firms fully appropriate industry profits ($v_1^* + v_2^* = \Lambda$), so the lab exactly breaks even ($v_0^* = 0$). Should a firm integrate the lab at no cost, it would appropriate more industry profits (point A for firm 1, or B for firm 2). However, competition in the equity market lowers firms' payoffs to $v_i^{\{0,j\}}$, for $i, j = 1, 2, j \neq i$, and results in the lab to appropriate a positive benefit, that is $v_0^{\{0,1\}} = v_0^{\{0,2\}} > 0$ (point V).

In the equilibrium industry structure, firm i 's owners have bidden their willingness to pay so they receive only $v_i^{\{0,j\}} < v_i^*$, a case of winner's curse. Uncertainty does not help, as by integrating the lab the acquirer cannot benefit any more from the contractual ability to shield (at least partly) its financial performance from adverse technological events.⁴⁶ The rival j 's owners are not better off, as

⁴⁵In (27) we have $v_{0+i}^{\{0,i\}} - v_i^{\{0,j\}} = 0$ only if $v(\{i\}) - v_i = v(\{j\}) - v_j = 0$, or $\phi_i = v(\{j\}) - v_j = 0$, $i, j = 1, 2, j \neq i$.

⁴⁶However, integration is more attractive if it entails a reduced ability for firm j , as an outsider, to transfer risks to the lab when the latter is controlled by its rival i . Still, by integrating the lab the acquirer must bear the consequence of risks that were transferred upstream in the initial outsourcing situation. So even when vertical integration modifies the design of contracts and the distribution of risks over R&D market participants, at this level of generality it is not clear whether the net effect of that change mitigates the winner's curse problem or not.

by contracting out for R&D with the integrated entity $\{0, i\}$ they earn only $v_j^{\{0,i\}} < v_j^*$. As for the lab's owners, they earn a payoff equal to the common maximum bid, which from (24) and (27) is equal to

$$v_0^{\{0,1\}} = v_0^{\{0,2\}} = \frac{v(\{1\}) - \underline{v}_1}{\Lambda - \underline{v}} (v_2^* - \underline{v}_2) + \frac{v(\{2\}) - \underline{v}_2}{\Lambda - \underline{v}} (v_1^* - \underline{v}_1) > v_0^* = 0, \quad (28)$$

with the *strict* inequality replaced by an equality sign only in the degenerate case where $v(\{i\}) = \underline{v}_i$ for the two firms ($i = 1, 2$). Otherwise, even if $v_i^* = \underline{v}_i$ for one of the two firms (say $i = 1$), the inequality remains strict (as necessarily $v_2^* - \underline{v}_2 = \Lambda - \underline{v} - (v_1^* - \underline{v}_1) > 0$).

Therefore, in expectation, the lab's owners extract a positive share of industry profits in the equity market (point V in Figure 1), unlike in the initial equilibrium of the R&D market (Proposition 2). This theoretical result is consistent with the empirical evidence in Higgins and Rodriguez (2006), where firms overbid for an external unit, and the acquirer succumbs to the winner's curse. More recently, Pisano (2015) also reflected on whether "pharmaceutical companies [are] paying more for R&D by acquiring companies than by carrying out the R&D themselves". According to our result, pharmaceutical companies pay more for R&D by acquiring the lab than by engaging in a contractual arrangement with it. This is because, in this model, competition is tougher in the equity market, where only one firm can acquire the lab, and the opportunity cost of not being that firm is very high, whereas in the R&D market firms can partially reconcile their antagonism through finely tuned contract offers.

Proposition 7 *With non-negative R&D externalities ($\epsilon \geq 0$), one of the two firms – which are possibly asymmetric – acquires the lab with equal probability $1/2$. The bidding contest in the equity market implies a strictly higher expected profit to the lab, and a lower one to each firm, than in the initial outsourcing equilibrium.*

The latter proposition points to exit payoffs to capital holders as a long-term financial incentive that can motivate investments in early-stage research activities (discovery). Indeed, from (28) the expected profit to the lab's owners in the equity market can be as high as the net industry level $\Lambda - \underline{v}$, which occurs when $v(\{i\})$ is set equal to $\Lambda - \underline{v}_j$, $i, j = 1, 2, j \neq i$. This case describes rather extreme situations where, in the initial outsourcing equilibrium, the net marginal contribution of each firm to the total industry value is equal to zero, that is $v(\{1, 2\}) - v(\{i\}) - \underline{v}_j = 0$, for $i, j = 1, 2, j \neq i$, implying that having two firms instead of only one does not change the industry value.

On the other hand, exit payoffs can also be very low. Again from (28), the gain to the lab's owners in the equity market are negligible whenever the difference $v(\{i\}) - \underline{v}_i$, for $i = 1, 2$, approaches zero. This situation relates typically to interesting situations where the lab's superior efficiency originates from economies of scope that can hardly be exploited when a firm controls the external unit exclusively for itself.⁴⁷ In that case, the lab's owners, who exactly break-even in the initial outsourcing equilibrium (Proposition 2), cannot reappropriate industry profits by selling the equity to a firm. They thus have little incentive to invest in the first place, even when large economies of scope imply a project of high total value Λ .

Negative R&D externalities — When indirect and direct R&D externalities are both negative, or in “mixed” situations with positive and negative externalities where the latter dominate, so that v is strictly subadditive ($\epsilon < 0$), from Proposition 3 the equilibrium expected payoffs in the initial outsourcing situation are $v_0^* = |\epsilon| > 0$, and $v_i^* = v(\{i\}) - |\epsilon| \geq \underline{v}_i$, $i = 1, 2$, so that $v_1^* + v_2^* < \Lambda$. As an alternative to the initial outsourcing situation, the firms can opt for an horizontal arrangement in order to procure jointly external R&D. In that case they behave cooperatively as a unique principal in the intermediate market for technology, and fully appropriate the maximum industry profit, with the lab breaking even exactly in expectation (point H in Figure 2 below).⁴⁸ We thus have $v_0^{\{1,2\}} = 0$ and $v_1^{\{1,2\}} + v_2^{\{1,2\}} = \Lambda$ (here the superscript $\{1,2\}$ refers to the industry structure with firms 1 and 2 procuring jointly).

The initial outsourcing equilibrium payoffs determine the firms' disagreement point (v_1^*, v_2^*) when they bargain over the agent's expected payoff $v_0^* = \Lambda - v_1^* - v_2^*$. The firms' expected payoffs $(v_1^{\{1,2\}}, v_2^{\{1,2\}})$ then verify

$$v_k^{\{1,2\}} = v_k^* + \omega_k (\Lambda - v_1^* - v_2^*), \quad (29)$$

where $k = 1, 2$, implying that bargaining powers (ω_1, ω_2) in $[0, 1]^2$, with $\omega_1 + \omega_2 = 1$, are

$$\omega_k = \frac{v_k^{\{1,2\}} - v_k^*}{\Lambda - v_1^* - v_2^*}. \quad (30)$$

⁴⁷To illustrate, consider Example 4 above (see Section 5), with $\beta = 1/2$ (so direct externalities are nil, for simplicity), and $\delta > 0$ (economies of scope), so $\epsilon > 0$. Then, whenever the cost parameter γ takes a sufficiently high value, supposing that firm i controls the lab for itself it must focus on internal R&D (the y_i dimension) to earn a maximum profit $v(\{i\})$ which is only slightly higher than the standalone value \underline{v}_i .

⁴⁸A horizontal arrangement here relates to the intermediate market for technology, as opposed to the final market for products, where the firms are assumed to remain competitors. This situation is similar to the cases observed by Majewski (2004) where firms engaged in a technology alliance jointly choose to outsource their R&D to a third party in order to split costs.

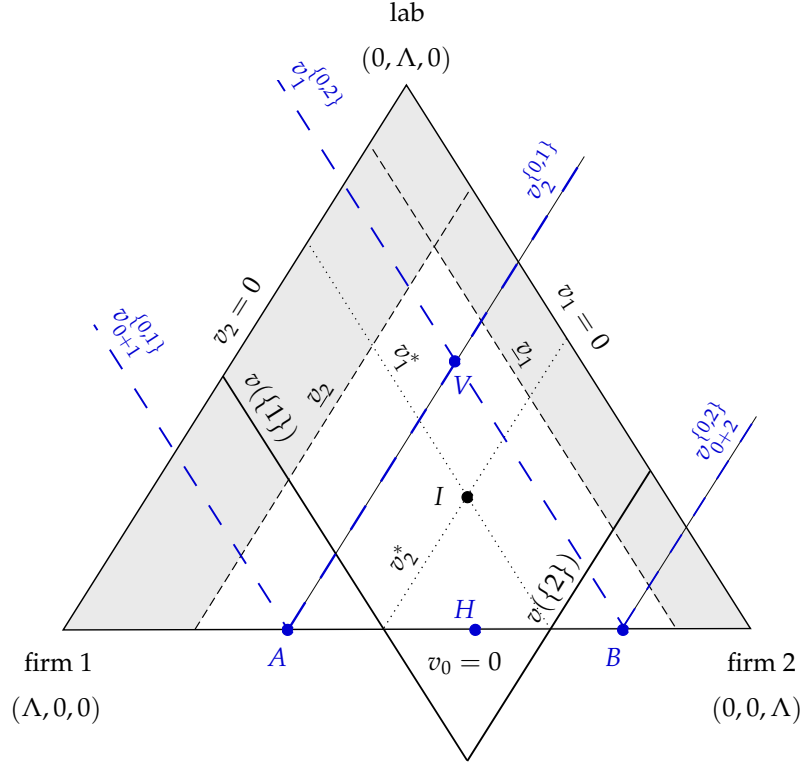


Figure 2: v is strictly subadditive ($\epsilon < 0$), so the loci for $v(\{1\})$ and $v(\{2\})$ intersect outside the simplex. In the initial R&D equilibrium (point I) the firms earn an expected profit $v_i^* = v(\{i\}) - |\epsilon|$, $i = 1, 2$, and the lab earns $v_0^* > 0$. By agreeing horizontally to coordinate R&D outsourcing, the firms fully reappropriate industry profits (point H). Should a firm integrate vertically with the lab, at no cost, it would increase profits (point A for firm 1, or B for firm 2). The bidding contest to acquire the lab leads both firms to earn $v_i^{\{0,j\}}$, $i, j = 1, 2, j \neq i$ (point V) in the equilibrium industry structure.

From Proposition 3 we know that $v_0^* = \Lambda - v_1^* - v_2^* > 0$, implying that in (29) we have $v_k^{\{1,2\}} \geq v_k^*$ for $k = 1, 2$, with a *strict* inequality sign for at least one firm, implying that the latter firm earns a positive gain by shifting to the horizontal arrangement. Moreover, the definition of ϵ in (10) together with $v_i^* = v(\{i\}) - |\epsilon|$ in (18) imply that $v_j^* = \Lambda - v(\{i\})$, so that $v_j^{\{1,2\}} \geq v_j^*$ and $v_j^{\{1,2\}} = \Lambda - v_i^{\{1,2\}}$ lead to $v_i^{\{1,2\}} \leq v(\{i\})$, $i, j = 1, 2, j \neq i$, again with a *strict* inequality sign for at least one firm. It follows that

$$v(\{k\}) - |\epsilon| \leq v_k^{\{1,2\}} \leq v(\{k\}), \quad (31)$$

where $k = 1, 2$, with at least one *strict* inequality sign. In (31) the first inequality states that any situation resulting in lower individual payoffs than in the initial equilibrium is rejected. The second

inequality indicates that each firm's expected payoff in the horizontal arrangement is bounded from above by $v(\{k\})$, the value generated when it acquires the external lab without contracting with its rival.

While the two firms' joint profit is maximized in the horizontal arrangement, each firm has an incentive to depart unilaterally from $\{1, 2\}$ by acquiring the lab, for a *strictly*⁴⁹ higher disagreement payoff $v(\{i\}) > v_i^*$ accruing to the integrated entity $\{0, i\}$, and a (weakly) lower disagreement payoff $\underline{v}_j \leq v_j^*$ to the other firm. By controlling the lab and benefitting exclusively from its technology, in case of disagreement the integrated entity can guarantee for itself the upper bound of the horizontal arrangement payoff in (31), while the outsider earns only its standalone value. The bargaining process, with vertical integration, implies an expected payoff to the unified entity equal to

$$v_{0+i}^{\{0,i\}} = v(\{i\}) + \omega_i (\Lambda - v(\{i\}) - \underline{v}_j) > v_i^{\{1,2\}}, \quad (32)$$

and an expected payoff to the outsider equal to

$$v_j^{\{0,i\}} = \underline{v}_j + \omega_j (\Lambda - v(\{i\}) - \underline{v}_j) < v_j^{\{1,2\}}, \quad (33)$$

$i, j = 1, 2, j \neq i$.⁵⁰

The lab's owners, as in the non-negative externalities situation of the previous section, can thus make the two firms compete in the equity market by soliciting bids in order to appropriate a share of industry profits. Provided that no restriction is introduced that limits payment offers, again the firms have the same willingness to pay for the lab, that is

$$v_{0+i}^{\{0,i\}} - v_i^{\{0,j\}} = \omega_j (v(\{i\}) - \underline{v}_i) + \omega_i (v(\{j\}) - \underline{v}_j) > 0, \quad (34)$$

$i, j = 1, 2, j \neq i$, and any of them becomes the acquirer with the same probability 1/2. The payoffs structure already obtained in the non-negative externalities case thus prevails, with each firm's respective owners earning exactly their outside value, $v_1^{\{0,2\}} < v_1^{\{1,2\}}$ and $v_2^{\{0,1\}} < v_2^{\{1,2\}}$, in any of the two possible equilibrium industry structures.

⁴⁹In this negative externalities situation ($\epsilon = \Lambda - v(\{i\}) - v(\{j\}) < 0$) we have $v(\{i\}) > \Lambda - v(\{j\}) = v_i^*$.

⁵⁰The strict inequality sign in (33) is a consequence of $v(\{i\}) > v_i^* \geq \underline{v}_i$, and possibly of firm j 's strictly lower disagreement value $\underline{v}_j < v_j^*$ (this differs from the non-negative externalities case in (26)). Then the strict inequality in (32) follows from $v_i^{\{1,2\}} + v_j^{\{1,2\}} = v_{0+i}^{\{0,i\}} + v_j^{\{0,i\}} = \Lambda$, which leads to $v_{0+i}^{\{0,i\}} - v_i^{\{1,2\}} = v_j^{\{1,2\}} - v_j^{\{0,i\}} > 0$.

However, with negative externalities it is not *a priori* established that the lab's owners are better off post integration than in the initial outsourcing equilibrium. Inserting the expression of the firms' respective bargaining powers in (34), and reorganizing terms (see Appendix A.10), we find that

$$v_0^{\{0,1\}} = v_0^{\{0,2\}} = \frac{v(\{1\}) - \underline{v}_1}{|\epsilon|} (v_2^{\{1,2\}} - v_2^*) + \frac{v(\{2\}) - \underline{v}_2}{|\epsilon|} (v_1^{\{1,2\}} - v_1^*) \geq v_0^* = |\epsilon|. \quad (35)$$

The value that can be extracted by the lab's owners by selling their property rights to any of the two – possibly asymmetric – firms (from *I* to *V* in Figure 2) is only *weakly* greater than the share of expected industry profits obtained in Proposition 3. To summarize:

Proposition 8 *With negative R&D externalities ($\epsilon < 0$): (a) If the firms can commit not to integrate the lab they horizontally coordinate external technology sourcing and appropriate the total industry value Λ ; (b) Otherwise, one of the two firms acquires the lab with the same probability 1/2, and the positive profit earned by the lab's owners in the equity market is only weakly superior than in the initial outsourcing equilibrium.*

Part (a) of Proposition 8 focuses on cases where the firms, for some exogenous reasons (e.g., a regulation), rule out the possibility to acquire the lab. When technological externalities are negative ($\epsilon < 0$), because multi-client R&D operations entail diseconomies of scope and inter-firm knowledge spillovers are limited, or as a consequence of a strong business-stealing effect in the final market, the firms are more likely to coordinate horizontally the sourcing of new technology from the same external lab whereas in the case of positive externalities they derive no benefit from coordination. This observation is reminiscent of Majewski (2004), where evidence is found that “when collaborative agreements involve firms that compete in downstream markets, they tend to outsource their collaborative R&D to a third party” (p. 2). Part (b) of Proposition 8 emphasizes that, with negative technological externalities (late-stage clinical development), the financial performance of the lab can only be weakly augmented in the equity market in comparison to the initial outsourcing equilibrium. As the upstream expected financial returns are already positive in the latter equilibrium, and increasing with the magnitude of ϵ (in Proposition 3), the lab's owners face relatively weak incentives to sell ownership to a downstream firm when their activities are characterized by strongly negative externalities.

Financial constraints — Propositions 7 and 8 are derived under the assumption that bids are unrestricted. However, in real-world business circumstances a financial constraint might be introduced

that limits firms' ability to compete for the control of an external entity. In the theoretical context of the model, the effect of such a constraint can be investigated by assuming that the price paid to the lab's owners, in case of vertical integration, cannot be so high as to imply a lower expected payoff to the acquiring firm than in the initial outsourcing equilibrium. Formally, the two firms' respective financial constraints are thus

$$v_i^* \leq v_i^{\{0,i\}} = \Lambda - v_j^{\{0,i\}} - v_0^{\{0,i\}}, \quad (36)$$

$i, j = 1, 2, j \neq i$. In principle such constraints make it more difficult for a firm to acquire the lab when the latter makes positive profits than when it exactly breaks even. They also help identifying the profile of the most aggressive bidder.

With non-negative R&D externalities ($\epsilon \geq 0$), as $\Lambda - v_i^* = v_j^*$ from Proposition 2, firm i 's constraint in (36) becomes $v_0^{\{0,i\}} \leq v_j^* - v_j^{\{0,i\}}$. In other words, firm i 's maximum bid, when it acquires the lab, must not exceed what firm j has lost, as an outsider, because of the change in bargaining positions vis-à-vis the outsourcing situation. By using (23) and (26), firm i 's financial constraint can thus be rewritten $v_0^{\{0,i\}} \leq \phi_j(v(\{i\}) - \underline{v}_i)$, $i, j = 1, 2, j \neq i$. The lab's owners face two competing bids, and select the highest, say the one of firm i if $\phi_j(v(\{i\}) - \underline{v}_i) \geq \phi_i(v(\{j\}) - \underline{v}_j)$ which, by using (24), is equivalent to

$$\frac{v_i^* - \underline{v}_i}{v(\{i\}) - \underline{v}_i} \leq \frac{v_j^* - \underline{v}_j}{v(\{j\}) - \underline{v}_j}. \quad (37)$$

The comparison in (37) predicts that the acquirer is the "weaker" firm, that is the one whose net equilibrium expected payoff in the initial outsourcing situation (that is $v_i^* - \underline{v}_i$), relatively to the net profit that the integrated entity can guarantee for itself ($v(\{i\}) - \underline{v}_i$), is lower.

With negative R&D externalities ($\epsilon < 0$), the same reasoning starting from (36) leads to the following condition for firm i to be the one that acquires the lab:

$$\frac{v_i^{\{1,2\}} - \underline{v}_i}{v(\{i\}) - |\epsilon| - \underline{v}_i} \leq \frac{v_j^{\{1,2\}} - \underline{v}_j}{v(\{j\}) - |\epsilon| - \underline{v}_j}. \quad (38)$$

Here the acquirer is the firm whose gain in the horizontal arrangement (that is $v_i^{\{1,2\}} - \underline{v}_i$), relatively to the initial equilibrium net expected payoff ($v_i^* - \underline{v}_i = v(\{i\}) - |\epsilon| - \underline{v}_i$), is lower.

The theoretical prediction of conditions (37 - 38) is compatible with the empirical evidence. In Higgins and Rodriguez (2006), the firms experiencing a deterioration of their research pipeline are found to be more likely to engage in the acquisition of a biotech entity. In Danzon et al. (2007), the

financially strong firms appear to be less likely to engage in acquisitions. In other words, the most active firms in the equity market are not the ones with the highest profit prospects nor the deepest pockets.

7 Conclusion

Our formal analysis offers a new rationale for the low average profitability of the science-based businesses of biotech (Pisano, 2006a, 2010), and the high amount of risk they take in comparison to their pharma sponsors (Golec and Vernon, 2009; Thakor et al., 2017), as observed since the emergence of genetic engineering in the 1970s. In light of our results, and their connection with empirical observations, we believe that limited financial returns should not be seen as evidence of disappointing technological progress, but can be interpreted as a confirmation that economies of scope and inter-firm knowledge spillovers have been significant in the biotechnology domain. Indeed, in such circumstances, our results establish that the decision by competing firms to outsource early-stage research activities to a common external unit leads most expected value, possibly very substantial, to be appropriated by downstream sponsors. This conclusion does not extend, in our theoretical framework, to contracted-out development services that are characterized by negative technological externalities. Moreover, the higher level of idiosyncratic risk (specific to an individual unit or project) observed in biotech firms than in pharma companies is explained in our model by the ability of downstream firms to transfer – at least partly – the financial consequences of R&D uncertainties to the supply side of the market for technology by the means of contingent transfer payments.

The contracting-out of discovery and clinical tasks is attractive from the viewpoint of big pharma companies, because it allows them to transfer risks to an external unit whose distinctive capabilities, and the ability to internalize technological externalities, are sources of efficiency gains. However, the possible delinkage of upstream investment incentives from total industry value, and the vulnerability of investors' net returns to negative shocks, together theorize the abandonment of projects precisely in those early-stage areas that can generate critical advances toward new treatments or preventives. An important consequence is that, although the long-run perspective of substantial exit payoffs in the equity market can in some cases generate incentives to start a biotech unit, externalizing research does not always qualify as a relevant pathway to address the declining productivity in innovation that has characterized the biopharmaceutical sector over several decades. Our theoretical results thus

do not support the view of R&D outsourcing as the panacea often described by business experts or industry publications.

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A Appendix

We first develop the derivatives $\frac{dy_j^*}{dx_j}$ and $\frac{dy_i^*}{dx_j}$, which are needed to prove Propositions 1 to 5 afterwards.

A.1 Derivation of $\frac{dy_j^*}{dx_j}$ and $\frac{dy_i^*}{dx_j}$

As the arguments x_i and y_i enter additively into g_i (hence \hat{g}_i), we have

$$\frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_i} - \frac{\partial \hat{f}_i(y_i^*)}{\partial y_i} = 0, \quad (39)$$

and similarly

$$\frac{\partial \hat{g}_j(x_j + y_j^*, x_i, y_i^*)}{\partial x_j} - \frac{\partial \hat{f}_j(y_j^*)}{\partial y_j} = 0, \quad (40)$$

where the Nash strategies $y_i^* = y_i^*(x_i, x_j)$ and $y_j^* = y_j^*(x_i, x_j)$ result from the two firms' non-cooperative profit-maximization in their respective internal R&D levels, for $i, j = 1, 2, j \neq i$.

Differentiating (39) and (40) w.r.t. x_j , and using again $s_i = x_i + y_i$ in \hat{g}_i , and $s_j = x_j + y_j$ in \hat{g}_j , we obtain the system of equations

$$\begin{pmatrix} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} & \frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \\ \frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} & \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \end{pmatrix} \begin{pmatrix} \frac{dy_j^*}{dx_j} \\ \frac{dy_i^*}{dx_j} \end{pmatrix} = \begin{pmatrix} -\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \\ -\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \end{pmatrix},$$

where $\hat{g}_i = \hat{g}_i(x_i + y_i^*, x_j, y_j^*)$, $\hat{g}_j = \hat{g}_j(x_j + y_j^*, x_i, y_i^*)$, $\hat{f}_i = \hat{f}_i(y_i^*)$, and $\hat{f}_j = \hat{f}_j(y_j^*)$, for clarity.

This yields the solution

$$\begin{pmatrix} \frac{dy_j^*}{dx_j} \\ \frac{dy_i^*}{dx_j} \end{pmatrix} = \frac{1}{\Delta} \begin{pmatrix} -\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} & \frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \\ \frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} & -\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \end{pmatrix} \begin{pmatrix} -\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \\ -\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \end{pmatrix} \quad (41)$$

where

$$\Delta = \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) - \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i}. \quad (42)$$

We thus have

$$\frac{dy_j^*}{dx_j} = \frac{1}{\Delta} \left[\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} - \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \right], \quad (43)$$

$$\frac{dy_i^*}{dx_j} = \frac{1}{\Delta} \left[\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \right]. \quad (44)$$

We know that $\frac{\partial^2 \hat{f}_i(y_i^*)}{\partial y_i^2} \geq 0$ (by assumption) and $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} < 0$ (second-order condition), which holds also for firm j . As $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ and $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i}$ have the same sign (by assumption), $\left\| \frac{\partial^2 \hat{g}_i}{\partial x_i^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \right\|$ and $\left\| \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \right\|$ (see (7)), we obtain from (42) that $\Delta \geq 0$.⁵¹

Moreover, we know also from Henriques (1990) that the reaction functions in the internal R&D space (y_i, y_j) cross “correctly”, so that the Nash equilibrium (y_i^*, y_j^*) is stable, only if

$$\left| \frac{\partial^2 [\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)]}{\partial y_i^2} / \frac{\partial^2 [\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)]}{\partial y_i \partial y_j} \right| < 1, \quad (45)$$

for $i, j = 1, 2, j \neq i$.

Again, the argument $s_i = x_i + y_i$ in \hat{g}_i , together with \hat{f}_i being a function of y_i only, imply that $\frac{\partial^2 [\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)]}{\partial y_i \partial y_j} = \frac{\partial^2 \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_i \partial y_j} = \frac{\partial^2 \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_i \partial y_j}$, so that (45) becomes $\left| \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) / \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \right| < 1$.

1. The latter inequality, together with $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} < 0$ for $i = 1, 2$ (second-order condition) and $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \geq 0$ for $i, j = 1, 2, j \neq i$ (partial cross-derivatives, for both firms, have the same sign by assumption) imply from (42) that Δ is nonzero at (y_i^*, y_j^*) , and the derivatives in (43) and (44) are well defined.

Suppose now that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2}$ is nonzero for $i = 1, 2$ (the case $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} = 0$ is considered below in the proof of Proposition 1). Then, a careful reorganization of terms in the expression of $\frac{dy_j^*}{dx_j}$ in (43) leads to

$$\frac{dy_j^*}{dx_j} = \frac{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2}}{\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2}} \left[1 - \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{jj}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \Delta} \right], \quad (46)$$

where $N_{jj} = \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$.

⁵¹From the expression in (2), the argument $s_i = x_i + y_i$ of the gross profit function g_i , hence also of the reduced-form \hat{g}_i , implies that inequalities (6 - 7) can be rewritten by substituting the derivatives with respect to x_i for the ones with respect to y_i . Thus $\partial^2 \hat{g}_i / \partial y_i \partial x_i = \partial^2 \hat{g}_i / \partial x_i^2$, $\partial^2 \hat{g}_i / \partial y_i \partial x_j = \partial^2 \hat{g}_i / \partial x_i \partial x_j$, and $\partial^2 \hat{g}_i / \partial y_i \partial y_j = \partial^2 \hat{g}_i / \partial x_i \partial y_j$, for $i, j = 1, 2, j \neq i$. We make use of these substitutions throughout the appendix.

Similarly, a reorganization of terms in the expression of $\frac{dy_i^*}{dx_j}$ in (44) leads to

$$\frac{dy_i^*}{dx_j} = \frac{-\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}}{\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2}} \left[1 - \frac{\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}}{-\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}} \frac{N_{ij}}{\Delta} \right], \quad (47)$$

where $N_{ij} = \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} - \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \frac{\partial^2 \hat{g}_j}{\partial x_j^2}$.

Both expressions in (46) and (47) are well defined because the denominators of their respective first terms are nonzero by assumption (second-order condition for a unique $\mathbf{y}^*(\mathbf{x})$).

A.2 Proof of Proposition 1.

We want to establish that $\frac{dy_i^*}{dx_i} < 0 \Leftrightarrow \frac{\partial^2 \hat{g}_i}{\partial s_i^2} < 0$, where $s_i = x_i + y_i$, and with $\hat{g}_i = \hat{g}_i(x_i + y_i^*, x_j, y_j^*)$, $\hat{g}_j = \hat{g}_j(x_j + y_j^*, x_i, y_i^*)$, $\hat{f}_i = \hat{f}_i(y_i^*)$, and $\hat{f}_j = \hat{f}_j(y_j^*)$, $i, j = 1, 2, j \neq i$, throughout this section for clarity. There are three cases:

Case 1: $\frac{\partial^2 \hat{g}_i}{\partial s_i^2} = 0$. Recalling from $s_i = x_i + y_i$ in \hat{g}_i that $\frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_i} = \frac{\partial^2 \hat{g}_i}{\partial x_i^2}$ and $\frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_j} = \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$, from (6) we have $\left\| \frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_i} \right\| = \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i^2} \right\| = 0 \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial y_i \partial x_j} \right\| = \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \right\|$, implying that $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} = 0$. Then, by inserting $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} = 0$ and $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} = 0$ into (43) and (44) we find

$$\frac{dy_j^*}{dx_j} = \frac{dy_i^*}{dx_j} = 0. \quad (48)$$

Case 2: $\frac{\partial^2 \hat{g}_i}{\partial s_i^2} < 0$. (i) Here $\frac{\partial^2 \hat{f}_i(y_i^*)}{\partial y_i^2} \geq 0$ implies that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \leq \frac{\partial^2 \hat{g}_i}{\partial x_i^2} < 0$, while $\left\| \frac{\partial^2 \hat{g}_i}{\partial x_i^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \right\|$ by assumption from (7) implies that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \leq \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$, and by transitivity $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \leq \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$. (ii) As $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} < 0$, here $\left\| \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \right\|$ by assumption from (6) leads to $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \leq \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i}$. From (i) and (ii) we obtain that

$$- \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \leq - \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \leq 0,$$

with an equality sign (the 1st one) if and only if $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} = \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} < 0$ and $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} = \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} < 0$.

Multiplying through by $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$, adding $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ on both sides, and reorganizing terms, leads to

$$1 \geq \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{jj}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \Delta},$$

so that the expression between brackets in (46) is non-negative, and finally we have

$$\frac{dy_j^*}{dx_j} = - \underbrace{\frac{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2}}{\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2}}}_{<0} \underbrace{\left[1 - \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{jj}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \Delta} \right]}_{\geq 0} \leq 0, \quad (49)$$

again with an equality sign if and only if $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} = \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} < 0$ and $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} = \frac{\partial^2 \hat{g}_j}{\partial x_i \partial x_j} < 0$, where the latter equality implies that $\frac{\partial^2 \hat{f}_j}{\partial y_j^2} = 0$.

Case 3: $\frac{\partial^2 \hat{g}_i}{\partial s_i^2} > 0$ ($i = 1, 2$). Here we have $\left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \frac{\partial^2 \hat{g}_j}{\partial x_j^2} < 0$, which together with $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \geq 0$ (partial cross-derivatives have the same sign by assumption) implies that $\left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \frac{\partial^2 \hat{g}_j}{\partial x_j^2} < \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$.

Multiplying through by $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$, adding $-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ on both sides of the inequality sign, and reorganizing terms, leads to

$$1 > \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{jj}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \Delta}, \quad (50)$$

so that the expression between brackets in (46) is positive. Then $-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right)^{-1} > 0$ implies finally that

$$\frac{dy_j^*}{dx_j} = \underbrace{\frac{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2}}{\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2}}}_{>0} \underbrace{\left[1 - \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{jj}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \Delta} \right]}_{>0} > 0. \quad (51)$$

The sign of $\frac{dy_j^*}{dx_j}$ in (48), (49) and (51), establishes Proposition 1. ■

A.3 Lemmas

The technical results introduced in this section are needed to prove Propositions 2, 3, and 5. The first two lemmas establish a connection between properties of $\hat{g}_i(\mathbf{x}, \mathbf{y})$ and $\hat{g}_i(\mathbf{x}, \mathbf{y}^*(\mathbf{x})) - \hat{f}_i(y_i^*(\mathbf{x}))$.

Lemma A.1 Suppose that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \leq 0$, $i = 1, 2$. Then $\frac{d[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*)]}{dx_j}$, $i, j = 1, 2, j \neq i$, has the same sign as $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j}$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j}$.

Proof. By the envelope theorem, as $y_i^* = y_i^*(x_i, x_j)$ maximizes $\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)$, we have

$$\frac{d \left[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*) \right]}{dx_j} = \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_j} + \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j} \frac{dy_j^*}{dx_j}. \quad (52)$$

Our objective is to determine the sign of the RHS expression in (52). Given the (same) sign of $\frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_j}$ and $\frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j}$, we need only characterizing $\frac{dy_j^*}{dx_j}$.

First, if $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} = 0$ ($i = 1, 2$), we know from (48) that $\frac{dy_j^*}{dx_j} = 0$, which is sufficient to conclude.

Next, if $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} < 0$ ($i = 1, 2$), we know from (49) that $\frac{dy_j^*}{dx_j} \leq 0$. Then toward a contradiction we suppose that $\left\| \frac{dy_j^*}{dx_j} \right\| > 1$, or equivalently here $\frac{dy_j^*}{dx_j} < -1$. Developing the expression in (46) then leads to

$$\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \left(\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} - \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \right) > \underbrace{-\frac{\partial^2 \hat{f}_j}{\partial y_j^2} \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i(y_i^*)}{\partial y_i^2} \right)}_{\substack{\geq 0 \\ < 0}}. \quad (53)$$

As $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ and $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j}$ have the same sign, and $\left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial x_j} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \right\|$ (model specifications in (6-7)), we know that the expression on the LHS of the strict inequality sign in (A.9) is non-positive. However, $\frac{\partial^2 \hat{f}_j}{\partial y_j^2} \geq 0$ (by assumption) and $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i(y_i^*)}{\partial y_i^2} < 0$ (second-order condition) imply that the product on the RHS is always non-negative, a contradiction. Hence $\left\| \frac{dy_j^*}{dx_j} \right\| \leq 1$. This, together with $\left\| \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_j} \right\| \geq \left\| \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j} \right\|$ (model specifications), is sufficient to conclude that $\frac{d[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*)]}{dx_j}$ in (52) has the same sign as $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j}$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j}$. ■

Lemma A.2 Suppose that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \leq 0$, $i = 1, 2$. If $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j} \geq 0$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j} \geq 0$, $i, j = 1, 2$, $j \neq i$, then $\frac{d[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*)]}{dx_i} \geq 0$ also.

Proof. By the envelope theorem, as $y_i^* = y_i^*(x_i, x_j)$ maximizes $\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)$, we have

$$\frac{d \left[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*) \right]}{dx_i} = \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_i} + \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j} \frac{dy_j^*}{dx_i}, \quad (54)$$

where $\frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_i} \geq 0$ as a model specification, and $\frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j} \geq 0$ as an assumption of the present lemma. In order to determine the sign of the RHS expression in (54), we thus need only characterizing $\frac{dy_j^*}{dx_i}$.

First, if $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} = 0$ ($i = 1, 2$), we know from (48) that $\frac{dy_j^*}{dx_i} = 0$, which is sufficient to conclude.

Next, if $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} < 0$ ($i = 1, 2$), recall from (47) in Section A.1 that

$$\frac{dy_j^*}{dx_i} = \frac{-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i}}{\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2}} \left[1 - \frac{\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} N_{ji}}{-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \Delta} \right], \quad (55)$$

where $N_{ji} = \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} - \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) \frac{\partial^2 \hat{g}_i}{\partial x_i^2}$. There are two possible cases that depend on the sign of $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i}$.

(i) If $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \geq 0$ ($i, j = 1, 2, j \neq i$), as $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$ we have $-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} / \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) \geq 0$. Then, toward a contradiction, suppose that the expression between brackets in (55) is negative. This, together with $\left\| \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} / \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \right\| \leq 1$ (model specifications in (6-7)), implies that $\frac{N_{ji}}{\Delta} < -1$, which can be rewritten as

$$\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \left(\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} - \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \right) < \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right),$$

where the expression on the LHS of the inequality sign is non-negative, whereas the expression on the RHS is non-positive, a contradiction. It follows that $\frac{dy_j^*}{dx_i} \geq 0$, which is sufficient to conclude directly that $\frac{d[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*)]}{dx_i}$ in (54) is non-negative also.

(ii) If $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} < 0$ ($i, j = 1, 2, j \neq i$), unlike in the previous case the model specifications do not imply that $\frac{dy_j^*}{dx_i} \geq 0$. Then, toward a contradiction, whenever $\frac{dy_j^*}{dx_i} < 0$ suppose that $\left\| \frac{dy_j^*}{dx_i} \right\| > 1$, or equivalently here $-\frac{dy_j^*}{dx_i} > 1$. From (55), by using $\Delta > 0$ (see (42) and related subsequent comments in Section A.1) we have

$$\frac{-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i^2} + \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right)}{\left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) - \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i}} > 1,$$

which can be rewritten as

$$-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i^2} + \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) > \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) - \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i},$$

with $\frac{\partial^2 \hat{g}_i}{\partial x_i^2}$ and $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ both negative here. Moreover we know by assumption from (7) that $\left\| \frac{\partial^2 \hat{g}_i}{\partial x_i^2} \right\| \geq \left\| \frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j} \right\|$. Therefore, substituting $\frac{\partial^2 \hat{g}_i}{\partial x_i^2}$ for $\frac{\partial^2 \hat{g}_i}{\partial x_i \partial y_j}$ in the last term above, by transitivity we obtain

$$-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i^2} + \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) > \left(\frac{\partial^2 \hat{g}_i}{\partial x_i^2} - \frac{\partial^2 \hat{f}_i}{\partial y_i^2} \right) \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right) - \frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \frac{\partial^2 \hat{g}_i}{\partial x_i^2},$$

which simplifies to

$$\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} < \frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \leq \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \leq 0.$$

As the latter inequalities contradict the initial assumption in (6) that $\left\| \frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \right\| \leq \left\| \frac{\partial^2 \hat{g}_j}{\partial x_j^2} \right\|$, it must be the case that $\left\| \frac{dy_j^*}{dx_i} \right\| \leq 1$. This, together with the model specification in (4-5) that $\left\| \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial x_i} \right\| \geq \left\| \frac{\partial \hat{g}_i(x_i + y_i^*, x_j, y_j^*)}{\partial y_j} \right\|$, is sufficient to conclude that $\frac{d[\hat{g}_i(x_i + y_i^*, x_j, y_j^*) - \hat{f}_i(y_i^*)]}{dx_i}$ in (54) is non-negative. ■

The next two lemmas were established in Laussel and Le Breton (2001). We restate them in the notation of this paper for a self-contained appendix:⁵²

Lemma A.3 *If v is superadditive, that is $\Lambda \geq v(\{1\}) + v(\{2\})$, then in all TSPNE $v_0^* = 0$, and all vectors of equilibrium profits (v_1^*, v_2^*) are such that $v_1^* + v_2^* = \Lambda$.*

Lemma A.4 *If v is strictly subadditive, that is $\Lambda < v(\{1\}) + v(\{2\})$, then in all TSPNE $v_0^* > 0$, and there exists a unique vector of equilibrium profits (v_1^*, v_2^*) , where $v_i^* = \Lambda - v(\{j\})$, $i, j = 1, 2, j \neq i$.*

A.4 Proof of Propositions 2 and 3.

Proof of Proposition 2. We first use Lemmas A.1 and A.2, and finally Lemma A.3, in order to extend a proof by Billette de Villemeur and Versaevel (2003, Proposition 1) to establish the (weak) superadditivity of $v(\cdot)$. Then we show that the equilibrium payoffs (v_1^*, v_2^*) exist that are (weakly) higher than the respective standalone values (v_1, v_2) .

1) Denote by $X_{\{i\}}^*$ the set of the lab's actions that maximize its expected joint profit with firm i , that is

$$X_{\{i\}}^* = \arg \max_{\mathbf{x}} \left(\max_{y_i} [\hat{g}_i(x_i + y_i, x_j, y_j) - \hat{f}_i(y_i)] - \hat{f}_0(\mathbf{x}) \right).$$

Define $\mathbf{a} = (a_1, a_2) \in X_{\{1\}}^*$ and $\mathbf{b} = (b_1, b_2) \in X_{\{2\}}^*$. We know from the initial model specifications that $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial s_i} \geq 0$, where $s_i = x_i + y_i$. Moreover, it is assumed in this proposition that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \leq 0$ (non-increasing returns to R&D), and from (13) that $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j} \geq 0$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j} \geq 0$ (non-negative R&D externalities). It follows that $\hat{g}_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x})) - \hat{f}_i(y_i^*(\mathbf{x}))$ is non-decreasing in x_j from Lemma A.1, and also in x_i from Lemma A.2. Therefore, for $\mathbf{u} = (u_1, u_2)$, with $u_1 = a_1 \vee b_1$

⁵²With two principals, the convexity condition introduced in Laussel and Le Breton (2001, Proposition 3.2 p. 103) coincides with the superadditivity of v in our model, and the *strong* subadditivity property (Proposition 3.3, p. 104) coincides here with strict subadditivity.

and $u_2 = a_2 \vee b_2$, we have

$$\hat{g}_1(a_1 + y_1^*(\mathbf{a}), a_2, y_2^*(\mathbf{a})) - \hat{f}_1(y_1^*(\mathbf{a})) \leq \hat{g}_1(u_1 + y_1^*(\mathbf{u}), u_2, y_2^*(\mathbf{u})) - \hat{f}_1(y_1^*(\mathbf{u})), \quad (56a)$$

$$\hat{g}_2(b_2 + y_2^*(\mathbf{b}), b_1, y_1^*(\mathbf{b})) - \hat{f}_2(y_2^*(\mathbf{b})) \leq \hat{g}_2(u_2 + y_2^*(\mathbf{u}), u_1, y_1^*(\mathbf{u})) - \hat{f}_2(y_2^*(\mathbf{u})). \quad (56b)$$

The non-negative cross-derivative in (12) implies the weak submodularity of \hat{f}_0 (Topkis, 1995). This property, with (56a) and (56b), together lead to

$$\begin{aligned} & \underbrace{\hat{g}_1(a_1 + y_1^*(\mathbf{a}), a_2, y_2^*(\mathbf{a})) - \hat{f}_1(y_1^*(\mathbf{a})) - \hat{f}_0(\mathbf{a})}_{=v(\{1\})} + \underbrace{\hat{g}_2(b_2 + y_2^*(\mathbf{b}), b_1, y_1^*(\mathbf{b})) - \hat{f}_2(y_1^*(\mathbf{b})) - \hat{f}_0(\mathbf{b})}_{=v(\{2\})} \\ & \leq \underbrace{\hat{g}_1(u_1 + y_1^*(\mathbf{u}), u_2, y_2^*(\mathbf{u})) - \hat{f}_1(y_1^*(\mathbf{u})) + \hat{g}_2(u_2 + y_2^*(\mathbf{u}), u_1, y_1^*(\mathbf{u})) - \hat{f}_2(y_2^*(\mathbf{u})) - \hat{f}_0(\mathbf{u})}_{\leq v(\{1,2\})} - \underbrace{\hat{f}_0(\mathbf{a} \wedge \mathbf{b})}_{\geq 0}, \end{aligned}$$

which in turn establishes that $v(\{1\}) + v(\{2\}) \leq v(\{1,2\})$. The conclusion that $v_0^* = 0 < v_1^* + v_2^* = v(\{1,2\})$ follows directly from Lemma A.3.

2) To check that $v_i^* \geq \underline{v}_i$, recall that $\underline{v}_i = E_\theta[\tilde{g}_j(\mathbf{x}_j^*, \theta)]$, where $\mathbf{x}_j^* \in \arg \max_{\mathbf{x}} E_\theta[\tilde{g}_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$ describes the lab's actions when firm j has exclusive access to it (for $i, j = 1, 2, j \neq i$). Moreover, by assumption firm i 's exclusive control of the lab dominates the standalone value, that is $v(\{i\}) \geq \underline{v}_i$. Then from the superadditivity of $v(\cdot)$, together with $v_1^* + v_2^* = v(\{1,2\})$ as established above, we have directly

$$\underline{v}_1 + \underline{v}_2 \leq v(\{1\}) + v(\{2\}) \leq v(\{1,2\}) = v_1^* + v_2^*,$$

and the equilibrium set $\{(v_1^*, v_2^*) \mid v_1^* + v_2^* = \Lambda, v_1^* \geq \underline{v}_1, v_2^* \geq \underline{v}_2\}$ is nonempty. ■

Proof of Proposition 3. We first use Lemmas A.1 and A.4 to prove the strict subadditivity of $v(\cdot)$, before establishing that the equilibrium payoffs (v_1^*, v_2^*) are (weakly) higher than the respective standalone values $(\underline{v}_1, \underline{v}_2)$.

1) Pick any $\mathbf{x}^* = (x_1^*, x_2^*)$ in $X_{\{1,2\}}^*$, the set of R&D levels that maximize the expected industry profit.

It is assumed in this proposition that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \leq 0$ (non-increasing returns to R&D), and from (17) that that $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j} \leq 0$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j} \leq 0$ (weakly negative R&D externalities). It follows from Lemma A.1 that the net profit expression $\hat{g}_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x})) - \hat{f}_i(y_i^*(\mathbf{x}))$ is non-increasing in (x_1, x_2) so that, for all $x_1^*, x_2^* \geq 0$,

$$\hat{g}_1(x_1^* + y_1^*(\mathbf{x}^*), x_2^*, y_2^*(\mathbf{x}^*)) - \hat{f}_1(y_1^*(\mathbf{x}^*)) \leq \hat{g}_1(x_1^* + y_1^*(x_1^*, 0), 0, y_2^*(x_1^*, 0)) - \hat{f}_1(y_1^*(x_1^*, 0)), \quad (57a)$$

$$\hat{g}_2(x_2^* + y_2^*(\mathbf{x}^*), x_1^*, y_1^*(\mathbf{x}^*)) - \hat{f}_2(y_2^*(\mathbf{x}^*)) \leq \hat{g}_2(x_2^* + y_2^*(0, x_2^*), 0, y_1^*(0, x_2^*)) - \hat{f}_2(y_2^*(0, x_2^*)). \quad (57b)$$

The negative cross-derivative in (16) implies the strict supermodularity of \hat{f}_0 (Topkis, 1995), with

$\hat{f}_0(0,0) = 0$. This property, together with (57a) and (57b), lead to

$$\begin{aligned}
& \underbrace{\hat{g}_1(x_1^* + y_1^*(\mathbf{x}^*), x_2^*, y_2^*(\mathbf{x}^*)) - \hat{f}_1(y_1^*(\mathbf{x}^*)) + \hat{g}_2(x_2^* + y_2^*(\mathbf{x}^*), x_1^*, y_1^*(\mathbf{x}^*)) - \hat{f}_2(y_2^*(\mathbf{x}^*)) - \hat{f}_0(x_1^*, x_2^*)}_{=v(\{1,2\})} \\
& < \underbrace{\hat{g}_1(x_1^* + y_1^*(x_1^*, 0), 0, y_2^*(x_1^*, 0)) - \hat{f}_1(y_1^*(x_1^*, 0)) - \hat{f}_0(x_1^*, 0)}_{\leq v(\{1\})} \\
& \quad + \underbrace{\hat{g}_2(x_2^* + y_2^*(0, x_2^*), 0, y_1^*(0, x_2^*)) - \hat{f}_2(y_2^*(0, x_2^*)) - \hat{f}_0(0, x_2^*)}_{\leq v(\{2\})},
\end{aligned}$$

which establishes that $v(\{1,2\}) < v(\{1\}) + v(\{2\})$. The conclusion that $v_0^* > 0$ and $v_i^* = \Lambda - v(\{j\})$, $i, j = 1, 2, j \neq i$, follows directly from Lemma A.4.

2) For any \mathbf{x}_1^* and \mathbf{x}_2^* , by definition of $v(\cdot)$ we have

$$\begin{aligned}
E_\theta [\tilde{g}_1(\mathbf{x}_1^*, \theta) + \tilde{g}_2(\mathbf{x}_1^*, \theta) - f_0(\mathbf{x}_1^*, \theta)] & \leq v(\{1,2\}), \\
E_\theta [\tilde{g}_1(\mathbf{x}_2^*, \theta) + \tilde{g}_2(\mathbf{x}_2^*, \theta) - f_0(\mathbf{x}_2^*, \theta)] & \leq v(\{1,2\}).
\end{aligned}$$

Then by reorganizing terms, and recalling that $v(\{i\}) = E_\theta [\tilde{g}_i(\mathbf{x}_i^*, \theta) - f_0(\mathbf{x}_i^*, \theta)]$ and $\underline{v}_i = E_\theta [\tilde{g}_i(\mathbf{x}_j^*, \theta)]$, where $\mathbf{x}_j^* \in \arg \max_{\mathbf{x}} E_\theta [\tilde{g}_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$, $i, j = 1, 2, j \neq i$, we obtain

$$\begin{aligned}
v(\{1\}) + \underline{v}_2 & \leq v(\{1,2\}), \\
v(\{2\}) + \underline{v}_1 & \leq v(\{1,2\}),
\end{aligned}$$

which, together with $v_i^* = \Lambda - v(\{j\})$, $i, j = 1, 2, j \neq i$, as established above, implies that $\underline{v}_i \leq v_i^*$. ■

A.5 Bilateral profit maximization.

We demonstrate that an element of

$$X(\tilde{t}_i, t_j) = \arg \max_{\mathbf{x}} \{E_\theta [\tilde{t}_i(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\},$$

the set of actions that maximize the expected payoff to the agent (the lab) given the principals' (firms') strategies (\tilde{t}_i, t_j) , is also an element of

$$X_{\{i\}}^* = \arg \max_{\mathbf{x}} \{E_\theta [\tilde{g}_i(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\},$$

the set of actions that maximize the joint payoff to the agent and principal i . That is:

Lemma A.5 *If $\tilde{\mathbf{x}}$ is an element of $X(\tilde{t}_i, t_j)$, then $\tilde{\mathbf{x}}$ is also an element of $X_{\{i\}}^*$.*

Proof. We suppose that $\tilde{\mathbf{x}} \notin X_{\{i\}}^*$, and look for a contradiction. In equilibrium, the strategy \tilde{t}_i is truthful relative to the equilibrium choice $\tilde{\mathbf{x}}$, that is $\tilde{t}_i(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)]\}$, for all $\theta \in \Theta$, implying that

$$\tilde{t}_i(\mathbf{x}, \theta) \geq \tilde{g}_i(\mathbf{x}, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)],$$

all $\theta \in \Theta$, all \mathbf{x} . This holds in particular for any given $\mathbf{x}^* \in X_{\{i\}}^*$, so that $\tilde{t}_i(\mathbf{x}^*, \theta) \geq \tilde{g}_i(\mathbf{x}^*, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)]$, all $\theta \in \Theta$. Adding $t_j(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)$ on each side of the inequality, leads to

$$v_0(\mathbf{x}^*, \theta) \geq \tilde{g}_i(\mathbf{x}^*, \theta) + t_j(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta) - \tilde{g}_i(\tilde{\mathbf{x}}, \theta) + \tilde{t}_i(\tilde{\mathbf{x}}, \theta).$$

By introducing $t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)$ on the right-hand side only, and reorganizing terms, we obtain

$$\begin{aligned} v_0(\mathbf{x}^*, \theta) &\geq [\tilde{g}_i(\mathbf{x}^*, \theta) + t_j(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] \\ &\quad - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] + \tilde{t}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta), \end{aligned}$$

all $\theta \in \Theta$. Obviously, if this holds for all $\theta \in \Theta$, this is also true in expectation, that is

$$\begin{aligned} E_\theta[v_0(\mathbf{x}^*, \theta)] &\geq E_\theta[\tilde{g}_i(\mathbf{x}^*, \theta) + t_j(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] \\ &\quad - E_\theta[\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] + E_\theta[v_0(\tilde{\mathbf{x}}, \theta)]. \end{aligned} \quad (58)$$

Observe that $\mathbf{x}^* \in X_{\{i\}}^*$ and $\tilde{\mathbf{x}} \notin X_{\{i\}}^*$ together imply that $E_\theta[\tilde{g}_i(\mathbf{x}^*, \theta) + t_j(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] > E_\theta[\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]$, which in turn implies from (58) that

$$E_\theta[v_0(\mathbf{x}^*, \theta)] > E_\theta[v_0(\tilde{\mathbf{x}}, \theta)].$$

The latter comparison says that $\tilde{\mathbf{x}} \notin X(\tilde{t}_i, t_j)$, a contradiction. Therefore, $\tilde{\mathbf{x}} \in X_{\{i\}}^*$. ■

A.6 Proof of Lemma 1.

Consider $\mathbf{x}^o \in X(t_i^o, t_j)$, a choice of the agent (the lab) when it faces principal (firm) i 's strategy (contract offer) $t_i^o(\mathbf{x}, \theta)$, the other strategy $t_j(\mathbf{x}, \theta)$ remaining unchanged. Formally,

$$\mathbf{x}^o \in \arg \max_{\mathbf{x} \in X} \{E_\theta[t_i^o(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\}.$$

We want to prove that \mathbf{x}^o cannot be distinguished from the action $\tilde{\mathbf{x}}$, as chosen by the agent when principal i 's strategy is $\tilde{t}_i(\mathbf{x}, \theta)$. That is, we want to establish that

$$\mathbf{x}^o \in \arg \max_{\mathbf{x} \in X} \{E_\theta[\tilde{t}_i(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\},$$

and that the strategy t_i^o results in the same expected payoff to the agent and both principals.

(i) We first prove that $\tilde{\mathbf{x}}$ leads to the same expected payoff to the agent when facing $t_i^o(\mathbf{x}, \theta)$ as when facing $\tilde{t}_i(\mathbf{x}, \theta)$ so that principal i 's change of strategy from \tilde{t}_i to t_i^o should not result in the agent turning down the new contract offer. Toward this aim, observe that $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) = \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)$, by definition, for all $\theta \in \Theta$. From inequality (21), we have

$$h(\theta) + \tilde{t}_i(\tilde{\mathbf{x}}, \theta) \geq \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \underline{g}_i(\theta) \geq 0,$$

so that

$$v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta) = \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - [\tilde{t}_i(\tilde{\mathbf{x}}, \theta) + h(\theta)] \leq \tilde{g}_i(\tilde{\mathbf{x}}, \theta),$$

for all $\theta \in \Theta$. As a result

$$t_i^o(\tilde{\mathbf{x}}, \theta) = \sup \{0, \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\} = \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)],$$

for all $\theta \in \Theta$, and hence

$$\begin{aligned} E_\theta [t_i^o(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] &= E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)] + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] \\ &= E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] \\ &= E_\theta [\tilde{t}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)], \end{aligned} \quad (59)$$

where the passage from the first to the second equality is justified by the zero expected value of a lump-sum transfer adjustment (equation (20)), and the passage from the second to the third directly follows from the definition of principal i 's equilibrium payoff: $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) = \tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)$.

(ii) We now prove that \mathbf{x}^o , as chosen by the agent when facing t_i^o , must be an element of

$$\arg \max_{\mathbf{x} \in X} \{E_\theta [\tilde{t}_i(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\}$$

so that, for principal i , it is indistinguishable from the action $\tilde{\mathbf{x}}$ chosen when the agent faces \tilde{t}_i . To see that, recall that by construction $t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\}$ is truthful with respect to $\tilde{\mathbf{x}}$ as associated to the equilibrium payoff $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta) \geq 0$. Then, as established by Lemma (A.5), truthful equilibria are (bilaterally) efficient so that it must be the case that

$$E_\theta [\tilde{g}_i(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] = E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]. \quad (60)$$

It follows that

$$\begin{aligned}
E_\theta [\tilde{t}_i(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] &\geq E_\theta [\tilde{g}_i(\mathbf{x}^o, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] \\
&= E_\theta [\tilde{g}_i(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] - E_\theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)] \\
&= E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] - E_\theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)] \\
&= E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] \\
&= E_\theta [\tilde{t}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)],
\end{aligned}$$

where the inequality follows from the definition of the truthful strategy \tilde{t}_i , the first equality follows from the linearity of the expectation operator, the second equality follows from equation (60), the third equality uses again the linearity of the expectation operator, and finally the bottom line follows from the definition of principal i 's equilibrium payoff $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)$. Thus, the agent's expected profit, when offered \tilde{t}_i by principal i and choosing \mathbf{x}^o , is at least as high as the one earned by choosing $\tilde{\mathbf{x}}$. Because the latter action maximizes the agent's payoff when offered \tilde{t}_i by principal i , the inequality cannot be strict. Therefore,

$$E_\theta [\tilde{t}_i(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] = E_\theta [\tilde{t}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]. \quad (61)$$

(iii) We now prove that, by offering t_i^o rather than \tilde{t}_i , principal i is not conceding more profit to the agent. Indeed, by definition, and using the linearity of the expectation operator again, we have

$$\begin{aligned}
E_\theta [t_i^o(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] &\geq E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)] + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] \\
&= E_\theta [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] - E_\theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)] \\
&= E_\theta [\tilde{g}_i(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] - E_\theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)] \\
&= E_\theta [\tilde{g}_i(\mathbf{x}^o, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)] + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)],
\end{aligned}$$

where the inequality follows from the definition of the truthful strategy t_i^o , and the second equality follows from equation (60). We also know that $\tilde{g}_i(\mathbf{x}^o, \theta) \geq \underline{g}_i(\theta)$ by definition (lower bound), and that $\underline{g}_i(\theta) \geq v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)$ from the first inequality in (21), so

$$\tilde{g}_i(\mathbf{x}^o, \theta) \geq \underline{g}_i(\theta) \geq v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta), \quad (62)$$

and hence

$$\begin{aligned}
t_i^o(\mathbf{x}^o, \theta) &= \sup \{0, \tilde{g}_i(\mathbf{x}^o, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\} \\
&= \tilde{g}_i(\mathbf{x}^o, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)],
\end{aligned}$$

for all $\theta \in \Theta$, and we have

$$\begin{aligned} E_\theta [t_i^o(\tilde{\mathbf{x}}, \theta) + t_j(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] &\geq E_\theta [t_i^o(\mathbf{x}^o, \theta) + t_j(\mathbf{x}^o, \theta) - f_0(\mathbf{x}^o, \theta)] \\ &= \max_{\mathbf{x} \in X} E_\theta [t_i^o(\mathbf{x}, \theta) + t_j(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)], \end{aligned}$$

which, by definition of a maximum, cannot be strict. Thus, there is no other efficient choice \mathbf{x}^o that results in a higher payoff than $\tilde{\mathbf{x}}$ when the agent is offered t_i^o by principal i .

As we have already shown that the choice of $\tilde{\mathbf{x}}$ implies the same payoff to the agent whether offered t_i^o or \tilde{t}_i (see equation (59)), the agent cannot improve on its expected payoff when facing the first strategy rather than the second.

(iv) From Lemma (A.5), because both strategies are truthful their associated choices are efficient, that is the expected joint profit of principal i and the agent is a maximum and hence unchanged whether the agent is offered $t_i^o(\mathbf{x}, \theta)$ or $\tilde{t}_i(\mathbf{x}, \theta)$. Since we have just shown that the expected payoff of the agent is also unchanged, the one of principal i must also be unchanged.

Eventually, from the previous steps we obtain that, when offering the strategy t_i^o rather than \tilde{t}_i , principal i still induces the agent to make efficient choices, and the expected payoffs to the agent and both principals end up unchanged. However, from equation (62) we obtain that principal i 's realized (*ex-post*) payoff is now given by $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)$, whereas the one of the agent is now equal to $v_0(\tilde{\mathbf{x}}, \theta) + h(\theta)$. ■

A.7 Proof of Proposition 4.

There are two possible cases to consider, depending on the occurrence of favorable (A.7.1) or, possibly, unfavorable circumstances (A.7.2) relative to the realization of θ .

A.7.1 Suppose that $\underline{g}_i(\theta) \geq v_i^*$ for almost all $\theta \in \Theta$.

We define the function $h : \Theta \rightarrow \mathbb{R}$ by

$$h(\theta) = v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - v_i^*, \quad (63)$$

that is the exact difference between firm i 's *realized* equilibrium payoff with payment $\tilde{t}_i(\tilde{\mathbf{x}}, \theta)$ to the lab, for any θ , and its *expected* equilibrium payoff $v_i^* (= E_\theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)])$.

By construction $E_\theta [h(\theta)] = 0$, and from $0 \leq v_i^* \leq \underline{g}_i(\theta)$, we have

$$v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta) \leq h(\theta) \leq v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta),$$

for almost all $\theta \in \Theta$. Then we know from Lemma 1 that the truthful strategy

$$t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\}$$

is a best-response strategy to \tilde{t}_j , for the same equilibrium outcomes $(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}})$ and a realized equilibrium payoff equal to $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)$. Given the specification of $h(\theta)$ in (63), the modified truthful strategy $t_i^o(\mathbf{x}, \theta)$ is actually given by

$$t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - v_i^*\},$$

so that firm i 's realized equilibrium payoff is $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta) = v_i^*$, which is independent of θ .

A.7.2 Suppose that $\underline{g}_i(\theta) < v_i^*$ for a subset of Θ with strictly positive measure (with $\underline{g}_i(\theta)$ non-negative for almost all θ).

For a given constant $\bar{v}_i \geq v_i^*$, define

$$\underline{\Theta}(\bar{v}_i) \doteq \{\theta \in \Theta \mid \underline{g}_i(\theta) \leq \bar{v}_i\},$$

the subset of Θ whose elements are such that the gross equilibrium profit $\underline{g}_i(\theta)$ is lower than \bar{v}_i .⁵³ By construction $\underline{\Theta}(\bar{v}_i)$ is of strictly positive measure,⁵⁴ and it induces a family of ordered sets for the inclusion relation. That is,

$$\bar{v} \leq \bar{v}' \Leftrightarrow \underline{\Theta}(\bar{v}) \subseteq \underline{\Theta}(\bar{v}'),$$

for any $(\bar{v}, \bar{v}') \geq (0, 0)$.

We now define the function $h : \Theta \rightarrow \mathbb{R}$ by

$$h(\theta) = \begin{cases} v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta) & \text{for all } \theta \in \underline{\Theta}(\bar{v}_i), \\ v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}_i & \text{otherwise.} \end{cases} \quad (64)$$

We must prove that conditions (20) and (21) in Lemma 1 are satisfied.

Condition (20) – To show that there exists a unique constant $\bar{v}_i \geq v_i^*$ such that $E_\theta[h(\theta)] = 0$, observe from (64) that $h(\theta)$ is (weakly) decreasing in \bar{v}_i , as established by shifting \bar{v}_i from \bar{v} to \bar{v}' , with $\bar{v} < \bar{v}'$:

⁵³More precisely, recall from Lemma 1, that $\underline{g}_i(\theta)$ is actually the lower bound of firm i 's gross payoff over all possible equilibrium choices. Unless there exists a multiplicity of optima, $\underline{g}_i(\theta)$ does not differ from the equilibrium gross payoff $\tilde{g}_i(\tilde{\mathbf{x}}, \theta)$. We assume that $\underline{g}_i(\theta) \geq 0$ for almost all θ (one does not expect adverse events to be so extreme as to more than cancel out the gross value of a firm's operations).

⁵⁴We know that $v_i^* \leq \bar{v}_i$ by assumption, implying that $\underline{g}_i(\theta) < \bar{v}_i$ for any θ such that $\underline{g}_i(\theta) < v_i^*$, which we suppose occurs with positive probability in this section.

- (1) if $\underline{g}_i(\theta) \leq \bar{v} < \bar{v}'$, that is $\theta \in \underline{\Theta}(\bar{v})$ and $\theta \in \underline{\Theta}(\bar{v}')$, then $h(\theta)$ remains equal to $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i$;
- (2) if $\bar{v} < \underline{g}_i(\theta) \leq \bar{v}'$, that is $\theta \notin \underline{\Theta}(\bar{v})$ and $\theta \in \underline{\Theta}(\bar{v}')$, then $h(\theta)$ decreases (strictly) from $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}$ to $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta)$;
- (3) if $\bar{v} < \bar{v}' < \underline{g}_i(\theta)$, that is $\theta \notin \underline{\Theta}(\bar{v})$ and $\theta \notin \underline{\Theta}(\bar{v}')$, then $h(\theta)$ decreases (strictly) from $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}$ to $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}'$.

Whenever the subset $\Theta \setminus \underline{\Theta}(\bar{v}_i)$ is of strictly positive measure, the latter case (3) occurs with a strictly positive probability, implying that $E_\theta[h(\theta)]$ is strictly monotone in \bar{v}_i .

(For an intuitive interpretation of the monotonicity of $h(\theta)$ in \bar{v}_i , recall that in equilibrium $t_i^o(\tilde{\mathbf{x}}, \theta) = \tilde{t}_i(\tilde{\mathbf{x}}, \theta) + h(\theta)$. As $\tilde{t}_i(\tilde{\mathbf{x}}, \theta)$ is independent of \bar{v}_i , we obtain that the adjusted payment $t_i^o(\tilde{\mathbf{x}}, \theta)$ is decreasing in $\bar{v}_i > v_i^*$. In other words, the higher \bar{v}_i , the lower the transfer to the lab, and the higher the payoff to the firm.)

By definition,

$$E_\theta[h(\theta)] = \int_{\underline{\Theta}(\bar{v}_i)} [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta)] d\mu(\theta) + \int_{\Theta \setminus \underline{\Theta}(\bar{v}_i)} [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}_i] d\mu(\theta),$$

where $\mu(\theta)$ is the probabilistic measure associated to the distribution of $\theta \in \Theta$. The latter expected value can be rewritten as

$$E_\theta[h(\theta)] = \int_{\underline{\Theta}(\bar{v}_i)} [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - v_i^* + v_i^* - \underline{g}_i(\theta)] d\mu(\theta) + \int_{\Theta \setminus \underline{\Theta}(\bar{v}_i)} [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - v_i^* + v_i^* - \bar{v}_i] d\mu(\theta).$$

Again by definition, $v_i^* = E_\theta[v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta)]$, implying that $\int_\Theta [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - v_i^*] d\mu(\theta) = 0$, so we obtain

$$E_\theta[h(\theta)] = \int_{\underline{\Theta}(\bar{v}_i)} [v_i^* - \underline{g}_i(\theta)] d\mu(\theta) - \int_{\Theta \setminus \underline{\Theta}(\bar{v}_i)} [\bar{v}_i - v_i^*] d\mu(\theta). \quad (65)$$

We now consider the sign of the latter expression for two particular values of \bar{v}_i chosen in $[v_i^*, \infty)$.

(i) Suppose first that $\bar{v}_i = v_i^*$ (lower bound). Then

$$E_\theta[h(\theta)] = \int_{\underline{\Theta}(v_i^*)} [v_i^* - \underline{g}_i(\theta)] d\mu(\theta) > 0, \quad (66)$$

where the strict positivity follows directly from the assumption that, in this section A.7.2, we have $\underline{g}_i(\theta) < v_i^*$ for a subset of Θ with positive measure.

(ii) Suppose now that $\bar{v}_i = \bar{\bar{v}}$ (upper bound), with

$$\bar{\bar{v}} = \inf_{v \in \mathbb{R}_+} \left\{ \underline{g}_i(\theta) \leq v, \text{ for almost all } \theta \in \Theta \right\}.$$

From the very definition of \bar{v} we have $\underline{g}_i(\theta) \leq \bar{v}$ for almost all $\theta \in \Theta$. Hence $\underline{\Theta}(\bar{v}) \equiv \Theta$, except possibly for a subset of Θ with zero measure. It follows from the definition of $h(\theta)$ in (64) that

$$h(\theta) = v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta),$$

for almost all $\theta \in \Theta$. Therefore,

$$\begin{aligned} E_\theta[h(\theta)] &= E_\theta[v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta)], \\ &= E_\theta[\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \underline{g}_i(\theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)] \\ &\leq -E_\theta[\tilde{t}_i(\tilde{\mathbf{x}}, \theta)] \end{aligned}$$

since, by definition, $\underline{g}_i(\theta) = \inf_{\mathbf{x} \in X^*} [\tilde{g}_i(\mathbf{x}, \theta)] \leq \tilde{g}_i(\tilde{\mathbf{x}}, \theta)$ for all $\theta \in \Theta$. Whenever expected transfers to the agent are strictly positive in equilibrium (a necessary condition for contract offers to provide incentives to the agent), we thus obtain

$$E_\theta[h(\theta)] \leq -E_\theta[\tilde{t}_i(\tilde{\mathbf{x}}, \theta)] < 0.^{55} \quad (67)$$

Finally, the strict monotonicity of $E_\theta[h(\theta)]$ over $[v_i^*, \bar{v}]$, together with $E_\theta[h(\theta)]$ being positive for $\bar{v}_i = v_i^*$ in (66) and negative for $\bar{v}_i = \bar{v}$ in (67), imply that there exists a unique value $\bar{v}_i \in (v_i^*, \bar{v})$ such that $E_\theta[h(\theta)] = 0$, and condition (20) in Lemma 1 is verified.

Condition (21) – We know from (64) that, by definition,

$$h(\theta) = \begin{cases} v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta) & \text{for all } \theta \in \underline{\Theta}(\bar{v}_i), \\ v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \bar{v}_i & \text{otherwise.} \end{cases}$$

Then from the non-negativity of $\underline{g}_i(\theta)$ and v_i^* , with $\bar{v}_i \geq v_i^*$, we establish directly that, for all $\theta \in \Theta$,

$$h(\theta) \leq v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta). \quad (68)$$

Moreover, from the definition of the subset $\underline{\Theta}(\bar{v}_i)$, we know that $\underline{g}_i(\theta) > \bar{v}_i$ if $\theta \notin \underline{\Theta}(\bar{v}_i)$. Then, again from the two-part expression of $h(\theta)$ in (64) we obtain that, for all $\theta \in \Theta$,

$$v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - \underline{g}_i(\theta) \leq h(\theta). \quad (69)$$

Therefore, from (68) and (69), the definition of $h(\theta)$ in (64) verifies condition (21) in Lemma 1.

⁵⁵We exclude from the analysis the case where $E_\theta[\tilde{t}_i(\tilde{\mathbf{x}}, \theta)] = 0$ for almost all $\theta \in \Theta$. It would refer to a situation where the lab chooses $\tilde{\mathbf{x}}$ without being incentivized to do so by firm i .

Firm i 's equilibrium outcome – From the definition of $h(\theta)$ in (64), the adjusted payment strategy

$$t_i^o(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)]\}$$

can be rewritten as

$$t_i^o(\mathbf{x}, \theta) = \begin{cases} \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - \underline{g}_i(\theta)\} & \text{for all } \theta \in \underline{\Theta}(\bar{v}_i), \\ \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - \bar{v}_i\} & \text{otherwise.} \end{cases}$$

For a chosen $\bar{v}_i \geq v_i^*$ such that conditions (20)-(21) are satisfied (and whose existence and uniqueness was demonstrated above), we know from Lemma 1 that the adjusted payment strategy is a truthful best reply to t_j that incentivizes the lab to choose an action which is identical to (or indistinguishable from) $\tilde{\mathbf{x}}$, for the same *expected* equilibrium outcomes. Then firm i 's *realized* payoff $v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta)$ is

$$v_i(\tilde{\mathbf{x}}, \tilde{\mathbf{y}}, \tilde{\mathbf{z}}, \theta) - h(\theta) = \begin{cases} \underline{g}_i(\theta) & \text{for all } \theta \in \underline{\Theta}(\bar{v}_i), \\ \bar{v}_i & \text{otherwise.} \end{cases}$$

This says that firm i 's (net) equilibrium payoff is equal to the gross equilibrium payoff $\underline{g}_i(\theta)$, with no transfer to the lab, if circumstances are so unfavorable that the realized θ is in $\underline{\Theta}(\bar{v}_i)$, whereas the net payoff is constant and equal to $\bar{v}_i \geq v_i^*$ otherwise.

Firm i 's choice of \bar{v}_i – The expression of the expected value of $h(\theta)$ in (65) and $E_\theta[h(\theta)] = 0$ (condition (20) in Lemma 1) together imply that

$$\int_{\Theta \setminus \underline{\Theta}(\bar{v}_i)} [\bar{v}_i - v_i^*] d\mu(\theta) = \int_{\underline{\Theta}(\bar{v}_i)} [v_i^* - \underline{g}_i(\theta)] d\mu(\theta), \quad (70)$$

which can be rewritten as

$$\bar{v}_i - v_i^* = \frac{\text{Prob}\{\theta \in \underline{\Theta}(\bar{v}_i)\}}{1 - \text{Prob}\{\theta \in \underline{\Theta}(\bar{v}_i)\}} E_{\theta \in \underline{\Theta}(\bar{v}_i)} [v_i^* - \underline{g}_i(\theta)].$$

An alternative characterization follows by adding $\int_{\underline{\Theta}(\bar{v}_i)} [\bar{v}_i - v_i^*] d\mu(\theta)$ on both sides in (70), to obtain

$$\begin{aligned} \bar{v}_i - v_i^* &= \int_{\underline{\Theta}(\bar{v}_i)} [\bar{v}_i - \underline{g}_i(\theta)] d\mu(\theta) \\ &= E_\theta [\sup \{0, \bar{v}_i - \underline{g}_i(\theta)\}]. \end{aligned}$$

In other words, in unfavorable circumstances where $\underline{g}_i(\theta) < v_i^*$ for a subset of Θ with strictly positive measure, the strictly positive *ex-post* margin $\bar{v}_i - v_i^*$ is chosen by firm i when $\theta \notin \underline{\Theta}(\bar{v}_i)$ so that, in expectation, shortfalls that occur when $\theta \in \underline{\Theta}(\bar{v}_i)$ are exactly recouped, and the expected equilibrium payoff remains equal to v_i^* . ■

A.8 Proof of Proposition 5.

First, Lemma A.1 extends to the case $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \geq 0$ ($i = 1, 2$). Indeed we have established in (48) that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} = 0 \Rightarrow \frac{dy_j^*}{dx_j} = 0$, and in (51) that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} > 0 \Rightarrow \frac{dy_j^*}{dx_j} > 0$. This is sufficient to conclude directly that $\frac{d[\hat{g}_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x})) - \hat{f}_i(y_i^*(\mathbf{x}))]}{dx_j}$ in (52) has the same sign as $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial x_j}$ and $\frac{\partial \hat{g}_i(x_i + y_i, x_j, y_j)}{\partial y_j}$.

To extend Lemma A.2 as well, note that $\frac{\partial^2 \hat{g}_i}{\partial x_i^2} \geq 0$ ($i = 1, 2$) implies $\frac{N_{ji}}{\Delta} \geq 0$ in (55), because $\Delta > 0$ (from stability condition) and $N_{ji} \geq 0$ from $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$ (second-order condition) and $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} \geq 0$ (assumption in this proposition). Then there are only two possible cases:

(i) If $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \geq 0$ then $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \geq 0$ also (model specifications). As $\frac{N_{ji}}{\Delta} \geq 0$, we obtain that the expression between brackets in (55) is positive. Moreover, $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$ (second-order condition) here implies that $-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right)^{-1} \geq 0$. Therefore, from (55) we have $\frac{dy_j^*}{dx_i} \geq 0$, which is sufficient to conclude directly that $\frac{d[\hat{g}_i(x_i + y_i^*(\mathbf{x}), x_j, y_j^*(\mathbf{x})) - \hat{f}_i(y_i^*(\mathbf{x}))]}{dx_i}$ in (54) is non-negative also.

(ii) If $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \leq 0$ then $\frac{\partial^2 \hat{g}_j}{\partial x_j \partial y_i} \leq 0$ also (model specifications). As $\frac{N_{ji}}{\Delta} \geq 0$, again the expression between brackets in (55) is positive. Moreover, $\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} < 0$ (second-order condition) implies here that $-\frac{\partial^2 \hat{g}_j}{\partial x_j \partial x_i} \left(\frac{\partial^2 \hat{g}_j}{\partial x_j^2} - \frac{\partial^2 \hat{f}_j}{\partial y_j^2} \right)^{-1} \leq 0$. Therefore, from (55) we have that $\frac{dy_j^*}{dx_i} \leq 0$, implying that $\left\| \frac{dy_j^*}{dx_i} \right\| = -\frac{dy_j^*}{dx_i}$. So, recalling that $\left\| \frac{\partial \hat{g}_i}{\partial x_j} \right\| \geq \left\| \frac{\partial \hat{g}_i}{\partial y_j} \right\|$ (model specifications in (6-7)), a sufficient condition for Lemma A.2 to be robust to the increasing R&D return specification is $\frac{dy_j^*}{dx_i} > -1$. ■

A.9 Proof of industry profit maximization result in Proposition 6.

Recall from the model specifications in Section 4 that, in equilibrium, for any given pair of transfer payment functions $(\tilde{t}_1, \tilde{t}_2)$ we know that $\tilde{\mathbf{x}}$ is an element of $X(\tilde{t}_1, \tilde{t}_2) = \arg \max_{\mathbf{x}} \{E_{\theta} [v_0(\mathbf{x}, \theta)]\}$, the set of external R&D choices that maximize the lab's profit. We want to demonstrate that $\tilde{\mathbf{x}}$ is also an element of $X_{\{1,2\}}^* = \arg \max_{\mathbf{x}} \{E_{\theta} [\tilde{g}_1(\mathbf{x}, \theta) + \tilde{g}_2(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]\}$, the set of external R&D levels that maximize industry profit. The proof is a simple adaptation, in the notation of our model, of a common agency efficiency result in Bernheim and Whinston (1986b, Theorem 2, p. 14).

We suppose that $\tilde{\mathbf{x}} \notin X_{\{1,2\}}^*$, and look for a contradiction. In equilibrium, the strategy \tilde{t}_i is truthful relative to the equilibrium choice $\tilde{\mathbf{x}}$ for all $\theta \in \Theta$, that is $\tilde{t}_i(\mathbf{x}, \theta) = \sup \{0, \tilde{g}_i(\mathbf{x}, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)]\}$, all $\theta \in \Theta$, all \mathbf{x} , implying that

$$\tilde{g}_i(\mathbf{x}, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)] \leq \tilde{t}_i(\mathbf{x}, \theta).$$

This holds in particular for any given $\mathbf{x}^* \in X_{\{1,2\}}^*$, so that $\tilde{g}_i(\mathbf{x}^*, \theta) - [\tilde{g}_i(\tilde{\mathbf{x}}, \theta) - \tilde{t}_i(\tilde{\mathbf{x}}, \theta)] \leq \tilde{t}_i(\mathbf{x}^*, \theta)$, all $\theta \in \Theta, i = 1, 2$. Summing the latter inequality for the two firms, and subtracting $f_0(\mathbf{x}^*, \theta)$ on each side, leads to

$$\tilde{g}(\mathbf{x}^*, \theta) - \tilde{g}(\tilde{\mathbf{x}}, \theta) + \tilde{t}(\tilde{\mathbf{x}}, \theta) - f_0(\mathbf{x}^*, \theta) \leq \tilde{t}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta),$$

all $\theta \in \Theta$, where $\tilde{g}(\mathbf{x}, \theta) = \tilde{g}_1(\mathbf{x}, \theta) + \tilde{g}_2(\mathbf{x}, \theta)$, and $\tilde{t}(\mathbf{x}, \theta) = \tilde{t}_1(\mathbf{x}, \theta) + \tilde{t}_2(\mathbf{x}, \theta)$. By introducing $f_0(\tilde{\mathbf{x}}, \theta)$ on the left-hand side only, and reorganizing terms, we obtain

$$[\tilde{g}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] - [\tilde{g}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] + \tilde{t}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta) \leq \tilde{t}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta),$$

all $\theta \in \Theta$. Obviously, if this inequality holds for all $\theta \in \Theta$, it holds also in expectation, that is

$$E_\theta [\tilde{g}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] - E_\theta [\tilde{g}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] + E_\theta [\tilde{t}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] \leq E_\theta [\tilde{t}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)]. \quad (71)$$

Observe that $\mathbf{x}^* \in X_{\{1,2\}}^*$ and $\tilde{\mathbf{x}} \notin X_{\{1,2\}}^*$ together imply that $E_\theta [\tilde{g}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] > E_\theta [\tilde{g}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)]$, which in turn implies from (71) that

$$E_\theta [v_0(\tilde{\mathbf{x}}, \theta)] = E_\theta [\tilde{t}(\tilde{\mathbf{x}}, \theta) - f_0(\tilde{\mathbf{x}}, \theta)] < E_\theta [\tilde{t}(\mathbf{x}^*, \theta) - f_0(\mathbf{x}^*, \theta)] = E_\theta [v_0(\mathbf{x}^*, \theta)].$$

The latter comparison says that $\tilde{\mathbf{x}} \notin X(\tilde{t}_1, \tilde{t}_2)$, a contradiction. Therefore, $\tilde{\mathbf{x}} \in X_{\{1,2\}}^*$. ■

A.10 Proof of $v_0^{\{0,1\}} = v_0^{\{0,2\}} \geq v_0^* = |\epsilon|$ in Proposition 8 (for $\epsilon < 0$).

Suppose that $\epsilon < 0$, and consider firm i 's two alternatives: if it acquires the lab, as an integrated entity it earns $\Lambda - v_j^{\{0,i\}}$; otherwise, as an outsider it earns $v_i^{\{0,j\}}$. The difference of the latter two payoffs is firm i 's willingness to pay for the lab, which is equal to the one of firm j . Therefore, competition for the acquisition of the lab implies that in equilibrium $v_0^{\{0,i\}} = v_0^{\{0,j\}} = \Lambda - v_1^{\{0,2\}} - v_2^{\{0,1\}}$.

Suppose now that firm i is the one that acquires the lab, while firm j remains independent, $i, j = 1, 2, j \neq i$. In the latter industry structure, the integrated entity $\{0, i\}$ and firm j bargain over the value generated by the acquired lab, with respective disagreement payoffs $v(\{i\})$ and \underline{v}_j . Firm j 's payoff is thus

$$v_j^{\{0,i\}} = \underline{v}_j + \omega_j \left(\Lambda - \underline{v}_j - v(\{i\}) \right), \quad (72)$$

where from (30) firm j 's bargaining power is

$$\omega_j = \frac{v_j^{\{1,2\}} - v_j^*}{\Lambda - v_1^* - v_2^*}. \quad (73)$$

Given that $v_0^{\{0,i\}} = \Lambda - v_1^{\{0,2\}} - v_2^{\{0,1\}}$, $i = 1, 2$, as established above, and using (72-73), we have

$$v_0^{\{0,i\}} = \Lambda - \left(\underline{v}_1 + \frac{v_1^{\{1,2\}} - v_1^*}{\Lambda - v_1^* - v_2^*} (\Lambda - \underline{v}_1 - v(\{2\})) \right) - \left(\underline{v}_2 + \frac{v_2^{\{1,2\}} - v_2^*}{\Lambda - v_1^* - v_2^*} (\Lambda - \underline{v}_2 - v(\{1\})) \right),$$

which, by reorganizing terms, can be rewritten as

$$v_0^{\{0,i\}} = \left(\frac{v(\{1\}) - \underline{v}_1}{\Lambda - v_1^* - v_2^*} \right) (v_2^{\{1,2\}} - v_2^*) + \left(\frac{v(\{2\}) - \underline{v}_2}{\Lambda - v_1^* - v_2^*} \right) (v_1^{\{1,2\}} - v_1^*).$$

Then, recalling that $v_0^* = |\epsilon| = v(\{1\}) + v(\{2\}) - \Lambda$, and that $\Lambda = v_1^{\{1,2\}} + v_2^{\{1,2\}}$, after a few steps we obtain that $v_0^{\{0,1\}} \geq v_0^*$ if and only if

$$\left(\frac{v(\{1\}) - v_1^{\{1,2\}}}{|\epsilon|} \right) [\underline{v}_1 + v(\{2\}) - \Lambda] + \left(\frac{v(\{2\}) - v_2^{\{1,2\}}}{|\epsilon|} \right) [\underline{v}_2 + v(\{1\}) - \Lambda] \leq 0. \quad (74)$$

As the two added terms in (74) are symmetric, we focus on the first one:

(i) Consider the expression between square brackets. By definition of $\Lambda = \max_{\mathbf{x}} E_{\theta}[\tilde{g}_1(\mathbf{x}, \theta) + \tilde{g}_2(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$, we have $\Lambda \geq E_{\theta}[\tilde{g}_1(\mathbf{x}_2^*, \theta) + \tilde{g}_2(\mathbf{x}_2^*, \theta) - f_0(\mathbf{x}_2^*, \theta)]$, where $\mathbf{x}_2^* \in \arg \max_{\mathbf{x}} E_{\theta}[\tilde{g}_2(\mathbf{x}, \theta) - f_0(\mathbf{x}, \theta)]$. Since $\underline{v}_1 = E_{\theta}[\tilde{g}_1(\mathbf{x}_2^*, \theta)]$ and $v(\{2\}) = E_{\theta}[\tilde{g}_2(\mathbf{x}_2^*, \theta) - f_0(\mathbf{x}_2^*, \theta)]$, we have $\underline{v}_1 + v(\{2\}) - \Lambda \leq 0$.

(ii) Consider the numerator in the term between parentheses. From Proposition 3 we know that $v_2^* = \Lambda - v(\{1\})$. Moreover, $\Lambda - v_1^* - v_2^* = v_0^* > 0$ implies from (29) that $v_2^{\{1,2\}} > v_2^*$ for all (ω_1, ω_2) in $(0, 1)^2$. It follows that $v_2^{\{1,2\}} > \Lambda - v(\{1\})$, and it is sufficient to recall that $v_2^{\{1,2\}} = \Lambda - v_1^{\{1,2\}}$ (the lab makes no profit in the horizontal arrangement) to establish that $v(\{1\}) - v_1^{\{1,2\}} > 0$.

Therefore, (74) is always true, with a strict inequality sign whenever $\Lambda > E_{\theta}[\tilde{g}_i(\mathbf{x}_i^*, \theta) + \tilde{g}_j(\mathbf{x}_i^*, \theta) - f_0(\mathbf{x}_i^*, \theta)]$, for some $i = 1, 2, j \neq i$, unlike in Examples 2 and 3 where firms' interests are so antagonistic as to have $\Lambda = v(\{1\}) + \underline{v}_2 = v(\{2\}) + \underline{v}_1$. ■