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Disentanglement of natural interest rate shocks and monetary policy shocks nexus

Gleb Kurovskiy*

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Abstract

This paper proposes a novel three-step identification procedure of monetary policy and natural interest rate shocks. Altogether, monetary policy and natural interest shocks explain about 90% of total inflation dynamics. The paper exploits (Arias et al., 2019) procedure, which allows getting canonical impulse response functions to monetary policy shocks. I find no evidence of price and output puzzles. The estimated natural interest rate declines from 2015 to 2019 years. Furthermore, Bank of Russia follows mandate and reacts to inflation in monetary policy feedback rule, while does not respond to output fluctuations.

Keywords: SVAR, monetary policy, natural interest rate, Russia

JEL Classification: E52, E58, C32

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Introduction and literature review

The impact of monetary policy on the real part of economy has been in the focus of researchers attention for almost five decades. The question renewed its importance when the world’s most influential central banks switched to inflation targeting regime. There are two competing strategies on how to achieve the inflation target. The first approach is to forecast inflation ahead, compare it with a desired target, and manipulate the monetary policy rate to keep inflation on target. The second approach is to estimate the natural interest rate and keep the policy rate at the natural level. This paper shows how these two approaches may coexist and explains how monetary policy shocks may be estimated simultaneously with the natural interest rate within one model.

The first approach means that central banks, for instance, would hike the policy rate to shrink inflation in two years and return it to the target if (i) they estimate the delay of the policy instrument effect on inflation and economic activity to be two years and (ii) they predict inflation going above the inflation target in two years. However, not all policy rate hikes lead to a decrease in inflation or economic activity but only those hikes that are unexpected to economic agents. In the present paper, I follow Christiano, L. J. et al., (1999) and define monetary policy shocks as unanticipated to economic agents changes (or unchanges) in the policy rate. One of the dominating methods of obtaining structural shocks is the identification of structural vector autoregression models (SVAR). For an extensive review of identification techniques, I refer to papers by Christiano, L. J. et al. (1999) and Ramey, V. A. (2016). The problem with such an approach is double uncertainty around the estimates of monetary policy shocks and predictions of macroeconomic variables.

The second approach means that central banks’ experts conduct their monetary policy via monetary stance (the difference between the policy rate and the natural interest rate). I define the natural interest rate in the same way as Laubach, T. and Williams, J. C. (2003), as a real interest rate when the output is equal to its natural level and inflation is equal to its target. Central bankers compare the natural interest rate with the policy rate. If the natural rate is higher than the policy rate, then the output is higher than its potential level or/and the inflation is higher than its target. Therefore, central banks should hike the policy rate to stabilize inflation and output to its potential and target levels. However, there are at least two problems related to this approach.

Firstly, the gap could never close due to nominal wage and price rigidities (Amato 2005). Secondly, a natural interest rate is an unobservable variable, and natural rate estimates are highly imprecise. It is a well-known fact that estimates of the natural rate of interest, commonly referred to as r*, are highly uncertain no matter which approach is used. For example, the Holston-Laubach-Williams estimate of the
US natural rate could currently be anywhere between -3% and +5% speech by Benot Cur 17 September 2018 at ECB. To evaluate monetary policy stance, central bank economists need to estimate natural interest rate and forecast factors which influence a natural interest rate future dynamics. The dominating part of a natural interest factors come from the real part of the economy.

In Ramsey model (Ramsey, 1928) of neoclassical growth, the natural interest rate depends on the intertemporal substitution, population growth and technological growth. The other factors could be the potential output, fiscal policy, demography (T. Laubach and J. C. Williams, 2003); (Holston, K., 2017); (Orphanides, A., and Williams, J. C., 2002). Therefore, to conduct monetary policy central bankers should predict the factors of a natural interest rate and determine how these factors influence a natural rate. Supply shocks, technological shocks, fiscal policy shocks, intertemporal preferences shocks are a number of shocks from the real side of the economy which could be summarized in natural rate shocks.

From the two approaches one may observe that there are two different economic reasons for a policy rate hikes, moreover, the magnitude of policy rate hikes could be dependent on the approach.

In practice, both monetary policy shocks and natural interest rate shocks affect the stance of monetary policy. Monetary policy shocks change policy rate. One could expect three possible monetary policy shocks: unexpected policy rate hike, cut or flat. At least two of three types of shocks result in change of policy rate. The effect of monetary shocks on natural interest rate is negligible because natural interest rate is an interest rate which balances savings and investments in the long-term. Monetary policy shocks have only short-term impact on real variables, while monetary policy is neutral in long-run (e.g. Walsh, 1998). Natural interest rate shocks affect natural rate. However, the natural interest rate shocks impact on policy rate is more complex. Only monetary authorities could change policy rate. To the first glance, there is no effect of natural rate on policy rate.

However, there is a two-way feedback between an economic state and monetary policy. Thus, monetary authorities could predict, for instance, a decline in natural interest rate. To keep the degree of stance, authorities will decrease a policy rate as well. Despite natural rate shocks are unobservable, central bankers will face rising or decreasing tightness of monetary stance after shifts of natural rate. Therefore, central bankers will react to natural interest shocks with a lag. Though natural interest rate shocks affect policy rate, they are orthogonal to monetary policy shocks. To sum up, both types of shocks determine the stance of monetary policy. There are several open question. How to identify separately monetary policy shocks and natural interest rate shocks? Which of two types of shocks are more important in explaining the inflation variance?

This paper is novel in the following aspects. First, Russia has already had data of at least five years period of inflation targeting. This period is sufficient to estimate transmission from monetary policy
shocks to inflation and output. The identification scheme follows the paper by (Arias et al., 2019). The identification accounts for the two-way feedback monetary rule and allows getting canonical impulse response functions. The results do not suffer from price or output puzzles. Second, Bank of Russia follows a mandate of stabilizing inflation but not output or unemployment (like the Fed). The paper checks whether Bank of Russia follows the mandate in reality. The results confirm that the Bank of Russia cares about inflation and does not account for output. Thirdly, the paper proposes a three-step procedure of estimating both monetary policy and natural interest rate shocks. The closest study for the first step of monetary policy shocks identification is (Arias et al., 2019). The closest work for the second step of natural interest rate shock identification is (Barsky, Sims, 2011).

The rest of the paper is the following. Section 2 discusses the identification of monetary and natural interest rate shocks. Section 3 provides the data. Section 4 discusses the results for Russian economy.

## II. Model

The idea to identify two types of shocks that drive the same variable goes back to Cholesky decomposition. Such decomposition allows to simultaneously identify several macroeconomic shocks. The problem with Cholesky identification is that it restricts the analysis to short-run, medium-run or long-run identification but not its pairwise combinations. In the case of monetary policy and natural interest shocks, I want to combine short-run and medium-run identification. The (Barsky, Sims, 2011) two-step procedure allows identifying shocks that drive total factor productivity. The first step is the identification of short-run total factor productivity individual shock. The second step involves medium-run identification. The paper by (Uhlig 2004) introduced medium-run analysis to identify labour productivity shocks. The idea behind the second step is that news shocks are the sources of total factor productivity fluctuations.

A natural interest rate should be also subject to medium-run or long-run shocks. A natural interest is a long-term equilibrium rate. Therefore, the dynamics of current variables should explain the natural interest rate only at long horizons. Such an idea is very close to the concept of news shock. Moreover, total factor productivity is one of the drives of the natural interest rate. Thus, news shock should also explain some variance of the natural interest rate. Long-run identification bases on the assumption that the data is infinite. Such restriction is bounding in the case of the Russian economy. The homogenous data is only available for five years under the inflation targeting regime. Therefore, the analysis is restricted to medium-run identification for up to five years. (Barsky, Sims, 2011) identify first step shock as a reduced-form innovation technology shock, which is not appropriate in my case. I perform a slight modification of (Barsky, Sims, 2011) procedure in application to policy rate.
The monetary policy shock is fully identified in the first step as in (Arias et al., 2019). In the second step, I perform counterfactual simulations to obtain all the series which are cleaned from the monetary policy shocks. Further, I perform (Uhlig, 2004) approach to get natural interest rate shocks. The latter shocks should explain the maximum forecast error variance of the policy rate at five years horizon. Two-step procedure allows getting monetary policy and natural interest rate shocks. Moreover, I follow (Benati, 2019) and calculate natural interest rate by simulating counterfactual series which are driven only by natural interest rate shocks. All the other shocks I assume to be equal to zero. Natural interest rate is also not affected by monetary policy shocks because they are cleaned at the second step. I summarize the model in the following steps in equations (1), (2). First step:

\[ Y_t = B_0 + B_1 Y_{t-1} + \ldots + B_k Y_{t-k} + A_0 \epsilon_t \]  

where \( Y_t \) is the vector of \( n \times 1 \) endogenous variables at period \( t \), \( B_k \) is the \( n \times n \) matrix of parameters given \( k \in [0, 1, k + 1, \ldots, p] \), \( p \) is a maximum lag order of VAR in canonical form. I calculate lag order as the maximum order by Hannan-Quinn and BIC criteria. \( A_0 \) is the \( n \times n \) matrix of structural shocks, \( \epsilon_t \) is the vector of \( n \times 1 \) structural shocks at period \( t \). I consider three monetary policy rules imposing sign and zero restrictions on both parameters and structural shocks matrices. The rules differ in endogenous reaction of central bank to changes in macroeconomic variables. The rules will allow determining whether the central bank follows mandate.

**Monetary policy rule I:**

A set of restrictions on endogenous monetary policy is the following. Central bank hikes policy rate in response to inflation increase. Such a rule essentially means that the central bank reacts to inflation disturbances in the current period. The central bank does not respond to changes in the exchange rate, output or unemployment. The one-period impulse response functions restrictions are the next: contractionary monetary policy shock results in the hike of interest rates and lowering of inflation. I also consider additional sign restrictions. Contractionary monetary policy shock decreases output and strengthens ruble. However, latter restrictions are excessive for the next monetary policy rules II and III. All the restrictions are symmetric, which means that the policy rate cuts have precisely the opposite effect.

**Monetary policy rule II:**

Bank of Russias mandate is to keep stable and low inflation. Thus, Bank of Russia considers a range of indicators which could potentially impact inflation in the forecast horizon. One of such indicators is
the exchange rate. In Russia, the exchange rate is a variable which reflects the dynamics of oil prices and policy uncertainty. Before the 2017 year, oil prices had an almost one-to-one correlation with the exchange rate USD/RUB.

Negative oil price shocks resulted in ruble weakening. The latter leads to inflation increase due to exchange rate pass-through effect. Thus, monitoring oil prices could allow central bank to timely react to future changes in inflation. Starting from 2014 year, some foreign countries introduced a range of sanctions on Russia. One of the effects of sanctions is the ruble weakening. Russia is a small open economy; exchange rate fluctuations have a significant effect on internal inflation. Bank of Russia could possibly react with policy rate hike in response to exchange rate weakening. By doing so Bank of Russia could smooth future exchange rate pass-through effect in inflation. A set of restrictions on endogenous monetary policy is the following. Central bank hikes policy rate in response to inflation increase, exchange rate weakening. Central bank does not respond to changes in output or unemployment. The one period impulse response functions restrictions are similar to monetary policy rule I.

**Monetary policy rule III:**

To check whether the central bank reacts to output fluctuations, I implement another monetary policy rule. A set of restrictions on endogenous monetary policy is the following. Central bank hikes policy rate
in response to inflation increase, output increase, exchange rate weakening. The central bank does not respond to changes in unemployment. The one-period impulse response functions restrictions are similar to monetary policy rule I. If impulse response functions of inflation to monetary policy shocks in rules II and III are identical, then adding output response in feedback rule is excessive. The one-period impulse response functions restrictions are similar to monetary policy rule I.

Second step, I re-run the series in a way to clean the data from monetary policy shocks. Define $\hat{Y}_t$ as counterfactual series which are subject to all the shocks except for the monetary policy shocks. Finally, the model is identified via (Uhlig, 2004) approach to explain a maximum forecast error variance of policy rate, cleaned from monetary policy shocks, at five year horizon.

$$\hat{Y}_t = C_0 + C_1 \hat{Y}_{t-1} + ... + C_k \hat{Y}_{t-k} + D_0 u_t$$ (2)

Where $C_k$ is the $n \times n$ matrix of parameters given $k \in [0, 1, k+1, ..., p]$, $p$ is a maximum lag order of VAR in canonical form identical to the first step. $D_0$ is the $n \times n$ matrix of structural shocks, $u_t$ is the vector of $n \times 1$ structural shocks at period $t$.

### III. Data

The dataset contains monthly Russian data on oil prices (Oil), interbank interest rate (MIACR) from 2 to 7 days, consumer price index (CPI), unemployment (U), exchange rate USD/RUB (ExR), two economic activity series: index of industrial production (IPI) and index of core industries output (IBI) from January 2014 to July 2019. The source of Brent oil prices is FINAM. The source of CPI, U, IPI, IBI is Federal State Statistic Service. The source of exchange rate and MIACR is Bank of Russia. I calculate monthly growth rates for oil prices, exchange rate, CPI, IPI, IBI and keep unemployment and MIACR at levels. The number of variables is identical to J.E. Arias et al. (2019) except for total reserves, nonborrowed reserves. I exclude the latter variables because Bank of Russia never targeted them during the period of analysis. Except for the exchange rate and MIACR, all the series are seasonally adjusted with X13-ARIMA-SEAT.

### IV. Results

This section provides results of monetary policy rule estimates, covers benefits and drawbacks of the chosen rule. Finally, the section discusses the natural interest rate shocks and the dynamics of natural interest rate itself.
Implicit monetary policy rule

To choose the implicit monetary policy rule, I rely on the analysis of impulse response functions and policy feedback rule. Standalone, it is not sufficient to compare either impulse response functions or policy feedback across different monetary policy rules. Policy feedback rule is defined by coefficients in the VAR model. Impulse response functions are additionally determined by the matrix of structural shocks. Both coefficients and structural matrix differ from monetary policy rule one to three. Going from monetary policy rule one to three, I impose additional information on central bank behaviour, being the third rule with the most number of restrictions. If augmentation of information keeps the reaction of inflation to monetary shocks and feedback rule the same, then such constrains are excessive. To assess the uncertainty around the estimates I perform the bootstrap procedure.

Matrix of structural of shocks is not fully identified in (J.E. Arias et al., 2019) procedure. Therefore, I choose a number of rotation matrices to characterize uncertainty around the identification. Further, I perform bootstrap procedure to describe uncertainty around the path of matrices of structural shocks estimates. I calculate all further confidence intervals for impulse response functions, policy feedback rules, forecast error variances decompositions, structural shocks and counterfactual simulations via bootstrap.

Note: The black line is median point estimate of the draws that satisfy monetary policy rule I. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.

Figure 2. Impulse response functions to unit monetary policy shock under monetary policy rule I

To estimate monetary policy rules, I include unemployment (U), interbank interest rate (MIACR) from
2 to 7 days, consumer price index (CPI), exchange rate USD/RUB (ExR), index of core industries output (IBI). I exclude oil prices from the analysis subject to several reasons. Firstly, oil prices mainly characterize the state of foreign markets. Exchange rate includes this information. Prior to 2017 year, the dynamics of oil prices and exchange rates was almost one-to-one. Secondly, the period of analysis is limited; I prefer to shrink the number of included variables to five to decrease uncertainty around coefficients estimates. In (fig. 2) I draw the response of macroeconomic variables to unit monetary policy shock under the first monetary policy rule.

The results show that unexpected interest rate hike leads to the decline of economic activity. CPI becomes lower, output declines, unemployment increases. There is no price or output puzzles. The ruble appreciates because interest rate hike makes the economy more attractive for foreign investors. They can get higher returns for a ruble of investments, thus foreign investors increase demand for ruble and its price. The results are significant for exchange rate, output and unemployment for one month.

![Graphs showing response of macroeconomic variables to unit monetary policy shock under monetary policy rule I](image)

Note: The black line is median point estimate of the draws that satisfy monetary policy rule I. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.

Figure 3. Impulse response functions to unit monetary policy shock under monetary policy rule II

In (fig. 3), I augment restrictions by imposing the reaction of a central bank to an exchange rate in policy feedback rule. The response of inflation has changed from parabolic to hump-shaped. The effect of shock has distributed more smoothly along the periods. Moreover, the period of inflation response has increased from four to seven months. Exchange rate response has also increased its significant reaction to
four months. Further, in (fig. 4) the restrictions are augmented by the endogenous response of a central bank to changes in output.

Note: The black line is median point estimate of the draws that satisfy monetary policy rule I. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.

Figure 4. Impulse response functions to unit monetary policy shock under monetary policy rule III

Responses of macroeconomic variables to identical monetary policy shocks are almost the same (at 90% level) under monetary policy rules II and III. Thus, I draw a conclusion that monetary policy rule II is sufficient to obtain canonical impulse responses\(^1\). I further investigate policy feedback under different monetary policy rules. Equation (1) implies the following feedback rule:

\[
MIACR_t = \beta_0 + \beta_y IPI_t + \beta_{\pi} CPI_t + \beta_{er} EXR_t + \beta_u U_t + \sum_{k=1}^{p} [L_k(\beta_y IPI_k + \beta_{\pi} CPI_k + \beta_{er} EXR_k + \beta_u U_k)] + \sum_{i=1}^{N} \alpha_i^0 \epsilon_{it}
\]  

(3)

Where \(\beta_j\) are feedback coefficients of our interest \(j = 1, \ldots, N + 1\), \(N\) is a number of variables, \(L^k\) is a lag operator of order \(k\), the maximum lag order is equal to one, \(\alpha^0 \epsilon_{it}\) is a multiple of the first raw structural shocks coefficients by structural shocks. I summarize the results in (tab. 1):

Table 1 implies that for the second and third monetary policy rules under or without sign restrictions

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\(^1\)The results for impulse response functions in case of the absence of sign restrictions on exchange rate and output are similar. Monetary policy rule II without these restrictions also produces canonical impulse responses. For the sake of space, I do not provide them. Nevertheless, I could provide them on request.
Table 1. Monetary policy feedback rule contemporary coefficients

<table>
<thead>
<tr>
<th>Models</th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
<th>Model 1 sign</th>
<th>Model 2 sign</th>
<th>Model 3 sign</th>
</tr>
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<tbody>
<tr>
<td>$\beta_\pi$</td>
<td>2.25</td>
<td>1.74</td>
<td>1.76</td>
<td>2.55</td>
<td>1.76</td>
<td>1.74</td>
</tr>
<tr>
<td></td>
<td>(1.57 3.22)</td>
<td>(0.70 3.27)</td>
<td>(0.56 4.49)</td>
<td>(1.87 3.54)</td>
<td>(0.76 3.20)</td>
<td>(0.55 4.47)</td>
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<tr>
<td>$\beta_{er}$</td>
<td>0</td>
<td>0.10</td>
<td>0.10</td>
<td>0</td>
<td>0.09</td>
<td>0.11</td>
</tr>
<tr>
<td></td>
<td>(0.03 0.21)</td>
<td>(0.03 0.23)</td>
<td>(0.03 0.20)</td>
<td>(0.03 0.20)</td>
<td>(0.03 0.30)</td>
<td>(0.03 0.30)</td>
</tr>
<tr>
<td>$\beta_y$</td>
<td>0</td>
<td>0</td>
<td>3.10</td>
<td>0</td>
<td>0</td>
<td>3.08</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>0</td>
<td>(0.71 9.53)</td>
<td>0</td>
<td>0</td>
<td>(0.78 9.12)</td>
</tr>
</tbody>
</table>

Note: The confidence intervals are 16% and 84% percentiles. All the other contemporary coefficients are equal to zero. MP stands for the abbreviation of monetary policy rule, the mark sign means that I additionally impose sign restrictions on exchange rate and output.

endogenous reaction of a central bank is identical. However, one can still observe differences for the first feedback rule. In general, the 1 percentage point of inflation increase should result in 1.75 percentage points hike of the interest rate. The 10% ruble weakening should result in 1 percentage points hike of the interest rate. Together with impulse response functions, feedback rules suggest that monetary policy rule II is sufficient, while the third rule does not help in estimation of IRFs and policy rules. All further results are presented for monetary policy rule II.

Monetary policy shocks themselves are of the interest in this paper. Shocks allow describing the episodes of monetary policy decisions from the expectation perspective. Bloomberg and Reuters regularly survey analytics before and after decisions of the Bank of Russia Board of Governors. Thus, central bankers can understand whether their changes of policy rates are in line with the projections of the analysts. Such surveys provide evidence on the efficacy of forward guidance policy. Nevertheless, analytics are only a small fraction of population and surveys could only partly reveal the expectation of population in general. I estimate monetary policy shocks for overall economy; hence, shocks better reflect whether the expectations of policy rate changes correspond to the actual hikes, cuts or flats. Fig. 5 describes various episodes of monetary policy shocks on the example of four statistically significant shocks.

Bank of Russia suspended exchange rate market operations on November 10. I correspond this date to the beginning of the floating exchange rate regime. In two months ruble exchange rate plummeted almost two times due to an oil price shock. Bank of Russia reacted to inflation shock and raised the policy rate up to 17%. Such an increase was an unexpected hike to economic agents. At that time, central bank just started the inflation targeting and the communication could not have been effective. The end of 2014-year shock is the highest shock with the point estimate to be 2.4, and the upper 68% boundary up
to 4.0 percentage points. March 2016 and summer 2017 are the episodes which shed light on the concept of monetary policy shocks. Though, in these periods the policy rate was flat indeed economy experienced shocks.

According to Bloomberg, 21 out of 39 analysts were expecting policy rate cut on June 2017. The Board of Governors decision to keep the policy rate flat was unexpected to analysts, and hence, the decision can be characterized as a shock. The peak shock in summer 2017 is 1.5 percentage points. Analysts found the economy recovery supported by the lowest monthly seasonally adjusted inflation on August 2017; they were waiting for the lessening of the monetary policy. According to Bloomberg data, all analysts out of 16 people were expecting policy rate flat at autumn 2018. Bank of Russia hiked policy rate to prevent future consequences of VAT pass-through on inflation. This episode is an example of unexpected hike. Overall, the standard deviation of monetary shocks has decreased from 1.08 during the 2014 and 2017 years to 0.38 afterwards. The volatility dynamics shrinkage could be attributed to the rising efficacy of forward guidance and budget rule.
Benefits and drawbacks of (J.E. Arias et al., 2019) method on the Russian example

The previous results suggest that there is an absence of output and price puzzles, the impact of monetary shocks on inflation and other variables is statistically significant. My results are different from those obtained for Russian economy earlier. The paper (Borzyh O. A., 2016) studies the transmission of monetary shocks to volume of credits. The author exploits recursive identification and obtains that the contractionary effect of monetary policy can be observed only on some subsamples. Another paper (Pestova, A. A. et al. 2019) supports (Borzyh, 2016) study that contractionary monetary policy does not lead to the inflation slowdown by applying factor analysis with sign restrictions. The other paper (Shestakov, D. E., 2017) finds evidence on the absence of cost channel in Russian economy. All these papers apply either recursive identification or sign restrictions on impulse response functions.

The problem with such identifications is that they allow a central bank to react in a policy irrelevant way. For instance, if there is an output slowdown, than central bankers can hike interest rate. (J.E. Arias et al., 2019) procedure restricts central bank to hike interest rates only in response to output accumulation. To provide evidence that such restrictions are meaningful, I have estimated the feedback rule under sign restrictions on impulse response function and without feedback rule restrictions (tab. 2). The absence of feedback rule restrictions results to a nonzero probability hike of policy rate in response to exchange rate strengthening or output declining.

Table 2. Unrestrictive monetary policy feedback rule

<table>
<thead>
<tr>
<th>Models</th>
<th>MP No</th>
<th>MP III</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta_\pi$</td>
<td>2.27</td>
<td>1.76</td>
</tr>
<tr>
<td></td>
<td>(0.76 6.60)</td>
<td>(0.56 4.49)</td>
</tr>
<tr>
<td>$\beta_{er}$</td>
<td>0</td>
<td>0.10</td>
</tr>
<tr>
<td></td>
<td>(-0.11 0.31)</td>
<td>(0.03 0.23)</td>
</tr>
<tr>
<td>$\beta_y$</td>
<td>-0.09</td>
<td>3.10</td>
</tr>
<tr>
<td></td>
<td>(-3.31 9.43)</td>
<td>(0.71 9.53)</td>
</tr>
</tbody>
</table>

Note: The confidence intervals are 16% and 84% percentiles. All the other contemporary coefficients are equal to zero. MP stands for the abbreviation of monetary policy rule, the mark no means that I impose sign restrictions on impulse response function and do not impose feedback rule restrictions.

To further investigate the appropriateness of identification applied in this paper, I estimate forecast error variance decompositions (fig. 6).
Note: The black line is median point estimate of the draws that satisfy monetary policy rule II. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.

Figure 6. Forecast error variance decompositions of monetary policy shock under monetary policy rule II

Monetary policy shocks explain 10% of interest rate dynamics and 20% of CPI growth. Though the shares of forecast error variance attributed to monetary policy shocks are significant, they are small. I cannot compare forecast error variance decompositions with (J.E. Arias et al., 2019) paper because they do not provide these results. The question is what does explain the rest of inflation and policy rate?

Natural interest rate results

Natural interest rate could shed light on small forecast error variance decompositions under monetary policy shocks. I identify natural interest rate shocks to the series cleaned from monetary policy shocks via (Uhlig, H.,2004) approach. From the rest of the shocks I choose the linear combination of those that best explain the cleaned policy rate at five-year horizon. Five-year period is sufficient to decimate the effect of temporary nominal shocks. Output is driven itself by demographic trends, total factor productivity shocks, total factor productivity shocks, budget policy shocks. Hence, these long-term factors could explain natural interest rate shocks. The (fig. 7) depicts the impact of unit natural interest rate shock on macroeconomic variables.

Nevertheless, one can reproduce the results of (J.E. Arias et al., 2019) and get that monetary policy shocks explain less than 20% of the Fed rate and less than 20% of the consumer price index.
Note: The black line is median point estimate of the draws that satisfy monetary policy rule II, which essentially means that all the series were cleaned from the monetary policy shocks under monetary policy rule II. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.

Figure 7. Impulse response functions to unit natural interest rate shock

The results of identification suggest that natural interest rate increase lead to CPI and output increase. Suppose that natural interest rate is lower than the policy rate. Hence, there is a contractionary effect of monetary policy on economy. The economy is hit by a positive natural interest shock. The difference between the natural interest rate and the policy rate shrinks, namely the natural interest rate goes up more than the policy rate. Thus, the contractionary effect of monetary policy declines. There is a stimulating effect of a positive natural interest rate shock on inflation and output. Natural interest rate shocks explain about 60% of consumer prices variation and around 30% of output (Appendix A). The variance of policy rate, inflation and output that not explained by monetary policy shocks is mostly explained by natural interest shocks. Monetary policy shocks and natural interest rate shocks altogether explain up to 90% of variation in inflation. These two types of shocks are sufficient to describe the stance of monetary policy.

I suppose that the only drivers of changes in natural interest rate are natural interest rate shocks. I perform counterfactual simulations (fig. 8) where I keep only natural interest rate shocks\(^1\). The (fig. 8) illustrates that natural interest rate (the upper-right graph) is declining from 13% in 2015 year to 6% in summer 2019 year. The natural interest rate dynamics are volatile but if I change the output proxy variable to the index of production function then natural rate becomes less volatile (Appendix B). Overall,

\(^1\)The nominal natural interest rate is equal to a real natural interest rate plus the inflation expectations at a long horizon, which are assumed to be constant and equal to the inflation target of 4%. 


Note: The black line is the median estimate of the series driven by only natural interest rate shocks. The light grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The grey lines are actual series.

Figure 8. Counterfactual simulations of the series driven by only natural interest rate shocks

for both proxy variables the summer 2019 year is under contractionary effect of monetary policy.
Conclusion

This paper proposes a procedure of identification of monetary policy and natural rate shocks, which are the dominating drivers of the monetary policy stance. To disentangle natural rate shocks from monetary policy shocks, I perform a three-stage procedure. Firstly, I estimate monetary policy shocks. Secondly, I clean out the series from the impact of monetary policy shocks and, finally, explain the rest of the policy rate variance by the natural interest shocks\(^1\).

To identify monetary policy shocks, I exploit (J.E. Arias et al., 2019) procedure, which allows getting canonical impulse response functions. Further, I interpret monetary policy shocks during the period of Bank of Russia inflation targeting. Overall, shocks resemble the expectations of professional analysts. The novel identification procedure of natural interest rate shocks allows to quantitatively estimate the impact on natural interest rate shocks on macroeconomic variables, to characterize the stance of monetary policy. The natural rate estimates support the global tendency of declining rates and together with monetary policy shocks explain 90\% of inflation variance.

Further investigation could include the analysis of factors that resulted in natural interest rate shocks. One could also develop a model on whether the monetary policy and natural interest shocks will be determined simultaneously. The limitation of the current approach is that there is double uncertainty coming from cleaning of monetary policy shocks and estimates of natural interest rate shocks. In the current paper, I neglect the first uncertainty and work with the median values of series cleaned out from monetary policy shocks.

\(^1\)One could answer the question whether is it possible to firstly identify natural interest rate shocks and secondly detect monetary policy shocks. In that case long-term natural interest shocks will be distorted by short-term monetary policy shocks. To provide some evidence on this, in Appendix C I estimate natural interest rate shocks without the first stage. The results are poor: the response of output is insignificant, the response of inflation lasts for only one month and the unemployment rises.
References


Appendix A: Forecast error variance decompositions of natural interest rate shock

Note: The black line is median point estimate of the draws that satisfy monetary policy rule II. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.
Appendix B: Counterfactual simulations of the series driven by only natural interest rate shocks (IPI is a proxy for output dynamics)

Note: The black line is the median estimate of the series driven by only natural interest rate shocks. The light grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The grey lines are actual series.
Appendix C: Impulse response functions to unit natural interest rate shock neglecting first step of identification monetary policy shocks

Note: The black line is median point estimate of the response to natural interest rate shocks. The grey lines are one-standard deviation confidence intervals: 16% and 84% percentiles. The period is equal to 1 month.